

COMPUTER SCIENCE

Database Management System

File Org. & Indexing

Lecture _3



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A graphic of a construction barrier with orange and white diagonal stripes and two yellow bollards at the top.

**TOPICS
TO BE
COVERED**

01

File Structure & Indexing

02

B Tree & B+ Tree

Indexing

① P.T

② C.T

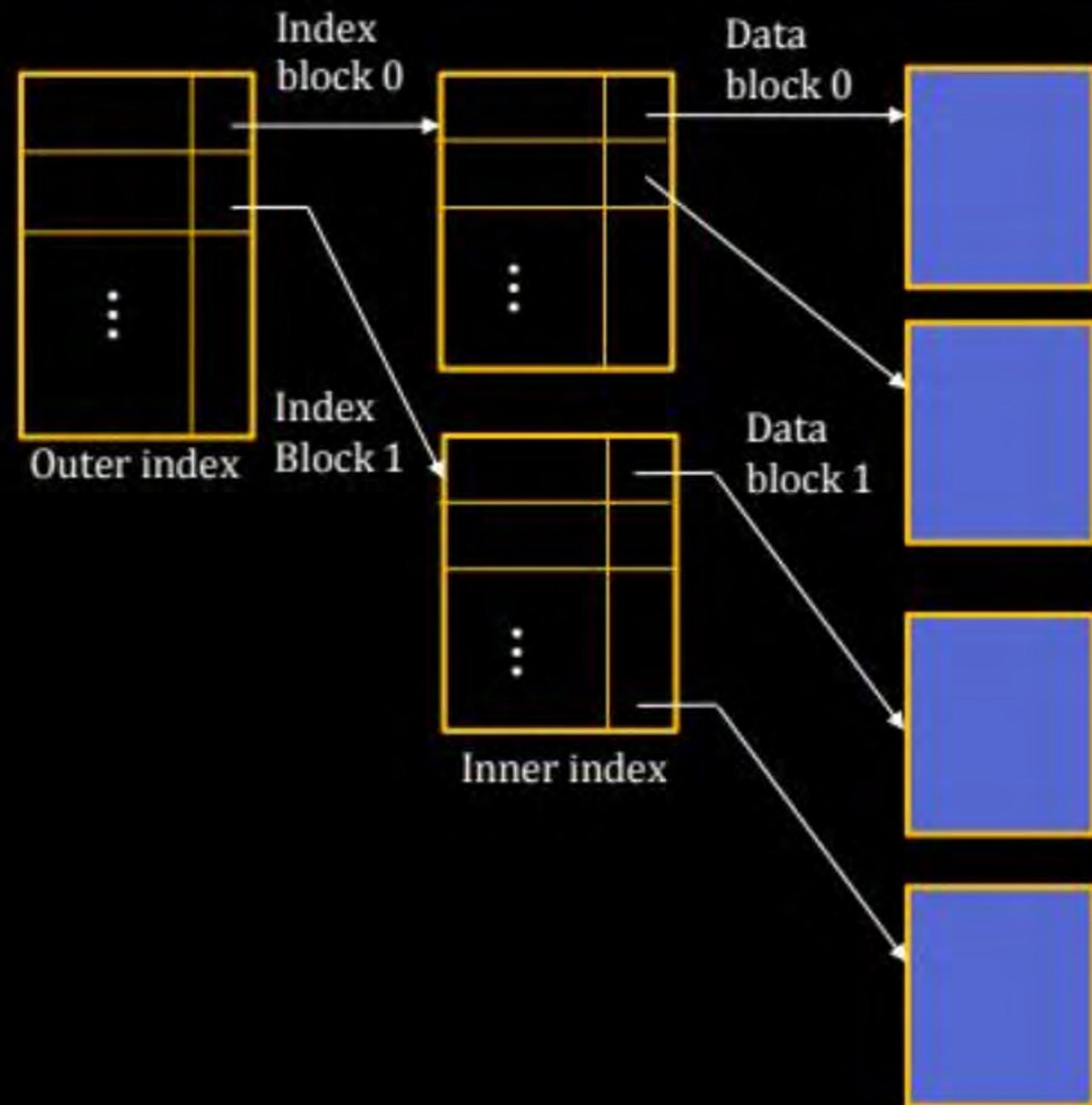
③ S.T

Multilevel Indexing

Multilevel Index

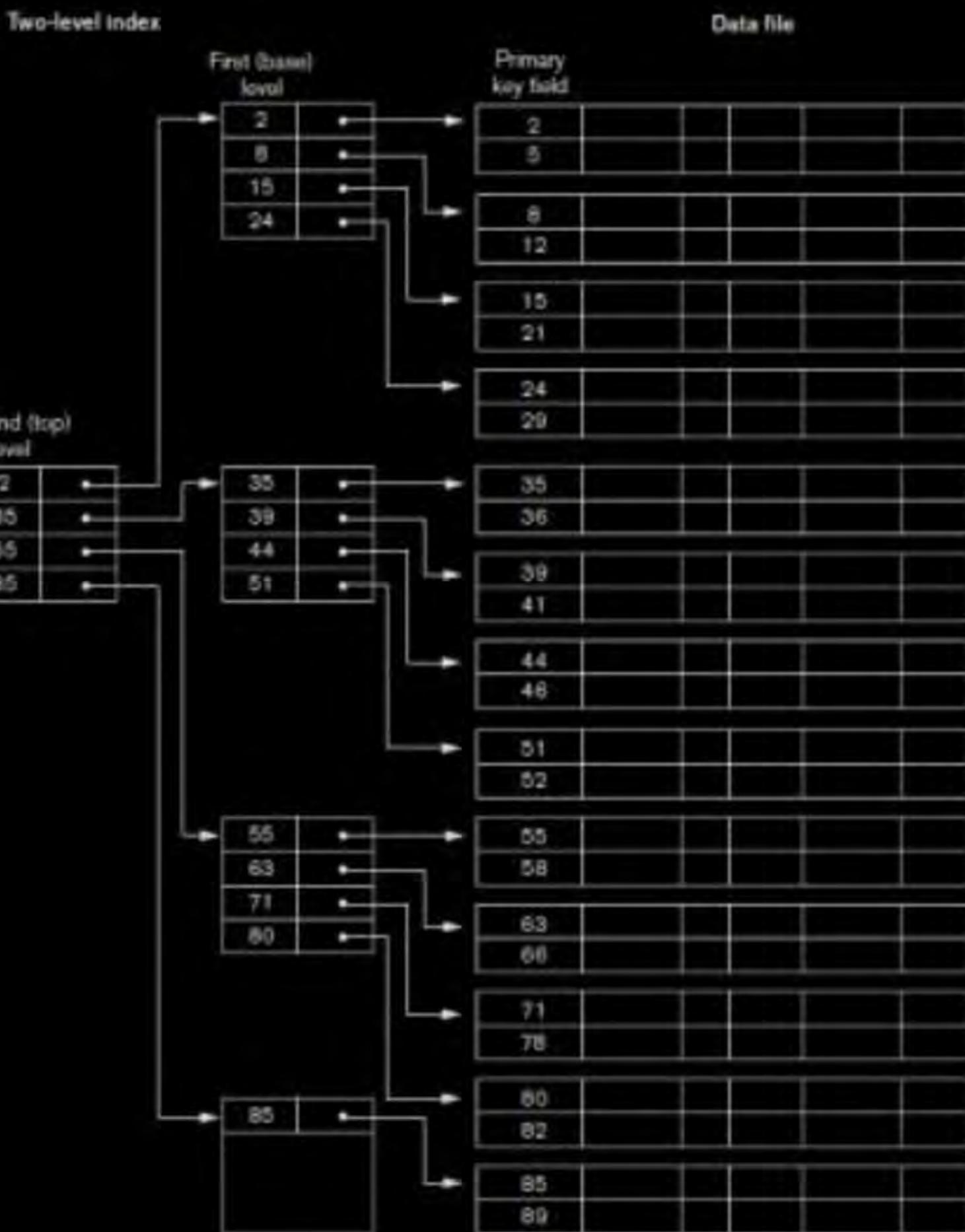
- ❑ If index does not fit in memory, access becomes expensive.
- ❑ Solution: treat index kept on disk as a sequential file and construct a sparse index on it.
 - ❖ outer index - a sparse index of the basic index
 - ❖ inner index - the basic index file
- ❑ If even outer index is too large to fit in main memory, yet another level of index can be created, and so on.
- ❑ Indices at all levels must be updated on insertion or deletion from the file.

Multilevel Index (Contd..)



Multilevel Indexes

- ❑ Designed to greatly reduce remaining search space as search is conducted
- ❑ Index file
 - ❖ Considered first (or base level) of a multilevel index
- ❑ Second level
 - ❖ Primary index to the first level
- ❑ Third level
 - ❖ Primary index to the second level



A two-level primary index resembling ISAM (indexed sequential access method) organization

NOTE: We can Repeat the above process until index entries fit into One Block.

NOTE: If there are n level in multilevel index then the number of Block Access to search for a record = $n + 1$
(at each level One Index Block + 1 Data Block)

Q.3

Find the average number of block access required to search for a record if multilevel Index is created on the Data file of Question 2.



Block factor of Index file = 68 Index entries per Block

Ist Level: Total number of Index Block = 442 Index Block

IInd Level: number of Index Records (entries) = 442 (SPARSE number of Ist level block) & Block factor = 68 Index entries for block

Total number Index Block = $\left\lceil \frac{442}{68} \right\rceil = 7$ Index Block

IIIrd Level: Number of Index Record = 7 (number of 2nd level block)

Total number of index Block = $\left\lceil \frac{7}{68} \right\rceil = 1$

Average Number of block Access = 1 + 1 + 1 + 1 = 4

Q.1

A clustering index is defined on the fields which are of type

P
W

[GATE-2008 : 1 Mark]

- A Non-key and ordering
- B Non-key and non-ordering
- C key and ordering
- D key and non-ordering

Q.2

Consider a file of 16384 records. Each record is 32 bytes long and its key field is of size 6 bytes. The file is ordered on a non-key field, and the file organization is unspanned. The file is stored in a file system with block size 1024 bytes, and the size of block pointer is 10bytes. If the secondary index is built on the key field of the file, and a multilevel index scheme is used to store the secondary index, the number of first-level and second-level block in the multilevel index are respectively [GATE-2008 : 2 Marks]

