

# COMPUTER SCIENCE



Database Management  
System

Query Language

Lecture\_1

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An orange diamond-shaped sign with a black border, mounted on a white pole. The sign contains the text 'TOPICS TO BE COVERED' in black capital letters.

TOPICS  
TO BE  
COVERED

A red diamond-shaped sign with a white border, containing the white number '01'.

01

**Relational Algebra**

A red diamond-shaped sign with a white border, containing the white number '02'.

02

**Operators**



- ✓ ① FD & Normalization
  - ✓ ② Transaction & Concurrency Control
  - ✓ ③ ER Model & Foreign Key Concept
  - ④ Query language. - 20 to 30 q.
  - ⑤ File org & Indexing - 10 to 15 q.
- Remaining GATE Question.
- 92 GATE Question
- 500



# Query language

(Formal)

Procedural  
Query Language

[e.g. Relation  
Algebra]

(Informal)

Non Procedural  
Query Language

[e.g. SQL  
TRC] →

# Query Language



```
graph TD; A[Query Language] --> B[Procedural Query Language]; A --> C[Non Procedural Query Language]
```

## Procedural Query Language

- WHAT to Retrieve From DB
- HOW to Retrieve from DB

Relational Algebra:

## Non Procedural Query Language

WHAT to Retrieve from DB.

- ❑ SQL (Structured Query Language)
- ❑ TRC (Tuple Relational Calculus)



# Procedural Query Language and Non-procedural Query Language



Procedural Query Language	Non-procedural Query Language
Formulation of <u>how</u> to access data from the database table and <u>what</u> <u>data</u> required to retrieve from DB tables.  "Relational Algebra"	Formulation of <u>what data</u> retrieve from DB tables.  "Relational Calculus"  "SQL"  DRC TRC ✓

# Relational Algebra

- Procedural Query Language
- By Default eliminate Duplicate value.



# Relational Algebra



(Always generate distinct tuples)

Relational algebra refers to a procedural query language that takes relation instances as input and returns relation instances as output

**Note** Basic Idea of Query Language is Query executed on DB Table  
One Tuple at a time. Tuple by Tuple (Row by Row)



# Relation Algebra.

$R: [1, 2, 3, 4, 5, 6]$

$S: [4, 5, 6, 7, 8]$

$R - S = [1, 2, 3]$

$R - (R - S) = [4, 5, 6]$   
 $\equiv R \cap S$

## Basic operators

- ① Selection  $[\sigma]$
- ② Projection  $[\pi]$
- ③ CROSS Product  $[X]$
- ④ UNION  $[U]$
- ⑤ Minus / set Difference  $[-]$
- ⑥ Rename  $[P]$

## Derived operator

- ① JOIN  $[\bowtie]$
- ② DIVISION  $[/]$
- ③ Intersection  $[\cap]$

$$R \cap S = R - (R - S)$$

# Relational Algebra



## Basic operators

- ①  $\pi$  : Projection operator
- ②  $\sigma$  : Selection operator
- ③  $\times$  : Cross-product operator / Cartesian Product
- ④  $\cup$  : Union
- ⑤  $-$  : Set difference
- ⑥  $\rho$  : Rename operator



# Relational Algebra



## Derived operators

- ①  $\cap$  : Intersection {using “\_”}
- ②  $\bowtie$  : Join {using  $X, \sigma$ }
- ③  $/$  or  $\div$  : Division {using  $\pi, x, -$ }

$$R \cap S = R - (R - S)$$

## Projection [ $\pi$ ]

(Column)

It Select [Project] Attribute @  
Attribute List from the Relation

### Syntax

$\pi_{\text{Attribute (or) Attribute List}} (\text{Relation})$

eg

$\pi_{\text{name}} (\text{Student})$

$\pi_{\text{name Contact}} (\text{STUDENT})$

$\pi_A (R)$

$\pi_{ABCD} (R)$

## Selection [ $\sigma$ ]

(Row)

It Select the Tuple / Record from the  
Relation Based on Specified Condition

### Syntax

$\sigma_{\text{Condition}} (\text{Relation})$

eg

$\sigma_{\text{CGPA} > 9} (\text{STUDENT})$

eg

$\sigma_{\text{State} = \text{'mp'}} (\text{STUDENT})$

eg

$\sigma_{\text{Branch} = \text{'cs'}} (\text{Student})$



Q W.A.Q [Write an Query] to Reterive Name of Student  
Whose CGPA > 9.

