

CS & IT ENGINEERING



Data Structure &
Programming
Tree

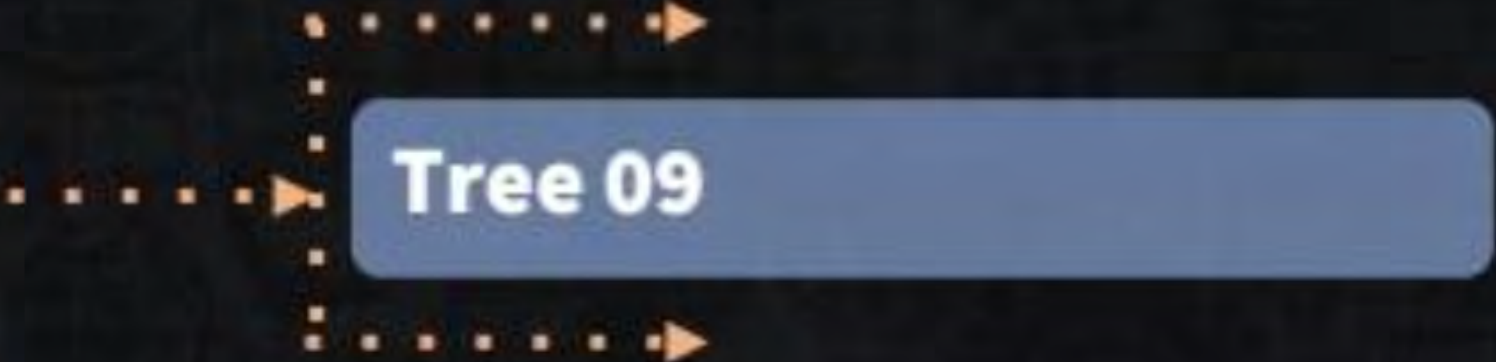
Lec- 09



By- Pankaj Sharma Sir



TOPICS TO
BE
COVERED



Tree 09

Expression tree

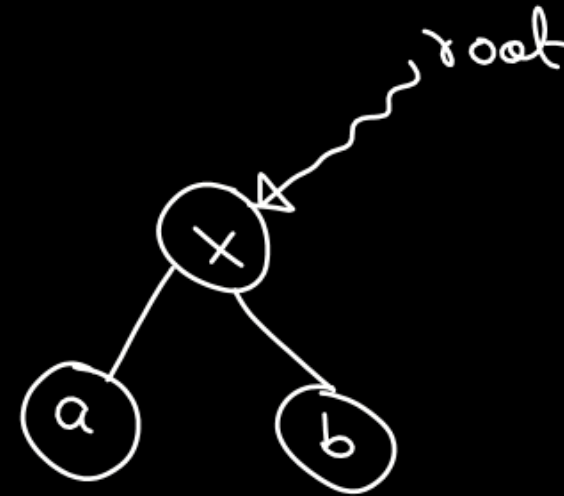
Infix : $a \times b + c/d - e$

high
↓
low

\times	$/$
$+$	$-$

{ operands : leaf
operators : Internal nodes

$a \times b$



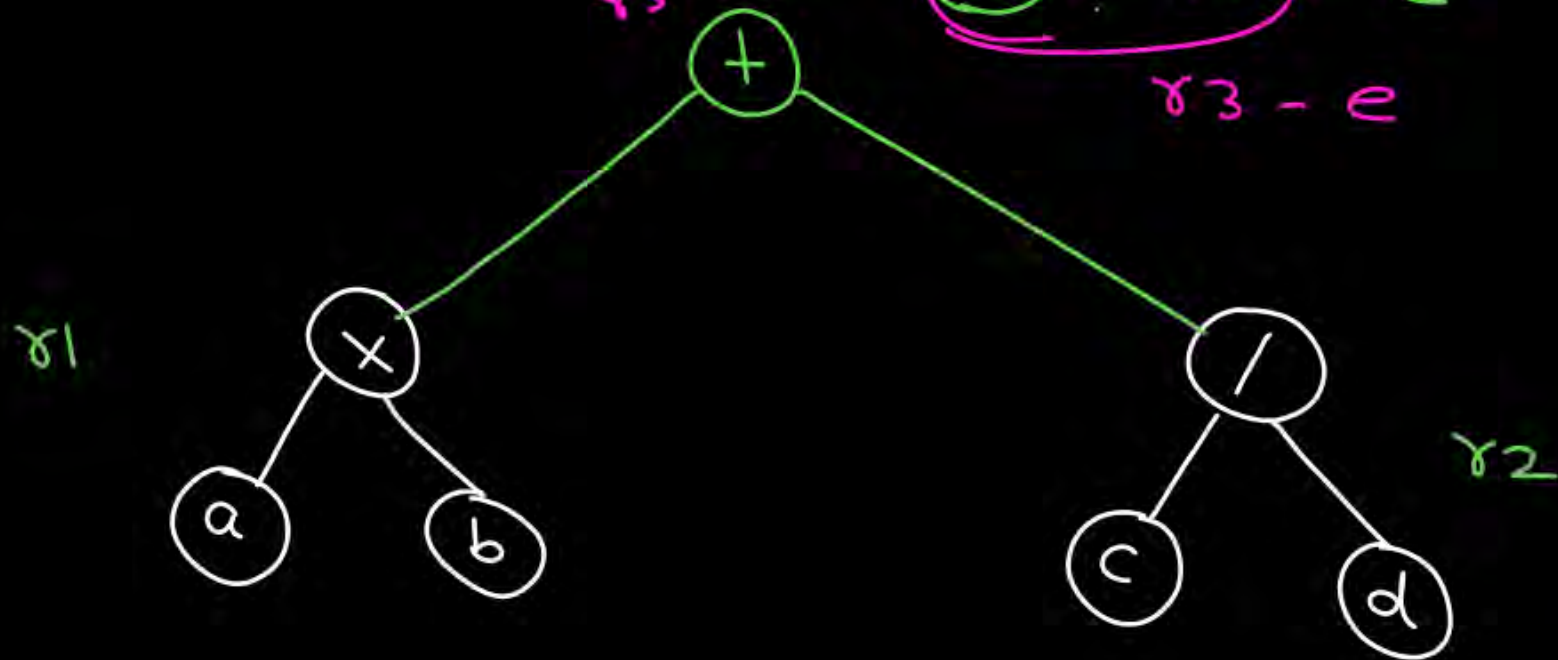
Expression tree

Infix : $a \times b + c/d - e$

γ_1 γ_2

$\gamma_1 + \gamma_2 - e$

