

Synchronization via Semaphores

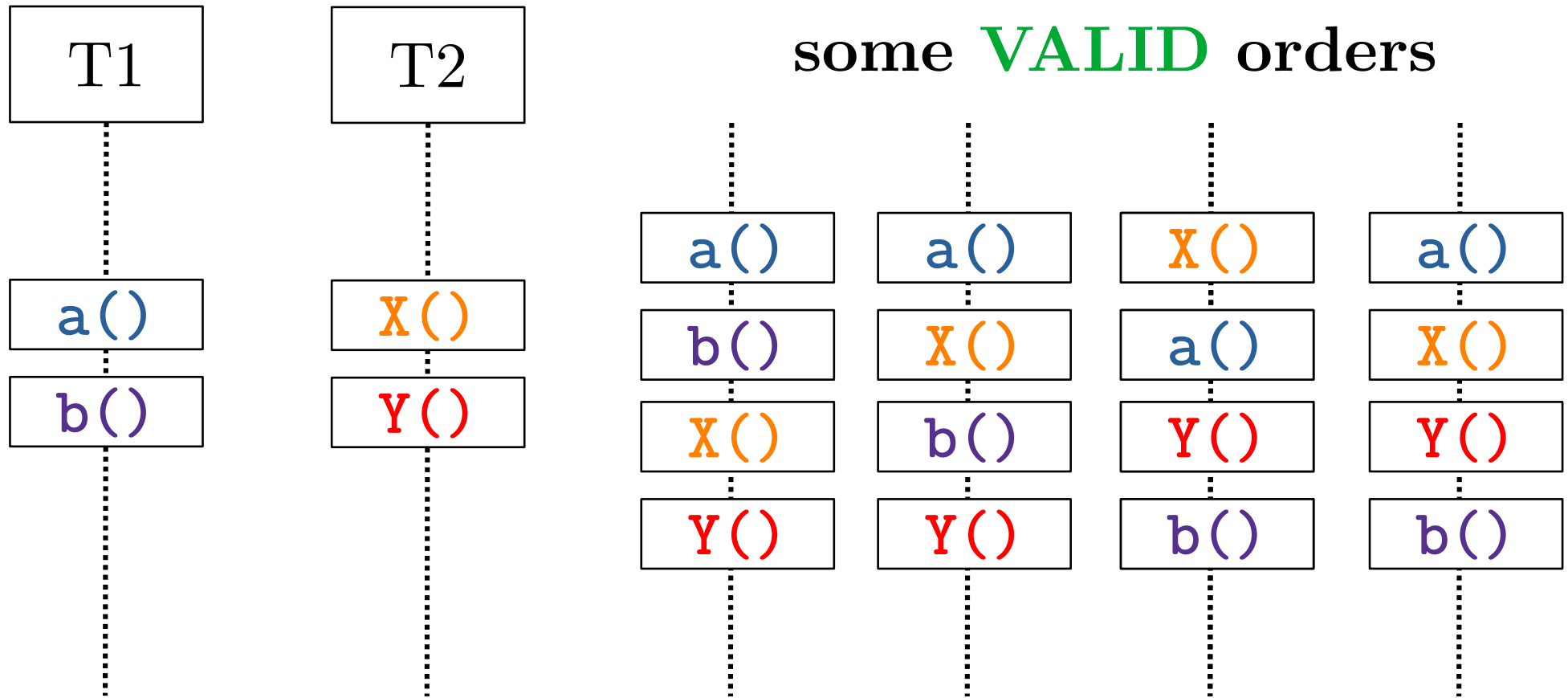
General Synchronization Task

- Operations or instructions of concurrent processes (or threads) can interleave.
- Depending on the situation, there are **orders** of operations/instructions that can be considered **VALID** and there are orders that can be considered **INVALID**.
- **Synchronization** is about implementing different mechanisms such that only the **VALID orders** of operation/instructions can occur regardless of how the threads/processes are scheduled by the operating system.

Synchronization Task/Problem 1a: **(Thread) Barrier**

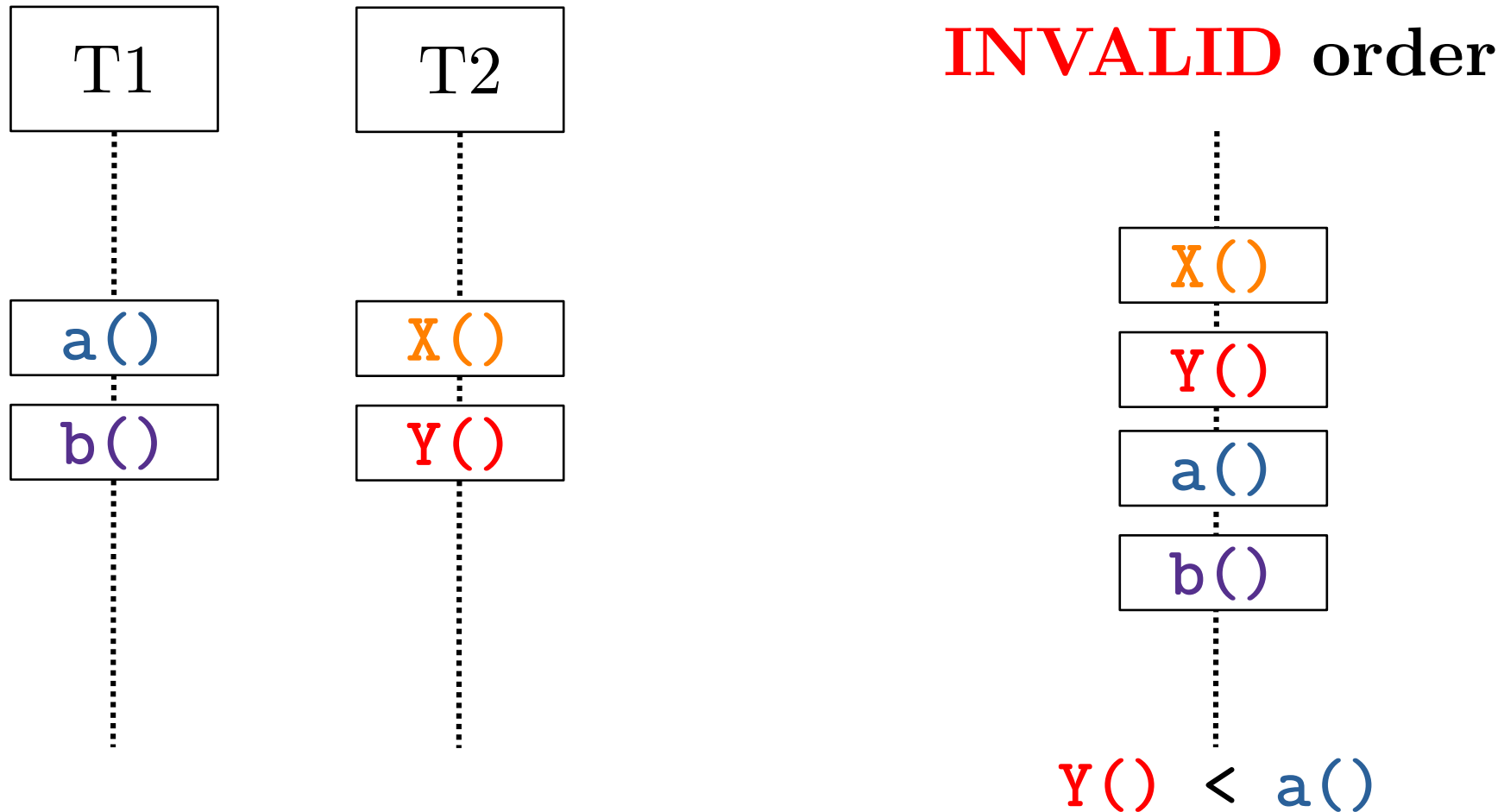
[Problem Description]

Task/Problem 1a: Barrier: $a() < y()$



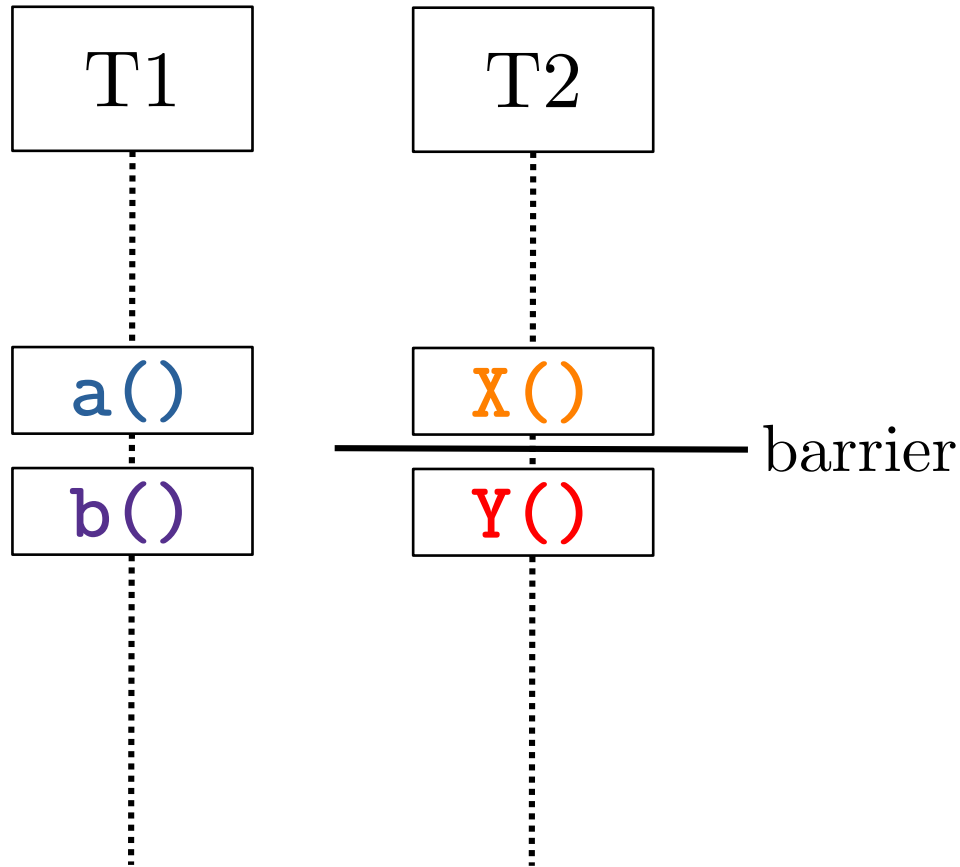
Constraint: We consider only those orders where $a()$ is performed before $y()$ as **VALID**.

Task/Problem 1a: Barrier: $a() < y()$



Constraint: We consider only those orders where $a()$ is performed before $y()$ as **VALID**.

Task/Problem 1a: Barrier: $a() < y()$



A *barrier* should be placed before the call $y()$ in T2.

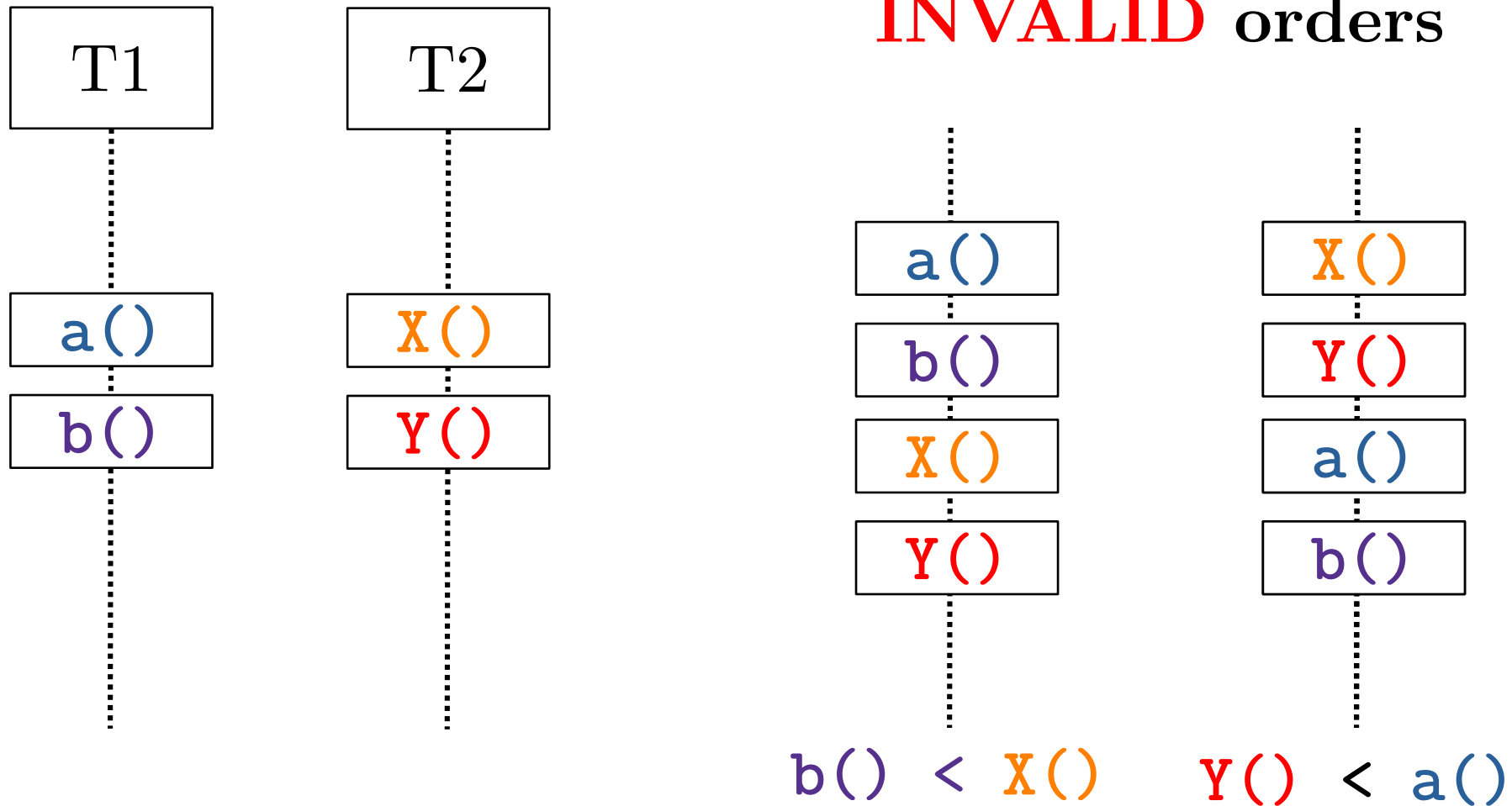
This barrier means T2 has to wait for T1 to complete the $a()$ call before performing $y()$.

Constraint: We consider only those orders where $a()$ is performed before $y()$ as **VALID**.

Synchronization Task/Problem 1b: **(Thread) Barriers**

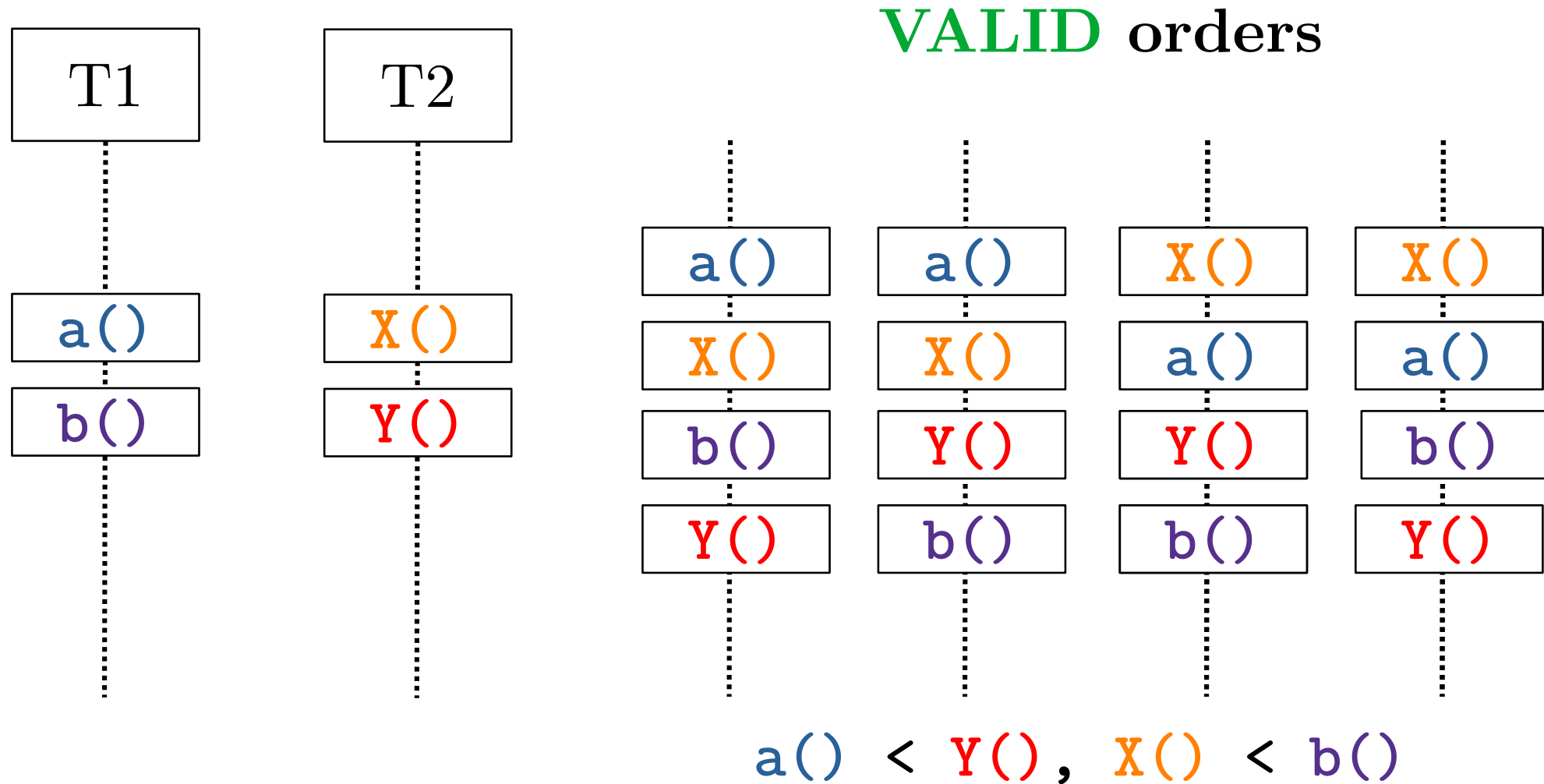
[Problem Description]

Task/Problem 1b: Barriers: $a() < y()$, $x() < b()$



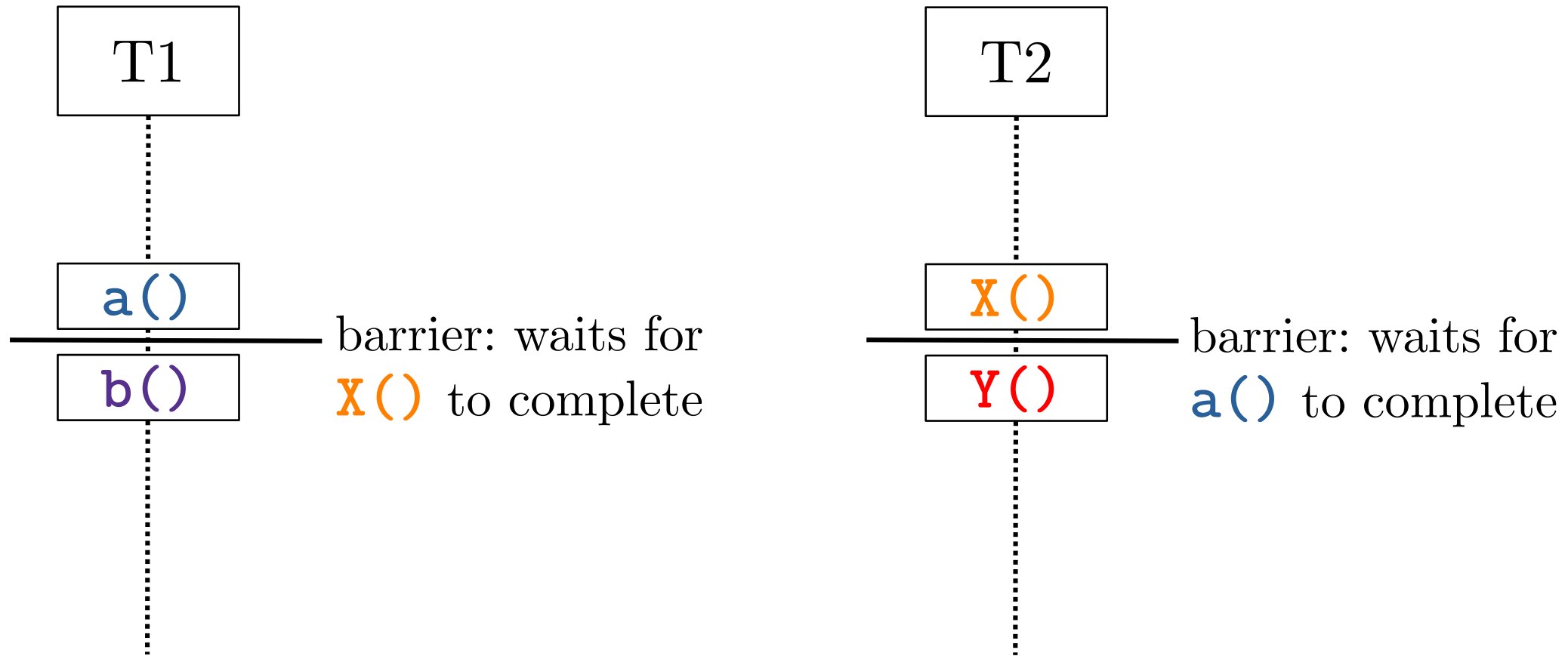
Constraint: We consider only those orders where $a()$ is performed before $y()$ and $x()$ is performed before $b()$ as **VALID**.

Task/Problem 1b: Barriers: $a() < Y()$, $X() < b()$



Constraint: We consider only those orders where $a()$ is performed before $Y()$ and $X()$ is performed before $b()$ as **VALID**.

Task/Problem 1b: Barriers: $a() < y()$, $x() < b()$



Constraint: We consider only those orders where $a()$ is performed before $y()$ and $x()$ is performed before $b()$ as **VALID**.

Semaphores

Synchronization Object: Semaphore

Semaphore **S** is an **integer** that signals permission or availability of resources.

S = n > 0 means there are **n** permits or resources available.

wait(S) – a method called by a process/thread in order to request (to **wait** for) a permit or access to a resource.

Decrements S (i.e. **S--;**).

signal(S) – a method called by a process/thread in order to return a permit or a resource. **Increments S** (i.e. **S++;**).

Synchronization Object: Semaphore

```
wait(S)
{
    while(S <= 0)
    {
        // busy wait
    }
    S--;
}
```

```
signal(S)
{
    S++;
}
```

Semaphores: Other Names for `wait` and `signal`

C

C++

`wait(S)`

`sem_wait(S)`

`S.acquire()`

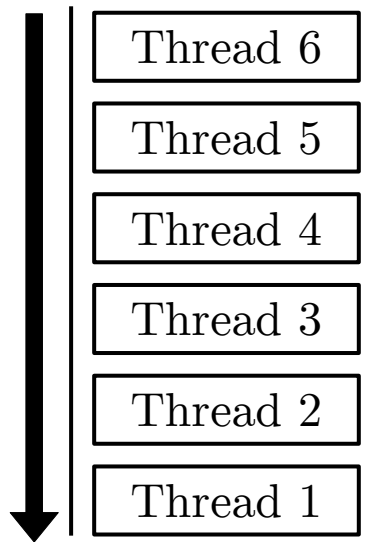
`signal(S)`

`sem_post(S)`

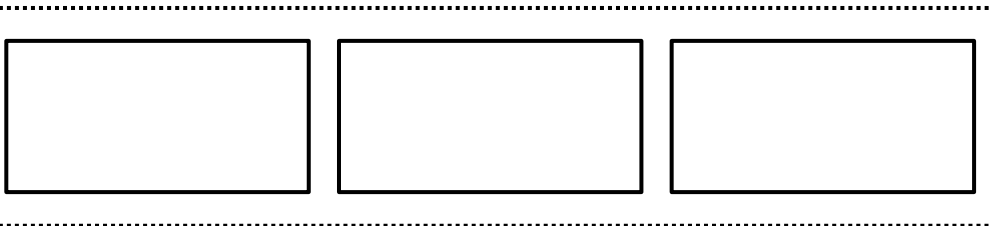
`S.release()`

Semaphore: Analogy + Some Information

Queue to Semaphore **S**



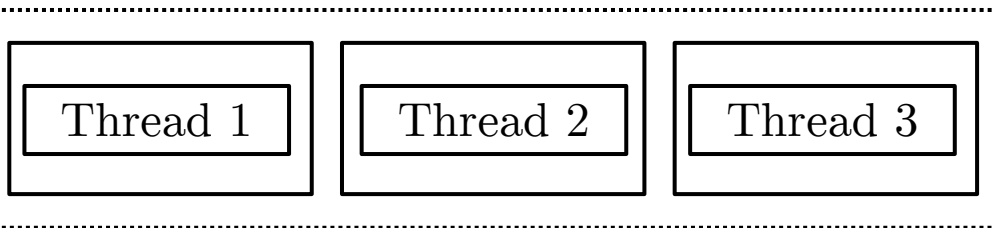
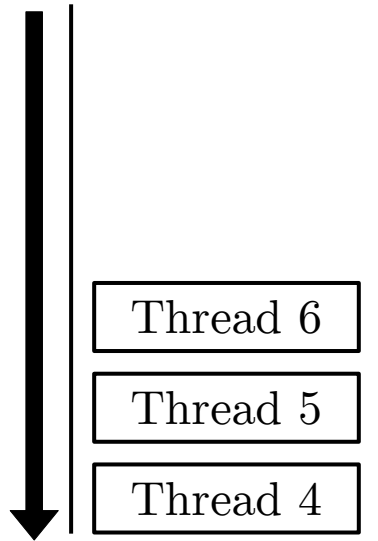
- The boxes represent the permits or available resources.
- The initial number of boxes represent the initial value of the semaphore which is the number of permits or resources available.
- The queue represent all threads that call **wait(S)**. These threads want permits or resources associated with **semaphore S**.
- **Multiplexing** is the idea that multiple threads can acquire permits or resources at the same time.



