

COMPUTER SCIENCE



Operating System

Virtual Memory

Lecture No:07



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Virtual memory

VIRTUAL MEMORY

LRU Approximations: (They approximate to the behaviour of LRU)

- a) Reference Bit (R)
- b) Additional Ref bits
- c) Second chance (clock Algo)
- d) Enhanced Second chance
(Not Recently Used)
(NRU)

Reference Bit (R)

1) Reference bit (R)

Criteria: R

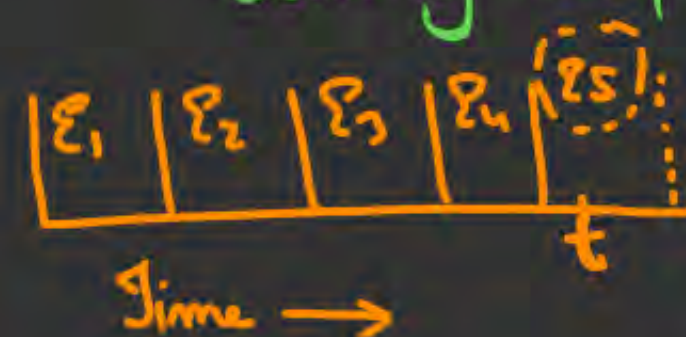
Start Search from first entry of P.T to find a Page whose R value is '0';

0 → Page has not been Referred during the Present Epoch;

1 → Page has been referred atleast once during the present Epoch;

P	f	V/I	T.O.L	R
0	a	1	1	1
1	b	1	3	1
2	-	0	-	-
3	k	1	0	1
4	l	1	2	1

Page Table



When all values of 'R' is one
"Fails"

(ii) Additional Ref. bits

Each page is associated with multiple Ref. bits
- 8 'R' bits.

	R ₁	R ₂	R ₃	R ₄	R ₅	R ₆	R ₇	R ₈
P _a	1	1	0	1	1	1	1	1
P _b	0	0	1	1	1	1	1	1
P _c	1	0	1	0	1	1	1	1

P₃ × → P.T

When Curr. Epoch gets over

Current Epoch

P_a ×

P_c ✓

All 'R' values of Curr. Epoch are cleared to '0' & they are shifted left

③ Second chance
 * clock Algorithm

Criteria: T.O.L + R

→ FIFO: → Belady's Anomaly

P	f	V/I	T.O.L	R	M
0	a	1	2	1	0
1	b	1	4	1	0
2	—	0	—	—	—
3	c	1	0	0	1
4	d	1	3	1	0
5	f	1	1	0	1

R: 1 ✓

P₅

P₃ ✓

: P₄ ✓

: P₃

4) Enhanced
Second chance

NRU:

Criteria: R + M

↑
 Modified bit

LRU

<u>RM</u>			
0	0	—	1
0	1	—	1
1	0	—	1
1	1	—	1

Thrashing: Excessive/High Paging activity;

