

# MC3203: PPS

## #21: Memory Layout for Lists/Objects

Spring 2019



## Copy/Equality Operations for Built-In Data Structures: Summary

### Copy operations for lists

- `=` : **alias**
- `[:]` : shallow copy (copy of only top-level list)
  - ▶ deep copy for “one-dimensional” lists (e.g. `[1, 2, 3]`)
  - ▶ not deep copy for list of lists (of lists (of lists ..))
- `copy.deepcopy()` : **deep** copy
  - ▶ recursively copies lists of all levels

### Equality operations for lists

- `is` : check if **aliased**
- `==` : **deep** equality ( $a \text{ is } b \Rightarrow a == b$  , but not vice versa)

### Copy/Equality operations for user-defined objects:

- `=` / `copy.deepcopy()` / `is` : the same as for lists
- `==` : 
$$\begin{cases} \text{as you wish (e.g. deep equality)} & \text{if overloaded by } \text{--eq--} \\ \text{is (check if aliased)} & \text{otherwise} \end{cases}$$

Copy/Equality operations for sets/dictionaries: the same as for lists

# Outline

## 1 Memory Layout for Lists

## 2 List Copy

## 3 List as Function I/O

## 4 List Equality

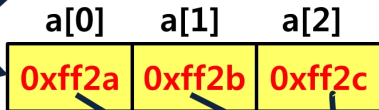
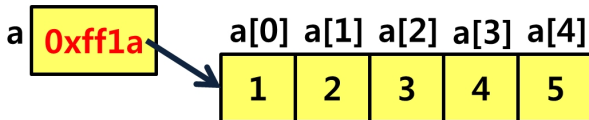
## 5 User-Defined Objects

# Memory Layout for Lists (1/3) (simplified for easier understanding)

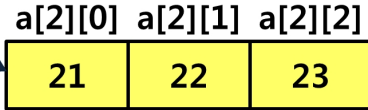
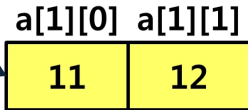
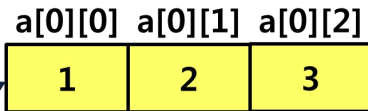
$a = 1$



$a = [1, 2, 3, 4, 5]$



$a = [$   
 $[1, 2, 3],$   
 $[11, 12],$   
 $[21, 22, 23]$   
 $]$

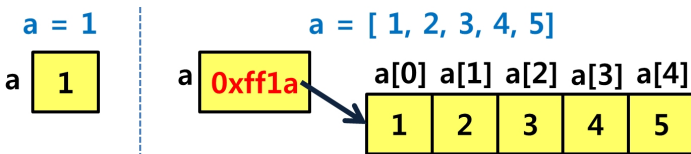


## Memory Layout for Lists (2/3) (simplified for easier understanding)

What kind of **value** does a **variable** have?

- For a **primitive type** variable: number/string/.. (e.g. **1**)
  - ▶ primitive type: int, float, bool, ...
- For a **list** type variable: **memory address** (e.g. **0xff1a**)
  - ▶ address of the **start** (e.g. **a[0]**) of contiguous memory block
  - ▶ since each **a[i]** is a primitive type variable, **a[i]** has number as its value

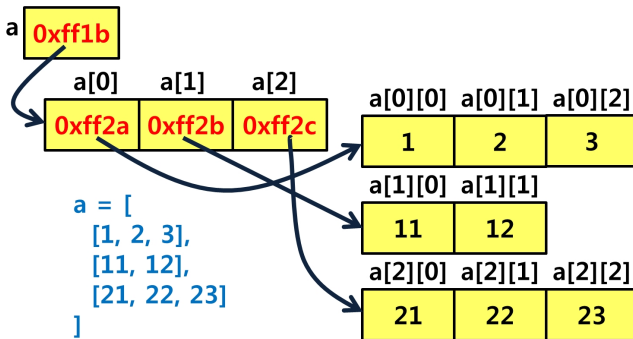
- The **value** of a **list type variable**  $\neq$  **list**  
 $=$  **memory address** to list



## Memory Layout for Lists (3/3) (simplified for easier understanding)

What about a **list of lists**?