Initial: Semaphore S = 3

Semaphore: Analogy + Some Information

Queue to Semaphore **S**

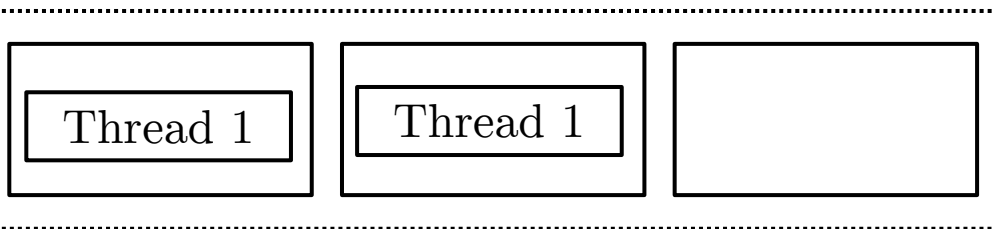
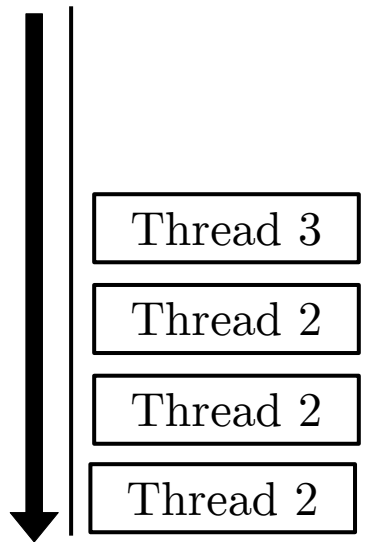


Semaphore **S** = 0

- The boxes represent the permits or available resources.
- The initial number of boxes represent the initial value of the semaphore which is the number of permits or resources available.
- The queue represent all threads that call **wait(S)**. These threads want permits or resources associated with **semaphore S**.
- **Multiplexing** is the idea that multiple threads can acquire permits or resources at the same time.

Semaphore: Some Information

Queue to Semaphore **S**

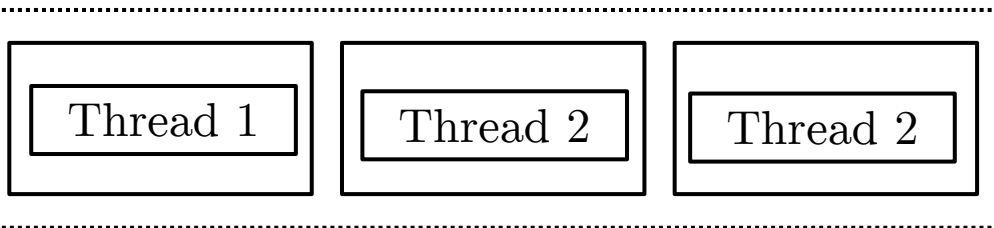
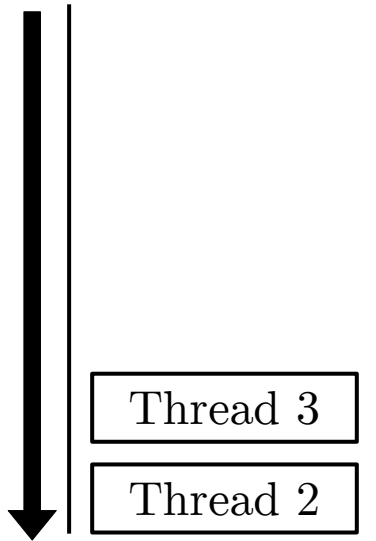


Semaphore S = 1

- **Multiplexing** is the idea that multiple threads can acquire permits or resources at the same time.
- A semaphore is called **counting** if it can give more than 1 permit or resource.
- A semaphore is called **binary** if at most it can give 1 permit or 1 resource. $S \leq 1$.
- A thread calling **wait(S)** multiple times means it wants multiple permits or access to multiple resources associated with semaphore **semaphore S**.

Semaphore: Analogy + Information

Queue to Semaphore **S**



Semaphore S = 0

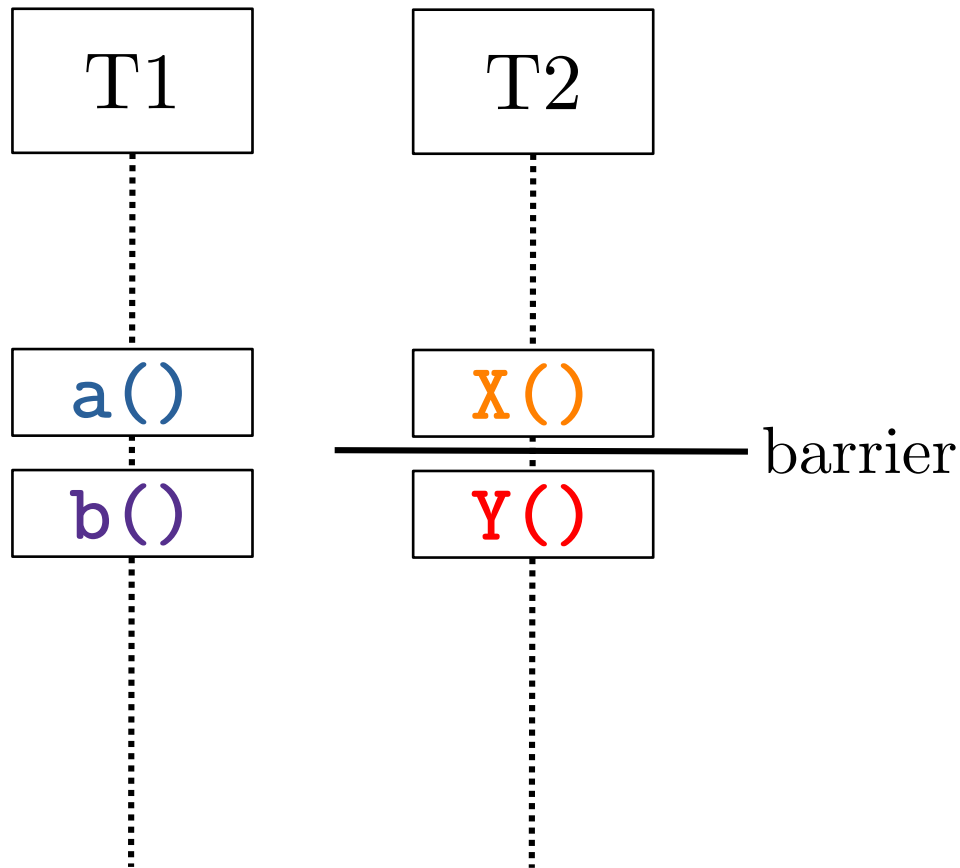
Thread 1 **signal(S)**

- Threads calling the **signal(S)** increments **semaphore S** and thus increasing the number of permits or resources available that are associate with **semaphore S**.
- In different programming languages, you can specify a semaphore's upper limit value which is the maximum number of permits or resources associated with that semaphore.

Synchronization Task/Problem 1a: **(Thread) Barrier**

[Solution Description]

Solution 1a: Barrier: $a() < y()$

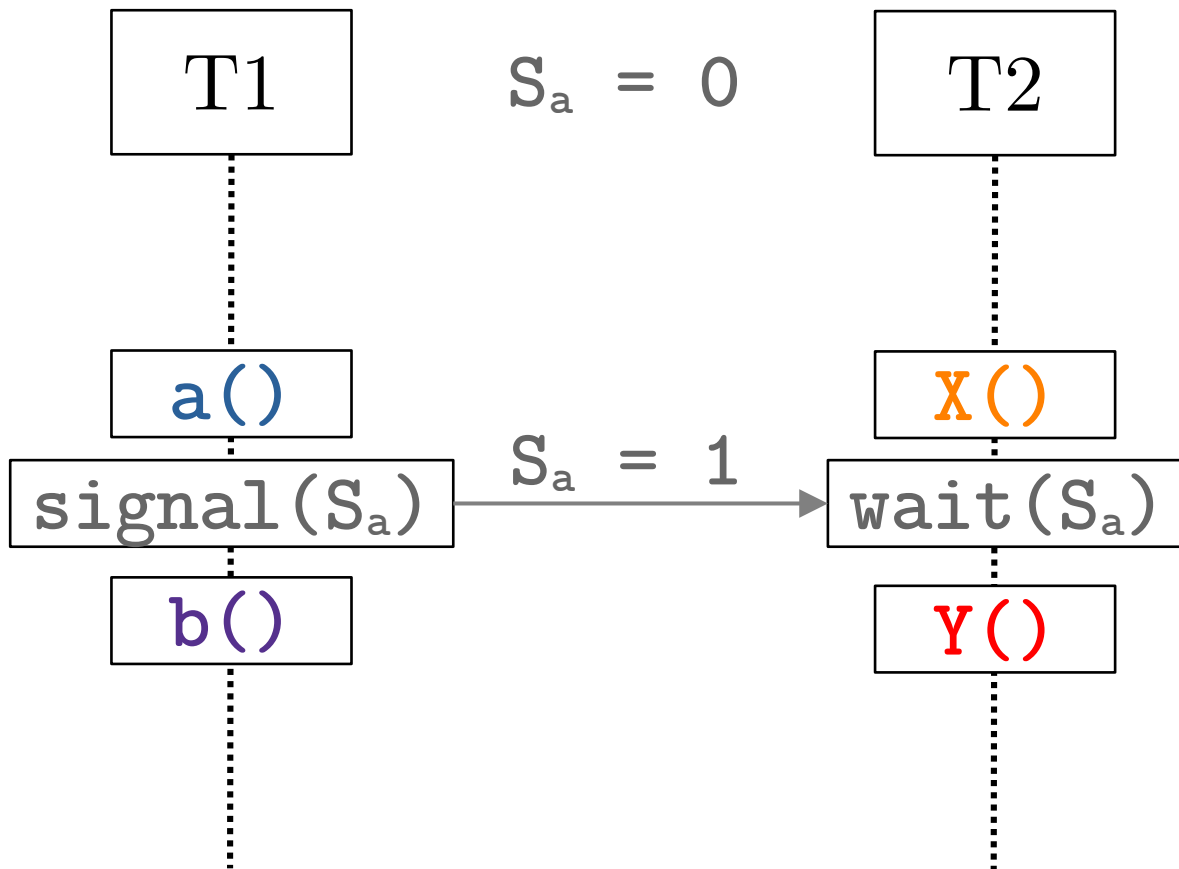


A *barrier* should be placed before the call $y()$ in T2.

This barrier means T2 has to wait for T1 to complete the $a()$ call before performing $y()$.

Constraint: We consider only those orders where $a()$ is performed before $y()$ as **VALID**.

Solution 1a: Barrier: $a() < y()$



S_a represents the
‘y’ *permit*.

Initially, $S_a = 0$.

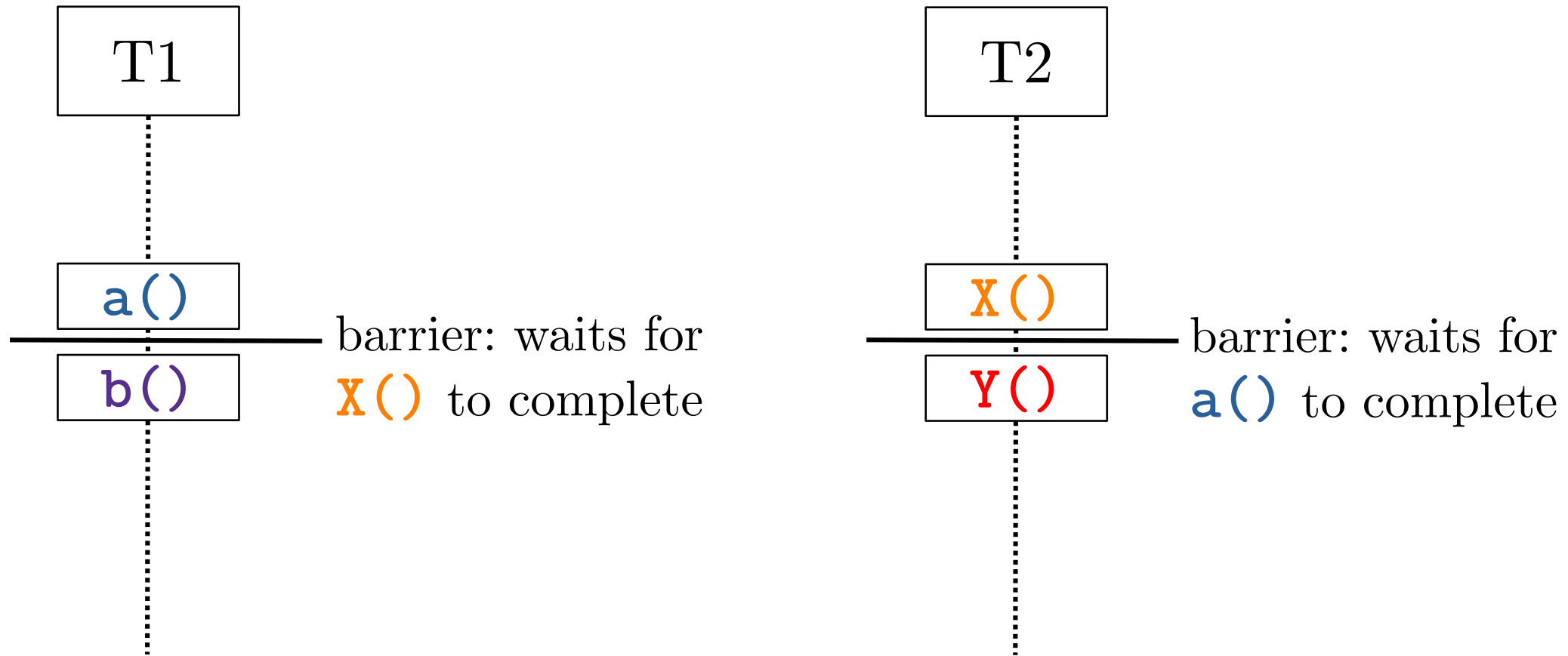
T2 can only exit
 $\text{wait}(S_a)$ and call
y() if there is at
least *1 permit*.

The *1 permit* is
only available when
T1 calls $\text{signal}(S_a)$
after $a()$ executes.

Synchronization Task/Problem 1b: **(Thread) Barriers**

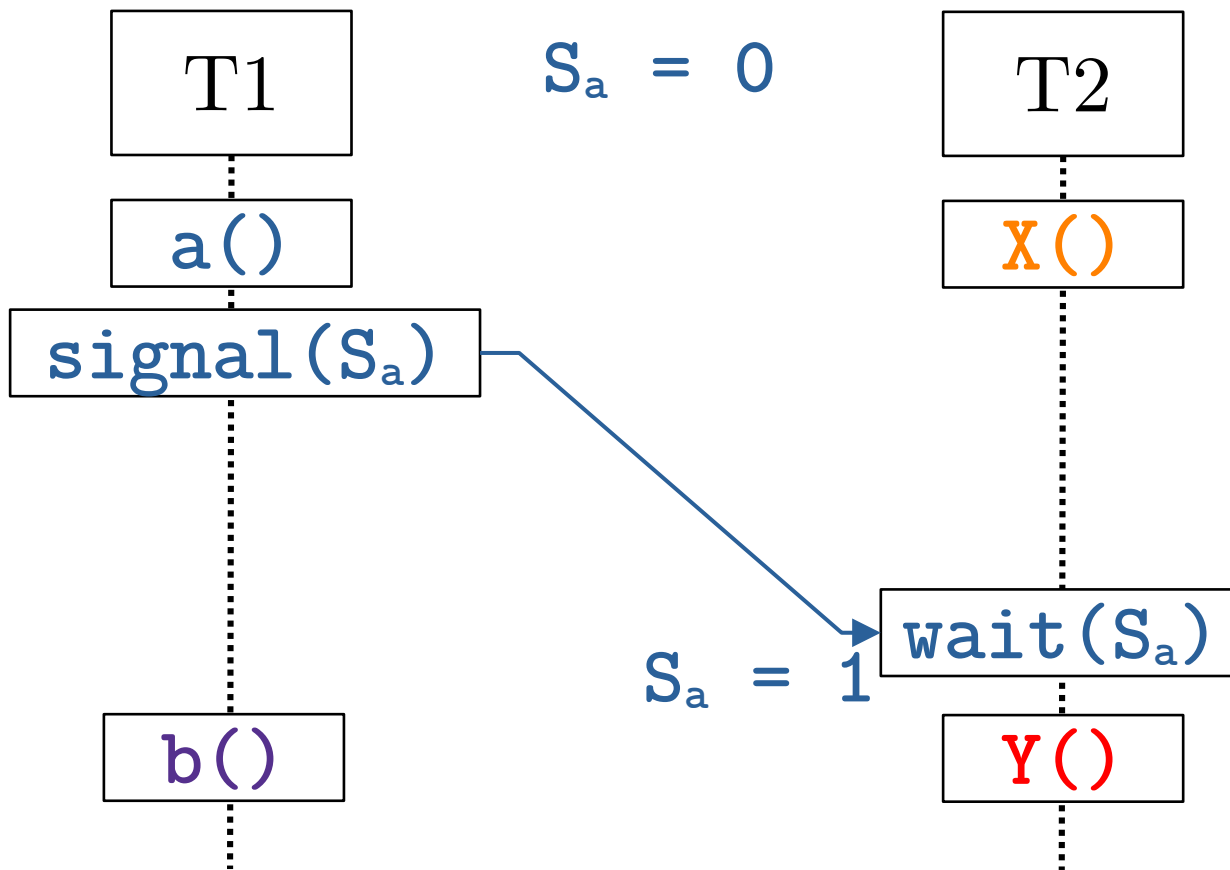
[Solution Description]

Solution 1b: Barriers: $a() < y()$, $x() < b()$



Constraint: We consider only those orders where $a()$ is performed before $y()$ and $x()$ is performed before $b()$ as **VALID**.

Solution 1b: Barriers: $a() < y()$, $x() < b()$



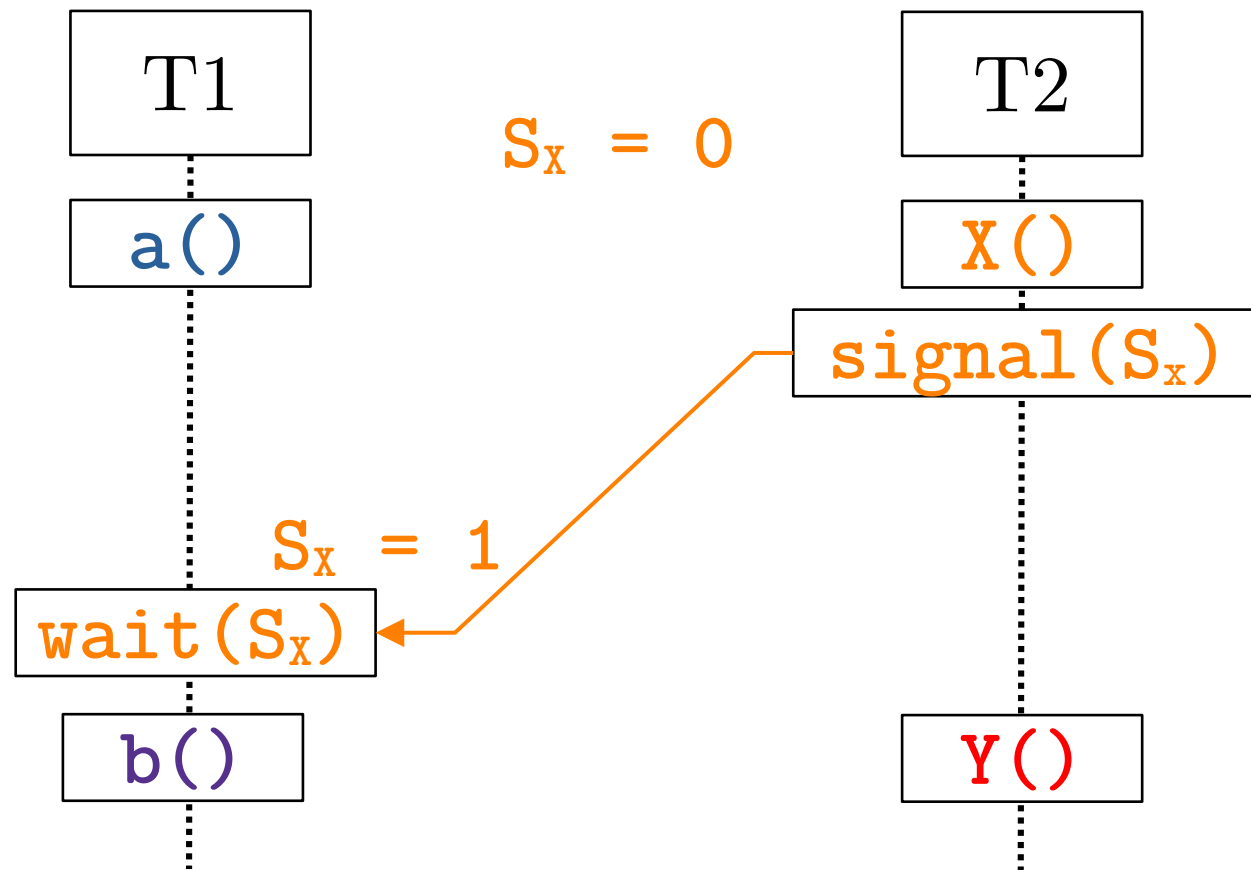
S_a represents the
'y' *permit*.

Initially, $S_a = 0$.

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 $\text{wait}(S_a)$ and call
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Solution 1b: Barriers: $a() < y()$, $x() < b()$



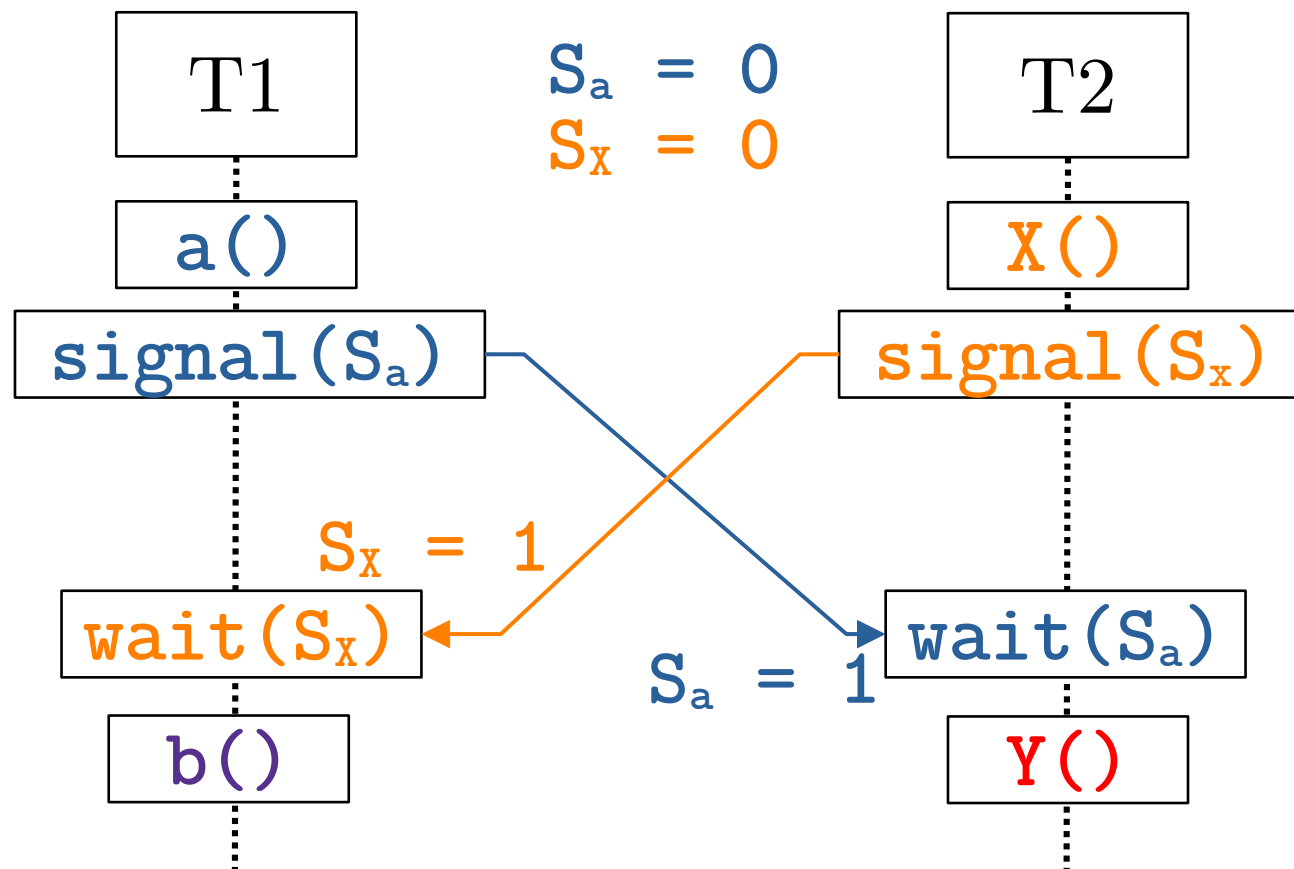
S_x represents the
'b' *permit*.

Initially, $S_x = 0$.

T1 can only exit
 $wait(S_x)$ and call
 $b()$ if there is at
least *1 permit*.

The *1 permit* is
only available when
T2 calls $signal(S_x)$
after $x()$ executes.

