

CS & IT ENGINEERING



DIGITAL LOGIC
COMBINATIONAL CIRCUIT
Lecture No. 8



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TOPICS TO BE COVERED

01 COMPARATOR

02 QUESTION PRACTICE

03 DISCUSSION

COMPARATOR

DESIGNING OF COMBINATIONAL CIRCUIT

- Step 1. Find the number of inputs and outputs. ✓
- Step 2. Write the truth table. ✓
- Step 3. Write the logical expression. ✓
- Step 4. Minimize the logical expression. ✓
- Step 5. Hardware implementation. ✓

COMPARATOR

DESIGNING OF COMBINATIONAL CIRCUIT

1. Design a one-bit comparator



Step - 1

Step - 2 Truth table.

A	B	X (A > B)	Y (A < B)	Z (A = B)
0	0	0	0	1
0	1	0	1	0
1	0	1	0	0
1	1	0	0	1

COMPARATOR

DESIGNING OF COMBINATIONAL CIRCUIT

Step 3. Logical expression

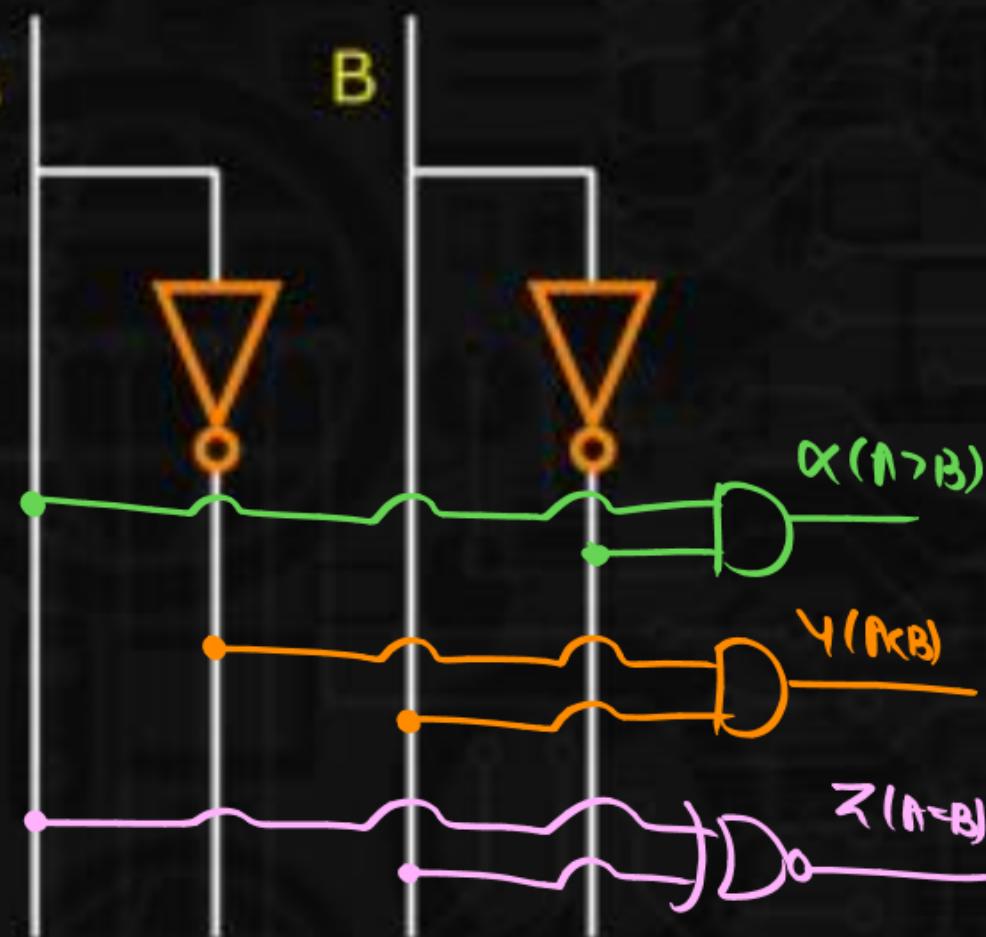
$$X(A > B) = \bar{A} \bar{B}$$

$$Y(A < B) = \bar{A} B$$

$$Z(A = B) = \bar{A} \bar{B} + A B = A \oplus B$$

Step 4. Minimization → Already minimized.

