

CS & IT ENGINEERING

Compiler Design

Lexical Analysis & Syntax Analysis

Lecture No. 11



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- LR(0) Table
- SLR(1) "
- LALR "
- CLR "
- LR Algorithms
- Operator precedence

operator precedence :

→ order of operators to evaluate

→ In C: unary,
Binary,
Ternary

→ Single character,
double character,

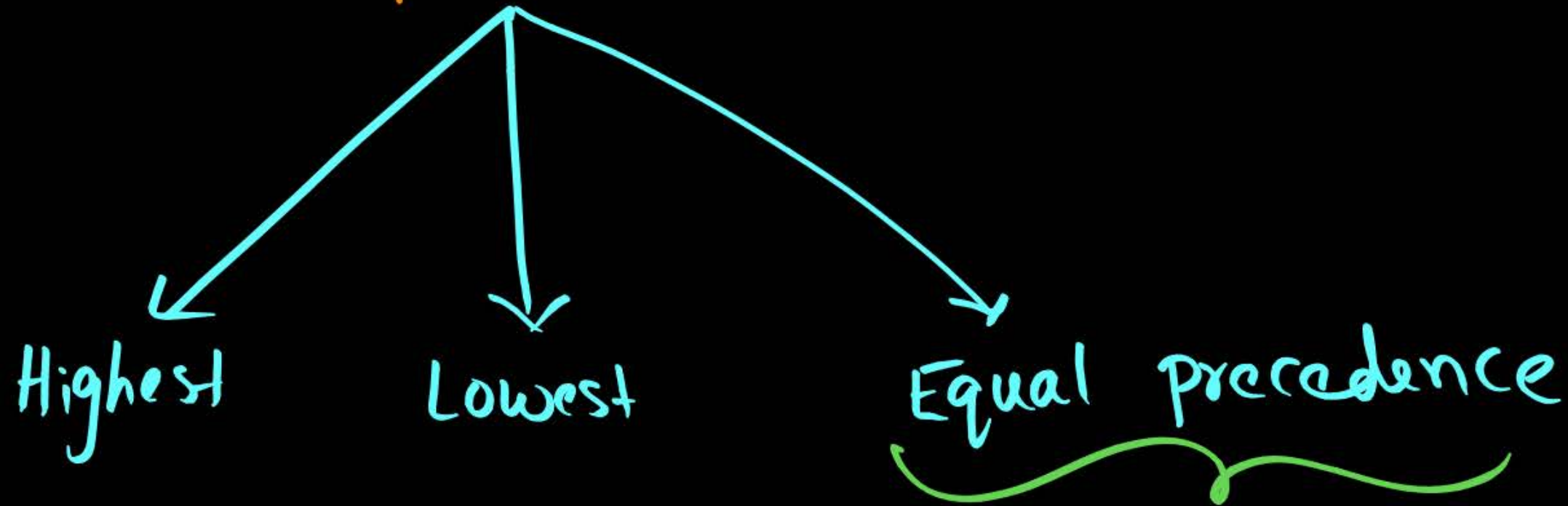
Based on no. of operands
Based on length of operator

/, *
+

$$2 + 3 * 5 / 6$$

$$2 + 3 / 5 * 6$$

Precedence Rules



Associativity Rules



* Highest

+ Lowest

$$a + \boxed{b * c}$$

$$\boxed{a * b} + c$$

$\frac{*}{/}$ } Equal \Rightarrow Associativity?
 Left to Right

$$\boxed{a/b} * c$$

$$\boxed{a * b} / c$$

***P



$*((*P))$

* } equal
*



Operator Grammar

↳ It is CFG in which "no rule contains 2 consecutive non-terminals" and also "no null productions present".

