

COMPUTER SCIENCE



Database Management System

Transaction & Concurrency Control

Lecture_8

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An orange diamond-shaped sign with a black border and the text 'TOPICS TO BE COVERED' in black capital letters.

TOPICS
TO BE
COVERED

A red diamond-shaped sign with a white border and the number '01' in white.

01

Recoverable Schedule



Total # of Concurrent
Schedule.

→ Serial Schedule

→ Non Serial Schedule.



$T_1: 2$

$T_2: 3$

$T_3: 4$

$$\text{Total \# Concurrent Schedule} = \frac{(2+3+4)!}{(2!)(3!)(4!)} = \underline{1260} \text{ Ans}$$

$$\text{Serial Schedule} = 3! = 6 \text{ Serial Schedule} \text{ Ans}$$

$$\text{Non Serial Schedule} = 1260 - 6 = \underline{1254} \text{ Ans}$$

Finding Total Number of concurrent Schedule

T ₁	T ₂
R ₁ (A) W ₁ (A)	R ₂ (B) W ₂ (B)

T ₁	T ₂
L ₁ L ₂	L ₃ L ₄

T ₁	T ₂
0 0	1 1

$L_1L_2L_3L_4$
 $L_3L_4L_1L_2$

$L_1L_3L_2L_4$ (or) $L_1L_3L_4L_2$

$L_3L_1L_4L_2$ (or) $L_3L_1L_2L_4$

T ₁	T ₂
R(A) W(A)	R(B) W(B)

$S_1 \langle T_1T_2 \rangle$
 (1)

T ₁	T ₂
R(A) W(A)	R(B) W(B)

$S_2 \langle T_2T_1 \rangle$
 (2)

T ₁	T ₂
R(A) W(A)	R(B) W(B)

(3)

T ₁	T ₂
R(A) W(A)	R(B) W(B)

(4)

T ₁	T ₂
R(A) W(A)	R(B) W(B)

(5)

T ₁	T ₂
R(A) W(A)	R(B) W(B)

(6)

$$\text{Total \# Concurrent Schedule} = \frac{(n_1 + n_2)!}{(n_1)!(n_2)!}$$

$$= \frac{(2+2)!}{(2)!(2)!} = \frac{4 \times 3 \times 2}{2 \times 2} = 6$$

$T_1 \rightarrow n_1$ operation
2 operation

$T_2 \rightarrow n_2$ operation
2 operation

$$\text{Total Concurrent} = 6$$

$$\begin{aligned} \text{Total non serial Schedule} &= \text{Total Concurrent} - \text{Serial schedule}(m!) \\ &\quad m: \# \text{ of transaction} \\ &= 6 - 2 \end{aligned}$$

$$\text{Serial} = 2$$

$$\text{Total non Serial} = 4$$

NOTE:

The Number of Concurrent schedule that can be formed
Over m transaction having n_1 n_2 n_3 n_m operation respectively

$$\text{Total \# of Concurrent Schedule} = \frac{(n_1 + n_2 + n_3 + \dots + n_m)!}{(n_1!)(n_2!)(n_2!) \dots (n_m!)}$$

$$\text{Total \# of Non Serial Schedule} = \frac{(n_1 + n_2 + n_3 + \dots + n_m)!}{(n_1!)(n_2!)(n_2!) \dots (n_m!)} - m!$$

① A → Atomicity

✓ C → Consistency → Programmer → 'Consistent'

✓ I → Isolation → 'Serializability'

② D → Durability

→ Recoverability

Serializability

[Consistent]

- Conflict Serializable
- View Serializable

Recoverability

[Must be able to Recover
Under Any Case of failure]

- Recoverable Schedule
- Cascadeless Schedule
- Strict Recoverable Schedule.



Recoverability.



Complete
Schedule : Commit

Abort

✓

& Read by another

Dependency

→ ① ④ ⑥



(1)

T_1	T_2
$W(A)$ \vdots \vdots Commit	$R(A)$

YES.

(2)

T_1	T_2
$W(A)$ <u>commit</u>	$R(A)$ \vdots

No

(3)

T_1	T_2
$W(A)$ rollback	$R(A)$

No

(4)

T_1	T_2
$W(A)$	$w(A)$

No

(5)

T_1	T_2
$W(A)$	$W(A)$ $R(A)$

No

(6)

T_1	T_2
$W(A)$	$W(B)$ $R(A)$
$R(B)$	

YES.

Dependency



(1)

T_1	T_2
<u>W(A)</u> ⋮ Commit	<u>R(A)</u>

YES (T_2 Depends on T_1)
Here T_2 Read a value of DATA Item 'A' that is written by Uncommitted Transaction T_1 .

(2)

T_1	T_2
W(A) <u>commit</u>	<u>R(A)</u> ⋮

No Dependency
 T_2 , Not Depend on T_1
Bcz T_1 Committed

(3)

T_1	T_2
<u>A=100</u> <u>A=500</u> W(A) <u>rollback</u>	R(A) <u>A=100</u>

No Dependency
Bcz T_1 fail then Rollback.

Dependency



Uncommitted Read

Update by one uncommitted transaction & Read by another transaction.

(Not Uncommitted / Dirty) Read.

No Dependency

No Dependency.