- Similarly, the value of `a` is the memory address to `a[0..2]`
- Also, the value of each `a[i]` is the **memory address** to `a[i][0]`, `a[i][1]`, `...`
- Each `a[i][j]` is now a primitive type variable, so `a[i]` has number as its value



# Outline

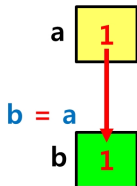
- 1 Memory Layout for Lists
- 2 List Copy**
- 3 List as Function I/O
- 4 List Equality
- 5 User-Defined Objects

## = vs. [ : ] for Lists

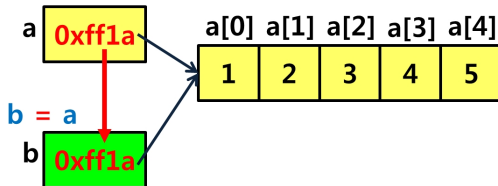
The assignment operation `=` just copies the **value** of a variable

- Recall: the **value** of a **list type variable** is NOT list but **address**
- Thus, for list `a`, the effect of “`b = a`” is to make `b` and `a` point to the **same list**
  - `b` is called an **alias** of `a`

`a = 1`



`a = [ 1, 2, 3, 4, 5 ]`



`c = a[:]`



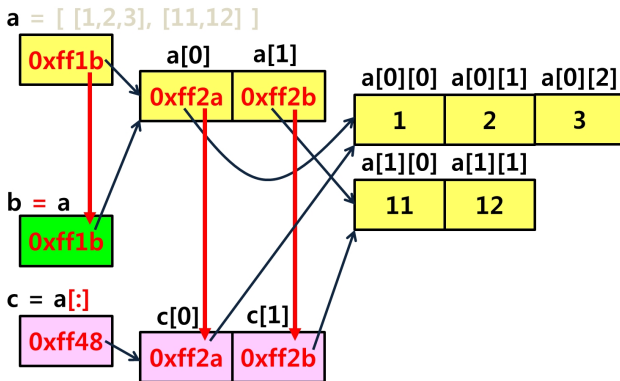
The slicing op `[ : ]` creates a new **copy of list**



## = vs. [ : ] for Lists of Lists

`=` just copies the **value** of a variable (**alias**)

- a and b point to the **same list** a[0], a[1], ...



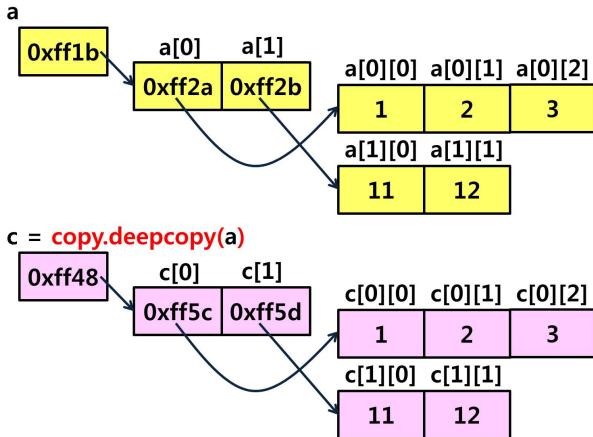
`[ : ]` creates a new **copy** of **only top-level** list (**shallow copy**)

- a and c point to **different lists** (top-level deep copy)
- BUT, a[i] and c[i] point to the **same list** a[i][0], ...

## `copy.deepcopy()` for Lists of Lists

`copy.deepcopy()` create a new copy of **whole** list, **recursively**

- `c = copy.deepcopy(a)` makes `a` and `c` **share nothing**
- If what you want is a new deep copy of **list of lists**, then use `copy.deepcopy` instead of `[:]`



## Exercise: Figure out why the output is..

```
a = [ [1, 2, 3],
      [11,12] ]
```

```
b = a
```

```
c = a[:]
```

```
d = copy.deepcopy(a)
```

```
a[1][0] = 0
```

```
a[0] = [4,5]
```

```
print(b[1][0], c[1][0], d[1][0]) # 0 0 11
```