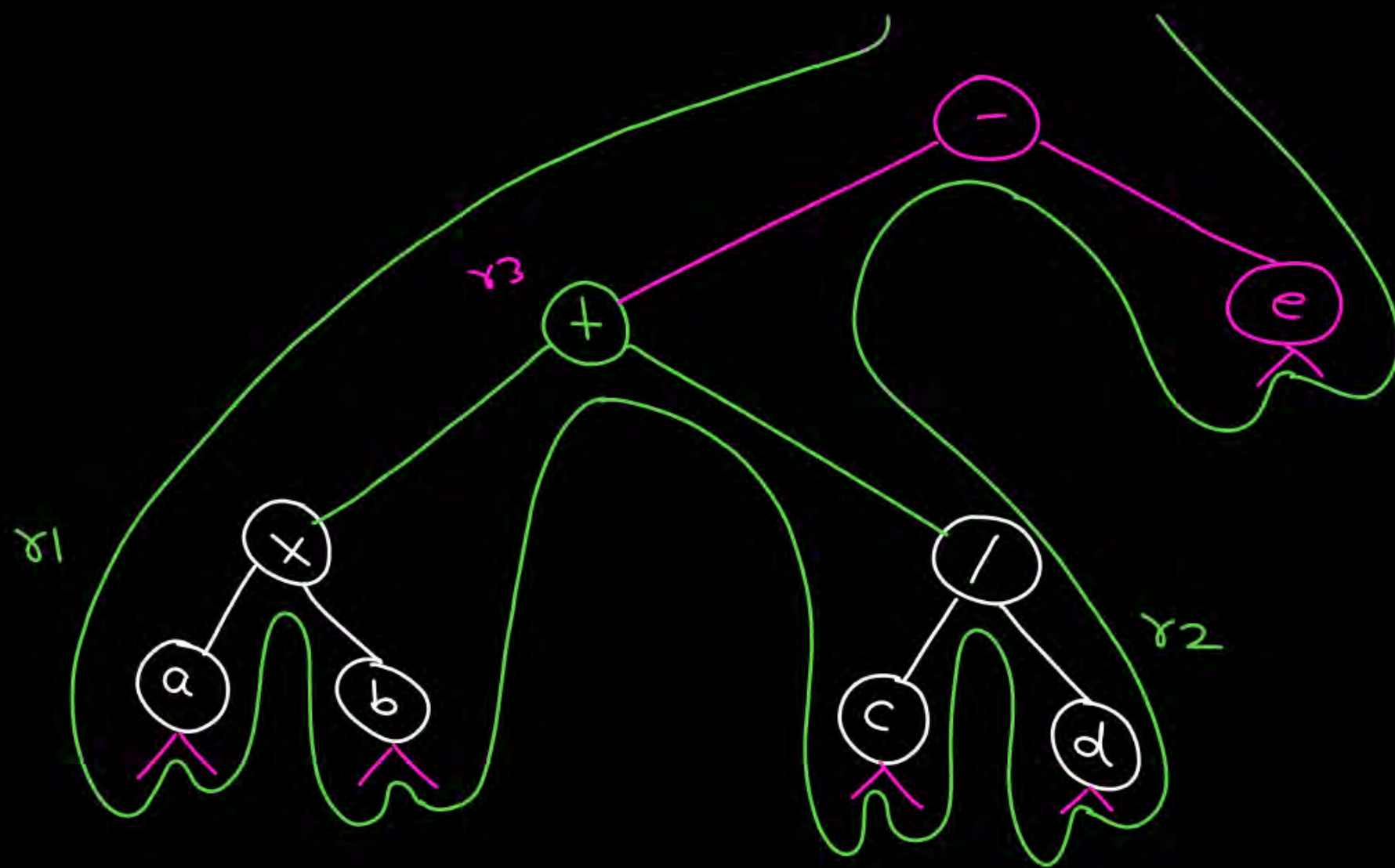
$\gamma_3 - e$



Expression tree

Infix : $\underbrace{a \times b}_{r1} + \underbrace{c/d}_{r2} - e$

$(r1) + r2 - e$
 $r3 - e$



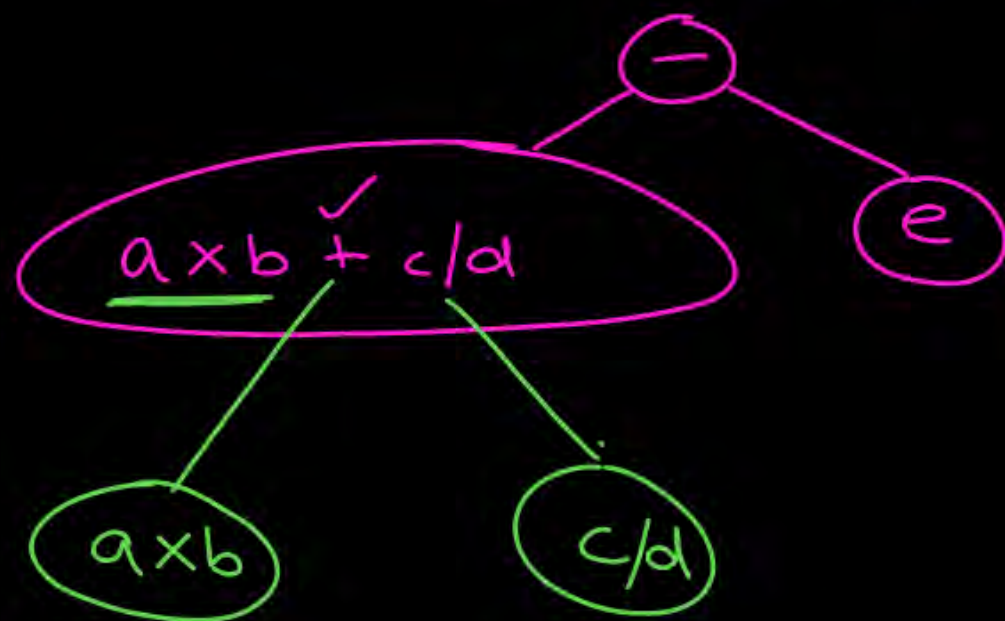
Root \Rightarrow least priority
last

Inorder : $a \times b + c/d - e$

Expression tree

Infix : $a \times b + c/d - e$

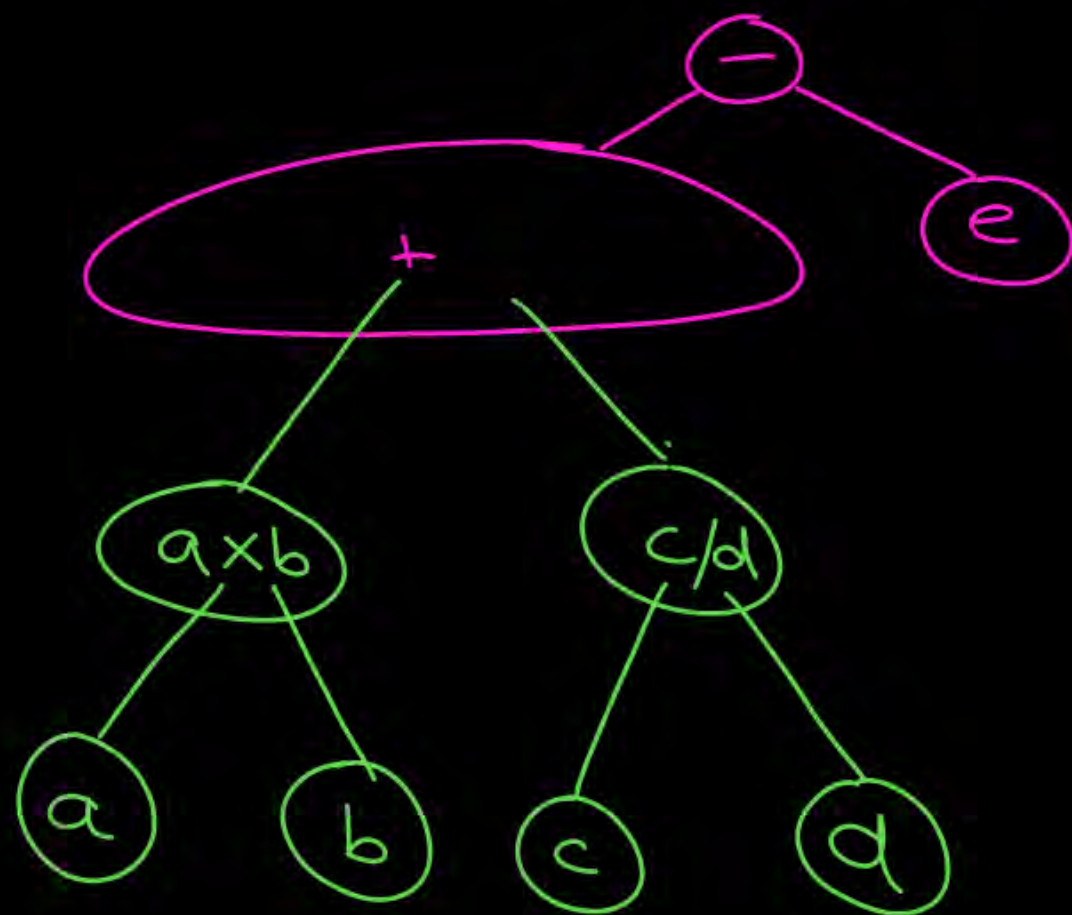
$a \times b + c/d - e$



Expression tree

Infix : $a \times b + c/d - e$

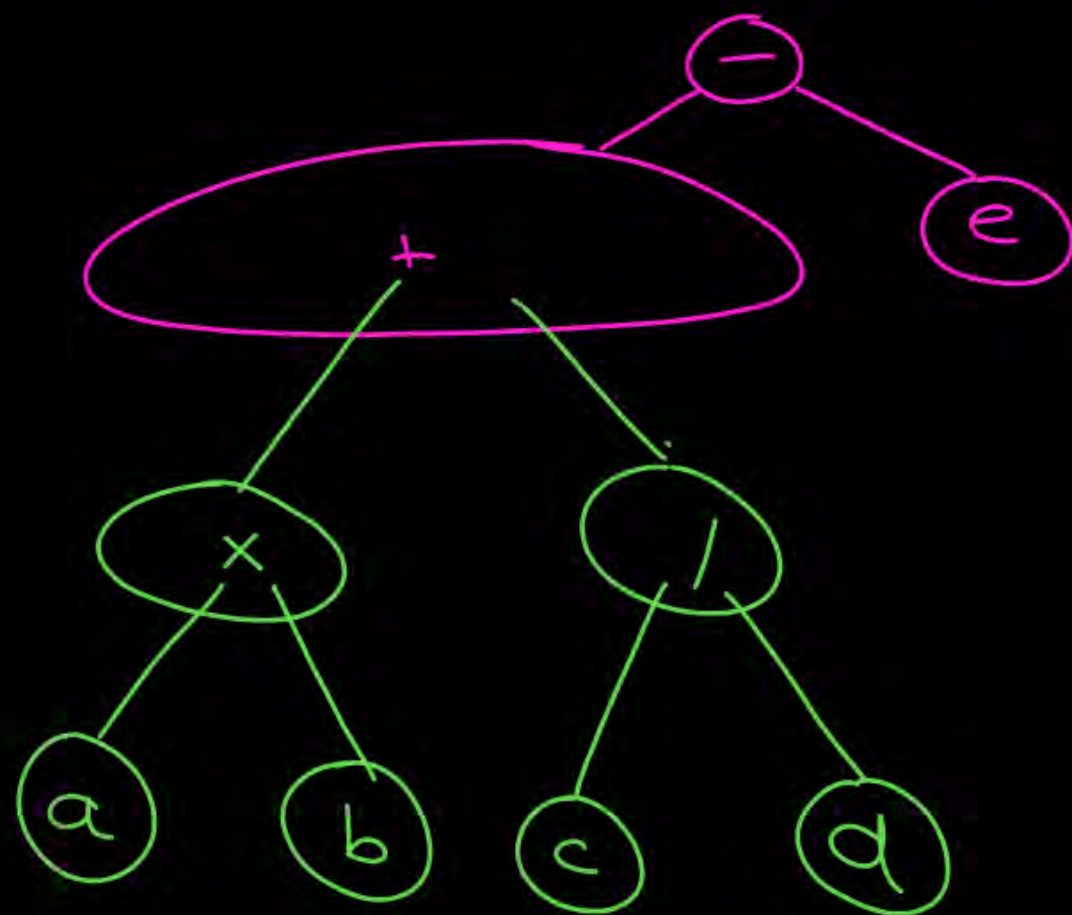
