

# CS & IT ENGINEERING

## Compiler Design

*Lexical Analysis & Syntax Analysis*

Lecture No. 10



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TOPICS TO BE  
COVERED

→ LR(0) Table

SLR(1) "

LALR "

CLR "

→ LR Algorithms

→ Operator precedence



# LR(0) Table construction :

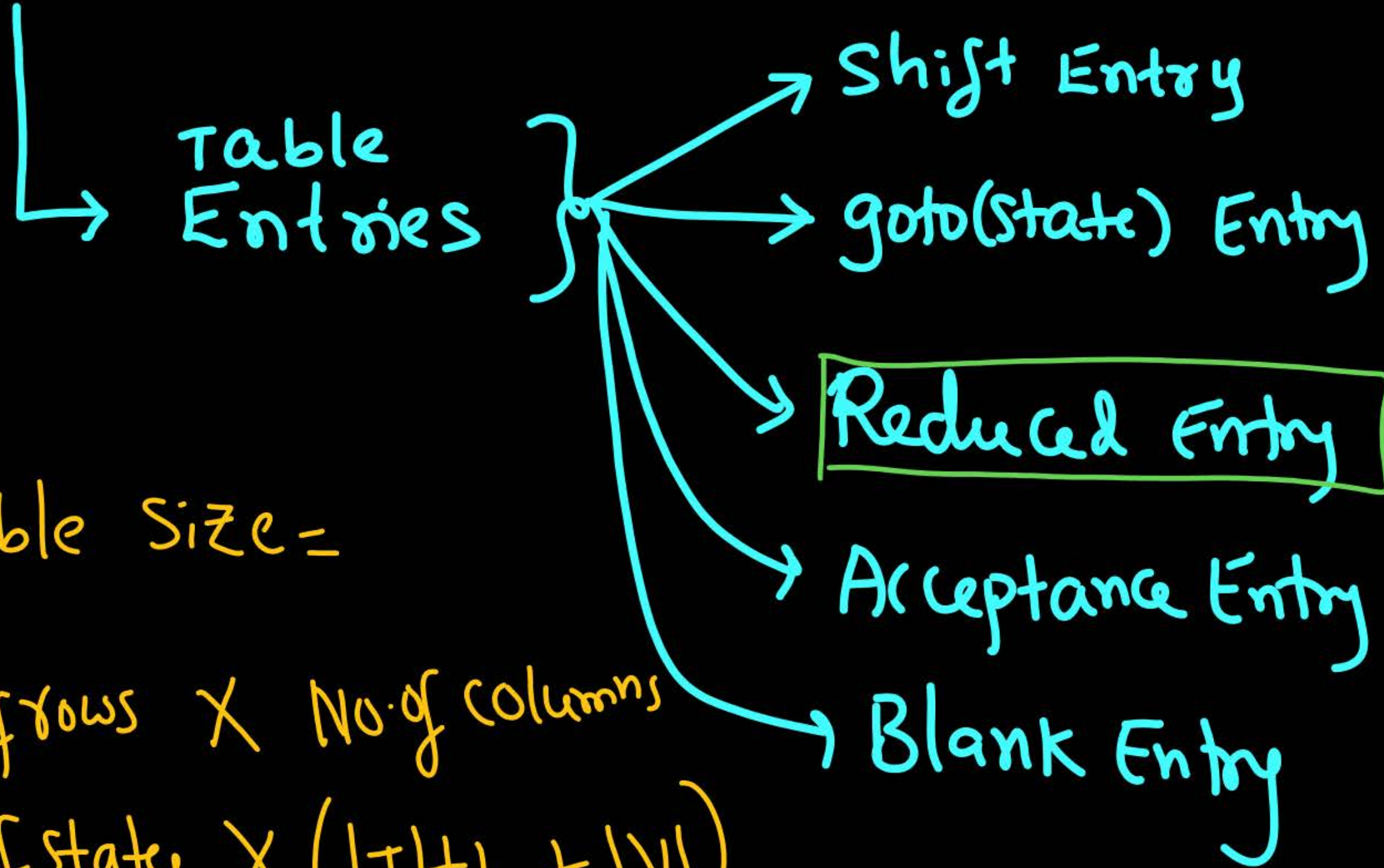
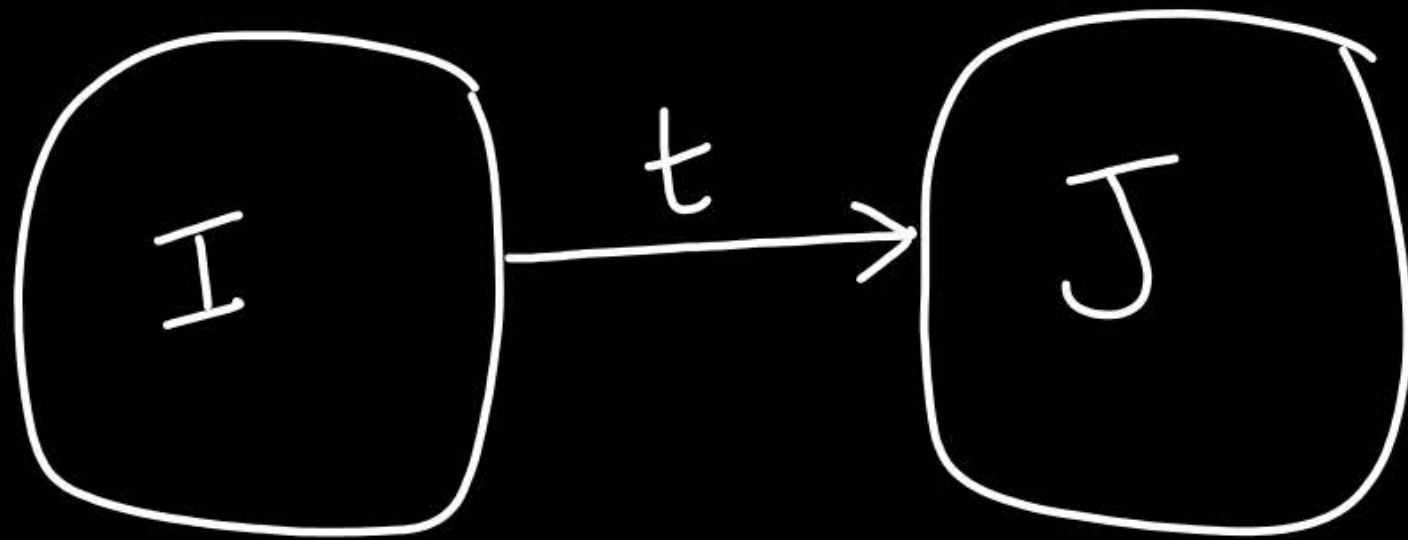