- A 8 and 0
- B 128 and 6
- C 256 and 4
- D 512 and 5



TREE
Binary Tree [At Most Degree = 2]
BST.
AVL

B Tree Definition

Balanced Tree

P
W

DSA

ORDER : P

Max. element = P - L

Min. element = $\lceil \frac{P}{2} \rceil - 1$

ORDER : P

Max. key = P - L

Min. key = $\lceil \frac{P}{2} \rceil - L$

③ ORDER: 5

Max. keys = 5 - 1 = 4

Minimum keys = $\lceil \frac{5}{2} \rceil - 1 = 3 - 1 = 2$

BP

Dynamic Multi Level Indexing

B Tree

ORDER : P

(*) $B_P : P$

key = P - 1

R_P = P - 1



B Tree Definition**Balanced Tree****① ORDER : 2**

$$B_P = 2$$

$$\text{key} = 1$$

$$R_P = \perp$$

**② ORDER : 3**

$$B_P = 3$$

$$\text{Keys} = 2$$

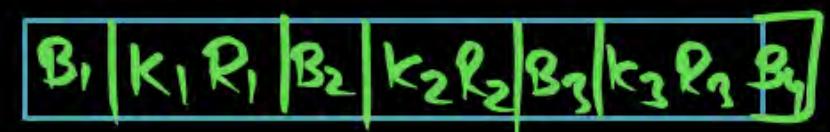
$$R_P = 2$$

**③ ORDER : 4**

$$B_P = 4$$

$$\text{key} = 3$$

$$R_P = 3$$

**④ ORDER : 5**

$$B_P = 5$$

$$\text{key} = 4$$

$$R_P = 4$$

**⑤ ORDER : 6**

$$B_P = 6$$

$$\text{key} = 5$$

$$R_P = 5$$

**⑥ ORDER : P**

$$B_P = P$$

$$\text{Keys} = P - 1$$

$$R_P = P - 1$$

B Tree Definition

Balanced Tree

BSX

ORDER : P

$B_P = P$

Max. keys = P-L

$R_P = P-L$

Min keys = $\lceil \frac{P}{2} \rceil - L$



ORDER : 5

② 1, 5, 3, 7, 9, 11

$B_P = 5$
max key = 4

min key = $\lceil \frac{P}{2} \rceil - 1 = 2$

1	3	5	7
9			

BTree
Condition Violate

11	3	5	7	9
9				

B Tree Definition

Balanced Tree

DBMS

$$\text{ORDER : } P$$

$$B_P = P.$$

$$\text{Max. keys} = \underline{P-L}$$

$$R_P = \underline{P-L}$$

$$\text{Min keys} = \lceil \frac{P}{2} \rceil - L$$

ORDER: 5

$$B_P = 5$$

$$\text{key} = 4$$

$$R_P = 4$$

(e)

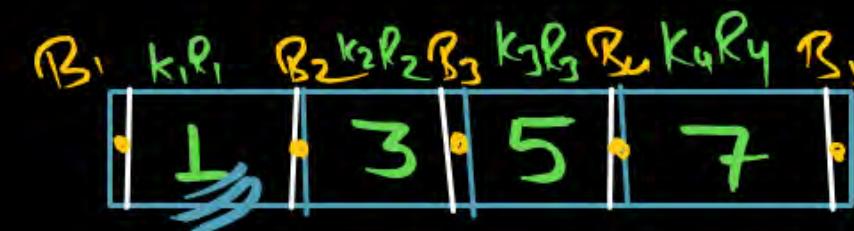
ORDER: 5

1, 5, 3, 7, 9, 11

$$B_P = 5$$

$$\text{max key} = 4$$

$$\text{min key} = \lceil \frac{P}{2} \rceil - 1 = 2$$



BTree

Condition Violate



Height: 1



B Tree DefinitionBalanced TreeDS^A ORDER: 4

$$\text{Max key} = 4 - 1 = 3$$

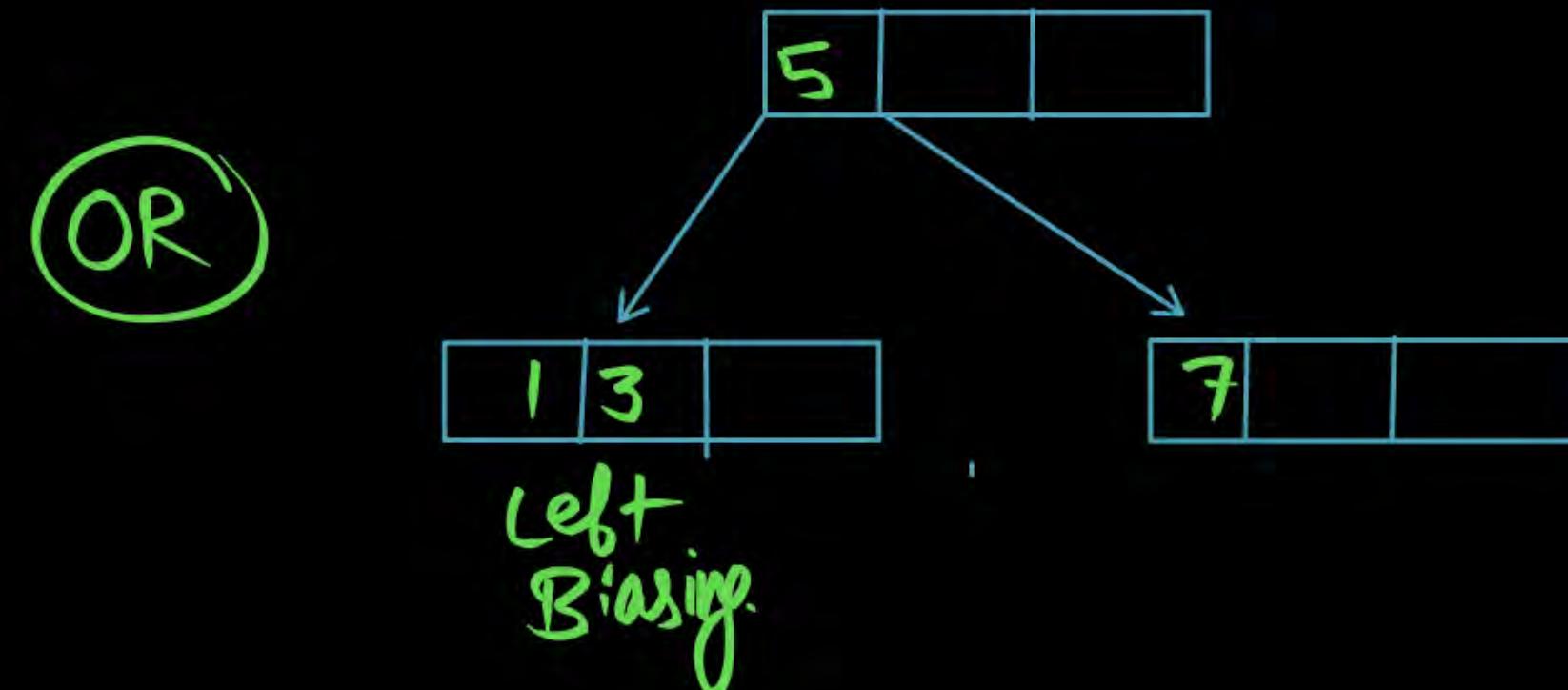
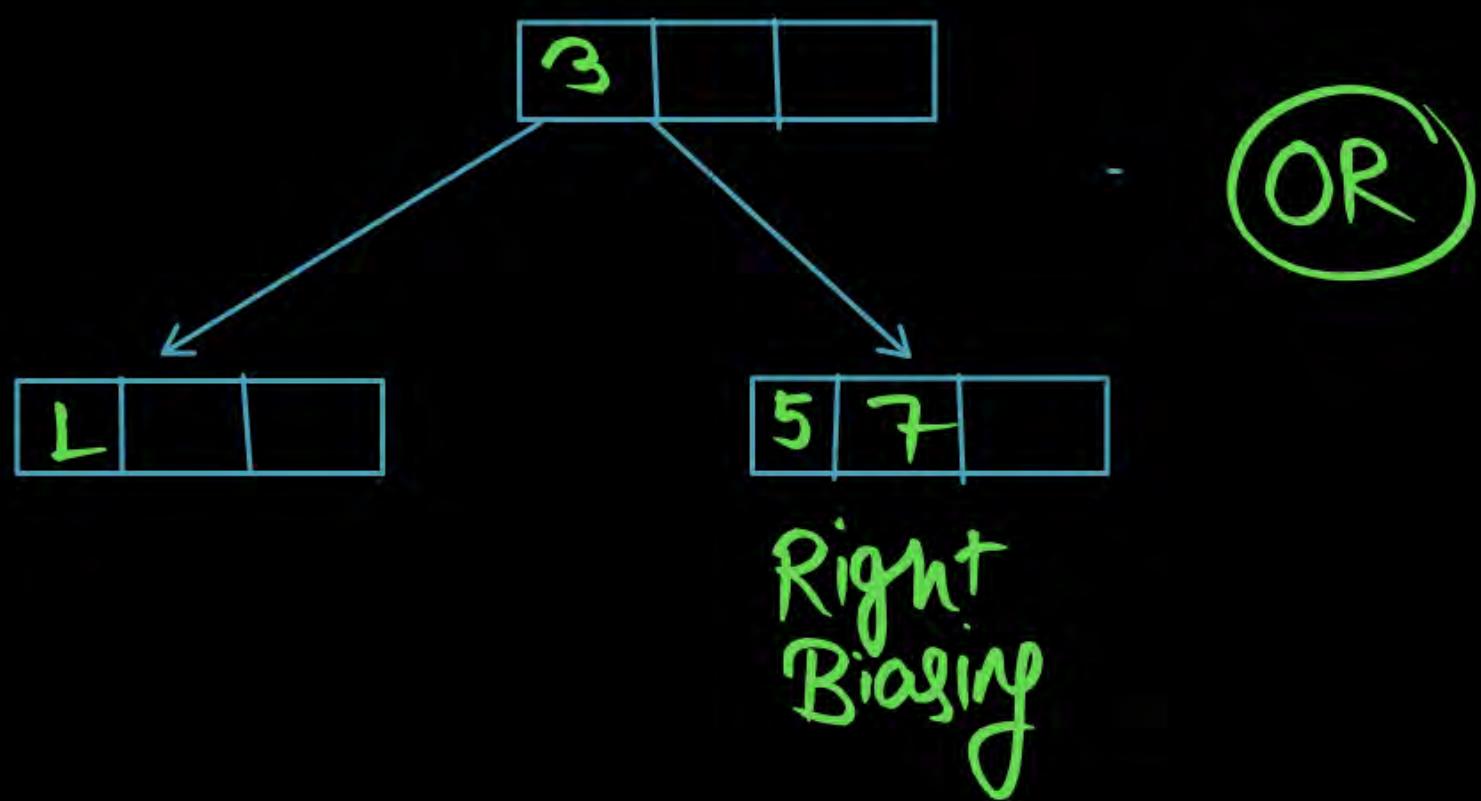
$$\text{Min key} = \lceil \frac{4}{2} \rceil - 1 \Rightarrow 2 - 1 = 1$$

1, 3, 5, 7, 9, 11

1	3	5	7
---	---	---	---

B Tree Definition
Violate

1	3	5	7
---	---	---	---



B Tree Definition

Balanced Tree

~~DBMS~~ ORDER: 4

$$\text{Max key} = 4 - 1 = 3$$

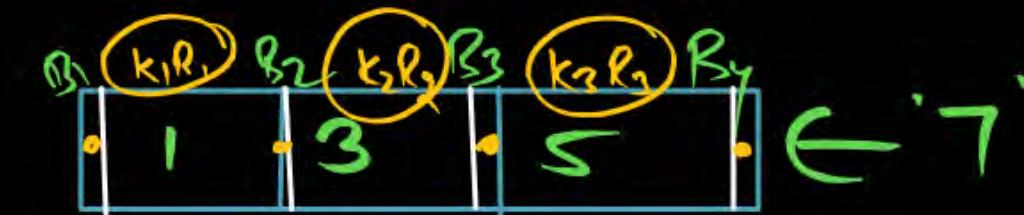
$$\text{Min key} = \lceil \frac{4}{2} \rceil - 1 \Rightarrow 2 - 1 = 1$$