$a \times b + c/d - e$



Expression tree

Infix : $a \times b + c/d - e$

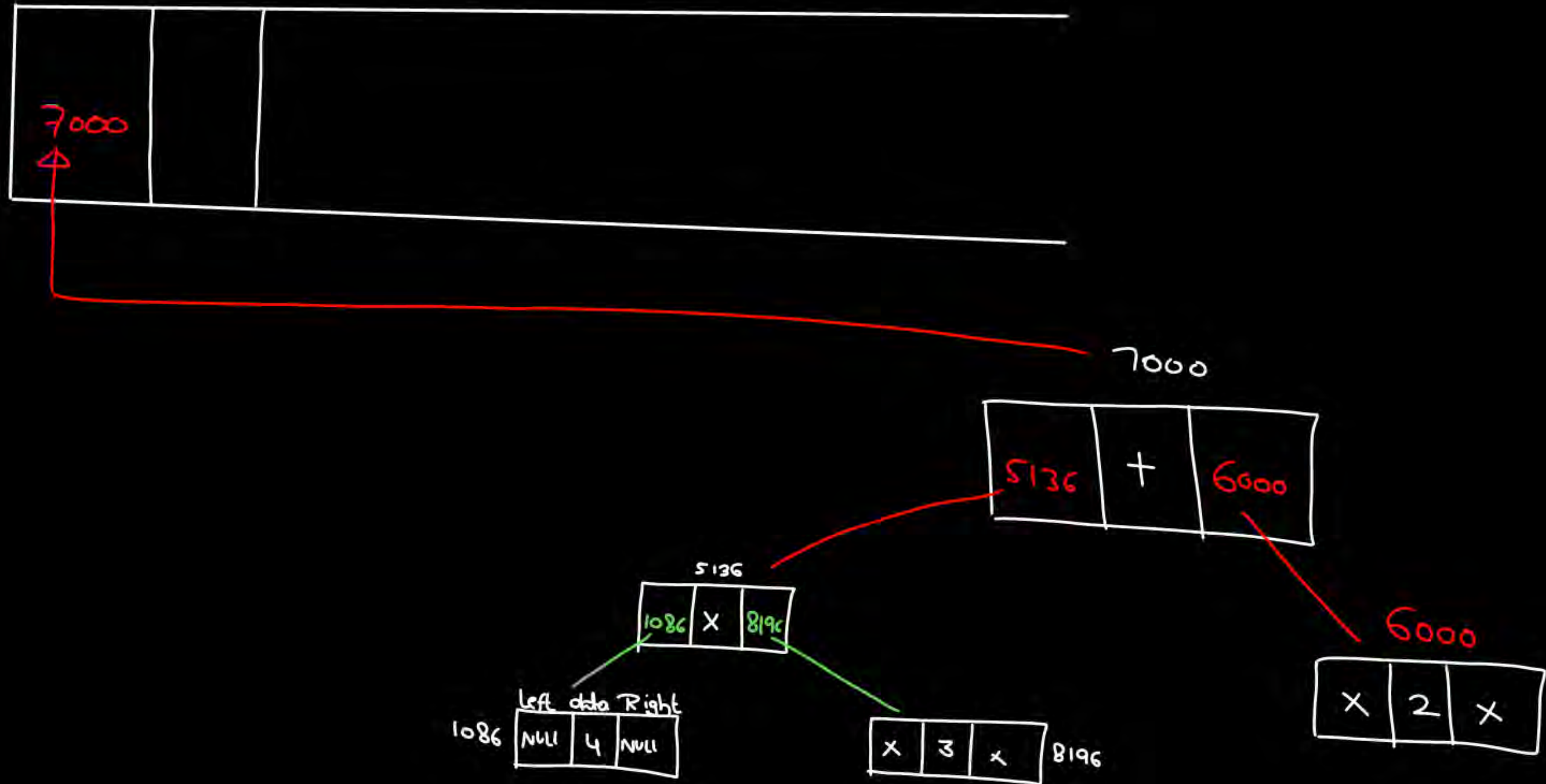
$a \times b + c/d - e$



Postfix to Expression tree

Infix : $4 \times 3 + 2$

Postfix : $4 \ 3 \times 2 \ + \text{End}$



Prefix to
Exp. tree

Infix: $2+3 \times 4$

Prefix: $+2 \times 34$

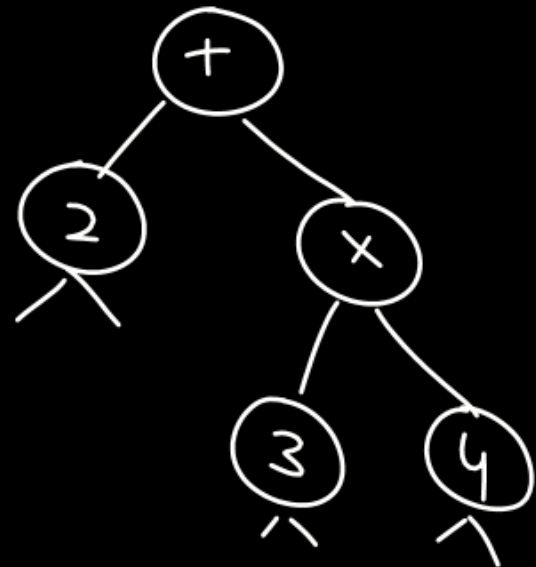
Reverse: $43 \times 2 + \text{End}$

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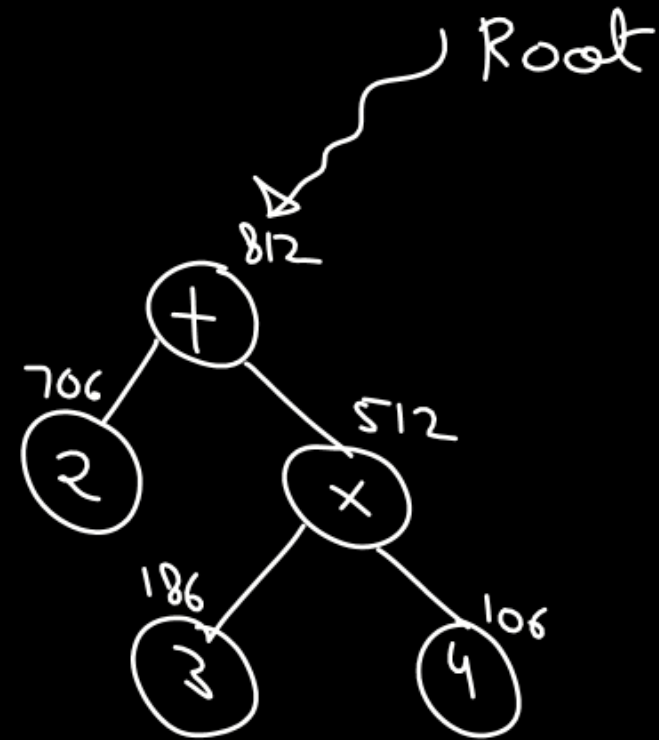