< very high page fault rate of processes in the system >

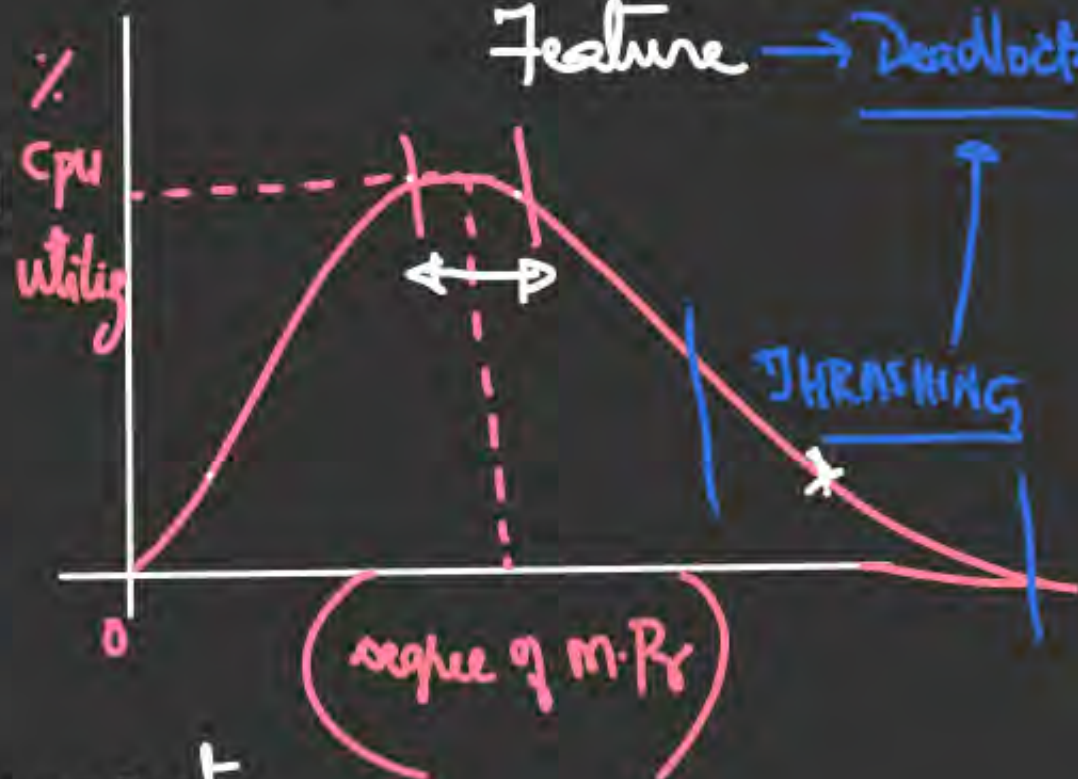
↳ Act of servicing the Page fault;

→ is an undesirable feature → Deadlock

Reasons:

I: Primary:

- ✓ → Lack of Frames (Memory)
- ✓ → High degree of M.P.R



II. Other Reasons:

→ Page replacement Algo.

→ Page-Size: large → (No. of Pages will be less)

Thrashing Control Strategies

Prevention

Controlling degree of M.P.R

< LTS >

Detection & Recovery

Recovery

→ High Paging disk utiliz.

Suspension

(M.T.S)

Low CPU Utiliz.
High degree of M.P.R

Programming Techniques & Data Structures

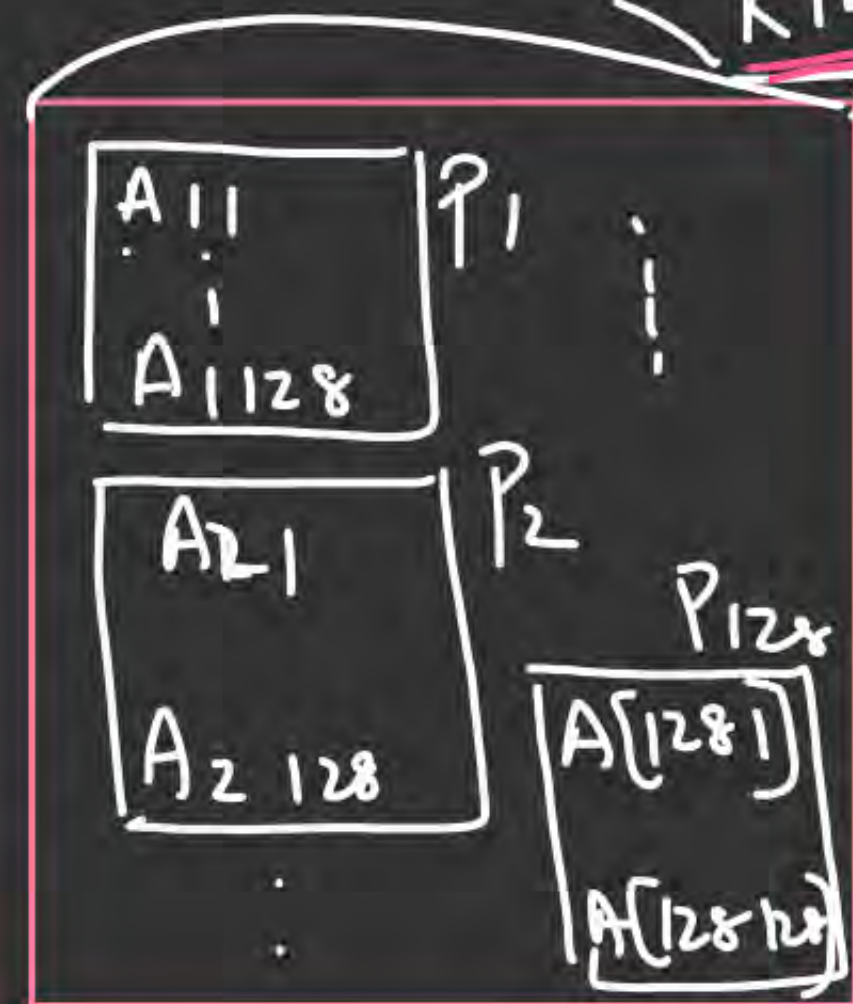
① int A[1..128, 1..128]; PS=128; FIFO; P.D.P; M=127

