CS & IT SENGING

Algorithms

Sorting Methods

One Shot



Recap of Previous Lecture











Topic

Graph Techniques

Topics to be Covered











Topic

Sorting Methods

SORTING TECHNIQUES



- classification:
 - (i) Internal us External Sort
 - (ii) Comparison vs Non-Comparison based (Radin Sort)
 - (iii) Recursive vs Iterative
 - (iv) In place us NOT-IN-PLACE

 Space Regit is

 gen O(1)

 or atmost O(logn)

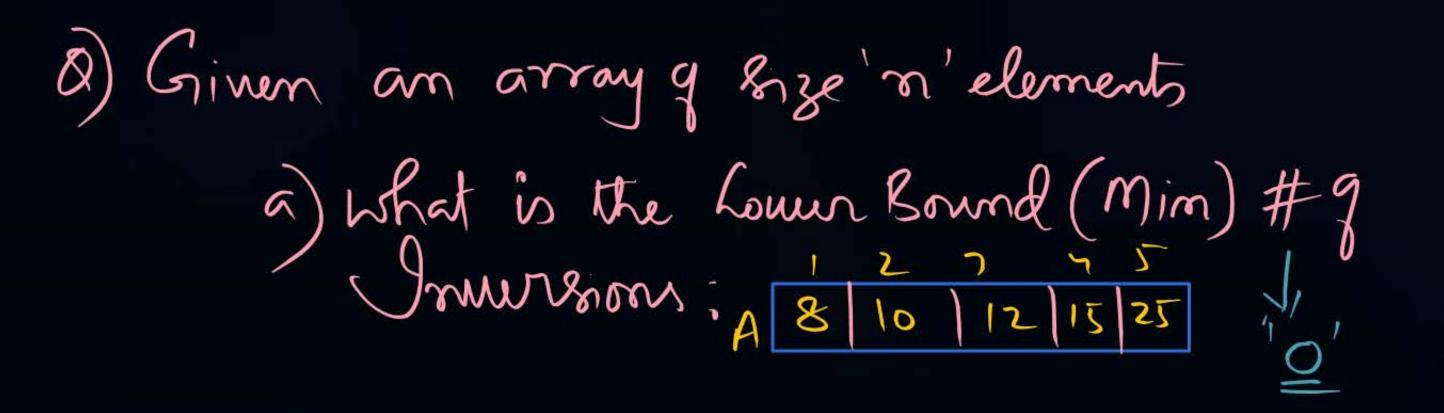
 for Rec. Stack)

(V) Stable vs unstable (QS; FIJ the relative order q Non-Distinct elements are maintained, Let All. n) be an array of n-elements Let i,j be two indices (i \pm j) y (A[i]=A[i]) & y A[i] precedes A(j) in the Re-Sorted list, then the Borting method in Stable, if A(i) Preceden A(i) in The Find Sorted list also;

(Stable)