Sol<sup>n</sup>

CGPA > 9 (Student)

T<sub>name</sub> [CGPA > 9 (Student)]

o/p. →

Name
Biswjeet
Sohini
Gagan

STUDENT

Rollno	Name	Branch	Gender	Contact	CGPA
1	Ajay	CS.	M.	-	8
2	Ankit	IT	M.	-	9
3	Biswjeet	CS.	M.	-	9.1
4	Sohini	IT	F.	-	9.2
5	Pankaj	CS.	M.	-	8.5
6	Gagan	IT	M.	-	9.4



Q) W.A.Q [Write an Query] to Retrieve Name of Student <sup>Branch</sup> Whose CGPA > 9.

Sol<sup>n</sup>

CGPA > 9 (Student)

SELECT Name Branch FROM Student WHERE CGPA > 9

STUDENT					
Rollno	Name	Branch	Gender	Contact	CGPA
1	Ajay	CS	M	-	8
2	Ankit	IT	M	-	9
3	Biswjeet	CS	M	-	9.1
4	Sohini	IT	F	-	9.2
5	Pankaj	CS	M	-	8.5
6	Gagan	IT	M	-	9.4

o/p. →

Name	Branch
Biswjeet	CS
Sohini	IT
Gagan	IT



Same o/p

$$\left[ \sigma_{C_3} \left( \sigma_{C_2} \left( \sigma_{C_1} (R) \right) \right) \right] \equiv \sigma_{C_1} \left( \sigma_{C_3} \left( \sigma_{C_2} (R) \right) \right)$$

⑧  $C_{SPA} > 9$ ,  $C_1$  Gender = M,  $C_2$  Branch = CS,  $C_3$

op  $\rightarrow$  Biswjeet

$C_1 \wedge C_2 \wedge C_3$

$C_{SPA} > 9 \wedge \text{Gender} = 'M' \wedge \text{Branch} = 'CS'$

## Basic operators

### I. $\pi$ : Projection

- $\pi_{\text{Attribute name}}(R)$ : It is used to project required attribute from relation R.
- $\sigma_{\text{Condition}(P)}(R)$ : It is used to select records from relation R, those satisfied the condition (P).



# Example:

GIVEN Table

R	A	B	C
	8	4	5
	2	4	5
	7	4	6
	3	5	5

①

$\pi_{B,C}(R):$

Loop

B	C
4	5
4	6
5	5

②

$\sigma_{A \neq 5}(R):$

A	B	C
8	4	5
7	4	6



## Reserves (R<sub>1</sub>)

<u>Sid</u>	<u>Bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

## Sailors(S<sub>1</sub>)

<u>Sid</u>	Sname	Rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

## Sailors(S<sub>2</sub>)

<u>Sid</u>	Sname	Rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0



# Selection ( $\sigma$ )



Q.1

$\sigma_{\text{rating} > 8} (S_2)$

Sailors ( $S_2$ )

<u>Sid</u>	Sname	Rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0



## Selection ( $\sigma$ )



**Ans.1**

$\sigma_{\text{rating} > 8} (S_2)$

**Output:**

Sid	Sname	Rating	age
28	yuppy	9	35.0
58	rusty	10	35.0

**Sailors ( $R_2$ )**

<u>Sid</u>	Sname	Rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0



$\pi_{\text{sname, rating}} (\sigma_{\text{rating} > 8} (S_2))$

Output:

yuppy 9  
rusty 10.