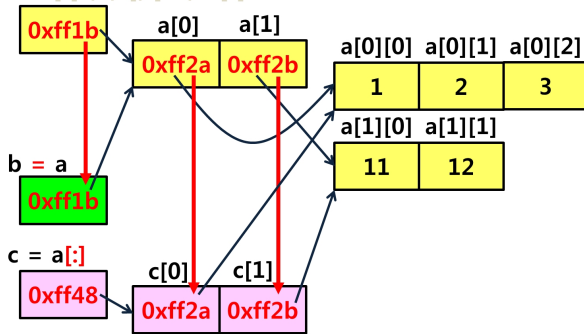
```
print(b[0],c[0],d[0]) # [4,5] [1,2,3] [1,2,3]
```

```
a[0],a[1] = a[1],a[0] # swapping rows
```

```
print(a,b) # [[0,12], [4,5]] [[0,12], [4,5]]
```

```
print(c) # [[1,2,3], [0,12]]
```

```
a = [ [1,2,3], [11,12] ]
```



# Outline

1 Memory Layout for Lists

2 List Copy

**3 List as Function I/O**

4 List Equality

5 User-Defined Objects

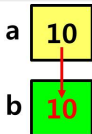
## Lists as Function Input (1/2)

- Passing an argument **a** to function as a parameter **b** has the effect of **b = a** (i.e. **aliasing**)
- For each case, figure out why the output is :

### Number as input

```
def f(b): # b = a
    b = 0
```

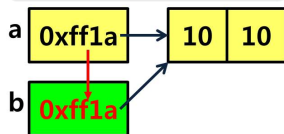
```
a = 10
f(a)
print(a)
```



### List as input

```
def f(b): # b = a
    b[1] = 0
```

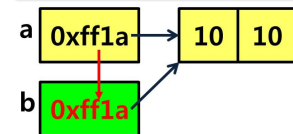
```
a = [10, 10]
f(a)
print(a)
```



### List as input, but ..

```
def f(b): # b = a
    b = [0, 0]
```

```
a = [10, 10]
f(a)
print(a)
```

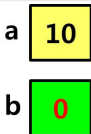


## Lists as Function Input (2/2)

- Passing an argument **a** to function as a parameter **b** has the effect of **b = a** (i.e. **aliasing**)
- For each case, figure out why the output is :

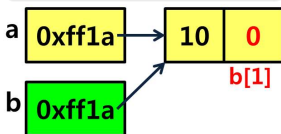
### Number as input

```
def f(b):  
    b = 0  
  
a = 10  
f(a)  
print(a) # 10  
# a is not modified
```



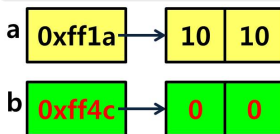
### List as input

```
def f(b):  
    b[1] = 0  
  
a = [10,10]  
f(a)  
print(a) # [10,0]  
# a is modified
```



### List as input, but ..

```
def f(b):  
    b = [0,0]  
  
a = [10,10]  
f(a)  
print(a) # [10,10]  
# a is not modified
```



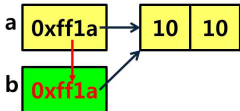
# Modifier vs. Pure Function (1/3)

## Modifier

```
def f(b): # b = a

    for i in range(len(b)):
        b[i] = b[i] + 1
```

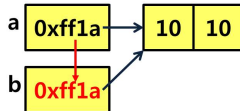
```
a = [10,10]
f(a)
```



## Pure Function

```
def f(b): # b = a
    c = [0]*len(b)
    for i in range(len(b)):
        c[i] = b[i] + 1
    return c
```

```
a = [10,10]
d = f(a)
```

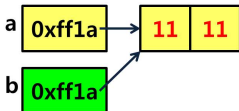


## Modifier vs. Pure Function (2/3)

### Modifier

```
def f(b):
    for i in range(len(b)):
        b[i] = b[i] + 1
```

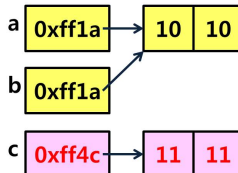
```
a = [10,10]
f(a)
```



### Pure Function

```
def f(b):
    c = [0]*len(b)
    for i in range(len(b)):
        c[i] = b[i] + 1
    return c
```

```
a = [10,10]
d = f(a)
```





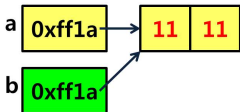
## Modifier vs. Pure Function (3/3)