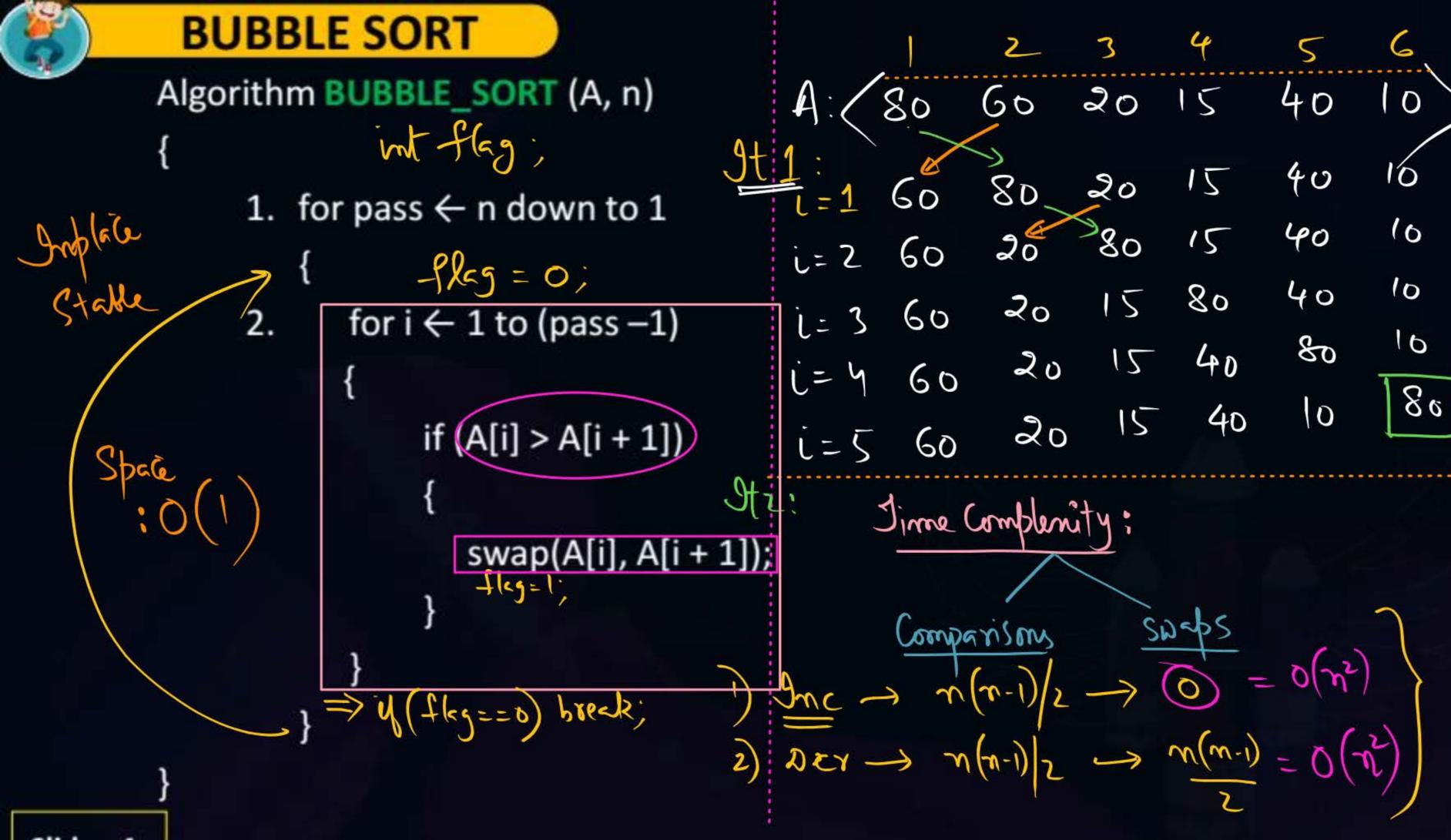
farameters that influence the Time Complenity of Comparison Based Jime-Complenity (Comp. based = f (No. of Comparisons;
Sort) = f (No. of Comparisons; Mergesoot Inversion of an Array as a size of Imput (n) O (n. Cogn) t (2; upers) Jime = O(n2)

Inverson quantray: -> Let A[1-..n] be an array, 'i' & j' be indices (i + j) y(i < j) and (A(i) > A(j)) then the pain (i, j) in known as inversion of the A 8 9 4 5 1 2 (1,3)(1,4)(1,5)(1,6)=4 (2,3) (2,4) (2,5) (2,6)=4 (3,5) (3,6) = 2 (415) (416)=2



b) what is the man (upper Bound) # of Inversions:

A 10 8 5 4 2 1



optimized Bubble Sort (flas)



(i) Best Case: O(n): Inc. orden

let 7(n) repr. Time Complemity of (worst Case) B.c Bulkle-Sort (n) $T(n) = n + T(n-1) = O(n^2)$

$$T(n) = n-1+c = O(n)$$

$$T(n) = n + T(n-1) = O(n^2)$$



SELECTION SORT

- 1. Find the smallest element in the list.
- 2. Swap it with the value in the current ith position. $\begin{bmatrix} -1 & \infty 1 \end{bmatrix}$
- Repeat this process for all elements until the array is sorted.

