

GATE



ALL BRANCHES

GENERAL APTITUDE

Quantitative Aptitude



Lecture No: 05

By-Amulya Ratan Sir





TOPICS TO BE COVERED



More on Mixtures Alligations



Concept of Counting Theory



With & Without repetition ways



Questionnaire on the Topic



More Questions:



$$\underline{\underline{x = 5 \text{ lit} + \checkmark}}$$

A 40 litres of mixture contains 10% water in it and remaining milk. How many litres of water are to be added to the mixture, so that it would become 20% water in it?

$$\frac{36}{40+x} = \frac{80}{100}$$

Water
4 lit

40 lit ^{Min} ✓

Milk

✓ 36 lit

$$\frac{4+x}{40+x} = \frac{20}{100}$$

$$\frac{4+x}{36} = \frac{20}{80}$$



Q.

A 40 litres of mixture contains 10% water in it and remaining milk. How many litres of water are to be added to the mixture, so that it would become 20% water in it?

Mix: water

$$= 80 : 10$$

$$= 8 : 1$$

$$\times 5 \quad \times 5$$

$$= 40 : 5$$

Mix

10%

Water

100%

20

80

10

$$\frac{8 \times 2}{1 \times 2}$$



Q. In a mixture of 40 litres, the ratio of milk and water is 4:1.
How much water much be added to this mixture so that
the ratio of milk and water becomes 2:3?



A. 20 litres



B. 32 litres



C. 40 litres



D. 30 litres

Mix: water

$$= \frac{4}{5} : \frac{1}{5}$$

$$= 4 : 1$$

$$= 40 : 40$$

Mix

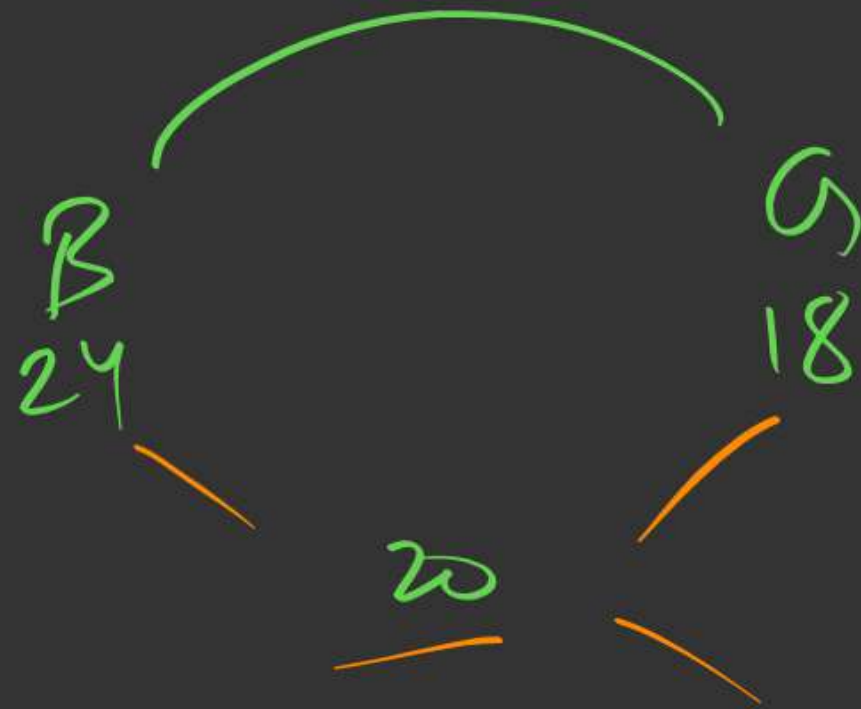
$$\frac{1}{5}$$

Water

$$\frac{2}{5}$$

$$\frac{2}{5}$$

$$\frac{2}{5}$$



$$24B + 18G = 20B + 20G$$

$$4B = 2G$$

$$\frac{B}{G} = \frac{2}{4}$$



Q.

An alloy A consist of iron & copper in the ratio 5 : 7, whereas alloy B consist iron & copper in the ratio 3 : 1. In what ratio these two alloys are to be mixed to form a new alloy with iron & copper in the ratio 2 : 1?



A. 5 : 13



B. 3 : 1



C. 7 : 5



D. 1 : 3

$$A:B = \frac{1}{12} : \frac{3}{12}$$

$$= \underline{\underline{1:3}}$$

$$A$$

$$\frac{5}{12}$$

$$B$$

$$\frac{3}{4} = \frac{9}{12}$$

$$\frac{8}{12} = \frac{2}{3}$$

$$\frac{1}{12}$$

$$\frac{1}{3}$$



Q.