Table size =

No. of rows  $\times$  No. of columns

No. of states  $\times$   $\left( \underbrace{|T|+1}_{\text{Action}} + \underbrace{|V|}_{\text{goto}} \right)$

# Shift Entry in LR(0) / SLR(1) / LALR(1) / CLR(1) :



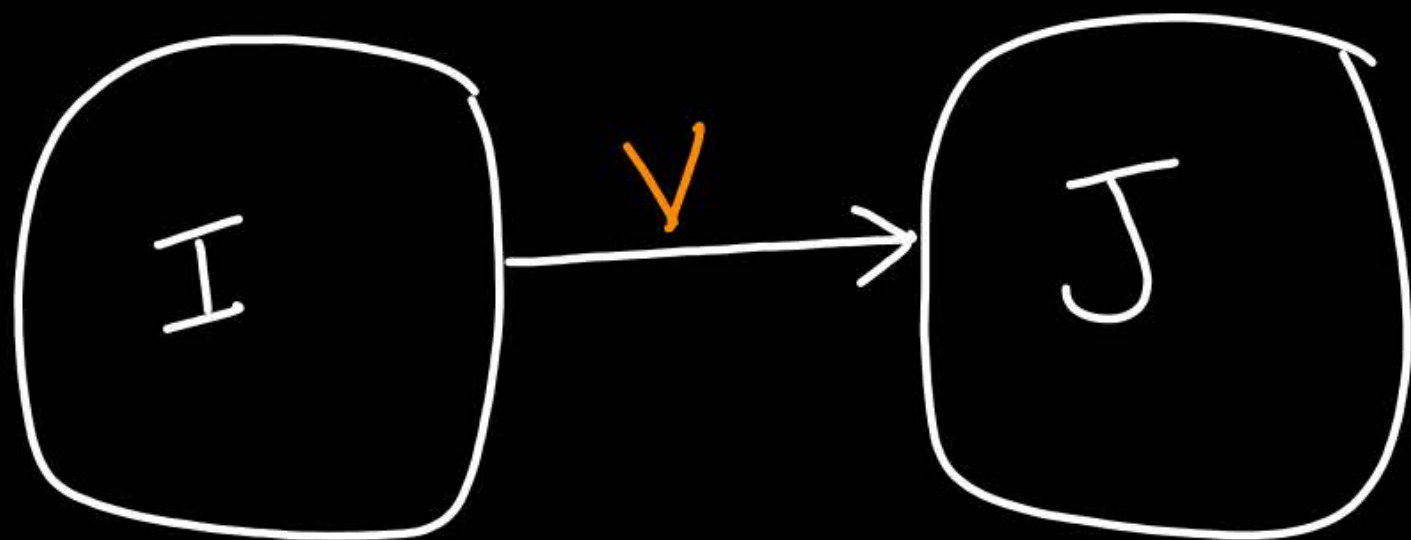
Every terminal transition  
will make one shift entry

	t
I	S <sub>J</sub>

No. of terminal transitions  
=  
No. of Shift Entries



State Entry in LR(0) / SLR(1) / LALR(1) / CLR(1) :  
(goto)



Every Non-terminal transition  
will make one goto entry

	V
I	J

No. of Nonterminal transitions  
=  
No. of goto Entries

Acceptance Entry: for LR(0) / SLR(1) / LALR(1) / (LR(1))



$S' \rightarrow S.$   
Acceptance Item

I

	\$
I	accept



Reduced Entries for LR(0): [Every Reduced Item in every state, need to apply the below Rule]



I  
(ii)  $X \rightarrow \alpha.$

I

← Action →				
$R_{ii}$	$R_{ii}$	$R_{ii}$	$R_{ii}$	
$x \rightarrow \alpha$	$x \rightarrow \alpha$	$x \rightarrow \alpha$	$x \rightarrow \alpha$	

Reduced Entries for CLR & LALR:

I  
(ii)  $X \rightarrow \alpha., t_1$

Reduced Entries for SLR(1)

