

Tutorial - 1

Q 1

→ Asymptotic notation is used to describe the running time of an algorithm. Or asymptotic notation tells how much time an algorithm takes to complete wrt the given input.

— Types of asymptotic notations

(a) Big O notation (O)

(b) Big theta notation (Θ)

(c) Big Omega (Ω)

→ Big O → worst case

Big Ω → best case or best running time

Big Θ → used in cases where running time is same in all cases (worst, best) -

Q 2

→ for ($i=1$ to n)
 { $i=i*2$; }

time complexity = $O(\log_2 n)$

as the value of "i" is incremented by a factor of 2

Q 3

$$\rightarrow T(n) = \begin{cases} 3T(n-1) & , n > 0 \\ 1 & \end{cases}$$

Q 4

$$\rightarrow T(n) = \begin{cases} 2T(n-1) - 1 & , n > 0 \\ 1 & \end{cases}$$

Q5 time complexity of:

```
int i=1;
int s=1;
while (s<=n){
    i++;
    s=s+i;
    printf("#");
}
```

→ value of $s \rightarrow 1, 3, 6, 10, \dots, z = n$
 loop executes z times (suppose)
 the final value of s will be n :

$$\frac{z(z+1)}{2} = n$$

$$\frac{z^2+z}{2} = n$$

$$O(\sqrt{n})$$

Q6 complexity of:

```
void func(int n)
{
    int i, count=0;
    for (int i=1; i*i<=n; i++)
        count++;
}
```

→ $O(n)$

Q7

→ time complexity $\rightarrow O(n \log n)$

Q8

time complexity

```

fun(int n)
{
    if (n == 1) return;
    for (i = 1 to n)
        for (j = 1 to n)
            printf("x");
}

```

```

fun(int n)
{
    fun(n - 3);
}

```

T.C = $O(n^2)$

Q9

void fun(int n)

```

{

```

```

    for (i = 1 to n)

```

```

        for (j = 1; j <= n; j++)
            printf("x");
}

```

Time complexity = $O(n^2)$

Q10

$n^k = O(c^n)$