✓ a) $\text{for } i \leftarrow 1 \text{ to } 128 : \quad (128)^2$
 $\text{for } j \leftarrow 1 \text{ to } 128 : \quad \text{Page fault}$
 $\text{CMD } A[j, i] = 1; \quad \left. \vphantom{\text{for } j \leftarrow 1 \text{ to } 128} \right\} (128)$

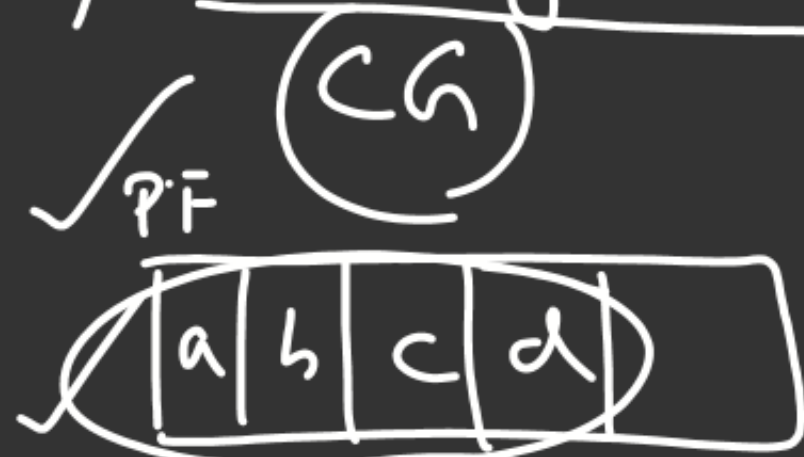
✓ b) $\text{for } i \leftarrow 1 \text{ to } 128 : \quad (128) \cdot 1$
 $\text{Efficient } \left\{ \begin{array}{l} \text{for } j \leftarrow 1 \text{ to } 128 \\ A[i, j] = 1; \end{array} \right. \quad \text{Locality Model}$
RMD



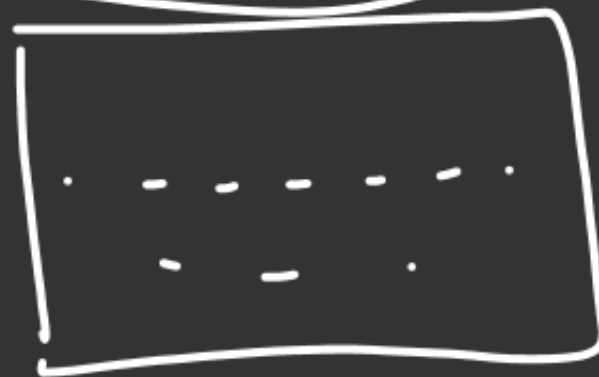
frames $N_{\text{pages}} = 128$
 $\langle \text{RMD} \rangle$