① $E \rightarrow E + E \mid E * E \mid a$ ✓ operator Grammar

② $E \rightarrow \boxed{EE} \mid E + E \mid a$
 2 consecutive non-terminals

③ $E \rightarrow E + E \mid \epsilon$
 null rule

④ $E \rightarrow \boxed{EE} \mid E + E \mid \epsilon$

not operator grammar

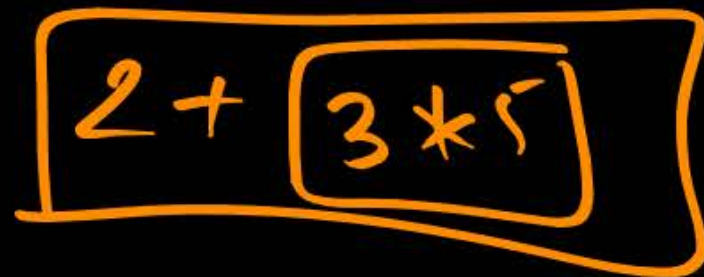
Operator Grammars

Vs

LR Grammars



$2 + 3 * 5$

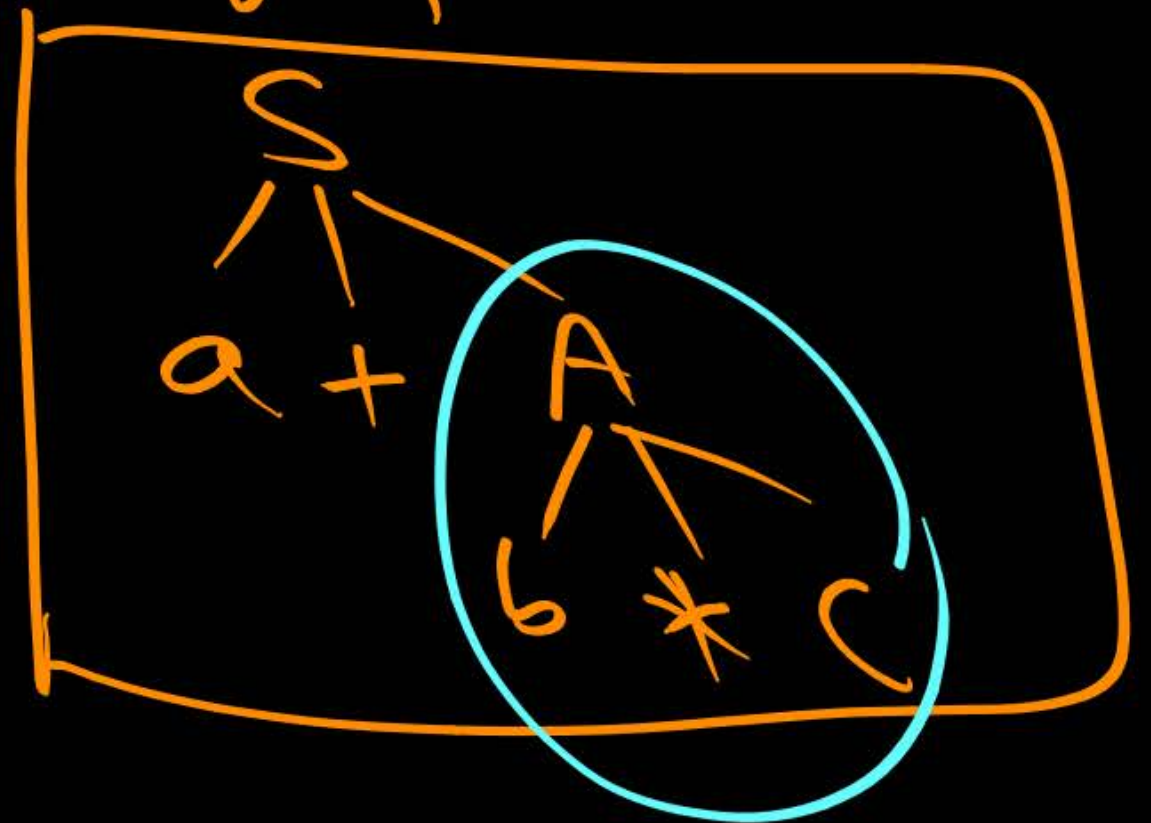


$S \rightarrow a + A$

$A \rightarrow b * c$

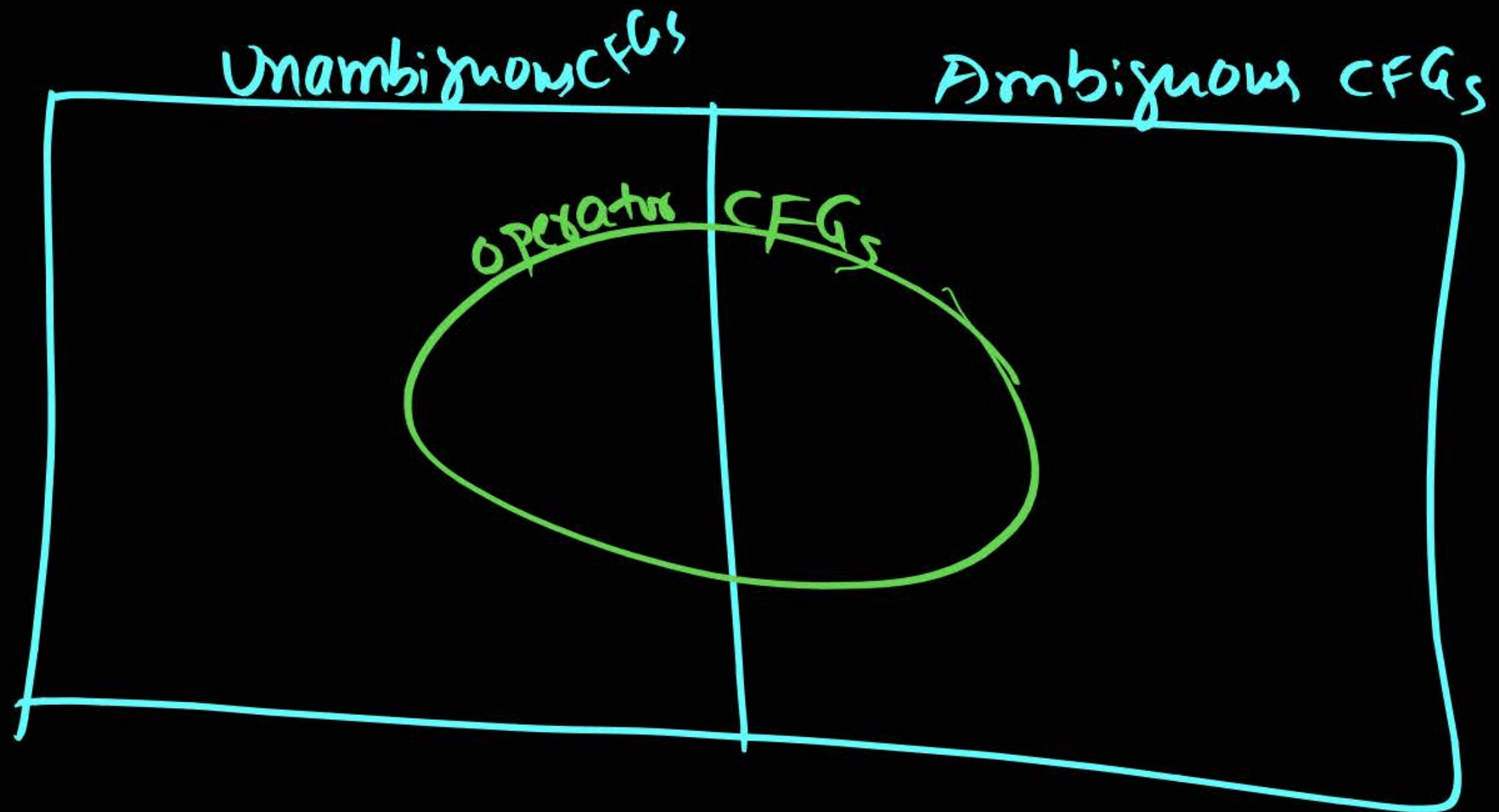
$2 + 3 * 5$

possible to generate
or parse tree or not?