(4)

T ₁	T ₂
<u>W(A)</u>	<u>w(A)</u>

(5)

T ₁	T ₂
<u>W(A)</u>	<u>W(A)</u> R(A)

A=500

A=25000

(6)

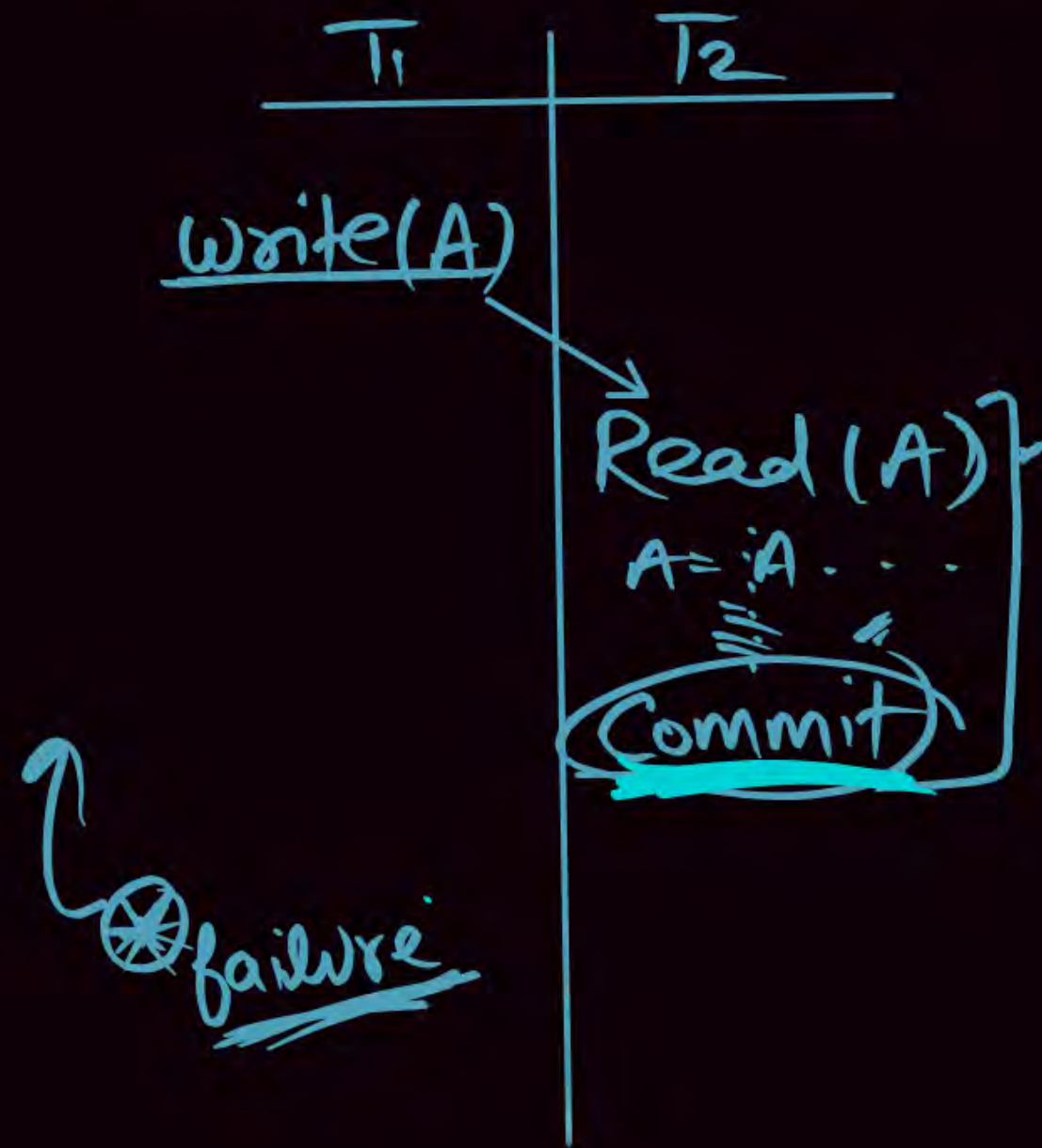
T ₁	T ₂
W(A) R(B)	W(B) R(A)

T₂ Depends on T₁

T₁ Depends on T₂.

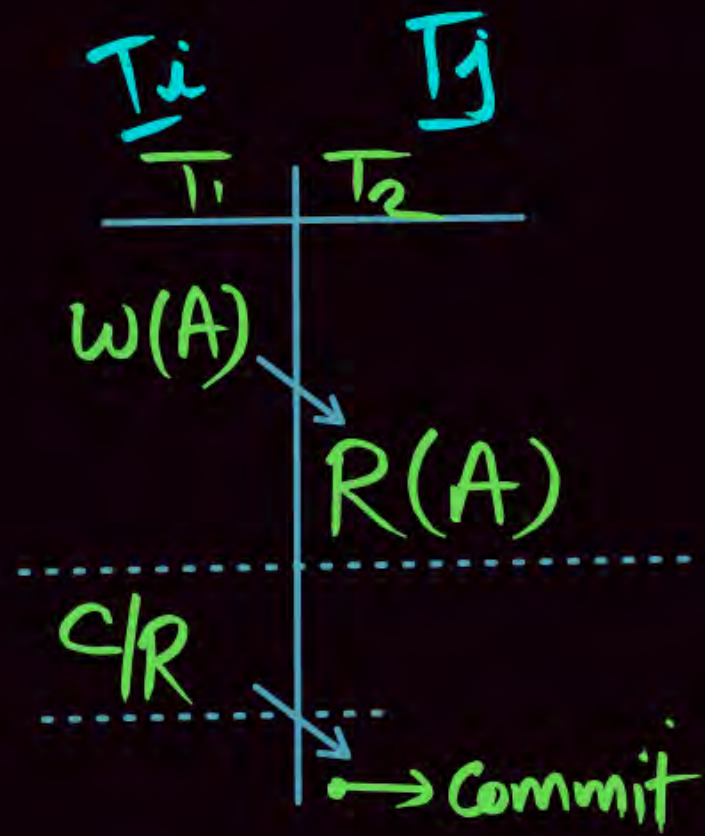
YES, Dep.

IR-Recoverable | Non-recoverable Schedule.



