Hybrid Parallelised Framework for the solution of PDEs on HPC Clusters

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SCEE

AIM:

To develop a hybrid framework to utilize HPC resources to solve LINEAR EQUATIONS (and hence Partial Differential Equations) using background parallelisation tools (PETSc).

Solving LINEAR EQUATIONS

$$\begin{bmatrix} \cdot \cdot \cdot & & & & & \\ & -1 & 2 & -1 & & \\ & & -1 & 2 & -1 & \\ & & & & \cdot \cdot \end{bmatrix} \begin{bmatrix} \cdot & & \\ \phi^{i-1} & & \\ \phi^{i} & & \\ \phi^{i+1} & & \\ 0 & & \\ 0 & & \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

ITERATIVE METHODS

- Jacobi Method
- Gauss-Seidel Method
- Steepest Descent Method
- Conjugate Gradient Method
- Many more....

PROGRESS after MID TERM EVALUATION

- Finalising the problem statement.
- Running PETSC codes on cluster.
- Benchmarking GMRES method.
- Analysing Hybrid approach for Conjugate gradient method

CONTAINERIZATION

SINGULARITY

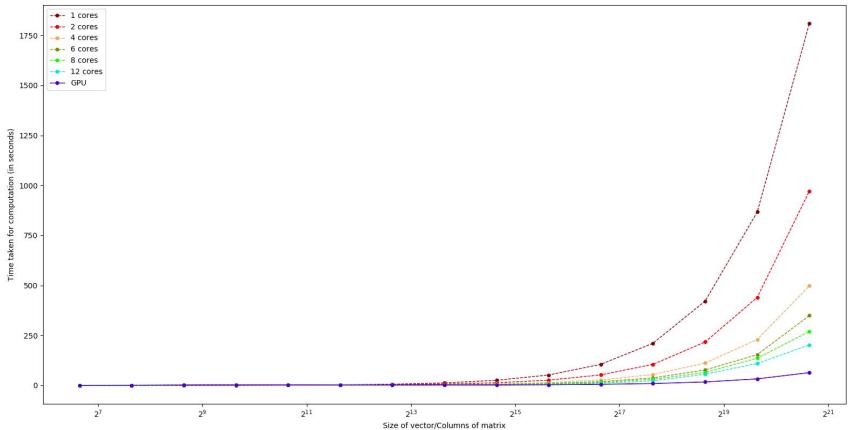
- To create custom runtime environment to run simulations on IIT Mandi HPC Cluster.
- Created Singularity images for both CPU and GPU implementations.
- Singularity also exposes the host's working directory inside the container unlike docker.

```
Bootstrap: docker
From: nvidia/cuda:9.0-devel
%files
    petsc-3.10.5.tar.gz
%post
   fileecho="## nvcc command
# - PATH includes /usr/local/cuda-9.0/bin
export PATH=/usr/local/cuda-9.0/bin: $PATH
# - LD_LIBRARY_PATH includes /usr/local/cuda-9.0/lib64
export LD LIBRARY PATH=/usr/local/cuda-9.0/lib64:$LD LIBRARY PATH
## Binding against the driver on the peregrine
# - LD LIBRARY_PATH includes /usr/lib64/nvidia
export LD_LIBRARY_PATH=/usr/lib64/nvidia:$LD_LIBRARY_PATH"
    mkdir -p /usr/lib64/nvidia
    echo $fileecho > /environment
    export PATH=/usr/local/cuda-9.0/bin:$PATH
    export LD_LIBRARY_PATH=/usr/local/cuda-9.0/lib64:$LD_LIBRARY_PATH
   export LD LIBRARY PATH=/usr/lib64/nvidia:$LD LIBRARY PATH
   nvcc --version
    sed -i 's|http://archive.ubuntu|http://jp.archive.ubuntu|g' /etc/apt/sources.list
    apt update -v
    apt -y install git wget python g++ gcc gfortran curl
    apt -y install mpich libblas-dev liblapack-dev
   apt -y install build-essential valgrind
   apt -y install python3
   curl https://bootstrap.pypa.io/get-pip.py -o get-pip.py || echo "curl failed"
   python3 get-pip.py || echo "script failed"
    rm get-pip.py || echo "removal failed"
    python3 -m pip install --upgrade pip || echo "pip upgrade failed"
   python3 -m pip install matplotlib || echo "matplotlib failed"
   # wget http://ftp.mcs.anl.gov/pub/petsc/release-snapshots/petsc-3.12.1.tar.gz
    mkdir /petsc dir/
    tar xvzf /petsc-3.10.5.tar.gz -C /petsc dir/
    rm -r /petsc-3.10.5.tar.qz
    petsc_dir=/petsc_dir/petsc-3.10.5/
    cd $petsc dir
    sed -i '1s/^/NVCCFLAGS += -Xcompiler -openmp\nNVCCFLAGS += -Xcompiler -fopenmp\n/'
makefile
    ./configure --with-cuda=1 --with-precision=single --with-clanguage=c --download-cusp
    make all test
    cp -r ./lib/petsc /lib
    cd /
```