Unambiguous CFGs

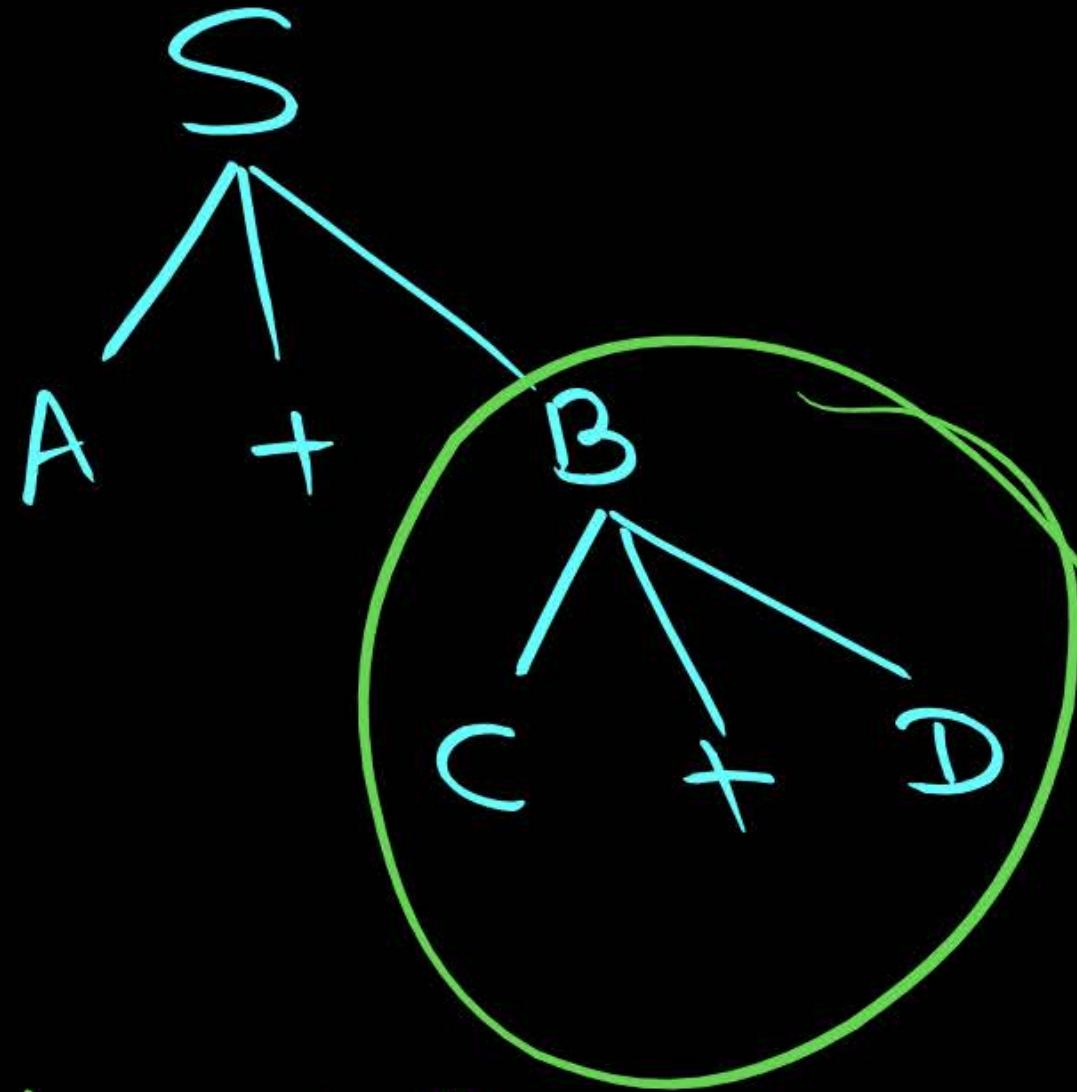
LR(1) CFGs



Find precedence rules using parse tree



①

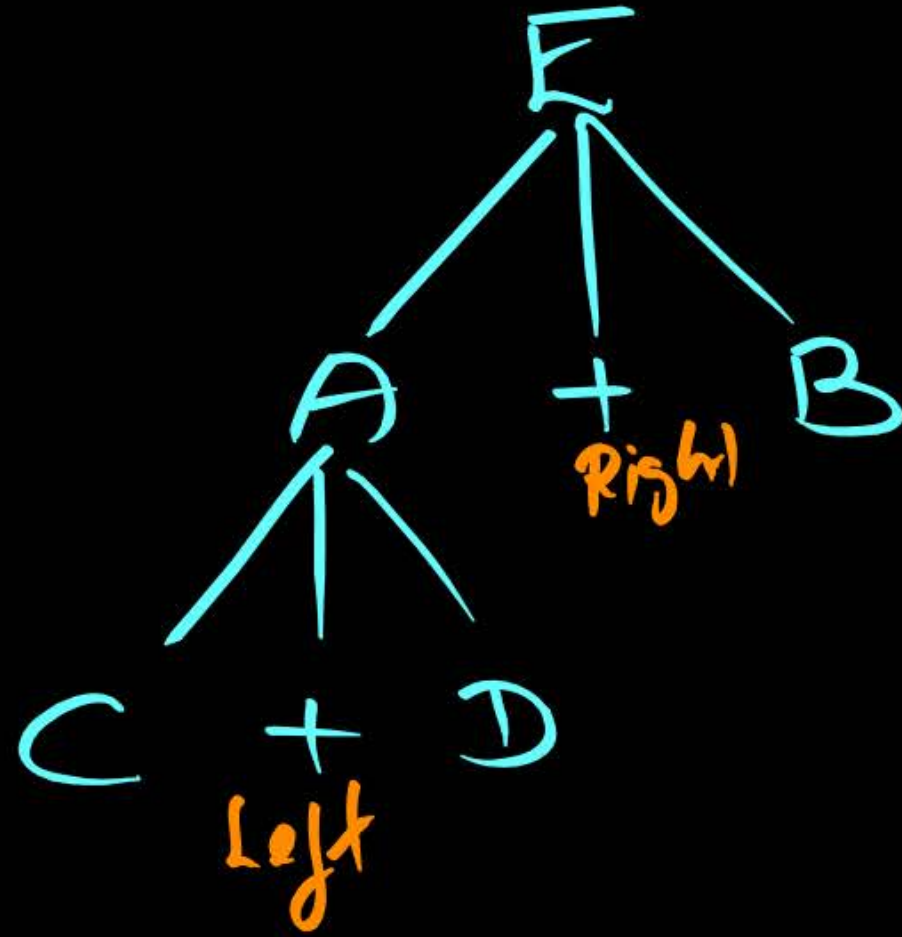


$2+3+S$
Left Right

$+$ is Right to Left Associative.