'X'

Recoverable Schedule:



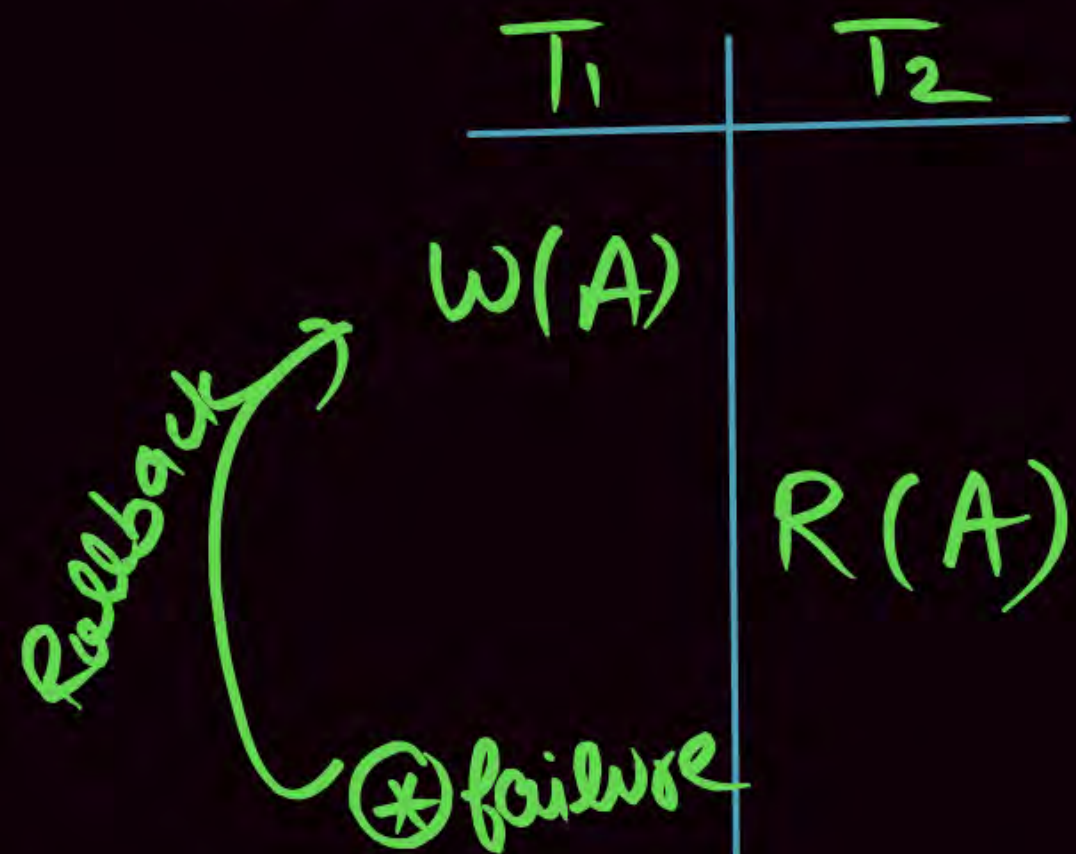
Recoverable
Schedule

Recoverable Schedule is one, where for each pair of transaction T_i & T_j such that, if T_j Read a Data Item, that was previously written by T_i then Commit of T_i appear before Commit of T_j .

(OR)

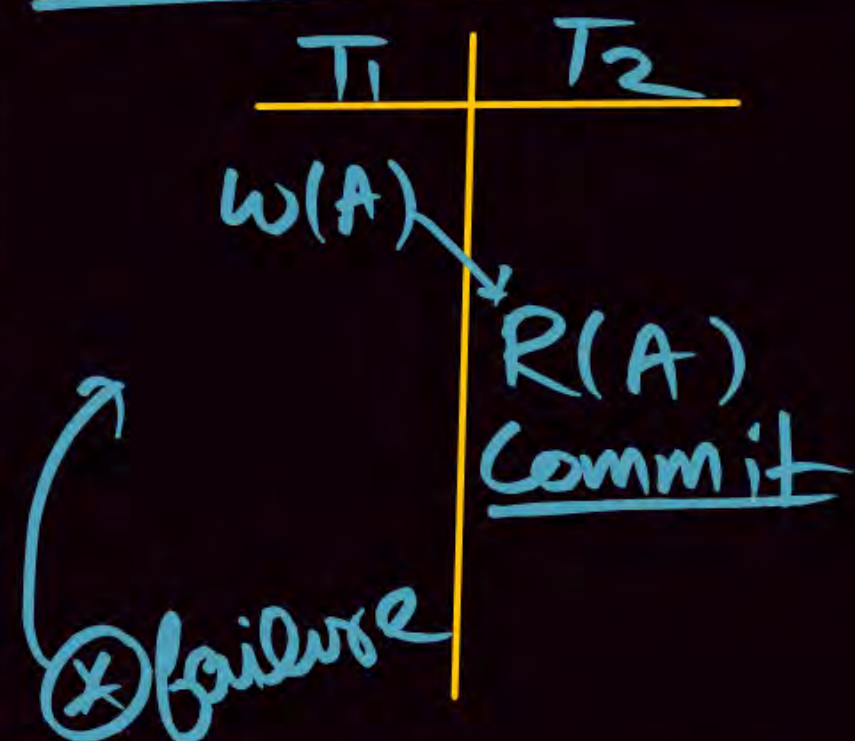
If T_2 Depends on T_1 (T_2 Read a Value written by uncommitted transaction) then Commit of T_2 must be Delayed until Commit/Rollback of T_1 .

Recoverable Schedule



If T_1 fail then T_1 Rollback
& Due to Dependency T_2 also Rollback

Irrecoverable Schedule.



If T_1 failure then T_1
Tries to Rollback But this
value Read by T_2 & T_2
Commit so Not able to
Recover.

T_1	T_2
$w(A)$	
	$R(A)$
c/r	

→ Commit

Recoverable
Schedule

C : Commit

R : Rollback

C_1 : Commit of transaction T_1 .

C_2 : Commit of transaction T_2 .

Recoverable Schedules

Need to address the effect of transaction failures on concurrently running transactions.