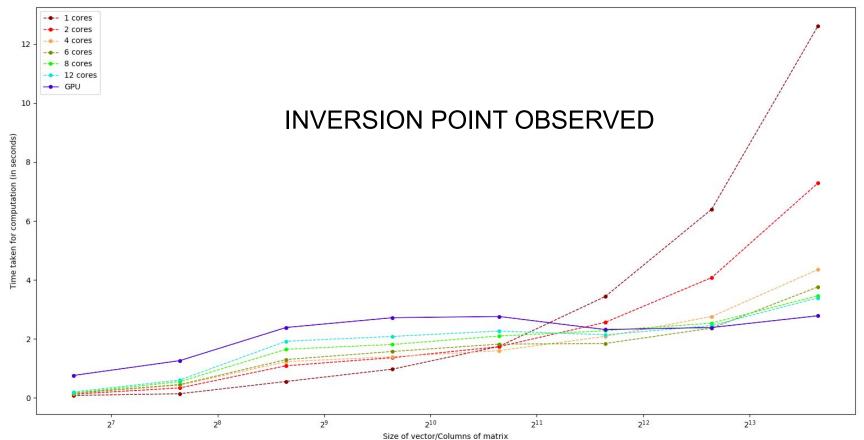
BENCHMARKING - I

- PETSC code
 - Solving Linear Equation for Tridiagonal Matrix
 - Using GMRES method and JACOBI preconditioner.
 - Multicore Simulation (#cores from 1 to 12)
 - GPU Simulation

OBSERVATIONS



OBSERVATIONS



CONJUGATE GRADIENT METHOD

- Our own implementation
 - Using PETSC data structures
 - Easy to choose between CPU or GPU implementation for same code
- Ran the code with 1 core CPU implementation and GPU
- Implemented a Hybrid version of the same

CONJUGATE GRADIENT METHOD

```
VecSetRandom(x, NULL);
MatMult(A, x, r);
VecAXPY(r,minusone,b);
//Initialize p=-r
VecSet(p, zero);
VecAXPY(p,minusone,r);
for (i=0;i<iters;++i){
   VecNorm( r , NORM_2 , &rdot);
   rdot = rdot*rdot;
   MatMult(A,p,Ap);
   VecDot(p, Ap, &pAp);
   alpha = rdot/pAp;
   VecAXPY(x, alpha, p);
   VecAXPY(r,alpha,Ap);
   VecNorm(r, NORM 2, &val);
   val = val*val;
   beta = val/rdot;
   VecAXPBY(p, minusone, beta, r);
```

Compute
$$r_0 = Ax_0 - b, p_0 = -r_0$$

For k = 0, 1, 2, ... until convergance

$$\alpha_k = \frac{r_k^T r_k}{p_k^T A p_k}$$

$$x_{k+1} = x_k + \alpha_k p_k$$

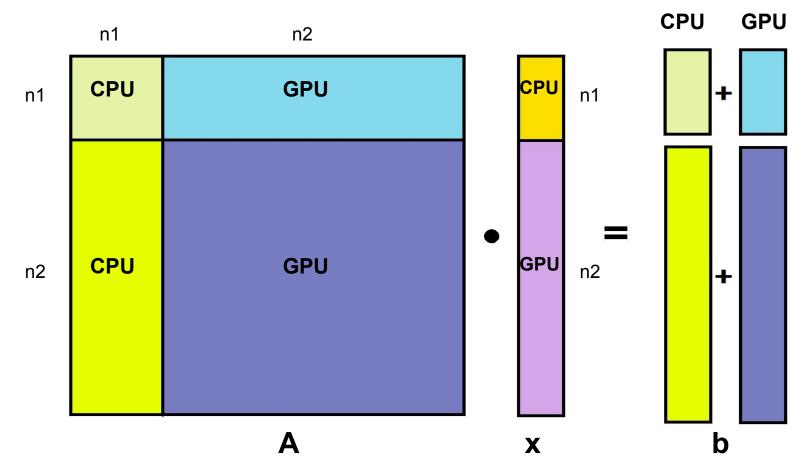
$$r_{k+1} = r_k + \alpha_k A p_k$$

$$\beta_k = \frac{r_{k+1}^T r_{k+1}}{r_k^T r_k}$$

$$p_{k+1} = -r_{k+1} + \beta_k p_k$$

End

HYBRID IMPLEMENTATION



HYBRID IMPLEMENTATION

- CPU routines for VEC1 (n1)