Left $+$ is lowest than Right $+$
Right $+$ is highest than left $+$

②

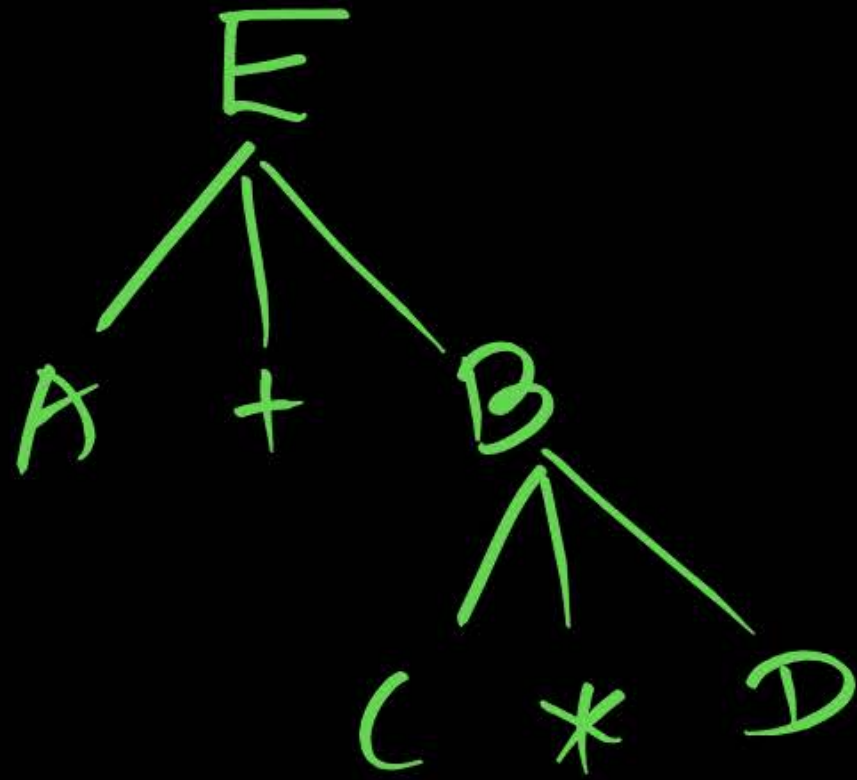


$$a + b + c$$

+ is Left to Right Associative
(Left Associative)

