

Machine Learning With TensorFlow

X433.7-001 (2 semester units in COMPSCI)

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Machine Learning With TensorFlow

Class 2 ...

TensorFlow and TensorBoard, Data types, Linear algebra fundamentals ...

Course Content Outline

- Machine Learning With TensorFlow[®]
- Introduction, Python pros and cons
- Python modules, DL packages and scientific blocks
- Working with the shell, IPyton and the editor
- Installing the environment with core packages
- Writing "Hello World"

Tensorflow and TensorBoard basics

- Linear algebra recap
- Data types in Numpy and Tensorflow
- Basic operations in Tensorflow
- Graph models and structures with Tensorboard

TensorFlow operations

- Overloaded operators
- Using Aliases
- Sessions, graphs, variables, placeholders
- Name scopes

HW2 (5pts)

HW1 (5pts)

Data Mining and Machine Learning concepts

- Basic Deep Learning Models
- Linear and Logistic Regression
- Softmax classification

Neural Networks

- Multi-layer Neuaral Network
- Gradient descent and Backpropagation
- Object recognition with Convolutional Neural Network (CNN)
- Activation Functions

OUC Berkeley Extension

HW3 (5pts)

- Vector: 1) is a mathematical object that has a direction and a magnitude, used to find
 the position of one point in space relative to another point. 2) is a computer object, an
 array of data with individual items located with a single index
- Matrix is a 2-dimensional (rectangular) array of elements represented by: symbols, numbers, or expressions, all arranged in rows and columns. Matrix consist of vectors
- Array is an arrangement or a series of elements such as symbols, numbers, or expressions. Arrays can be n-dimensional, so matrix is an array with 2 dimensions
- Tensor is an objects describing the linear relationship among scalars, vectors and other tensors
- Rank of a matrix is the maximum number of linearly independent column (or row) vectors in the matrix



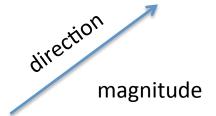
Vector

- 1) is a mathematical object that has a direction and a magnitude, used to find the position of one point in space relative to another point
- 2) is a computer object, an array of data with individual items located with a single index

Example:

mathematical meaning

computer meaning



[3245-69210]



• Matrix is a 2-dimensional (rectangular) array of elements represented by: symbols, numbers, or expressions, all arranged in rows and columns. Matrix consist of vectors

Example:

```
In [1]: a = matrix([[2, -4, 6], [-12, 5, 1], [-3, 8, 4]])
In [2]: a
Out[2]:
matrix([[ 2, -4, 6],
In [3]: b = matrix([[2],[8],[-4]])
In [4]: b
Out[4]:
matrix([[ 2],
       [8],
       [-4]])
In [5]: a*b
Out[5]:
matrix([[-52],
       [ 12],
       [ 42]])
```



Array can be n-dimensional, but matrix is an array with 2 dimensions

Example: numpy.array is a function that returns a numpy.ndarray and there for convenience

```
In [37]: c = np.zeros(shape=(4,5)) # the array contains zeroes for all elelements
In [38]: c
Out[38]:
array([[ 0., 0., 0., 0., 0.],
      [0., 0., 0., 0., 0.],
      [ 0., 0., 0., 0., 0.],
      [ 0., 0., 0., 0., 0.]])
In [39]: d = np.empty(shape=(2,2)) # the array contains meaningless data
In [40]: d
Out[40]:
array([[ 0., 0.],
   [ 0., 0.]])
In [41]: e = np.ndarray(shape=(2,3), dtype=complex, offset=np.float ().itemsize, order='C')
In [42]: e
Out[42]:
array([[ 0.00000000e+000 +1.72723382e-077j,
         2.12316144e-314 +2.14479474e-314j,
         2.12375379e-314 +2.24090241e-314j],
        2.12530167e-314 +2.12303539e-314j,
         2.24504872e-314 +3.27074300e+015j,
         3.28995843e-318 +8.34402697e-309[]])
```



NumPy array

Example:

```
In [23]: a = np.array([[12, 34, 41], [54, 62, 18], [72, 84, 96]], np.int16)
In [24]: a
Out[24]:
array([[12, 34, 41],
      [54, 62, 18],
      [72, 84, 96]], dtype=int16)
In [25]: a.size
Out[25]: 9
In [26]: a.shape
Out[26]: (3, 3)
In [27]: type(a)
Out[27]: numpy.ndarray
In [28]: a.dtype
Out[28]: dtype('int16')
In [29]: a[2,2] # this is how we index a particular elemnt in the array (#9)
Out[29]: 96
In [30]: b = a[0,:]
In [31]: b
Out[31]: array([12, 34, 41], dtype=int16)
In [32]: b.shape
Out[32]: (3,)
In [33]: b[2] = 88 # this is how we reassign another value to a member in the array
In [34]: a[2,2] = 99 # the change above also affects the original array
In [35]: a
Out[35]:
array([[12, 34, 88],
      [54, 62, 18],
      [72, 84, 99]], dtype=int16)
In [36]: b
Out[36]: array([12, 34, 88], dtype=int16)
```

- Difference between a numpy.matrix and 2D numpy.ndarray
 - basic operations such as multiplications and transpose are included in NumPy for both matrix and ndarray types
 - numpy.matrix has a proper interface for matrix operations than numpy.ndarray
 - however, the numpy.matrix class does not add anything that cannot be achieved by using 2D numpy.ndarray objects
 - the implementation of this class resembles the one in Matlab
 - scipy.linalg operations can be used just as good to 2D numpy.ndarray objects as well as to numpy.matrix



Difference between a numpy.matrix and 2D numpy.ndarray

the I and T class members serve as shortcuts for inverse and transpose respectively

the numpy.matrix class does not add anything that cannot be achieved by using 2D numpy.ndarray objects

```
In [45]: # Matrix vs Array:
In [46]: # 1. Matrix:
In [47]: import numpy as npy
In [48]: a = npy.mat('[12 34 41;52 64 72]') # create matrix 'a'
In [49]: a
Out[49]:
matrix([[12, 34, 41],
       [52, 64, 72]])
In [50]: type(a)
Out[50]: numpy.matrixlib.defmatrix.matrix
In [51]: a.I # inverse of matrix 'a'
Out[51]:
matrix([[-0.05885099, 0.03258602],
         0.01490374, -0.00181295],
       [ 0.02925572, -0.00803395]])
In [52]: b = npy.mat('[84 92]') # create matrix 'b'
In [53]: b
Out[53]: matrix([[84, 92]])
In [54]: type(b)
Out[54]: numpy.matrixlib.defmatrix.matrix
In [55]: b.T # transpose of matrix 'b'
Out[55]:
matrix([[84],
       [92]])
In [56]: a.T*b.T # multiplication of two matrices
Out[56]:
matrix([[ 5792],
        8744],
       [10068]])
```



Difference between a numpy.matrix and 2D numpy.ndarray

scipy.linalg operations can be used just as good to 2D numpy.ndarray objects as well as to numpy.matrix

Note:

npy.mat and npy.matrix are the same. Try, using 'id'

```
    Python —

                    3
In [57]: # Matrix vs Array:
In [58]: # 2. Array:
In [59]: import numpy as npy
In [60]: from scipy import linalg
In [61]: c = npy.array([[12,34,41],[52,64,72],[84,91,98]]) # create array 'c'
In [62]: c
Out[62]:
array([[12, 34, 41],
       [52, 64, 72],
       [84, 91, 98]])
In [63]: type(c)
Out[63]: numpy.ndarray
In [64]: linalq.inv(c) # calculate the inverse of a matrix
Out[64]:
array([[-0.10752688, 0.15322581, -0.06758833],
       [ 0.3655914 , -0.87096774, 0.48694316],
       [-0.24731183, 0.67741935, -0.38402458]])
In [65]: d2 = npy.array([[2,12,28]]) # create 2D array
In [66]: d2
Out[66]: array([[ 2, 12, 28]])
In [67]: type(d2)
Out[67]: numpy.ndarray
```