Follow(X) =  $\{t_1, t_2\}$

I

	$t_1$	$t_2$
$R_{ii}$		
	$R_{ii}$	$R_{ii}$

Computes follow set using whole CFG

I

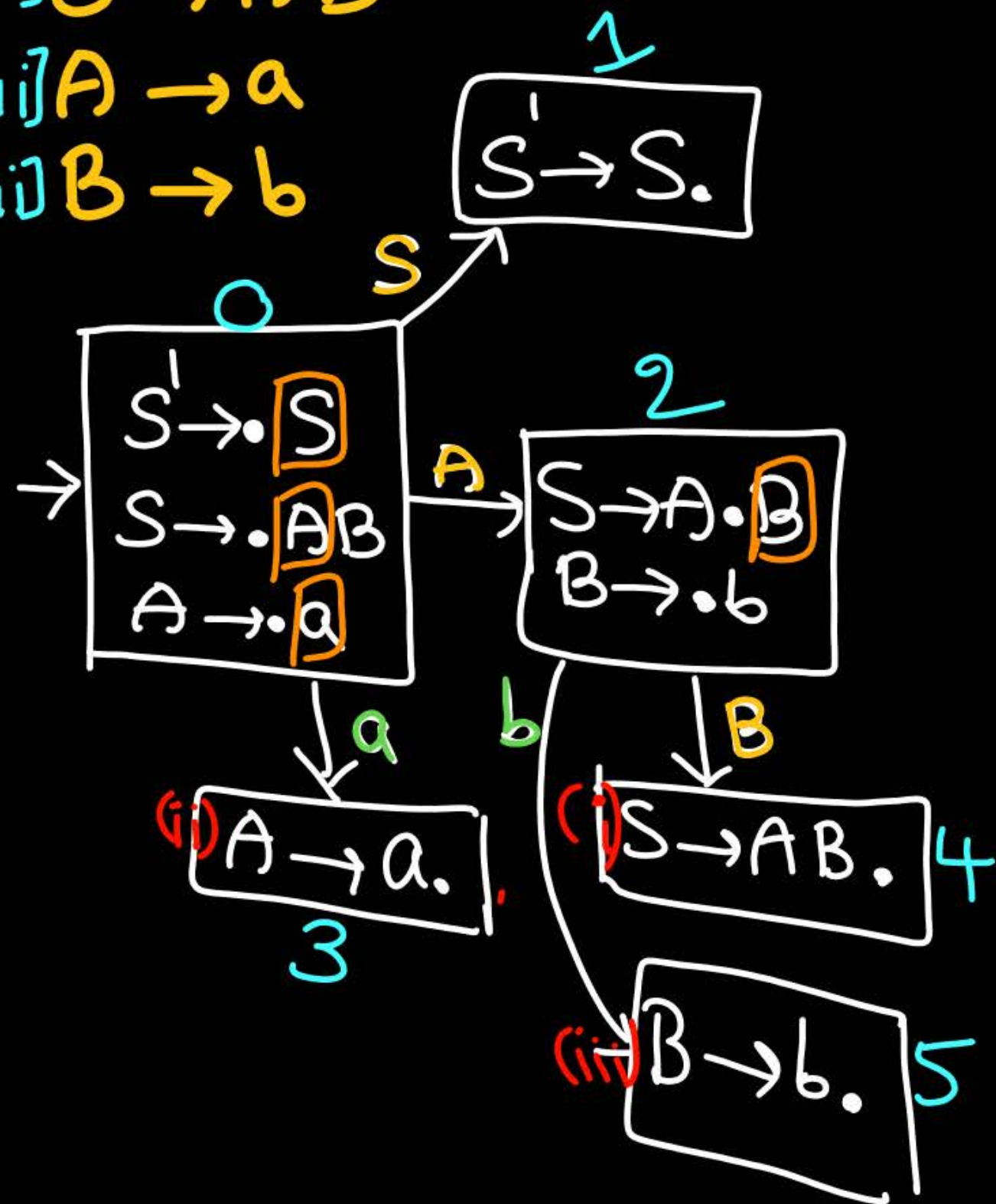
	$t_1$
$R_{ii}$	

# LR(0) Table:

[i]  $S \rightarrow AB$

[ii]  $A \rightarrow a$

[iii]  $B \rightarrow b$



States

LR(0)	Action			Goto			P W
	a	b	\$	S	A	B	
0	$S_3$			1	2		
1			Accept				
2		$S_5$				4	
3	$R_{ii}$	$R_{ii}$	$R_{ii}$				
4	$R_i$	$R_i$	$R_i$				
5	$R_{iii}$	$R_{iii}$	$R_{iii}$				



SLR(1) Table:

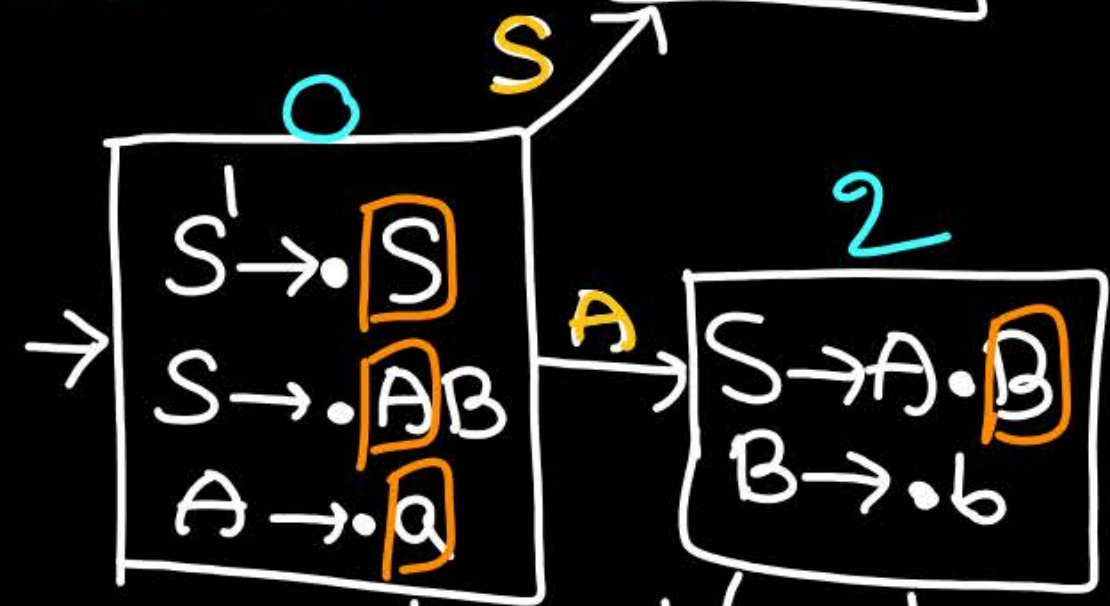
$F_0(S) = \{ \$ \}$   
 $F_0(A) = \{ b \}$   
 $F_0(B) = \{ \$ \}$

[i]  $S \rightarrow AB$

[ii]  $A \rightarrow a$

[iii]  $B \rightarrow b$

1  
 $S' \rightarrow S \cdot$



$F_0(a) = \{ b \}$   
 (ii)  $A \rightarrow a \cdot$   
 3

$3 \mid b$   
 $R_{ii}$

(i)  $S \rightarrow AB \cdot$   
 4

(iii)  $B \rightarrow b \cdot$   
 5

States

SLR(1)	Action			Goto			P W
	a	b	\$	S	A	B	
0	$S_3$			1	2		
1			Accept				
2		$S_5$				4	
3		$R_{ii}$					
4			$R_i$				
5			$R_{iii}$				