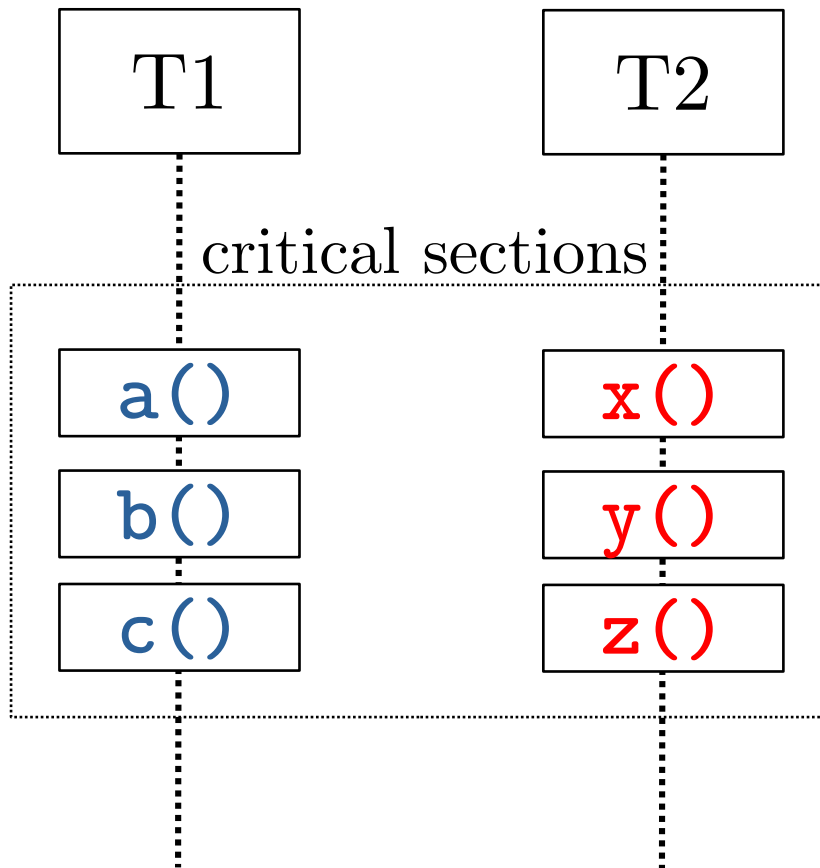
Solution 1b: Barriers: $a() < y()$, $x() < b()$



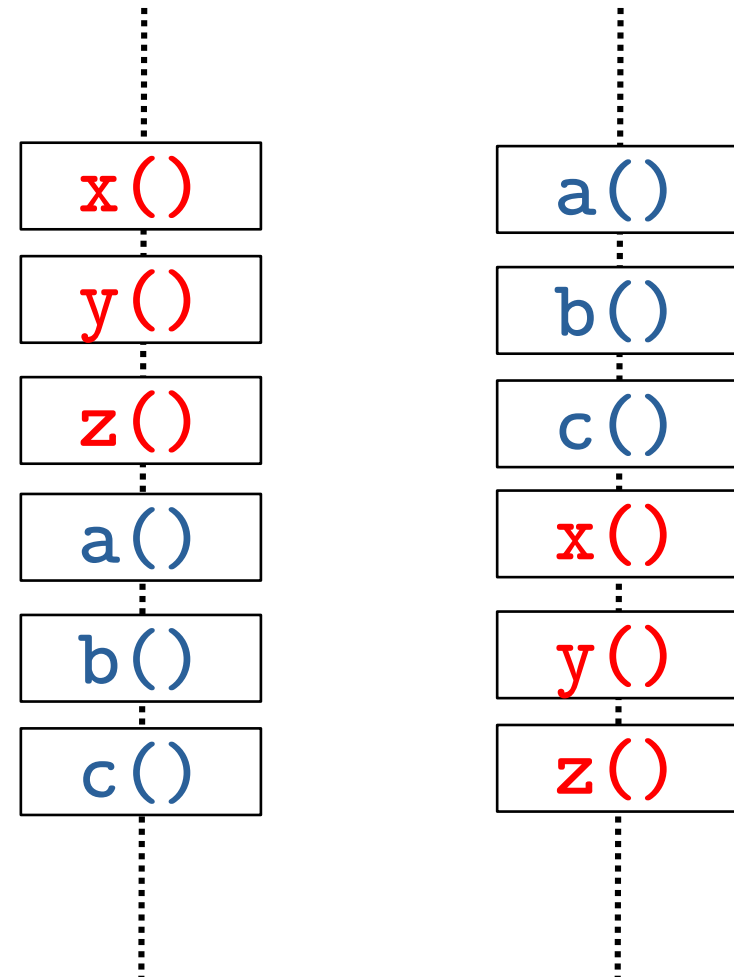
Synchronization Task/Problem 2: **Mutual Exclusion**

[Problem & Solution Descriptions]

Task/Problem 2: Mutual Exclusion

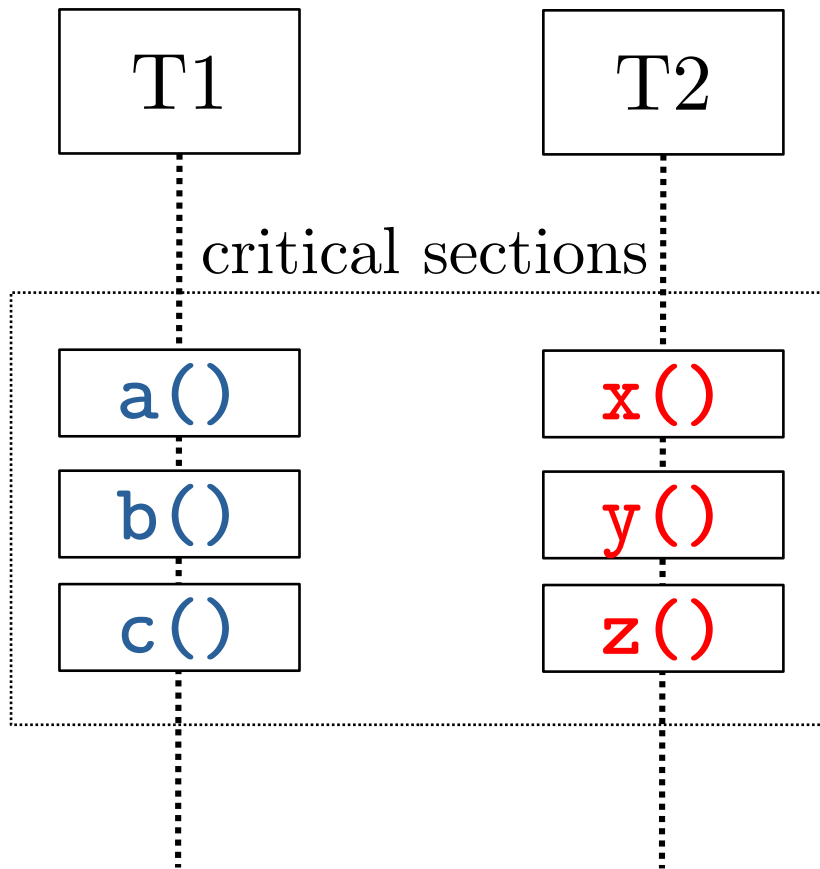


VALID orders

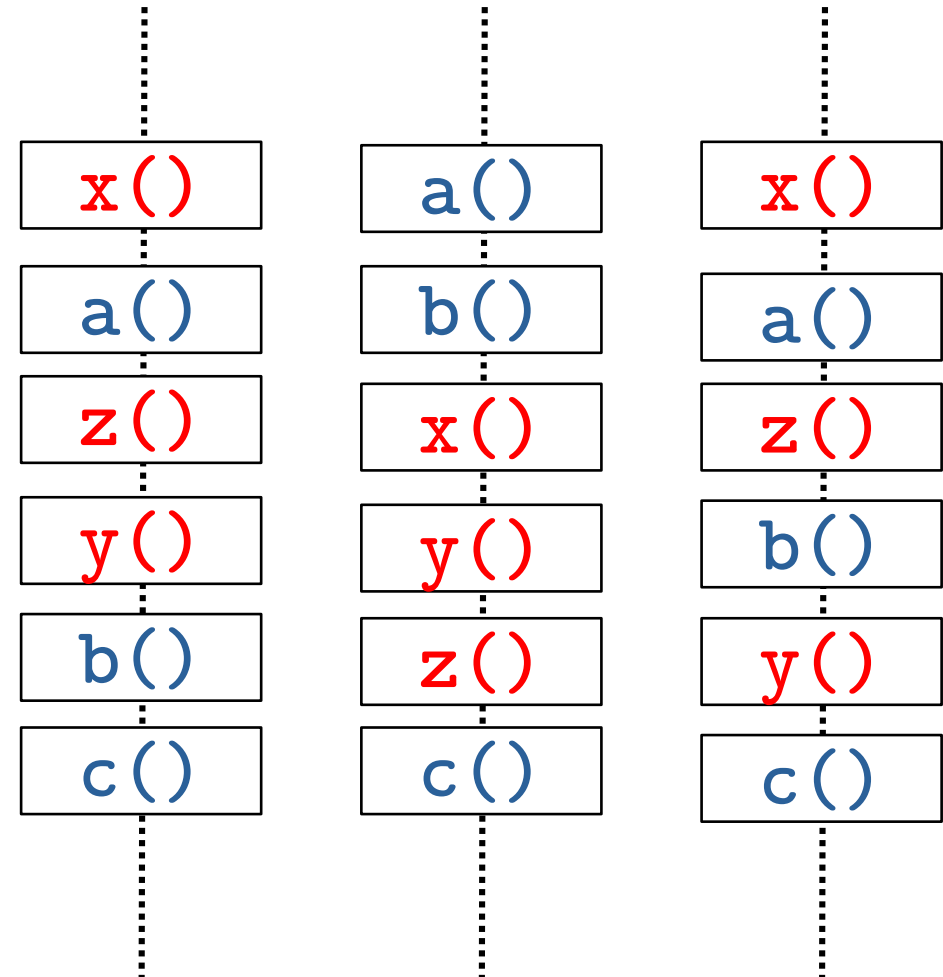


Constraint: Instructions/Operations in T1 and T2's critical sections should NOT interleaved.

Task/Problem 2: Mutual Exclusion

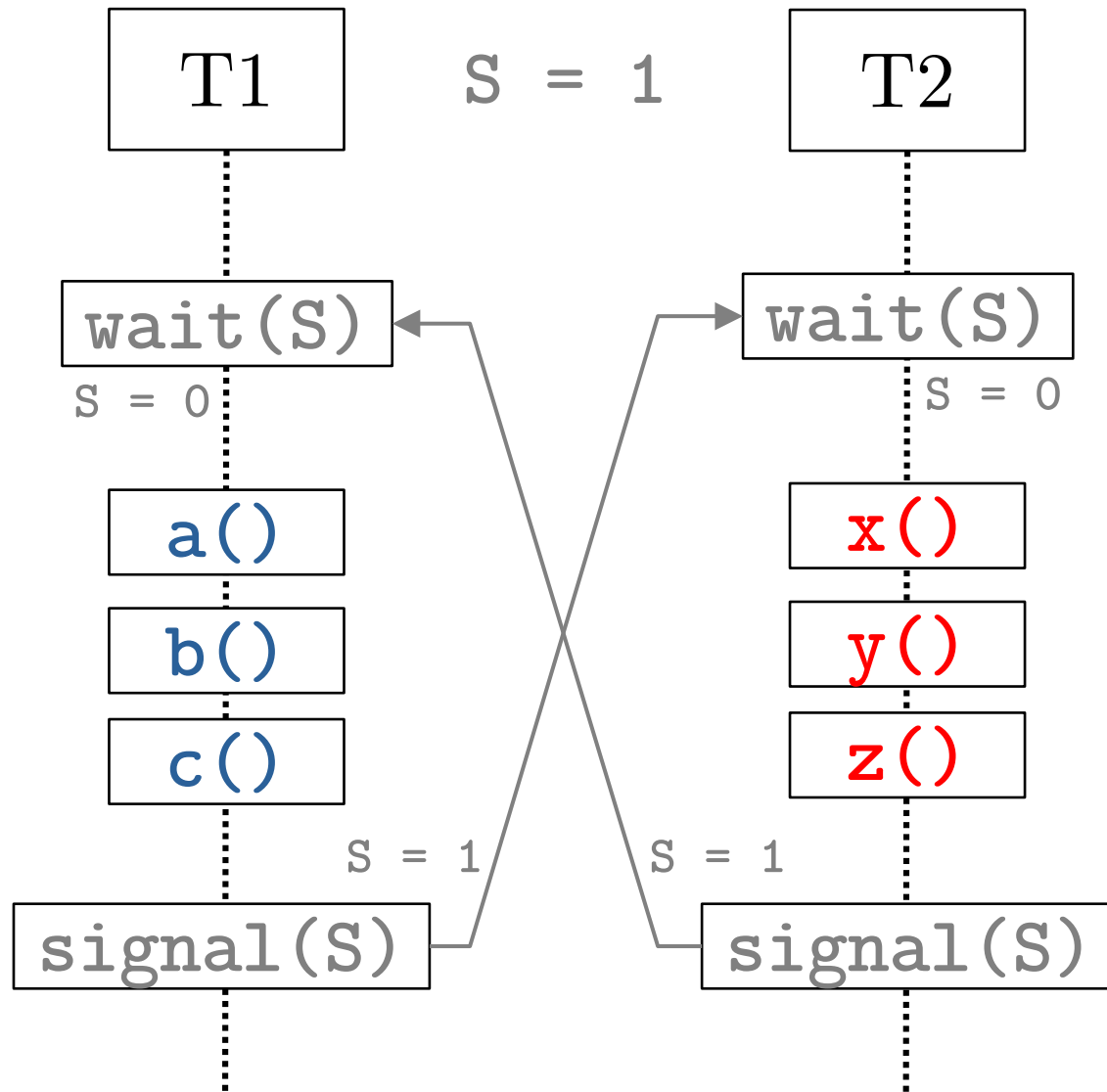


some **INVALID** orders



Constraint: Instructions/Operations in T1 and T2's critical sections should NOT interleaved.

Solution 2: Mutual Exclusion

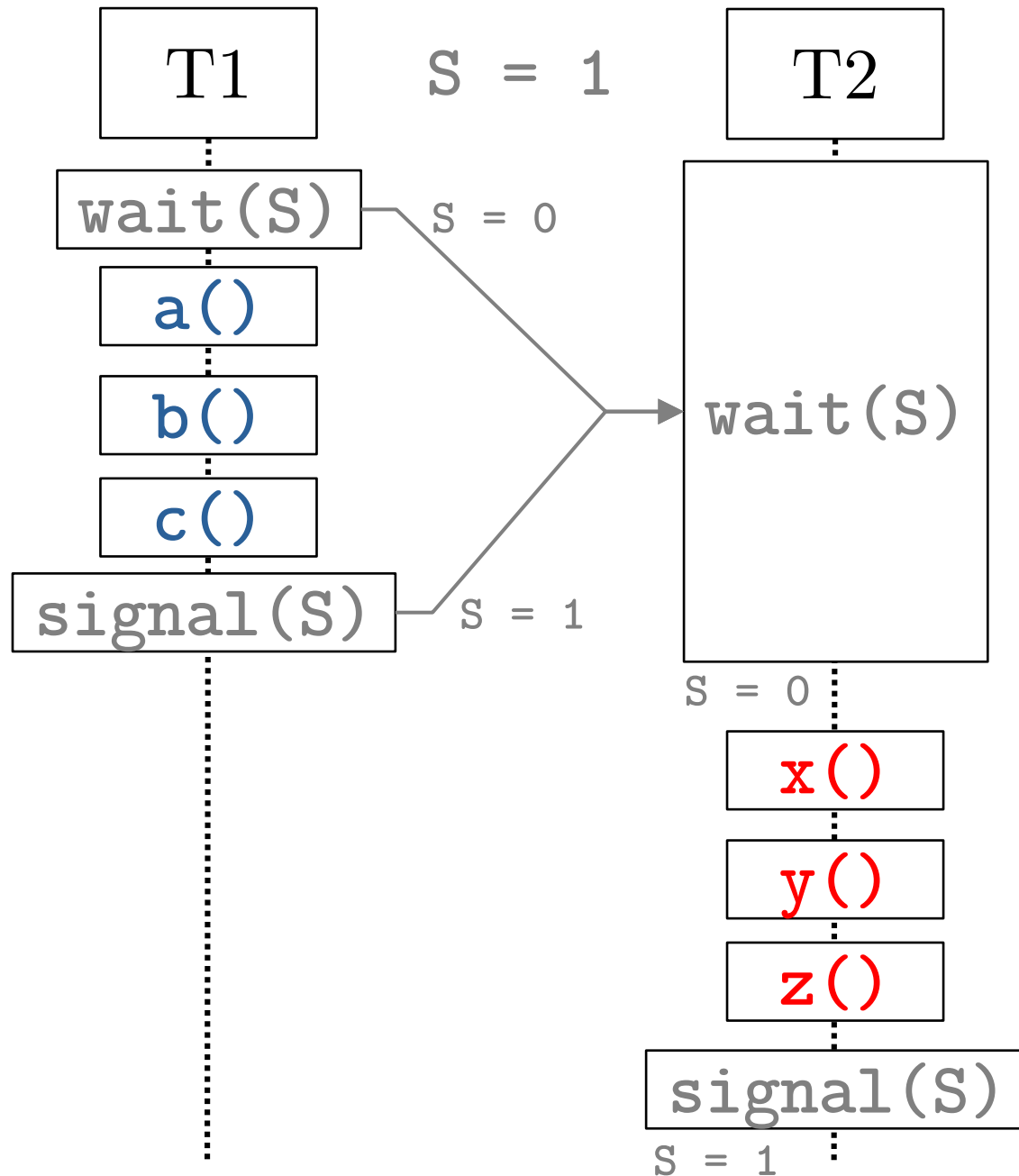


$S = 1$ means *1 permit* is available.

Only one thread, **T1** or **T2**, will be given the permit and can exit the `wait(S)` loop, set $S = 0$, and enter its critical section.

After executing its critical section, the thread will now call `signal(S)` and set $S = 1$ which gives the other thread a permit to enter its critical section.

Solution 2: Mutual Exclusion

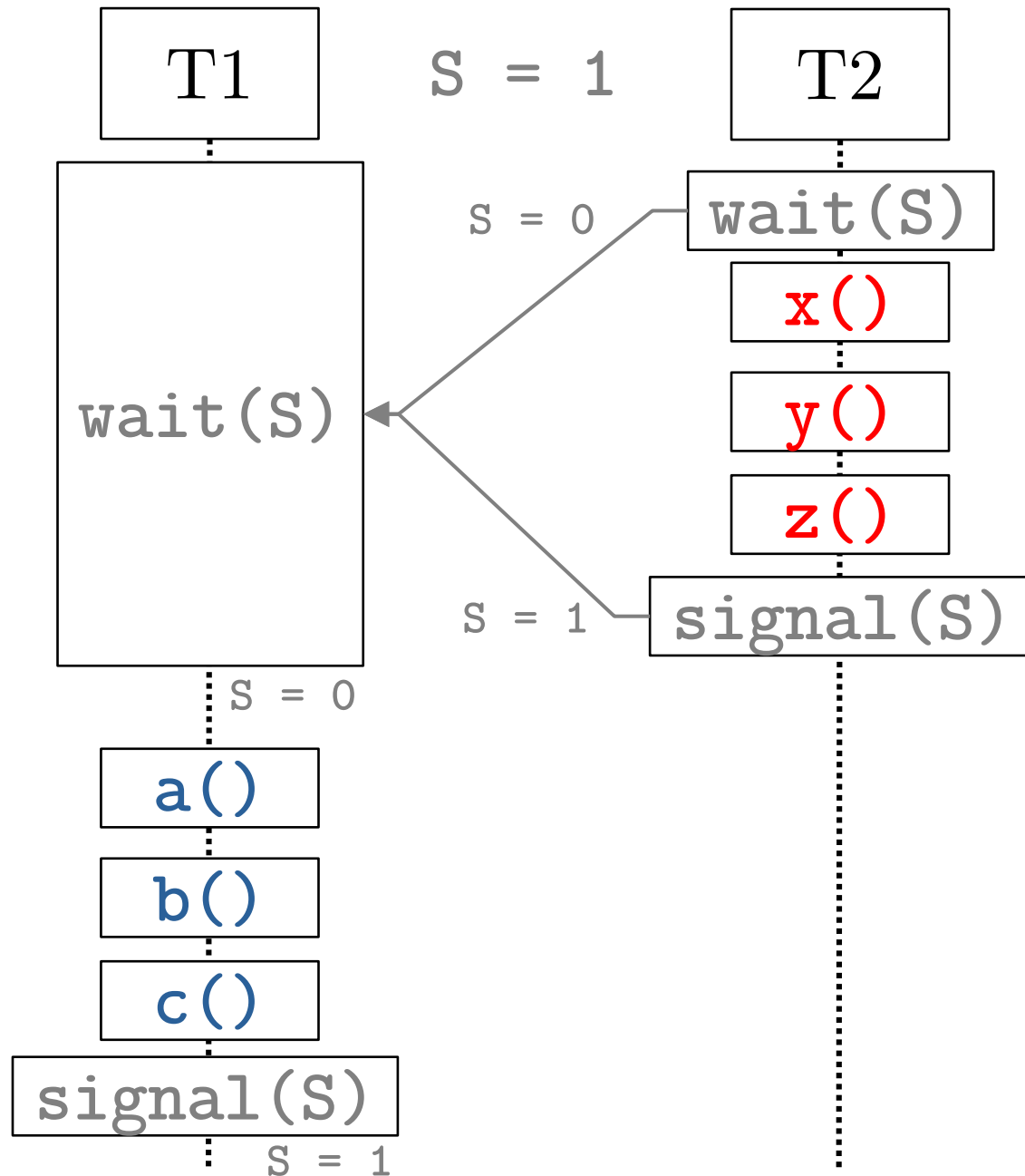


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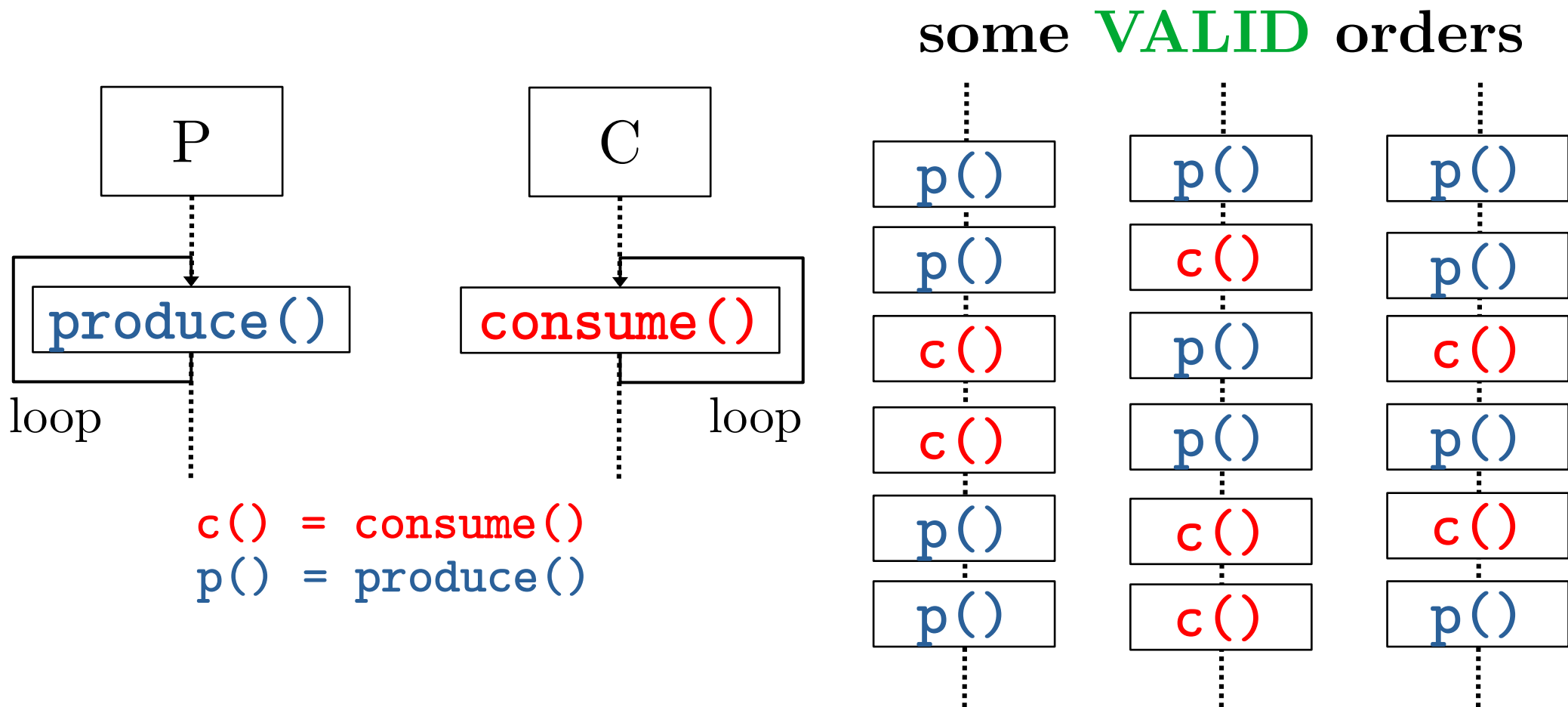
After executing its critical section, the thread will now call `signal(S)` and set $S = 1$ which gives the other thread a permit to enter its critical section.