- Receiving return value **c** to variable **d** has the effect of **d = c**

### Modifier

```
def f(b):  
  
    for i in range(len(b)):  
        b[i] = b[i] + 1
```

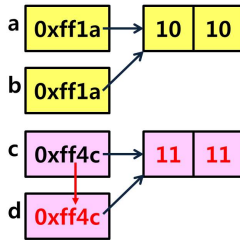
```
a = [10,10]  
f(a)  
print(a)  # [11,11]
```



### Pure Function

```
def f(b):  
    c = [0]*len(b)  
    for i in range(len(b)):  
        c[i] = b[i] + 1  
    return c
```

```
a = [10,10]  
d = f(a)  # d = c  
print(a)  # [10,10]
```



# Outline

1 Memory Layout for Lists

2 List Copy

3 List as Function I/O

**4 List Equality**

5 User-Defined Objects

## == vs. is for Lists

- `==` checks if list **contents** are the same (deep equality)
- `is` checks if **aliased** (i.e. the same list) (shallow equality)
- `a is b`  $\Rightarrow$  `a == b` , but not vice versa

```
a = [1,2,3,4,5]
```

```
b = a
```

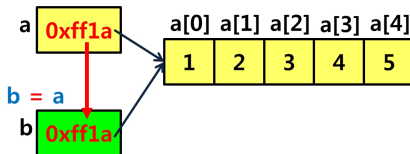
```
c = a[:]
```

```
d = copy.deepcopy(a)
```

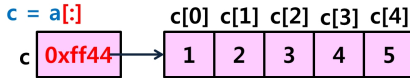
```
print(a==b, a==c, a==d) # True True True  
# list contents are the same
```

```
print(a is b) # True (the same list)  
print(a is c) # False (different lists)  
print(a is d) # False (different lists)
```

`a = [1, 2, 3, 4, 5]`



`c = a[:]`



## == vs. is for Lists of Lists

- `==` checks if list **contents** are the same (deep equality)
- `is` checks if **aliased** (i.e. the same list) (shallow equality)

```
a = [ [1,2,3],  
      [4,5] ]
```

```
b = a
```

```
c = a[:]
```

```
d = copy.deepcopy(a)
```

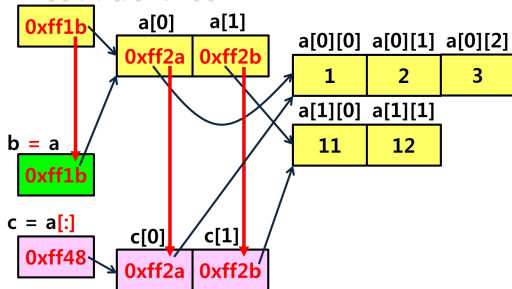
```
print(a==b, a==c, a==d) # True True True  
# list contents are the same
```

```
print(a is b) # True (the same list)
```

```
print(a is c) # False (different lists)
```

```
print(a is d) # False (different lists)
```

```
a = [ [1,2,3], [11,12] ]
```



## Copy/Equality Operations for Lists: Summary

### Copy operations for lists

- `=` : **alias**
  - ▶ Beginners **mistakenly** use alias instead of deep copy
  - ▶ Nevertheless, sometimes useful (e.g. practice problems 1-2)
- `[:]` : shallow copy (deep copy of only top-level list)
  - ▶ Useful as deep copy for **list of numbers** (e.g. `[1,2,3]`)
- `copy.deepcopy()` : **deep** copy
  - ▶ Useful for **multi-dimensional lists** (e.g. practice problem 2)

### Equality operations for lists

- `is` : check if **aliased**
  - ▶ **Seldom** used (not used in this course)
- `==` : **deep** equality
  - ▶ Works well with **multi-dimensional lists**
  - ▶  $a \text{ is } b \Rightarrow a == b$  , but not vice versa

# Outline

1 Memory Layout for Lists

2 List Copy

3 List as Function I/O

4 List Equality

5 User-Defined Objects

# Copy/Equality Operations: Lists vs. User-Defined Objects

## Recall

Copy/Equality operations for user-defined objects:

- `=` / `copy.deepcopy(·)` / `is` : the same as for lists
  - `==` :  $\begin{cases} \text{as you wish (e.g. deep equality)} & \text{if overloaded by } \text{__eq__} \\ \text{is (check if aliased)} & \text{otherwise} \end{cases}$
- 
- The **list** is a special case of **objects**
    - ▶ where `==` is overloaded by `__eq__` that recursively checks deep equality
  - A user-defined **object** can be thought of as a **list** of instance variables
  - Thus, copy/equality operations for user-defined objects **work** almost the **same** as those for lists

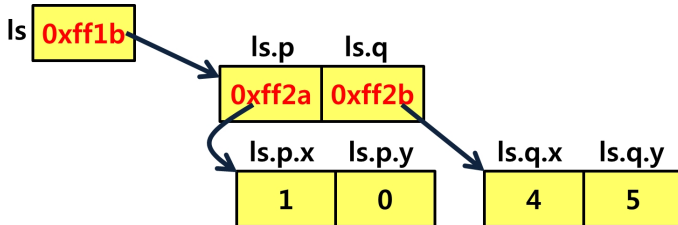
# Memory Layout for Objects

(simplified for easier understanding)

```
class Point:
    def __init__(self,x,y):
        self.x = x
        self.y = y

class LineSegment:
    def __init__(self,point1,point2):
        self.p = point1
        self.q = point2

ls = LineSegment(Point(1,0), Point(4,5))
```

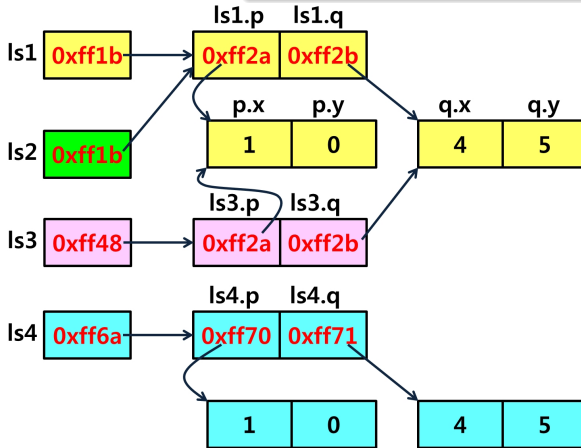




# Copy Operations for Objects

```
p = Point(1,0)
q = Point(4,5)
ls1 = LineSegment(p,q)
```

```
ls2 = ls1
ls3 = LineSegment(p,q)
ls4 = copy.deepcopy(ls1)
ls4 = LineSegment(copy.deepcopy(p),
                  copy.deepcopy(q))
```



## Equality Operations for Objects

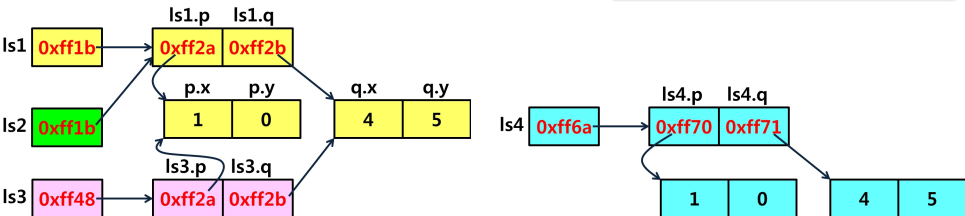
- `is` checks if **aliased** (i.e. the same list) (shallow equality)
- `==` :  $\begin{cases} \text{as you wish (e.g. deep equality)} & \text{if } \text{__eq__} \text{ defined} \\ \text{is (check if aliased)} & \text{otherwise} \end{cases}$

```
def Point:
    def __eq__(self,p):
        return self.x==p.x and self.y==p.y

def LineSegment:
    def __eq__(self,l):
        return self.p==l.p and self.q==l.q
```

```
print(ls1 == ls2) # True
print(ls1 == ls3) # True
print(ls1 == ls4) # True
```

```
print(ls1 is ls2) # True
print(ls1 is ls3) # False
print(ls1 is ls4) # False
```



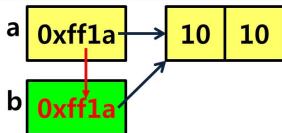
## Objects as Function Input (1/2)