Step 5. Hardware implementation

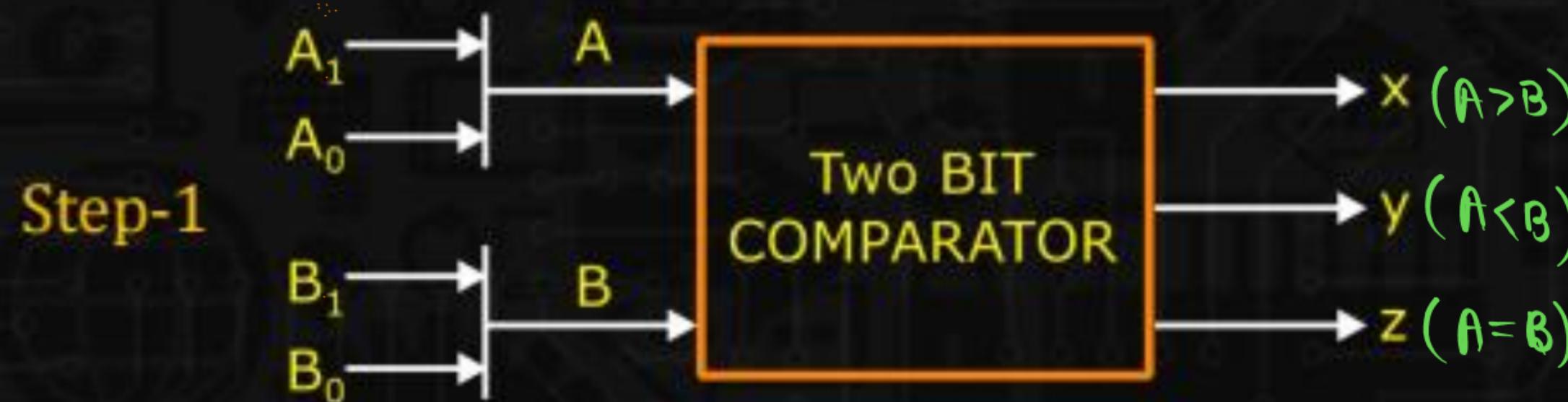




COMPARATOR

DESIGNING OF COMBINATIONAL CIRCUIT

2. Design a two-Bit comparator?



COMPARATOR

Step 2: Truth table

$$X(A > B) = \sum m(4, 8, 9, 12, 13, 14)$$

$$Y(A < B) = \sum m(1, 2, 3, 6, 7, 11)$$

$$Z(A = B) = \sum m(0, 5, 10, 15)$$

	A		B		$(A > B)$	$(A < B)$	$(A = B)$
	A_1	A_0	B_1	B_0	X	Y	Z
0→	0	0	0	0	0	0	1
1→	0	0	0	1	0	1	0
2→	0	0	1	0	0	1	0
3→	0	0	1	1	0	1	0
4→	0	1	0	0	1	0	0
5→	0	1	0	1	0	0	1
6→	0	1	1	0	0	1	0
7→	0	1	1	1	0	1	0
8→	1	0	0	0	1	0	0
9→	1	0	0	1	1	0	0
10→	1	0	1	0	0	0	1
11→	1	0	1	1	0	1	0
12→	1	1	0	0	1	0	0
13→	1	1	0	1	1	0	0
14→	1	1	1	0	1	0	0
15→	1	1	1	1	0	0	1