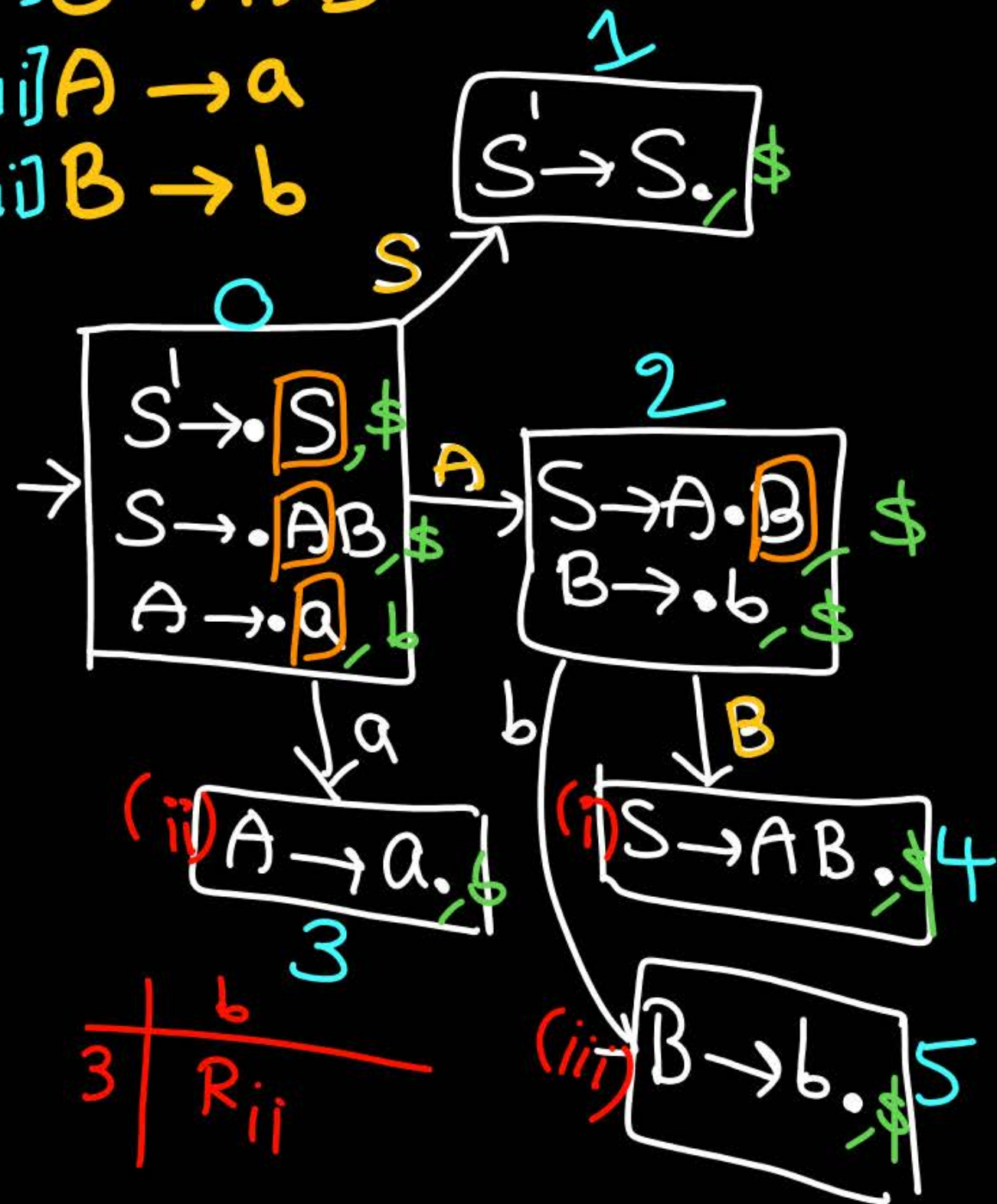


# LALR(1) Table:

[i]  $S \rightarrow AB$

[ii]  $A \rightarrow a$

[iii]  $B \rightarrow b$



Current LALR(1) Table:

States	Action			Goto			P W
	a	b	\$	S	A	B	
0	$S_3$			1	2		
1			Accept				
2		$S_5$				4	
3		$R_{ii}$					
4			$R_i$				
5			$R_{iii}$				





If CLR DFA & LALR DFA same

then Table also same.

If CLR DFA has more States than LALR

then Table size also different

State numbering

0 1 2 3 4 . . .

production  
numbering

i ii iii





$\hookleftarrow$   
 $(i) A \rightarrow a.$   
 $(ii) B \rightarrow a.$

RR conflict

$\underbrace{|T|+1}_{3+1}$   
 4 RR conflicts in LR(0)

	a	b	c	\$
$R_i$	$R_i$	$R_i$	$R_i$	$R_i$
$R_{ii}$	$R_{ii}$	$R_{ii}$	$R_{ii}$	$R_{ii}$





$n_1$   
LR(0)

$n_2$   
SLR

$n_3$   
LALR

$n_4$   
CLR

(No. of rows)  
No. of States

$$n_1 = n_2 = n_3 \leq n_4$$

$n_i \rightarrow \text{no. of states}$

Size of Table

$$n_1 = n_2 = n_3 \leq n_4$$

$n_i \rightarrow \text{Size of Table}$

No. of Shift Entries

$$n_1 = n_2 = n_3 \leq n_4$$

$n_i \rightarrow \text{no. of shift entries}$

No. of goto entries

$$n_1 = n_2 = n_3 \leq n_4$$

$n_i \rightarrow \text{no. of goto entries}$

\*\*\* No. of Reduced Entries

$$n_1 \geq n_2 \geq n_3 \geq n_4$$

$n_i \rightarrow \text{no. of reduced entries}$

No. of columns

$$n_1 = n_2 = n_3 = n_4$$

$n_i \rightarrow \text{no. of columns}$



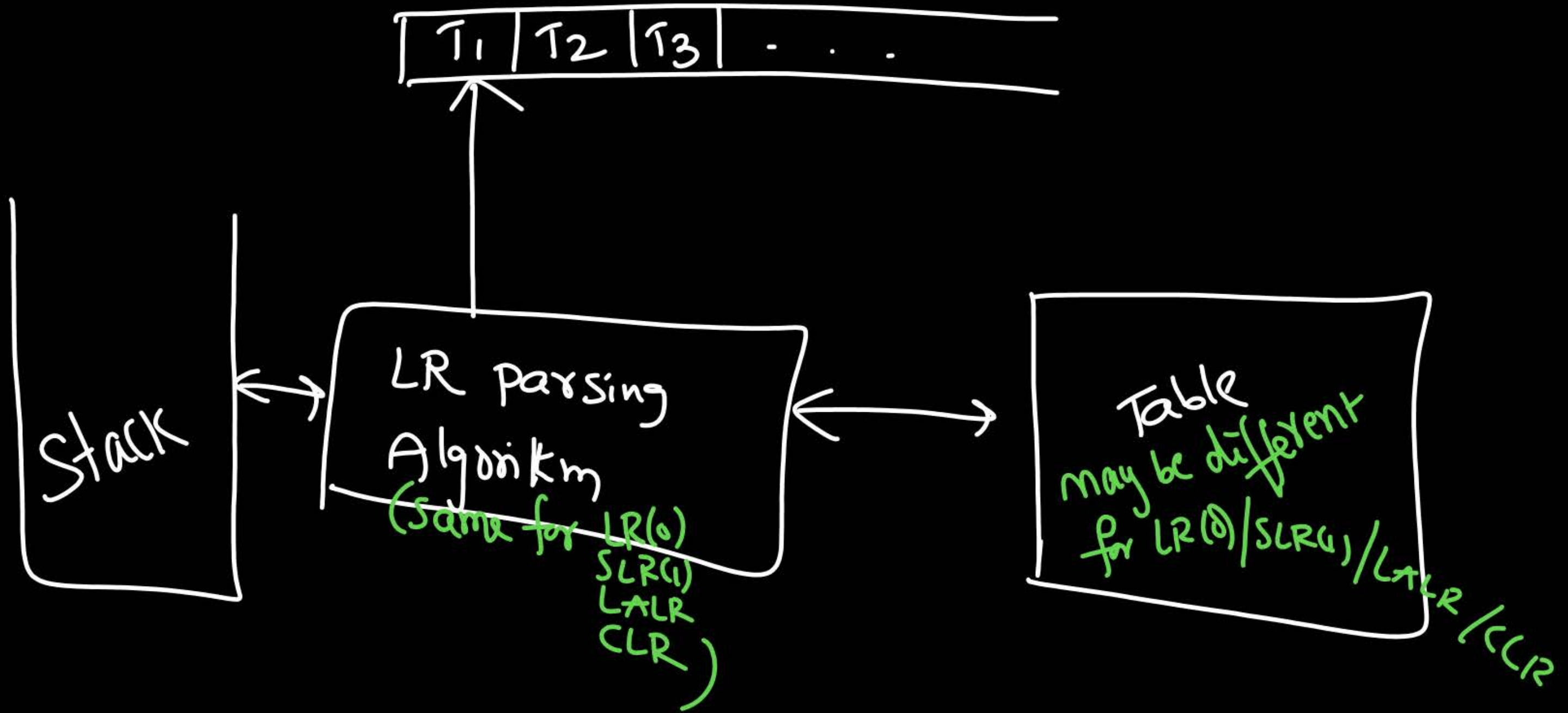
# Reduced Entries

- In LR(0) : no knowledge of look-a-heads  

All columns of action table will have reduced entries
- In SLR(1) : Simple knowledge for computing look-a-heads using whole CFG.  