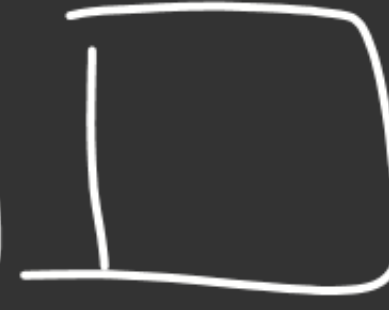
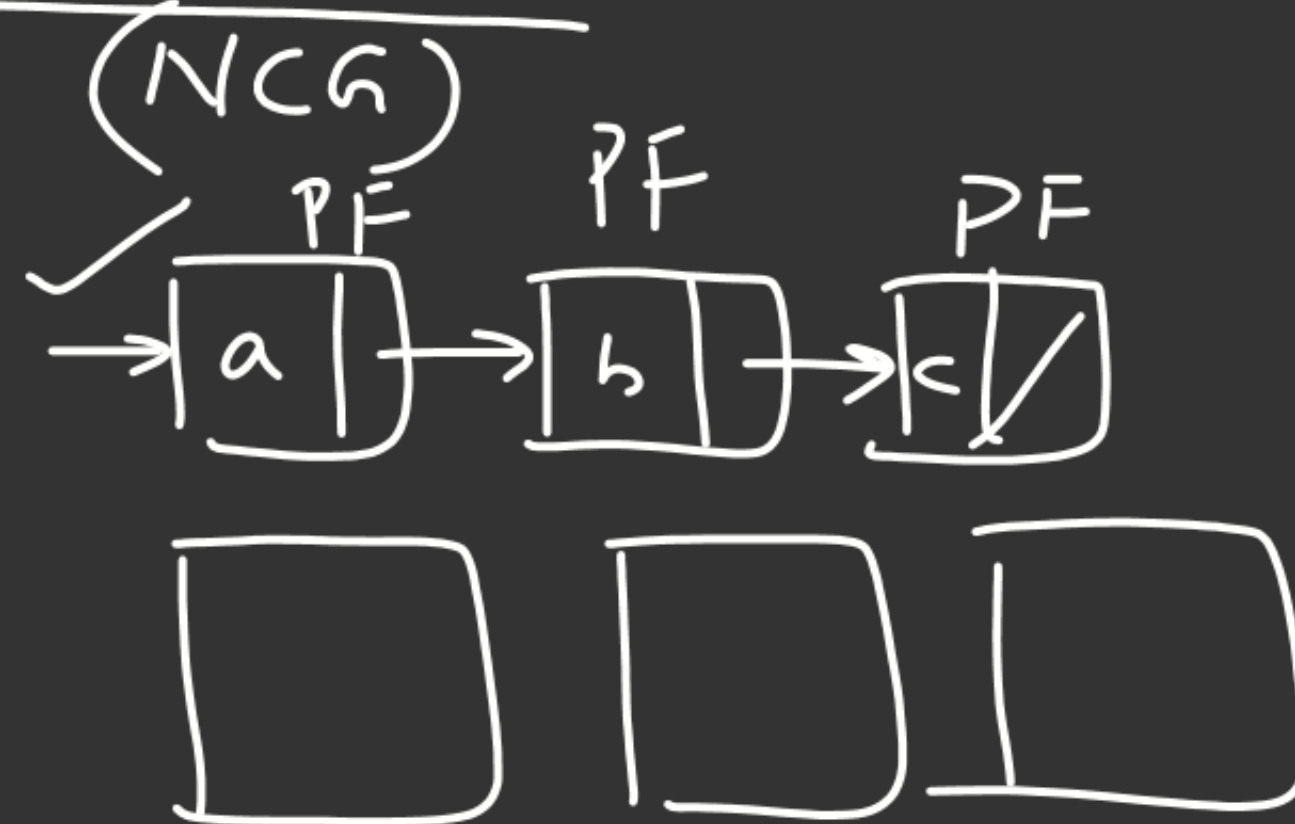
II Arrays vs Linked list