Synchronization Task/Problem 3a:

Producer-Consumer

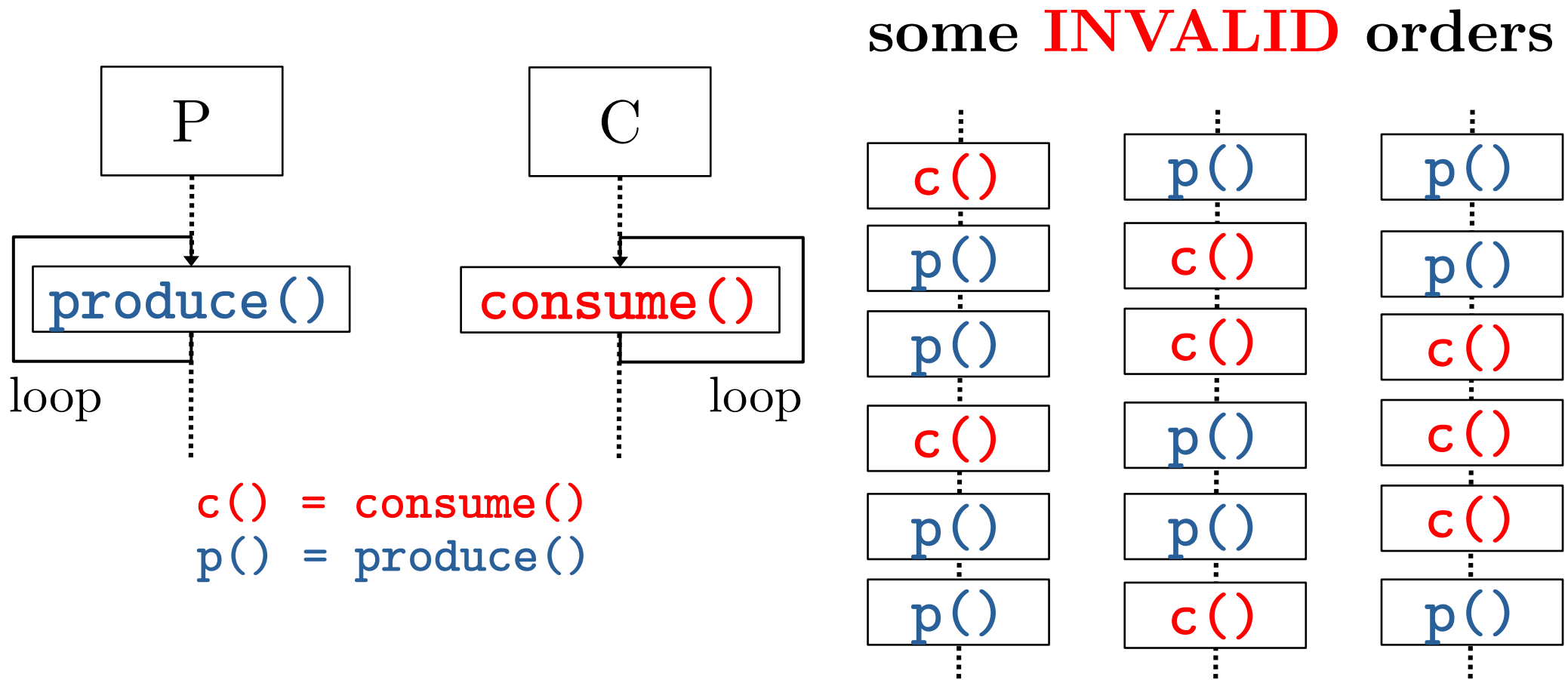
[Problem & Solution Descriptions]

Task/Problem 3a: Producer(**p**)-Consumer(**c**) Problem



Constraint: Before a **consume()** call can occur a corresponding **produce()** call should have occurred first.

Task/Problem 3a: Producer(**p**)-Consumer(**c**) Problem



Constraint: Before a **consume()** call can occur a corresponding **produce()** call should have occurred first

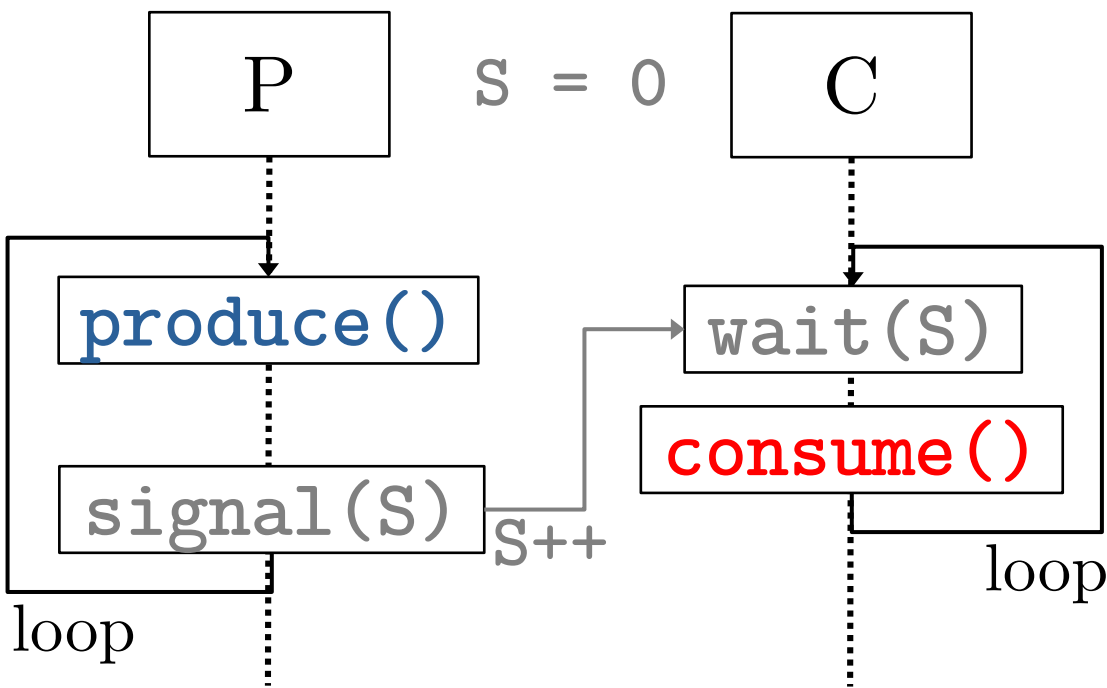
Task/Problem 3a: Producer(**p**)-Consumer(**c**) Problem

$S = 0$ means 0 *permit* is available.

Thread **C** is the one calling `wait(S)` and is waiting for a permit to call **consume()**.

Thread **P** will call `signal(S)` only after calling **produce()**. `signal(S)` will increment S .

Thread **C** can only call **consume()** if there is a corresponding call to **produce()** prior.

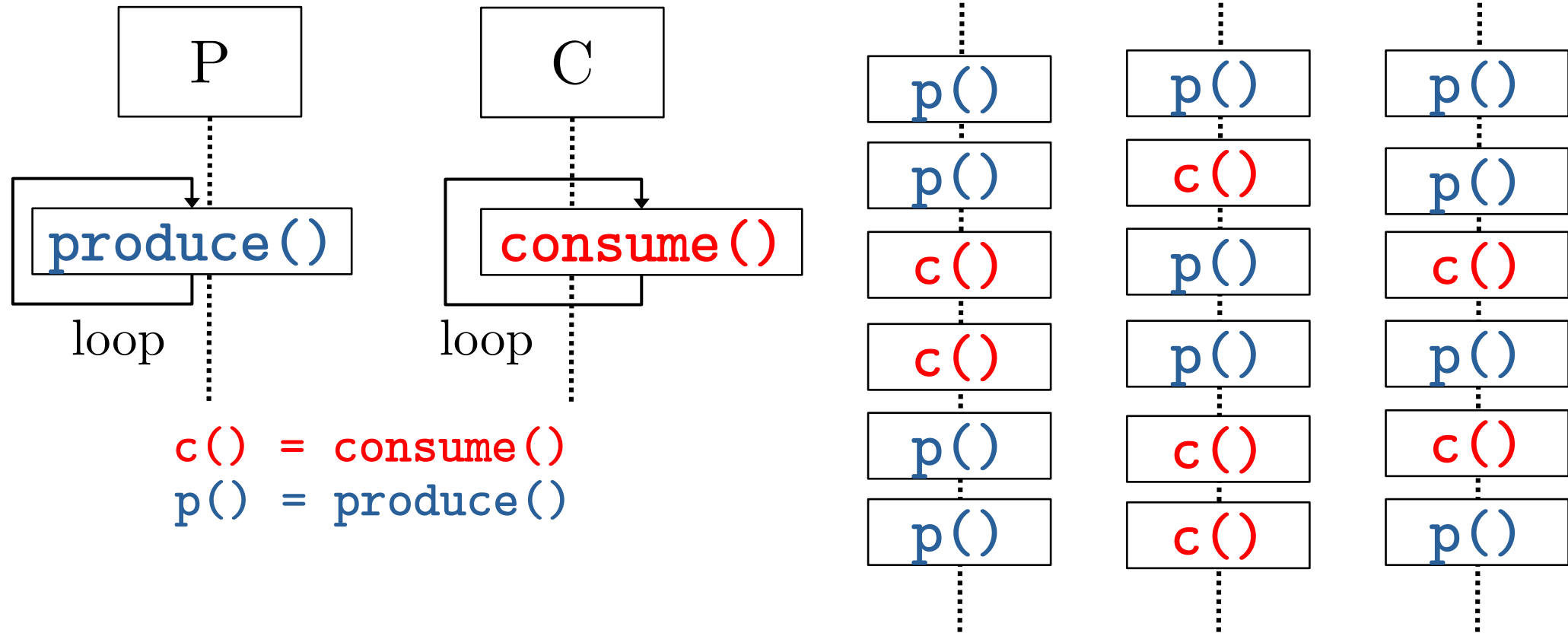


Synchronization Task/Problem 3b: **Bounded Buffer**

[Problem & Solution Descriptions]

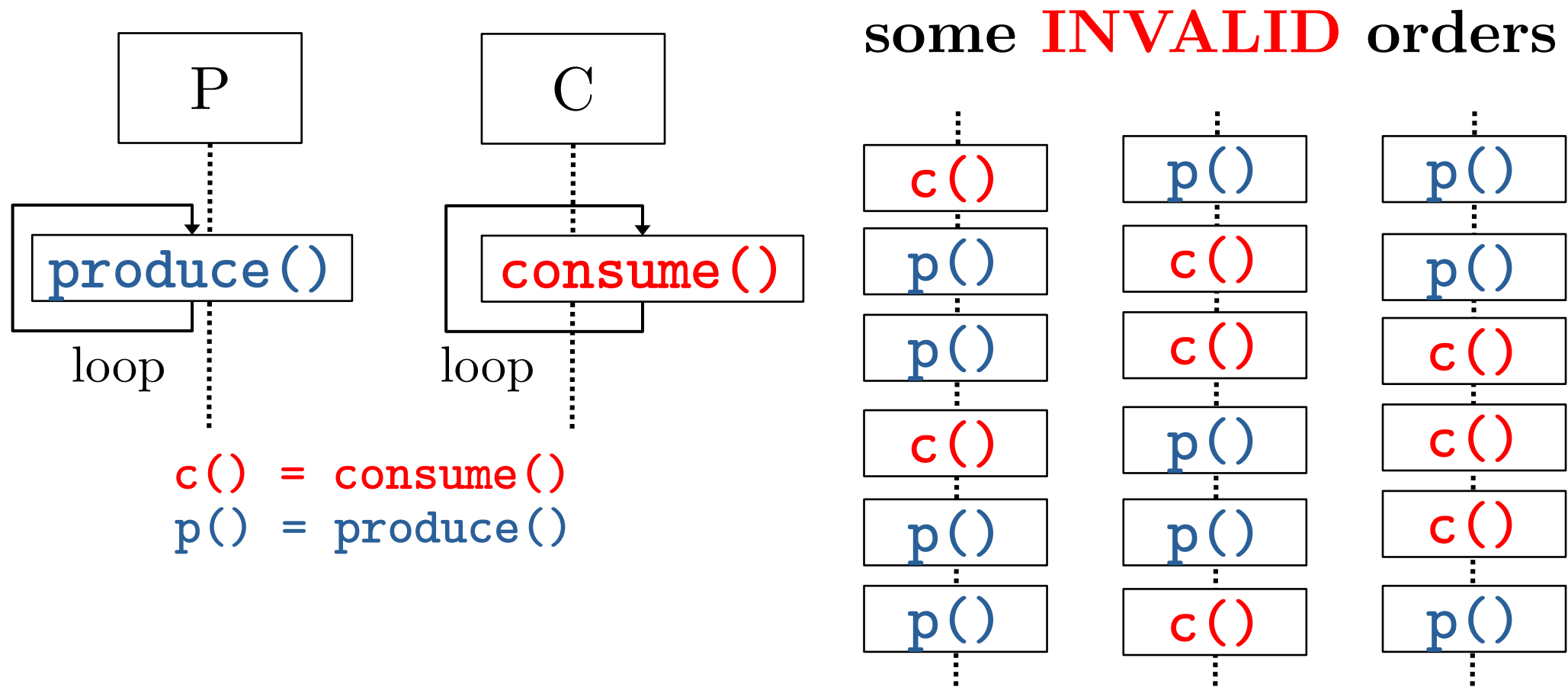
Task/Problem 3b: Bounded Buffer. i.e. Buffer Size = 3

some **VALID** orders



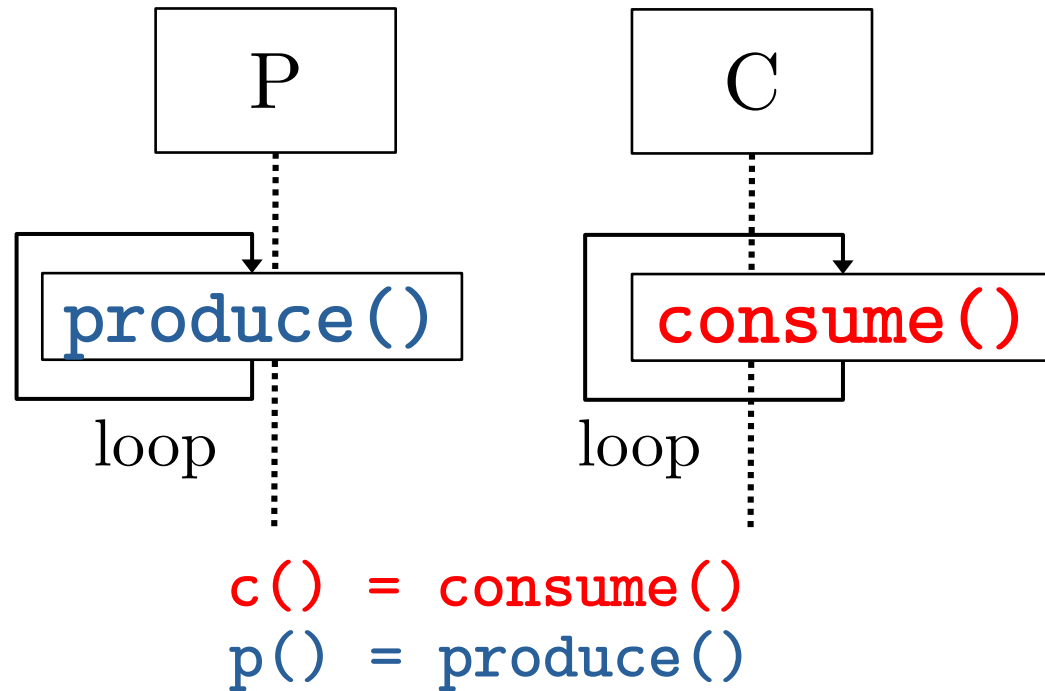
Constraint: Before a `consume()` call can occur a corresponding `produce()` call should have occurred first. At most 3 calls to `produce()` can occur that have no corresponding calls to `consume()`. i.e. Buffer is full after 3 calls to `produce()` (and 0 calls to `consume()`).

Task/Problem 3b: Bounded Buffer. i.e. Buffer Size = 3

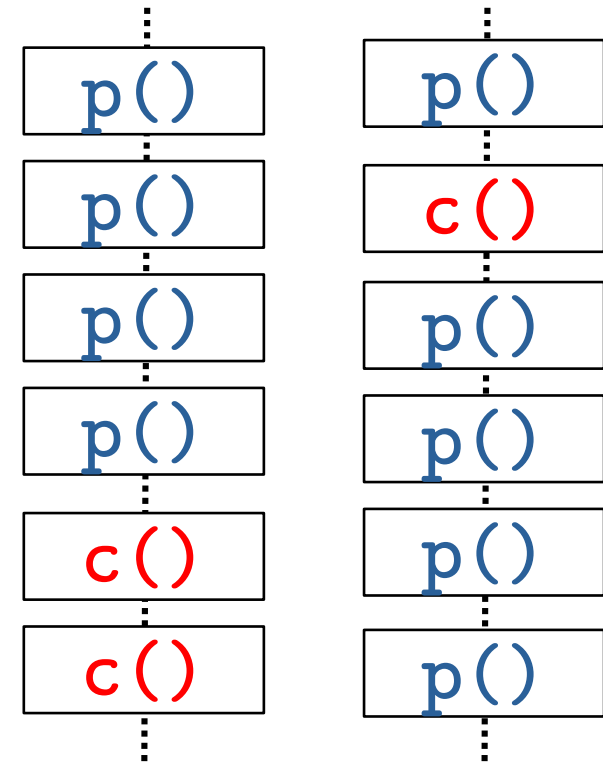


Constraint: Before a **consume()** call can occur a corresponding **produce()** call should have occurred first. At most 3 calls to **produce()** can occur that have no corresponding calls to **consume()**.
i.e. Buffer is full after 3 calls to **produce()**.

Task/Problem 3b: Bounded Buffer. i.e. Buffer Size = 3



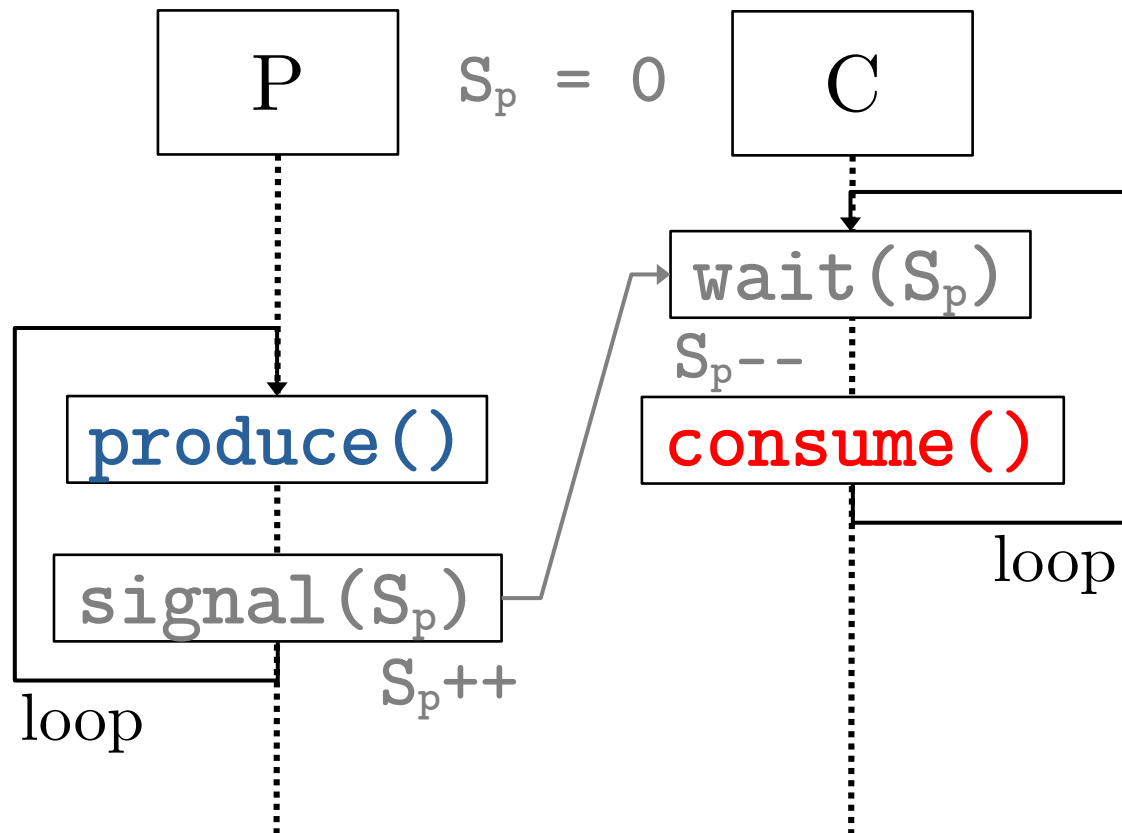
some **INVALID** orders



Constraint: Before a **consume()** call can occur a corresponding **produce()** call should have occurred first. At **most 3 calls** to **produce()** can occur that have no corresponding calls to **consume()**. i.e. Buffer is full after 3 calls to **produce()**.

Task/Problem 3b: Bounded Buffer. i.e. Buffer Size = 3

$S_p = 0$ means 0 '**consume**' *permit* is available.



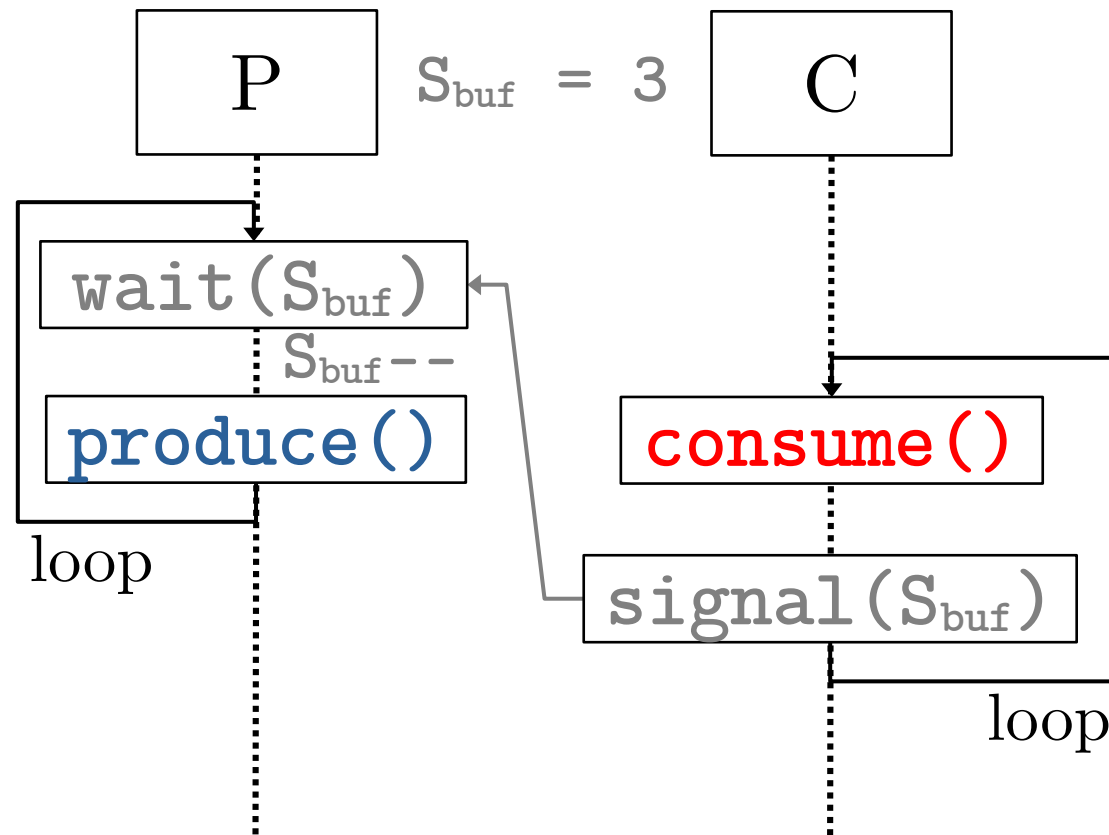
Thread **C** is the one calling `wait(S_p)` and is waiting for a permit before calling **consume()**.

Thread **P** will call `signal(S_p)` only after calling `produce()`. `signal(S_p)` will increment S_p .

Thread C can only call **consume()** if there is a corresponding call to `produce()` prior.

Task/Problem 3b: Bounded Buffer. i.e. Buffer Size = 3

$S_{\text{buf}} = 3$ means 3 ‘**produce**’ *permit* is available.



Thread **P** is the one calling `wait(S_{buf})` and is waiting for a permit before calling **produce()**.

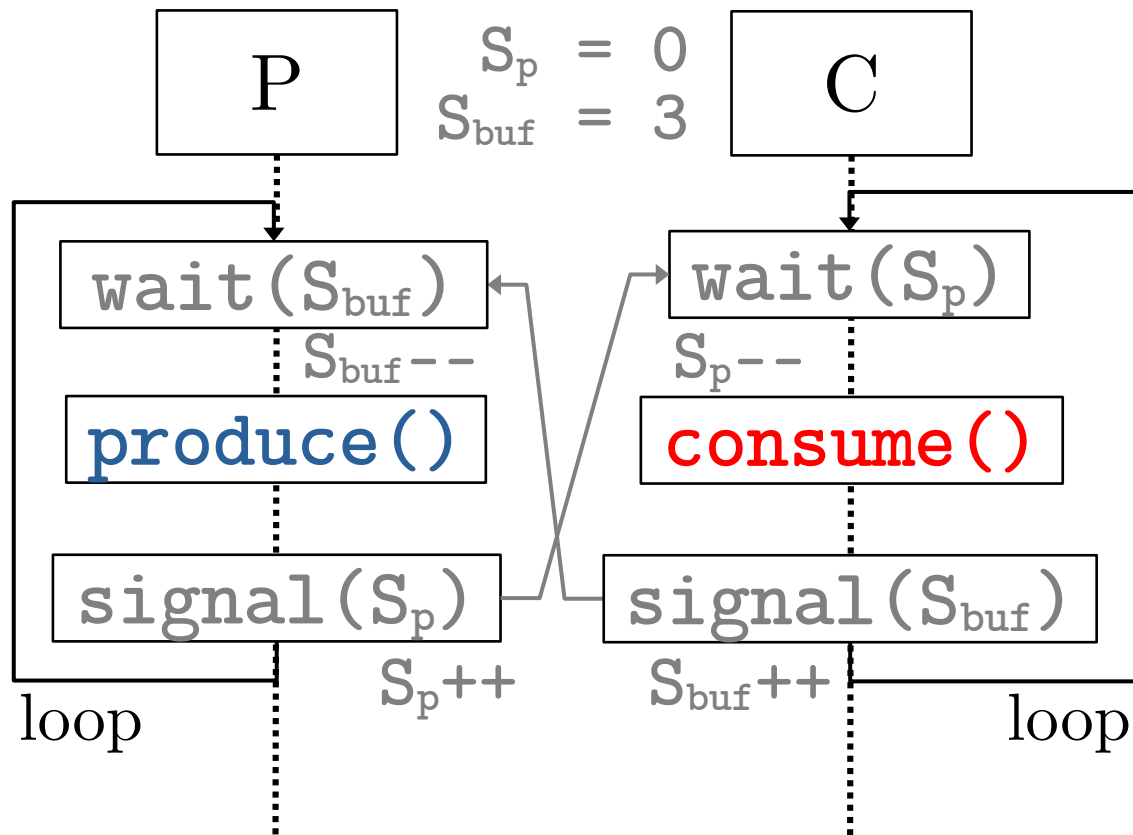
Thread **C** will call `signal(S_p)` only after calling **consume()**. `signal(S_p)` will increment S_p .

Thread C can only call **consume()** if there is a corresponding call to **produce()** prior.

Task/Problem 3b: Bounded Buffer. i.e. Buffer Size = 3

S_p represents the number of
'**consume**' *permits*.

S_{buf} represents the number of
'**produce**' *permits*.