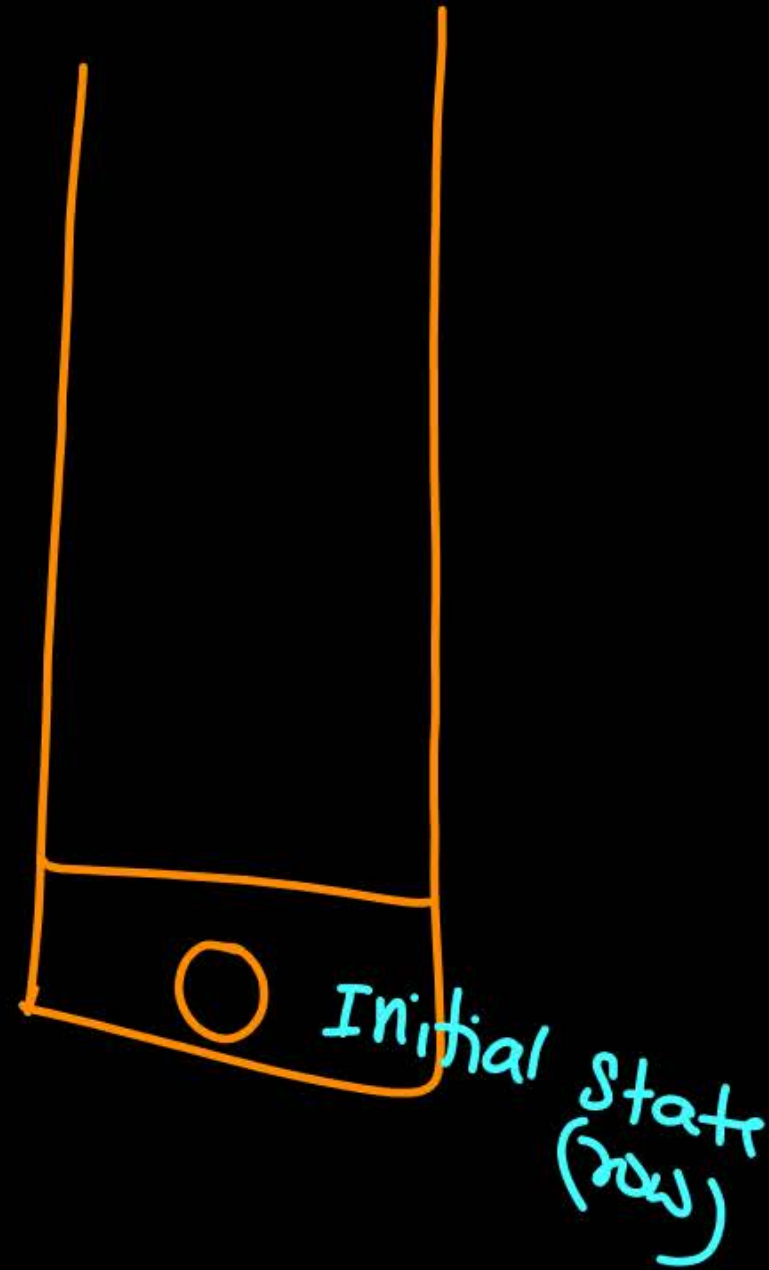
Follow Set of Reduced Item decides Reduced Entries
- In LALR(1) : Combined paths knowledge to compute look-a-heads
- In CLR(1) : Exact path knowledge  
 (Canonical)

# LR parser





# LR Parsing Algorithm:



I) Shift Action

II) Reduced Action  
(goto will be used internally for reduced action)

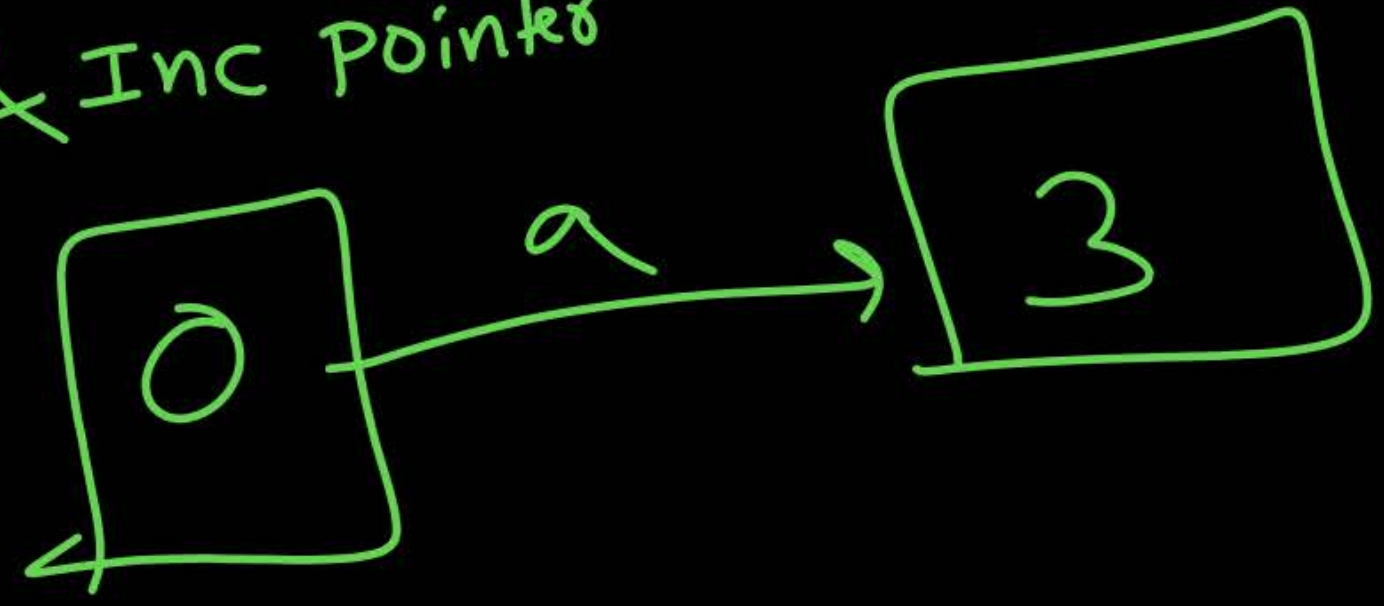
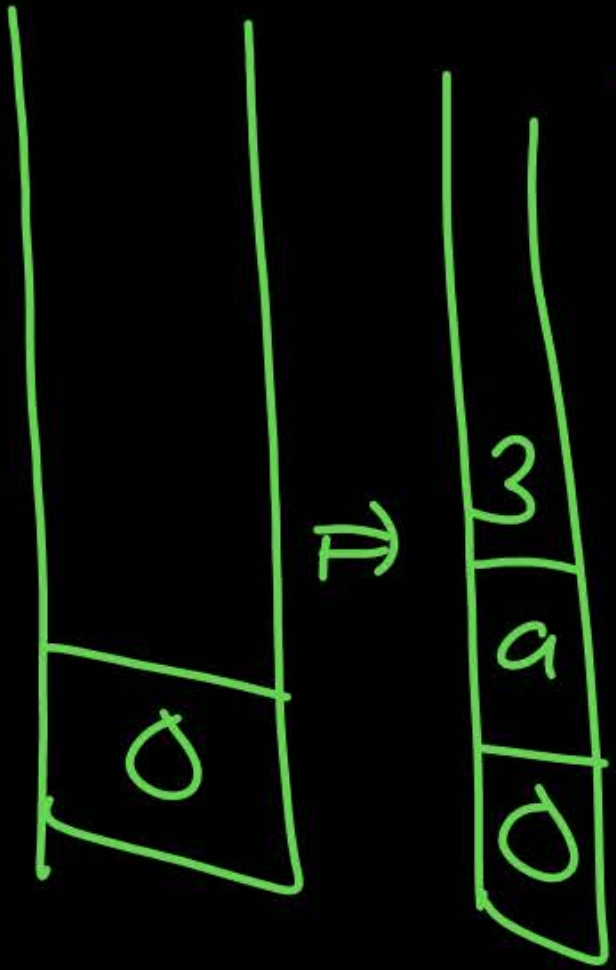
III) Accept Action