COMPARATOR

DESIGNING OF COMBINATIONAL CIRCUIT

Step 3. Logical expression

$$X(A > B) = \sum m(4, 8, 9, 12, 13, 14)$$

$$Y(A < B) = \sum m(1, 2, 3, 6, 7, 11)$$

$$Z(A = B) = \sum m(0, 5, 10, 15)$$

2 bit

Total combination = 16

Equal = 4

Unequal = $16 - 4 = 12$

Greater = Less = 6

COMPARATOR

DESIGNING OF COMBINATIONAL CIRCUIT

Step 4. Minimization

Minimized Expression.

$$X(A > B) = A_1 \bar{B}_1 + A_1 A_0 \bar{B}_0 + A_0 \bar{B}_1 \bar{B}_0$$

For X ($A > B$)

$$X(A > B) = A_1 \bar{B}_1 + (A_1 + \bar{B}_1) A_0 \bar{B}_0$$

		$\bar{B}_1 \bar{B}_0$	$\bar{B}_1 B_0$	$B_1 B_0$	$B_1 \bar{B}_0$
		00	01	11	10
$\bar{A}_1 \bar{A}_0$	00				
$\bar{A}_1 A_0$	01	1			
$A_1 A_0$	11	1	1		
$A_1 \bar{A}_0$	10	1	1		

For Y ($A < B$)

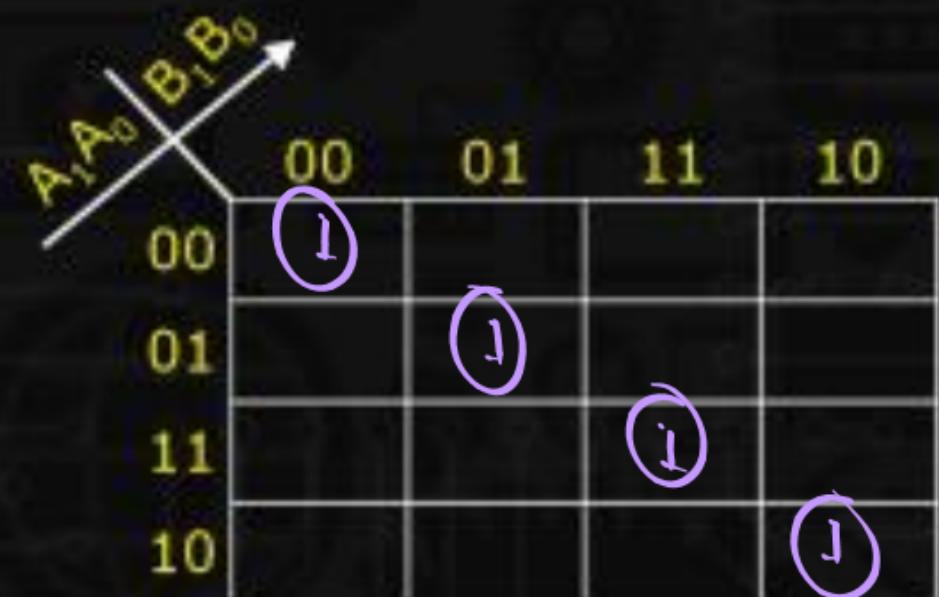
		$\bar{B}_1 \bar{B}_0$	$\bar{B}_1 B_0$	$B_1 B_0$	$B_1 \bar{B}_0$
		00	01	11	10
$\bar{A}_1 \bar{A}_0$	00				
$\bar{A}_1 A_0$	01			1	
$A_1 A_0$	11		1	1	
$A_1 \bar{A}_0$	10		1	1	