A mixture contains milk and water in the ratio 5:1. On adding 5 liters of water, the ratio of milk to water becomes 5:2. the quantity of milk in the mixture earlier was:



A.

16 litres



B.

25 litres



C.

32.5 litres



D.

22.75 litres

30 lit

Milk

5 lit

Water

$$\frac{7}{42} = \frac{1}{6}$$

Milk: Water

$$= 30:5$$

$$\frac{12}{42}$$

$$\frac{6 \times 2}{6 \times 7}$$

$$\frac{30}{42}$$

$$\frac{42}{42}$$

$$\frac{5}{8} \times \frac{5}{30}$$

$$\frac{5}{42}$$

$$25 \text{ lit}$$



Q. In what ratio must a grocer mix two varieties of pulses costing ₹15 and ₹20 per kg respectively so as to get a mixture worth ₹16.50 per kg?

A. 5:3

B. 7:3

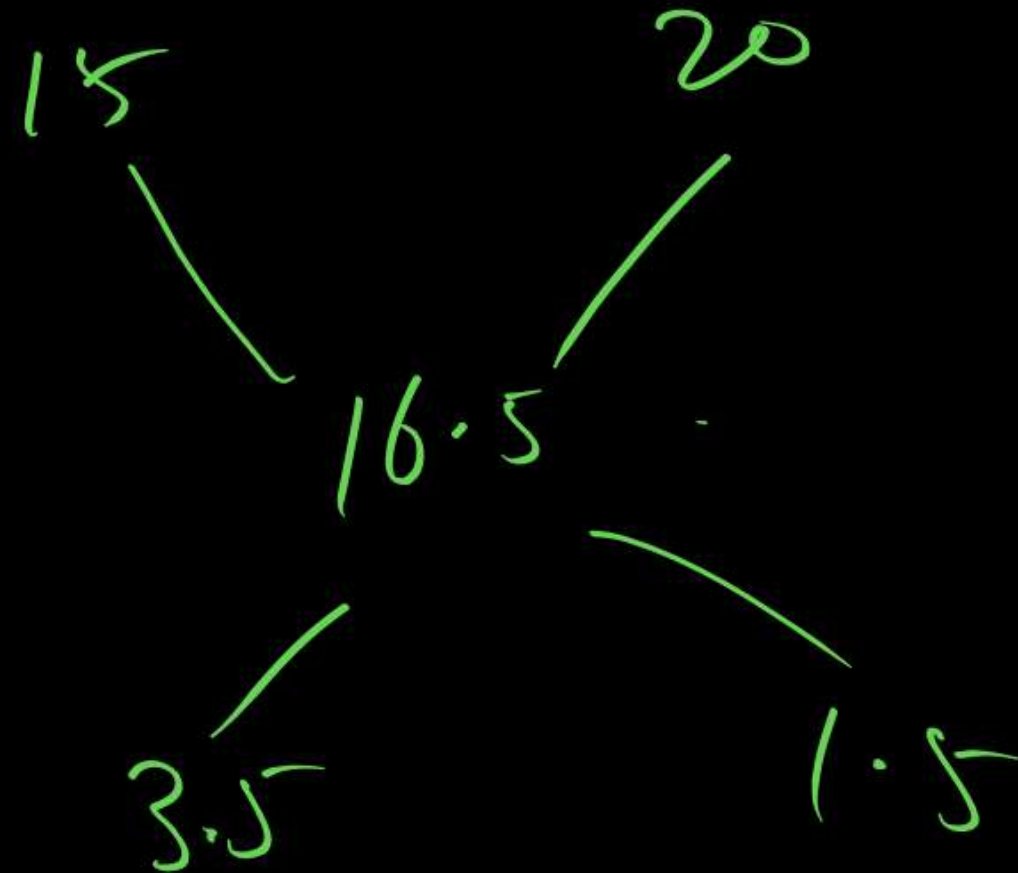
C. 3:8

D. 4:5

$$3.5 : 1.5$$

$$= 35 : 15$$

$$= 7 : 3$$





Q. In what ratio must Ankit mix two varieties of sugar worth ₹20 per kg and ₹32 per kg so that by selling the mixture at ₹36 per kg he may gain 20%?