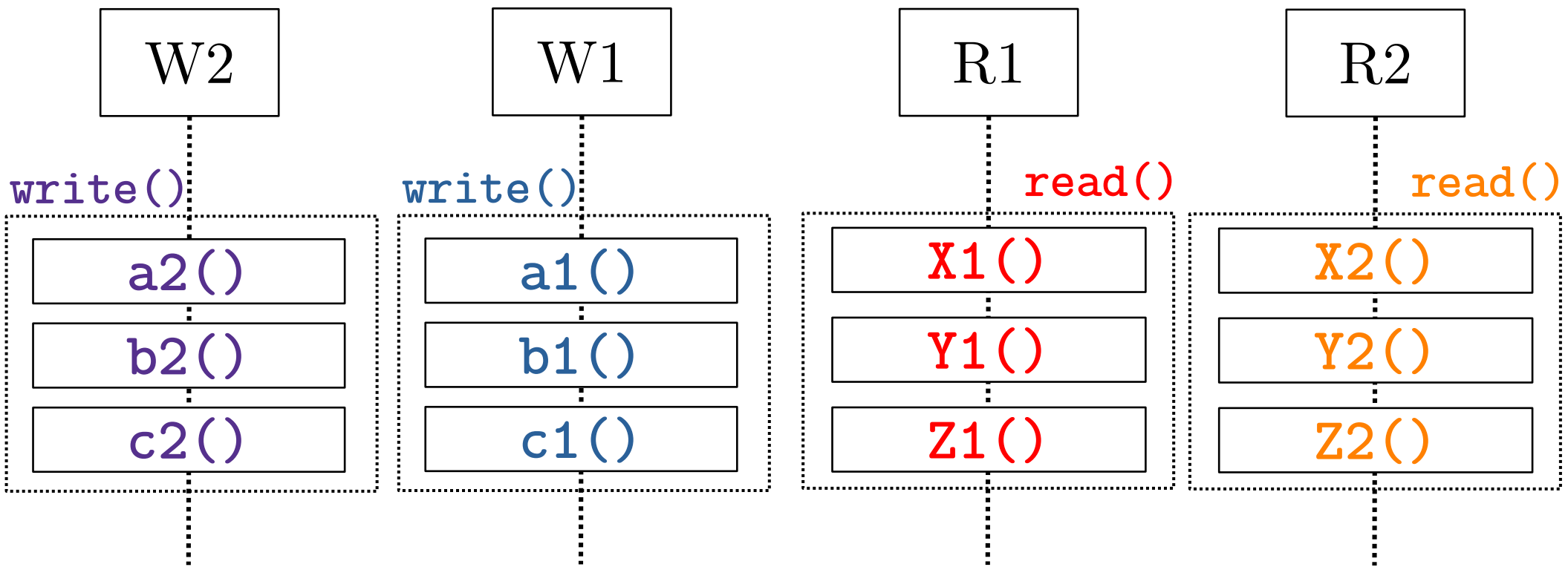
Thread **P** calls `wait(S_{buf})` to wait for a '**produce**' *permit* before calling `produce()`. After calling `produce()`, thread **P** calls `signal(S_p)` to increment the **consume** permit.

Thread **C** calls `wait(S_p)` to wait for a '**consume**' *permit* before calling `consume()`. After calling `consume()`, thread **C** calls `signal(S_{buf})` to increment the **produce** permit.

Synchronization Task/Problem 4: **Readers-Writers**

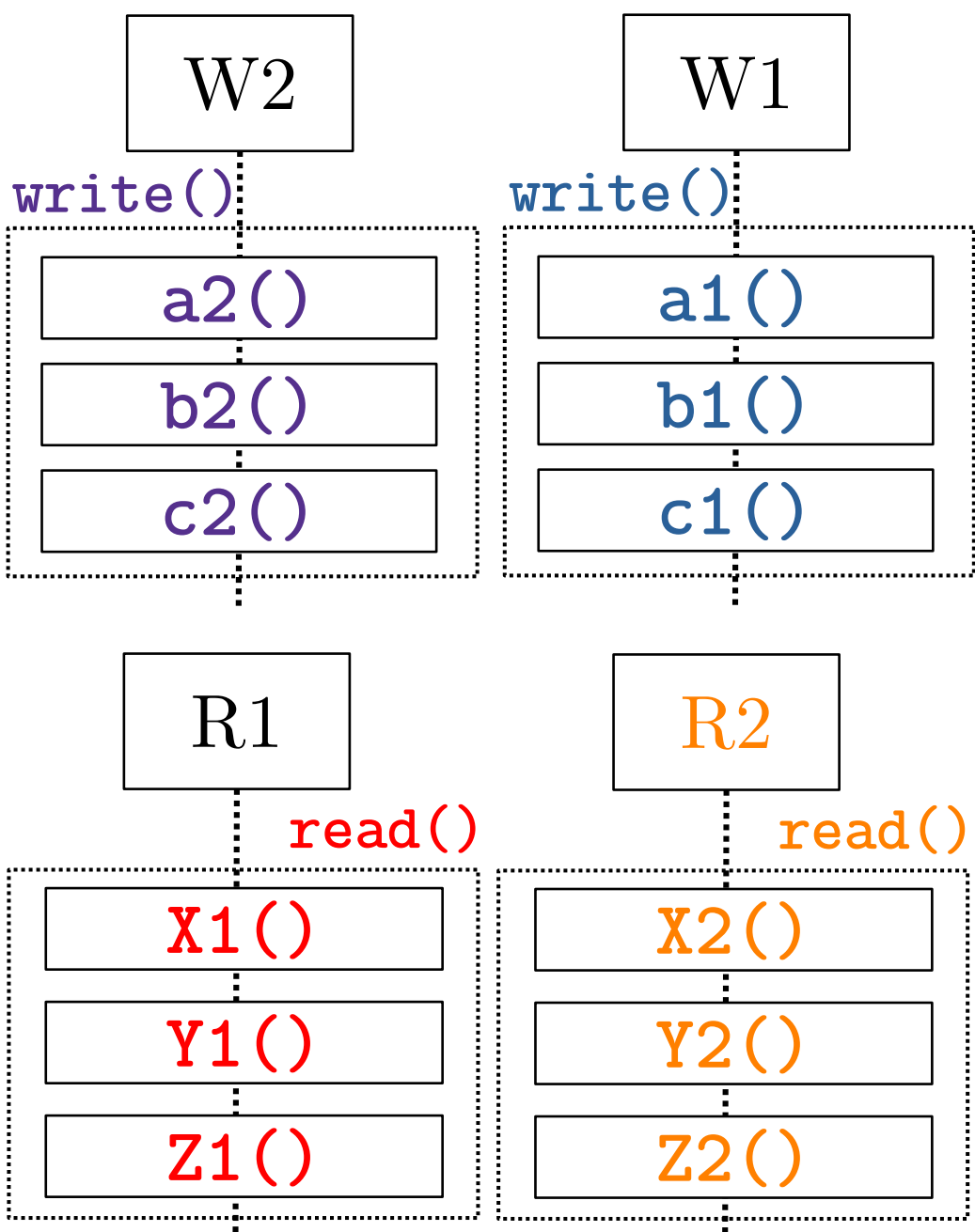
[Problem & Solution Descriptions]

Task/Problem 4: Reads-Writers

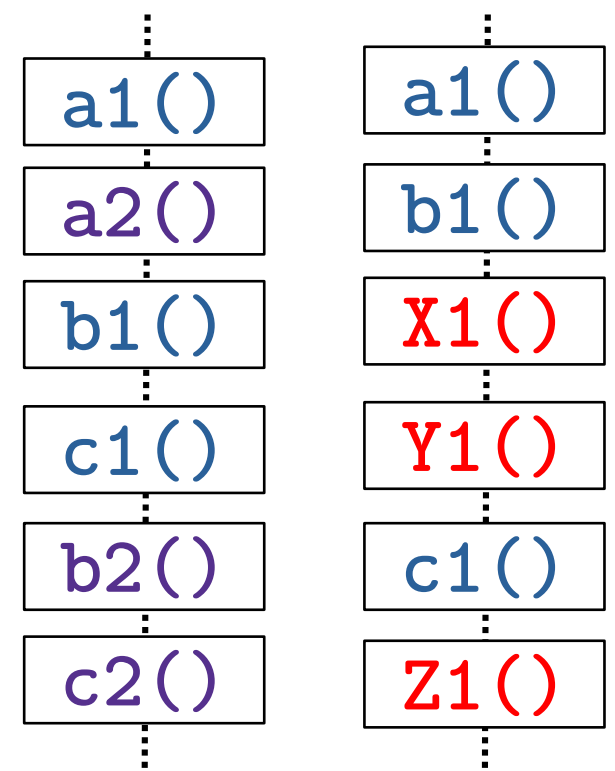


Constraint: A writer thread has exclusive access. No other threads (writer or reader) can access their `write()` or `read()` function if there is a writer thread calling `write()`. Reader threads, as a group, can access call their `read()` function concurrently and no writer threads can call their `write()` function while at least one reader thread is calling `read()`.

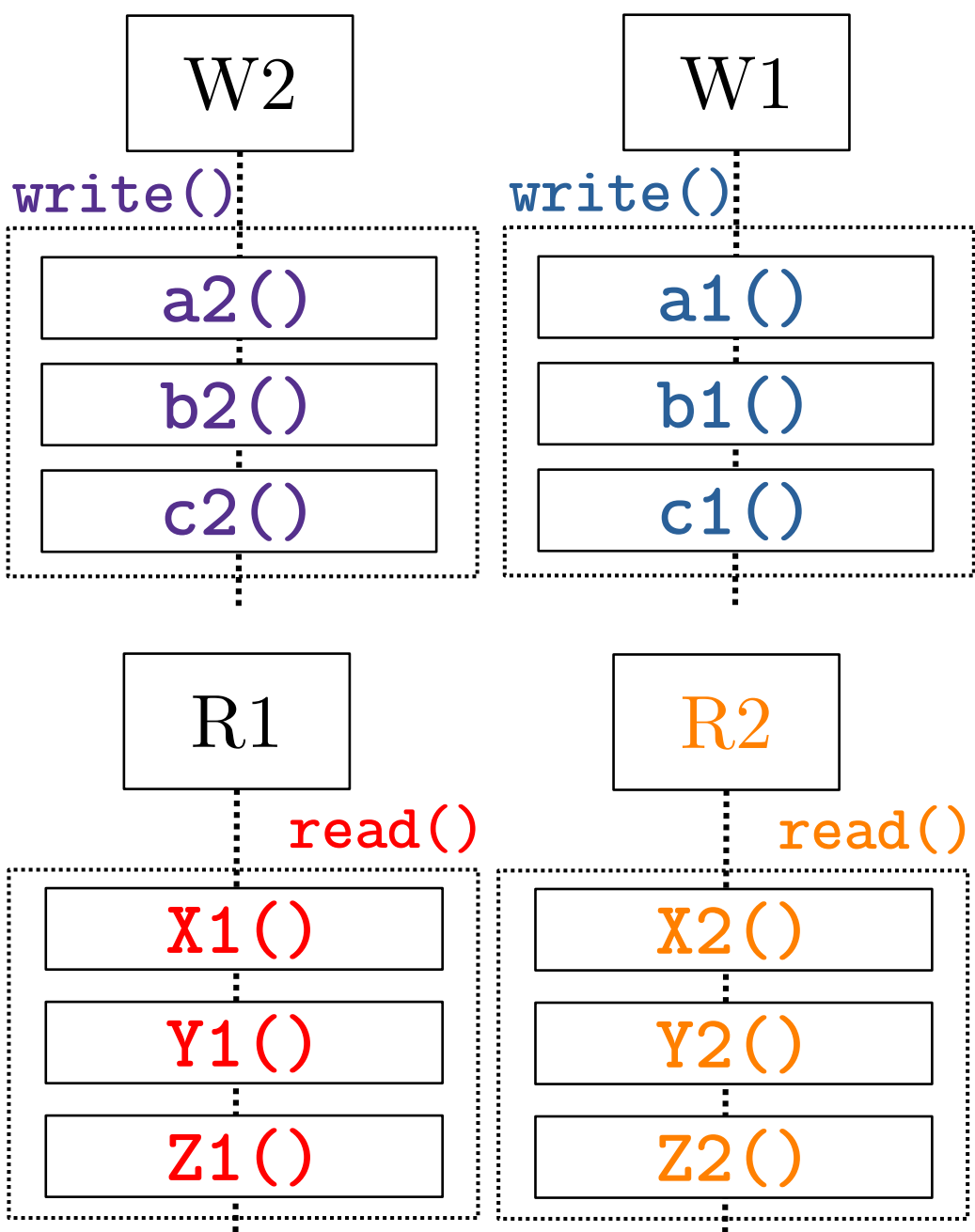
Task/Problem 4: Reads-Writers



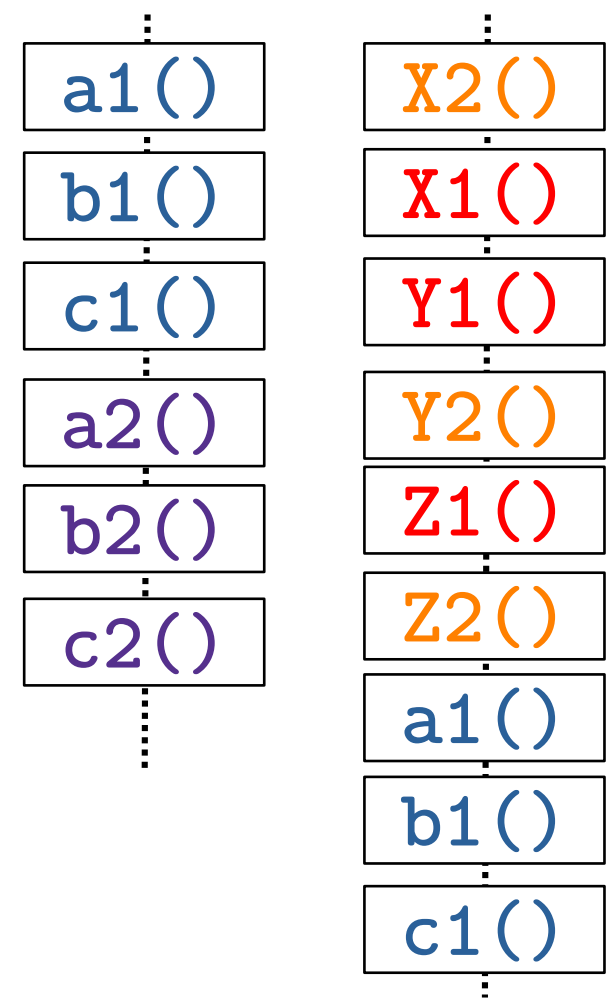
some **INVALID** orders



Task/Problem 4: Reads-Writers

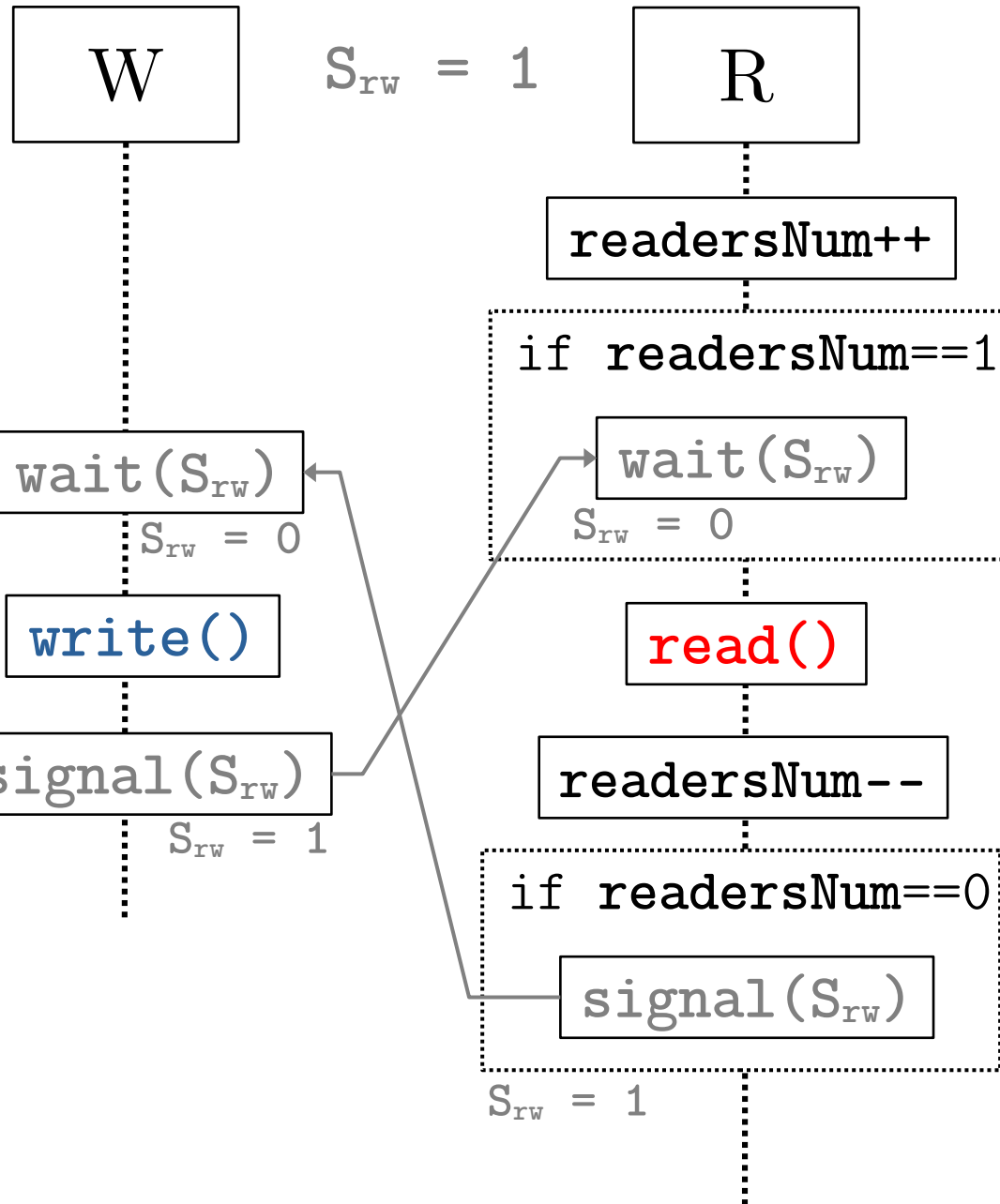


some **VALID** orders



Solution 4: Reads-Writers

readersNo = 0

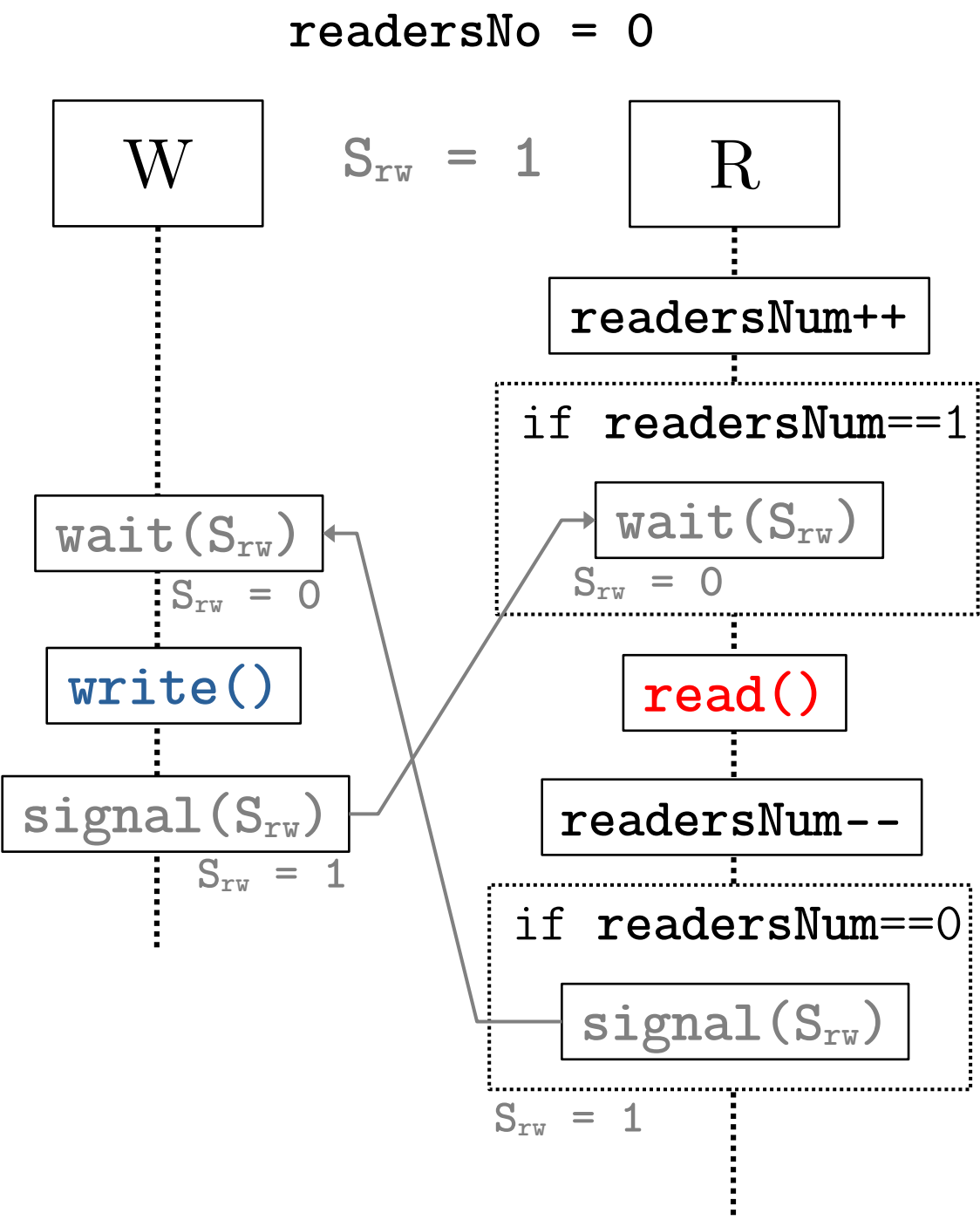


S_{rw} represents the **read-write permit**. Initially, $S_{rw} = 1$.

Writer **W** calls `wait(Srw)` to wait for a **read-write permit** before calling `write()`. After calling `write()`, writer **W** calls `signal(Srw)` to release the **read-write permit**. $S_{rw} = 1$

Reader **R** increments the variable **readersNo**. If **readersNo==1** after being incremented, then Reader **R** is the first reader thread trying to perform the **read()** operation.

Solution 4: Reads-Writers

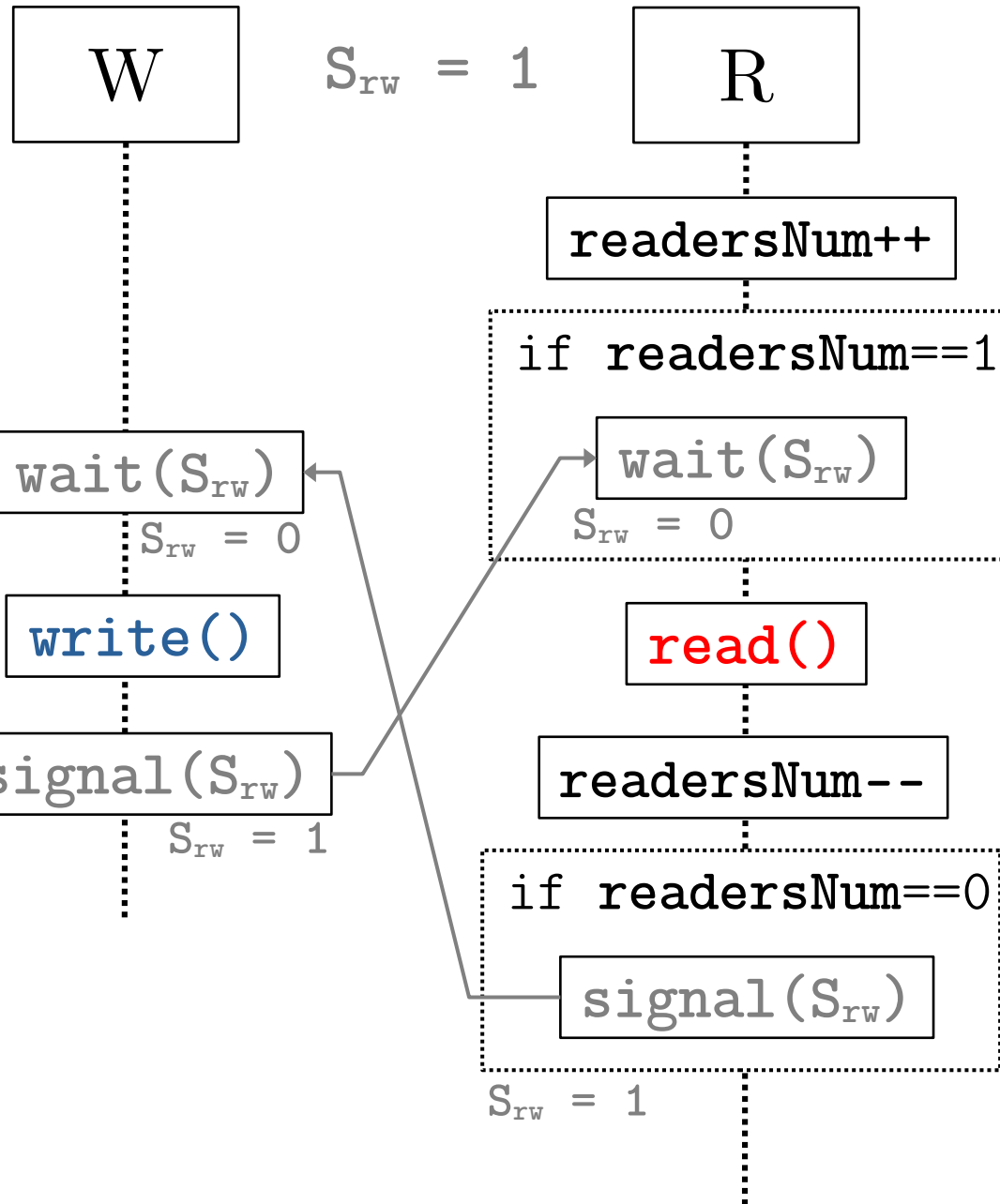


Reader **R** increments the variable `readersNum`. If `readersNum==1` after being incremented, then reader **R** is the first reader thread trying to perform the **read()** operation. If it is the first reader thread, then it will call `wait(S_{rw})` to wait for the **read-write permit**.