ORDER: 4 1, 3, 5, 7, 9, 11

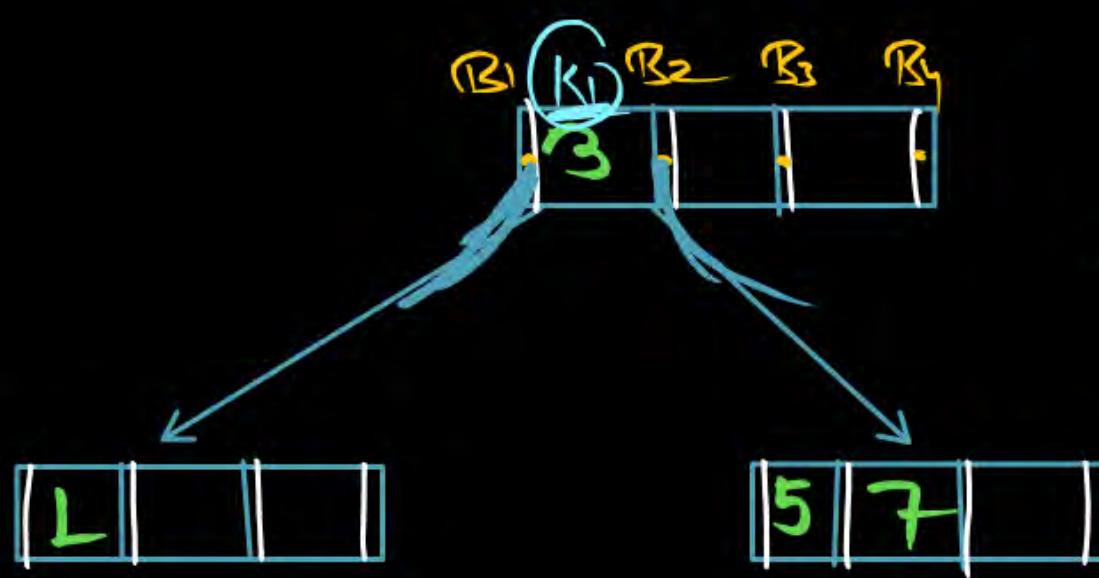
$$B_p = 4$$

$$\text{key} = 3$$

$$R_p = 3$$

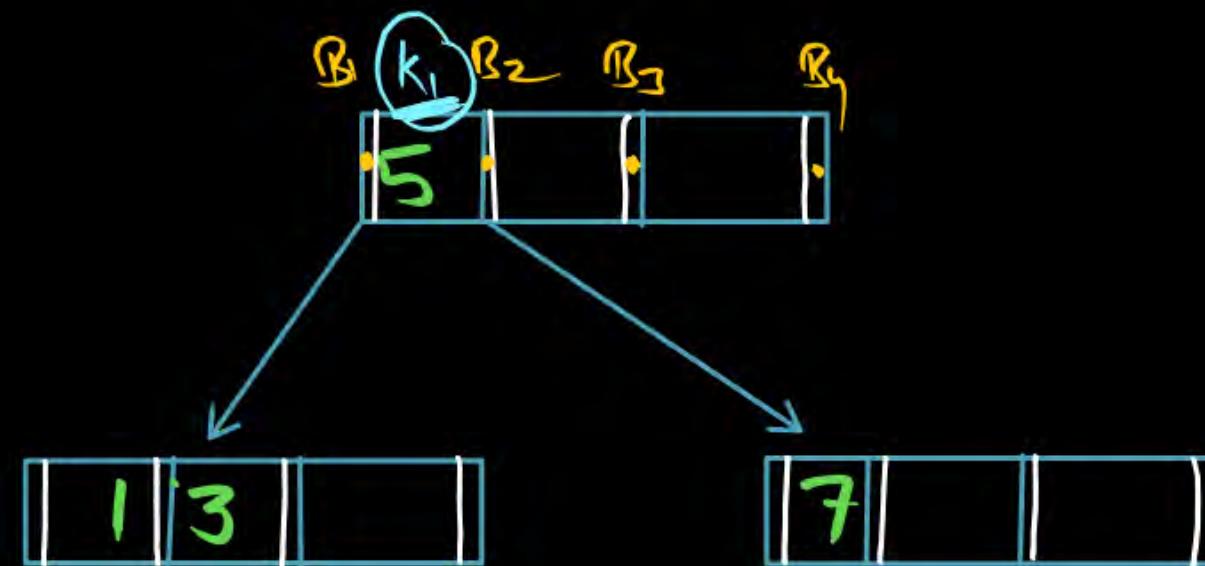


BTree Definition
Violate



Right
Biasing

OR



Left
Biasing

B Tree Definition

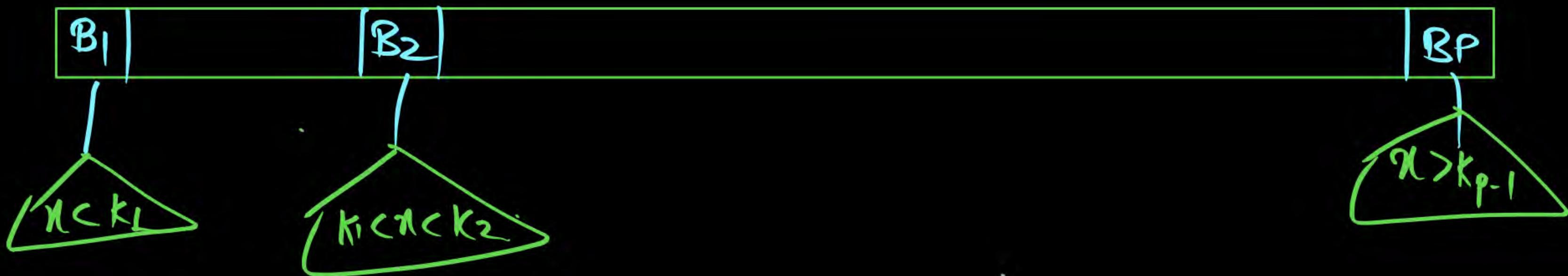
Balanced Tree

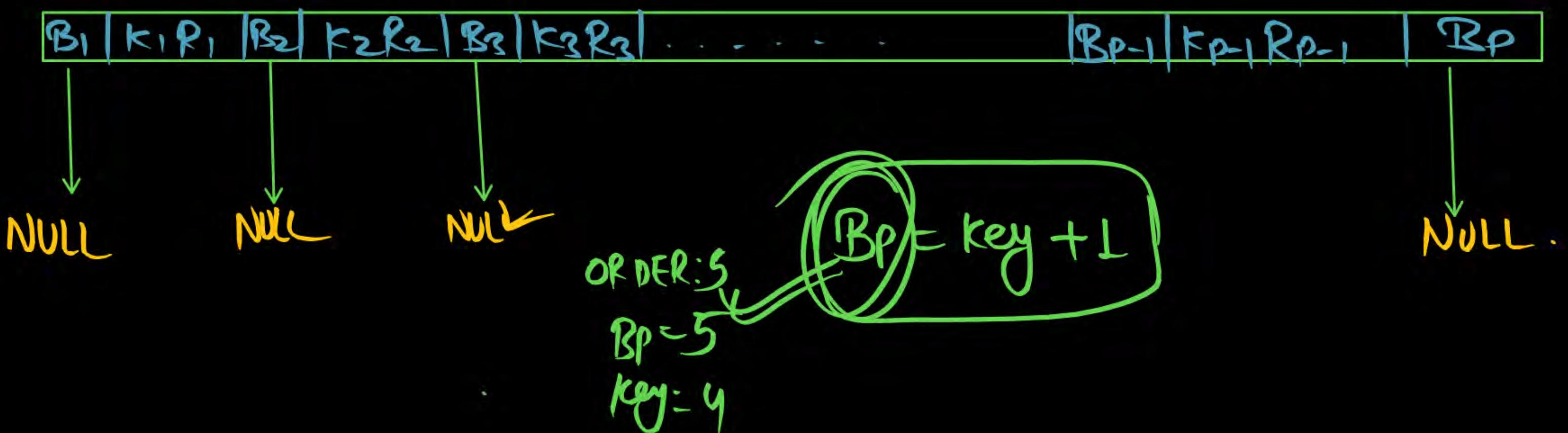
ORDER: P

P
W

① structure of Internal Node

$B_1 k_1 R_1 B_2 k_2 R_2 B_3 k_3 R_3 \dots$	$ B_{P-1} k_{P-1} R_{P-1} B_P$
---	-------------------------------------



② structure of Leaf Node:

- ③ Every Internal Node except the Root Node Contain at least $\lceil \frac{P}{2} \rceil$ Block Pointer ($\lceil \frac{P}{2} \rceil - 1$ keys) & atmost $\lceil \frac{(P-1)}{P} \text{ key} \rceil$ Block Pointer
- ④ Root Can be Contain at least 2 Block Pointer (+key) & at most P Block Pointer ($P-1$ keys)
- ⑤ All keys Within the Node Must be assending order
- ⑥ ALL the leaf Node Should be at Same Level.

B Tree Definition

ORDER: P

Capacity of B Tree

B_1	$k_1 R_1$	B_2	$k_2 R_2$	B_3	$k_3 R_3$...	B_{P-1}	$k_{P-1} R_{P-1}$	B_P
-------	-----------	-------	-----------	-------	-----------	-----	-----------	-------------------	-------

