

# EE, EC, CS & IT ENGINEERING



Digital Logic  
Number System

BASE CONVERSION

DPP Solution 01



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## TOPICS TO BE COVERED

01 Questions

02 Discussion

**Q.1**

The two addition operations  $24 + 14 = 41$  and  $23 + 12 = 101$  are performed on number bases  $b_1$  and  $b_2$  respectively. The values of  $b_1$  and  $b_2$  are respectively

- A. ~~7 and 4~~
- B. 4 and 7
- C. 8 and 4
- D. 4 and 8

$$(24)_{b_1} + (14)_{b_1} = (41)_{b_1}$$

$$2b_1 + 4 + b_1 + 4 = 9b_1 + 1$$

$$\boxed{b_1 = 7}$$

$$(23)_{b_2} + (12)_{b_2} = (101)_{b_2}$$

$$2b_2 + 3 + b_2 + 2 = b_2^2 + 1$$

$$\boxed{b_2^2 - 3b_2 - 4 = 0}$$

$$b_2 = \frac{3 \pm \sqrt{9 + 16}}{2}$$

$$b_2 = \frac{3 \pm 5}{2} = \boxed{4}$$

**Q.2**

If  $x$  and  $y$  are successive numbers in a number system of base  $b$  such that  $(xy)_b = (25)_{10}$  and  $(yx)_b = (31)_{10}$ , then

**A.**

$$x = 4, y = 5 \text{ and } b = 7$$

$$x \times b^1 + y \times b^0 = 25$$

$$xb + y = 25$$

$$yb + x = 31$$

**B.**

$$x = 3, y = 4 \text{ and } b = 6$$

$$\begin{aligned} 3 \times 7 + 4 \\ 21 + 4 = 25 \end{aligned}$$

$$\begin{aligned} 4 \times 7 + 3 \\ 28 + 3 = 31 \end{aligned}$$

**C.**

$$x = 4, y = 5 \text{ and } b = 6$$

$$x = 3, y = 4 \text{ and } b = 7$$

~~**D.**~~

**Q.3**

If  $a = (4.4)_5$  and  $b = (3.3)_5$ , then  $a + b = (x)_5$ . The subscript 5 denotes the base on which the corresponding number is expressed. The value of x is

- A. 31.2
- B. 7.2
- C. 8.7
- D. 13.2

$$\begin{array}{r} & 1 \\ & (4 \cdot 4)_5 \\ + & (3 \cdot 3)_5 \\ \hline (1, 3 \cdot 2) & 5 \end{array}$$

$$\begin{array}{r} 0 \leftarrow 5 \\ 1 \leftarrow 6 \\ \textcircled{2} \leftarrow 7 \\ 3 \leftarrow 8 \\ 4 \leftarrow 9 \\ \hline 1 & 0 \checkmark \\ | & | \\ 8 & 2 \\ - & - \\ \hline 1 & 2 \\ | & | \\ 1 & 2 \\ - & - \\ \hline 1 & 2 \end{array}$$

$$\begin{array}{r} 1 \\ \hline 2 \end{array}$$

**Q.4**

If  $(X \ 1CY)_{16} = \underline{(120702)}_8$ , then X and Y are

- A. A and 2
- B. B and 1
- C. I and B
- D. 2 and A

001010000110000010

$$(A \ 1 \ C \ 2)_{16}$$
$$X \ 1 \ C \ Y$$

X = A    Y = 2

**Q.5**

Given  $(135)_b + (144)_b = (323)_b$  where subscript b denotes the base on which numbers are expressed. What is value of b ?

A. 4

$$(135)_b + (144)_b = (323)_b$$

$$b^2 + 3b + 5 + b^2 + 4b + 4 = 3b^2 + 2b + 3$$

B. 5

$$b^2 - 5b - 6 = 0$$

C. 6

$$b = \frac{5 \pm \sqrt{25 + 4 \times 6}}{2}$$

$$b = \frac{12}{2} = 6$$

D. 7

$$b = \frac{5 \pm \sqrt{25 + 16}}{2}$$

$$b = \frac{5 \pm 7}{2}$$

Q. 6

In a digital computer, binary subtraction is performed

A. In the same way as we perform subtraction in decimal number system

B. Using two's complement method

$A + (-B)$

C. Using 9's complement method.

D. Using 10's complement

Q. 7

The greatest negative number, which can be stored in a computer that has 8-bit word length and uses 2's complement arithmetic, is

- A. -256
- B. -255
- C. -128
- D. -127

$$\begin{aligned}\text{Range} &= -[2^{n-1}] \text{ to } +[2^{n-1}-1] \\ &= -[2^{8-1}] \text{ to } [2^{8-1}-1] \\ &= -2^7 \text{ to } \{2^7-1\} \\ &\boxed{= -128 \text{ to } +127}\end{aligned}$$