Inorder: Infix

Preorder: Prefix

Postorder: Postfix

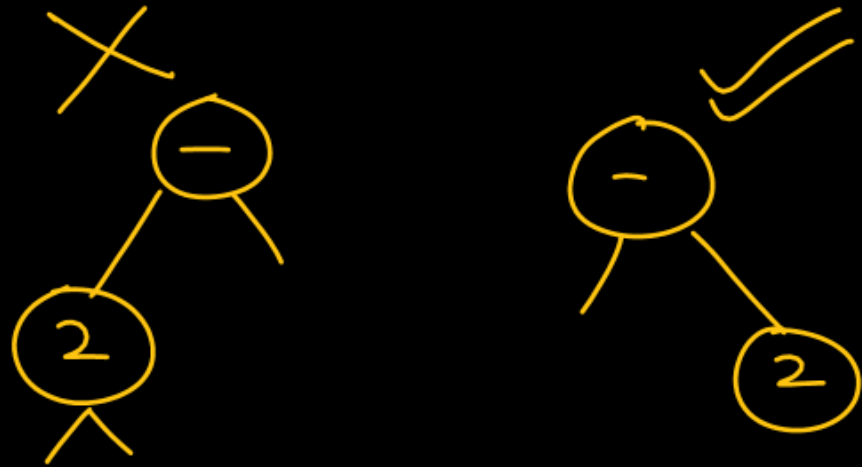


$2+3 \times 4$



Exp: Unary operator

-2



Inorder: 2-

-2

Unary operator > binary op.

$$3 \times \log(x+1)$$

$\log \rightarrow$ C operator \times

$\log \rightarrow$ 1 value
 $\log \rightarrow$ unary operator

$$3 \times \log(x+1)$$

Postfix

$$3 \times \log([x \ 1 \ +])$$

Operand

$$\begin{matrix} 3 & \times & [x \ 1 + \log] \\ \text{op1} & & \text{op2} \end{matrix}$$