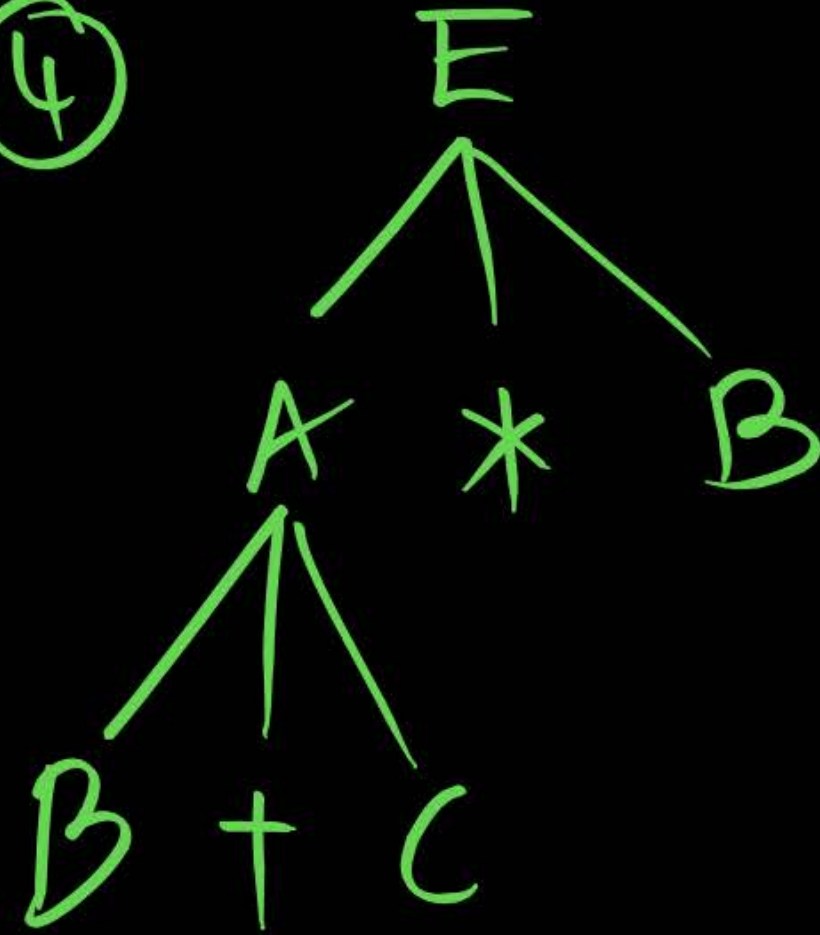
Left + is highest than Right +

③



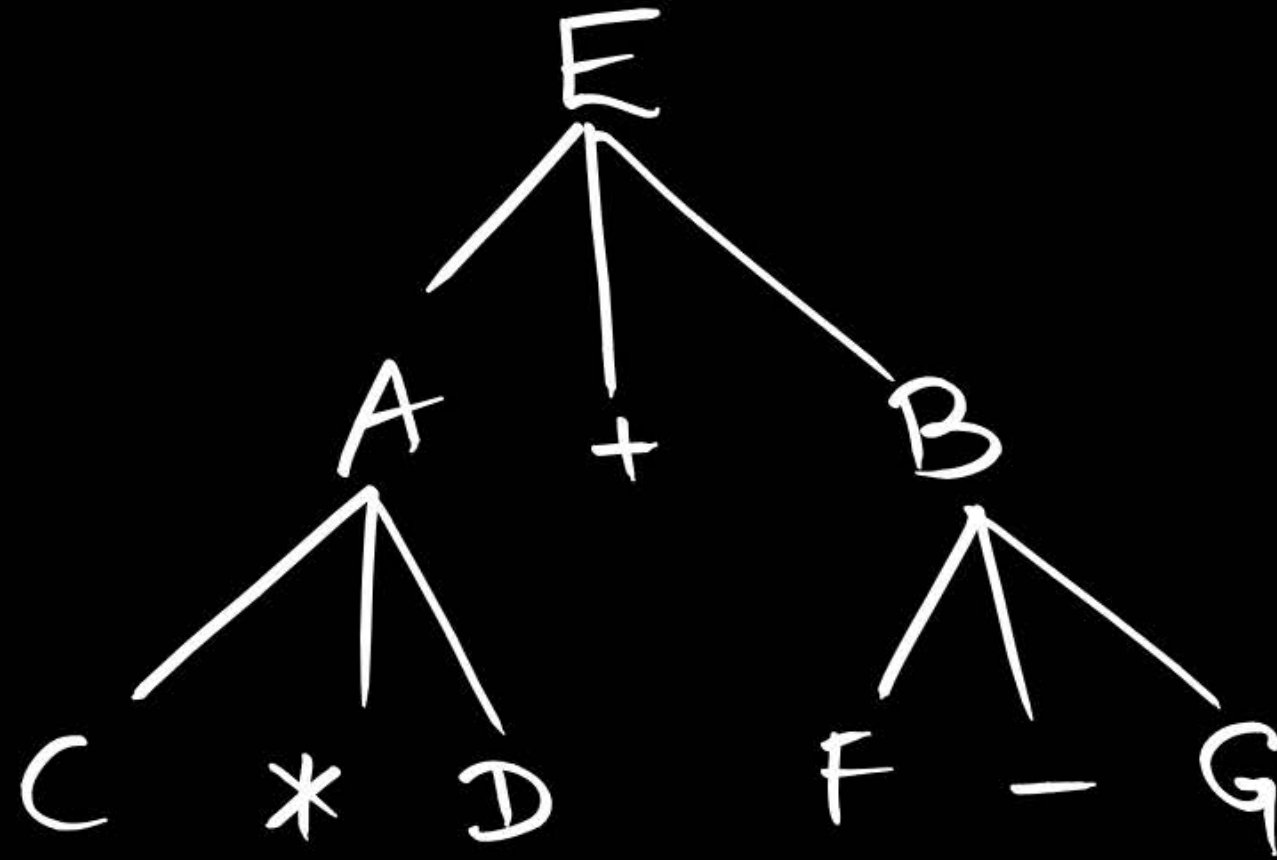
$*$ is highest
 $+$ is lowest

④



$+$ is highest
 $*$ is lowest

5



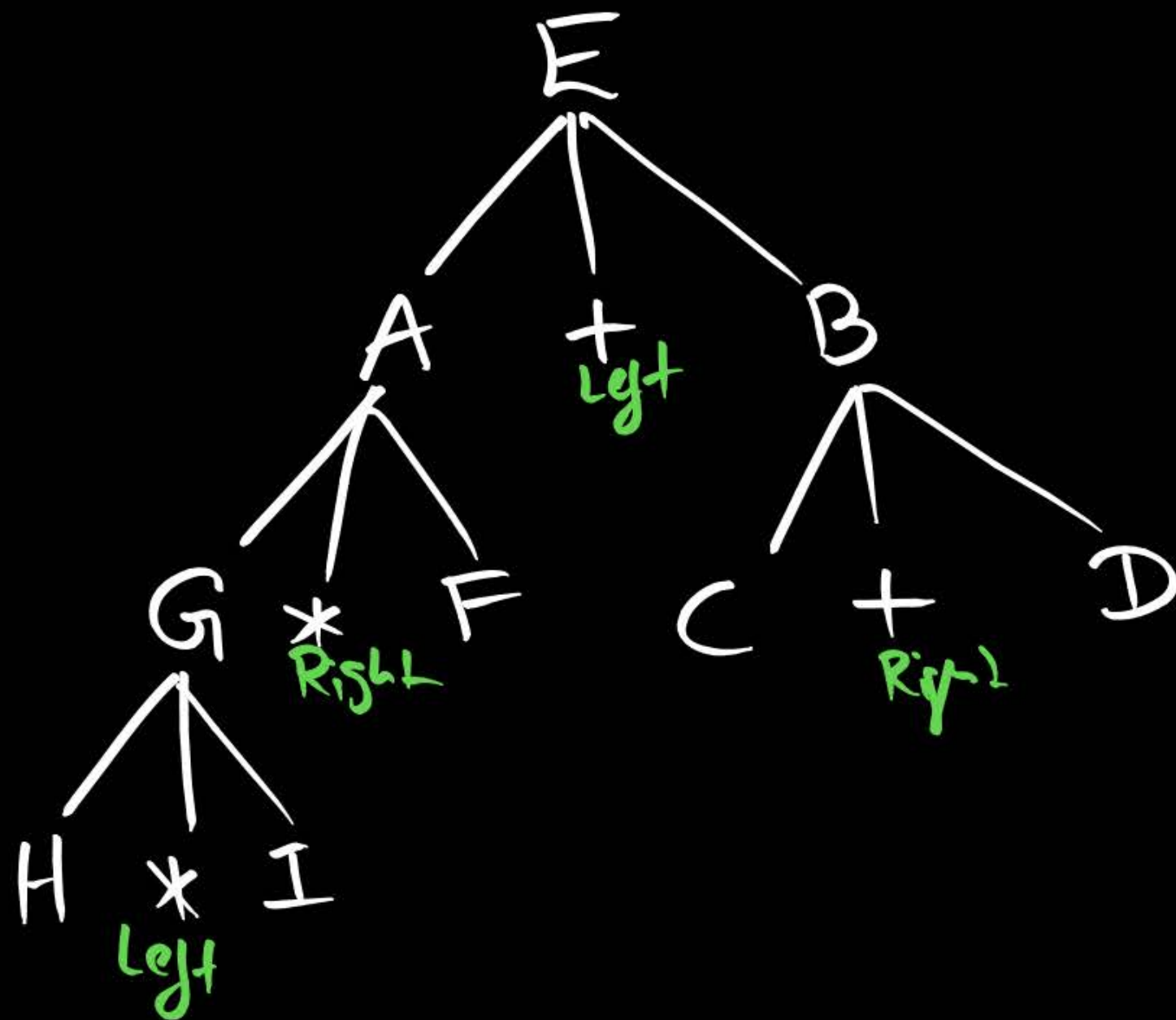
$*$, $+$, $-$
3 operators

$*$ is highest than $+$

$-$ is highest than $+$