- Passing an argument **a** to function as a parameter **b** has the effect of **b = a** (i.e. **aliasing**)

### Object as input

```
def f(b): # b = a
    b.y = 0
```

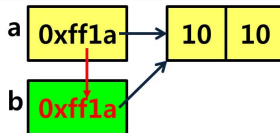
```
a = Point(10,10)
f(a)
print(a)
```



### Object as input, but ..

```
def f(b): # b = a
    b = Point(0,0)
```

```
a = Point(10,10)
f(a)
print(a)
```

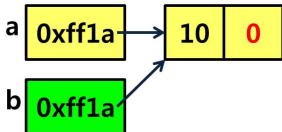


## Objects as Function Input (2/2)

- Passing an argument **a** to function as a parameter **b** has the effect of **b = a** (i.e. **aliasing**)

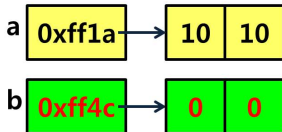
### Object as input

```
def f(b):  
    b.y = 0  
  
a = Point(10,10)  
f(a)  
print(a)  # (10,0)  
# a is modified
```



### Object as input, but ..

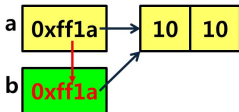
```
def f(b):  
    b = Point(0,0)  
  
a = Point(10,10)  
f(a)  
print(a)  # (10,10)  
# a is not modified
```



# Modifier vs. Pure Function (1/3)

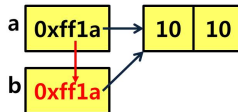
## Modifier

```
def f(b): # b = a  
  
    b.x = b.x + 1  
    b.y = b.y + 1  
  
a = Point(10,10)  
f(a)
```



## Pure Function

```
def f(b): # b = a  
    c = Point(0,0)  
    c.x = b.x + 1  
    c.y = b.y + 1  
    return c  
  
a = Point(10,10)  
d = f(a)
```



## Modifier vs. Pure Function (2/3)

### Modifier

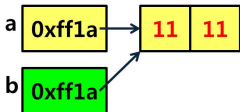
```
def f(b):
```

```
    b.x = b.x + 1
```

```
    b.y = b.y + 1
```

```
a = Point(10,10)
```

```
f(a)
```



### Pure Function

```
def f(b):
```

```
    c = Point(0,0)
```

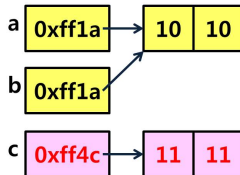
```
    c.x = b.x + 1
```

```
    c.y = b.y + 1
```

```
    return c
```

```
a = Point(10,10)
```

```
d = f(a)
```



## Modifier vs. Pure Function (3/3)

- Receiving return value **c** to variable **d** has the effect of **d = c**

### Modifier

```
def f(b):
```

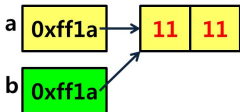
```
    b.x = b.x + 1
```

```
    b.y = b.y + 1
```

```
a = Point(10,10)
```

```
f(a)
```

```
print(a)  # (11,11)
```



### Pure Function

```
def f(b):
```

```
    c = Point(0,0)
```

```
    c.x = b.x + 1
```

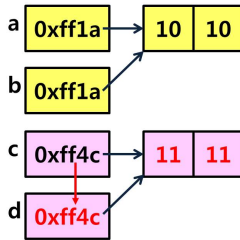
```
    c.y = b.y + 1
```

```
    return c
```

```
a = Point(10,10)
```

```
d = f(a)  # d = c
```

```
print(a, d)  # (10,10) (11,11)
```



## Modifiers for Lists?

`L.sort()`/`L.append()`/.. are really **modifiers** for lists?

- Think of lists as user-defined objects of the class `List`
- Then, `L.sort()` can be thought of `List.sort(L)` where `L` is pass as an argument to modifier `List.sort`, and sorting performs **directly on L**
- On the contrary, list concatenation operation `+` can be understood as a **pure function**

```
def f(L):  
    L.append(40)
```

```
L = [10,20,30]  
f(L)  
print(L)
```

Figure out why the output is:

```
[10, 20, 30, 40]
```