Difference between a numpy.matrix and 2D numpy.ndarray

scipy.linalg operations can be used just as good to 2D numpy.ndarray objects as well as to numpy.matrix

```
    Python —

In [68]: c*d2 # this is not matrix multiplication
Out[68]:
array([[ 24, 408, 1148],
        104, 768, 2016],
       [ 168, 1092, 2744]])
In [69]: c.dot(d2.T) # this is matrix multiplication using dot product function
Out[69]:
array([[1580],
       [2888],
       [400411)
In [70]: d1 = npy.array([2,12,28]) # this is 1D array
In [71]: d1
Out[71]: array([ 2, 12, 28])
In [72]: type(d1)
Out[72]: numpy.ndarray
In [73]: dl.T # this is not a matrix transpose
Out[73]: array([ 2, 12, 28])
In [74]: c.dot(d1) # dot product of two arrays
Out[74]: array([1580, 2888, 4004])
```

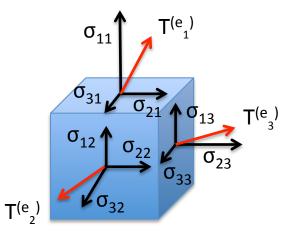
Finding the inverse of an array (matrix)

```
In [75]: # Finding the inverse of an array:
In [76]: import numpy as npy
In [77]: from scipy import linalg
In [78]: # Find the inverse of an array:
In [79]: # | 7 5 -4 |
In [80]: # | 4 -9 6 |
In [81]: # | 3 8 2 |
In [82]: e = npy.array([[7,5,-4],[4,-9,6],[3,8,2]]) # left hand-side matrix 'e':
In [83]: e
Out[831:
array([[ 7, 5, -4],
       4, -9, 6],
In [84]: linalg.inv(e) # finding the inverse of an array/matrix
Out[84]:
array([[ 0.10185185, 0.06481481, 0.00925926],
      [-0.0154321 , -0.04012346, 0.08950617],
      [-0.09104938, 0.0632716, 0.12808642]])
```

 Tensor is an objects describing the linear relationship among scalars, vectors and other tensors

Example:

a 2nd order tensor of a 3-dimensional space represent the matrix:



$$\sigma = [T^{(e_1)}T^{(e_2)}T^{(e_3)}] \qquad \text{or} \qquad \sigma = \begin{bmatrix} \sigma_{11}\sigma_{12}\sigma_{13} \\ \sigma_{21}\sigma_{22}\sigma_{23} \\ \sigma_{31}\sigma_{32}\sigma_{33} \end{bmatrix}$$

where, the columns are the forces e_n depicted on the 3 faces of the cube (e_1, e_2, e_3)

- Tensor is an objects describing the linear relationship among scalars, vectors and other tensors
 - A 0th order tensor can be represented by a scalar
 - A 1st order tensor can be represented by an array (vector)
 - A 2nd order tensor can be represented by a matrix
 - A 3rd order tensor can be represented as a 3-dimensional array of numbers
 - However tensor represents more than just an arrangement of components:
 - tensor shows how the array transforms upon a change of its basis
 - tensor is an ndarray satisfying a particular transformation law



- Rank of a matrix is the maximum number of linearly independent column (or row) vectors in the matrix, denoted as: rk(A) or rank(A)
 - The rank R of a tensor is independent of the number of dimensions N of the underlying space

- Rank-0 is a scalar
$$-N^0 = 1$$

- Rank-1 is an array (vector)
$$-N^1 = N$$

- Rank-2 is a matrix
$$-N^2 = N \times N$$
 aka dyad, dyadic

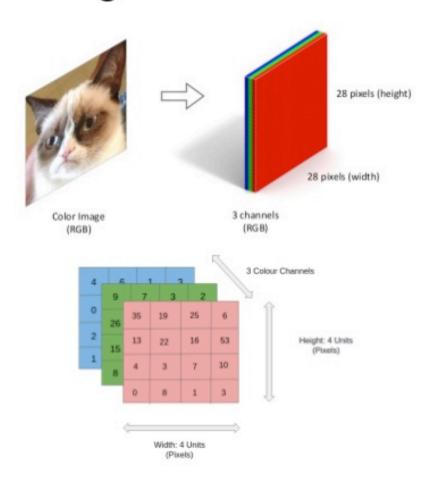
- Rank-3 is a 3-darray
$$-N^3 = N \times N \times N$$
 aka triad

- Rank-4 is a 4-darray
$$-N^4 = N \times N \times N \times N$$
 aka tetrad

etc



color image is 3rd-order tensor





- Rank of a matrix is the maximum number of linearly independent column (or row) vectors in the matrix, denoted as: rk(A) or rank(A)
 - How to find the rank:
 - They are generally: 0,1,2 and 3:

Rank(A) = 0 when matrix is null

Rank(A) = 1 when every sub-matrix of A is singular or $det(A_n) = 0$

Rank(A) = 2 when A is singular or |A| = 0, and at least one of its sub-matrix is $|A_1| \neq 0$

Rank(A) = 3 when A is non-singular or $|A| \neq 0$

Example:

$$A = \begin{bmatrix} -1 & -1 & 0 \\ 4 & 2 & 2 \\ 3 & 1 & 2 \end{bmatrix}, \quad 1) \det(A) = (-1)(2*2-2*1)-(-1)(4*2-2*3)+(0)(4*1-2*3) = -2+2-0=0$$

$$=> |A| = 0 \text{ is singular}$$

$$2) \det(A_1) = 4*1-2*3 = 4-6 = -2 --> A_1 \text{ is a sub-matrix of } A$$

$$=> |A_1| \neq 0 \text{ and is non-singular}$$

Therefore Rank(A) = 2



- Rank of a matrix is the maximum number of linearly independent column (or row) vectors in the matrix, denoted as: rk(A) or rank(A)
 - How to find the rank:
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Rank(A) = 3 when A is non-singular or $|A| \neq 0$

Example:

$$A = \begin{bmatrix} -1 & -1 & 0 \\ 4 & 2 & 2 \\ 3 & 1 & 2 \end{bmatrix}$$



NumPy data type objects

- Data type objects
 - NymPy supports much larger variety of types than what the standard Python implementation does:

Number type	Data type	Description
Booleans	bool, bool8, bool_	Boolean (True or False) stored as a byte – 8 bits
Integers	byte	compatible: C char – 8 bits
	short	compatible: C short – 16 bits
	int, int0, int_	Default integer type (same as C long; normally either int32 or int64) – 64 bits
	longlong	compatible: C long long – 64 bits
	intc	Identical to Cint – 32 bits
	intp	Integer used for indexing (same as C size_t) – 64 bits
	int8	Byte (-128 to 127) – 8 bits
	int16	Integer (-32768 to 32767) – 16 bits
	int32	Integer (-2147483648 to 2147483647) – 32 bits
	int64	Integer (-9223372036854775808 to 9223372036854775807) – 64 bits
Unsigned integers	uint, uint0	Python int compatible, unsigned – 64 bits
	ubyte	compatible: C unsigned char, unsigned – 8 bits
	ushort	compatible: C unsigned short, unsigned – 16 bits
	ulonglong	compatible: C long long, unsigned – 64 bits
	uintp	large enough to fit a pointer – 64 bits
	uintc	compatible: C unsigned int – 32 bits
	uint8	Unsigned integer (0 to 255) – 8 bits
	uint16	Unsigned integer (0 to 65535) – 16 bits
	uint32	Unsigned integer (0 to 4294967295) – 32 bits
	uint64	Unsigned integer (0 to 18446744073709551615) – 64 bits



NumPy data type objects

- Data type objects
 - NymPy supports much larger variety of types than what the standard Python implementation does:

Number type	Data type	Description
Floating- point numbers	half	compatible: C short - 16 bits
	single	compatible: C float – 32 bits
	double	compatible: C double – 64 bits
	longfloat	compatible: C long float – 128 bits
	float_	Shorthand for float64 – 64 bits
	float16	Half precision float: sign bit, 5 bits exponent, 10 bits mantissa
	float32	Single precision float: sign bit, 8 bits exponent, 23 bits mantissa
	float64	Double precision float: sign bit, 11 bits exponent, 52 bits mantissa
	float128	128 bits
Complex floating- point numbers	csingle	64 bits
	complex, complex_	Shorthand for complex128 - 128 bits
	complex64	Complex number, represented by two 32-bit floats (real and imaginary components)
	complex128	Complex number, represented by two 64-bit floats (real and imaginary components)
	complex256	two 256 bit floats

- To check how many bits each type occupies, use one of these notations:
 - 1) (np.dtype(np.<type>).itemsize)*8
 - 2) np.<type>().itemsize*8



NumPy data type objects

- Data type objects
 - the difference between signed and unsigned integers and long type variables is:
 - the signed and unsigned types are of the same size
 - the signed can represent equal amount of values around the '0' thus representing equal amount of positive and negative numbers
 - the unsigned can not represent any negative numbers, but can represent double the amount of total positive numbers as compared to the signed type
 - for 32-bit int we have:

int: -2147483648 to 2147483647

uint: 0 to 4294967295

for 64-bit long we have:

long: -9223372036854775808 to 9223372036854775807

ulong: 0 to 18446744073709551615



Below is the full list of data types available in TensorFlow:

```
@tf export("DType")
29
     class DType(object):
       """Represents the type of the elements in a `Tensor`.
31
                                                                        * `tf.uint64`: 64-bit unsigned integer.
32
                                                                45
      The following `DType` objects are defined:
                                                                        * `tf.int16`: 16-bit signed integer.
33
                                                                46
                                                                        * `tf.int32`: 32-bit signed integer.
34
                                                                47
       * `tf.float16`: 16-bit half-precision floating-point.
                                                                        * `tf.int64`: 64-bit signed integer.
                                                                48
       * `tf.float32`: 32-bit single-precision floating-point. 49
                                                                        * `tf.bool`: Boolean.
       * `tf.float64`: 64-bit double-precision floating-point.
37
                                                                50
                                                                        * `tf.string`: String.
       * `tf.bfloat16`: 16-bit truncated floating-point.
                                                                        * `tf.qint8`: Quantized 8-bit signed integer.
                                                                51
38
       * `tf.complex64`: 64-bit single-precision complex.
                                                                        * `tf.quint8`: Quantized 8-bit unsigned integer.
39
                                                                 52
       * `tf.complex128`: 128-bit double-precision complex.
                                                                        * `tf.qint16`: Quantized 16-bit signed integer.
                                                                53
       * `tf.int8`: 8-bit signed integer.
                                                                        * `tf.quint16`: Quantized 16-bit unsigned integer.
                                                                 54
41
                                                                        * `tf.qint32`: Quantized 32-bit signed integer.
       * `tf.uint8`: 8-bit unsigned integer.
42
                                                                55
       * `tf.uint16`: 16-bit unsigned integer.
                                                                        * `tf.resource`: Handle to a mutable resource.
43
       * `tf.uint32`: 32-bit unsigned integer.
                                                                        * `tf.variant`: Values of arbitrary types.
                                                                57
44
```

Examples:

```
    Python 

                    5
In [1]: import tensorflow as tf
In [2]: import numpy as np
In [3]: sess = tf.Session()
In [4]: a = 92
In [5]: type(a)
Out[5]: int
In [6]: a
Out[6]: 92
In [7]: a = tf.convert to tensor(a, dtype = tf.float16)
In [8]: type(a)
Out[8]: tensorflow.python.framework.ops.Tensor
              ... try it in class
```

```
Python 🚽 🌃 🎉
                   3
In [9]: a
Out[9]: <tf.Tensor 'Const:0' shape=() dtype=float16>
In [10]: sess.run(a)
Out[10]: 92.0
In [11]: type(sess.run(a))
Out[11]: numpy.float16
In [12]: a = sess.run(a)
In [13]: type(a)
Out[13]: numpy.float16
In [14]: a
Out[14]: 92.0
In [15]: a = tf.cast(a, tf.float32)
In [16]: type(a)
Out[16]: tensorflow.python.framework.ops.Tensor
In [22]: a = tf.cast(a, np.float64)
In [23]: type(a)
Out[23]: tensorflow.python.framework.ops.Tensor
In [24]: type(sess.run(a))
Out[24]: numpy.float64
In [27]: a = np.int16(sess.run(a))
In [28]: type(a)
Out[28]: numpy.int16
In [29]: a
Out[29]: 92
```

Few extra notes:

- Graphs save computation time
- Graphs break computation into small pieces to facilitates auto-differentiation
- Graphs handle distributed computation, that is they spread the work across multiple CPUs, GPUs, or devices
- Many machine learning models are taught and visualized as directed graphs
- Nodes in the graph are called ops (short for operations)
- An op takes zero or more Tensors, performs some computation, and produces zero or more Tensors
- Sessions gives us the environment to perform operations on our tensor data

- Few extra notes on types:
 - Using Python types to specify Tensor objects is quick and easy, and it is useful for prototyping ideas
 - However, there is an important and unfortunate downside to doing it this way:
 - TensorFlow has a plethora of data types, but basic Python types lack the ability to explicitly state what kind of data type we'd like to use!
 - Instead, TensorFlow has to infer which data type it was meant
 - TensorFlow is tightly integrated with NumPy, the scientific computing package designed for manipulating ndarrays

- Few extra notes on types:
 - In TensorFlow, all data passed from node to node are Tensor objects
 - TensorFlow Operations are able to look at standard Python types, such as integers and strings, and automatically convert them into tensors
 - 3. There are a variety of ways to create Tensor objects manually (that is, without reading it in from an external data source)
 - 4. ... so let's see them next: ...

Few extra notes on types:

- TensorFlow can take in Python numbers, booleans, strings, or lists of any of the above
- Single values will be converted to a 0-D Tensor (or scalar)
- Lists of values will be converted to a 1-D Tensor (vector)
- Lists of lists of values will be converted to a 2-D Tensor (matrix), and so on

Here is a small chart showcasing this:

- Few extra notes on types (cont.):
 - TensorFlow's data types are based on those from NumPy
 - Tensors are just a superset of matrices!
 - In fact, the statement np.int32 == tf.int32 returns True!
 - Any NumPy array can be passed into any TensorFlow Op, and the beauty is that you can easily specify the data type you need with minimal effort

The String data types problem:

- For numeric and boolean types, TensorFlow and NumPy dtypes match perfectly well
- However, tf.string does not have an exact match in NumPy due to the way NumPy handles strings
- That said, TensorFlow can import string arrays from NumPy perfectly fine just don't specify a dtype in NumPy!

Unlike Python, where a string can be treated as a list of characters,
 TensorFlow's tf.strings are indivisible values

Example:

```
'x' is a Tensor with shape (2,) and each element inside is a variable length string 
x = tf.constant(["This is a string", "This is another string"])
```

- TensorFlow provides the tf.decode_raw operator that takes tf.string tensor
 as input, but can decode the string into any other primitive data type
- To interpret the string as a tensor of characters, you can do:

- Few extra notes on types (cont.):
 - You can use the functionality of the numpy library both before and after running your graph, as the tensors returned from Session.run <u>are</u> NumPy arrays
 - Here's an example of how to create NumPy arrays, mirroring the previous example:

- Few extra notes on types (cont.):
 - You can use the functionality of the numpy library both before and after running your graph, as the tensors returned from Session.run <u>are</u> NumPy arrays
 - Here's an example of how to create NumPy arrays, mirroring the previous example:

Tensor Shape

- The shape in TensorFlow terminology describes both:
 - the number of dimensions in a tensor as well as
 - the length of each dimension
- Tensor shapes can either be Python lists or tuples containing an ordered set of integers:
 - there are as many numbers in the list as there are dimensions, and each number describes the length of its corresponding dimension