- ❑ Recoverable schedule — if a transaction T_j reads a data item previously written by a transaction T_i , then the commit operation of T_i appears before the commit operation of T_j .
- ❑ The following schedule is not recoverable

T_8	T_9
read(A)	
<u>write(A)</u>	Read(A)
	<u>commit</u>
read(B)	

Is recoverable

Non Recoverable

- If T_8 should abort, T_9 would have read (and possibly shown to the user) an inconsistent database state. Hence, database must ensure that schedules are recoverable.

Examples



3, 4, 5 & 6 Recoverable

(1)

T_1	T_2
$w(A)$	
	$R_1(A)$
	$C_2(\text{commit})$
Rollback	

Irrecoverable.

(3)

T_1	T_2
$w(A)$	
$C R$	$R(A)$

Recoverable

(5)

T_1	T_2
$w(A)$	
	$R(A)$
	rollback
$C R$	

Recoverable

(2)

T_1	T_2
$w(A)$	
	$R(A)$
	C_2
C_1	

Irrecoverable

(4)

T_1	T_2
$w(A)$	
	$w(A)$
	$R(A)$
	commit
Commit/ Rollback	

Recoverable

(6)

T_1	T_2
$w(A)$	
	$R(A)$
$C R$	
	$C R$

Recoverable

Recoverable Schedule.

- ① WR / Dirty Read / Uncommitted Problem.
- ② WW / Lost Update Problem.
- ③ RW Problem
- ④ Cascading Rollback are there.



NOTE: Recoverable schedule may or may not be free from

- ☐ ① WR problem / uncommitted Read
- ☐ ② RW Problem
- ☐ ③ WW Problem

T_1	T_2
<u>R(A)</u>	<u>W(A)</u>
Commit	Commit

Recoverable
But RW Problem

T_1	T_2
<u>W(A)</u>	<u>W(A)</u>
Commit	Commit

Recoverable
But WW Problem

T_1	T_2
R(A) <u>W(A)</u>	<u>R(A)</u>
<u>W(B)</u>	<u>R(B)</u>
Commit	Commit

Recoverable
But WR Problem

Cascading Rollback are possible.

T_1	T_2	T_3	T_4	T_5
W(A)	R(A)	R(A)	R(A)	R(A)

Rollback
⊗ failure

Here T_2, T_3, T_4 & T_5
Depends on Transaction T_1 .

If T_1 fails then T_1 Roll back.
then Due to Dependency
 T_2, T_3, T_4 & T_5 also Roll back.

Cascading Rollbacks

❑ Cascading rollback – a single transaction failure leads to a series of transaction rollbacks. Consider the following schedule where none of the transactions has yet committed (so the schedule is recoverable)

T_{10}	T_{11}	T_{12}
read(A) read(B) write(A) abort	read(A) write(A)	read(A)

If T_{10} fails, T_{11} and T_{12} must also be rolled back.

❑ Can lead to the undoing of a significant amount of work

② Cascadeless Schedule:

T_1	T_2
$w(A)$	
c/r	
	$R(A)$

A Cascadeless Schedule is one where for each pair of Transaction T_i & T_j such that T_j Read a Data Item that was previously written by T_i , then Commit of T_i appear before Read of T_j .

(OR)

Not allowed UnCommitted Read.

Cascadeless Schedules

Cascadeless Rollback Recoverable

- ❑ Cascadeless schedules — cascading rollbacks cannot occur;
- ❖ For each pair of transactions T_i and T_j such that T_j reads a data item previously written by T_i , the commit operation of T_i appears before the read operation of T_j .
- ❑ Every cascadeless schedule is also recoverable

T_1	T_2
$W(A)$ C/R	$R(A)$

Cascadeless Schedule

①

T ₁	T ₂
W(A)	R(A)
CLR	

1-Commit

Recoverable.

②

T ₁	T ₂
W(A)	
CLR	
	R(A)

CasCadeless.

③

T ₁	T ₂
W(A)	
CLR	
	R(A)/W(A)

Strict Recoverable
 (or)
 STRICT Schedule.

NOTE: Cascadeless schedule may or may not be free from

- ☐ RW Problem
- ☐ WW Problem

T_1	T_2
R(A)	W(A) Commit
Commit	

Cascadeless
But RW Problem

T_1	T_2
W(A)	W(A) Commit
Commit	

Cascadeless
But WW Problem



Strict Recoverable Schedule

T_1	T_2
$W(A)$ $C R$	$R(A) w(A)$

No WR Problem.
No WW Problem.
Only RW Problem.

NOTE: Strict Recoverable schedule may or may not be free from
□ RW Problem

T_1	T_2
R(A) Commit	W(A) Commit

Strict Recoverable
But RW Problem

(1)

T_1	T_2
W(A)	R(A)
C R	Commit

Recoverable

(2)

T_1	T_2
W(A) C R	R(A)

Cascadeless

(3)