$*$ and $-$ are not having any relation

⑥



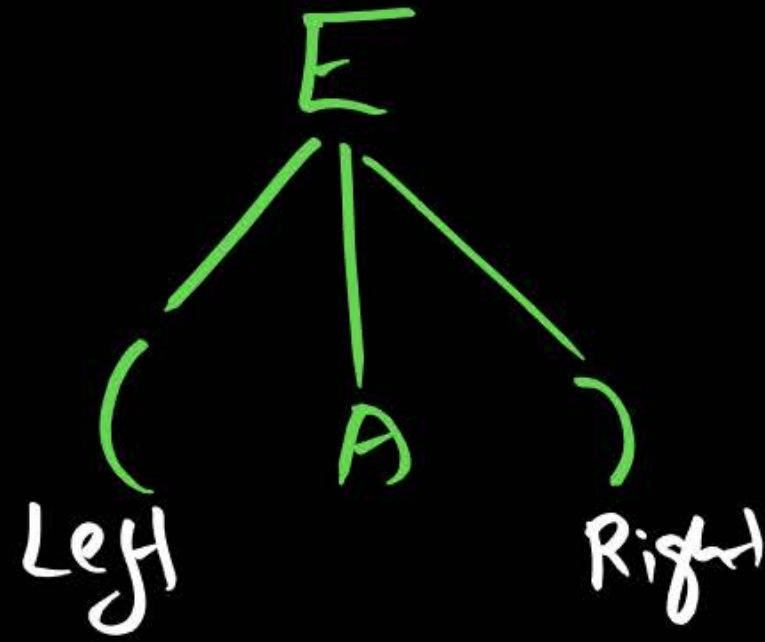
$+$, $*$
2 operators

✓ $*$ is highest than $+$

$+$ is Right Associative

$*$ is Left Associative

⑦



(is equal to)



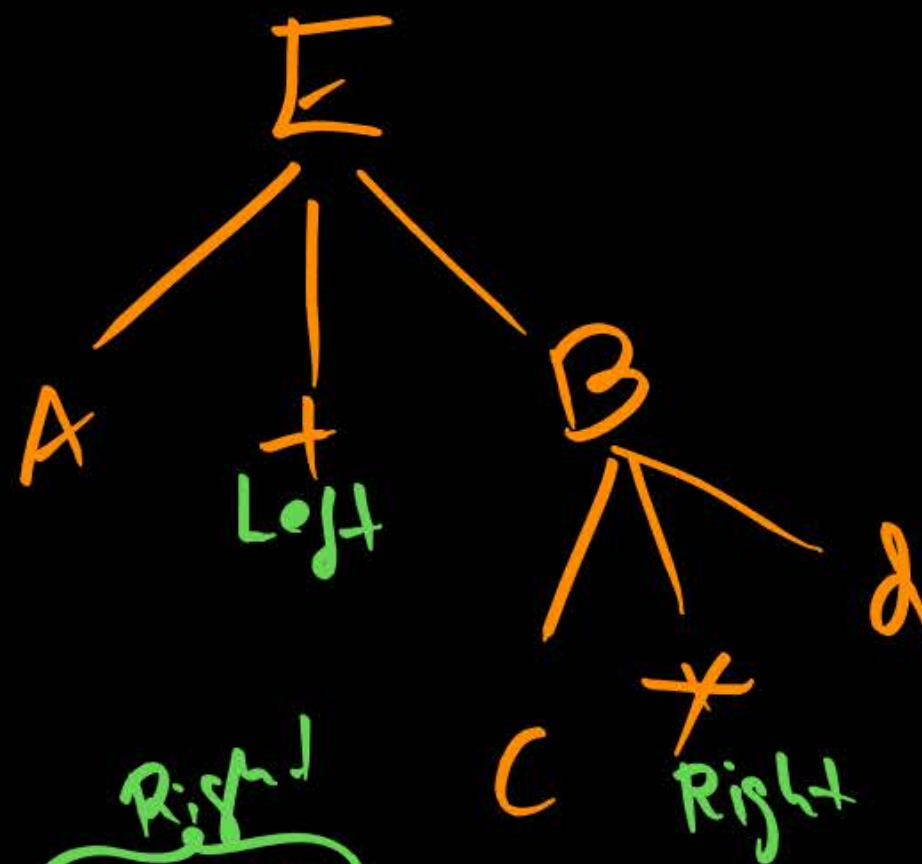
Find operator precedence using Operator Grammar