Sailors( $S_2$ )

<u>Sid</u>	Sname	Rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0





$\pi_{\text{sname, rating}} (\sigma_{\text{rating} > 8} (S_2))$



Output:

Sname	Rating
yuppy	9
rusty	10

Sailors( $S_2$ )

<u>Sid</u>	Sname	Rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

# Projection( $\pi$ )



Q.2

$\pi_{\text{age}}(S_2)$

Sailors ( ~~$S_2$~~ )

<u>Sid</u>	Sname	Rating	age
28	yuppy	9	<u>35.0</u> ✓
31	lubber	8	<u>55.5</u> ✓
44	guppy	5	35.0
58	rusty	10	35.0



# Projection( $\pi$ )



Ans.2  $\pi_{age}(S_2)$

Output:

age
35.0
55.5

Sailors ( $S_2$ )

<u>Sid</u>	Sname	Rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0



$\pi_{\text{sname, rating}} (S_2)$



Output:

Sname	Rating
yuppy	9
lubber	8
guppy	5
rusty	10



Set operators:  $[U, \cap, -]$

Union, Intersection, Minus(-)

R & S be the Two Relation. is Union Computable iff

① Number of Attribute [Arity] <sup>Degree/</sup> should be same.



Not possible to Apply.

② Range of Attribute Must be Similar.

RollNo	Name

Branch	Contact

Not possible



Arity (Degree) : Same

Range : Similar.



# Set operator



U: Union operator

– : Except or minus

$\cap$  : Intersection operator

❑ To apply set operations relations must be union compatible.

❑ R and S relations are union compatible

❑ If and only if-

(i) Arity of R equal to Arity of S and

(ii) <sup>(Range)</sup> Domain of attributes of R must be same as domain of attributes of s respectively.



Arity (Degree) : Same

Range  
(Domain) : Similar.



## Example



Example 1:

$$\pi_{\underline{Sid\ Sname}}(\dots \dots \dots) \cap \pi_{\underline{Sid}}(\dots \dots \dots)$$

{Arity not same so, set operation not allowed}

Example 2:

$$\pi_{\underline{Sid} \underline{Sname}}(\dots \dots \dots) \cap \pi_{\underline{Sid} \underline{Marks}}(\dots \dots \dots)$$

{Arity same but Sname domain is different from marks so, not allowed}

# Example



$$\pi_{\underline{Sid Sname}} (... ..) \cap \pi_{\underline{Stud ID}, \underline{Stud name}} (... ..)$$

{Arity and domains are same so, allowed for set operation}

1. Set operation on relation:

<b>R</b>	<b>A</b>	<b>S</b>	<b>A</b>
2	2	2	2
2	2	2	2
3	2	4	4
	3		

$$S - R : (x / x \in S \wedge x \notin R)$$

$$\underline{R \cup S} : \{x / x \in R \vee x \in S\} \equiv$$

A
2
3
4

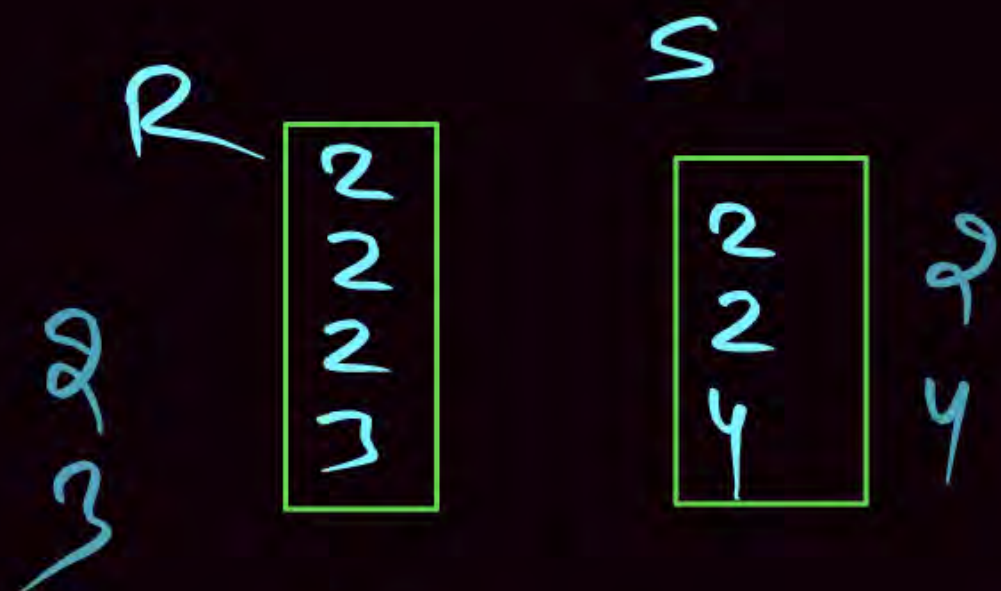
$$\underline{R - S} : \{x / x \in R \wedge x \notin S\} \equiv$$