$$3 \times 1 + \log X$$

1. Which one of the following seq. when stored in an array at loc. $A[1]$ to $A[10]$ result a max-heap.

Gate - 2023

A) 23, 14, 19, 1, 10, 13, 16, 12, 7, 5

B) 23, 17, 14, 7, 13, 10, 1, 5, 6, 12

C) 23, 17, 10, 6, 13, 14, 1, 5, 9, 12

D) 23, 17, 14, 6, 13, 10, 1, 5, 7, 15

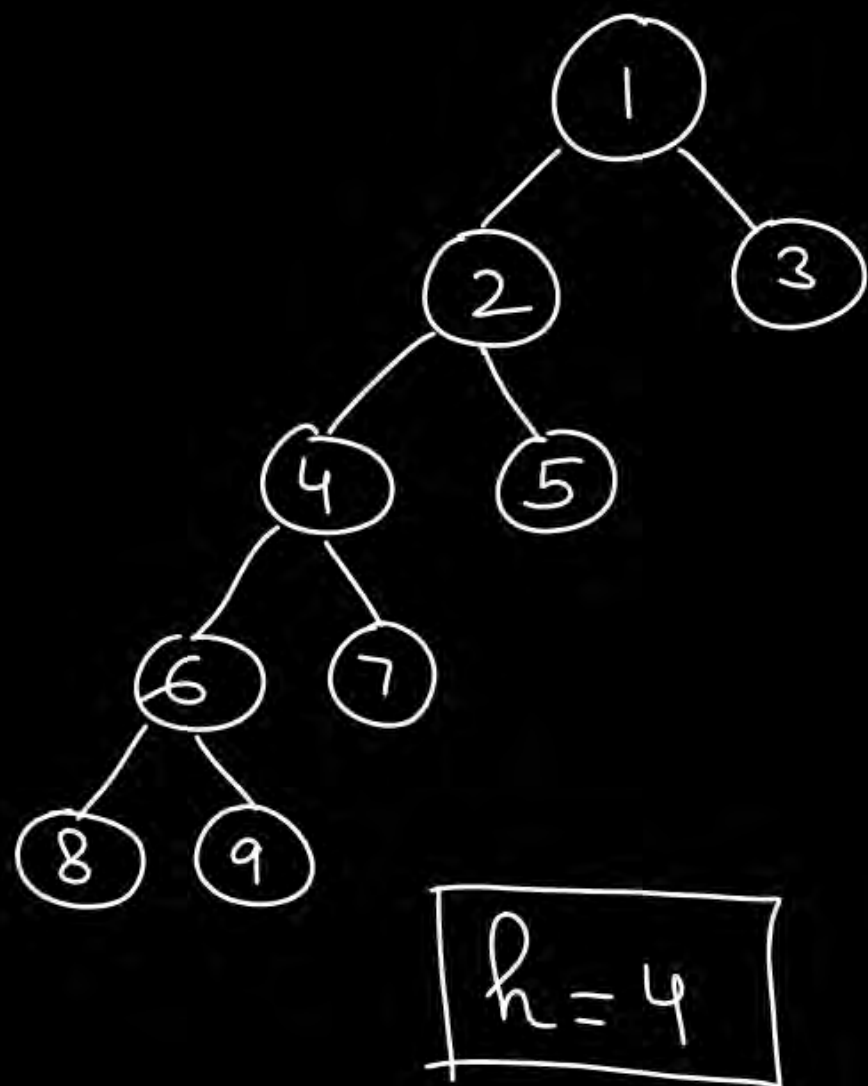
2.

The postorder traversal of a binary tree is 8, 9, 6, 7, 4, 5, 2, 3, 1.

The inorder trav. of the same tree is 8, 6, 9, 4, 7, 2, 5, 1, 3

The height of above binary tree is _____

2



Post : 8, 9, 6, 7, 4, 5, 2, 3, 1

In : 8, 6, 9, 4, 7, 2, 5, 1, 3

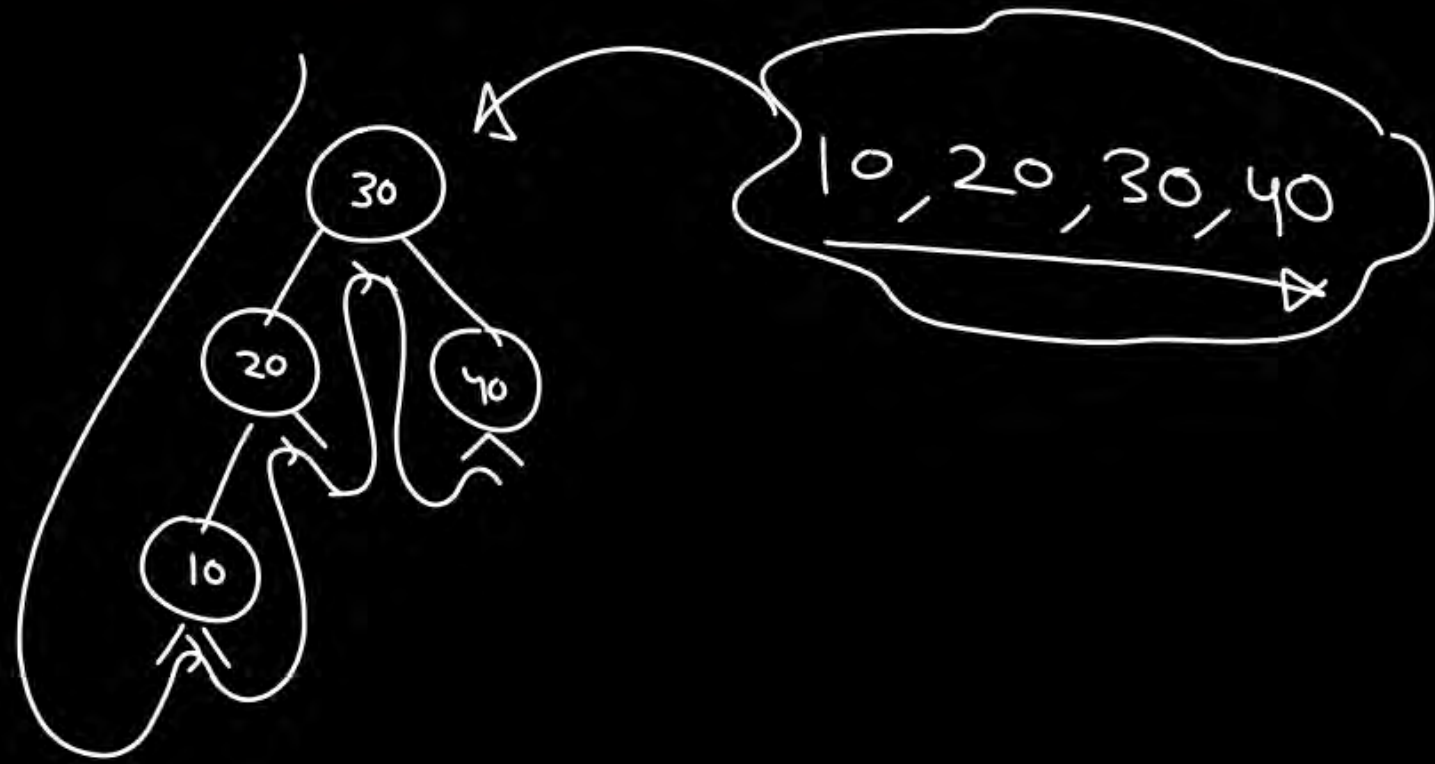
Q] We are given a set of n distinct elements and an unlabelled binary tree with n nodes. In how many ways can we populate the tree with given set so that it become a BST.

A] 0

B] 1

C] $n!$

D] $\frac{2n C_n}{n+1}$



Q] A BST stores values in the range 37 to 573.

Consider the following seq. of keys.

I) 81, 537, 102, 439, 285, 376, 305

II) 52, 97, 121, 195, 242, 381, 472

III) 142, 248, 520, 386, 345, 270, 307

IV) 550, 149, 507, 395, 463, 402, 270

Suppose the BST has been successfully searched for key 273.

Which all of above seq. list nodes in the order in which we could have encountered them in search.

Q] A BST stores values in the range 37 to 573.