① $E \rightarrow A + B \mid a$

$A \rightarrow b$

$B \rightarrow c * d$



$*$ is highest than $+$

$+ < *$

Left {

	$+$	$*$
$+$		$<$
$*$		

Right

I) $\overset{\text{Left}}{+} < \overset{\text{Right}}{*}$

II) $* > +$

$+ < *$

$\left. \begin{array}{c} + \\ * \end{array} \right\} \text{Left (Stack)}$

$\left. \begin{array}{c} + \\ * \end{array} \right\} \text{Right (Input)}$

$a + b * c$
 $a * b + c$

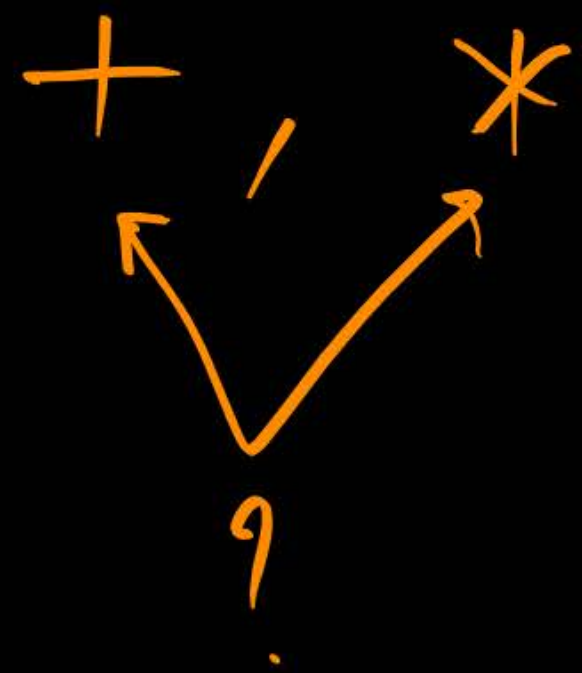
$* > +$



$$\begin{array}{ccc} \text{Left} & & \text{Right} \\ O_1 & < & O_2 \end{array}$$

$$O_1 > O_2$$

$$O_1 = O_2$$



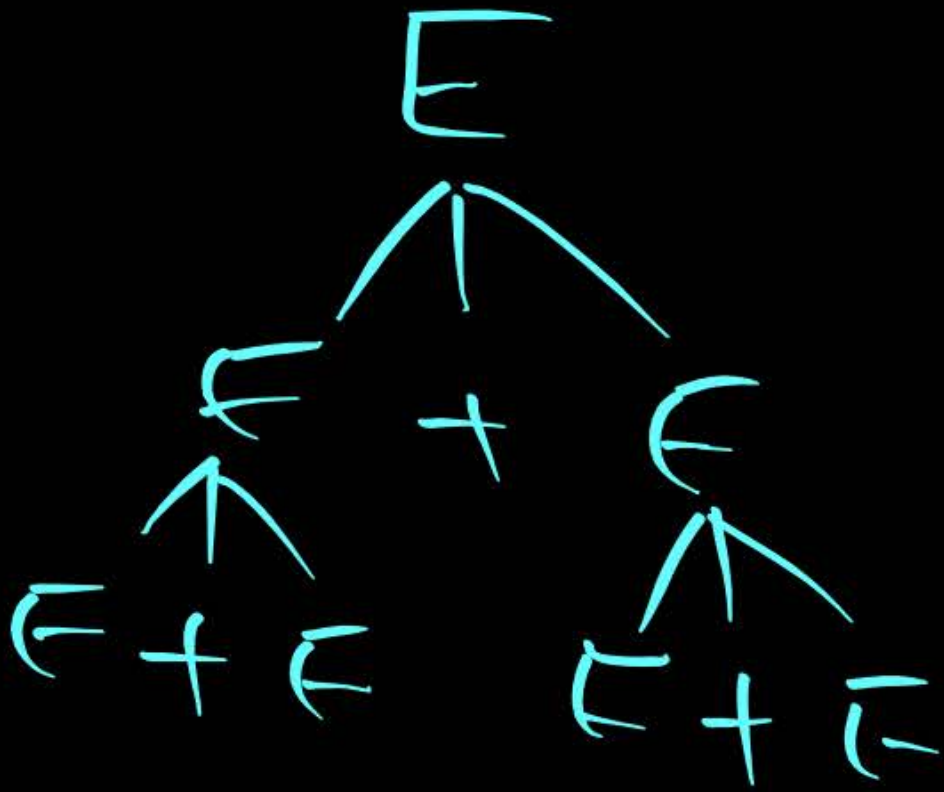
②

$$E \rightarrow E + E \mid a$$

Ambiguous CFG

multiple precedence rules

Left + Right +
< / >



③

$$E \rightarrow E + E \mid E - E \mid id$$



+ is highest

- is lowest

+ and - are Right Associative

	+	-
+	<	>
-	<	<

+ < +

+ is R to L Assoc.

+	R to L
-	R to L

Find o/p for

$$= -7$$

$$2 + 3 - 5 + 6 - 1 - 2$$

$$5 - 11 - 1 - 2$$

$$5 - 11 - (-1)$$

$$5 - 12$$

④

$$10 - 2 + 3 + 5 * 3 * 2 - 1 - 6 + 5$$

$$8 + 3 + 5 * 3 * 2 - (-5) + 5$$

$$8 + 3 + 5 * 3 * 7 + 5$$

$$8 + 3 + 105 + 5$$

$$= 121$$

==



	+	*	-
+	<	<	<
*	>	>	<
-	>	>	<

+ is Right Associative

* is Left "

- is Right "

- is Highest precedence

+ is lowest "

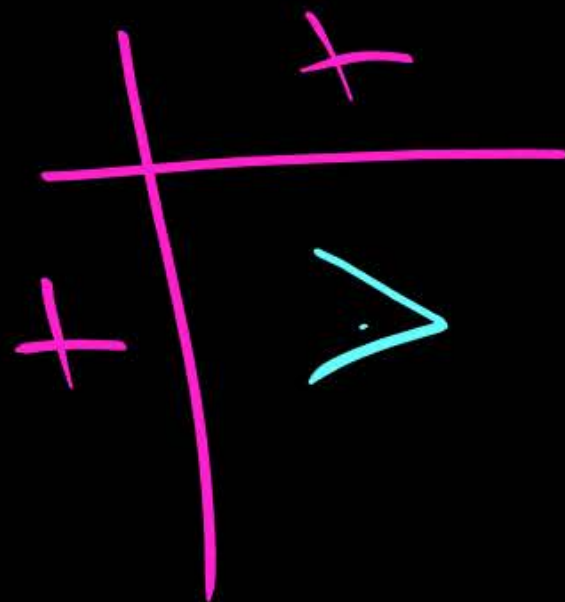
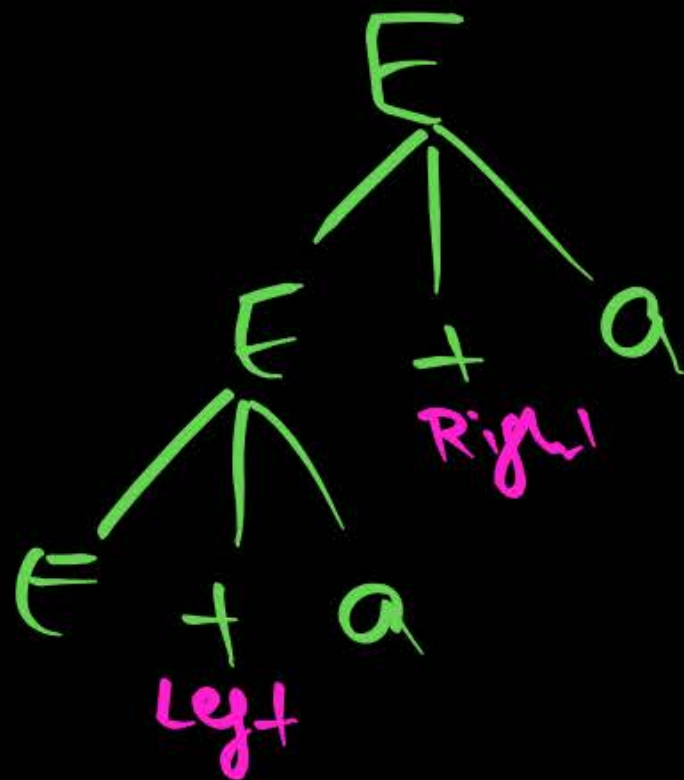
5