IV) Error Action

Shift Action:

$$M[0, a] = S_3$$

- i) Push a & Inc pointer
- ii) Push 3

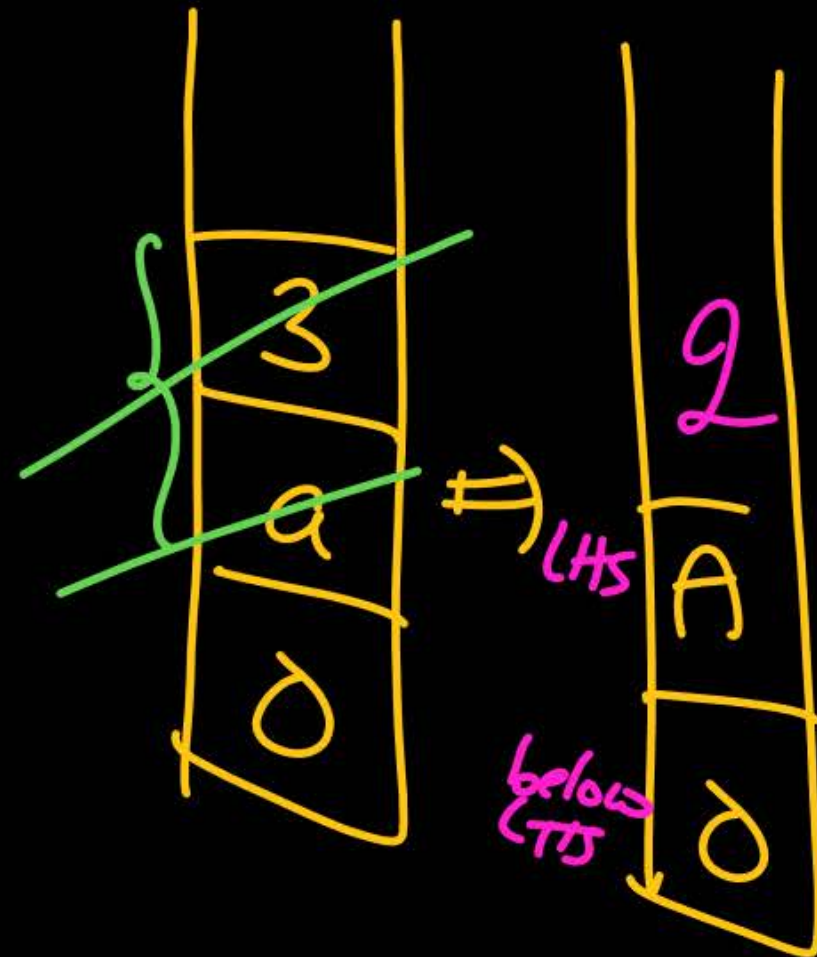
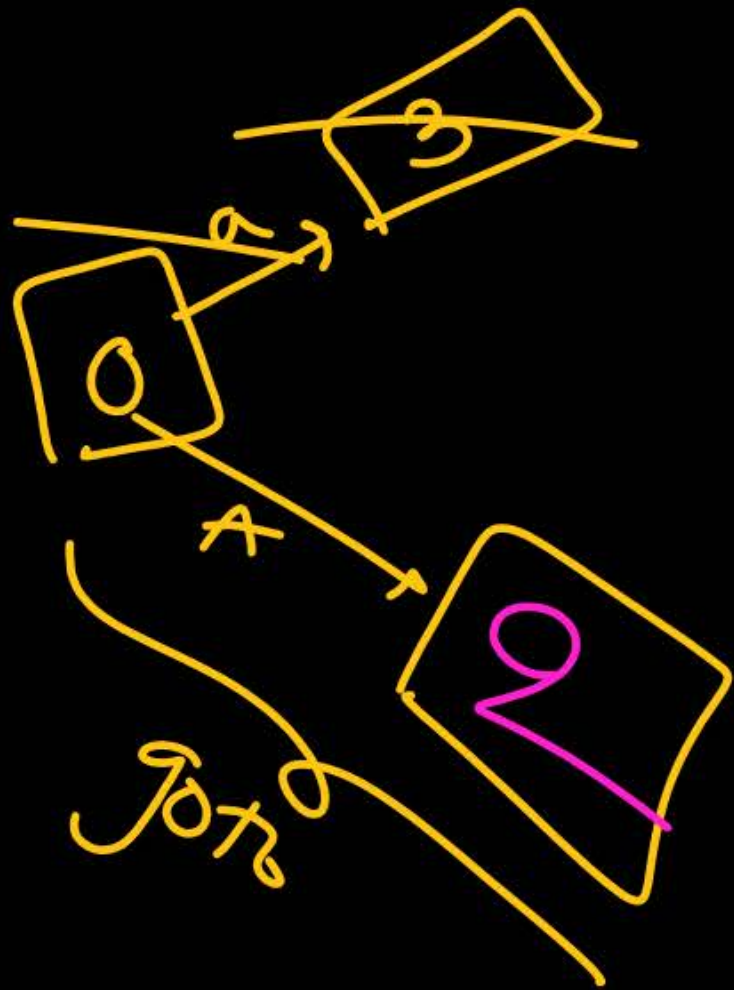