$$P \times B_P + (P-1) \text{ keys} + (P-1) R_P \leq \text{BLOCK Size.}$$



$$P \times B_P + (P-1) [key + R_P] \leq \frac{\text{BLOCK size}}{size}$$

P: Order

B_P : Block | Index | Tree Pointer

K: Key | search key

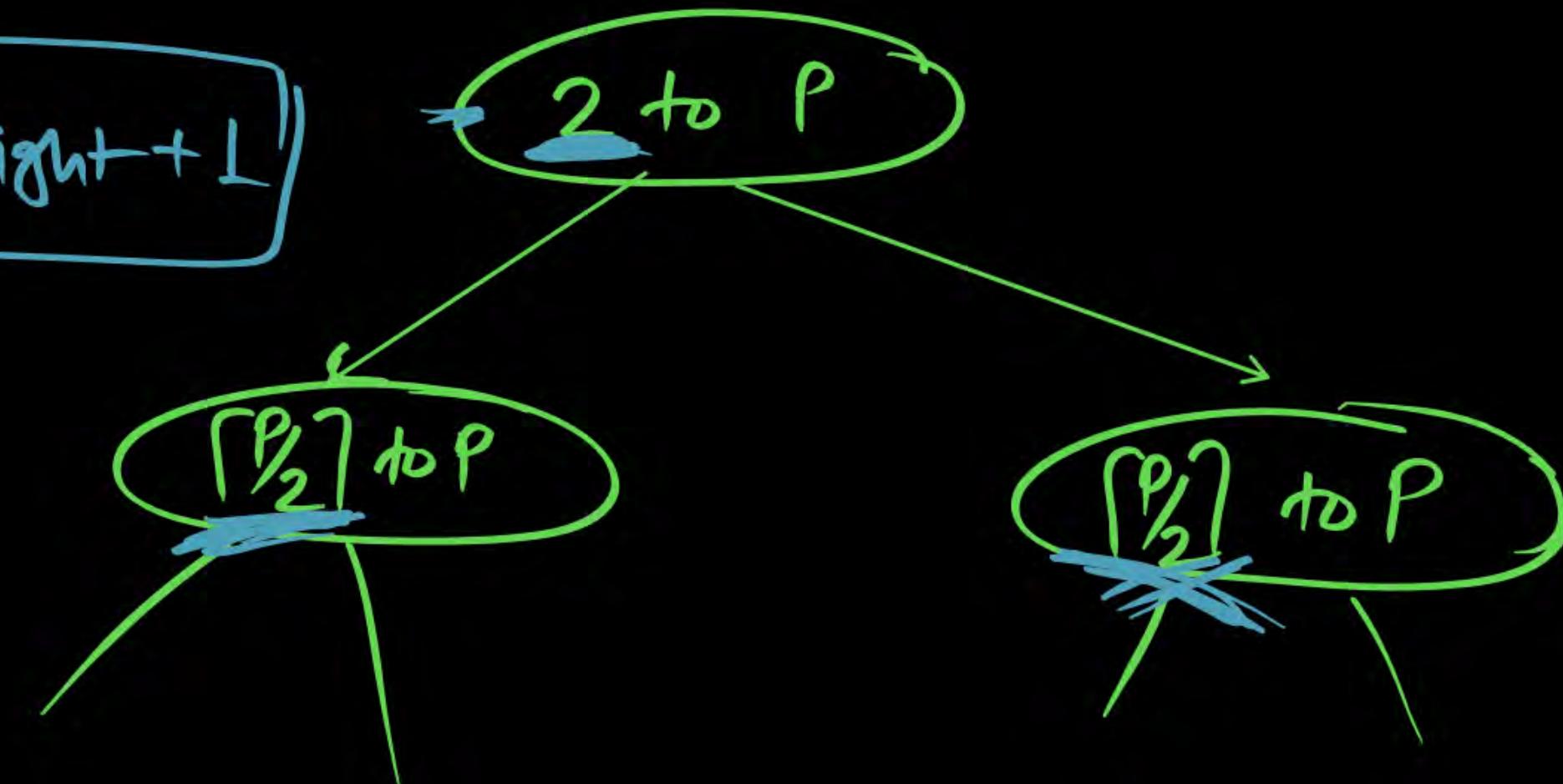
R_P: Read | Data | Record Pointer.

B Tree Definition

Balanced Tree

P
W

$$\text{Level} = \text{Height} + 1$$



B Tree Definition

ORDER : 1

P-5
 (P₁) - ③
 P
 W

Height/Level	Min # Nodes	Min # B ₀	Min # Keys	
0/1	1	2	1	1
1/2	2	$2 \lceil P_1 \rceil$	$2 \lceil P_1 \rceil - 1$	$2 \lceil P_1 \rceil - 1 = 4$
2/3	$2 \lceil P_1 \rceil$	$2 \lceil P_1 \rceil^2$	$2 \lceil P_1 \rceil (\lceil P_1 \rceil - 1)$	$3 \times 4 = 12$
3/4	$2 \lceil P_1 \rceil^2$	$2 \lceil P_1 \rceil^3$	$2 \lceil P_1 \rceil^2 (\lceil P_1 \rceil - 1)$	$3^2 \times 4 = 36$
4/5	$2 \lceil P_1 \rceil^3$	$2 \lceil P_1 \rceil^4$	$2 \lceil P_1 \rceil^3 (\lceil P_1 \rceil - 1)$	$3^3 \times 4 = 108$
h/h+1	$2 \lceil P_1 \rceil^{h-1}$	$2 \lceil P_1 \rceil^h$	$2 \lceil P_1 \rceil^{h-1} (\lceil P_1 \rceil - 1)$	(16) Ans

Q ORDER: 5 Level : 5 → Height = 4.
 $\rho = 5$
 Total Minimum # keys = ?

$P_1 = \left\lceil \frac{5}{2} \right\rceil - 1 = 3$

Ans 16L

$$2 \left[\left\lceil \frac{\rho}{2} \right\rceil - 1 \right]$$

$$2 \left[\left\lceil \frac{5}{2} \right\rceil - 1 \right] \rightarrow 2 \left[\cancel{3} - 1 \right] \Rightarrow 2 \times 2 = 4$$

B Tree Definition

ORDER : P

P
W

Height/Level	Max. # Nodes	Max. # BPs	maximum # Keys	$P=5 \Rightarrow (P-1)=4$
0 L	L	P	(P-L)	$4 = 4$
1/2	P	P^2	$P(P-1)$	$5 \times 4 = 20$
2/3	P^2	P^3	$P^2(P-1)$	$5^2 \times 4 = 100$
3/4	P^3	P^4	$P^3(P-1)$	$5^3 \times 4 = 500$
4/5	P^4	P^5	$P^4(P-1)$	$5^4 \times 4 = 2500$
h h+1	P^h	P^{h+1}	$P^h(P-1)$	3124

B Tree Definition

Q Level 5, ORDER = 5

Total # Max keys = ?

B Tree Definition

(Q.1)

Maximum Level ?

At each level minimum #key & Min #Bp.
 $(\lceil \frac{P}{2} \rceil - 1)$ $\lceil \frac{P}{2} \rceil$

(Q.2)

Minimum Level

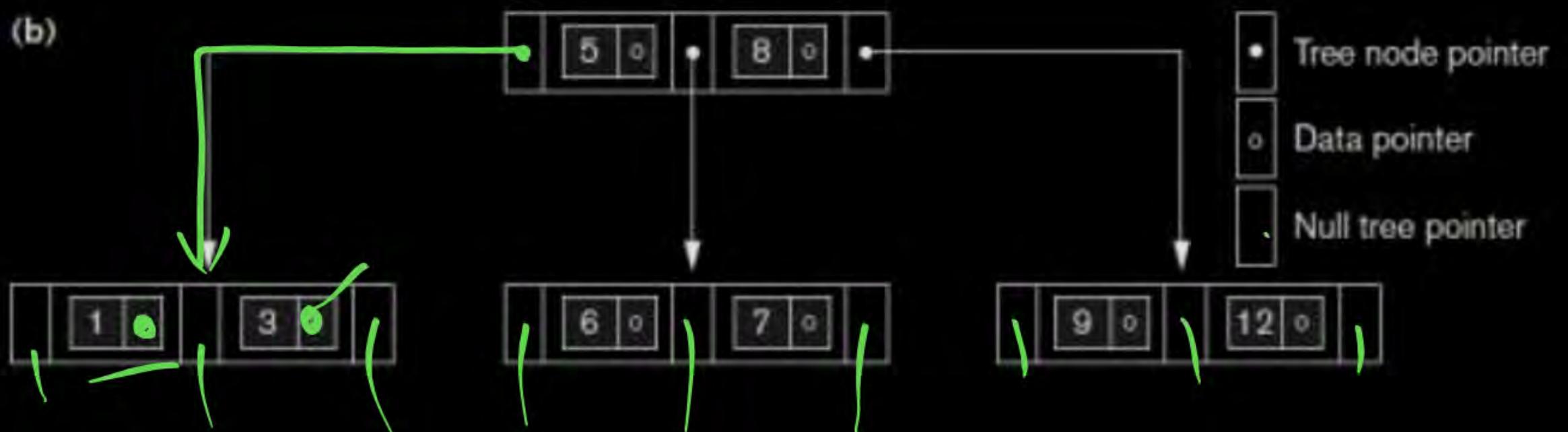
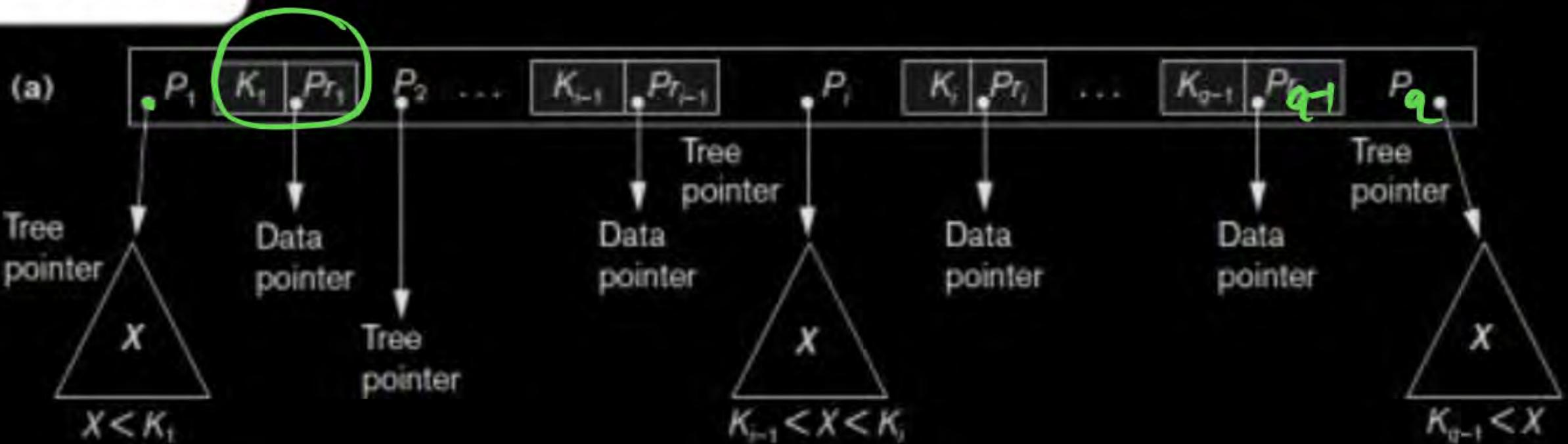
At each level Maximum #keys & Max #Bp.
 $[P-1]$ $[P]$

B Tree Structure

B-tree structures

(a) A node in a B-tree with $q-1$ search values

(b) A B-tree of order $p=3$. The values were inserted in the order $8, 5, 1, 7, 3, 12, 9, 6$