Locality

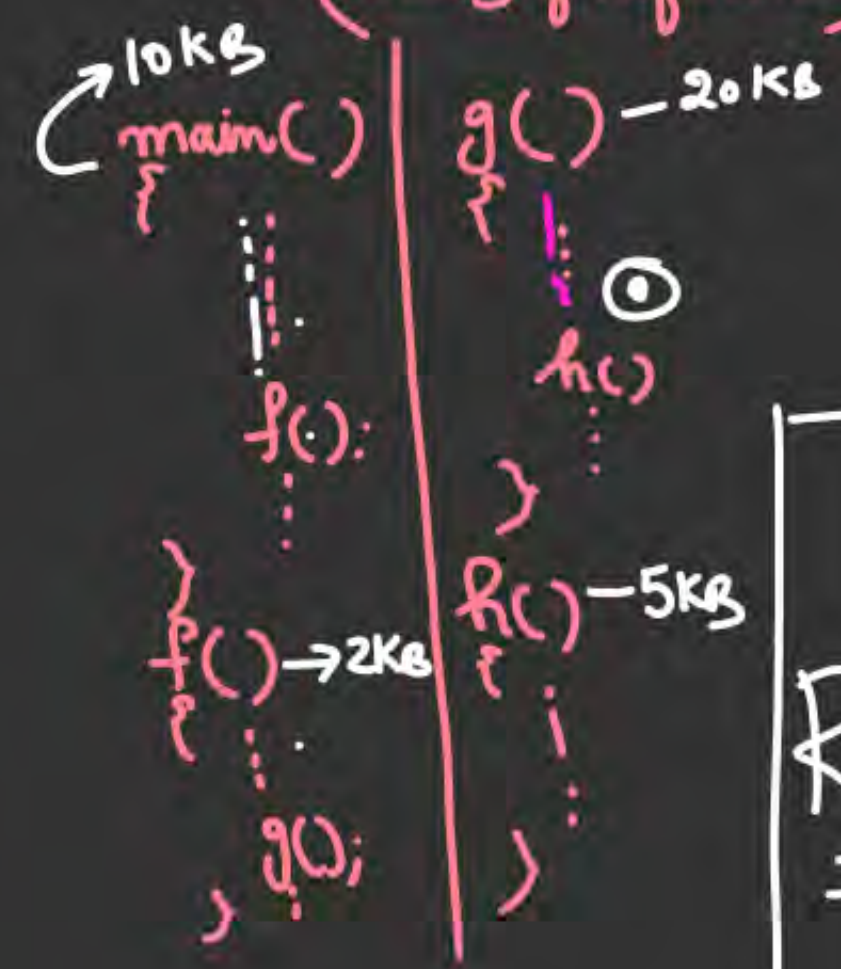


Page



WORKING SET MODEL

(Locality of Reference)



(helps Reduce P.F rate & utilizes Memory Efficiently)

Total Prog. Size: 37KB

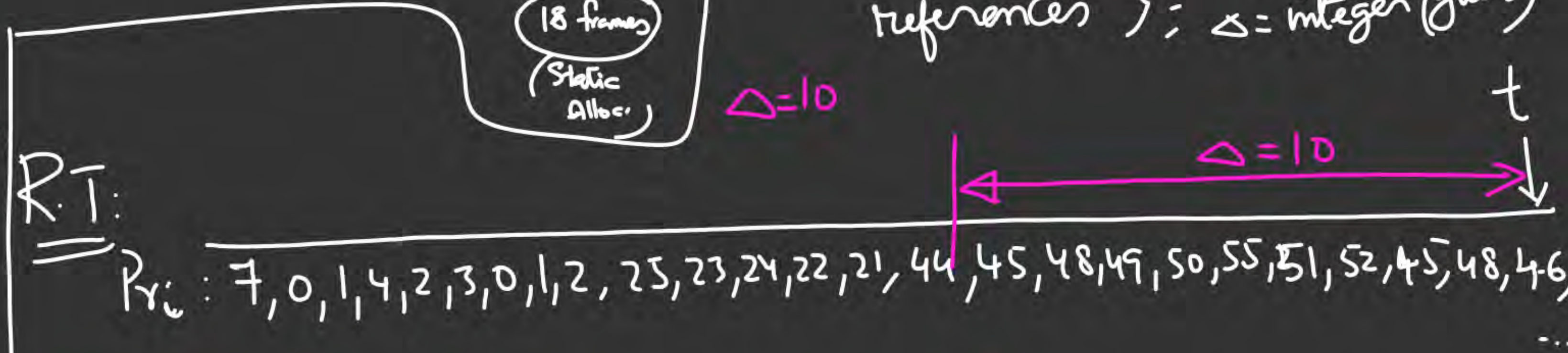
P.S = 1KB; No. of Pages = $\langle 37 \rangle$