If reader **R** is not the first reader (i.e. `readersNum>1`), then it does not need to wait for the **read-write permit** because some reader thread is currently calling **read()** has acquired it previously.

Solution 4: Reads-Writers

readersNo = 0

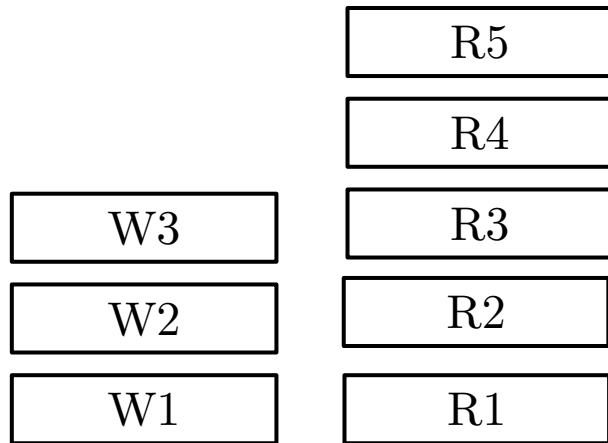


If reader **R** is not the first reader (i.e. `readersNum>1`), then it does not need to wait for the **read-write permit** because some reader thread is currently calling `read()` has acquired it previously.

After the call to `read()`, reader **R** will decrement `readersNum`, and it will release the **read-write permit** if it is the last reader that performed `read()`. i.e. If `readersNum==0`.

Solution 4: Reads-Writers: Lightswitch Design Pattern

Threads waiting for room access



Room for reading/writing

Lights OFF = Free Room

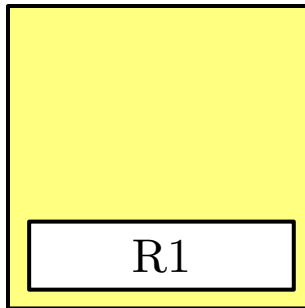
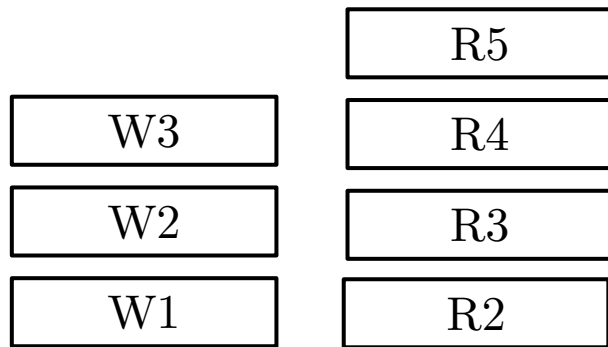
Semaphore $S_{rw}=1$

Analogy:

- The room is for reading/writing.
- Free Room – Lights OFF
- Room in Use – Lights ON
- Semaphore $S_{rw} = 1$ means a free room (lights OFF)
- Semaphore $S_{rw} = 0$ means a room in use (lights ON)
- Threads want to enter the room in order to **read()** or **write()**.

Solution 4: Reads-Writers: Lightswitch Design Pattern

Threads waiting for room access



Room for reading/writing

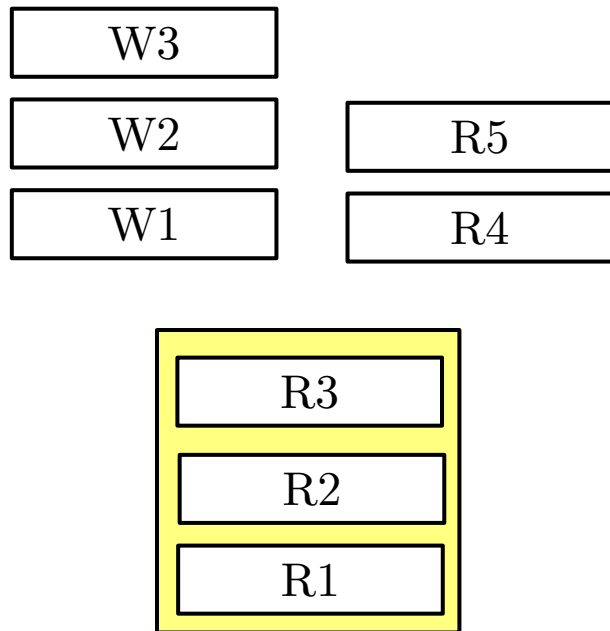
Lights ON = Room in Use

Semaphore $S_{rw}=0$

- R1 enters the room and turns ON the light.
- $S_{rw}=0 \rightarrow$ lights ON \rightarrow Room in Use
- When a reader is already in the room, other readers can enter the room and perform **read()**.

Solution 4: Reads-Writers: Lightswitch Design Pattern

Threads waiting for room access



Room for reading/writing

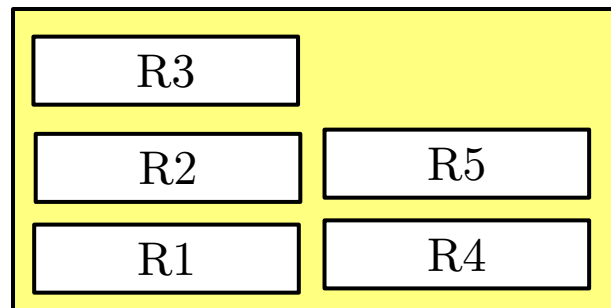
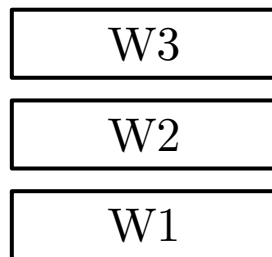
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Room for reading/writing

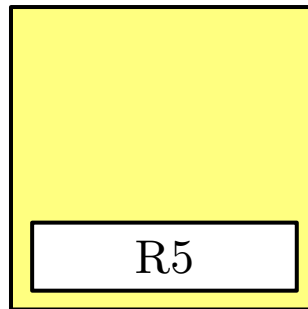
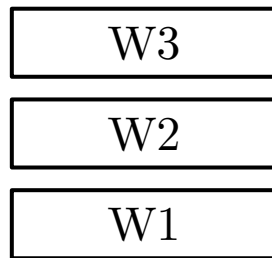
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Room for reading/writing

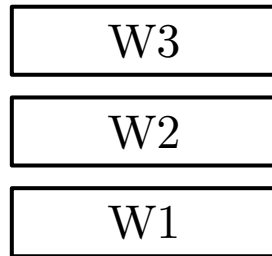
Lights ON = Room in Use

Semaphore $S_{rw}=0$

- The last reader in the room will be responsible for turning the light OFF.
- **lights OFF** $\rightarrow S_{rw}=0 \rightarrow$
Free Room

Solution 4: Reads-Writers: Lightswitch Design Pattern

Threads waiting for room access



Room for reading/writing

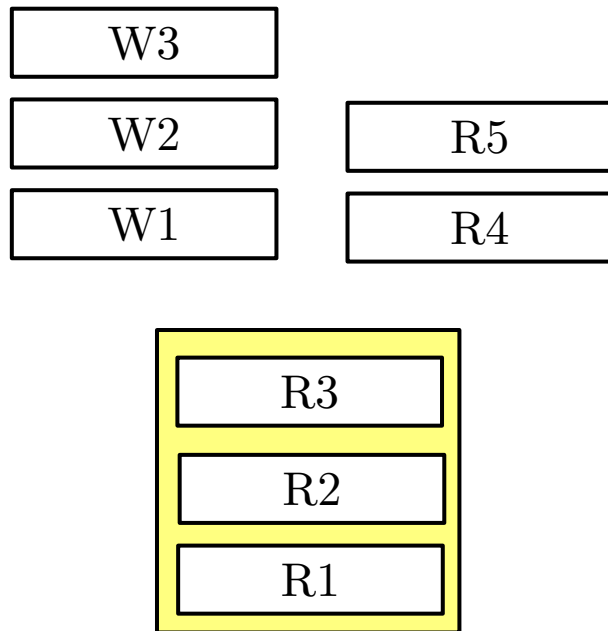
Lights OFF = Free Room

Semaphore $S_{rw}=1$

- The last reader in the room will be responsible for turning the light OFF.
- **lights OFF** $\rightarrow S_{rw}=0 \rightarrow$
Free Room

Solution 4: Reads-Writers: Lightswitch Design Pattern

Threads waiting for room access



Room for reading/writing

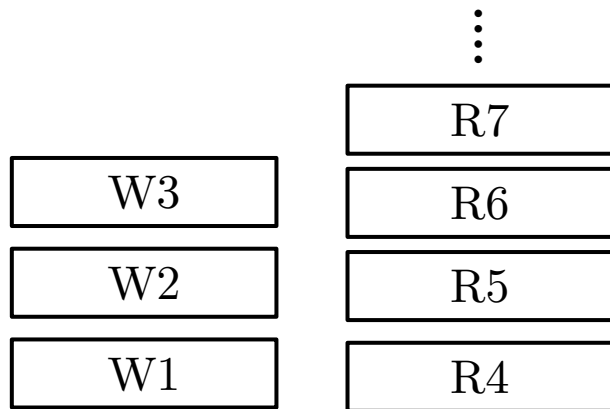
Lights ON = Room in Use

Semaphore $S_{rw}=0$

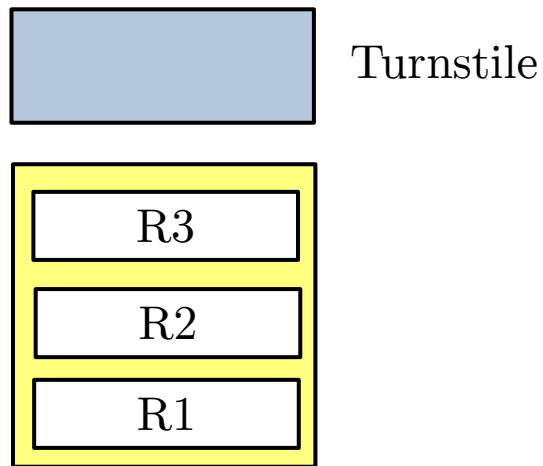
- **ISSUE:** If there is a continuous stream of readers while the room is occupied by at least one reader, the writers might '*starve*'.

Solution 4: Reads-Writers: Turnstile Design Pattern

Threads waiting for room access



- **ISSUE:** If there is a continuous stream of readers while the room is occupied by at least one reader, the writers might *'starve'*.



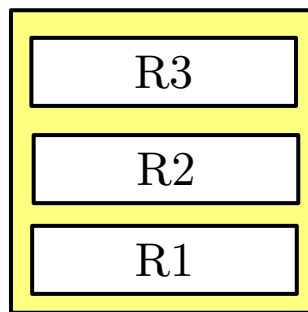
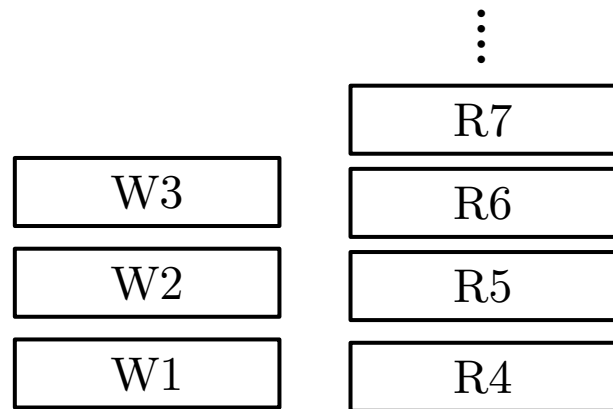
Lights ON = Room in Use
Semaphore $S_{rw}=0$

Turnstiles



Solution 4: Reads-Writers: Turnstile Design Pattern

Threads waiting for room access



Room for reading/writing

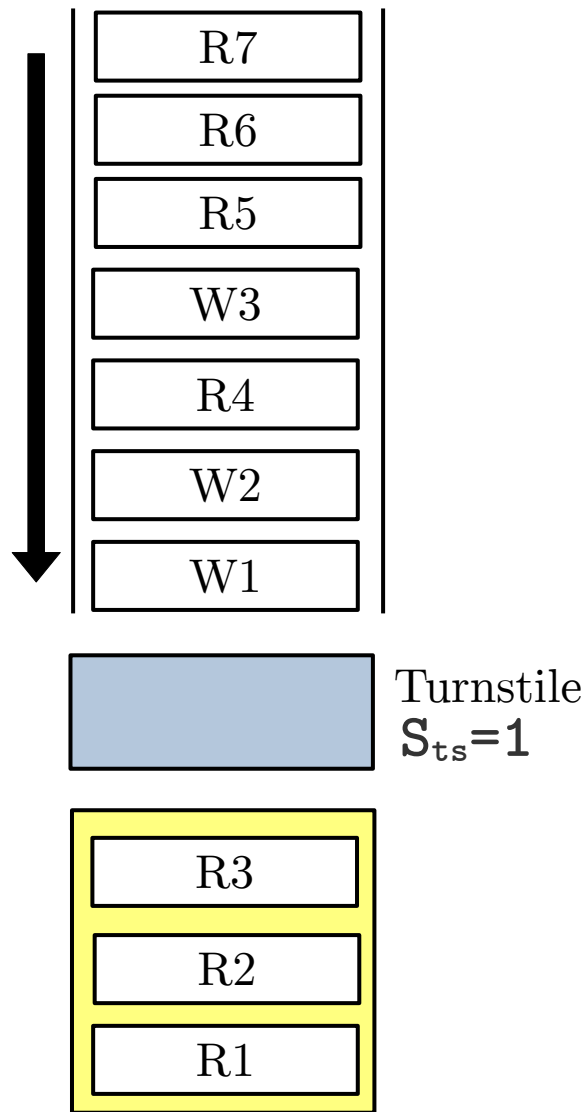
Lights ON = Room in Use

Semaphore $S_{rw}=0$

- **ISSUE:** If there is a continuous stream of readers while the room is occupied by at least one reader, the writers might '*starve*'.
- All threads should try to access the turnstile first before trying to enter the room.
- Only one thread at a time can access the turnstile.
- S_{ts} is the semaphore that hold that one *permit* to access the turnstile. Initially, $S_{ts}=1$.

Solution 4: Reads-Writers: Turnstile Design Pattern

Queue to Semaphore S_{ts}

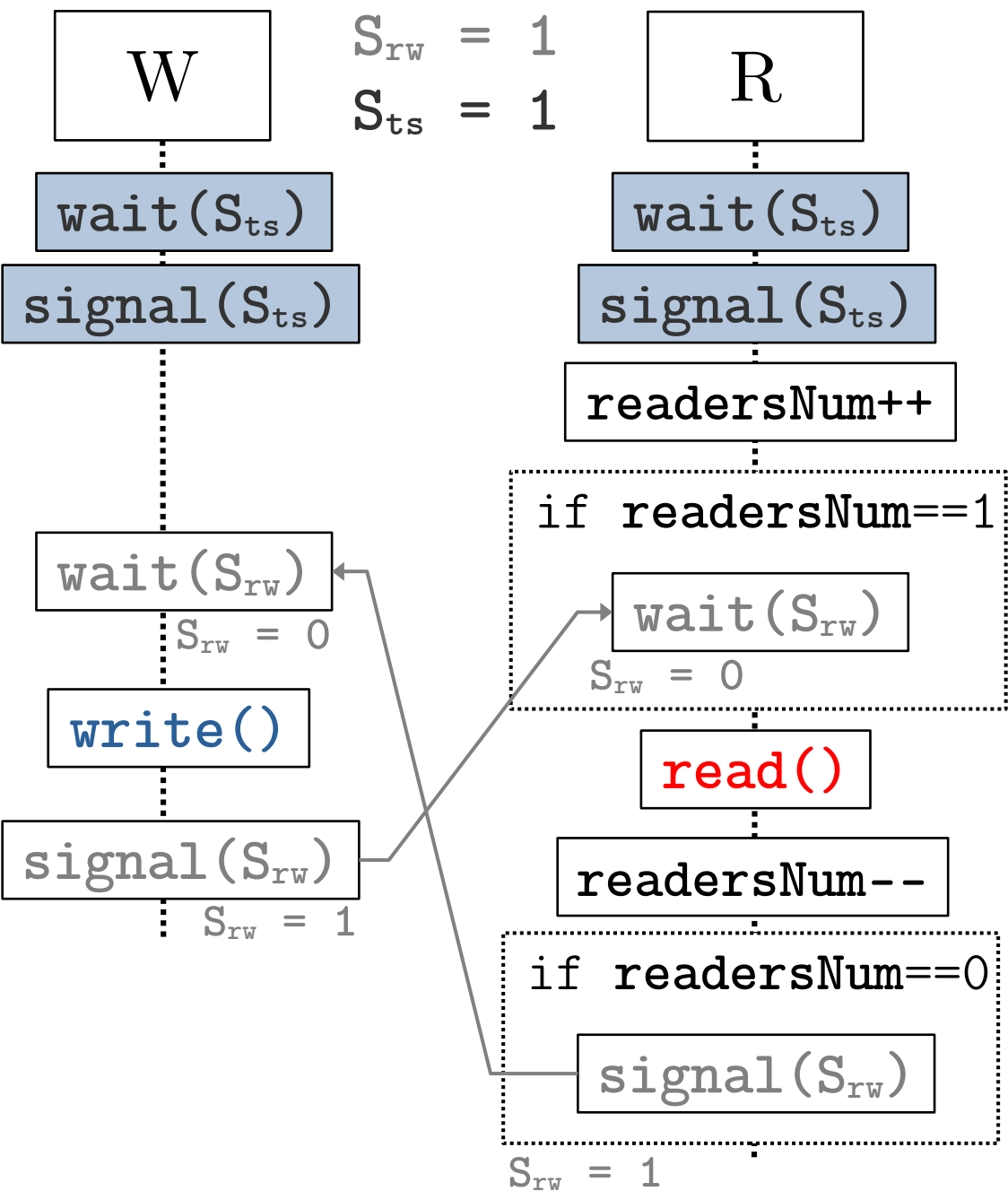


Room for reading/writing
Lights ON = Room in Use
Semaphore $S_{rw}=0$

- The turnstile mechanism forces all threads to form a line because all of the thread need to acquire the permit to access the turnstile which means all threads will call `wait(S_{ts})`.
- Without the turnstile, if the room is in use by a reader (lights ON), other readers do form a queue in order to access the room and call `read()`. A reader can immediate use to room and call `read()` concurrently with other readers.

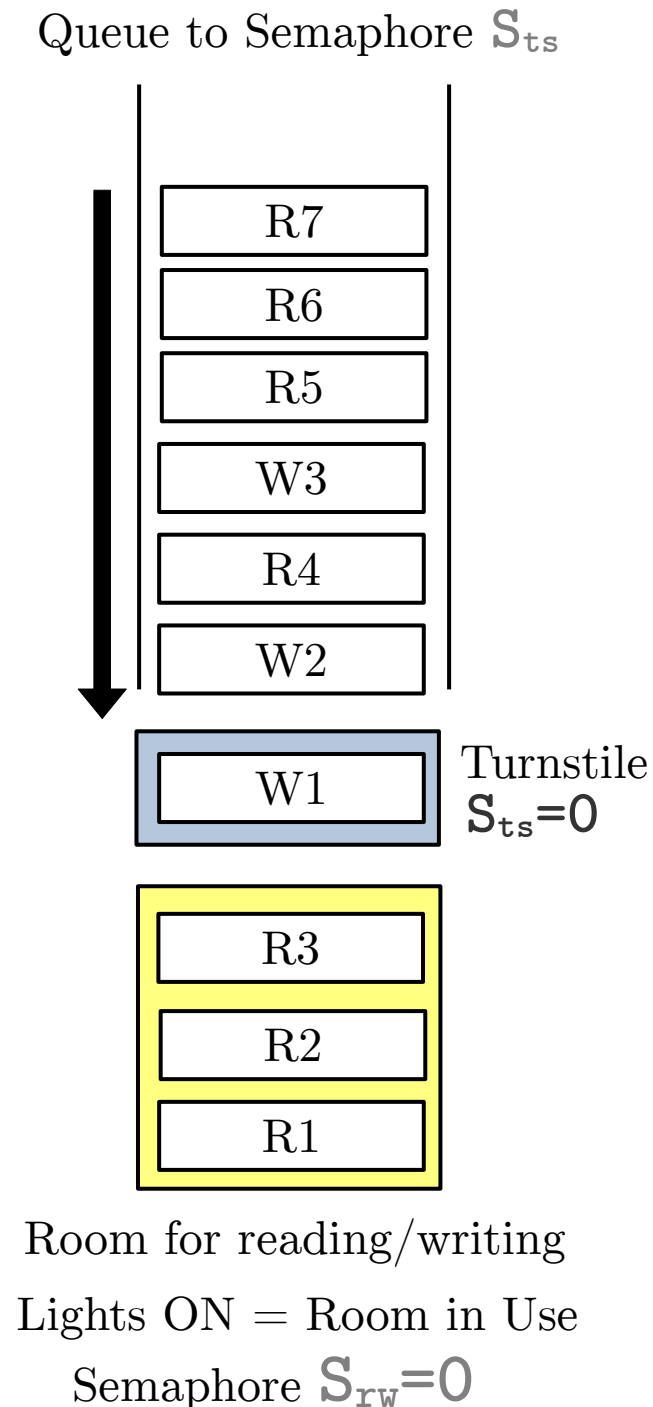
Solution 4: Reads-Writers: Turnstile Design Pattern

readersNo = 0



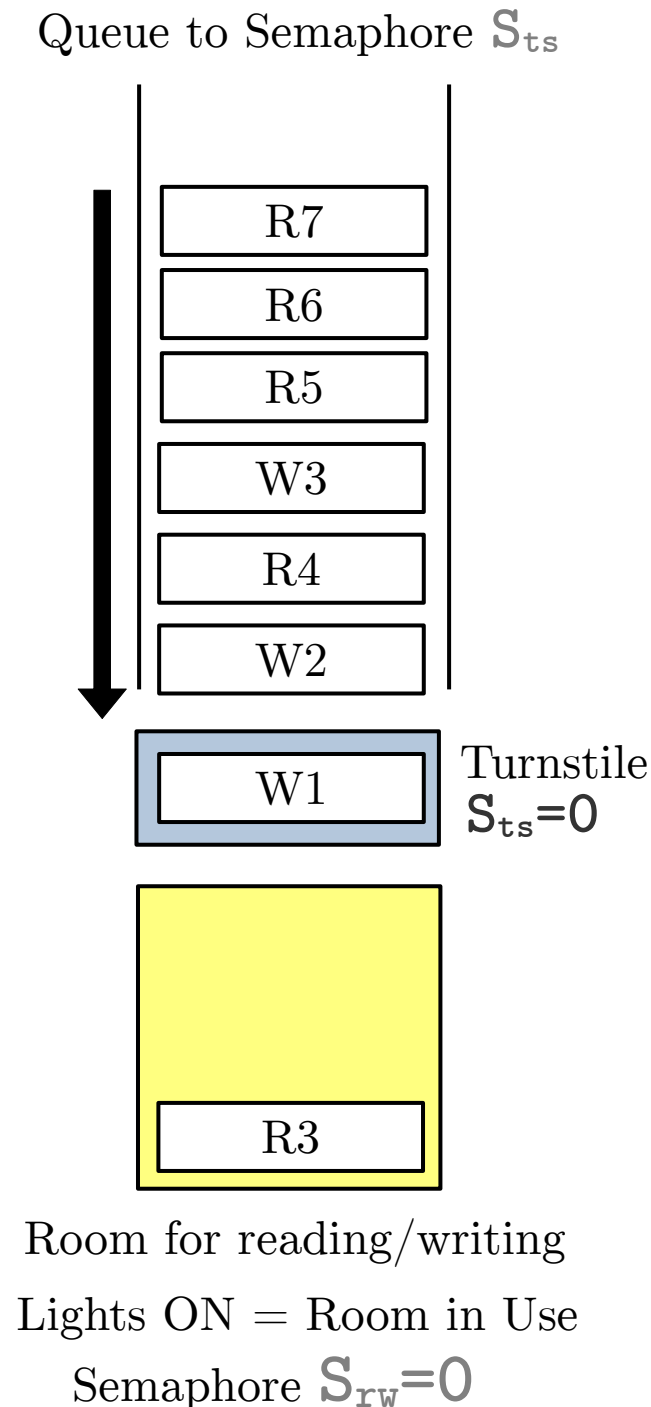
All threads now needs to go through the turnstile by calling `wait(S_{ts})` in order to ask for turnstile access permit then `signal(S_{ts})` is called afterwards.