Mine A: 80 60 20 15 40 10 i=1 / (10) (60 20 15 40 80) i=2 / (10) (15) (20 60 40 88) min = 7

Algorithm SELECTION_SORT (A, n) 1. for i ← 1 to n − 1 do $min \leftarrow i$; for $j \leftarrow i + 1$ to n O(n2) if (A[j] < A[min]) then $min \leftarrow j$; Bert 12661 swap(A[min], A[i];

Note => Selection is the only Sorting Jechnique in Comparison based Sorting, that requires least no. 9 Swaps (O(n)) in the worst-case,



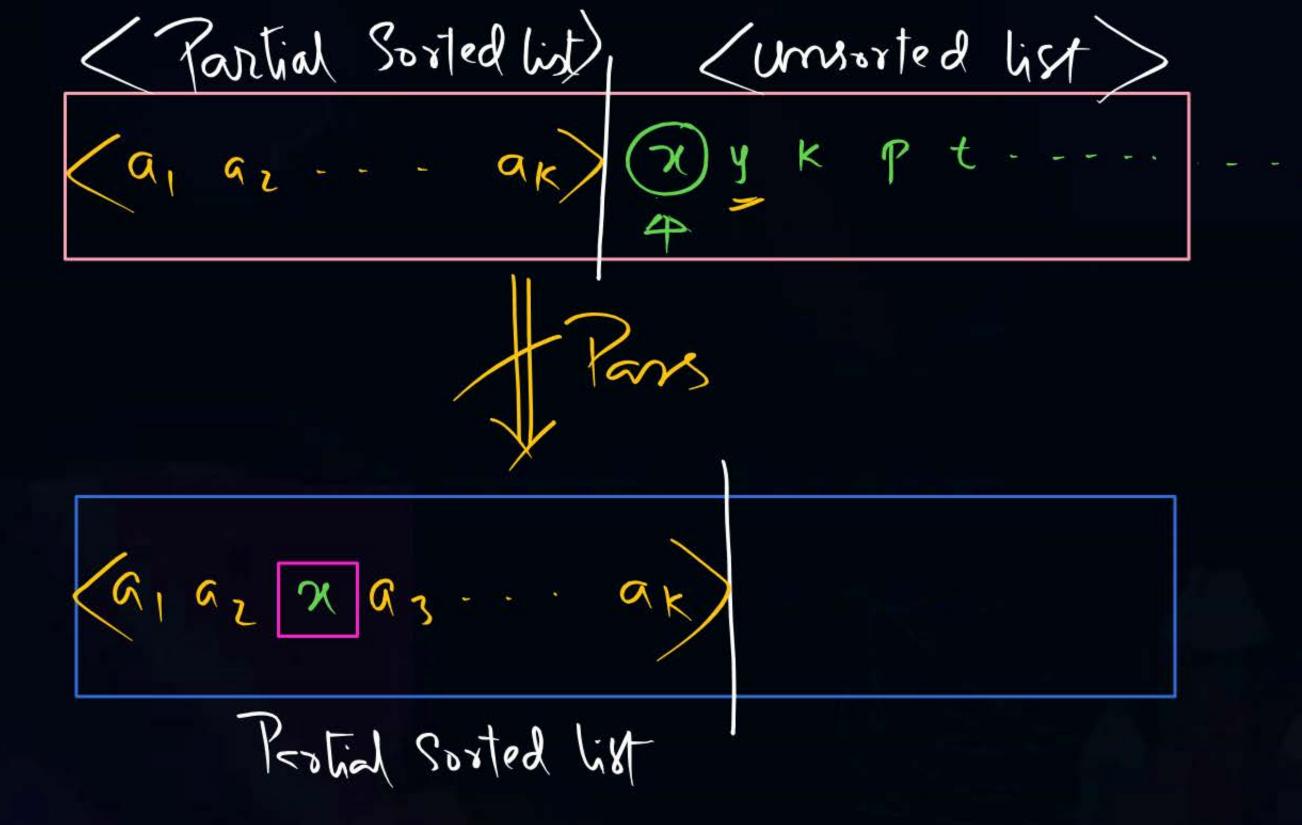
INSERTION SORT

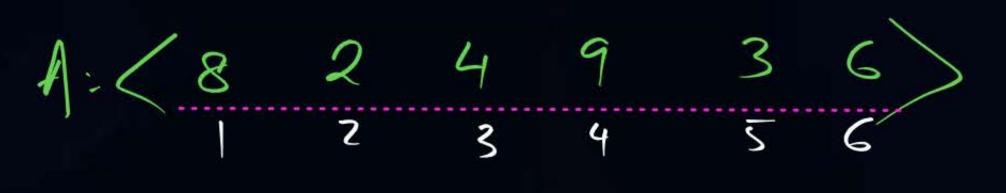
on-line Soot+ Enternal Sort / We property



- Effective for small data sets.
- If the input list is pre-sorted then it takes time of O(n + d); d = number of inversions.
- It is On-line.