COMPARATOR

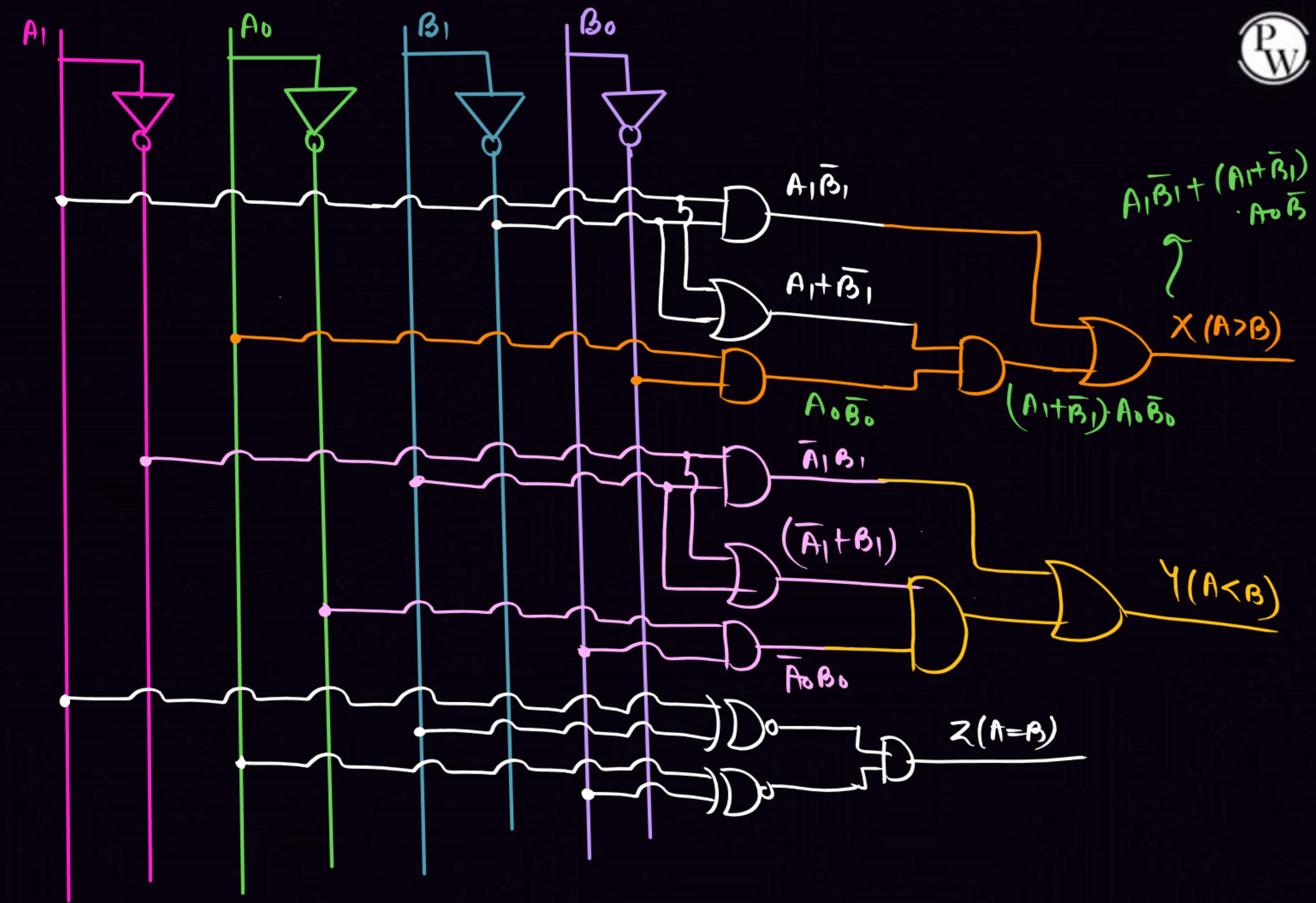
DESIGNING OF COMBINATIONAL CIRCUIT

Step 4. Minimization

For Z



$$\bar{Z}(A=B) = (A_1 \oplus B_1) \cdot (A_0 \oplus B_0)$$

Step 5.:

		$X(A > B)$	<u>Semiminimized</u>	
		$\bar{A}_1 \bar{B}_0 \quad \bar{B}_1 \bar{B}_0$	$\bar{B}_1 \bar{B}_0 \quad \bar{B}_1 B_0$	$B_1 B_0 \quad B_1 \bar{B}_0$
		$\bar{A}_1 \bar{A}_0$		
		J		
$A_1 A_0$		1	1	1
$A_1 \bar{A}_0$		1	1	

		$Y(A < B)$	<u>Semiminimized</u>	
		$\bar{A}_1 \bar{B}_0 \quad \bar{B}_1 \bar{B}_0$	$\bar{B}_1 \bar{B}_0 \quad \bar{B}_1 B_0$	$B_1 B_0 \quad B_1 \bar{B}_0$
		$\bar{A}_1 \bar{A}_0$		
		J	1	1
$\bar{A}_1 A_0$			1	1
$A_1 A_0$				
$A_1 \bar{A}_0$				1

$$\begin{aligned}
 X(A > B) &= \bar{A}_1 \bar{B}_1 + \bar{A}_1 A_0 \bar{B}_1 \bar{B}_0 + A_1 A_0 B_1 \bar{B}_0 \\
 &= A_1 \bar{B}_1 + (\bar{A}_1 \bar{B}_1 + A_1 B_1) A_0 \bar{B}_0
 \end{aligned}$$

$$X(A > B) = A_1 \bar{B}_1 + (A_1 \bar{B}_1) A_0 \bar{B}_0$$

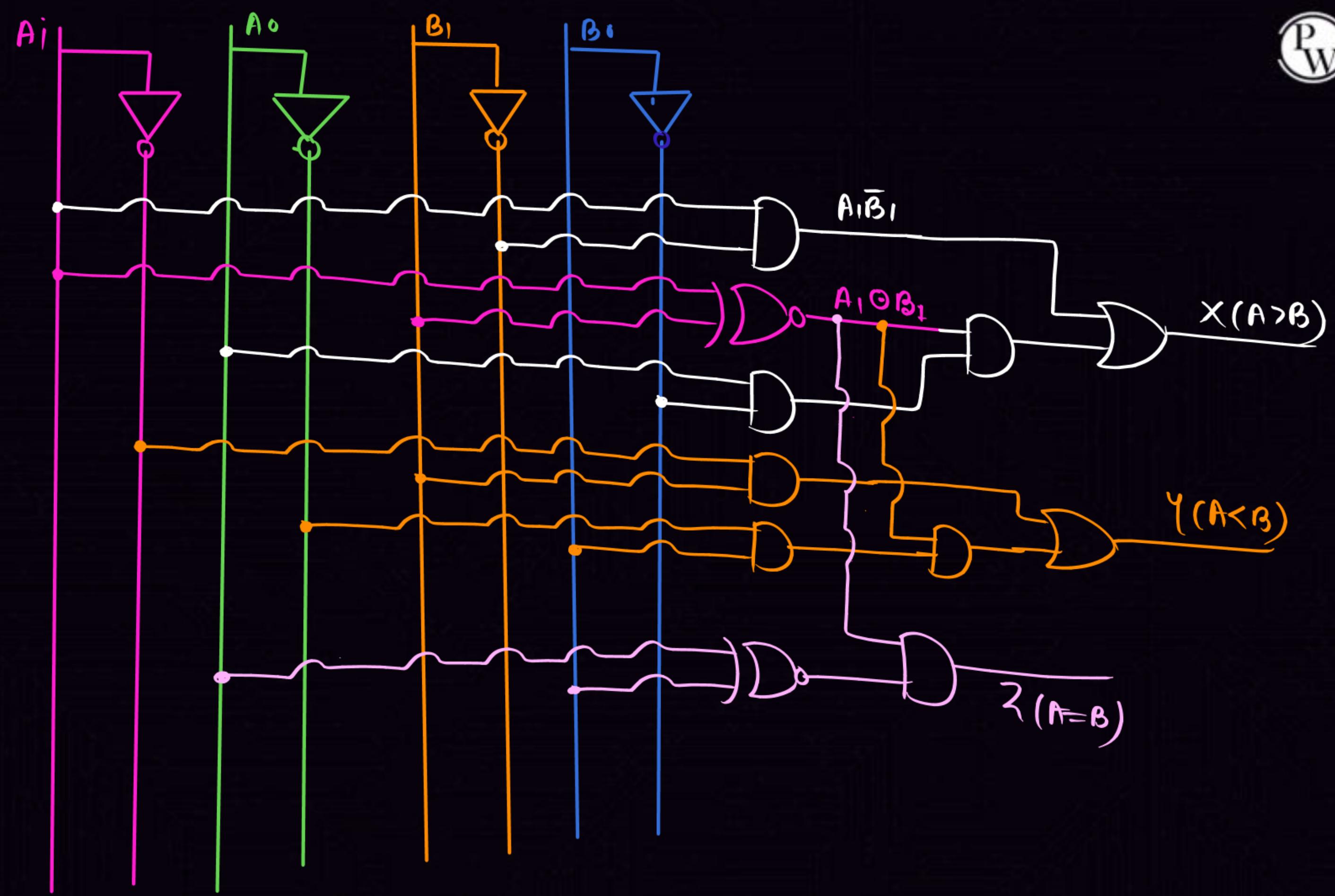
$$\begin{aligned}
 Y(A < B) &= \bar{A}_1 B_1 + \bar{A}_1 \bar{A}_0 \bar{B}_1 B_0 + A_1 \bar{A}_0 B_1 B_0 \\
 Y(A < B) &= \bar{A}_1 B_1 + (\bar{A}_1 \bar{A}_0 + A_1 B_1) \bar{A}_0 B_0
 \end{aligned}$$