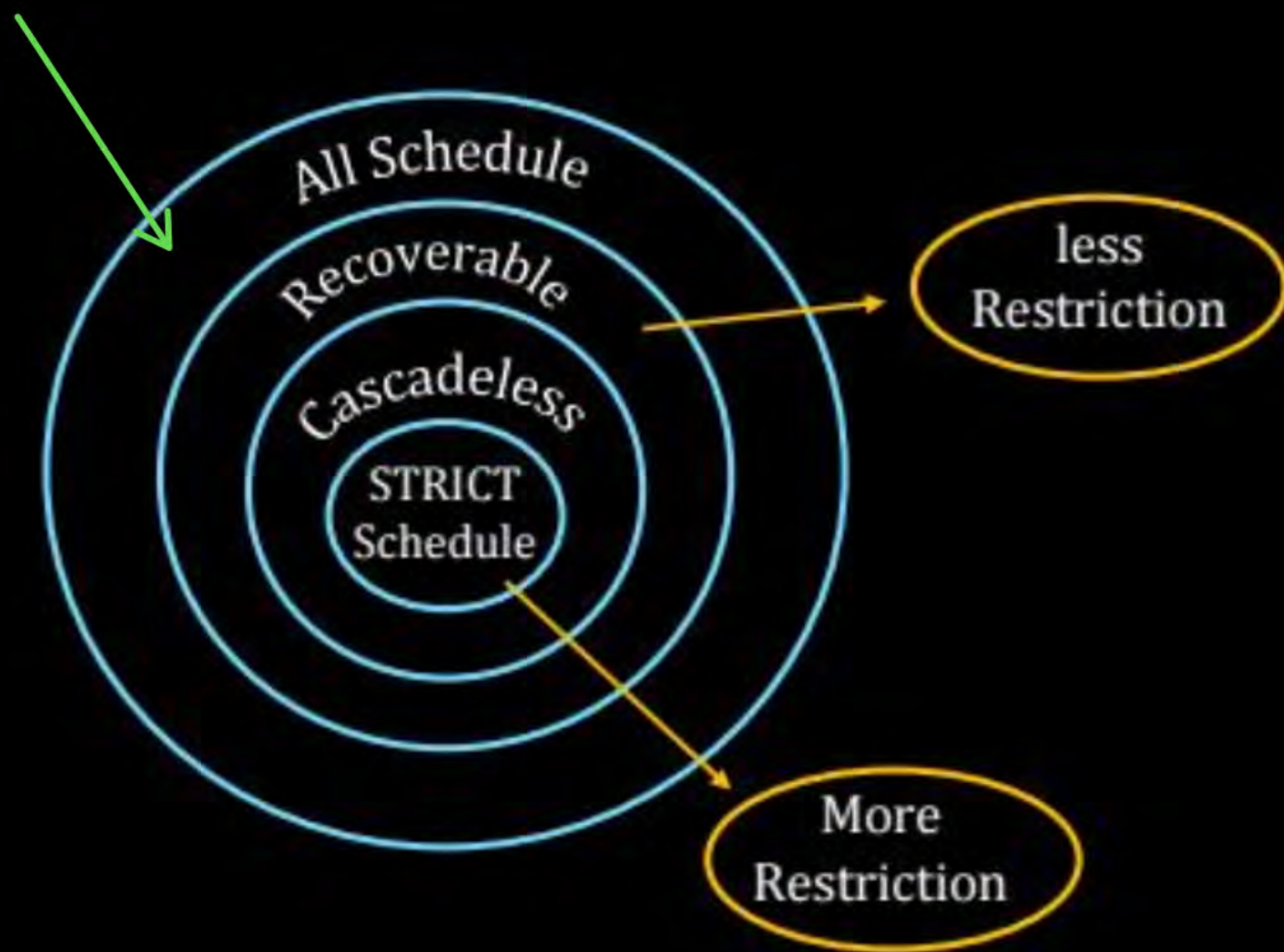
T_1	T_2
W(A) C R	R(A)/W(A)

Strict
schedule

WR Problem
WW
RW
Cascading Rollback

WW Problem
RW

RW Problem

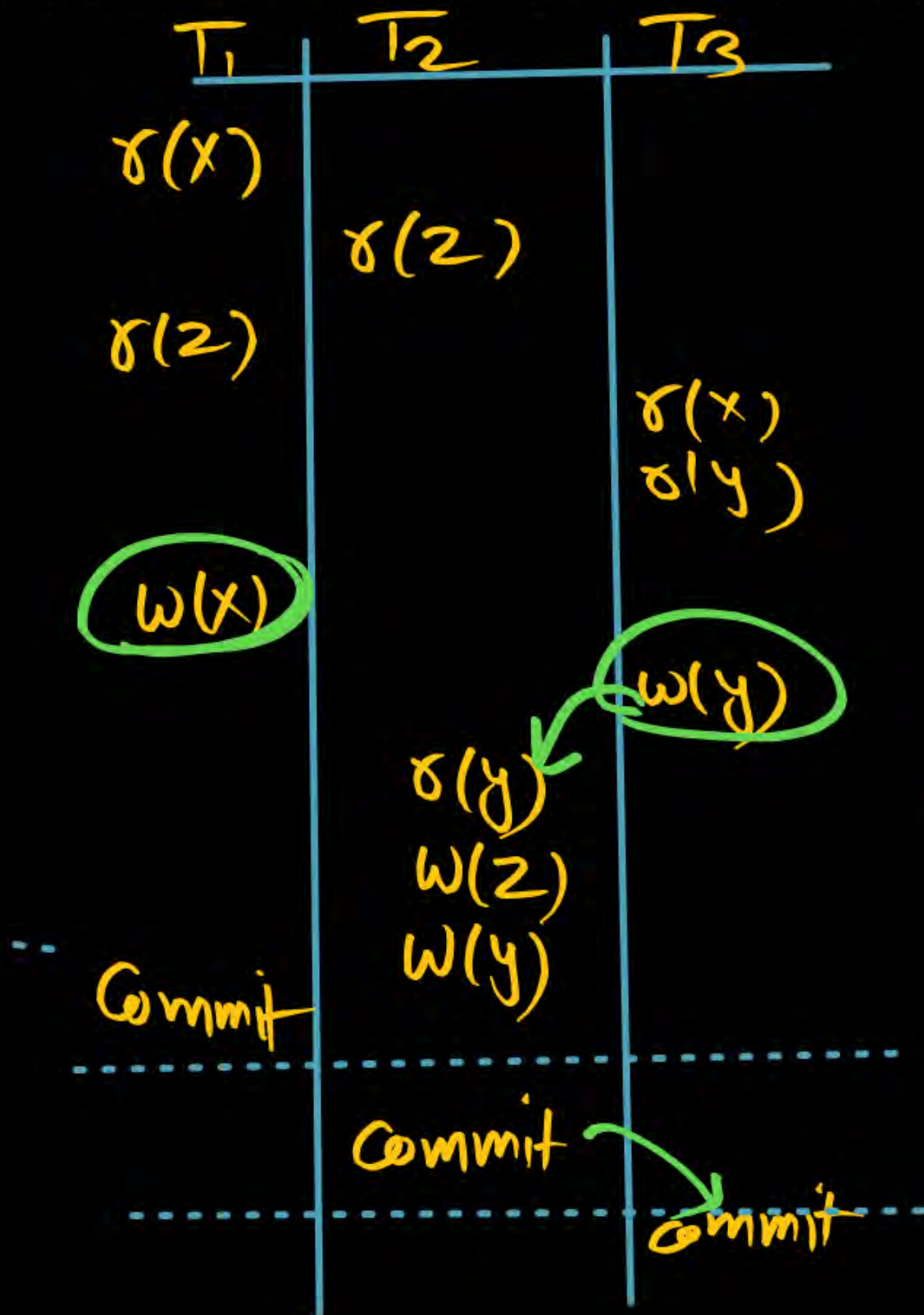


Q.