Example:

the list [2, 3] describes the shape of a 2-D tensor of length 2 in its first dimension and length 3 in its second dimension

^{*} Note that either: - tuples (wrapped with parentheses ()) or - lists (wrapped with brackets []) can be used to define shapes

Tensor Shape

Some examples:

```
# Shapes that specify a 0-D Tensor (scalar)
# e.g. any single number: 7, 1, 3, 4, etc.
s_0_list = []
s_0_tuple = ()

# Shape that describes a vector of length 3
# e.g. [1, 2, 3]
s_1 = [3]
```

```
# Shape that describes a 3-by-2 matrix

# e.g [[1 ,2],

# [3, 4],

# [5, 6]]

s_2 = (3, 2)
```

Tensor Shape

- In addition to being able to specify fixed lengths to each dimension, we are also able assign a flexible length by passing in None as a dimension's value
- This will tell TensorFlow to allow a tensor of any shape
- That is, a tensor with any amount of dimensions and any length for each dimension:

```
# Shape for a vector of any length:
s_1_flex = [None]

# Shape for a matrix that is any amount of rows tall, and 3
columns wide:
s_2_flex = (None, 3)

# Shape of a 3-D Tensor with length 2 in its first dimension,
and variable-
# length in its second and third dimensions:
s_3_flex = [2, None, None]

# Shape that could be any Tensor
s_any = None
```

Tensor Shape

- If we ever need to figure out the shape of a tensor in the middle of our graph, we can use the tf.shape Op
- It simply takes in the Tensor object we'd like to find the shape for, and returns it as an int32 vector:

```
import tensorflow as tf

# ...create some sort of mystery tensor

# Find the shape of the mystery tensor
shape = tf.shape(mystery_tensor, name="mystery_shape")
```

* Remember that tf.shape, like any other Operation, doesn't run until it is executed inside of a Session

Examples:

```
## Tensor Types
    import tensorflow as tf
    import numpy as np
 4
    # Define a 2x2 matrix in 3 different ways
    m1 = [[1.0, 2.0], [3.0, 4.0]]
                                                               # <class 'list'>
    m2 = np.array([[1.0, 2.0], [3.0, 4.0]], dtype=np.float32) # <class 'np.ndarray'>
                                                               # <class 'tensorflow'>
    m3 = tf.constant([[1.0, 2.0], [3.0, 4.0]])
    print(type(m1))
10
    print(type(m2))
11
    print(type(m3))
12
13
    # Create tensor objects out of various types
14
    t1 = tf.convert to tensor(m1, dtype=tf.float32)
                                                               # <class 'tensorflow'>
15
    t2 = tf.convert to tensor(m2, dtype=tf.float32)
                                                               # <class 'tensorflow'>
    t3 = tf.convert to tensor(m3, dtype=tf.float32)
16
                                                               # <class 'tensorflow'>
    print(type(t1))
17
18
    print(type(t2))
                                                        3

    Python —

    print(type(t3))
                                    In [1]: (executing cell "Tensor Types" (line 2 of "types.py"))
           Python -
                      7 4
                                    <class 'list'>
                                    <class 'numpy.ndarray'>
                                    <class 'tensorflow.python.framework.ops.Tensor'>
           In [9]: m3.op.name
           Out[9]: 'Const'
                                    <class 'tensorflow.python.framework.ops.Tensor'>
                                    <class 'tensorflow.python.framework.ops.Tensor'>
                                    <class 'tensorflow.python.framework.ops.Tensor'>
           ... try it in class
```

- Before you can use a variable, it must be initialized
- Most high-level frameworks such as <u>tf.contrib.slim</u>, <u>tf.estimator.Estimator</u> and Keras automatically initialize variables
- If you are explicitly creating your own graphs and sessions, you must explicitly initialize the variables
- To initialize all trainable variables in one go, before training starts, call: session.run(tf.global_variables_initializer())
- To ask which variables have still not been initialized: session.run(my variable.initializer)

Examples:

```
## A simple matrix and the InteractiveSession:
import tensorflow as tf
sess = tf.InteractiveSession()

matrix = tf.constant([[5., 6.]])
negMatrix = tf.negative(matrix)

result = negMatrix.eval()
print(result)
sess.close()
[[-5. -6.]]
```

tf.InteractiveSession:

- The <u>only difference</u> with a regular `Session` is that an `InteractiveSession` installs itself as the default session on construction.
- For example:

```
sess = tf.InteractiveSession()
a = tf.constant(5.0)
b = tf.constant(6.0)
c = a * b
# We can just use 'c.eval()' without passing 'sess'
print(c.eval())
sess.close()
```

Examples:

```
## Detecting Spikes:
    import tensorflow as tf
   sess = tf.InteractiveSession()
4
   # Create a boolean variable called `spike` to detect sudden a sudden increase in
   # a series of numbers. Since all variables must be initialized, initialize the
    # variable by calling `run()` on its `initializer`:
    vector = [3., -2., 8., -4., 0.2, 2.3, 7.5, 14.8]
    spike = tf.Variable(False)
10
11
   # Initiallizing our variable in one of two ways (choose one):
12
    # sess.run(spike.initializer)
13
    spike.initializer.run()
14
15
    # Loop through the data and update the spike variable when there is a
    # significant increase:
16
17
    for i in range(1, len(vector)):

    Python —

18
        if vector[i] - vector[i-1] > 5:
19
            updater = tf.assign(spike, tf.constant(True))
                                                                Spike False
20
            updater.eval()
                                                                Spike True
        else:
21
                                                                Spike False
22
            tf.assign(spike, False).eval()
                                                               Spike False
23
        print("Spike", spike.eval())
                                                               Spike True
24
                                                                Spike False
25
    # Check to see if there some uninitialized variables:
                                                               Spike True
    print(sess.run(tf.report uninitialized_variables()))
26
27
28
    sess.close()
```

Examples:

```
## Saving Variables in TensorFlow
    import tensorflow as tf
    sess = tf.InteractiveSession()
 4
   # Create a boolean vector called `spike` to locate a sudden spike in data.
   # Since all variables must be initialized, initialize the variable by calling
    # `run()` on its `initializer`.
   vector = [3., -2., 8., -4., 0.2, 2.3, 7.5, 14.8]
    spikes = tf.Variable([False] * len(vector), name='spikes')
 9
10
   # Initiallizing our variable in one of two ways (choose one):
11
    # sess.run(spikes.initializer)
                                                      spikes data saved in file: ./spikes.ckpt
12
    spikes.initializer.run()
13
14
    # The saver op will enable saving and restoring
15
    saver = tf.train.Saver()
16
17
    # Loop through the data and update the spike variable when there is a significant
    increase
18
19
    for i in range(1, len(vector)):
20
        if vector[i] - vector[i-1] > 5:
                                                             checkpoint
21
            spikes val = spikes.eval()
                                                             spikes.ckpt.data-00000-of-00001
22
            spikes val[i] = True
23
            updater = tf.assign(spikes, spikes val)
                                                             spikes.ckpt.index
24
            updater.eval()
25
                                                             spikes.ckpt.meta
26
    save path = saver.save(sess, "./spikes.ckpt")
27
    print("spikes data saved in file: %s" % save path)
28
29
    sess.close()
                                                                                    ... try it in class
```

Examples:

```
## Loading Variables in TensorFlow
   import tensorflow as tf
   sess = tf.InteractiveSession()
 4
   # Create a boolean vector called `spike` to locate a sudden spike in data.
   # Since all variables must be initialized, initialize the variable by calling
   # `run()` on its `initializer`.
    spikes = tf.Variable([False]*8, name='spikes')
    saver = tf.train.Saver()
10
11
   saver.restore(sess, "./spikes.ckpt")
12
    print(spikes.eval())
13
14
    sess.close()
```

INFO:tensorflow:Restoring parameters from ./spikes.ckpt
[False False True False False True True]