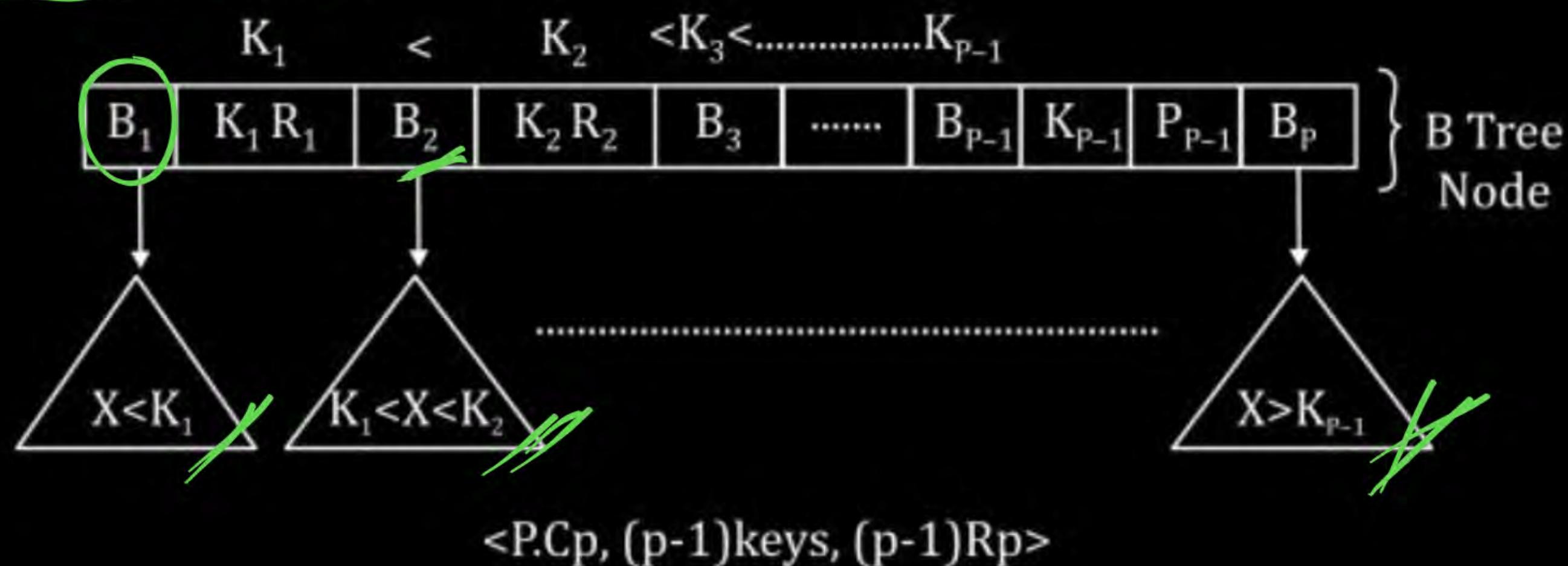


B Tree Definition

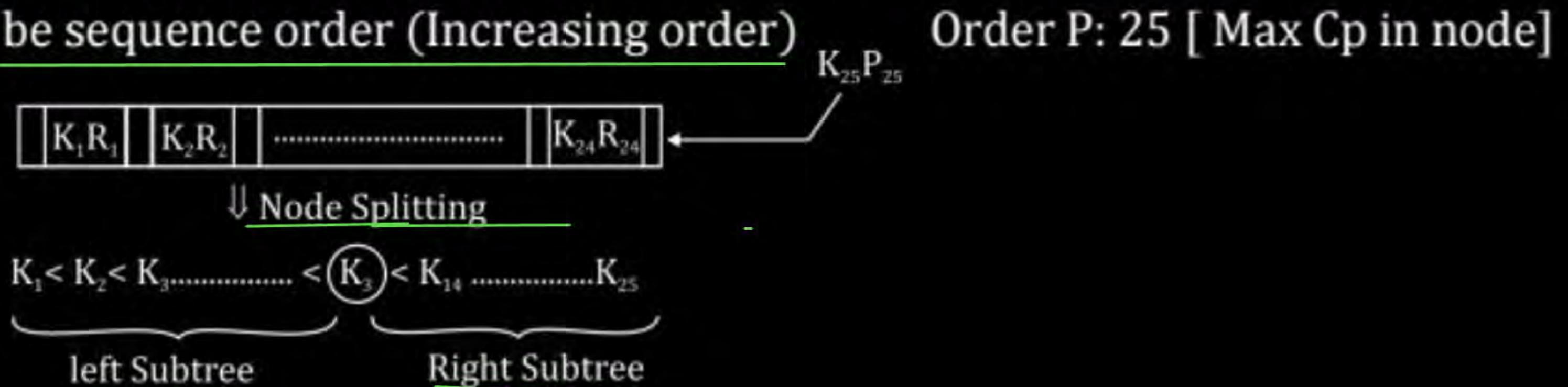
Order P: Max possible child pointers

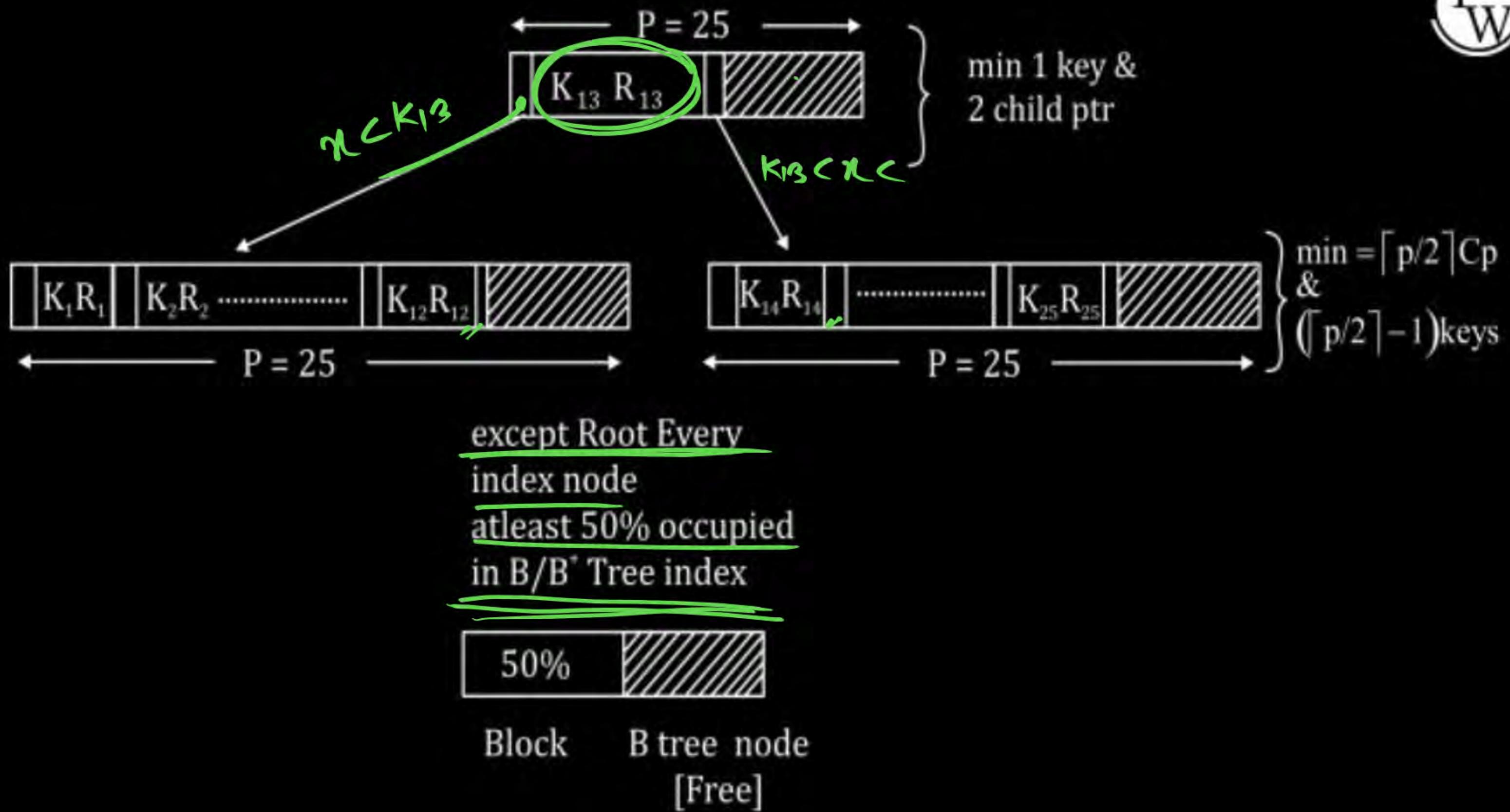
[degree] can store in B Tree node.

(1) Node structure:



- (2) Every internal node except root must be at least $[P/2]$ child pointer with $([P/2] - 1)$ key's and at most P children pointer with $(P - 1)$ key's must.
- (3) Root node can be at least 2 children with 1 key, at most P children pointer and $(P - 1)$ key's.
- (4) Every leaf node must be at same level and keys with in node should be sequence order (Increasing order)





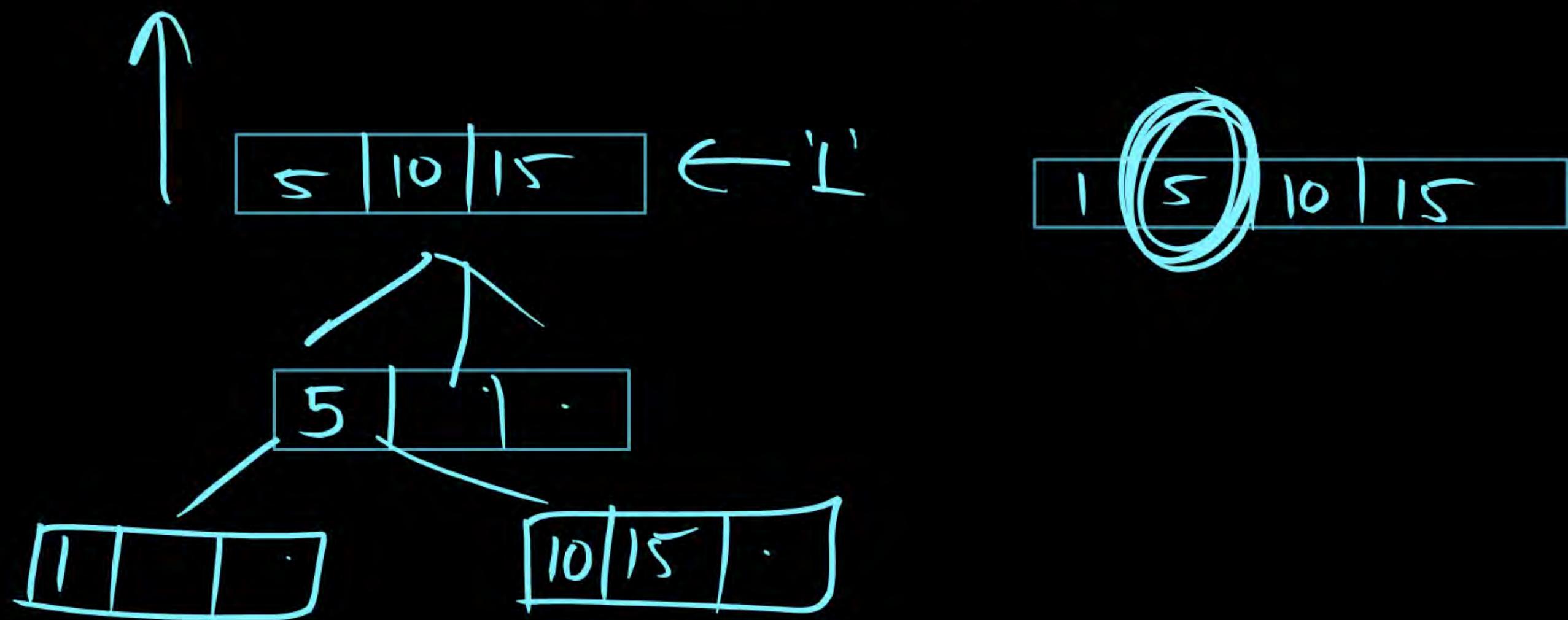
Q.