- GPU routines for VEC2 (n2)

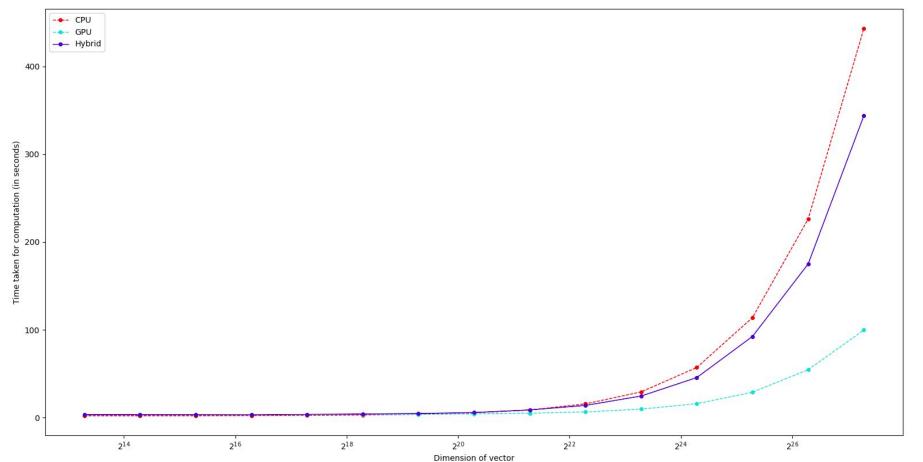
- Taking maximum time of two

HYBRID IMPLEMENTATION (Multi-Threaded)

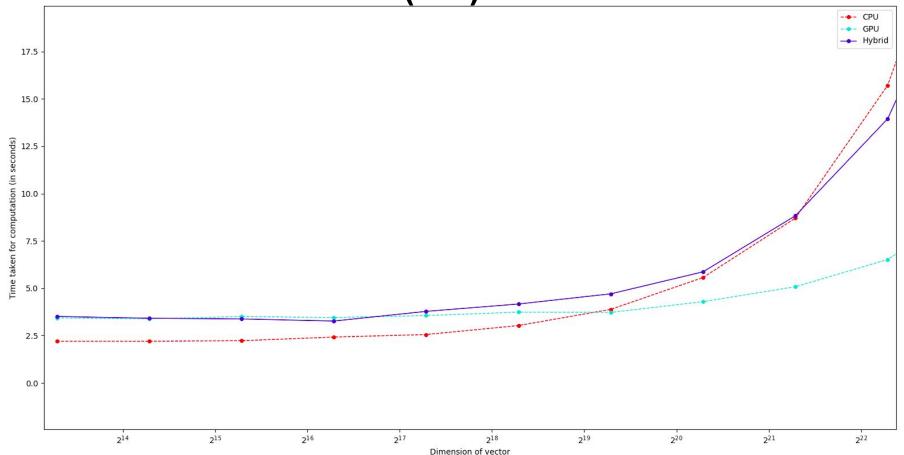
- Run CPU and GPU parts on different threads, thus almost simultaneously

```
typedef struct{
    Vec x;
    Vec v;
    PetscScalar *val;
}VecDot struct;
void* VecDot thread(void* ptr){
    VecDot struct *sptr = (VecDot struct*)ptr;
    VecDot(sptr->x, sptr->v, sptr->val);
    return NULL;
void VecDot_split(Vec x1, Vec x2, Vec y1, Vec y2, PetscReal *value){
    PetscReal a, b;
    pthread_t t1, t2;
    VecDot_struct s1 = \{x1, y1, &a\}, s2 = \{x2, y2, &b\};
    pthread_create(&t1, NULL, VecDot_thread, (void*)(&s1));
    pthread_create(&t2, NULL, VecDot_thread, (void*)(&s2));
    pthread_join(t1, NULL); pthread_join(t2, NULL);
    *value = (a+b);
    return;
```

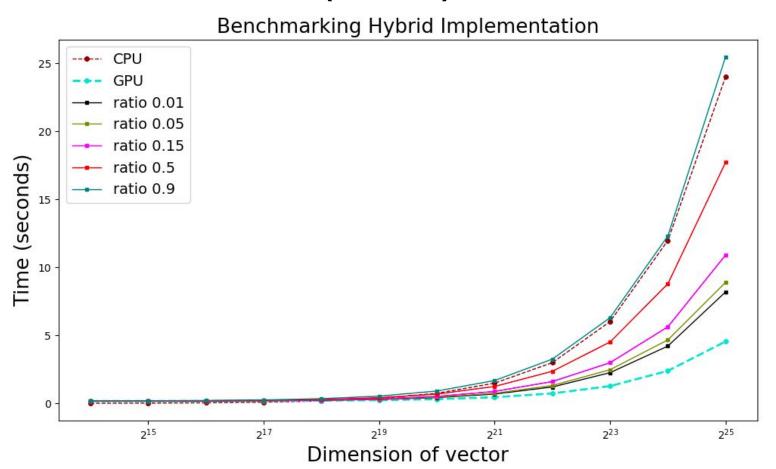
BENCHMARKING I - (n/2)



