

# CS & IT ENGINEERING

Discussion Notes

Theory of Computation



Undecidability & Decidability II  
DPP 02



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# TOPICS TO BE COVERED

01 Question

02 Discussion

Q.1



Let  $L = \{(X) \mid X \text{ is a DFA and } L(X) \text{ is an infinite language}\}$ ; where  $(X)$  represents the illustration of the deterministic finite automata (DFA).

[MSQ]

Then which of the statement is/are correct?

- A. It is recognizable by Turing. ✓
- B. Its complement is recognizable by Turing. ✓
- C. It is Turing decidable (recursive). ✓
- D. It is context-free but not regular.



Q.2

Which of the following statement is/are incorrect?

[MSQ]



*Incorrect*  
A.

If L is CFL and A is DCFL then  $L-A$  is CFL.

$$CFL - DCFL = CFL \cap \overline{DCFL} \Rightarrow CFL \cap DCFL \Rightarrow CSL$$

*Incorrect*  
B.

The subset of a decidable language is always decidable.

*Incorrect*  
C.

If L and A are DCFL then  $(\bar{L} \cap \bar{A})$  is CFL.

D.

None of the above are incorrect.



Q.3

Consider some language  $P \in \{0,1\}^*$  reduces to another language  $Q \in \{0,1\}^*$ . Which of the following statement is true?

[MCQ]



$$P \leq Q$$

A.

P is decidable.  $\times$

B.

A Turing machine that recognizes P can be used to construct a Turing machine that recognizes Q.  $\times$

C.

If Q is decidable then P is decidable.  $\checkmark$

D.

If P is decidable then Q is decidable.  $\times$



Q.4

[MCQ]



Consider the following statement:

$S_1$ : In phrase structured language, membership problem is semi decidable. *True*

$S_2$ : In context-free languages, membership problem can be solved in polynomial time. *True  $O(n^3)$*

A.

Only  $S_1$  is true

B.

Only  $S_2$  is true

☒ C.

Both  $S_1$  and  $S_2$  is true

D.

Neither  $S_1$  nor  $S_2$  is true

Q.5

[MCQ]



Consider the following statements:

$S_1$ : For a decidable language  $X$ ,  $X^R$  may or may not be decidable.

( $X^R$  represents the reverse of language  $X$ ). *false*

$S_2$ : If  $X$  is not recursively enumerable then  $\bar{X}$  must be recursively enumerable. *false*

- A. Only  $S_1$  is true
- B. Only  $S_2$  is true
- ☒ C. Both  $S_1$  &  $S_2$  are false
- D. Both  $S_1$  &  $S_2$  are true



Q.6

Consider the following statements about Turing machine.

[MCQ]



$S_1$ : If there is some Turing machine that accepts every string in  $L$  and rejects every string not in  $L$  then  $L$  is decidable. ✓

$S_2$ : If there is some Turing machine that accepts every string in  $L$  and either rejects or loops on every string not in  $L$ , then  $L$  is semi-decidable or computably enumerable (CE). ✓

A.

Only  $S_1$  is true

B.

Only  $S_2$  is true

☒ C.

Both  $S_1$  &  $S_2$  are true

D.

Neither  $S_1$  nor  $S_2$  is true



Q.7

Which of the following is/are decidable properties of context-free?



[MSQ]

A.

for context-free grammar  $X$ , find if string  $w \in L(X)$

B.

for context-free grammar  $X$ , find if  $L(X) = \phi$ .

C.

for context-free grammar  $X$ , find if  $L(X)$  is infinite.

D.

none of the above are decidable properties of context free.



Q.8

[MCQ]



Consider the following statements:

$S_1$ : There is language for which no TM available. Then surely language will be Not RE. *correct*

$S_2$ : Language is undecidable if and only there is no HTM available for language. *correct*

Which of the following is incorrect?

A.

$S_1$  only.

B.

$S_2$  only.

C.

Both  $S_1$  and  $S_2$ .

☒ D.

Neither  $S_1$  Nor  $S_2$ .