A
3

$$\underline{R \cap S} : \{x / x \in R \wedge x \in S\} \equiv$$

A
2





- ①  $R \cup S : 2, 3, 4$
- ②  $R \cap S : 2$
- ③  $R - S : 3$
- ④  $S - R : 4$

$$[x | x \in R \vee x \in S]$$

$$[x | x \in R \wedge x \in S]$$

$$[x | x \in R \wedge x \notin S]$$

$$[x | x \in S \wedge x \notin R]$$

Assume Relation R & Relation S consist M & N Tuple Respectively

Minimum

Maximum

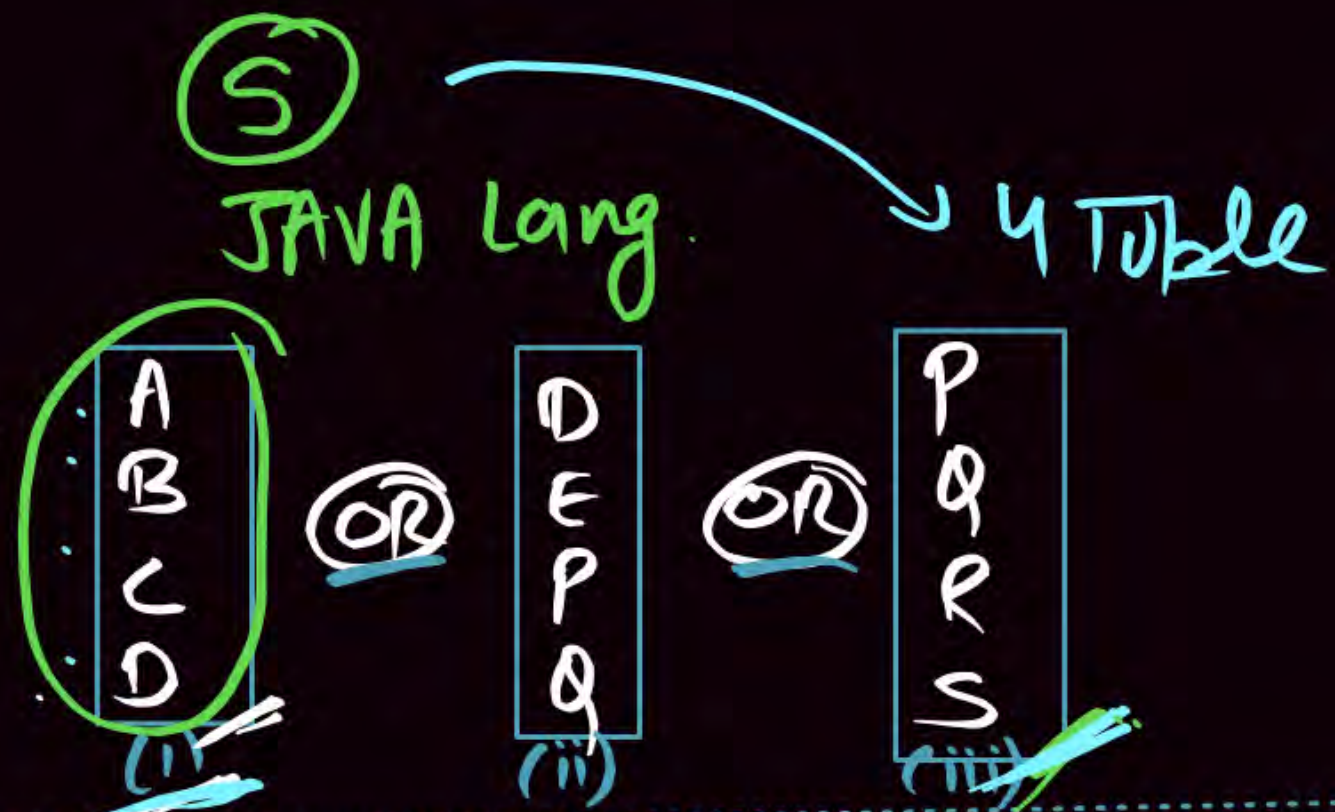
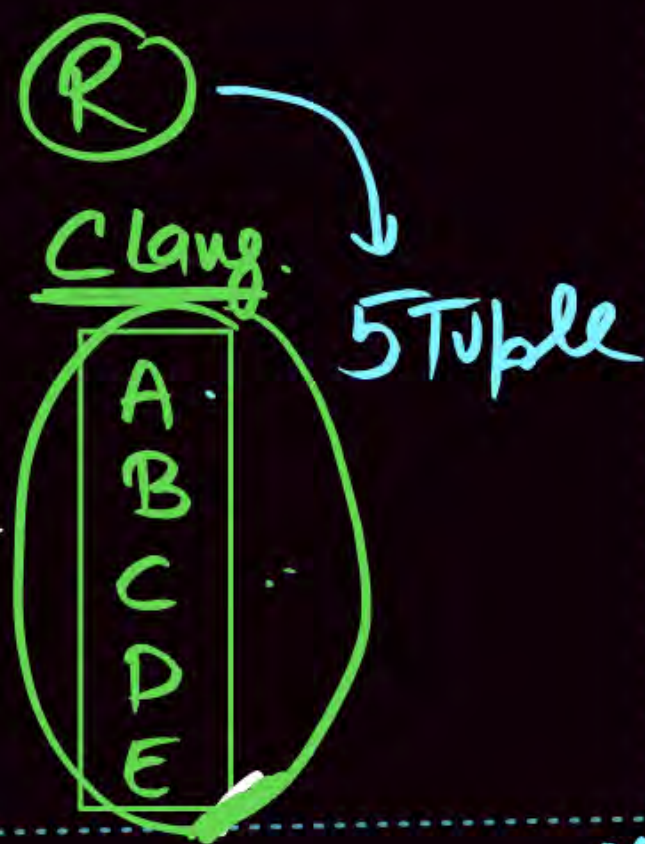
(1) Range of tuples in  $R \cup S = \max(M, N)$  to  $M + N$

(2) Range of tuples in  $R \cap S = \phi$  to  $\min(M, N)$

(3) Range of tuples in  $R - S = \phi$  to M

(4) Range of tuples in  $S - R = \phi$  to N





① RUS

② RAS

③ R-S

④ S-R

Minimum Maximum

$\max(M, N)$  to  $M+N$

$\phi$  to  $\min(M, N)$

$\phi$  to  $M$

$\phi$  to  $N$

R (5 Tuple)

RUS:  $\min$  5

$\max(M, N)$

RAS

$\phi$

S (4 Tuple)

7

$\max$  5+4  
to  $M+N$

4  $\min(M, N)$

## Union Operation

❑ Notation:  $r \cup s$

❑ Defined as :

$$r \cup s = \{t | t \in r \text{ or } t \in s\}$$

❑ For  $r \cup s$  to be valid.