$$Y(A < B) = \bar{A}_1 B_1 + (A_1 \bar{B}_1) \bar{A}_0 B_0$$

$$\chi(A > B) = A_1 \bar{B}_1 + (A_1 \odot B_1) \cdot A_0 \bar{B}_0$$

$$\psi(A < B) = \bar{A}_1 B_1 + (A_1 \odot B_1) \cdot \bar{A}_0 B_0$$

$$\zeta(A = B) = (A_1 \odot B_1) \cdot (A_0 \odot B_0)$$



COMPARATOR

FOR ONE BIT COMPARATOR

Total condition = 4

Equal condition = 2

Unequal condition = 2

Greater = Less condition = 1

COMPARATOR

FOR TWO BIT COMPARATOR

Total condition = 16

Equal condition = 4

Unequal condition = 12

Greater = Less condition = 6

COMPARATOR

FOR THREE BIT COMPARATOR

Total condition = 64

Equal condition = 8

Unequal condition = 56

Greater = Less condition = 28

COMPARATOR

'n' BIT COMPARATOR

Total condition = 2^{2n}

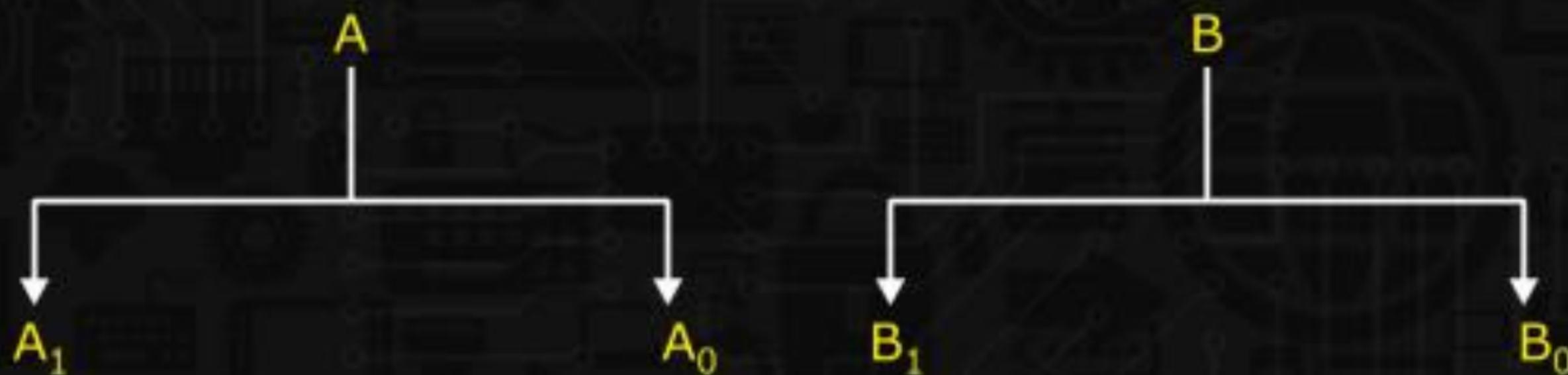
Equal condition = 2^n

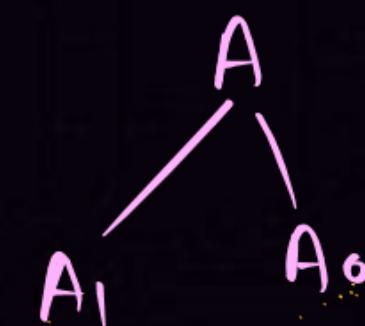
Unequal condition = $2^{2n} - 2^n$

Greater = Less condition = $(2^{2n} - 2^n)/2$

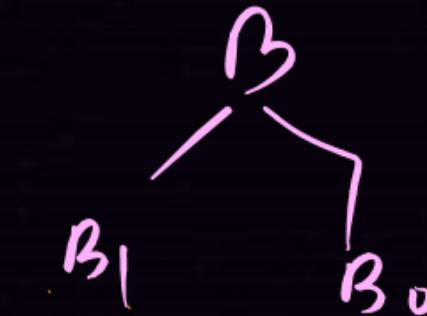
COMPARATOR

SHORT TRICK TO USE SEMI MINIMIZED EXPRESSION





=

Semiminimized

3 5

$$\chi(A > B) = A_1 \bar{B}_1 + (A_1 \odot B_1) \cdot A_0 \bar{B}_0$$

$$\psi(A < B) = \bar{A}_1 B_1 + (A_1 \odot B_1) \cdot \bar{A}_0 B_0$$

$$\zeta(A = B) = (A_1 \odot B_1) \cdot (A_0 \odot B_0)$$

3 5

Minimized

$$\chi(A > B) = A_1 \bar{B}_1 + (A_1 + \bar{B}_1) \bar{A}_0 \bar{B}_0$$

$$\psi(A < B) = \bar{A}_1 B_1 + (\bar{A}_1 + B_1) \bar{A}_0 B_0$$

$$\zeta(A = B) = (A_1 \odot B_1) \cdot (A_0 \odot B_0)$$

3bit semiminimized



$$X(A > B) = A_2 \bar{B}_2 + (A_2 \odot B_2) A_1 \bar{B}_1 + (A_2 \odot B_2) \cdot (A_1 \odot B_1) A_0 \bar{B}_0$$

$$Y(A < B) = \bar{A}_2 B_2 + (A_2 \odot B_2) \bar{A}_1 B_1 + (A_2 \odot B_2) \cdot (A_1 \odot B_1) \bar{A}_0 B_0$$

$$Z(A = B) = (A_2 \odot B_2) \cdot (A_1 \odot B_1) \cdot (A_0 \odot B_0)$$

HW

Design a 2bit comparator

by using one bit
comparator?