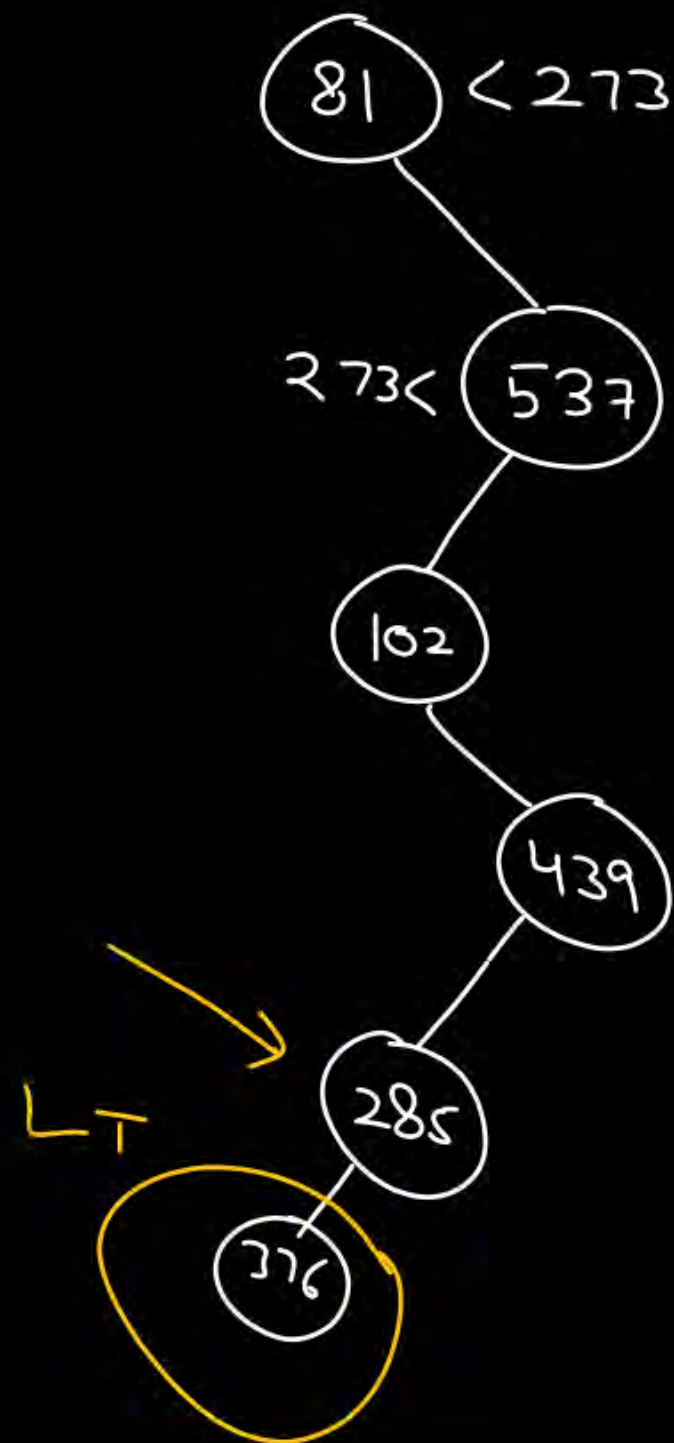
Consider the following seq. of keys.

I) 81, 537, 102, 439, 285, 376, 305 X

II) 52, 97, 121, 195, 242, 381, 472

III) 142, 248, 520, 386, 345, 270, 307

IV) 550, 149, 507, 395, 463, 402, 270



Q] A BST stores values in the range 37 to 573.

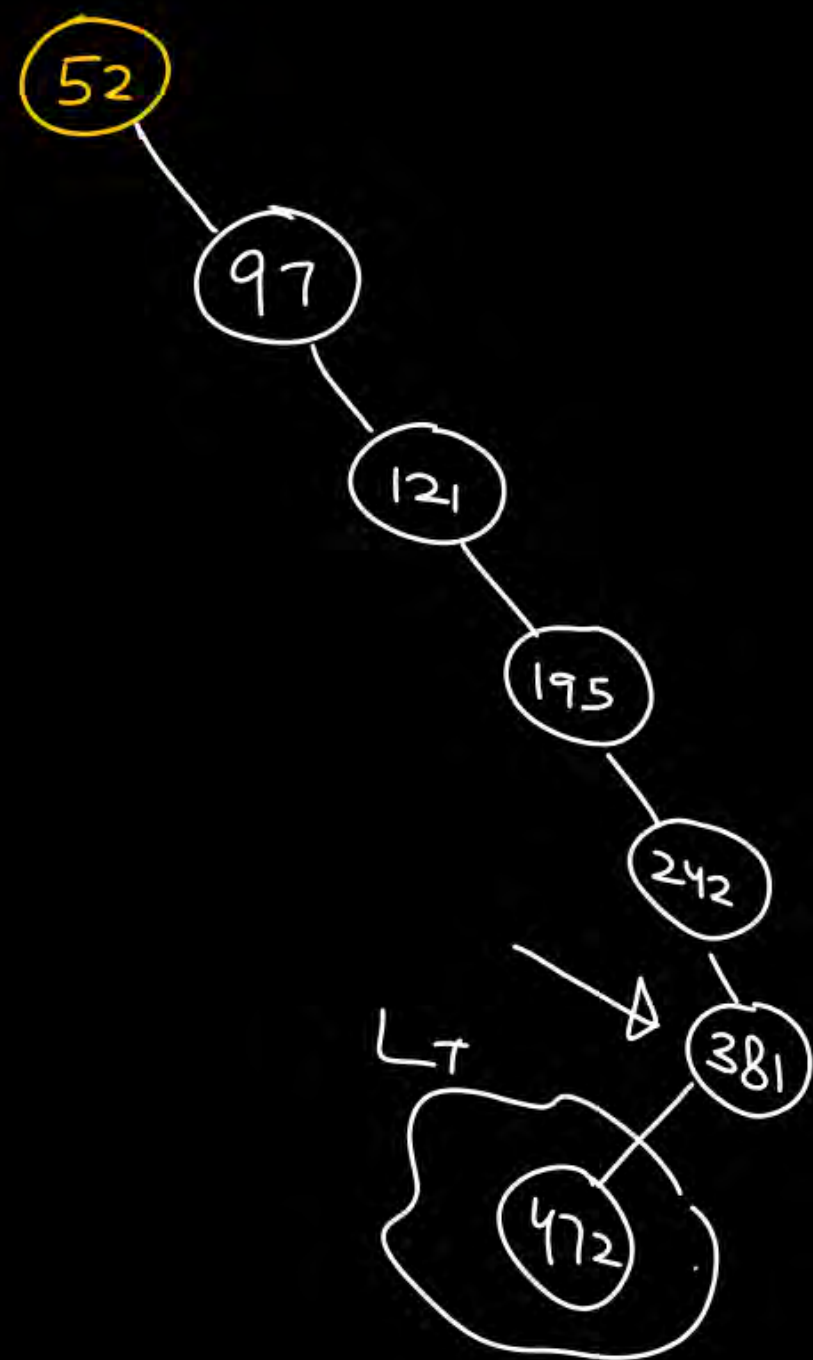
Consider the following seq. of keys.

I) 81, 537, 102, 439, 285, 376, 305 X

II) 52, 97, 121, 195, 242, 381, 472 X

III) 142, 248, 520, 386, 345, 270, 307

IV) 550, 149, 507, 395, 463, 402, 270



Q] A BST stores values in the range 37 to 573.