1.  $r, s$  must have the same arity (same number of attributes)
2. The attribute domains must be compatible (example: 2<sup>nd</sup> column of  $r$  deals with the same type of values as does the 2<sup>nd</sup> column of  $s$ )



## Example:

To find all courses taught in the Fall 2009 semester, or in the Spring 2010 semester, or in both.

$$\pi_{\text{course\_id}}(\sigma_{\text{semester} = \text{"Fall"} \wedge \text{year} = 2009}(\text{section})) \cup$$

$$\pi_{\text{course\_id}}(\sigma_{\text{semester} = \text{"Spring"} \wedge \text{year} = 2010}(\text{section}))$$

# Set Difference Operation

□ Notation:  $r - s$

□ Defined as :

$$r - s = \{t \mid t \in r \text{ and } t \notin s\}$$

□ Set differences must be taken between compatible relations.

❖  $r$  and  $s$  must have the same arity

❖ attribute domains of  $r$  and  $s$  must be compatible



## Example:

Example: to find all courses taught in the Fall 2009 semester, but not in the Spring 2010 semester

$$\pi_{\text{course\_id}}(\sigma_{\text{semester} = \text{"Fall"} \wedge \text{year} = 2009}(\text{section})) - \pi_{\text{course\_id}}(\sigma_{\text{semester} = \text{"Spring"} \wedge \text{year} = 2010}(\text{section}))$$

# Example:

Sailors (S<sub>1</sub>)

<u>Sid</u>	Sname	Rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

Sailors (S<sub>2</sub>)

<u>Sid</u>	Sname	Rating	age
28	Yuppy	9	35.0
31	Lubber	8	55.5
44	Guppy	5	35.0
58	rusty	10	35.0

$S_1 - S_2 = 22 \text{ Dustin}$   


---

 $S_2 - S_1 = 28 \text{ Yuppy } 9.35$   
 $44 \text{ Guppy } 5.35$

$S_1 \cap S_2 = 31$   
 $58$





**(1) Union**     $S1 \cup S2$

## (1) Union

Sid	Sname	Rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0
44	guppy	5	35.0
28	yuppy	9	35.0

$S1 \cup S2$



## (2) Set Difference

Sid	Sname	Rating	age
22	dustin	7	45.0

$S1 - S2$

### (3) Intersection

Sid	Sname	Rating	age
31	lubber	8	55.5
58	rusty	10	35.0

$S1 \cap S2$



## Basic operators

### II. Cross product ( $\times$ ):

- ❑  $R \times S$  : It result all attributes of R followed by all attributes of S, and each record of R paired with every record of S.
- ❑ Degree ( $R \times S$ ) = Degree (R) + Degree (S)
- ❑  $| (R \times S) | = | R | \times | S |$

## NOTE:



- ❑ Relation R with n tuples and
- ❑ Relation S with 0 tuples then
- ❑ number of tuples in  $R \times S = 0$  tuples



## I. Natural join ( $\bowtie$ )

$$R \bowtie S \equiv \pi_{\text{distinct attributes}}(\sigma_{\text{equality between common attributes of R and S}}(R \times S))$$

Example:

□  $T_1$  (ABC) and  $T_2$  (BCDE)

$$\therefore T_1 \bowtie T_2 = \pi_{ABCDE} \left( \sigma_{\substack{T_1.B = T_2.B \\ T_1.C = T_2.C}}(T_1 \times T_2) \right)$$

□  $T_1$  (AB) and  $T_2$  (CD)

$$\therefore T_1 \bowtie T_2 \equiv T_1 \times T_2 = \pi_{ABCD}(T_1 \times T_2)$$

## NOTE:



Natural join equal to cross-product if join condition is empty.