Each pass of insertion sort removes an element from the input data set, inserts it into the correct position in the already sorted list.







	1	2	3	4	5	6
Pass 1	8	2	4	9	3	6
Paros 1	12	8>	4	9	3	6
2	12	4	8	9	3	Q
3	< 2	4	8	9	3	C
4	2	3	4	8	9	5
5	2	3	4	6	8	9

INSERTION SORT

Algorithm INSERTION_SORT (A, n)

```
Stable
for j \leftarrow 2 to n
                            Implace
    key \leftarrow A[j];
   i \leftarrow j-1;
   while (i > 0 and A[i] > key) {
           A[i + 1] \leftarrow A[i];
           i \leftarrow i - 1;
   A[i + 1] \leftarrow key;
```

Jime - Complemity: (oft. BS)





- 1) Best Care: Inc. order (4 8 10 11 12 15) -0-Swaps;#9 Invs
 - Worst Case: -> Der order 15 10 8 6 2 $\omega_1 + \omega_2 = \mathcal{O}(\omega_2)$

Radin Sort < Num Comparison - based Sorting (7 = 10) A: 723 64 99 83 -723 83 333 64 4 7 723 124 333 545 64 65 64 65 83 99 124 Pans 3: 4 7 Jime: O(d*(m+b))~O(d*n)

b-base; d=(No. q bit (Disits
for brown No)





Q). Which of the following Sorting algorithms has lowest worst-case complexity?

i. Bubble Sort : n ii. Merge Sort : n logn iii. Quick Sort : n iv. Selection Sort : n

- Which of the following in place Sorting algorithm needs minimum number of Q). swaps? (N.C)
 - (a) Selection Sort

(b) Insertion Sort

(c) Heap Sort

(d) Quick Sort



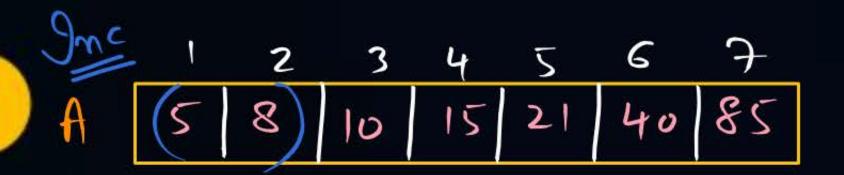


Q). What would be the worst case complexity of Insertion Sort if the inputs are restricted to permutation of 1 to n with at most 'n' Inversions?

Jime:
$$O(n+d)$$
 $d = no \cdot q$ Inversions

 $d = n$
 $O(n+n) = O(n)$







Q). Let 'S' be a Sorted Array of 'n' integers and T(n) denote the time taken for the most efficient algorithm to determine if there are 2 elements in the Array with the sum <1000. 4(A(1)+A(2) < 1000)

(a) T(n) is O(1)

(b) $n \le T(n) \le n \log n$

85 40 21 15 10 8 5

(c) $T(n) = {}^{n}C_{2}$

(d) nlogn <= T(n) < = ${}^{n}C_{2}$ A(n) + A(n-1) < 1000) Print (yes)else print (no)

Q). The traditional Insertion Sort to Sort an Array can be of n elements uses linear search to identify the position where an element is to be inserted into already Sorted part of the Array, if instead binary search is used to identify the position of newly inserted element then the worst case complexity will be order of

 $O(n^2)$. (rs) W. C: $n + m^2 = O(n^2)$ (rs) W. C: $n \cdot \log n + n$ (rs) L.S Partial Sorted Ling unsorted Ling
(a1 a2 · · · · ak) (a)





Q). Which one of the following in place sorting algorithms needs the minimum number of swaps?