$$E \rightarrow E + a \mid b$$

Left Recursion
+ is left Associative

+ is Left Associative



$$(6) \quad E \rightarrow \underbrace{a + E}_{\text{Right Rec}} \mid a$$

Right Rec

\Downarrow
 $+$ is Right associative

7.10
9-2014

⑦

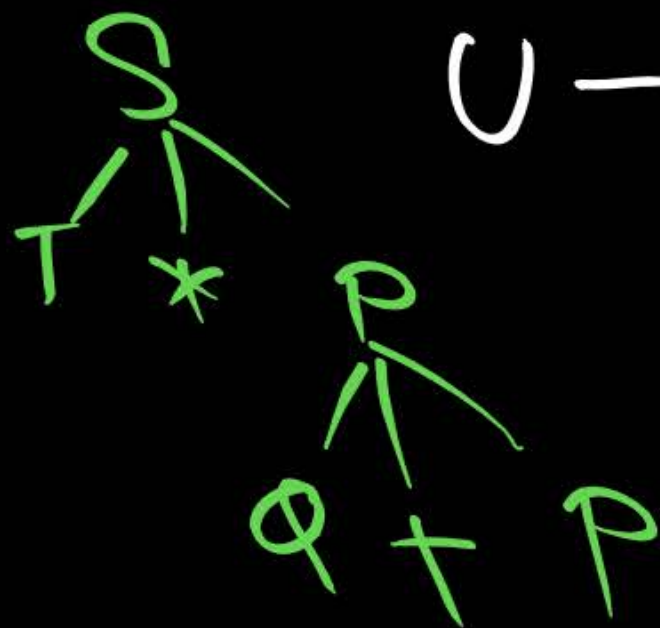
$$S \rightarrow T * P$$

$$T \rightarrow U \mid T * U$$

$$P \rightarrow Q + P \mid Q$$

$$Q \rightarrow \text{id}$$

$$U \rightarrow \text{id}$$



(Stack)
Left

Right (Input)	
+	*
+	<
*	<
	>

No entry
+ before *
never happens
in CFG

* is Left Associative
+ is Right "
+ is highest than *

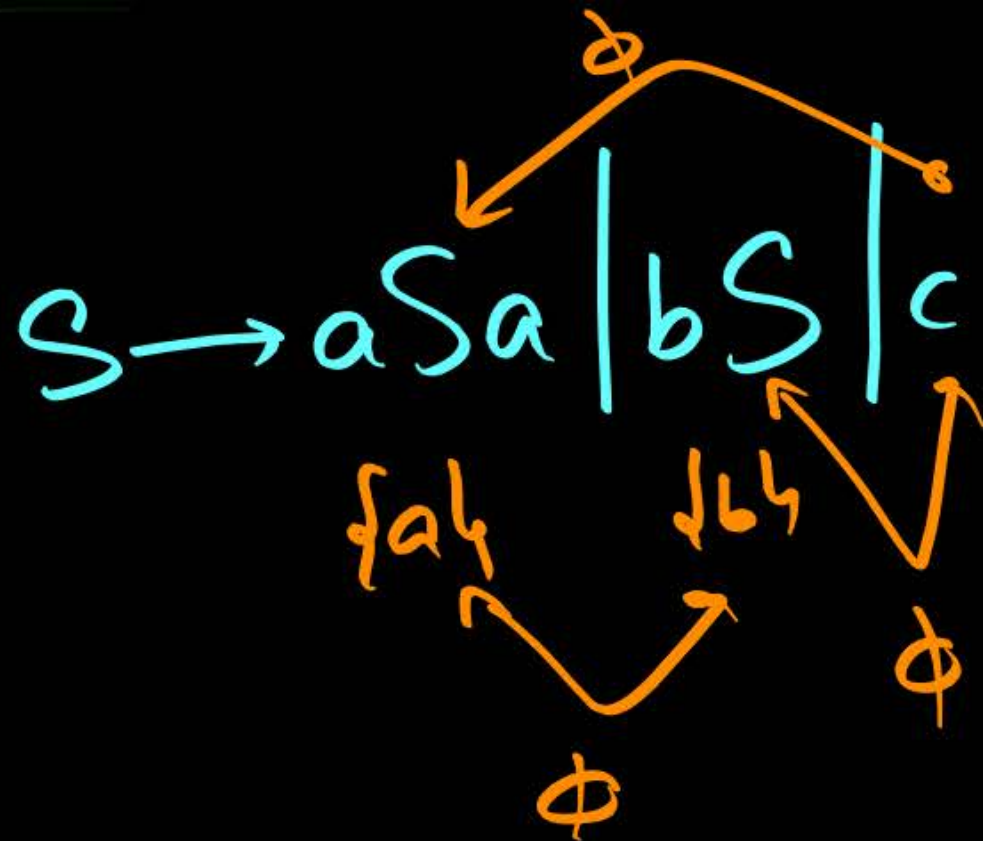


Note : precedence rules can be computed

- I) USING Parse Tree
- II) USING precedence Table
- III) USING Operator Grammar
*
Unambiguous

GATE

7.9 ①



is ———

- A) LL(1) but not LR(1)
- B) LR(1) but not LL(1)
- ~~C) Both LL(1) & LR(1)~~
- D) Neither LL(1) nor LR(1)



Note: Every LL(1) is LR(1)
CLR

7.8

②

G

$S \rightarrow F | H$
 $F \rightarrow p | c$
 $H \rightarrow d | c$

\Rightarrow

String = c

2 parse trees

Ambiguous CFG

S
 $|$
 F
 $|$
 c

S
 $|$
 H
 $|$
 c

FALSE

S_1 :

LL(1) can parse all strings that are generated using G

FALSE

S_2 :

LR(1)

" " " " " " " "

LL(1) parser not possible

LR(1)

" " " "

→ Syntax Analysis ✓
→ Next: SDTs