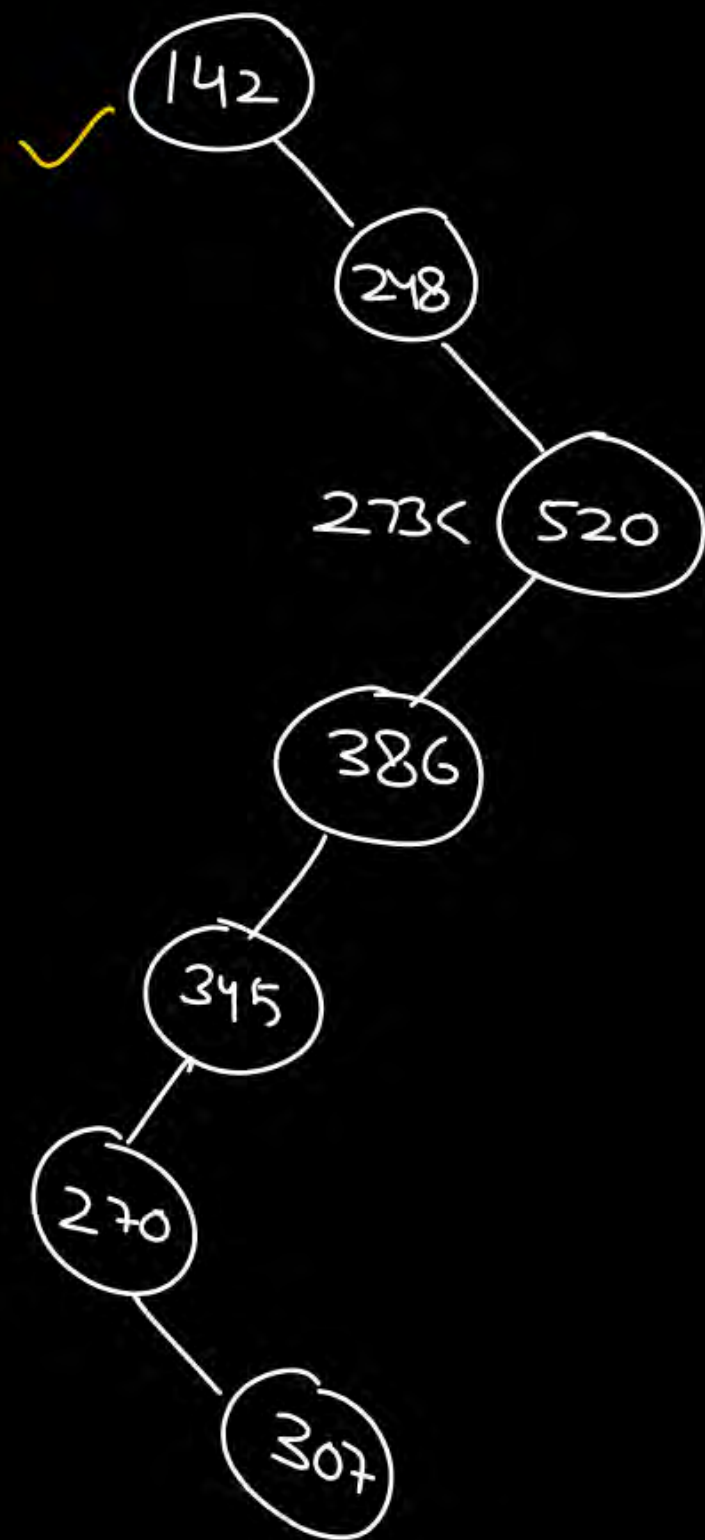
Consider the following seq. of keys.

I) 81, 537, 102, 439, 285, 376, 305 X

II) 52, 97, 121, 195, 242, 381, 472 X

III) 142, 248, 520, 386, 345, 270, 307 ✓✓

IV) 550, 149, 507, 395, 463, 402, 270



Q] A BST stores values in the range 37 to 573.

Consider the following seq. of keys.

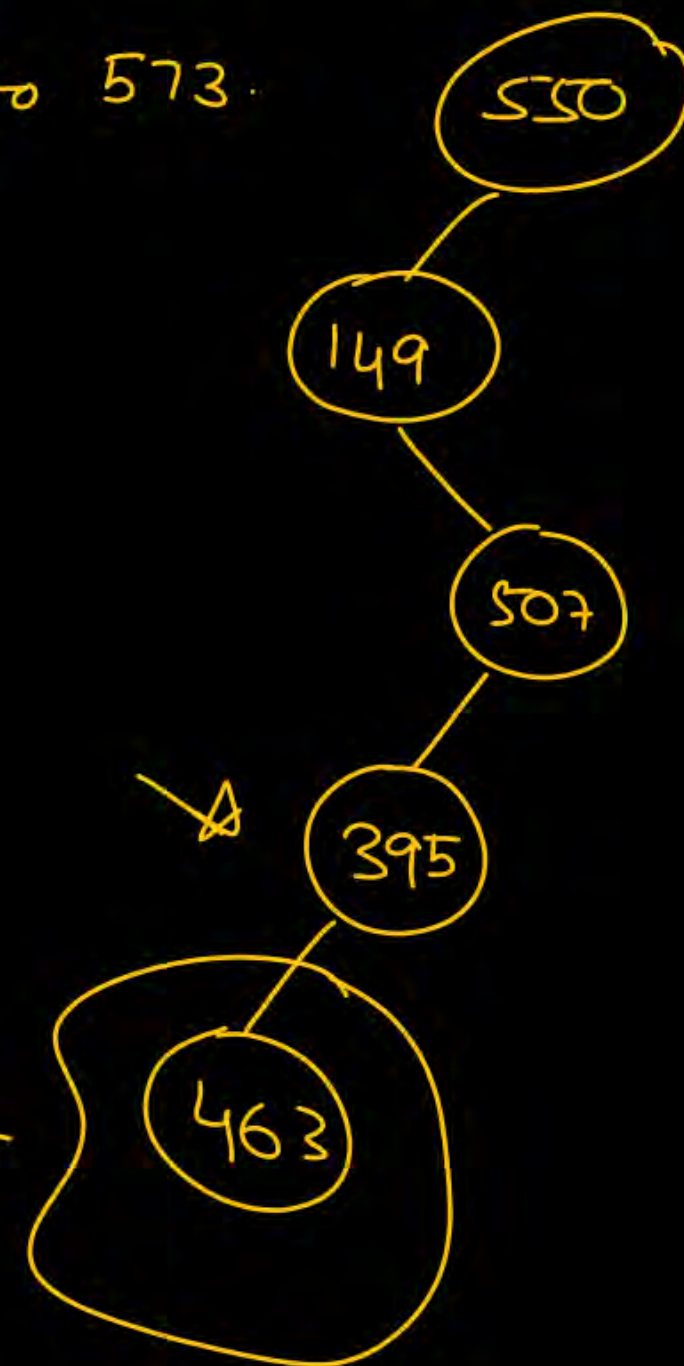
I) 81, 537, 102, 439, 285, 376, 305 X

II) 52, 97, 121, 195, 242, 381, 472 X

III) 142, 248, 520, 386, 345, 270, 307 ✓

IV) 550, 149, 507, 395, 463, 402, 270 X LT

III



When searching for the key 60 in a BST nodes containing keys 10, 20, 40, 50, 70, 80, 90 are trav. , not necessarily in this given order.

How many diff. orders are possible in which these key values can occur on the search path from root to the node containing key 60?