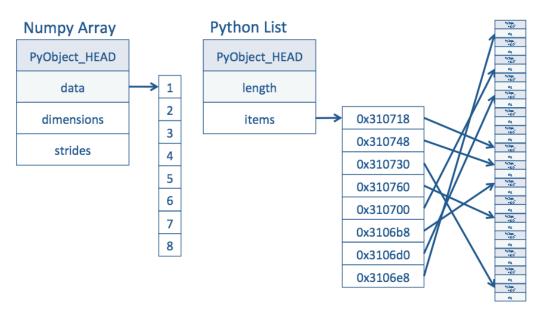
Examples:

Log example:

```
import tensorflow as tf
                 # Let's create a simple matrix:
                  matrix = tf.constant([[3., 4.]])
                  # Now negate it:
                  negMatrix = tf.negative(matrix)
              10 # Let's see where each operation is mapped to:
                  with tf.Session(config=tf.ConfigProto(log device placement=True)) as sess:
              11
              12
                      result = sess.run(negMatrix)
              13
              14 # Print results on screen:
              15 print(result)
              16 print(matrix.shape)
              17
              # To access each member inside a tensor do:
              19 print(matrix.shape[0])
2018-05-28 14:51:29.346491: I tensorflow/core/common runtime/direct session.cc:297] Device mapping:
2018-05-28 14:51:29.347240: I tensorflow/core/common runtime/placer.cc:874] Neg: (Neg)/job:localhost
replica:0/task:0/device:CPU:0
[[-3. -4.]]2018-05-28 14:51:29.347253: I tensorflow/core/common runtime/placer.cc:874] Const: (Const)
/job:localhost/replica:0/task:0/device:CPU:0
(1, 2)
```

NumPy arrays recap

- Difference between NumPy arrays vs Python Lists
 - NumPy array:
 - A NumPy array is a Python object build around a C array
 - This means that it has a pointer to a contiguous data buffer of values
 - Python Lists:
 - A Python list has a pointer to a contiguous buffer of pointers
 - All of them point to different Python objects, which in turn has references to its data (in this case, integers)
 - Conclusion:
 - NumPy is much more efficient than Python, in the cost of storage and in speed of access





NumPy arrays recap

NumPy arrays

Example:

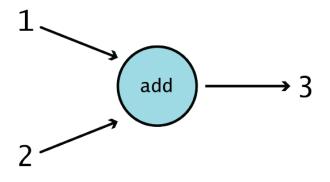
In [23]: a = np.array([[12, 34, 41], [54, 62, 18], [72, 84, 96]], np.int16) In [24]: a Out[24]: array([[12, 34, 41], [54, 62, 18], [72, 84, 96]], dtype=int16) In [25]: a.size Out[25]: 9 In [26]: a.shape Out[**26**]: (3, 3) In [27]: type(a) Out[27]: numpy.ndarray In [28]: a.dtype Out[28]: dtype('int16') In [29]: a[2,2] # this is how we index a particular elemnt in the array (#9) Out[29]: 96 In [30]: b = a[0,:]In [31]: b Out[31]: array([12, 34, 41], dtype=int16) In [32]: b.shape Out[**32**]: (3,) In [33]: b[2] = 88 # this is how we reassign another value to a member in the array In [34]: a[2,2] = 99 # the change above also affects the original array In [35]: a Out[35]: array([[12, 34, 88], [54, 62, 18], [72, 84, 99]], dtype=int16) In [36]: b Out[36]: array([12, 34, 88], dtype=int16)

... try it in class



- Let's discuss the basics of computation graphs without the context of Tensor-Flow
- This includes:
 - defining nodes
 - defining edges
 - dependencies
 - examples to illustrate key principles

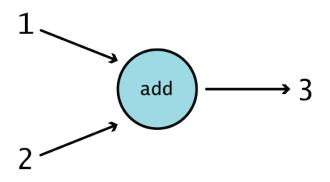
- Graph basics:
 - At the core of every TensorFlow program is the computation graph
 - It is a is a specific type of directed graph that is used for defining computational structure
 - In TensorFlow it is, a series of functions chained together, each
 passing its output to zero, one, or more functions further along in
 the chain



$$f(1,2) = 1 + 2 = 3$$

Graph basics:

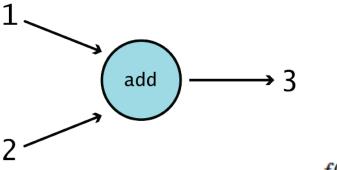
 Nodes: typically drawn as circles, ovals, or boxes, represent some sort of computation or action being done on or with data in the graph's context. In the example below, the operation "add" is the sole node.



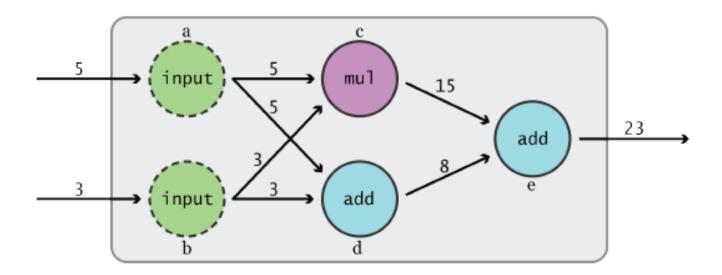
$$f(1,2) = 1 + 2 = 3$$

Graph basics:

- Edges: are the actual values that get passed to and from Operations, and are typically drawn as arrows
- In the "add" example, the inputs 1 and 2 are both edges leading into the node, while the output 3 is an edge leading out of the node
- We can think of edges as the link between different Operations as they carry information from one node to the next



f(1,2) = 1 + 2 = 3



We can decompose this graphical representation as a series of equations like this:

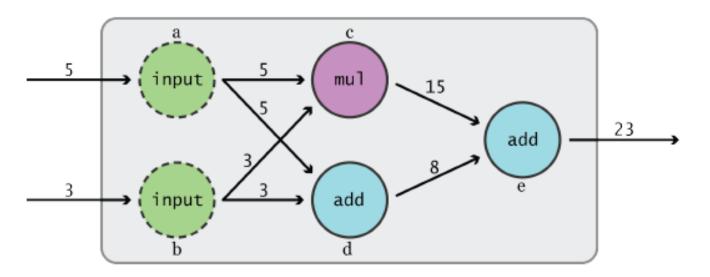
$$a = input_1; \ b = input_2$$
 $c = a \cdot b; \ d = a + b$
 $e = c + d$

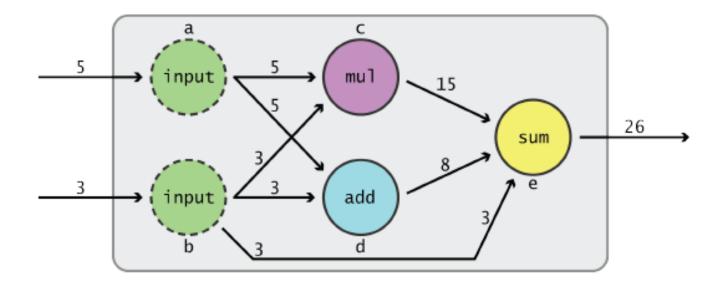
$$a = 5; \ b = 3$$

$$e = (a \cdot b) + (a + b)$$

$$e = (5 \cdot 3) + (5 + 3)$$

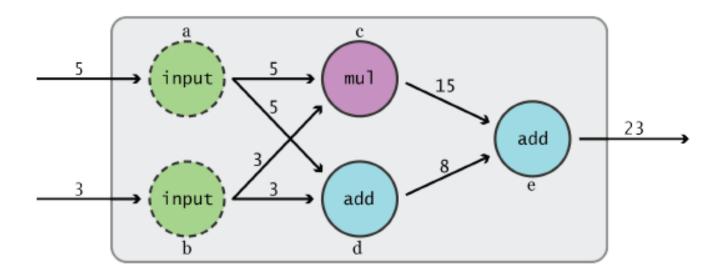
$$e = 15 + 8 = 23$$





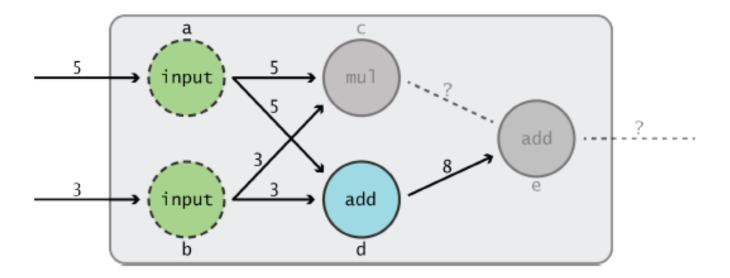
Graph basics:

• Dependencies: there are certain types of connections between nodes that aren't allowed, the most common of which is one that creates an unresolved *circular dependency*



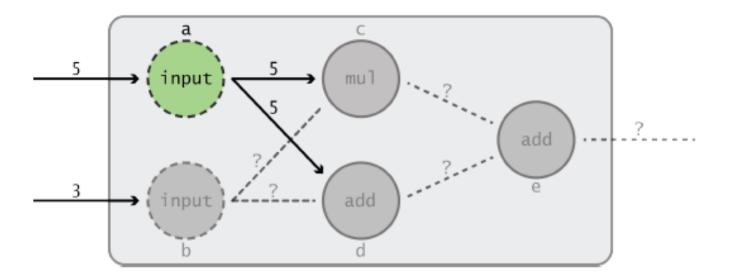
- Graph basics:
 - Dependencies: ...

let's take a look at what happens if the multiplication node c is unable to finish its computation (for whatever reason):



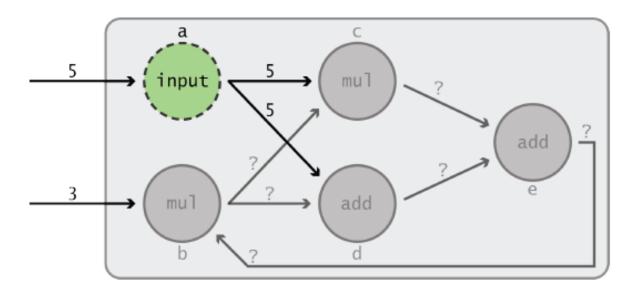
- Graph basics:
 - Dependencies: ...

What happens if one of the inputs fails to pass its data on to the next functions in the graph?



- Graph basics:
 - Dependencies: ...

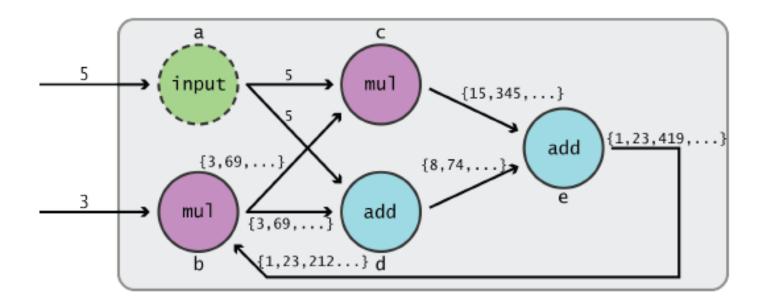
Let's see what happens if we redirect the output of a graph back into an earlier portion of it:



- Graph basics:
 - Dependencies: ...

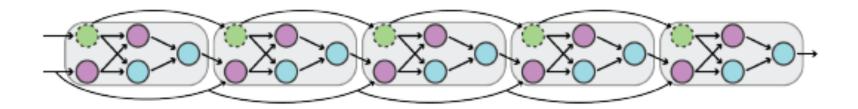
Because of this, truly circular dependencies can't be expressed in TensorFlow, which is not a bad thing.

Let's provide an initial state to the value feeding into either b or e. Let's give the graph a kick-start by giving the output of e an initial value of 1:

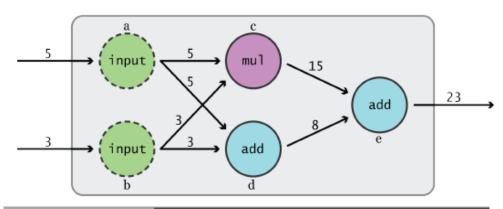


- Graph basics:
 - Dependencies: ...

By unrolling our graph like this, we can simulate useful cyclical dependencies while maintaining a deterministic computation.



Building our first graph in TensorFlow:



```
## Building our first TensorFlow graph:

## Building our first TensorFlow graph:

## First we need to import TensorFlow:

## import tensorflow as tf

## Let's define our input nodes:

## a = tf.constant(5, name="input_a")

## b = tf.constant(3, name="input_b")

## Defining the next two nodes in our graph:

## C = tf.multiply(a,b, name="mul_c")

## This last line defines the final node in our graph:

## This last line defines the final node in our graph:

## This last line defines the final node in our graph:

## This last line defines the final node in our graph:

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#### This last line defines the final node in our graph:

#### This last line defines the final node in our graph:

#### This last line defines the final node in our graph:

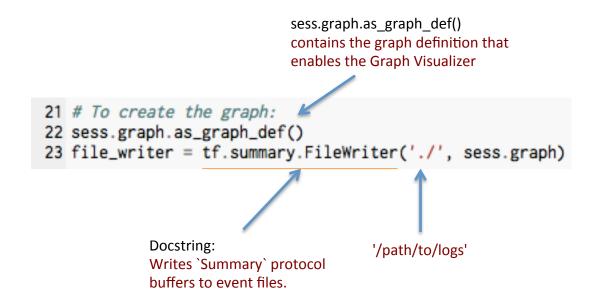
#### This last line defines the final node in our graph:

#### This last line defines the final no
```

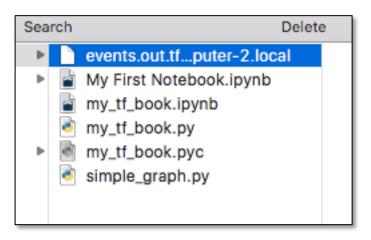
Building our first graph in TensorFlow:

```
О
                                Python
                                                                           /Users/alex
In [6]: whos
Variable
           Type
                     Data/Info
           Tensor
                     Tensor("input_a_1:0", shape=(), dtype=int32)
                     Tensor("input_b_1:0", shape=(), dtype=int32)
           Tensor
                     Tensor("mul_c:0", shape=(), dtype=int32)
           Tensor
С
d
                     Tensor("add_d:0", shape=(), dtype=int32)
           Tensor
                     Tensor("add_e:0", shape=(), dtype=int32)
           Tensor
tf
                     <module 'tensorflow' from<...>tensorflow/__init__.pyc'>
           module
           simple_graph.py
                                                                             To run we have to add
              1 ## Building our first TensorFlow graph:
                                                                             the two extra lines and
                                                                             run them in the shell:
              3 # First we need to import TensorFlow:
              4 import tensorflow as tf
                                                               In [7]: sess = tf.Session()
              6 # Let's define our input nodes:
                                                               In [8]: sess.run(e)
              7 a = tf.constant(5, name="input_a")
                                                               Out[8]: 23
              8 b = tf.constant(3, name="input_b")
             10 # Defining the next two nodes in our graph:
             11 c = tf.multiply(a,b, name="mul_c")
             12 d = tf.add(a,b, name="add_d")
             13
             14 # This last line defines the final node in our graph:
             15 e = tf.add(c,d, name="add_e")
```

- Let's construct the actual graph using TensorBoard:
 - First, we need to make sure we have generated summary data in a log directory by creating a summary writer:



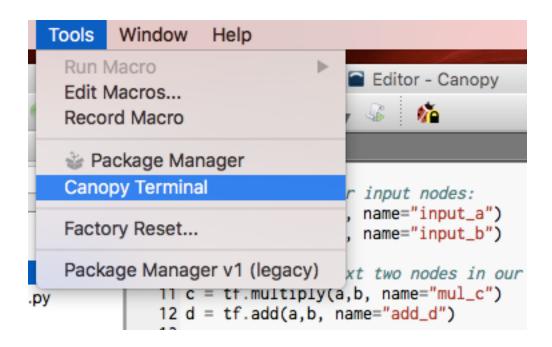
- Let's construct the actual graph using TensorBoard:
 - Once we run the previous code, a file with the session is generated in our current folder:



- Let's construct the actual graph using TensorBoard:
 - Before we continues we need to check if we have TensorBoard installed in our system:



- Let's construct the actual graph using TensorBoard:
 - Canopy does not provide TensorBoard in its repository, therefore we need to install it via the Canopy Terminal:



- Let's construct the actual graph using TensorBoard:
 - We then type: pip list to check for installed packages:

```
alex_examples — Canopy Terminal — -bash — 81×24
ssl-match-hostname (3.5.0.1
statsmodels (0.8.0)
supplement (0.5.dev0)
sympy (1.0)
tabulate (0.7.3)
tensorflow (1.3.0)
terminado (0.5)
testpath (0.2)
tornado (4.4.2)
traitlets (4.3.2)
traits (4.6.0)
traits-enaml (0.2.1)
traitsui (5.1.0)
tzlocal (1.2)
urllib3 (1.22)
wcwidth (0.1.7)
webencodings (0.5.1)
Werkzeug (0.14.1)
wheel (0.30.0)
widgetsnbextension (2.0.0)
wxPython (3.0.2.0)
zeromq (4.1.5)
zipfile2 (0.0.12)
(Canopy 64bit) Alexander-Ilievs-Computer-2:alex examples alex$ pip list
```

TensorBoard is not found in the list

- Let's construct the actual graph using TensorBoard:
 - We then type: pip install tensorboard in the terminal

```
alex_examples — Canopy Terminal — -bash — 81×24
ssl-match-hostname (3.5.0.1)
statsmodels (0.8.0)
supplement (0.5.dev0)
sympy (1.0)
tabulate (0.7.3)
tensorflow (1.3.0)
terminado (0.5)
testpath (0.2)
tornado (4.4.2)
traitlets (4.3.2)
                             $ pip install tensorboard
traits (4.6.0)
traits-enaml (0.2.1)
traitsui (5.1.0)
tzlocal (1.2)
urllib3 (1.22)
wcwidth (0.1.7)
webencodings (0.5.1)
Werkzeug (0.14.1)
wheel (0.30.0)
widgetsnbextension (2.0.0)
wxPython (3.0.2.0)
zeromg (4.1.5)
zipfile2 (0.0.12)
(Canopy 64bit) Alexander-Ilievs-Computer-2:alex examples alex$ pip list
```

- Let's construct the actual graph using TensorBoard:
 - We check again: tensorboard is now installed

```
alex examples — Canopy Terminal — -bash — 81×24
statsmodels (0.8.0)
supplement (0.5 dev0)
sympy (1.0)
tabulate (2.7.3)
tensorboard (1.7.0)
tensorflow (1.3.0)
terminado (0.5)
testpath (0.2)
tornado (4.4.2)
traitlets (4.3.2)
traits (4.6.0)
traits-enaml (0.2.1)
traitsui (5.1.0)
tzlocal (1.2)
urllib3 (1.22)
wcwidth (0.1.7)
webencodings (0.5.1)
Werkzeug (0.14.1)
wheel (0.30.0)
widgetsnbextension (2.0.0)
wxPython (3.0.2.0)
zeromq (4.1.5)
zipfile2 (0.0.12)
(Canopy 64bit) Alexander-Ilievs-Computer-2:alex examples alex$ pip list
```

- Let's construct the actual graph using TensorBoard:
 - WARNING: We check for compatibility: tensorflow + tensorboard

```
tensorboard
                                                                 1.6.0
                                 tensorflow
When installing tensorboard you might get this message:
When running tensorboard you might get this message:
         (Canopy 64bit) Alexandomputer2:alex examples alex$ tensorboard --logdir ./ --eve
         nt file events.out.tfevents.1527382420.Alexandomputer2
         2018-05-26 18:00:37.024647: I tensorflow/core/platform/cpu feature guard.cc:140]
          Your CPU supports instructions that this TensorFlow binary was not compiled to
         use: SSE4.1
         So you have to install a compatible version:
                                alex$ pip install tensorboard==1.6.0
         Make sure they match:
                              tensorboard
                                                                   1.6.0
                              ensorflow
                                                                   1.6.0
 When running tensorboard it runs without warnings:
 (Canopy 64bit) Alexandomputer2:alex examples alex$ tensorboard --logdir ./ --event file events.
```

[ensorBoard 1.6.0 at http://Alexandomputer2:6006 (Press CTRL+C to quit)

- Let's construct the actual graph using TensorBoard:
 - We must be operating in the correct directory before we go on:

```
alex_examples — Canopy Terminal — -bash — 81×24
statsmodels (0.8.0)
supplement (0.5.dev0)
sympy (1.0)
tabulate (0.7.3)
tensorboard (1.7.0)
tensorflow (1.3.0)
terminado (0.5)
testpath (0.2)
tornado (4.4.2)
traitlets (4.3.2)
traits (4.6.0)
                           cd 1*/A*/W*/3*/3*/4*/t*/c*/03*/m*
traits-enaml (0.2.1)
traitsui (5.1.0)
tzlocal (1.2)
urllib3 (1.22)
wcwidth (0.1.7)
webencodings (0.5.1)
Werkzeug (0.14.1)
wheel (0.30.0)
widgetsnbextension (2.0.0)
wxPython (3.0.2.0)
zeromq (4.1.5)
zipfile2 (0.0.12)
(Canopy 64bit) Alexander-Ilievs-Computer-2:alex examples alex$ pip list
```

- Let's construct the actual graph using TensorBoard:
 - We must be operating in the correct directory before we go on:

```
(Canopy 64bit) Alexander-Ilievs-Computer-2:alex examples alex$ pwd
/Users/alex/1.HD/Alex/Work/3.Berkeley Extension/3. final course material/3. Deep Learning using Python/code/more tf examples/alex examples
(Canopy 64bit) Alexander-Ilievs-Computer-2:alex examples alex$ ls -la
total 80
drwxr-xr-x 10 alex 501
                          340 Mar 31 15:34 .
            9 alex 501
                         306 Mar 3 17:38 ...
     --r--@ 1 alex 501 6148 Mar 31 15:34 .DS Store
drwxr-xr-x 6 alex 501
                        204 Mar 3 16:42 .ipynb checkpoints
-rw-r--r-- 1 alex 501 1316 Mar 3 16:12 My First Notebook.ipynb
rw-r--r-- 1 alex 501 1139 Mar 31 15:32 events.out.tfevents.1522528323.Alexander-Ilievs-Computer-2.local-
           - 1 alex 501 8698 Mar 4 13:0<del>5 my tf book.ipynb</del>
            1 alex 501 251 Mar 3 17:25 my tf book.py
            1 alex 501
                        430 Mar 3 17:26 my tf book.pyc
            1 alex 501
                          607 Mar 31 14:43 simple graph.py
(Canopy 64bit) Alexander-Ilievs-Computer-2:alex examples alex$
```

Then we make sure the graph summary file was created

- Let's construct the actual graph using TensorBoard:
 - Once we have the event file(s), we run TensorBoard while providing the log directory:

```
(Canopy 64bit) Alexander-Ilievs-Computer-2:alex_examples alex$ tensorboard --logdir ./
--event_file events.out.tfevents.1522372465.Alexander-Ilievs-Computer-2.local
```

- and specifically request the file to be executed
- or if you are in the same directory where the file resides simply run:

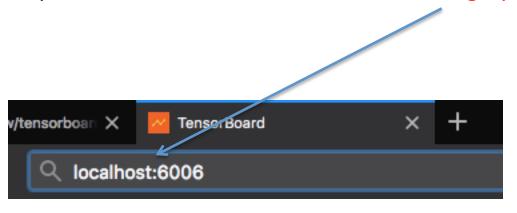
```
tensorboard --logdir ./
```

- Let's construct the actual graph using TensorBoard:
 - And the graph is already running in the background:

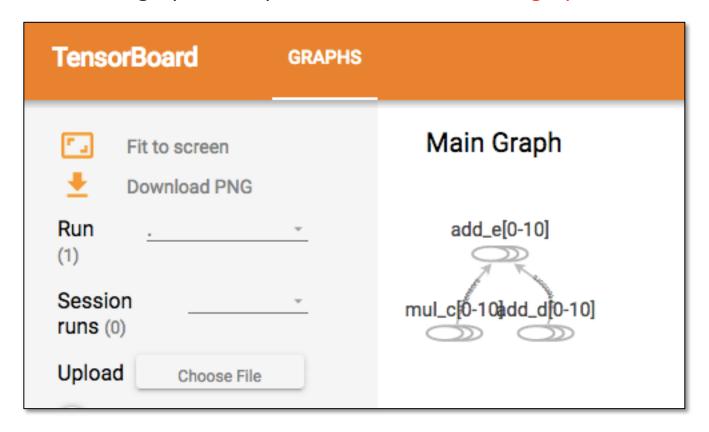
```
alex_examples — Canopy Terminal — tensorboard --logdir ./ --event_file events.out.tfevents.152252832...
(Canopy 64bit) Alexander-Ilievs-Computer-2:alex ex<mark>amples alex$ ls</mark>
My First Notebook.ipynb
                                                                        my tf book.py
events.out.tfevents.1522528323.Alexander-Ilievs-Computer-2.local
                                                                        my tf book.pyc
my tf book.ipynb
                                                                        simple graph.py
(Canopy 64bit) Alexander-Ilievs-Computer-2:alex examples alex$ pwd
/Users/alex/1.HD/Alex/Work/3.Berkeley Extension/3. final course material/3. Deep Learning using Python
/code/more tf examples/alex examples
(Canopy 64bit) Alexander-Ilievs-Computer-2:alex examples alex$ ls -la
total 80
drwxr-xr-x 10 alex 501
                         340 Mar 31 15:34 .
drwxr-xr-x 9 alex 501
                         306 Mar 3 17:38 ...
-rw-r--r--@ 1 alex 501 6148 Mar 31 15:34 .DS Store
drwxr-xr-x 6 alex 501 204 Mar 3 16:42 .ipynt checkpoints
-rw-r--r-- 1 alex 501 1316 Mar 3 16:12 My Fi∥st Notebook.ipynb
-rw-r--r-- 1 alex 501 1139 Mar 31 15:32 events.out.tfevents.<u>1522528323.Alexander-Ilievs-Computer-2</u>
.local
            1 alex 501 8698 Mar 4 13:05 my tf book.ipynb
-rw-r--r-- 1 alex 501
                         251 Mar 3 17:25 my tf book.py
-rw-r--r-- 1 alex 501
                         430 Mar 3 17:26 my tf book.pyc
-rw-r--r-- 1 alex 501
                          607 Mar 31 14:43 simple graph.py
(Canopy 64bit) Alexander-Ilievs-Computer-2:alex_ex<mark>amples alex$ tensorboard --logdir ./ --event_file_ev</mark>
ents.out.tfevents.1522528323.Alexander-Ilievs-ComWuter-2.local
TensorBoard 1.7.0 at http://Alexander-Ilievs-Computer-2.local:6006 (Press CTRL+C to quit)
W0331 15:43:15.306705 Thread-1 application.py:272] path /[[ dataImageSrc]] not found, sending 404
W0331 15:43:15.383185 Thread-1 application.py:272| path /[[ imageURL]] not found, sending 404
```

Let's construct the actual graph using TensorBoard:

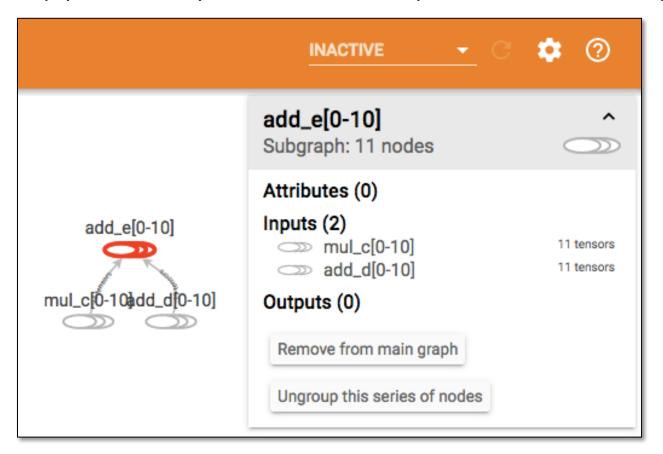
Next, we open our browser and take a look at the graph by typing:



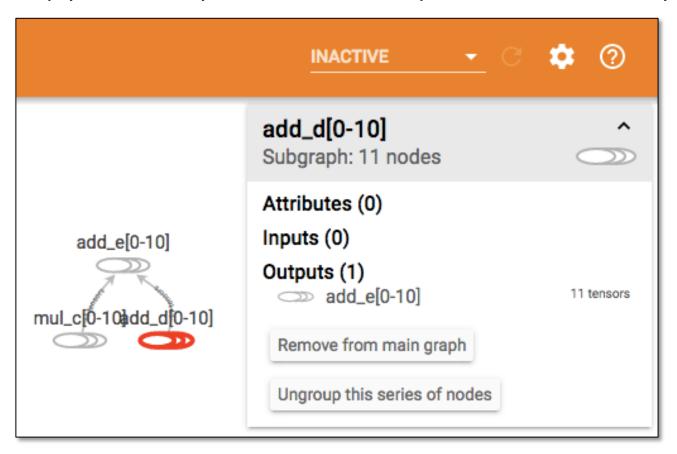
- Let's construct the actual graph using TensorBoard:
 - Below is a graphical representation of our first graph:



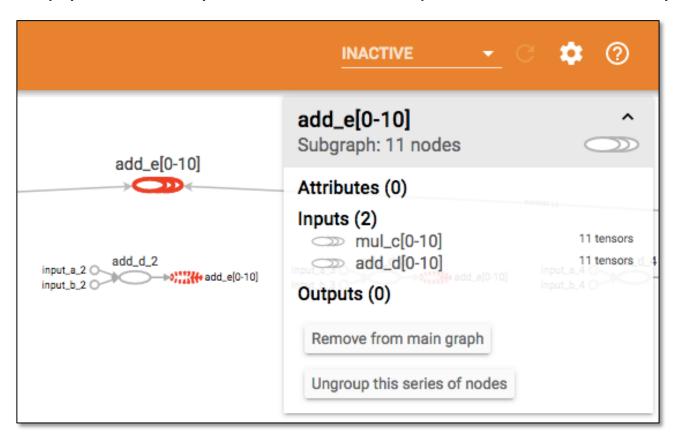
- Let's construct the actual graph using TensorBoard:
 - Simply click on any of the nodes to inspect them more closely:



- Let's construct the actual graph using TensorBoard:
 - Simply click on any of the nodes to inspect them more closely:



- Let's construct the actual graph using TensorBoard:
 - Simply click on any of the nodes to inspect them more closely:



- Let's construct the actual graph using TensorBoard:
 - Once you are done constructing our graph, we need to clean up and close the *file_writer* and *sess*:

```
25 # We clean up before we exit:
26 file_writer.close()
27 sess.close()
```

- In general, Session objects close automatically when the program terminates (or, in the interactive case, when you close/restart the Python kernel)
- However, it's best to explicitly close out of the Session to avoid any sort of weird edge case scenarios.

- Instead of having two separate input nodes, we can have a single input node that can take in a vector (or 1-D tensor) of numbers
- This graph has several advantages over our previous example:
 - 1. The client only has to send input to a single node, which simplifies using the graph
 - 2. The nodes that directly depend on the input now only have to keep track of one dependency instead of two
 - 3. We now have the option of making the graph take in vectors of any length, if we'd like. This would make the graph more flexible