Construct B Tree with order P: 4 [max Bp/cp (Block/child pointer) per node] and following sequence of key's _____

5, 10, 15, 1, 23, 34, 13, 8.

P=4

key = 3



Q.3

Consider a table T in a relational database with a key field K. A B-tree of order p is used as an access structure on K, where p denotes the maximum number of tree pointers in B-tree index node. Assume that K is 10 bytes long; disk block size is 512 bytes; each data pointer P_D is 8 bytes long and each block pointer P_B is 5 bytes long. In order for each B-tree node to fit in a single disk block, the maximum value of p is [GATE-2004 : 2 Marks]

- A 20
- B 22
- C 23
- D 32

key = 10 Byte

Rp = 8 Byte

Bp = 5 Byte

Block Size = 512 Byte

$$P \times B_p + (P-1) \text{key} + (P-1) R_p \leq \text{Block Size}$$

$$P \times 5 + (P-1) 10 + (P-1) 8 \leq \underline{512}$$

$$\underline{5P} + \underline{10P} - 10 + \underline{8P} - 8 \leq \underline{512}$$

$$23P - 18 \leq \underline{512}$$

$$23P \leq 530$$

$$P = \left\lfloor \frac{530}{23} \right\rfloor = (23.04)$$

$\underline{= 23 \text{ Ans}}$

If we taken 24, then its exceeds by Block size [512Byte].

Advantage:

- 1) B Tree index best suitable for Random access of some record.

select *

FROM R

WHERE A = 24 ;

One record
access

I/O cost: K + 1 blocks

$$\approx [\log_P n] + 1 = \theta(\log_P n)$$

Disadvantage:

- 1) B Tree index not best suitable for sequence access of range of records.

```
select *  
FROM R  
WHERE A ≥ 30 and A ≤ 85;
```

Range of record
Access required

← X blocks of DB →

I/O cost: $x[\log_p n + 1] + \text{cost of unsuccessful}$

More Access cost

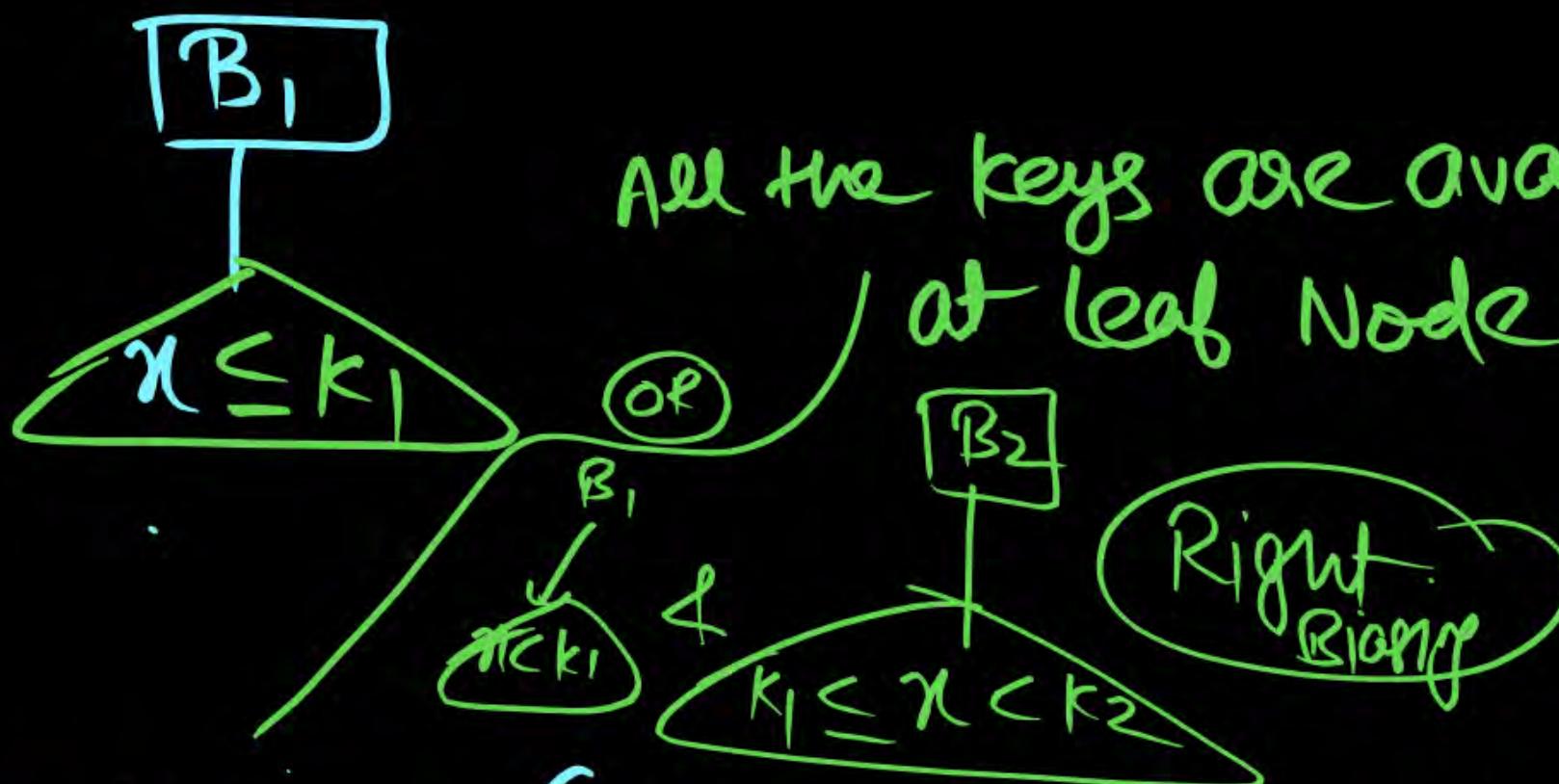
[Unordered File DB]

B⁺ Tree Definition

Total 3 Difference

① In Internal Node \Rightarrow No Read (Reward) Pointer.

②



All the keys are available
at leaf Node

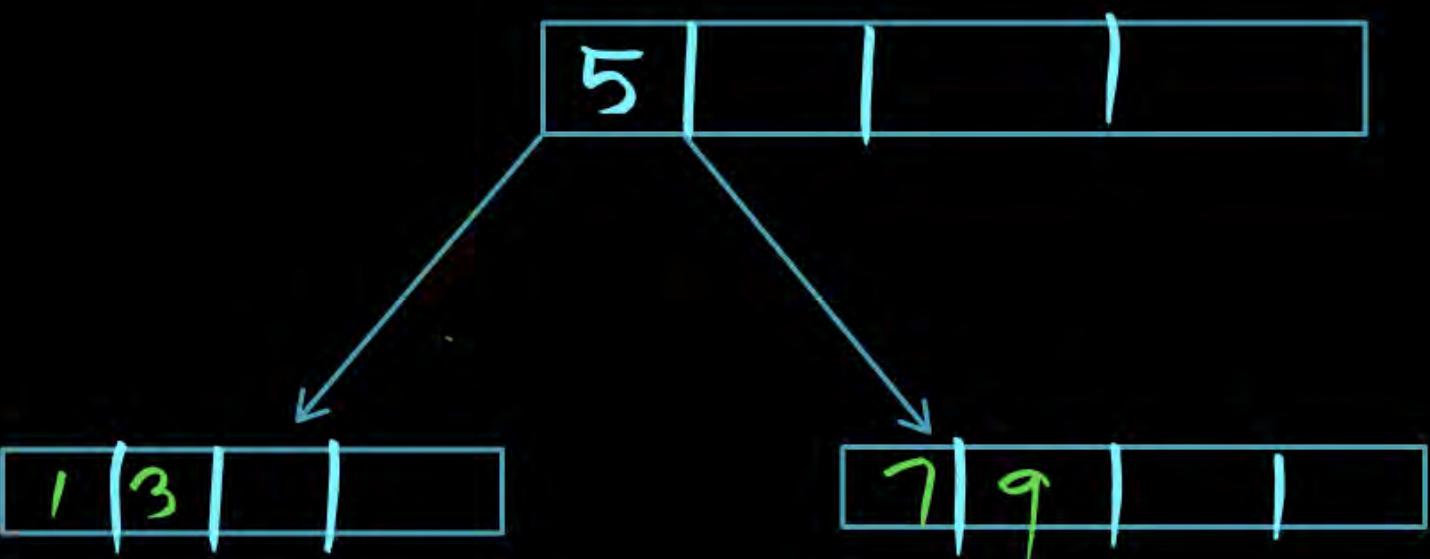
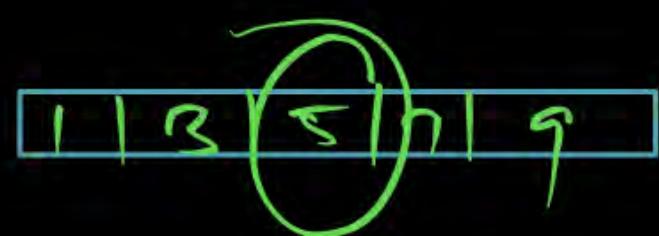
③ Leaf Node Contain (key + Rp) Pair + L Block Pointer.