Reduced Action:



$M[3, b] : A \rightarrow a$



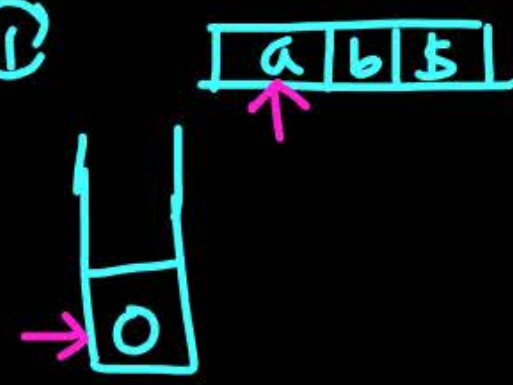
I) POP  $2 * |RHS|$   
POP  $2 * |a|$   
2

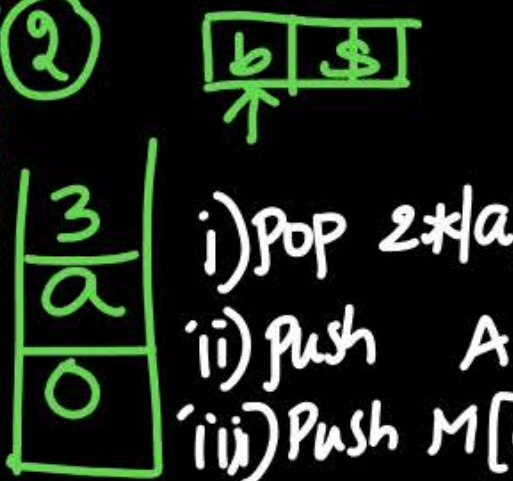
II) Push LHS  
(A)

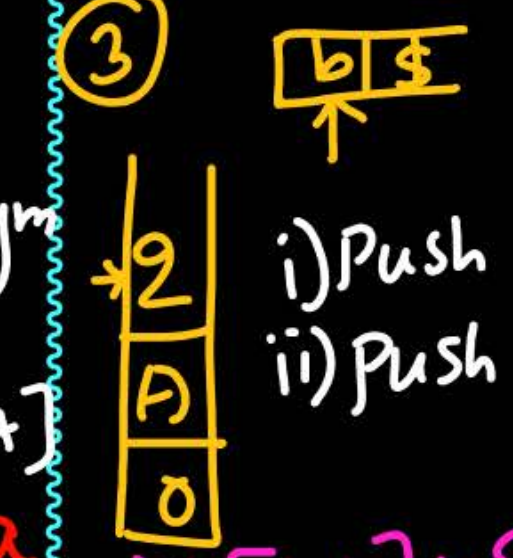
goto table  
III) Push  $M[\text{below LHS}, LHS]$   
 $M[0, A]$




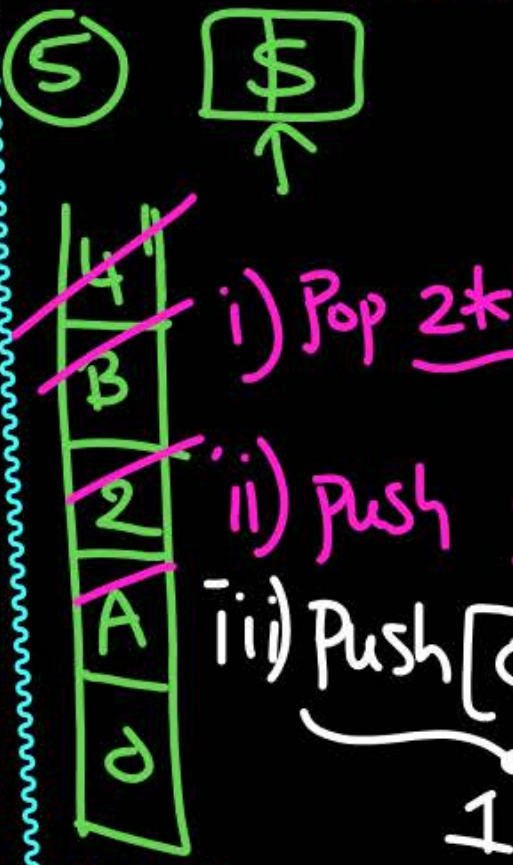


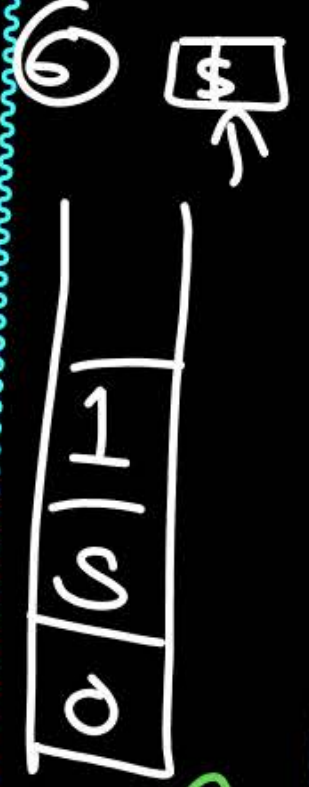
①   $M[0, a]: S_3$

②  i) Pop 2\*|A| sym  
ii) Push A  
iii) Push  $M[0, A]$   
 $M[3, b] = A \rightarrow a$

③  i) Push b, Inc  
ii) Push 5  
 $M[2, b]: S_5$

④  i) Pop 2 sym  
ii) Push B  
iii)  $M[2, B]$  Push 4  
 $M[5, \$]: B \rightarrow b$

⑤  i) Pop 2\*|AB| symbols, 4 symbols  
ii) Push S  
iii) Push  $[0, S]$  1  
 $M[4, \$]: S \rightarrow AB$

⑥   $M[1, \$] = \text{Accept}$

Input: ab

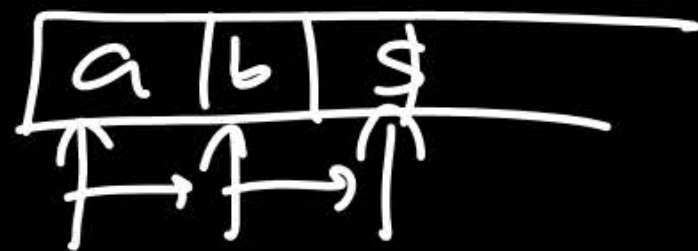
	a	b	\$	S	A	B
0	$S_3$			1	2	
1			Accept			
2		$S_5$				4
3		$A \rightarrow a$ $R_{ii}$				
4			$S \rightarrow AB$ $R_i$			
5			$B \rightarrow b$ $R_{iii}$			