A. 3 : 2



B. 2 : 3

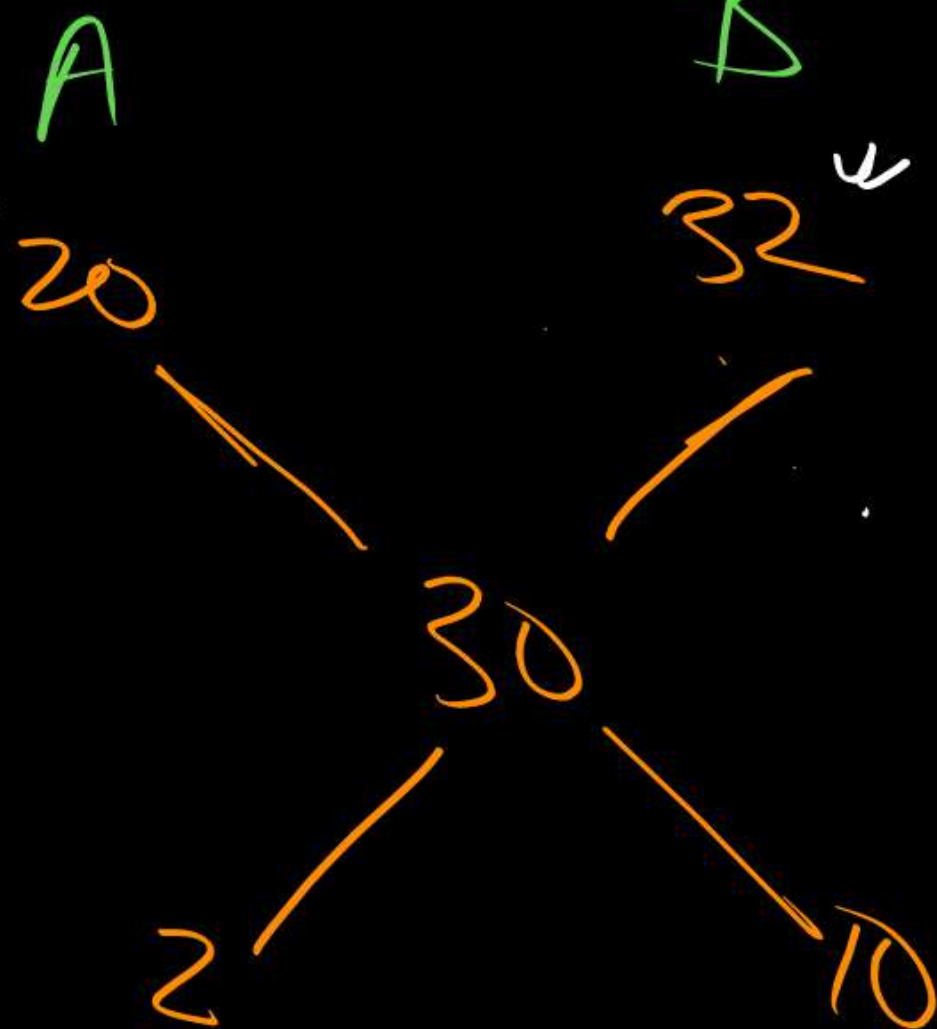


C. 3 : 5



D. 1 : 5

$$A:B = 2:10 \\ = 1:5$$



$$S.P = 36$$

$$P = 20\%$$

$$\frac{36}{C.P} = 1.2$$

$$\frac{36}{1.2} = C.P$$



Q.

A man buys milk at ₹5 per litre and after adding water, sells it at ₹6 per litre, thereby making a profit of $33\frac{1}{3}\%$. What is the proportion of milk to water in the mixture?

A.  1 : 9

B.  9 : 10

C.  9 : 1

D.  4 : 5

Assignment



Q.

A man purchases two mobiles for ₹65390, sells both of them so as to gain $13\frac{1}{2}\%$ on one and lose $2\frac{3}{4}\%$ on other. If on the whole he gains $7\frac{1}{4}\%$, then what would be the cost of cheaper mobile?

Assignment



A. ₹32000



B. ₹25150



C. ₹27500



D. ₹31000



← Quantitative

Counting
↓
calculation

Measurement

Comparison

(211) OR (+)

(3112) AND (X)



Counting Theory



ATM PIN Generate





Q. In how many different ways you can choose your ATM PIN?



0 0 0 0
9 9 9 9

8 ✓
9 ✓

0 ✓
1 ✓
2 ✓
3 ✓
4 ✓
5 ✓
6 ✓
7 ✓

$$10 \times 10 \times 10 \times 10$$

$$= 10,000$$



Q. In how many different ways you can select a six digit
phone password/passcode ?



$$10 \times 10 \times 10 \times 10 \times 10 \times 10$$

$$= 1,000,000$$



Q.

How many four digits number can be formed using 1, 2, 3, 4 & 5?