$r_1(x)r_2(z)r_1(z)r_3(x)r_3(y)w_1(x)w_3(y)r_2(y)w_2(z)w_2(y) C_1 C_2 C_3$

↓
Commit 3



$W \rightarrow R$

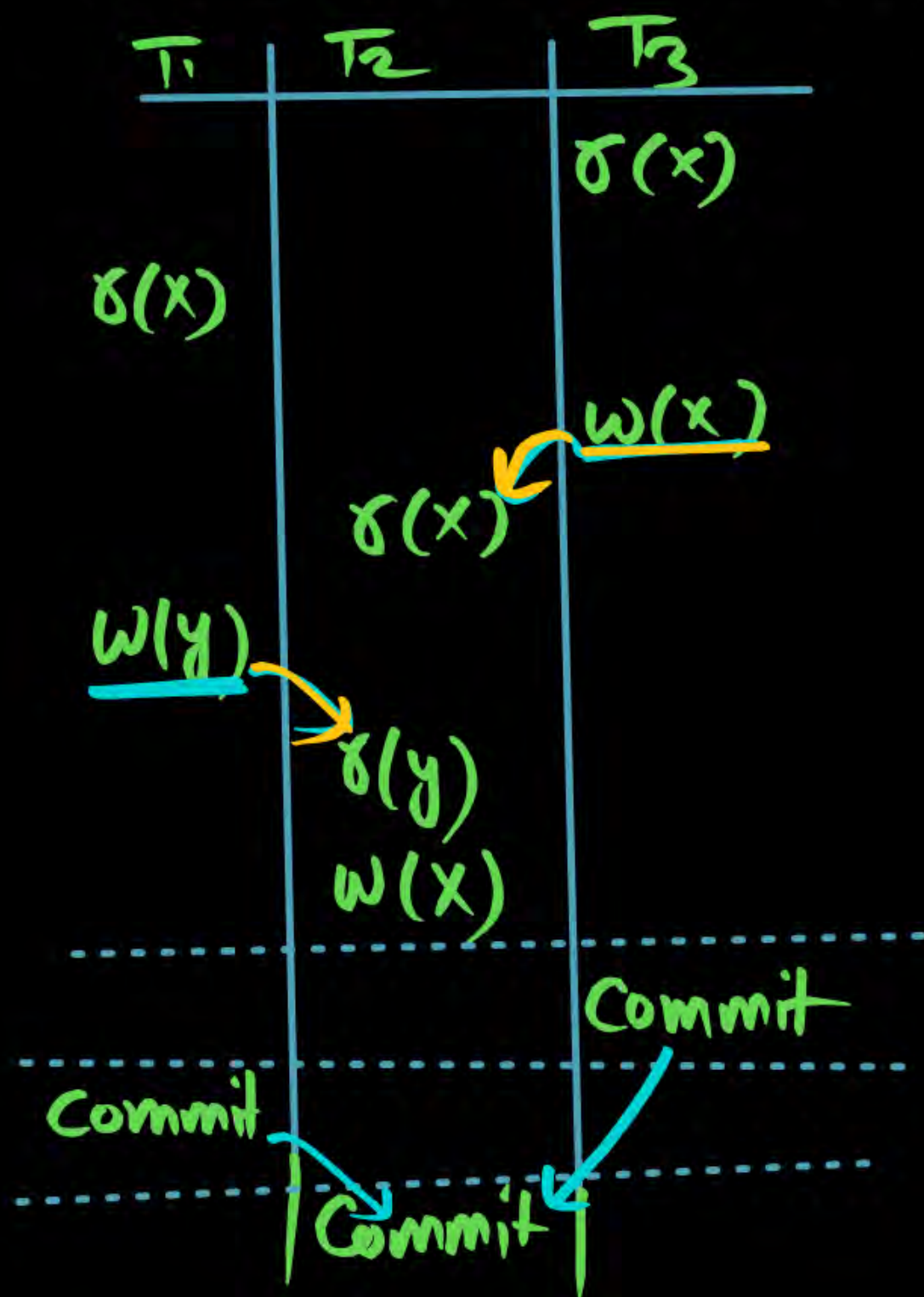
X Recoverable

Non Recoverable

Q.



$r_3(x) \ r_1(x) \ w_3(x) \ r_2(x) \ w_1(y) \ r_2(y) \ w_2(x) \ C_3 \ C_1 \ C_2$



✓ Recoverable.

✗ Cascadeless.

Bcz on Data Item x & y
UnCommitted Read.

Q.

$r_1(x) r_2(x) w_1(y) w_2(y) r_2(y) C_1 C_2$



T_1	T_2
$r(x)$	$r(x)$
<u>$w(y)$</u>	$w(y)$
Commit	$r(y)$
	Commit

✓ Recoverable

✓ Cascadeless

[No UnCommitted Read]
(No WR Case)

✗ Strict Recoverable

Q.68



Consider the following database schedule with two transactions, T_1 and T_2 .

$S = r_2(X); r_1(X); r_2(Y); w_1(X); r_1(Y); w_2(X); a_1; a_2$

where $r_i(Z)$ denotes a read operation by transaction T_i on a variable Z , $w_i(Z)$ denotes a write operation by T_i on a variable Z and a_i denotes an abort by transaction T_i

Which one of the following statements about the above schedule is TRUE?