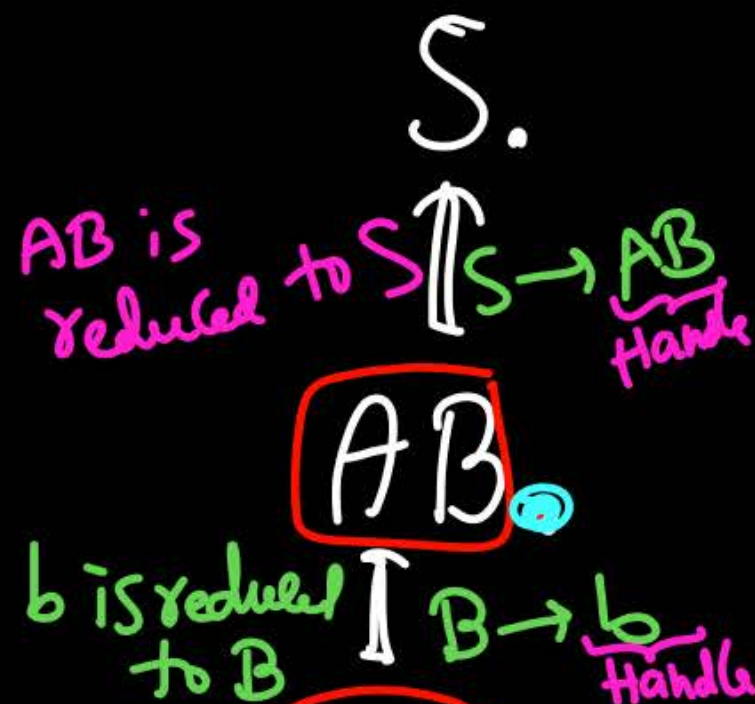
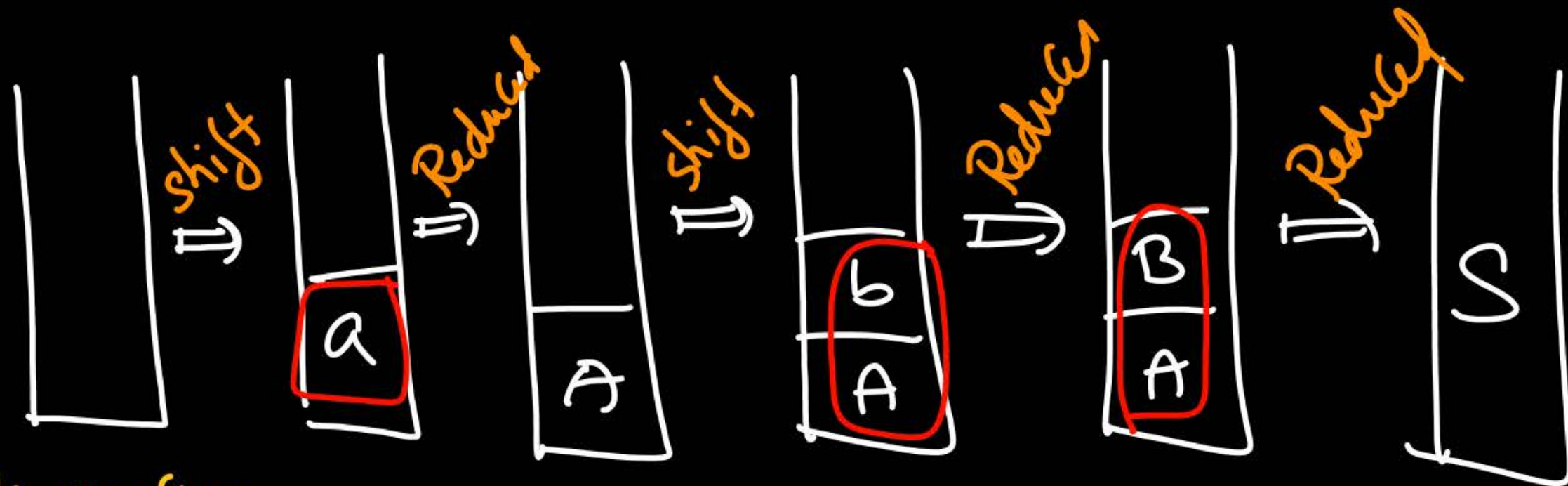
$S \rightarrow AB$

$A \rightarrow a$

$B \rightarrow b$



$w = ab$



viable prefix:

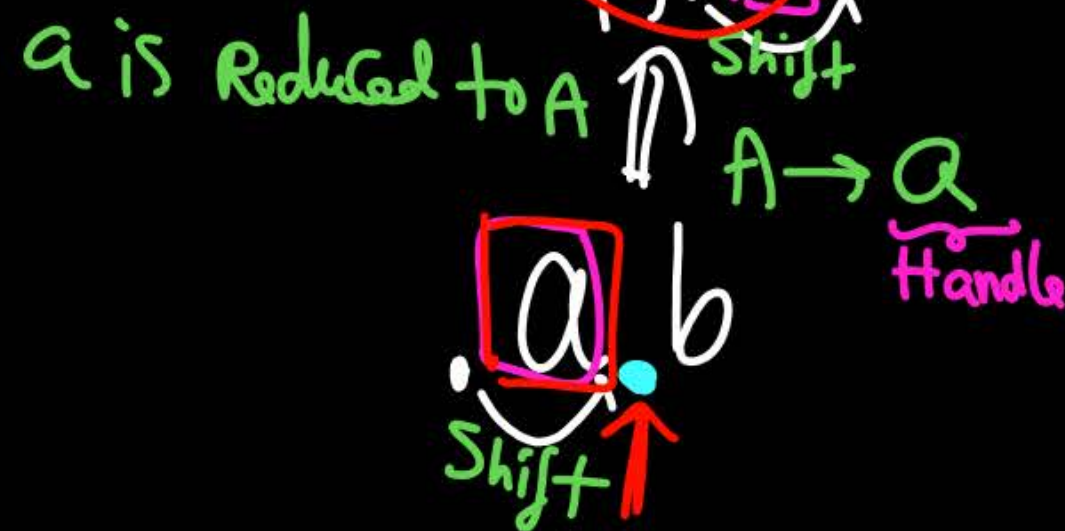
→ prefix of Right Sentential form and top of stack sequence

→ Dot is not allowing to move further

→ Indication to perform Reduced Action

$a$ ,  $Ab$ ,  $AB$

$bX$   
 $AX$   
 $BX$



→ Next: Operator precedence  
practice GATE PYQ