(a) Quick sort

(b) Insertion sort

(c) Selection sort

(d) Heap sort





- Q). The worst case running times of Insertion sort, Merge sort and Quick sort, respectively, are:
 - (a) $\Theta(n \log n)$, $\Theta(n \log n)$, and $\Theta(n^2)$
 - (b) $\Theta(n^2)$, $\Theta(n^2)$, and $\Theta(n \log n)$
 - (c) $\Theta(n^2)$, $\Theta(n \log n)$, and $\Theta(n \log n)$
 - (d) $\Theta(n^2)$, $\Theta(n \log n)$, and $\Theta(n^2)$







Q). You have n lists, each consisting of m integers sorted in ascending order.

Merging these lists into a single sorted list will take time:

- (a) O(nm log n)
- (b) O(mn log m)

(c) O(m + n)

(d) O(mn)

Q). If we use Radix Sort to sort n integers in the range $(n^{k/2}, n^k)$, for some k > 0 which

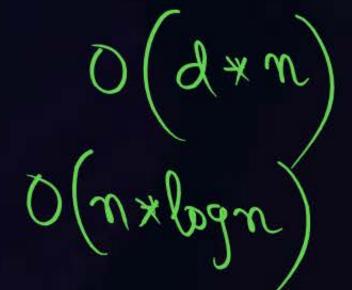
is independent of n, the time taken would be

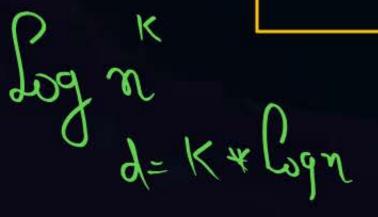
(a) Θ(n)

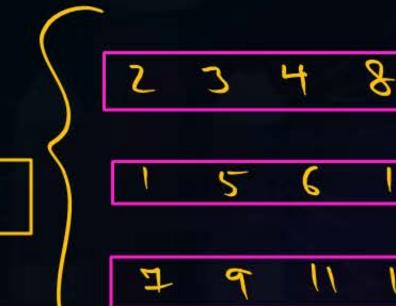
(b) Θ(kn)

(e) $\Theta(n \log n)$

(d) $\Theta(n^2)$





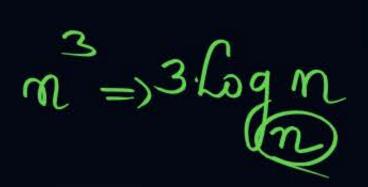






- Q). The worst case running times of Insertion sort, Merge sort and Quick sort, respectively are:
 - (a) $\Theta(n \log n)$, $\Theta(n \log n)$ and $\Theta(n^2)$
 - (b) $\Theta(n^2)$, $\Theta(n^2)$ and $\Theta(n \log n)$
 - (c) $\Theta(n^2)$, $\Theta(n \log n)$ and $\Theta(n \log n)$
 - (d) $\Theta(n^2)$, $\Theta(n \log n)$ and $\Theta(n^2)$







Q). Following algorithm(s) can be used to sort n integers in the range [1..n³] in O(n) time

(a) Heap sort

(b) Quick sort

(c) Merge sort

(d) Radix sort

$$0(d \cdot n)$$

$$0(3 \cdot n) = 0(n)$$

Q). For merging two sorted lists of sizes m and n into a sorted list of size m+n, we require comparisons of

(a) O(m)

(b) O(n)

(c) O(m+n)

(d) O(log m+ log n)





Q). Give the correct matching for the following pairs:



- (B) O(n) (Q) Insertion sort
- (C) O(n log n) (R) Binary search
- (D) O(n²) (S) Merge sort





Q). Assume that the algorithms considered here sort the input sequences in ascending order. If the input is already in ascending order, which of the following are TRUE?

- Quicksort runs in Θ(n²) time
- II. Bubble sort runs in Θ(n²) time
- III. Merge sort runs in $\Theta(n)$ time \times
- IV. Insertion sort runs in Θ(n) time
- (a) I and II only
- (c) II and IV only

- (b) I and III only
- (d) I and IV only



THANK - YOU