## Join ( $\bowtie$ )

### II. Conditional Join ( $\bowtie_c$ )

$$\square R \bowtie_c S \equiv \sigma_c (R \times S)$$



## III. Outer Joins:

### (a) LEFT OUTER JOIN

$R \bowtie S$  : It produces

$(R \bowtie S) \cup \{\text{Records of } R \text{ those are failed join condition with remaining attributes null}\}$

### (b) RIGHT OUTER JOIN ( $\bowtie\rightleftarrows$ )

$R \bowtie\rightleftarrows S$  : It produces

$(R \bowtie S) \cup \{\text{Records of } S \text{ those are failed join condition with remaining attributes null}\}$

### (c) FULL OUTER JOIN ( $\bowtie\rightleftarrows$ )

$R \bowtie\rightleftarrows S = (R \bowtie S) \cup (R \bowtie\rightleftarrows S)$

# Natural Join ⋈



**R**

A	B	C
1	2	4
3	2	6

**S**

B	C	D
2	4	8
2	7	4

**R × S =**

R.A	R.B	R.C	S.B	S.C	S.D
1	2	4	2	4	8
1	2	4	2	7	4
3	2	6	2	4	8
3	2	6	2	7	4



$$R \bowtie S = \pi_{ABCD} \left\{ \sigma_{R.B = S.B \wedge (R \times S)} \right\}$$

$$R \bowtie S =$$

A	B	C	D
1	2	4	8

# Left Outer Join [⋈]

$(R \bowtie S)$

**R**

A	B	C
1	2	4
3	2	6

**S**

B	C	D
2	4	8
2	7	4

$(R \bowtie S) =$

A	B	C	D
1	2	4	8

$R \bowtie S =$

A	B	C	D
1	2	4	8
3	2	6	Null



# Right Outer Join [⋈<sub>R</sub>]

$R \bowtie_R S =$

A	B	C	D
1	2	4	8
Null	2	7	4

# Full Outer Join [⋈]

Full outer join = Left outer join Union Right outer join

$$R \bowtie S = R \bowtie S \cup R \bowtie S$$

A	B	C	D
1	2	4	8
3	2	6	Null

U

A	B	C	D
1	2	4	8
Null	2	7	4

$$R \bowtie S =$$

A	B	C	D
1	2	4	8
3	2	6	Null
Null	2	7	4





Let R and S be two relations with the following schema

R(P, Q, R1, R2, R3)

S(P, Q, S1, S2)

Where {P, Q} is the key for both schemas. Which of the following queries are equivalent?

I.  $\pi_P (R \bowtie S)$

II.  $\pi_P(R) \bowtie \pi_P(S)$

III.  $\pi_P(\pi_{P,Q}(R) \cap \pi_{P,Q}(S))$

IV.  $\pi_P(\pi_{P,Q}(R) - (\pi_{P,Q}(R) - \pi_{P,Q}(S)))$

**A**

Only I and II

**B**

Only I and III

**C**

Only I, II and III

**D**

Only I, III and IV

## Rename operator ( $\rho$ )

It is used to rename table name and attribute names for query processing.

**Example:**

- (I) Stud (Sid, Sname, age)  
 $\rho(\text{Temp}, \text{Stud}) : \text{Temp} (\text{Sid}, \text{Sname}, \text{age})$
- (II)  $\rho_{I, N, A} (\text{Stud}) : \text{Stud} (I, N, A)$   
 All attributes renaming
- (III)  $\rho_{\substack{\text{sid} \rightarrow I \\ \text{age} \rightarrow A}} (\text{Stud}) : \text{Stud} (I, \text{Sname}, A)$

Some attribute renaming

- ❑ It is used to retrieve attribute value of R which has paired with every attribute value of other relation S.
- ❑  $\pi_{AB}(R)/\pi_B(S)$ : It will retrieve values of attribute 'A' from R for which there must be pairing 'B' value for every 'B' of S.



## Expansion of '/' by using basic operator

Example: Retrieve sid's who enrolled every course.

Result:

$$\pi_{sidcid}(\text{Enroll}) / \pi_{cid}(\text{Course})$$

Step 1: Sid's not enrolled every course of course relation.