$\Delta = 10$

Work Set Window (WSW)

= {Set of unique Pages in the ref string during the Past Δ references} ; Δ = integer (guar)



Size of locality = $\langle 45, 46, 48, 49, 50, 51, 52, 55 \rangle$

WSW_i^t = 8 pages demand of the Process

δ_i

→ n : no. of Processes

→ $\underline{S_i}$: demand of Process $\langle \underline{WSWS_i} \rangle$
for frames

→ D : Total demand

$$D = \sum_{i=1}^n S_i$$

→ M : Avail. frames

't'

I. $D \approx M$

: NO THRASHING

II. $\overset{(1000)}{D} > \overset{(100)}{M}$ (SWAP OUT)

: THRASHING _{Susp.}

III. $D < M$

: NO THRASHING

$\langle \text{Inc. degree of M.Pr} \rangle$

Q.1

Consider a virtual memory system with FIFO page replacement policy, for an arbitrary page access pattern, increasing the number of page frames in main memory will

11:45
am

- A Always decrease the number of page faults.
- B Always increase the number of page faults
- C Sometimes increase the number of page faults ✓ (Belady's Anomaly)
- D Never affect the number of page faults.

Q.2

The minimum number of page frames that must be allocated to a running process in a virtual memory environment is determined by

A

the instruction set architecture ✓

B

page size

C

physical memory size

D

number of processes in memory

Mim → Process should be able to succ. execute 1-Instn;