Solution 4: Reads-Writers: Turnstile Design Pattern



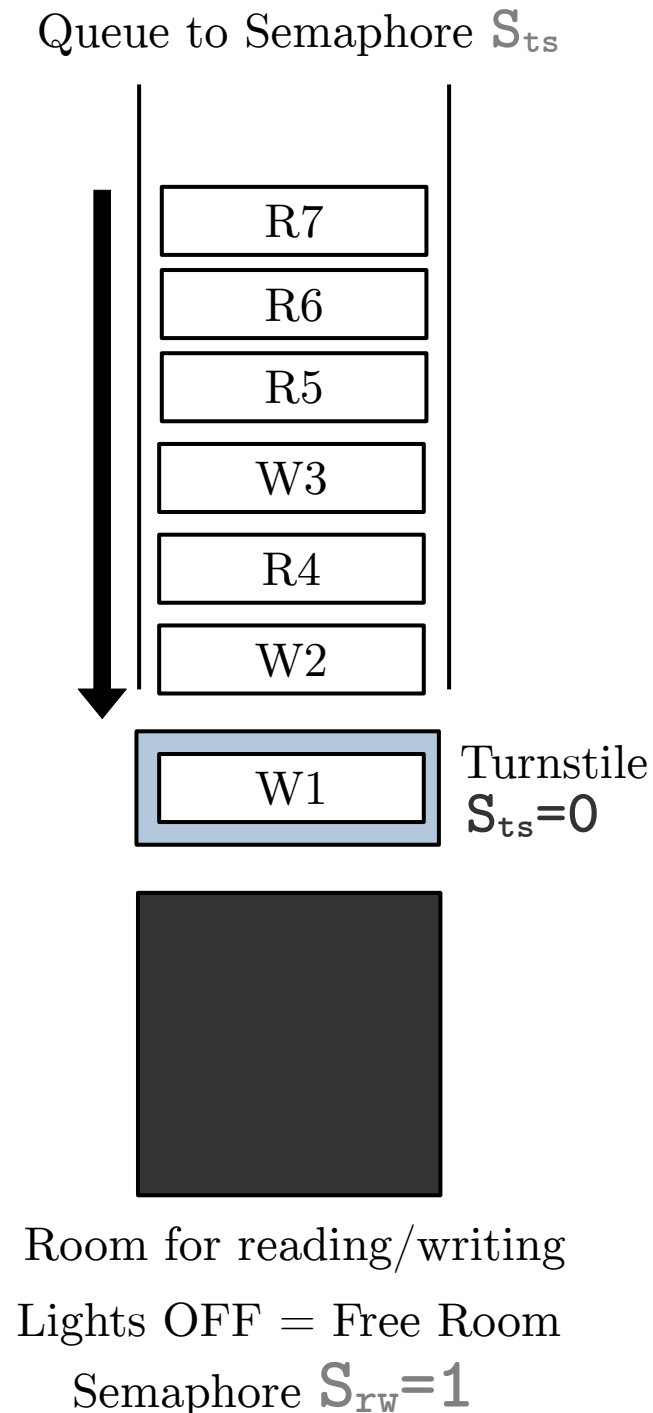
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Synchronization Task/Problem 5: **Dining Philosophers**

[Problem & Solution Descriptions]

Task/Problem 5: Dining Philosophers

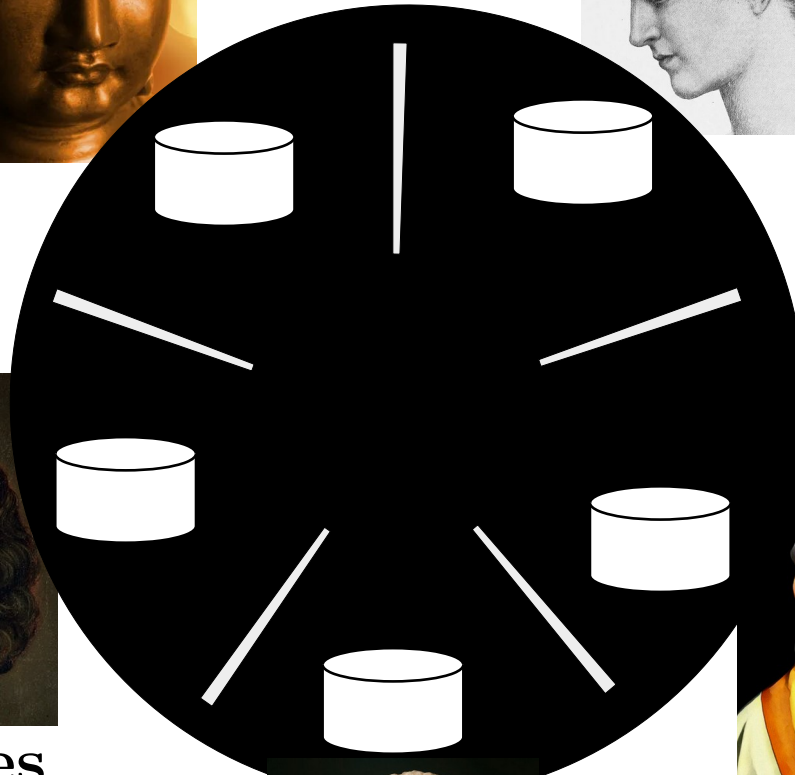
Siddhartha



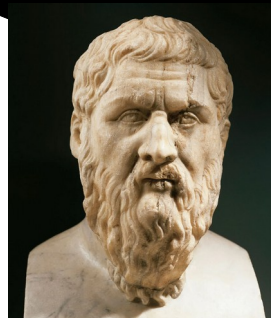
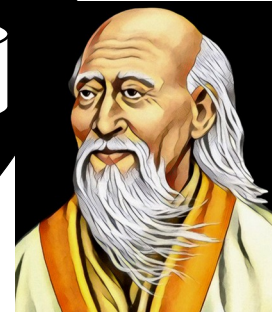
Hypatia



Descartes

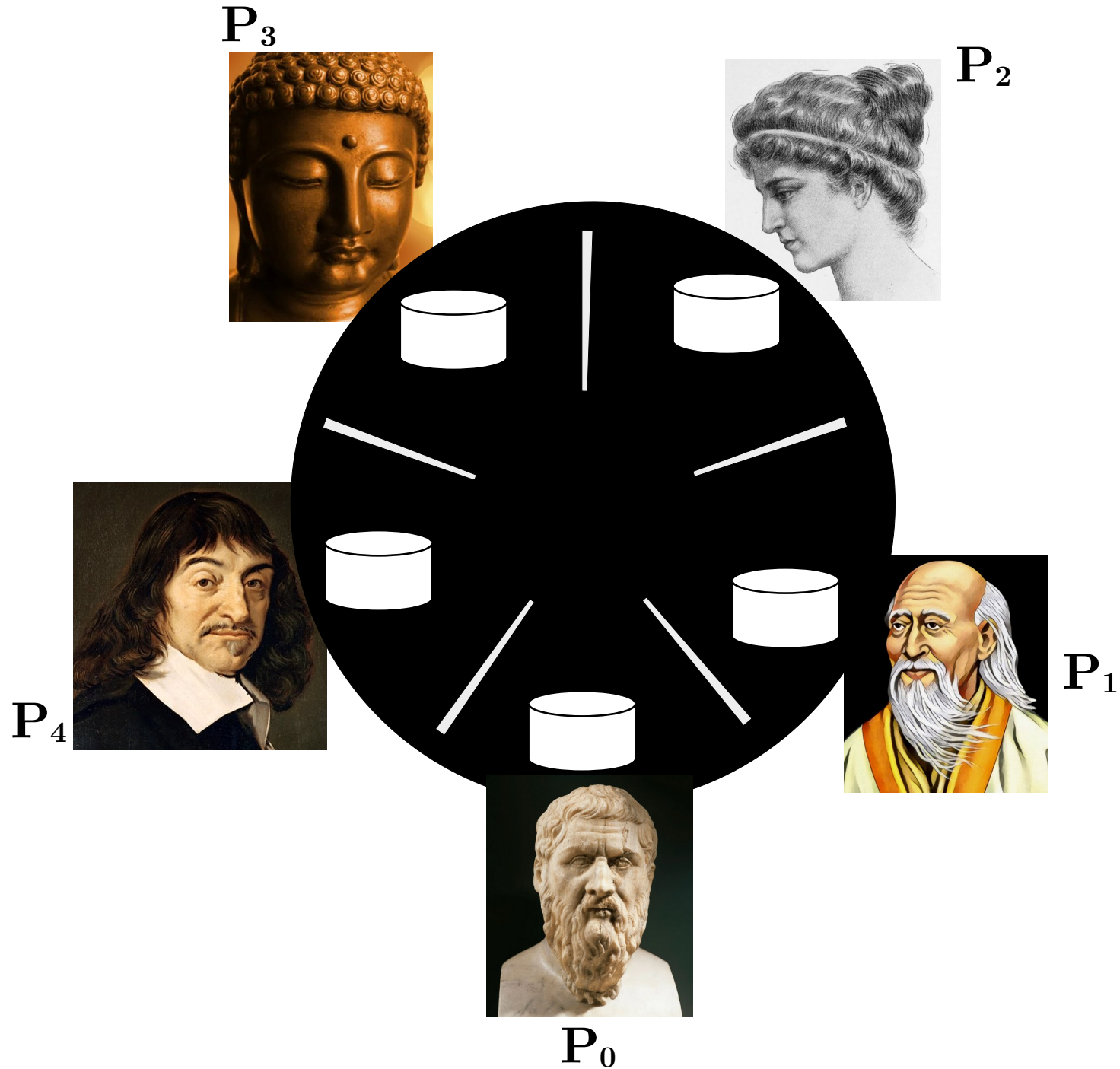


Lao Tzu

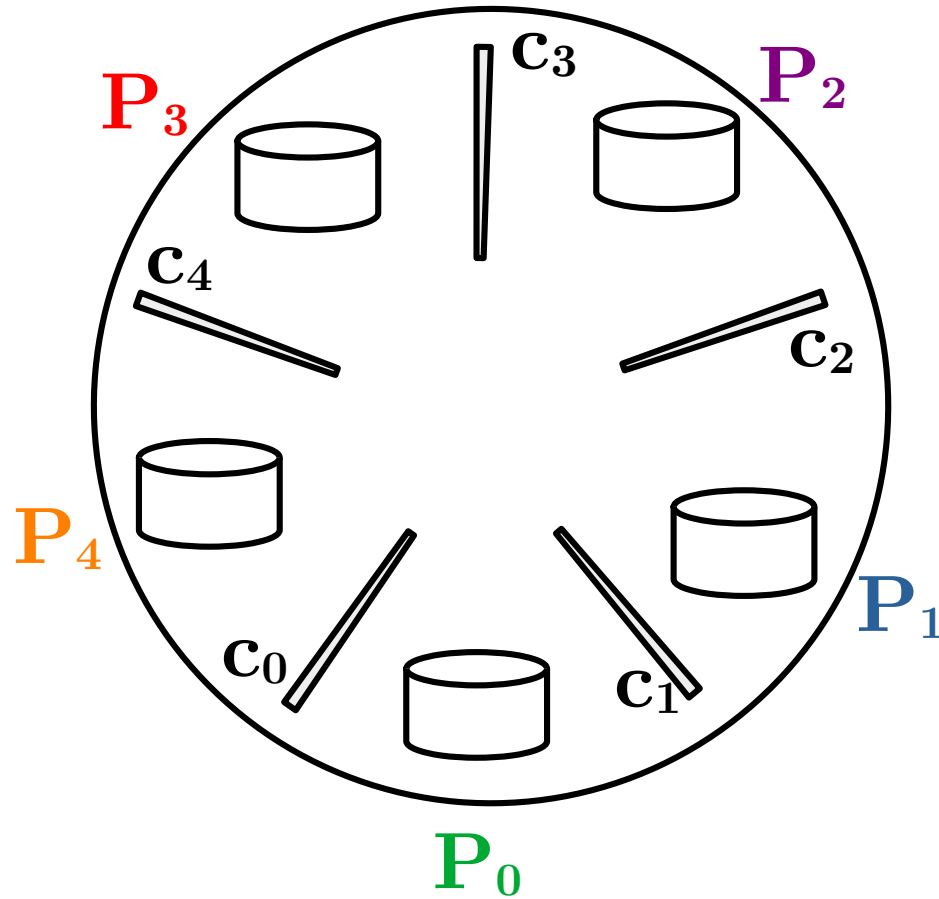


Plato

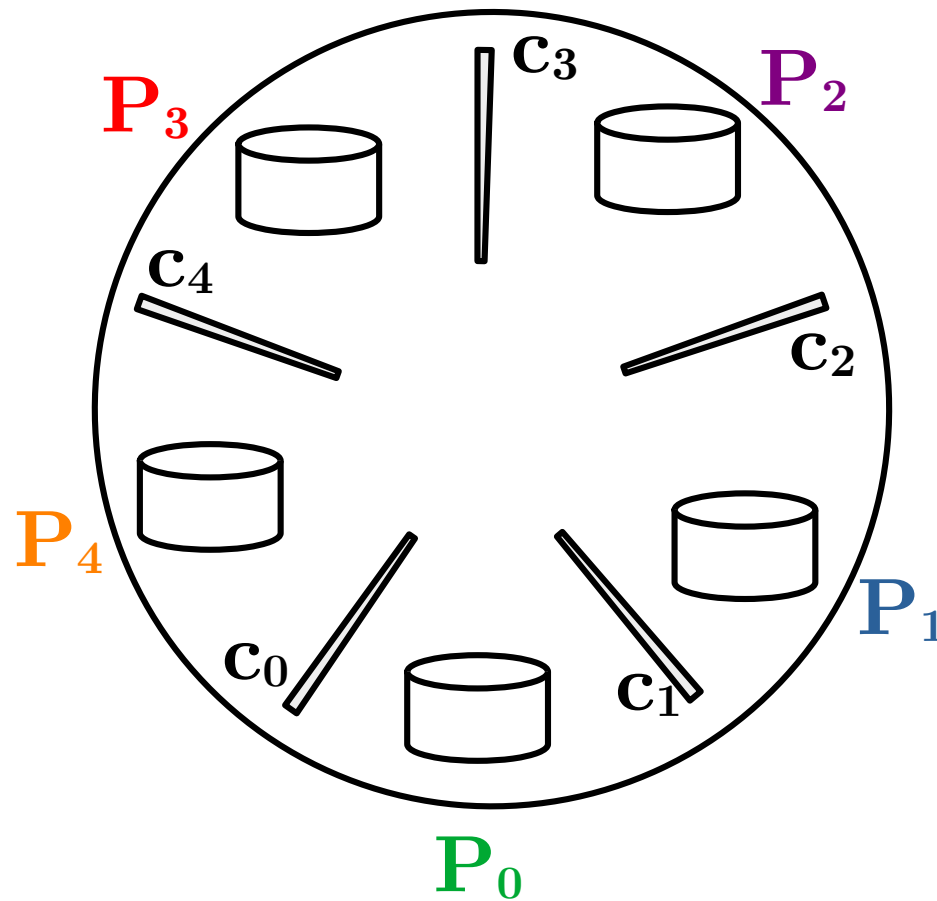
Task/Problem 5: Dining Philosophers



Task/Problem 5: Dining Philosophers



Task/Problem 5: Dining Philosophers



P_i needs c_i and c_{i+1} or more accurately

$$c_{(i+1)\%5}$$

Constraint: Each philosopher needs two chopsticks (left & right) to eat.

P_0 needs c_0 and c_1 ,

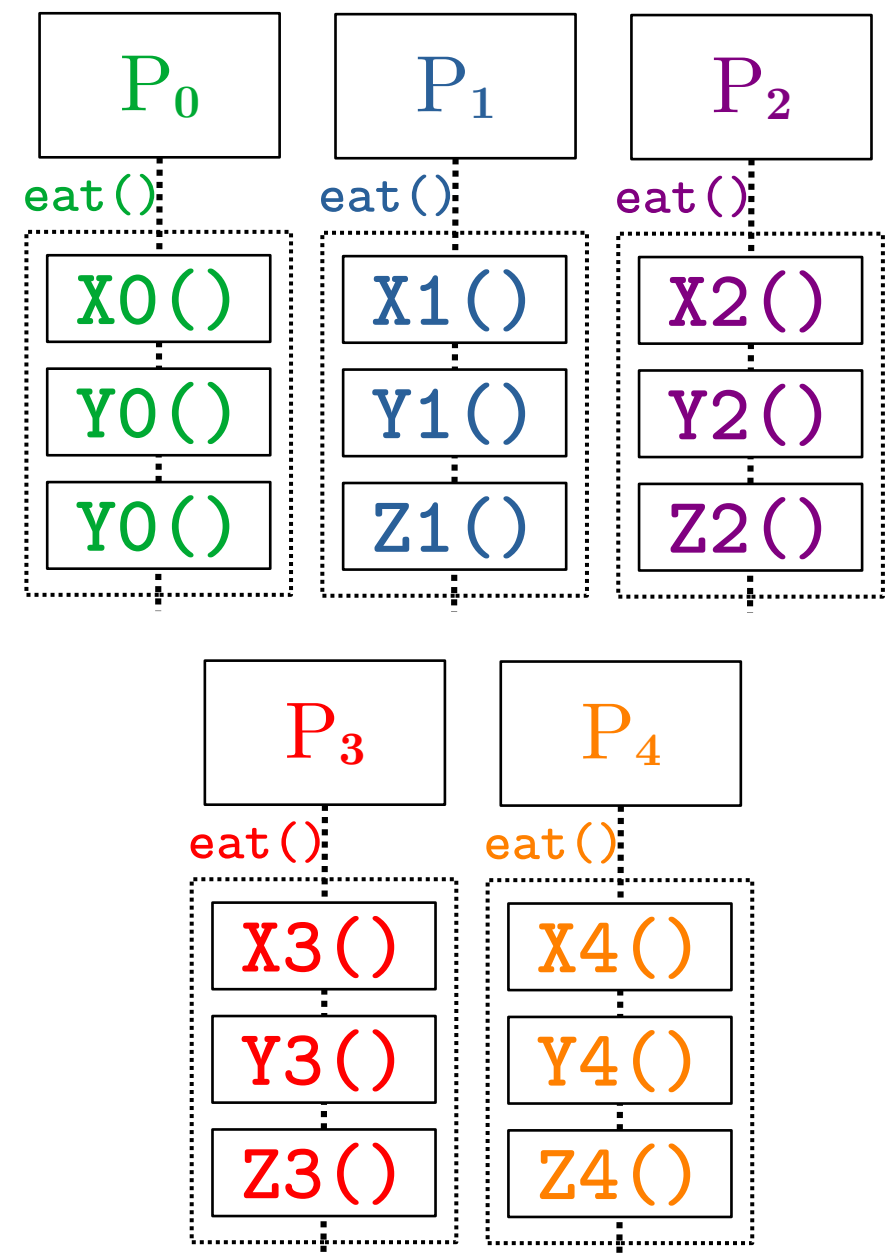
P_1 needs c_1 and c_2 ,

P_2 needs c_2 and c_3 ,

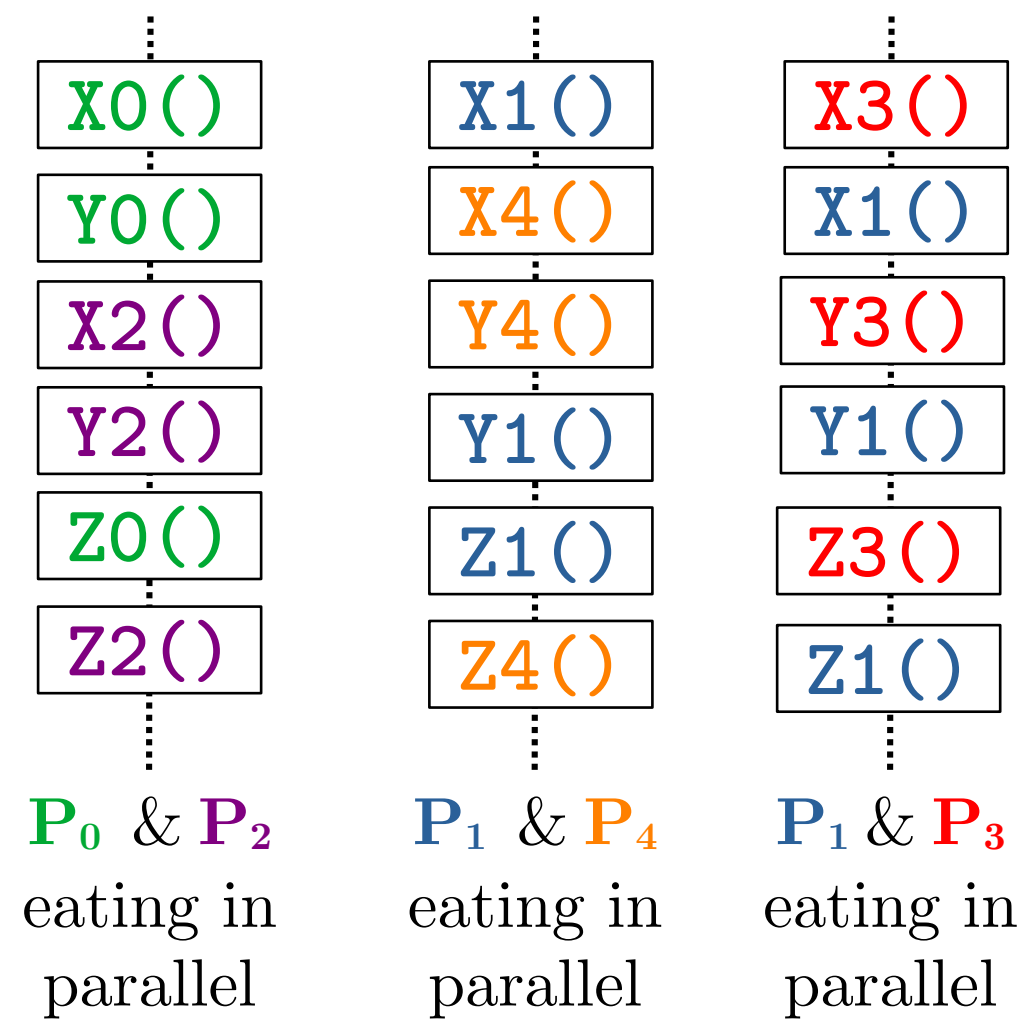
P_3 needs c_3 and c_4 ,

P_4 needs c_4 and c_0 ,

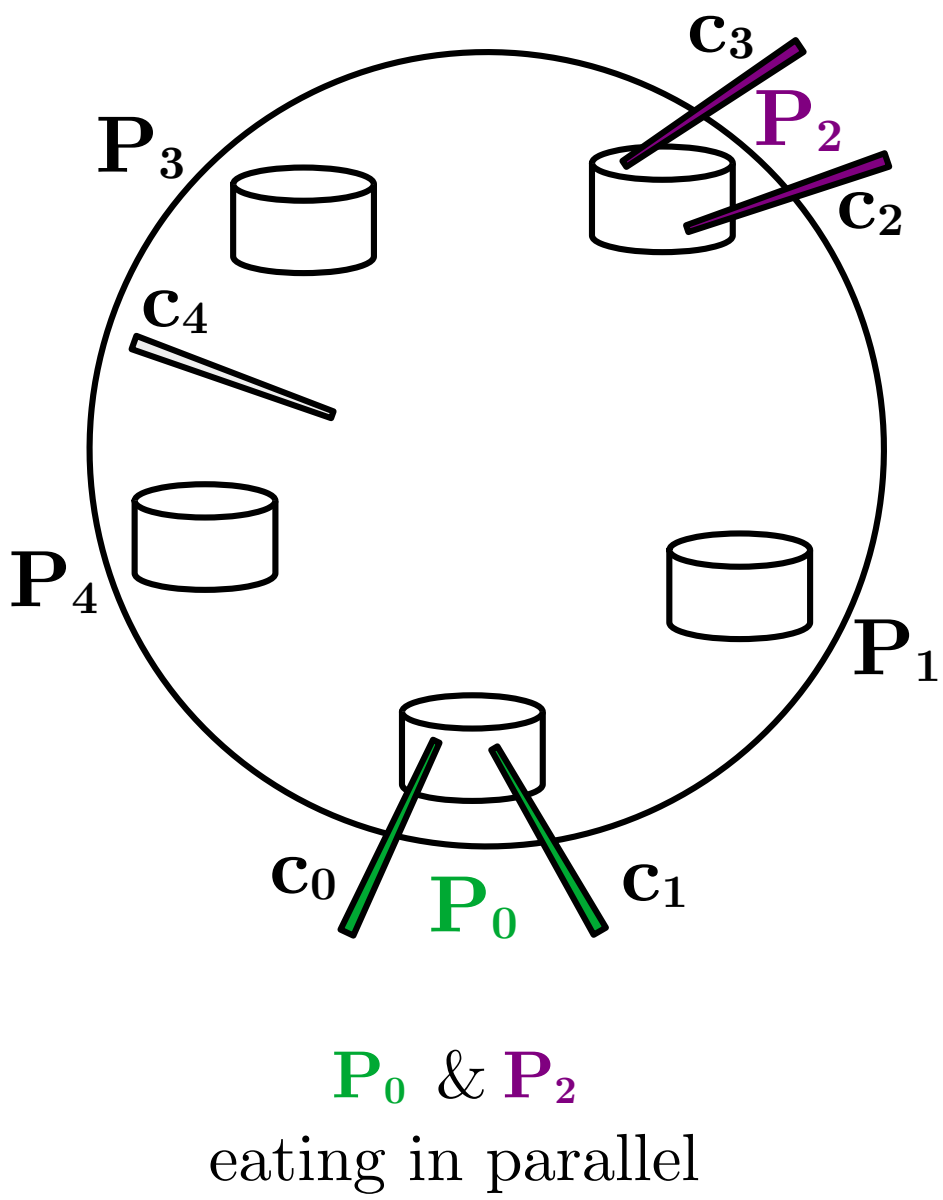
Task/Problem 5: Dining Philosophers



some **VALID** orders



Task/Problem 5: Dining Philosophers



some **VALID** orders

- $X0()$
- $Y0()$
- $X2()$
- $Y2()$
- $Z0()$
- $Z2()$

P_0 & P_2
eating in
parallel

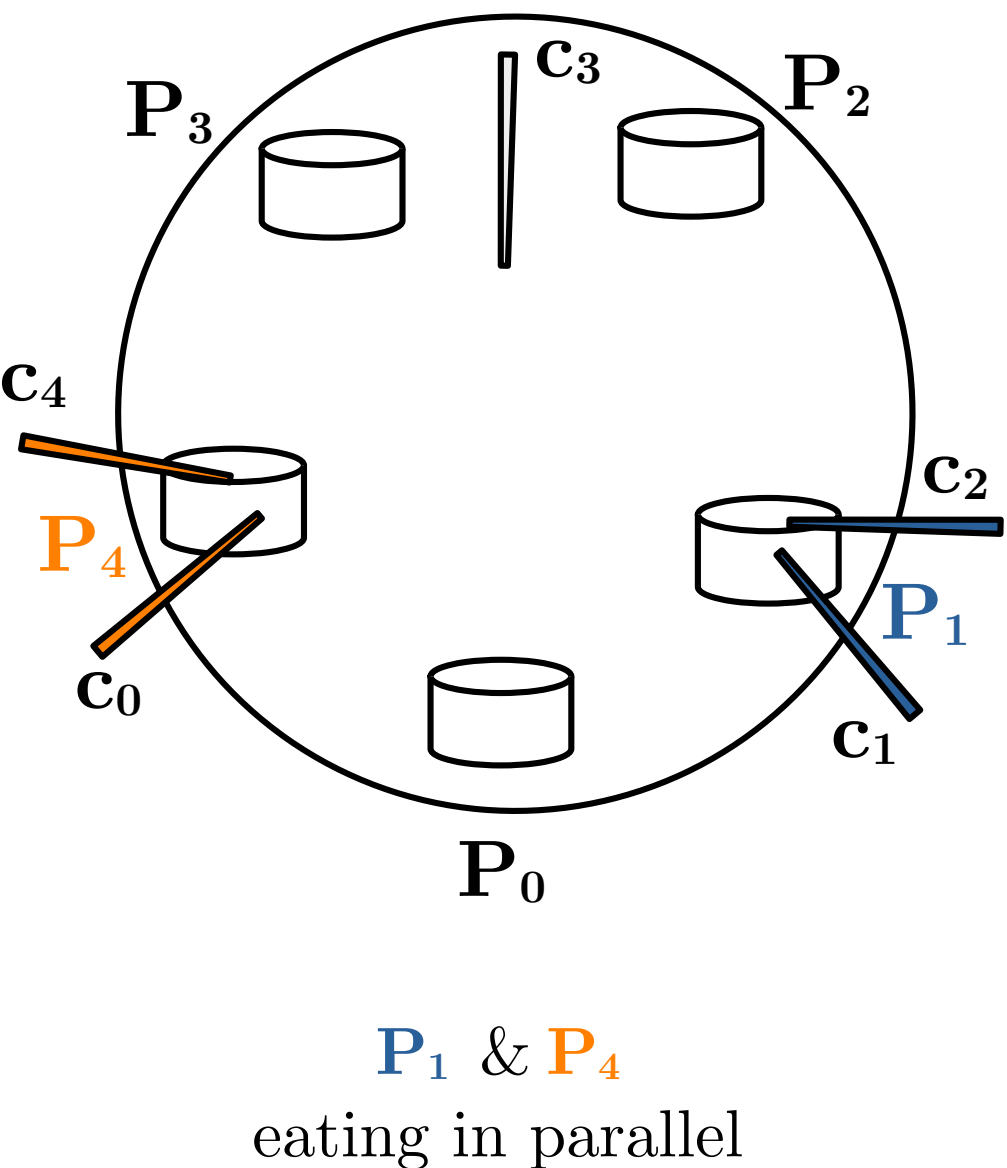
- $X1()$
- $X4()$
- $Y4()$
- $Y1()$
- $Z1()$
- $Z4()$