B⁺ Tree Definition

1, 3, 5, 7, 9, 11

ORDER : 5

BTree

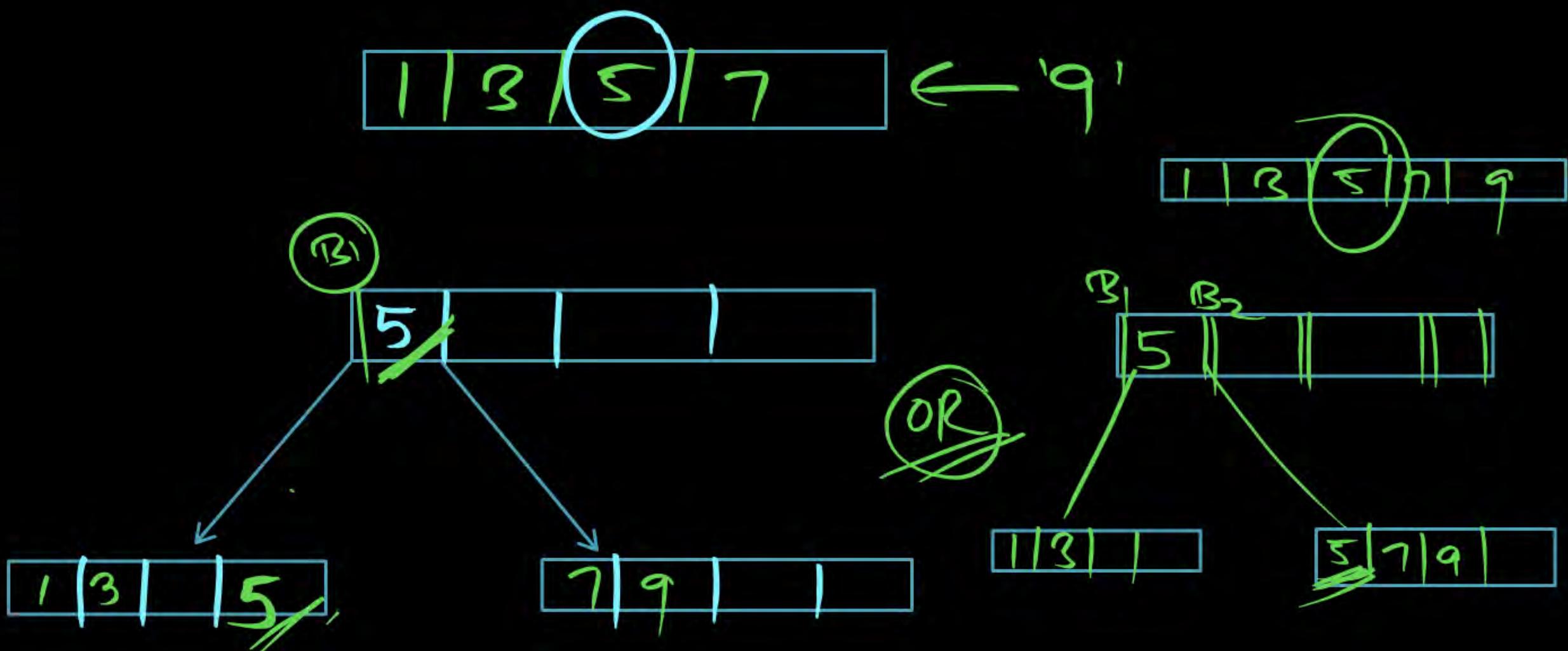


B⁺ Tree Definition

1, 3, 5, 7, 9, 11

ORDER : 5

B⁺Tree

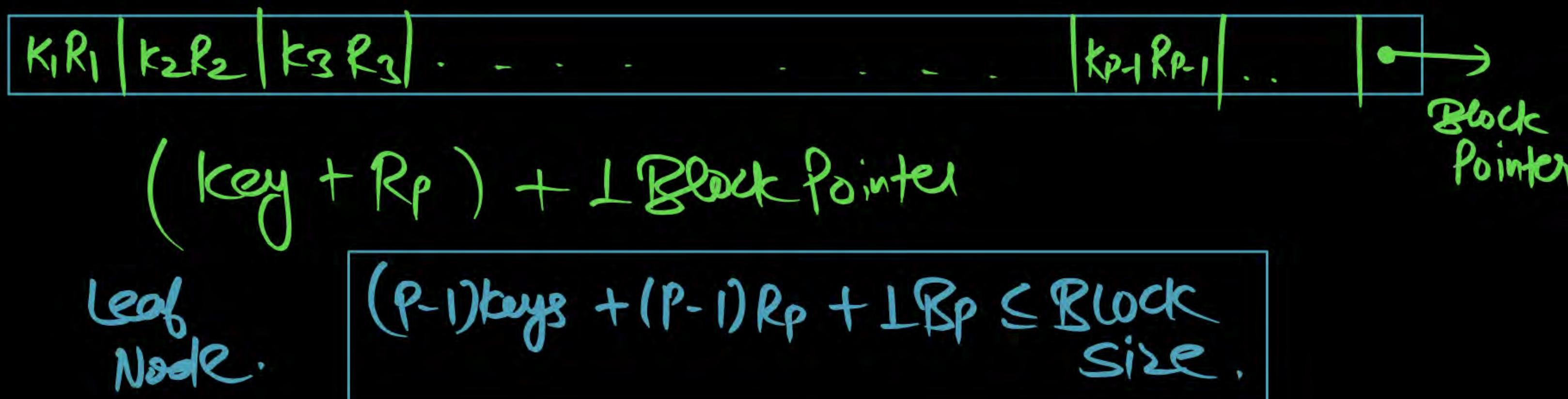


B⁺ Tree Definition

① Structure of Internal Node



② Structure of leaf Node



B⁺ Tree Definition

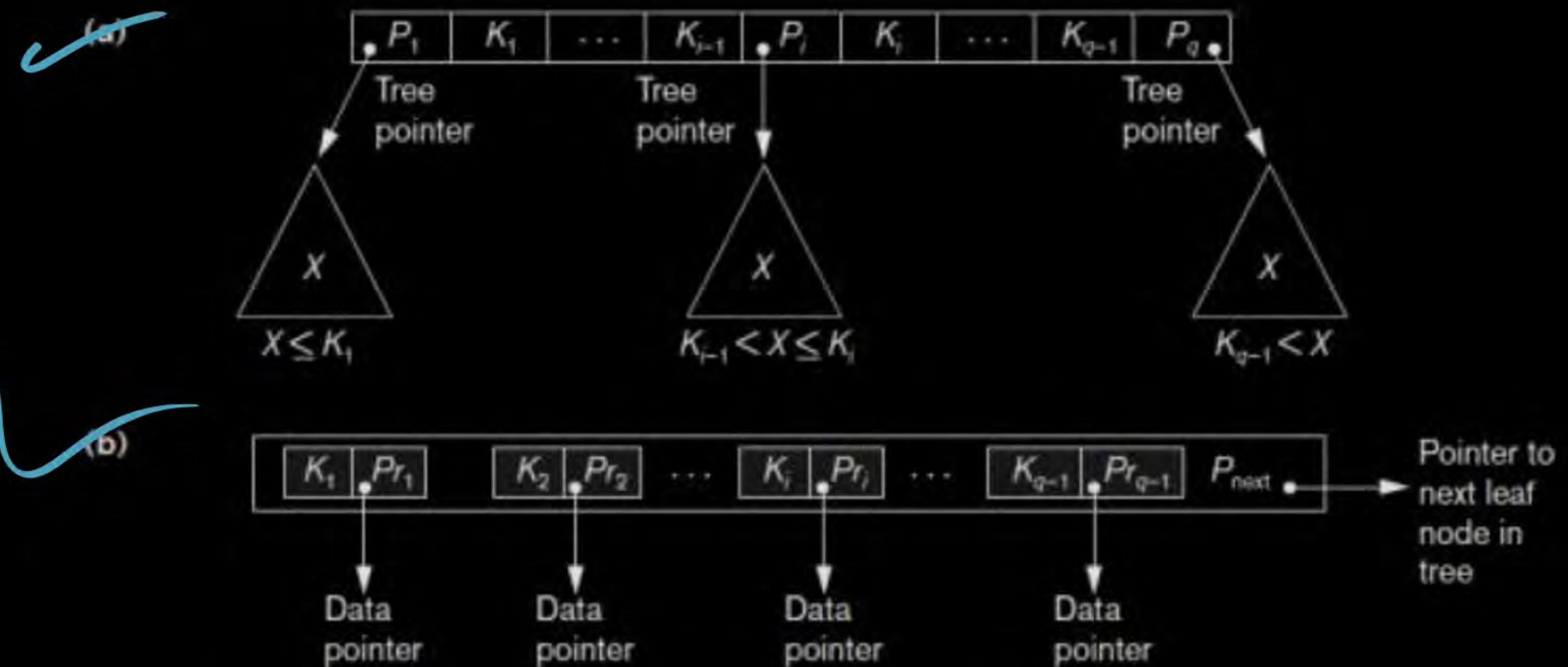
③ Internal Node Min $\lceil \frac{P}{2} \rceil B_p$ & Max $P B_p$

④ Root Node Min $2 B_p$ & Max $P B_p$

⑤ All the leaf Node Should be at same level

⑥ keys within the Node Should be in ascending order

B+ Tree



The nodes of a B+-tree
(a) Internal node of a B+-tree with $q-1$ search values
(b) Leaf node of a B+-tree with $q-1$ search values and $q-1$ data pointers

Non
Leaf | Internal Node

$$P \times B_P + (P-1) \text{ keys} < \frac{\text{BLOCK size}}{}$$

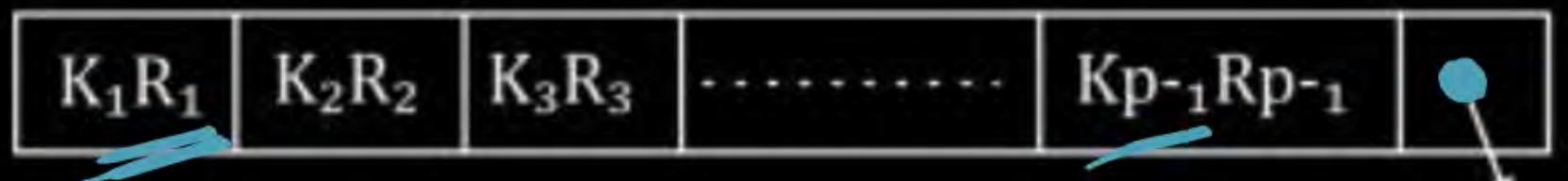
B⁺ Tree Definition

Order P: max possible pointers [degree] can store in B⁺ Tree node.

(1) Node Structure:

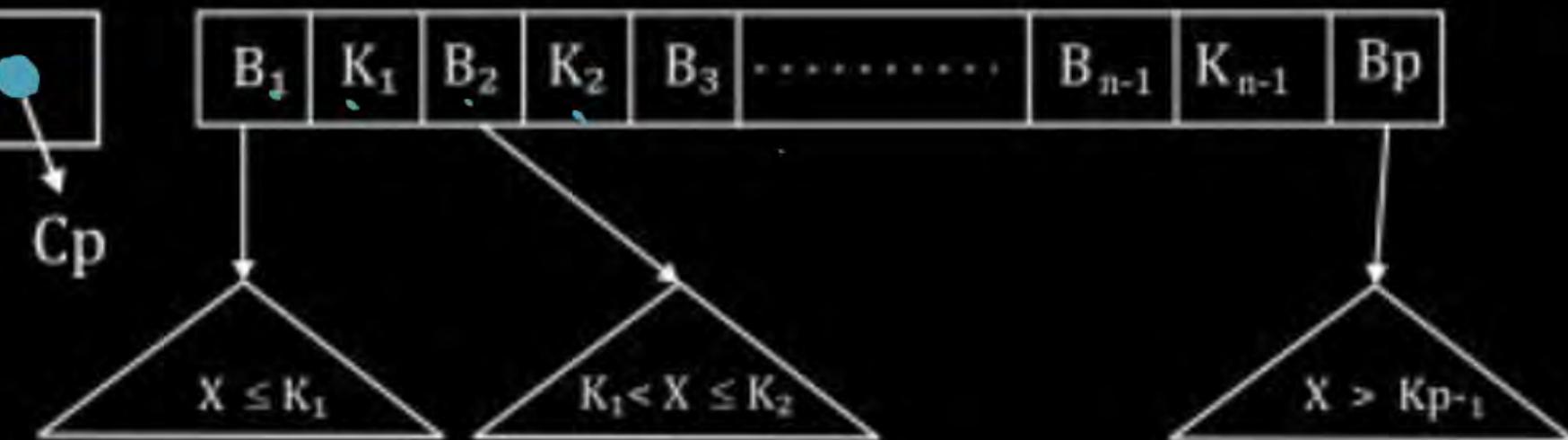
(a) Leaf Node

[set of (key, Rp) pair and only one block pointer pointed to next Leaf node]



(b) Internal Node

[key's and child pointer]
∴ No record pointer (Rp).

