Branch : CSE & IT **Batch : Hinglish**

Data Structure

Tree

DPP 03

[NAT]

1. The number of unlabelled binary trees possible with four nodes is _____.

[NAT]

2. The number of labelled binary trees possible with the nodes-10, 30, 25, 40 is _____.

[NAT]

3. The number of binary search trees possible with the nodes-10, 30, 25, 40 is _____.

[MCQ]

4. The pre-order traversal of a binary search tree is given as-
7, 3, 2, 1, 5, 4, 6, 8, 10, 9, 11
The post-order traversal of the above binary tree is-
(a) 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11
(b) 1, 2, 4, 6, 5, 3, 9, 11, 10, 8, 7
(c) 1, 2, 4, 5, 6, 3, 9, 10, 11, 8, 7
(d) 11, 9, 10, 8, 6, 4, 5, 1, 2, 3, 7

[MCQ]

5. Consider the following two statements:
Statement P: The last elements in the pre-order and in-order traversal of a binary search tree are always same.
Statement Q: The last elements in the pre-order and in-order traversal of a binary tree are always same.
Which of the following tree is/are CORRECT?
(a) Both P and Q only
(b) Neither P nor Q
(c) Q only
(d) P only

[MCQ]

6. Consider the following function:

```
struct treenode{
struct treenode *left;
int data;
struct treenode *right;
};
int func (struct treenode *t){
if(t==NULL) return 1;
else if(t->left==NULL && t->right==NULL)
return 1;
else if
((t → left → data < t->data) && (t → right → data > t->data))
return func(t->left) && func(t->right);
else
return 0;
}
```

Assume t contains the address of the root node of a tree. The function-
(a) Returns 1 if the given tree is a Binary Search Tree.
(b) Returns 0 if the given tree is a complete binary tree.
(c) Returns 0 if the given tree is a Binary Search Tree.
(d) Returns 1 if the given tree is a complete binary tree.

[MCQ]

7. Consider the following function:

```
struct treenode{
struct treenode *left;
int data;
struct treenode *right;
};
struct treenode * f(struct treenode *t, int x){
if(t==NULL) return NULL;
elseif(x==t->data) return ______a______;
else if (x<t->data) return ______b______;
else return ______c______;
}
```

Assume t contains the address of the root node of a binary search tree. The function finds an element x in the BST and returns the address of the node if found.
Which of the following statement(s) is/are CORRECT?
(a) a: NULL ; b: f(t->left, x) ; c: f(t->right, x)
(b) a: t ; b: f(t->right, x) ; c: f(t->left, x)
(c) a: NULL ; b: f(t->right, x) ; c: f(t->left, x)
(d) a: t ; b: f(t->left, x) ; c: f(t->right, x)

Answer Key

1. **(14)**
2. **(336)**
3. **(14)**
4. **(b)**
5. **(b)**
6. **(a)**
7. **(d)**

Hint & Solutions

1. (14)

Number of unlabelled binary trees possible with 4 nodes

$$= \frac{1}{4+1} \times \frac{(2\times 4)!}{4!\ 4!}$$

$$= \frac{1}{5} \times \frac{8!}{4!\ 4!}$$

$$= \frac{1}{\cancel{5}} \times \frac{\overset{2}{\cancel{8}} \times 7 \times \cancel{6} \times \cancel{5}}{\cancel{4} \times \cancel{3} \times \cancel{2} \times 1}$$

= 14

2. (336)

Number of labelled binary trees possible with 4 nodes-

= 4! × Number of unlabelled binary trees with 4 nodes

= 4! × 14

= 336

3. (14)

Number of BSTs with 4 = Number of unlabelled binary trees with nodes

4. (b)

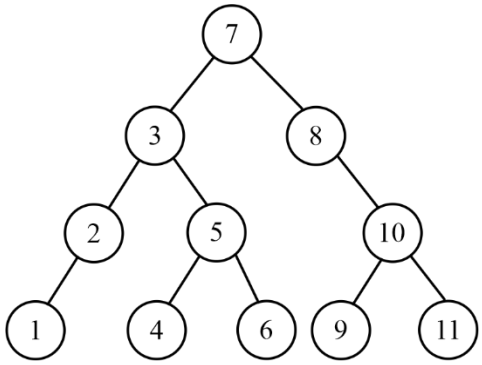
Pre-order traversal of BST:

7 3 2 1 5 4 6 8 10 9 11

In-order traversal of BST:

1 2 3 4 5 6 7 8 9 10 11

Tree is constructed as-



Post-order traversal-

1 2 4 6 5 3 9 11 10 8 7

5. (b)

P: INCORRECT. The last elements in the pre-order and in-order traversal of a binary search tree are not always same.(It violates for skewed BSTs)

Q: INCORRECT. The last elements in the pre-order and in-order traversal of a binary tree are not always same.

6. (a)

The function- Returns 1 if the given tree is a Binary Search Tree.

7. (d)

```
struct treenode{
struct treenode *left;
int data;
struct treenode *right;
};
void f(struct treenode *t, int x){
if(t==NULL) return NULL;
elseif(x==t->data) return t;
else if (x<t->data) return f(t->left, x);
else return f(t->right, x);
}
```