[MCQ:2016–2M]

- ☐ A S is non-recoverable
- ☐ B S is recoverable, but has a cascading abort
- ☐ C S does not have a cascading abort
- ☐ D S is strict



Let S be the following schedule of operations of three transactions T_1 , T_2 and T_3 in a relational database system:

$R_2(Y), R_1(X), R_3(Z), R_1(Y), W_1(X), R_2(Z), W_2(Y), R_3(X), W_3(Z)$

Consider the statements P and Q below:

P : S is conflict-serializable.

Q : If T_3 commits before T_1 finishes, then S is recoverable.

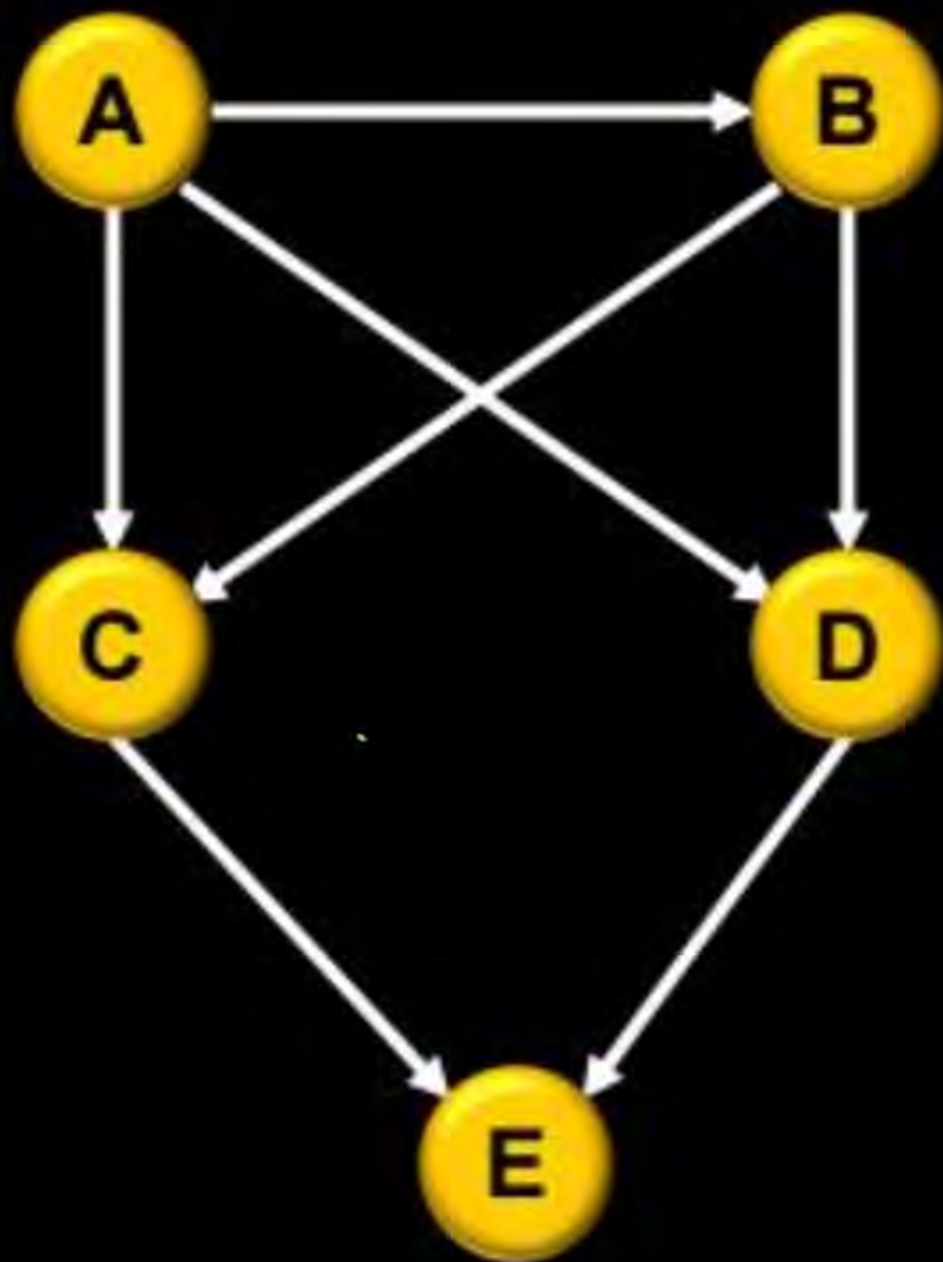
Which one of the following choices is correct?

[MCQ: 2021-2M]

- A** Both P and Q are true.
- B** P is true and Q is false.
- C** P is false and Q is true.
- D** Both P and Q are false.