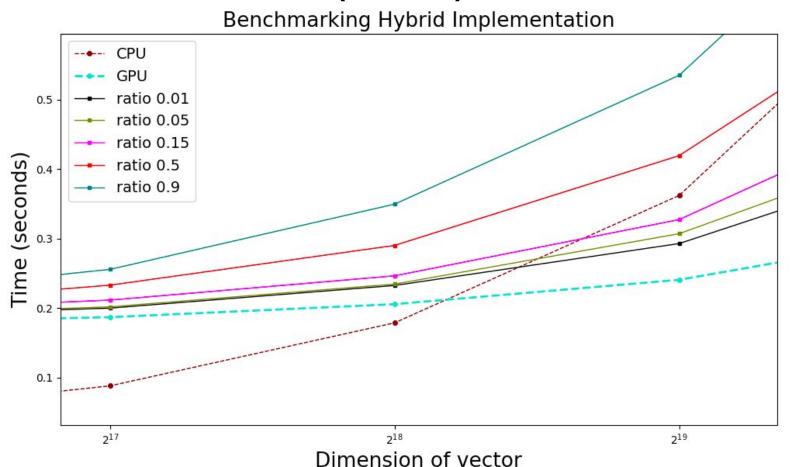
BENCHMARKING I - (n/2)



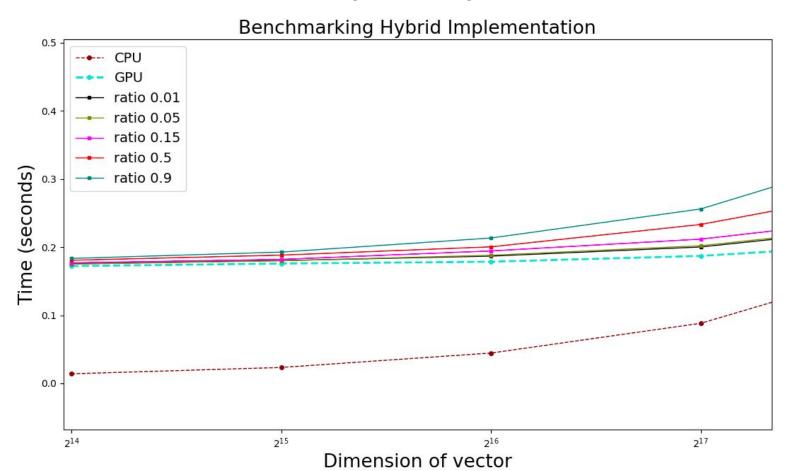
BENCHMARKING II - (n1, n2)



BENCHMARKING II - (n1, n2)



BENCHMARKING II - (n1, n2)



CONCLUSIONS

- PETSC is difficult to hybridise (lack of documentation)
- Multicore + GPU implementation leads to deadlock
 - Need to optimise
- Our Implementation
 - Time(GPU) < Time (Hybrid code) < Time (CPU Code)
- Our Aim is to achieve
 - Time(Hybrid code) < Time(GPU)
- IIT Mandi HPC Cluster incompatible with "Multinode + GPU" PETSC implementation.
 - Absence of InfiniBand connectivity

FUTURE SCOPE

- Improvise PETSC GPU implementation
 - Understanding PETSC structure in depth
 - New VECTOR and MATRIX type for hybridisation
- New Implementation of Linear Solvers
 - Hybrid implementation
 - CUDA / OpenMP / BLAS-LAPACK

VecType

String with the name of a PETSc vector

Synopsis

```
typedef const char* VecType;
#define VECSEQ
                        "seq"
#define VECMPI
                        "mpi"
#define VECSTANDARD
                        "standard"
                                     /* seg on one process and mg
#define VECSHARED
                        "shared"
#define VECSEQVIENNACL "segviennacl"
#define VECMPIVIENNACL
                       "mpiviennacl"
#define VECVIENNACL
                        "viennacl"
                                     /* segviennacl on one proces
#define VECSEQCUDA
                        "segcuda"
#define VECMPICUDA
                        "mpicuda"
#define VECCUDA
                        "cuda"
                                     /* sequuda on one process ar
#define VECNEST
                        "nest"
#define VECNODE
                        "node"
                                     /* use on-node shared memory
```

https://www.mcs.anl.gov/petsc/petsc-current/docs/manualpages/Vec/VecType.html

THANK YOU