(Sid's enrolled proper subset of course)

$$\pi_{sid}((\pi_{sid}(\text{Enroll}) \times \pi_{cid}(\text{course})) - \pi_{sidcid}(\text{Enroll}))$$

Step 2:

[sid's enrolled every course] = [sid's enrolled some course] - [sid's not enrolled every course]

$$\therefore \pi_{sidcid}(E) / \pi_{cid}(C) = \pi_{sid}(E) - \pi_{sid}((\pi_{sid}(E) \times \pi_{cid}(C) - \pi_{sidcid}(E)))$$

# Division



Q.

Retrieve all student who are Enrolled **Some course** or **Any course** or **at least one course**?

**Solution**  $\Pi_{\text{Sid}}(\text{Enrolled})$

Enrolled		Course
<u>Sid</u>	<u>Cid</u>	Cid
S <sub>1</sub>	C <sub>1</sub>	C <sub>1</sub>
S <sub>1</sub>	C <sub>2</sub>	C <sub>1</sub>
S <sub>1</sub>	C <sub>3</sub>	C <sub>3</sub>
S <sub>2</sub>	C <sub>1</sub>	
S <sub>2</sub>	C <sub>3</sub>	
S <sub>3</sub>	C <sub>1</sub>	

# Division



Q.

Retrieve all student who are Enrolled every course?

## Solution

$\Pi_{Sid.Cid} (Enrolled) / \Pi_{Cid} (Course)$

Find

2<sup>nd</sup> attribute must be same.

Enrolled	
<u>Sid</u>	<u>Cid</u>
S <sub>1</sub>	C <sub>1</sub>
S <sub>1</sub>	C <sub>2</sub>
S <sub>1</sub>	C <sub>3</sub>
S <sub>2</sub>	C <sub>1</sub>
S <sub>2</sub>	C <sub>3</sub>
S <sub>3</sub>	C <sub>1</sub>

Course
Cid
C <sub>1</sub>
C <sub>1</sub>
C <sub>3</sub>



## Division



$$\Pi_{\text{Sid}}(\text{Enrolled}) - \Pi_{\text{Sid}}[\Pi_{\text{Sid}}(\text{Enrolled}) \times \Pi_{\text{Cid}}(\text{Course}) - \text{Enrolled}]$$

# Division



$$\Pi_{AB}(R) / \Pi_B(S) = \Pi_A(R) - \Pi_A [\Pi_A(R) \times \Pi_B(S) - R]$$

Find

Connection

$$\Pi_{ABCD}(R) / \Pi_{CD}(S) \Rightarrow \Pi_{AB}(R) - \Pi_{AB} [\Pi_{AB}(R) \times \Pi_{CD}(S) - R]$$



Consider the following three relations in a relational database:



Employee (eId, Name), Brand (bId, bName), Own(eId, bId)

Which of the following relational algebra expressions return the set of eIds who own all the brands?  
[GATE: 2022]

- A  $\pi_{eId} (\pi_{eId, bId} (Own / \pi_{bId} (Brand)))$
- B  $\pi_{eId} (Own) - \pi_{eId} ((\pi_{eId} (Own) \times \pi_{bId} (Brand)) - \pi_{eId, bId} (Own))$
- C  $\pi_{eId} (\pi_{eId, bId} (Own) / \pi_{bId} (Own))$
- D  $\pi_{eId} ((\pi_{eId} (Own) \times \pi_{bId} (Own)) / \pi_{bId} (Brand))$



Consider the two relation Suppliers and Parts are given below.

Suppliers		Parts
$S_{no}$	$P_{no}$	$P_{no}$
$S_1$	$P_1$	$P_2$
$S_1$	$P_2$	$P_4$
$S_1$	$P_3$	
$S_1$	$P_4$	
$S_2$	$P_1$	
$S_2$	$P_2$	
$S_3$	$P_2$	
$S_4$	$P_2$	
$S_4$	$P_4$	

$$\pi_{S_{no} P_{no}} (\text{Suppliers}) / \pi_{P_{no}} (\text{Parts})$$

The number of tuples are there in the result when the above relational algebra query executes is \_\_\_\_\_.



**THANK  
YOU!**