Topological Sorting

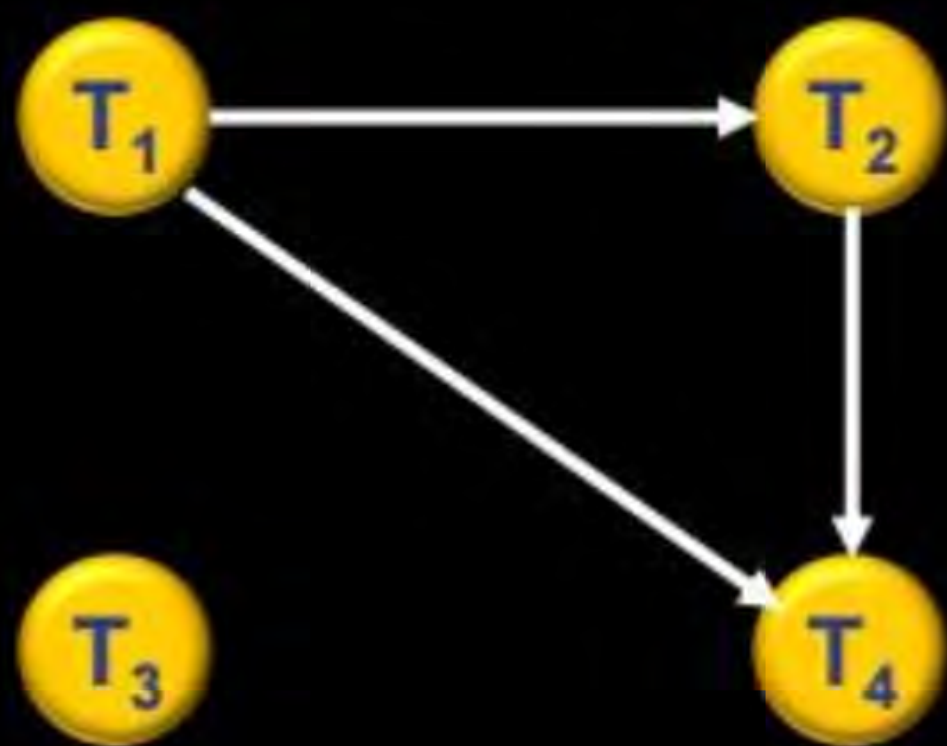
Q.



Topological Sorting



Q.



Q

T_1

T_2

T_2

T_4

T_3

I

II

III

~~T_1~~

T_3

①

T_2

②

T_4

③

①

T_1

②

T_2

③

T_4

④

= 4

—

T_2

—

T_1

—

T_4

—

= 4

—

T_2

—

T_4

—

T_1

—

= 4

12) Ans

Topological Sorting

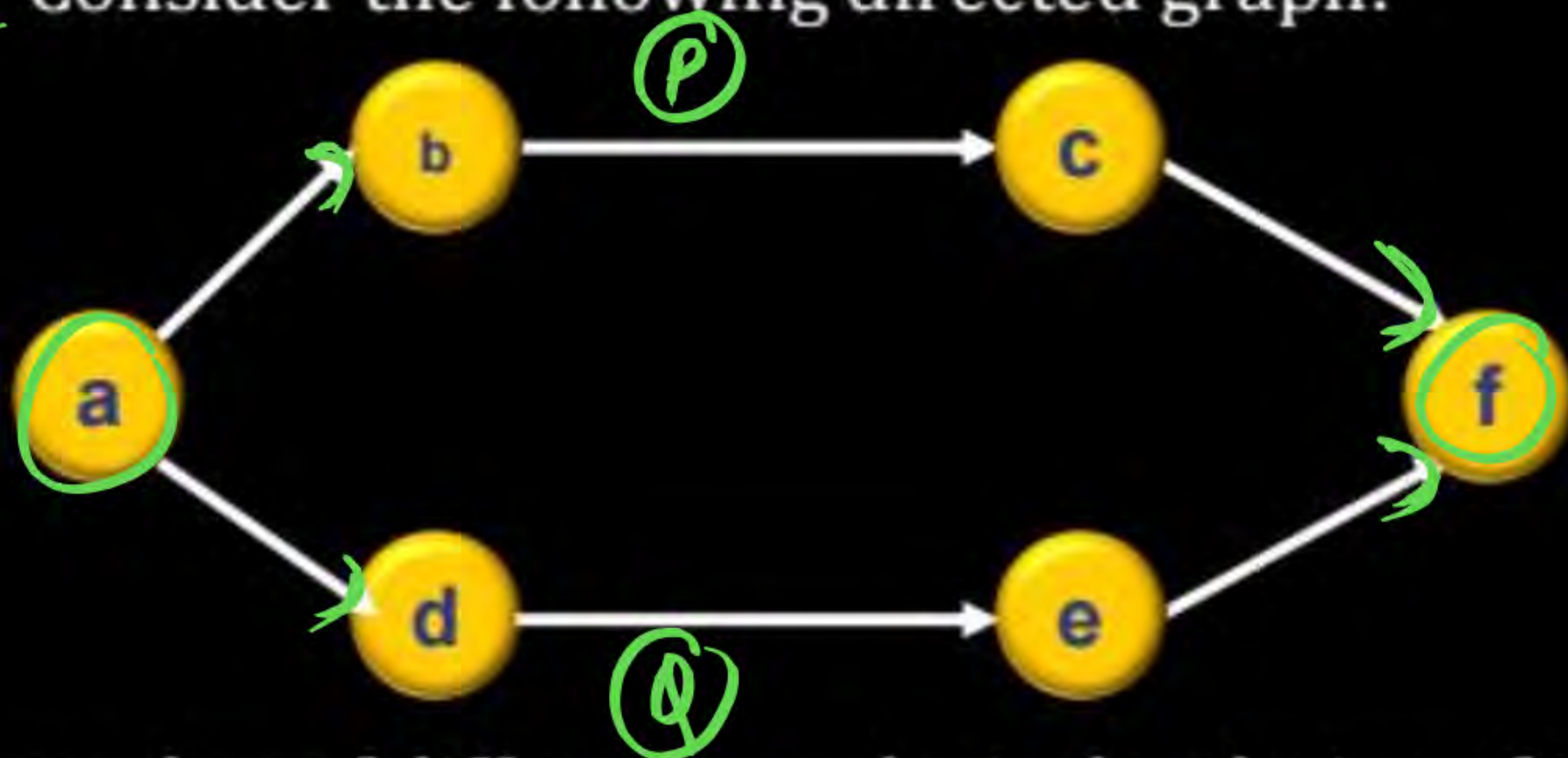
Q.

$R_4(A)$ $R_2(A)$ $R_3(A)$ $W_1(B)$ $W_2(A)$ $R_3(B)$ $W_2(B)$

Topological Sorting

Q. 70

Consider the following directed graph:



a b c d e f
a d e b c f
a b d c e f
a b d e c f
a d b e c f
a d b c e f

The number of different topological ordering of the vertices of the graph is _____.

[MCQ: 2016]



**THANK
YOU!**