Multiple Pgs



Add $\bar{D}_1, \bar{O}_2, \bar{O}_3$

Format

A.M

direct

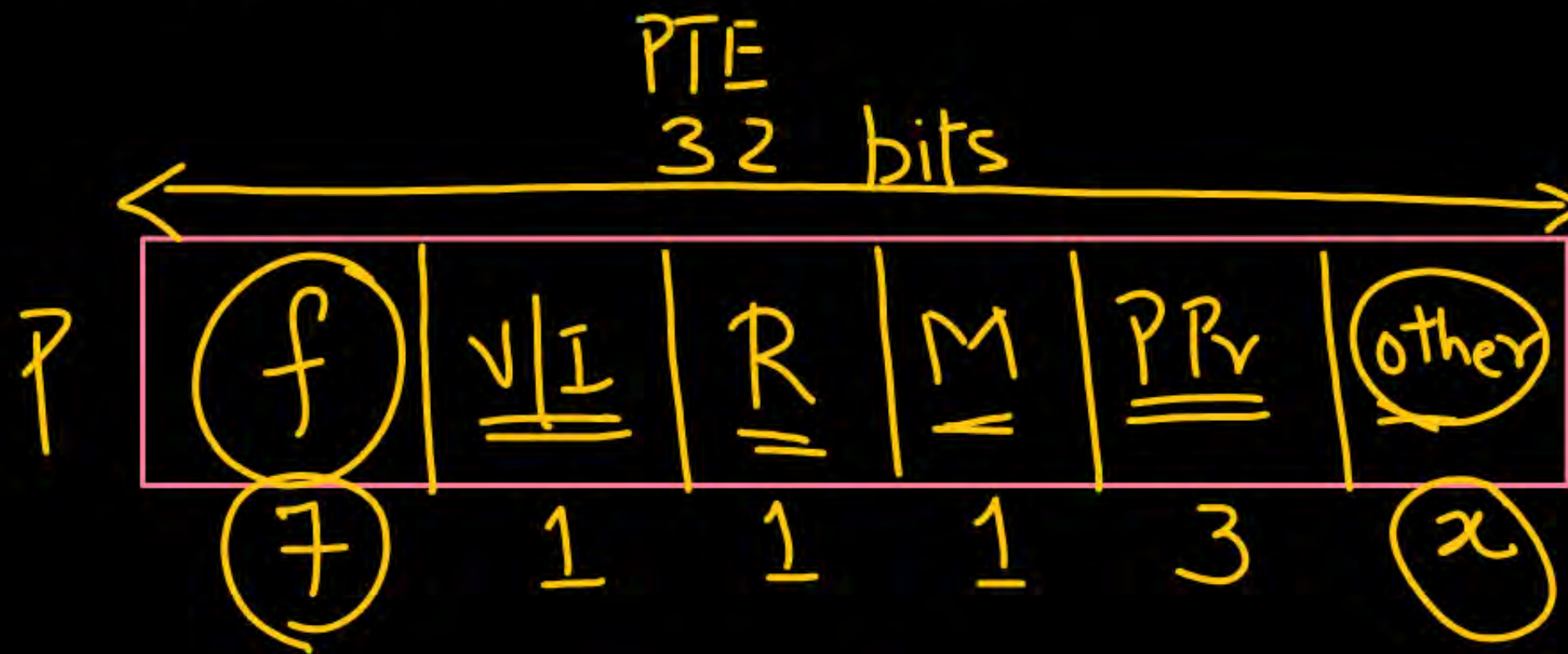
Indirect

I. Architecture

Q.3



Consider a System with $V.A.S = P.A.S = 2^{16}$ Bytes. Page Size is 512 Bytes. The size of Page Table entry is 32 bits. If the Page Table Entry contains besides other information 1 V/I bit, 1 Reference, 1 Modified bit, 3 bits for Page Protection. How many bits can be assigned for storing other attributes of the Page. Also compute Page Table Size in Bytes?



$$\begin{aligned} P.A.S &= V.A.S = 2^{16} B \\ \left\{ \begin{array}{l} P.S = 512 B \\ N = M = \frac{2^{16}}{2^9} = 2^7 \\ P = f = 7 \text{ bits} \end{array} \right. \end{aligned}$$

$$\begin{aligned} 13 + x &= 32 \\ x &= 19 \text{ bits} \checkmark \end{aligned}$$

$$\begin{aligned} P.T.S &= N * e \\ &= 128 * 4 B = 512 B \checkmark \end{aligned}$$

Q.4

Let the Page Reference and the Delta (\blacktriangle) be "c c d b c e c e a d" and 4, respectively. The initial Working Set at time $t = 0$ contains the pages {a, d, e}, where 'a' was referenced at time $t = 0$, 'd' was referenced at time $t = -1$, and 'e' was referenced at time $t = -2$. Determine the total number of page faults and the average number of page frames used by computing the working set at each reference.



$$\Delta = 4$$

$$\text{PF's: } 5$$

-2	-1	0	1	2	3	4	5	6	7	8	9	10
e	d	a	c	c	d	b	c	e	c	e	a	d

$$t_0: \langle \underline{e d a} \rangle: 3 \times$$

$$t_1: \langle \underline{e d a c} \rangle: 4$$

$$t_2: \langle \underline{d a c} \rangle: 3$$

$$t_3: \langle \underline{a c d} \rangle: 3$$

$$t_4: \langle \underline{c d b} \rangle: 3$$

$$t_5: \langle \underline{d b c} \rangle: 3$$

$$t_6: \langle \underline{d b e c} \rangle: 4$$

$$t_7: \langle \underline{b e c} \rangle: 3$$

$$t_8: \langle \underline{c e} \rangle: 2$$

$$t_9: \langle \underline{c e a} \rangle: 3$$

$$t_{10}: \langle \underline{c e a d} \rangle: 4$$

Q.5



Recall that Belady's anomaly is that the page-fault rate may increase as the number of allocated frames increases. Now, consider the following statements:

- ✓ **S1:** Random page replacement algorithm (where a page chosen at random is replaced) suffers from Belady's anomaly
- S2:** LRU page replacement algorithm suffers from Belady's
✗ anomaly

Which of the following is CORRECT?

- A** S1 is true, S2 is true
- ✓ **B** S1 is true, S2 is false
- C** S1 is false, S2 is true
- D** S1 is false, S2 is false

Q.6

In the context of operating systems, which of the following statements is/are correct with respect to paging?



msq

- A** Page size has no impact on internal fragmentation. ✗
- B** Paging helps solve the issue of external fragmentation. ✓
- C** Paging incurs memory overheads ✓ (P.T-Size ovhd)
- D** Multi-level paging is necessary to support pages of different sizes ✗

<Bc>



**THANK
YOU!**