P_1 & P_4
eating in
parallel

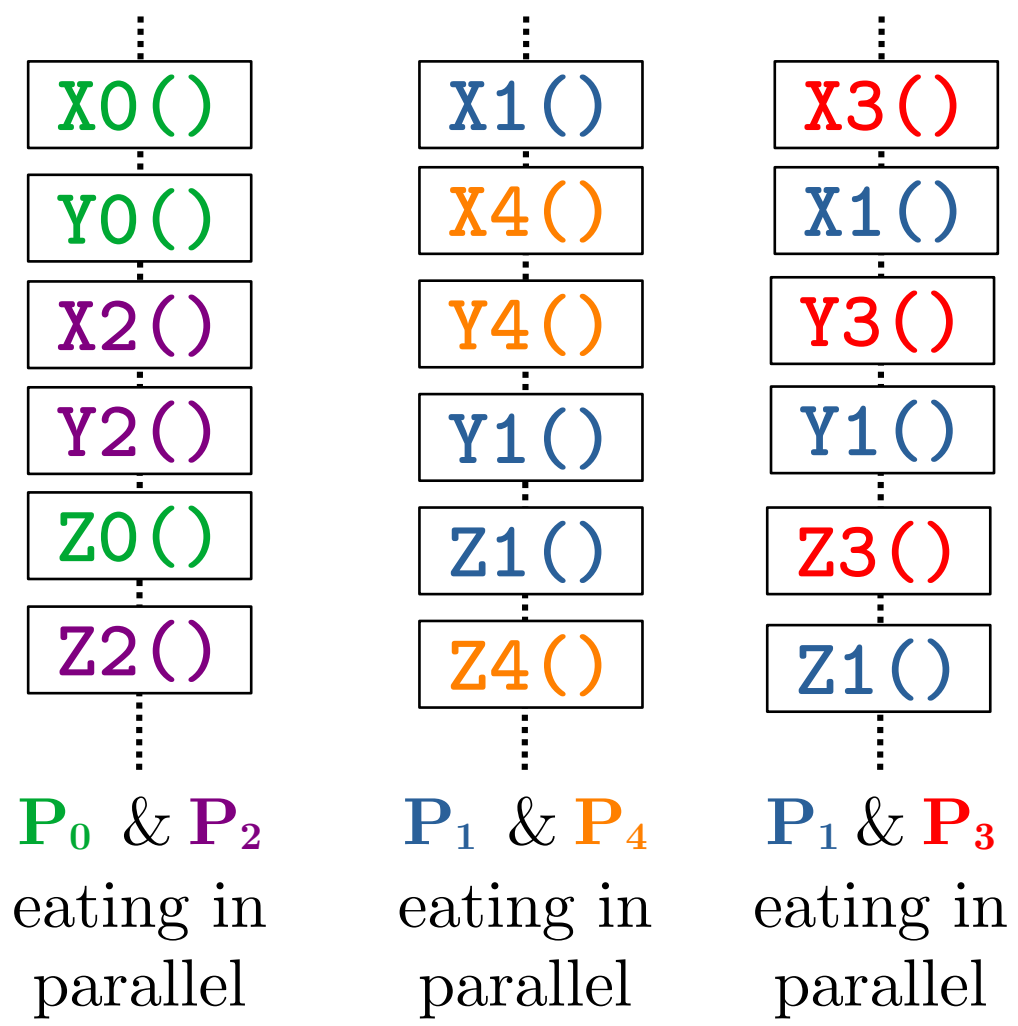
- $X3()$
- $X1()$
- $Y3()$
- $Y1()$
- $Z3()$
- $Z1()$

P_1 & P_3
eating in
parallel

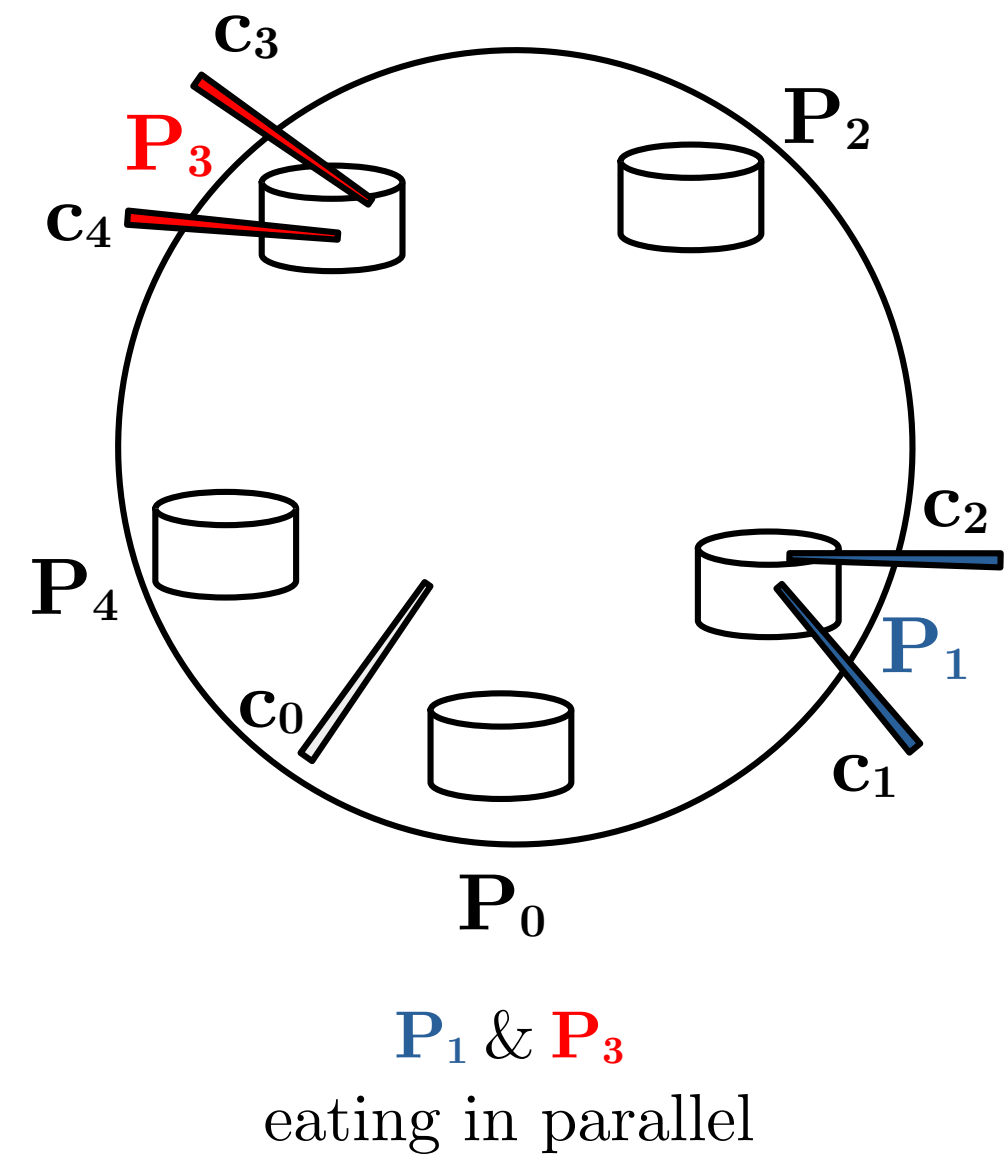
Task/Problem 5: Dining Philosophers



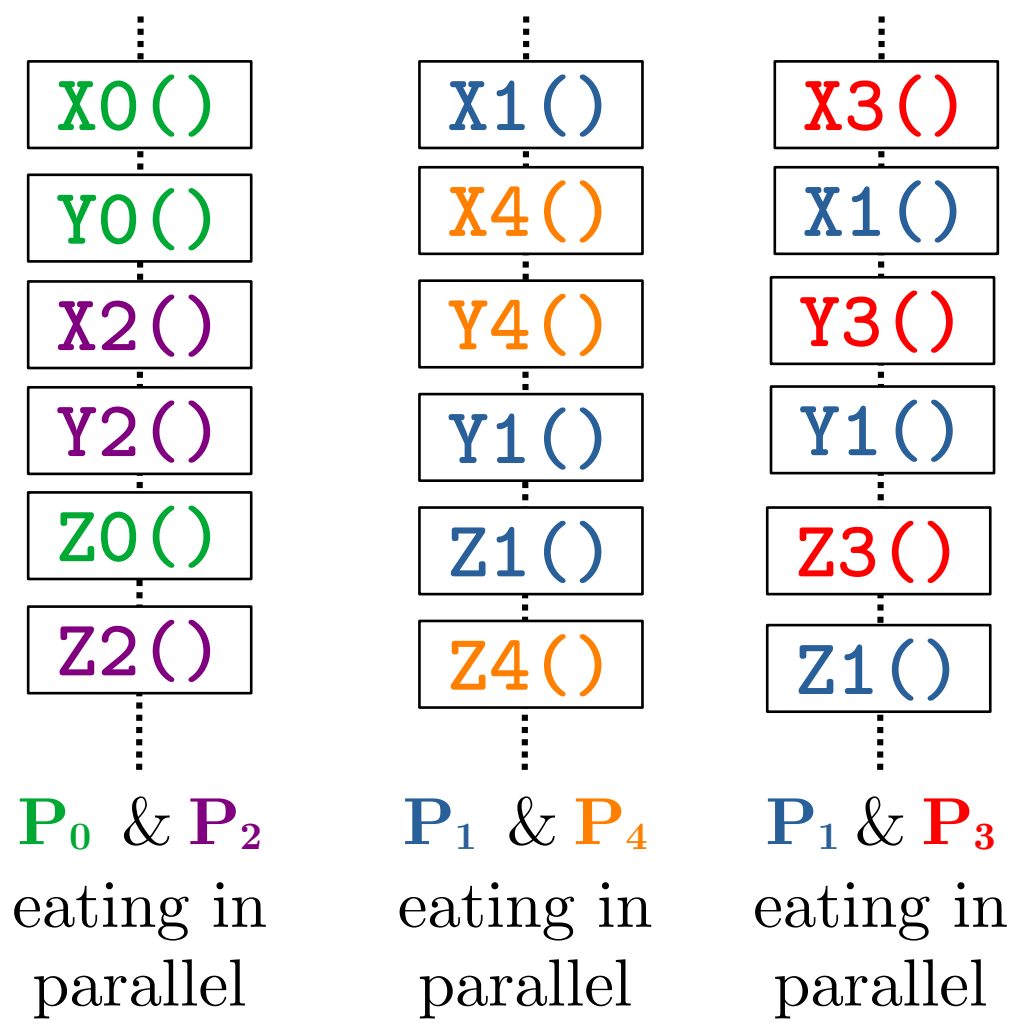
some **VALID** orders



Task/Problem 5: Dining Philosophers

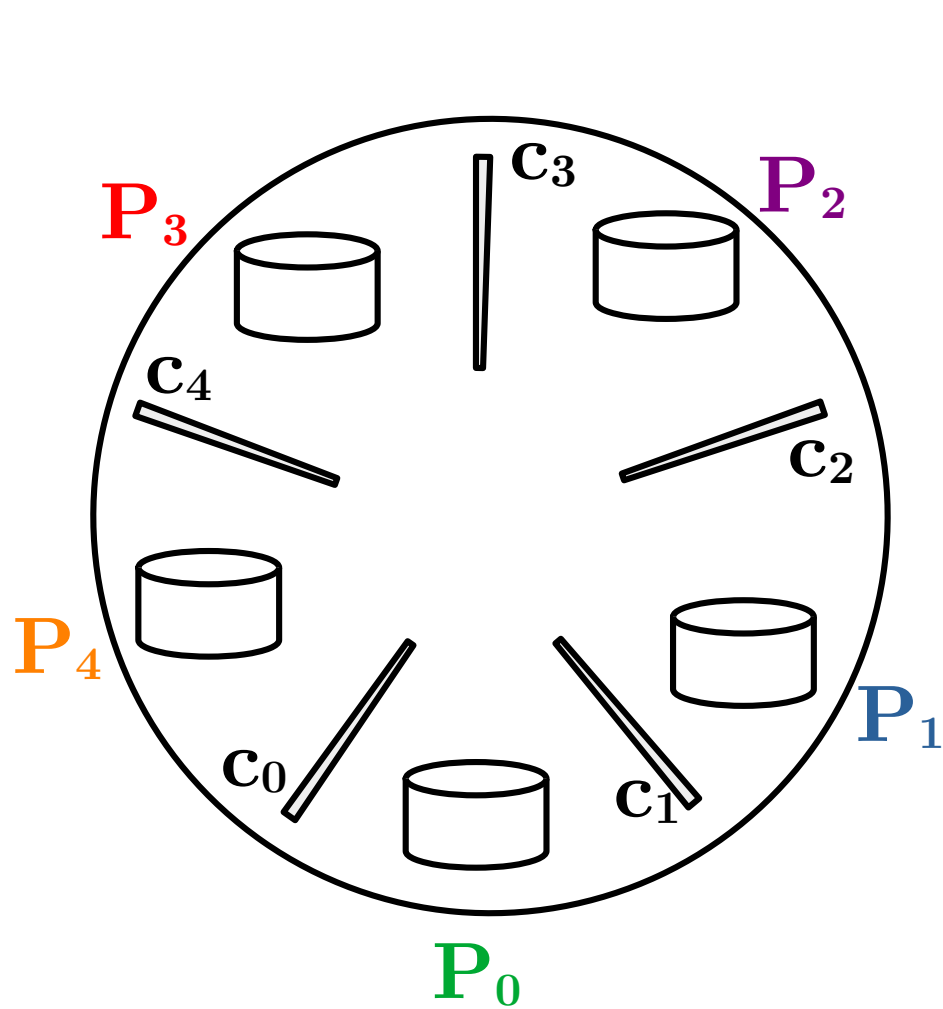


some **VALID** orders



Task/Problem 5: Dining Philosophers

some **INVALID** orders



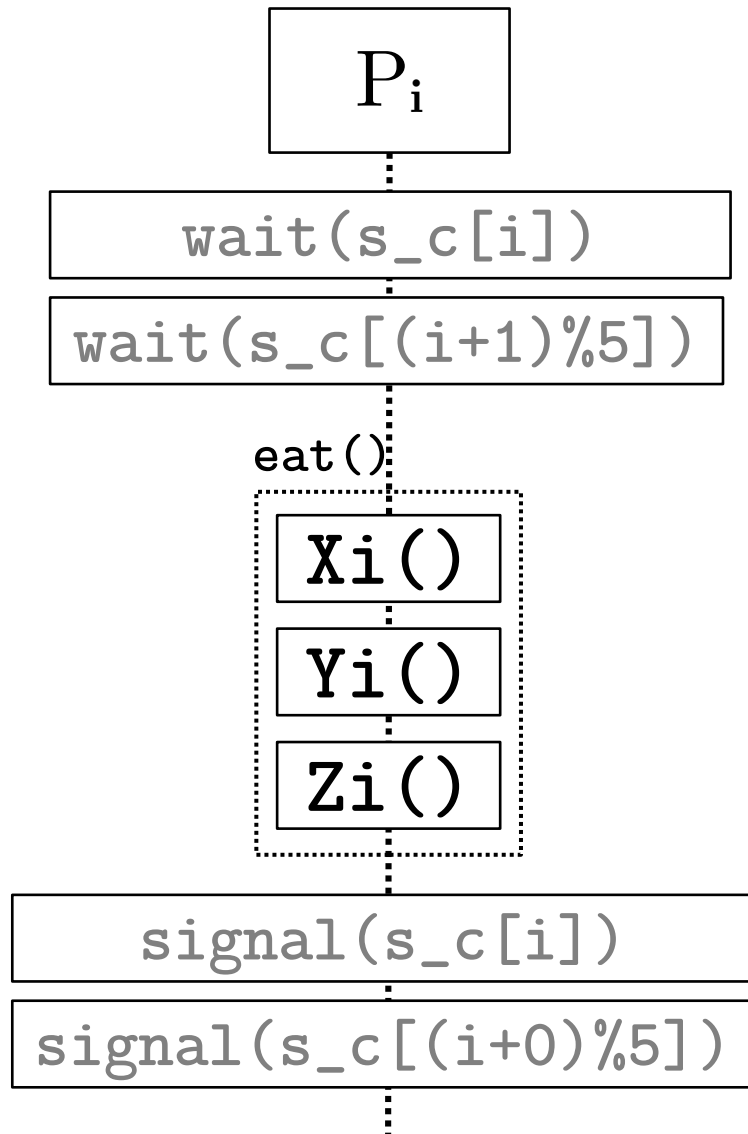
X0()
Y0()
X1()
Y1()
Z0()
Z1()
P0 & P1
eating in
parallel

X2()
Y2()
X3()
Y3()
Z3()
Z2()
P2 & P3
eating in
parallel

X4()
Y4()
X1()
X2()
Y2()
Y1()
Z1()
Z4()
Z2()
P1, P2, P4
eating in
parallel

Task/Problem 5: Dining Philosophers

`s_c[5] = {1, 1, 1, 1, 1}`

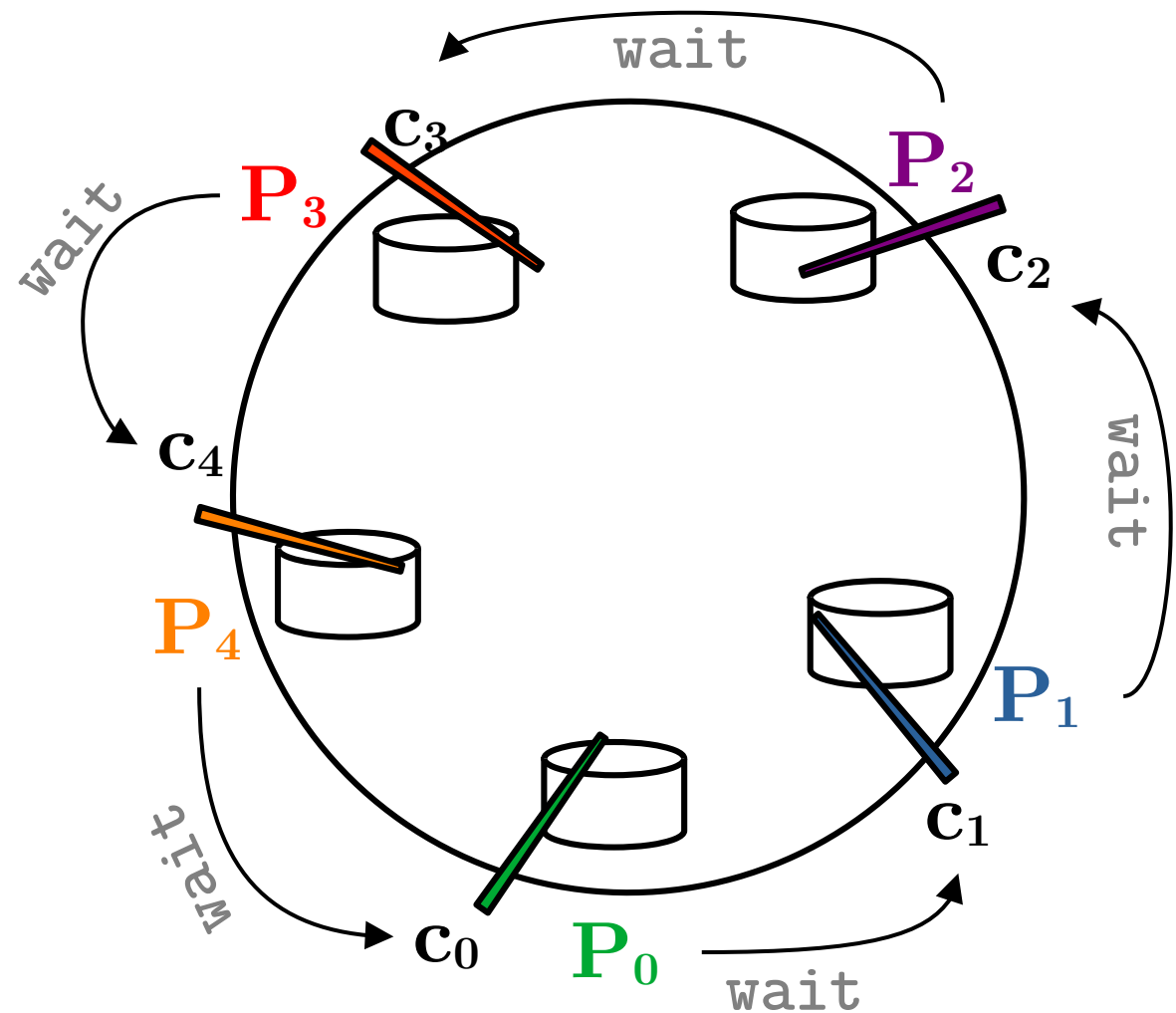
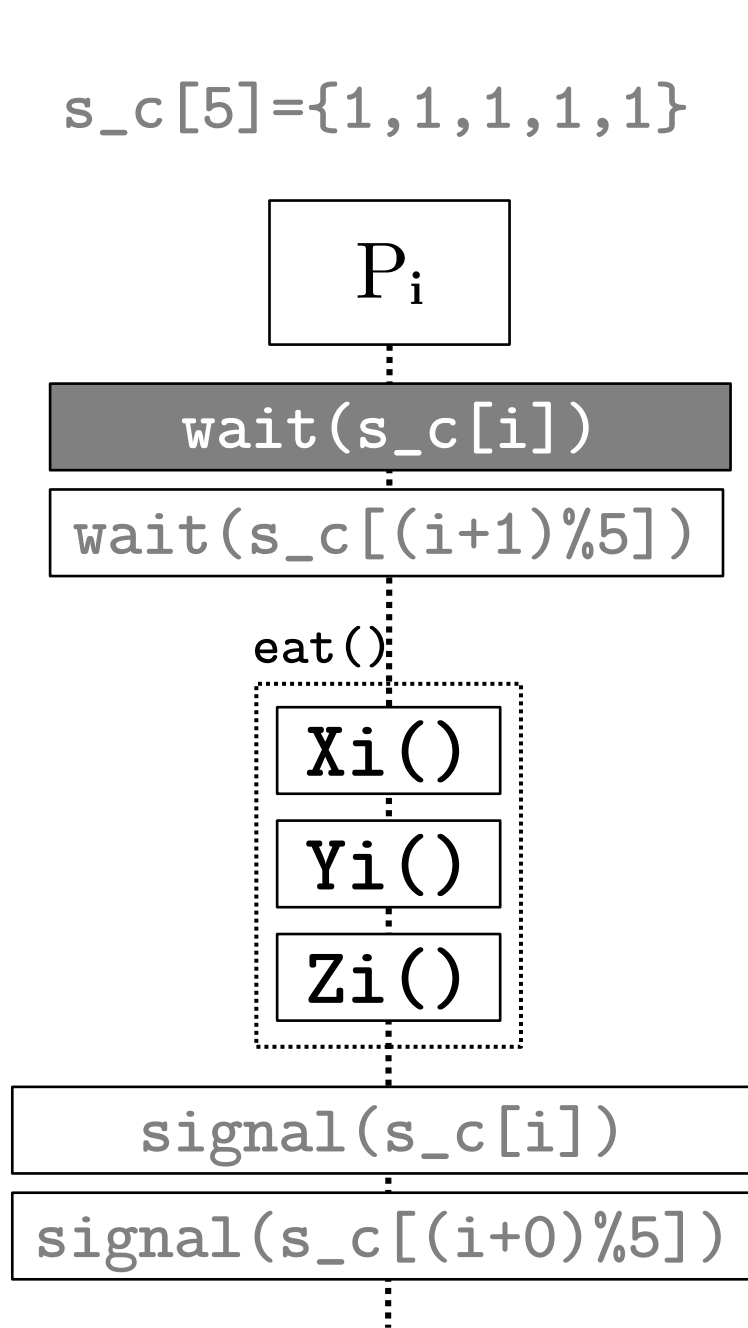


`s_c[5]` is array of semaphores of size 5, one semaphore for each chopstick. Each semaphore `s_c[i]` is initialized to 1.

Thread P_i calls `wait()` for the semaphores `s_c[i]` and `s_c[i+1]` (more accurately `s_c[(i+1)%5]`) associated with P_i 's left and right chopsticks.

After acquire the two chopstick permits, P_i will eat and then release both permits by calling `signal()` for each semaphore.

Task/Problem 5: Dining Philosophers: Deadlock



Each P_i was able to get the permission to use c_i (via semaphore $s_c[i]$) but each P_i is also waiting for permission to use c_{i+1} which is held by P_{i+1} .

Mutual/Circular waiting = Deadlock.