A) 35

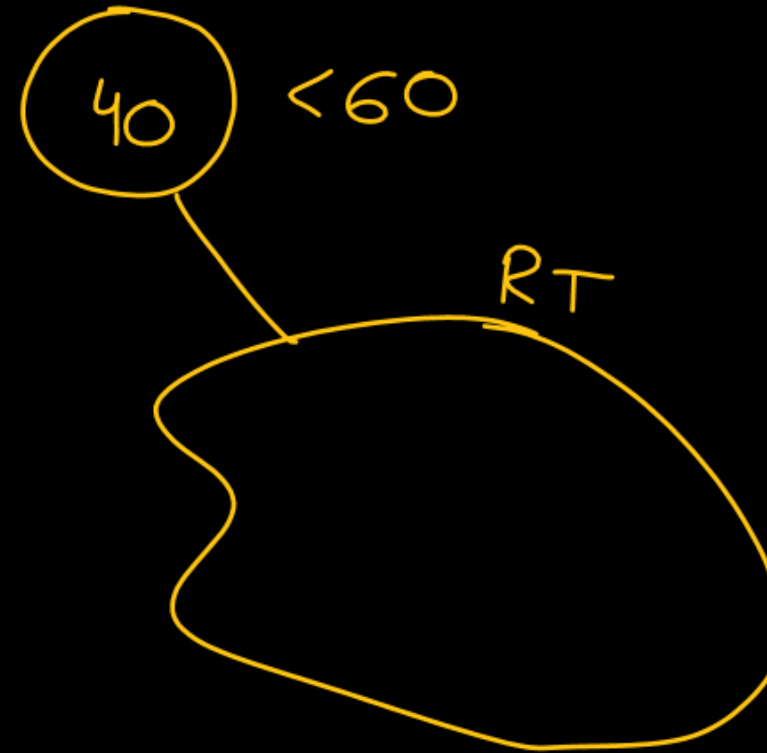
B) 64

C) 128

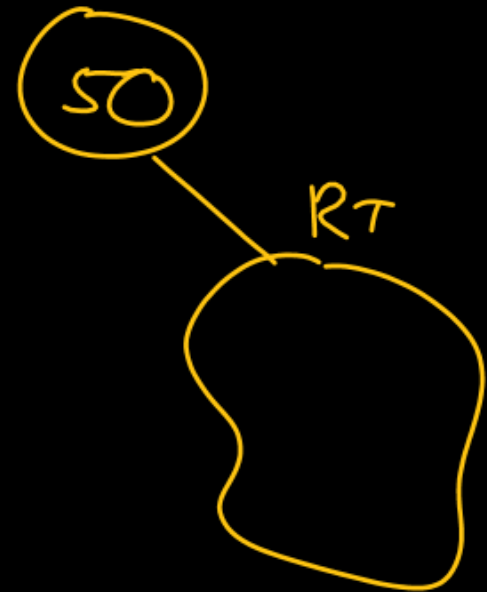
D) 5040

10, 20, 40, 50, 70, 80, 90

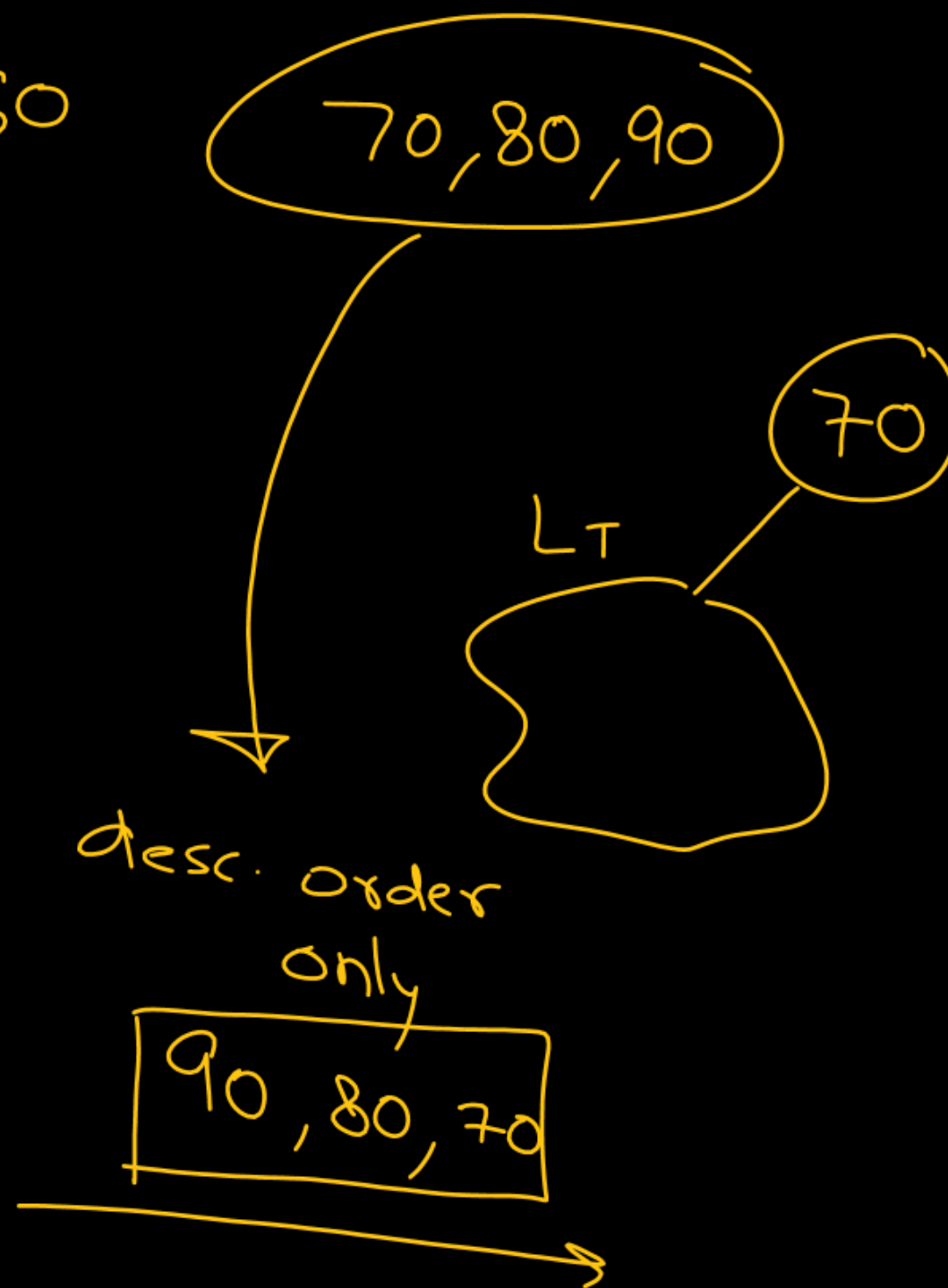
less than 40
10, 20



10, 20, 40



10, 20, 40, 50 → 60
these are
traversing only
in
ascending
order



80, 90
will
never
traversed

10, 20, 40, 50

90, 80, 70

3 place & 3 keys
No sel.
1 choice

7 space

✓ — — — — — ✓

Select any 4
place
out of

place \Rightarrow 1 choice

${}^7C_4 \times 1 = {}^7C_4 = 35$

10	90	20	80	70	40	50
✓		✓			✓	✓
90	10	20	80	70	40	50
	✓	✓			✓	✓
10	20	90	40	50	80	70
✓	✓		✓	✓		

PYQs + Coding (other than Gate)

→ Graph
→ Hashing $< \frac{1}{2}$ } Extra classes