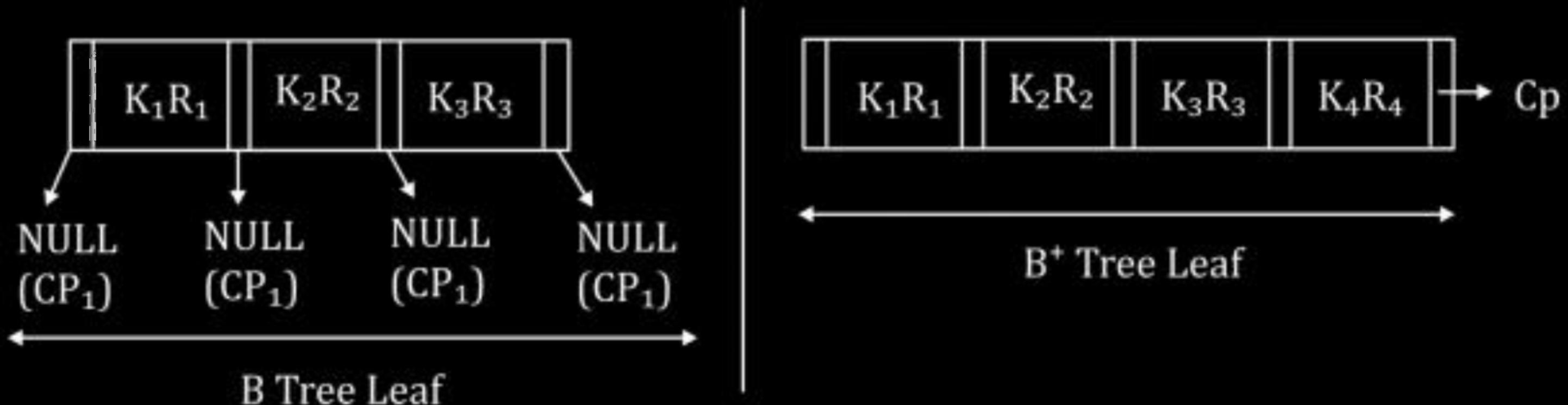


⇒ Left Biasing condition

$$k_1 < x \leq k_2 \dots$$

Right Biasing condition

$$k_1 \leq x < k_2 \dots x \geq k_{p-1}$$



⇒ Remaining Balancing Condition same as B Tree

Advantage:

- 1) B⁺ Tree index best suitable for sequence access of range of records.

[Range Queries runs faster using B⁺ Tree index]

Select *

FROM R

WHERE A ≥ 30 and A ≤ 85;

I/O cost: $[\log_p n + x + x]$

For
Index

For
Database
File

Q.4

The order of an internal node in a B⁺-tree index is the maximum number of children it can have. Suppose that a child pointer takes 6 bytes, the search field value takes 14 bytes, and the block size is 512 bytes. What is the order of the internal node?

- A 24
- B 25
- C 26
- D 27

$$P \times B_P + (P-1) \text{Keys} \leq \text{Block Size}$$

$$GP + (P-1)14 \leq 512$$

$$20P - 14 \leq 512$$

$$20P \leq 526$$

$$P = \frac{526}{20} = \underline{\underline{26}} = 26$$

$$B_P = 6$$

$$\text{Key} = 14$$

Q.5

Consider a B^+ -tree in which the maximum number of keys in a node is 5 . What is the minimum number of keys in any non-root node?

- (A) 1
- (B) 2
- (C) 3
- (D) 4

Maximum # = 5
keys ($P-1$)

$P-1 = 5$

$P=6$ ORDER = 6

Minimum #
keys = $\lceil \frac{P}{2} \rceil - 1 = \lceil \frac{6}{2} \rceil - 1 = 3 - 1 = 2$

JOIN with foreign key Concept.

Note

Whenever Two Tables are Joined (Natural Join)

with Respect to Primary key & foreign key then

^{maximum}
Number of Tuples in the Resulting Relation is equal to

Tuples in the Referencing [containing F.K] Relation.

Q.1

P
W

Consider the relations:

Supply (SupplierID, Itemcode) with 1000 tuples

Inventory (Itemcode, color) with 2500 tuples

Let p and q be the number of maximum and minimum records in Supply JOIN Inventory, the value of $p + q$ is _____. (Itemcode is FK in Supply table).

Supply (SupplierID, Item Code)
1000 Tuple

Inventory (Item code, color)
2500 Tuple

Maximum # Tuples in JOIN [p] = 1000 Ans

Minimum # Tuple [q] = 1000

$$p + q = 1000 + 1000$$

$$= \textcircled{2000} \text{ Ans}$$

The value present in the foreign key must be present in primary key

foreign key may contain duplicates & NULL value

Here Item Code is foreign key in Supply Table Reference P.K of Inventory table

But Here Item Code is also key in Supply Table

SUPPLY	
SID	Item Code
S1	C1
S1	C2
S2	C1
S2	C2

IID	SUPPLY (Supplier id)	Item Code
C1		
C2		
C3		
C4		
C5		
C6		

So Item Code cannot be NULL.

Q. 2

Consider the relations:

Employee(Eid, Ename) with 2000 tuples

Department(Eid, Did) with 1000 tuples

Let p and q be the number of maximum and minimum records in Employee JOIN Department, the value of $p + q$ is _____. (Eid is FK in Department table).

2000

Q.3

Consider the relations:

$R_1(A, \underline{B}, C)$ with n tuples

$R_2(\underline{B}, D, E)$ with m tuples (B is FK in R1).

maximum tuples in $R_1 \bowtie R_2 = n$

minimum tuples in $R_1 \bowtie R_2$ =
~~only~~ $R_1(A, \underline{B}, C)$ $R_2(\underline{B}, D, E)$
n Tuple m Tuple

Maximum $R_1 \bowtie R_2 = n$

Minimum $R_1 \bowtie R_2 = n$ (if foreign key Reference to
PK & F.K Not NULL)
= 0 [Not a foreign key
OR NULL]

P
W

Q.4

P
W

Consider the relations:

$R1(A, B, C)$ with n tuples

$R2(B, D, E)$ with m tuples (B is Not FK in R1).

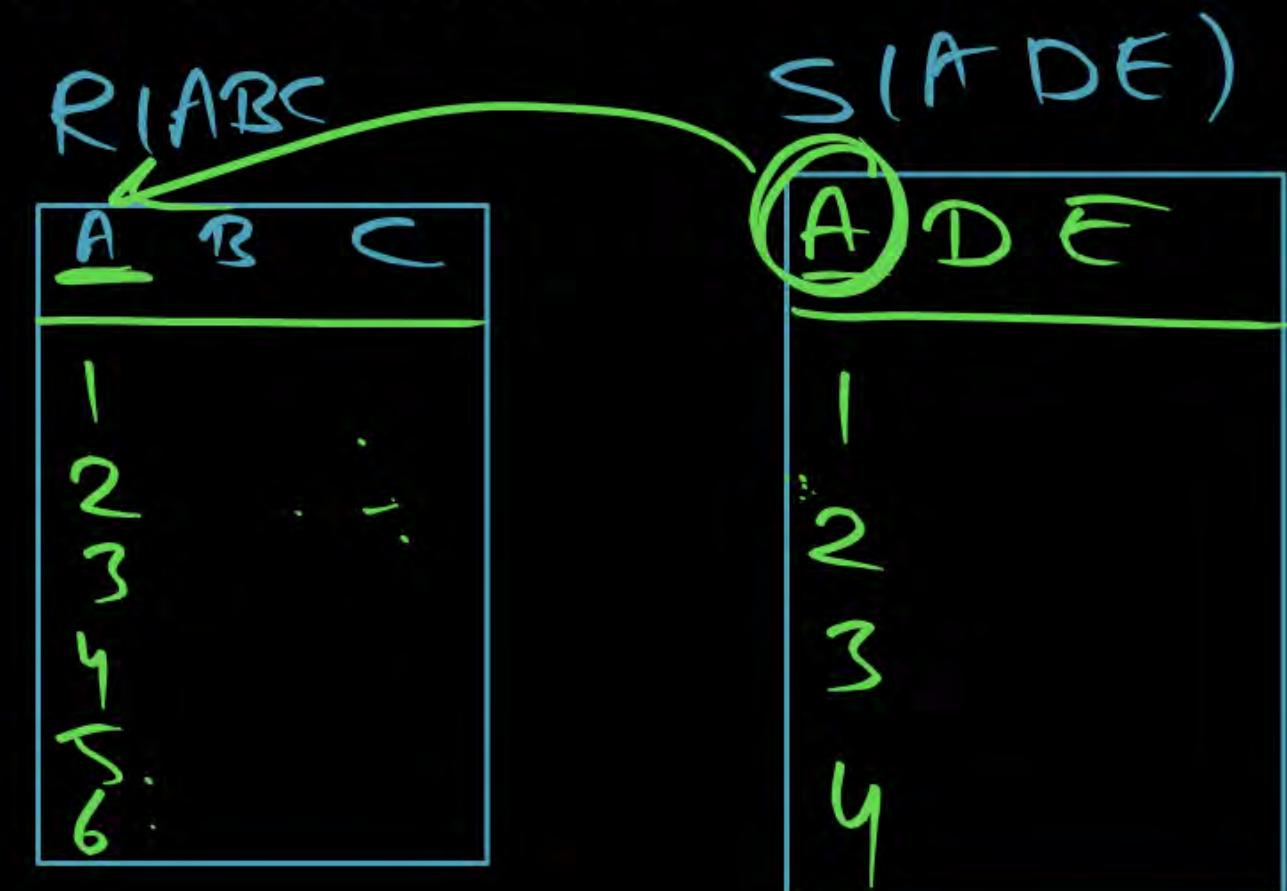
maximum tuples in $R1 \bowtie R2$

minimum tuples in $R1 \bowtie R2$

Q.5

Consider the join $R \bowtie S$ between $R (A B C)$ and $S (A D E)$ with attribute A being the primary key in both relations and attribute A in S is a Foreign Key referencing to attribute A in R. R has m tuples and S has n tuples, maximum and minimum number of tuples in $R \bowtie S$ respectively are?

- (a) $m, m + n$
- (b) $m * n, 0$
- (c) $\min(m, n), \min(m, n)$
- (d) $\max(m, n), \min(m, n)$



Q. 6

Consider the relations:

 $R_1(A, B, C)$ with n tuples $R_2(D, B, E)$ with m tuples $\{A \rightarrow B, B \rightarrow C, D \rightarrow B, B \rightarrow E\}$ maximum tuples in $R_1 \bowtie R_2$ minimum tuples in $R_1 \bowtie R_2$ $R_1(ABC)$ $R_2(DBE)$

C.I.C : A

C.I.C : D

B is Not
keyMaximum $R_1 \bowtie R_2 = n * m$

Minimum = 0

R is Non key Attribute
in Both Table

The following functional dependencies hold for relations R(A, B, C) and S(B, D, E) FD for both the tables.

$$B \rightarrow A$$

$$A \rightarrow C$$

The relation R contains 200 tuples and the relation S contains 100 tuples. What is the maximum number of tuples possible in the natural join $R \bowtie S$?

[GATE-2010-CS: 2M]

A 100

B 200

C 300

D 2000

**THANK
YOU!**