Q.8

F's complement of  $(2BFD)_{hex}$  is

- A. E304
- B. D403
- C. ~~D402~~
- D. C403

$$\begin{array}{r} \text{FFFF} \\ - 2BFD \\ \hline \text{B402} \end{array}$$

15

A=10  
B=11  
C=12  
D=13 ✓  
E=14  
F=15

**Q.9**

The result of addition operation  $34 + 43$  performed on minimum base is stored in an 8-bit register. The content of register will be

A. 01000011

B. ~~00101010~~

C. 01010101

D. 01010100

$$\begin{array}{r} (34) \\ \text{---} \\ (43) \end{array} \quad \begin{array}{l} 5 \\ 5 \end{array}$$

$$[3 \times 5^1 + 4 \times 5^0] + [4 \times 5^1 + 3 \times 5^0]$$

$$15 + 4 + 20 + 3$$

$$19 + 23 = 42$$

$$\begin{array}{r} 32 \ 18 \ 42 \ 1 \\ - 00 \ 10 \ 10 \ 10 \\ \hline \end{array}$$

Q.50

Which of the following is equal to  $\underline{\underline{(AB)}_{16}}$  ?

- A. ~~(B7)<sub>16</sub> - (A)<sub>16</sub>~~
- B. ~~(B5)<sub>16</sub> - (A)<sub>16</sub>~~
- C.  $(A0)_{16} + (D)_{16}$
- D.  $(BA)_{16} + (01)_{16}$

$$\begin{array}{r} 1011\overbrace{10}^A\overbrace{10}^B1 \\ - 00001010 \\ \hline 1010\overbrace{1011}^B \end{array}$$

$$\underline{\underline{(AB)}_{16}}$$

**Q. 11**

An equivalent 2's complement representation of the 2's complement number 1101 is

A. 110100

B. 001101

C. 110111

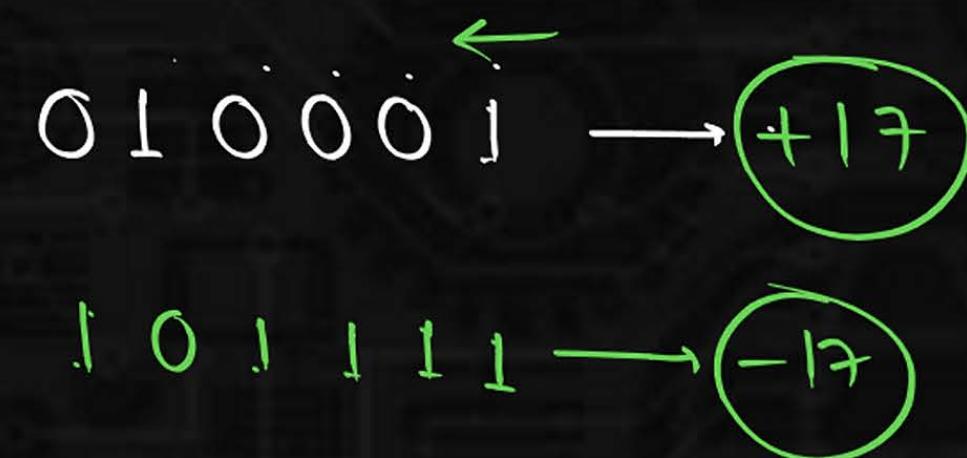
D. ~~111101~~

$$\begin{array}{r} \text{1101} \\ - \\ \text{11101} \end{array}$$

Q.12

The 2's complement representation of -17 is

- A. 101110
- B. 101111
- C. 111110
- D. 110001



**Q. 13**

11001, 1001 and 111001 correspond to the 2's complement representation of which one of the following sets of number?

- A. 25.9 and 57 respectively
- B. -6, -6 and -6 respectively
- C. -7, -7 and -7 respectively
- D. -25, -9 and -57 respectively

$$\begin{array}{r} 11001 \xrightarrow{\leftarrow} -7 \\ 00111 \xrightarrow{\rightarrow} +7 \\ \hline 11001 \xrightarrow{\rightarrow} -7 \\ 111001 \xrightarrow{\rightarrow} -7 \\ 11111001 \xrightarrow{\rightarrow} -7 \end{array}$$

Q. 14

X = 01110 and Y = 11001 are two 5-bit binary numbers represented in two's complement format. The sum of X and Y represented in two's complement format using 6 bits is

- A. 100111
- B. 001000
- C. 000111
- D. 101001

$$\begin{array}{r} X = 01110 = +14 \\ Y = 11001 \xleftarrow{\quad} = -7 \\ \hline ++ \\ \overline{000111} \end{array}$$