Repetition Allowed

Th	H	Tu	U
5	5	5	5

$$= \underline{\underline{625}}$$

Repetition Not Allowed

Th	H	Tu	U

$$5 \times 4 \times 3 \times 2$$

$$= \textcircled{120}$$



Q. In how many different ways you can choose your ATM PIN which is an even ?



$$\begin{array}{ccccccc} & \overline{\overline{10}} & \times & 10 & \times & 10 & \times & 5 \\ & \boxed{} & & \boxed{} & & \boxed{} & & \boxed{} \\ & & & & & & & \downarrow \\ = & \overline{\overline{5000}} & & & & & & \begin{array}{l} 0 \\ 2 \\ 4 \end{array} \\ & & & & & & & \begin{array}{l} 6 \\ 8 \end{array} \end{array}$$



How many three digits number can be formed using digits 0 to 9?



Repetition Allowed

~~✗~~

$$\begin{array}{ccc} \text{H} & \text{Ten} & \text{U} \\ \boxed{9} & \times \boxed{10} & \times \boxed{10} \\ 10-1 & & \end{array}$$

$$= 900$$

Without Repetition

$$\begin{array}{ccc} \text{H} & \text{10-1 Ten} & \text{10-2 Unit} \\ \boxed{9} & \times \boxed{9} & \times \boxed{8} \\ 9 & \times & 9 \times 8 \end{array}$$

$$= 81 \times 8 = 648$$



Q.

In how many ways four letters can be posted in 6 post boxes, if each box can take any number letters?



A.

4096



B.

1500



C.

24



D.

1296

$L_1 \quad L_2 \quad L_3 \quad L_4$

$6 \times 6 \times 6 \times 6$

$= 36 \times 36$

$= 1296$





Q. In how many ways can you arrange 5 Novels on a shelf?



720



120



360



300

$$\underline{5} \times \underline{4} \times \underline{3} \times \underline{2} \times \underline{1}$$

$$5-1 \quad 5-2 \quad 5-3 \quad 5-4$$

$$= \underline{\underline{120}}$$





Q.

Four persons A, B, C and D are to be seated in a row. C should not be seated at the second position from the left end of the row. The number of distinct seating arrangements possible is?



A.

6



B.

9



C.

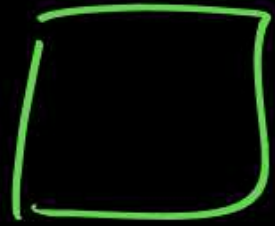
18



D.

24

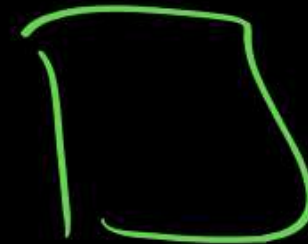
4-1



~~4-2~~



4-2



4-3



3

x

3

x

2

x

1

=

18





Q.

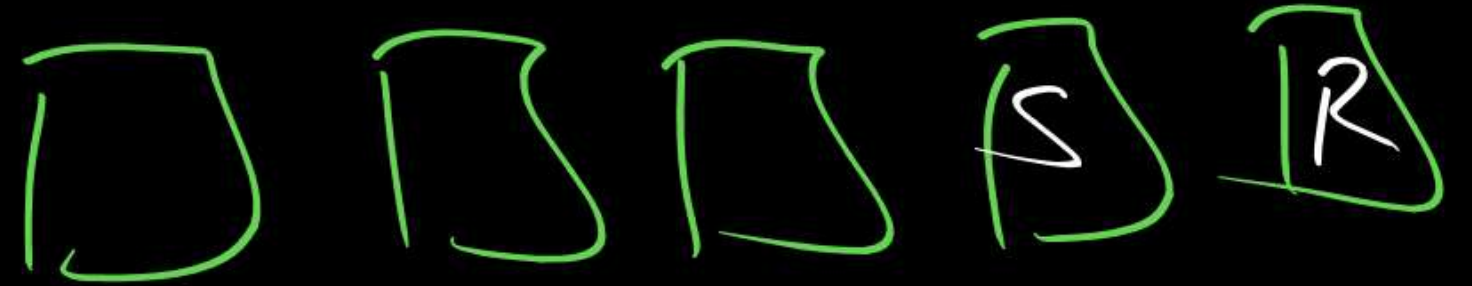
Five different book (P, Q, R, S, T) are to be arranged on a shelf. The books R and S are to be arranged first and second, respectively from the right side of the shelf. The number of different orders in which P, Q and T may be arranged is?



12



2



$$3 \times 2 \times 1$$



120



6

$$= 6$$



Q.

A library has two books each having three copies and three other books each having two copies. In how many ways can all these books be arranged in a shelf so that the copies of the same book are not separated?



A. 80



B. 100



C. 120



D. 140

Assignment ✓



Q. A license plate begins with 3 letters. If the possible letters are A, B, C, D and E, how many different ways these letters can be written if no letter is used more than once?

✓ Assignment

