

Assignment - 2

Q1: using namespace std;

```
string search (int arr[], int n, int x)
for (int i = 0; i < n; i++)
{
    if (arr[i] == x)
        return "Found";
    else
        return "Not found";
```

Q2. void sortReverse (int a[], int n)

```
{ if (n <= 1)
    return;
```

```
start Reverse (a, n-1);
```

```
int last = a[n-1];
```

```
int j = n-2;
```

```
while (j >= 0 & a[j] > last)
```

```
{ a[j+1] = a[j];
```

```
j--;
```

```
}
```

```
a[j+1] = last;
```

```
}
```

Iterative

```

void insert (int n) {
    for (i = 1; i < n; i++) {
        int t = a[i];
        int j = i - 1;
        while (j >= 0 && a[j] > t) {
            a[j + 1] = a[j];
            j--;
        }
        a[j + 1] = t;
    }
}

```

Insertion sort considers one input element per iteration and produces a partial solution without considering future elements. Thus insertion sort is an online algorithm.

Other sorting algorithms are →

- ✓ Inplace sorting algorithm - That do not take any extra space
- ✓ Stable sorting algorithm - When the relative order of equal elements do not

change after sorting

- ✓ External sorting algorithm → those algorithms that can handle maximum amount of data when the data being sorted does not fit into the main memory
- ✓ Internal sorting Algorithm → opposite to the External sorting algorithm here main memory is required and no external memory is there.

3. ✓ ~~Linear Search~~ Bubble sort → Time Complexity $\rightarrow O(N^2)$ for all cases
Space complexity $\rightarrow O(1)$

✓ Selection sort → Time complexity $\rightarrow O(N^2)$ for all cases
Space complexity = $O(1)$

✓ Insertion sort → Time complexity = $O(N^2)$ for worst cases
Space complexity = $O(1)$

✓ Count sort - Time complexity $\rightarrow O(N+K)$
 Space complexity $\rightarrow O(n+k)$

✓ Quick sort - Time complexity $\rightarrow O(n \log n)$ - Best/Avg
 $O(n^2)$ - Worst
 Space complexity $\rightarrow O(n \log n)$

✓ Mergesort - Time complexity $\rightarrow O(n \log n)$ - All case
 Space complexity $\rightarrow O(n)$

✓ Heapsort \rightarrow Time complexity $\rightarrow O(n \log n)$ - All cas
 Space complexity $\rightarrow O(1)$

Q4: Inplace sorting Algorithm

- Bubble sort
- Selection sort
- Insertion sort
- Quick sort
- Heap sort

Stable Sorting Algo

- Insertion sort
- Merge sort

Online sorting Algorithm

→ Insertion sort .

Binary (int array[], int target, low; high)
 if low > high:
 return Not found

$$\text{mid} = (\text{low} + \text{high}) / 2$$

if (array[mid] == target) :
 return mid .

else if (array[mid] > target) :

return binary (array, target, low, mid)

else :

return binary (array, target, mid + 1, high)

Iterative .

binary (int a[], int target) :

$$\text{low} = 0$$

$$\text{high} = \text{length}(\text{array}) - 1;$$

while low <= high :

$$\text{mid} = (\text{low} + \text{high}) / 2$$

if a[mid] == target :

between mid;
else if ($a[\text{mid}] < \text{target}$)
 low = mid + 1;

else
 high = mid - 1;

return Not found.

Time complexity $\rightarrow O(\log n)$] Binary
Space complexity $\geq O(1)$] search.

Time complexity = $O(n^2)$] linear
space complexity = $O(1)$] search.

Q6. $T(n) = T(n/2) + 1$.

Q6. Quick sort is the best for practical use.

9.

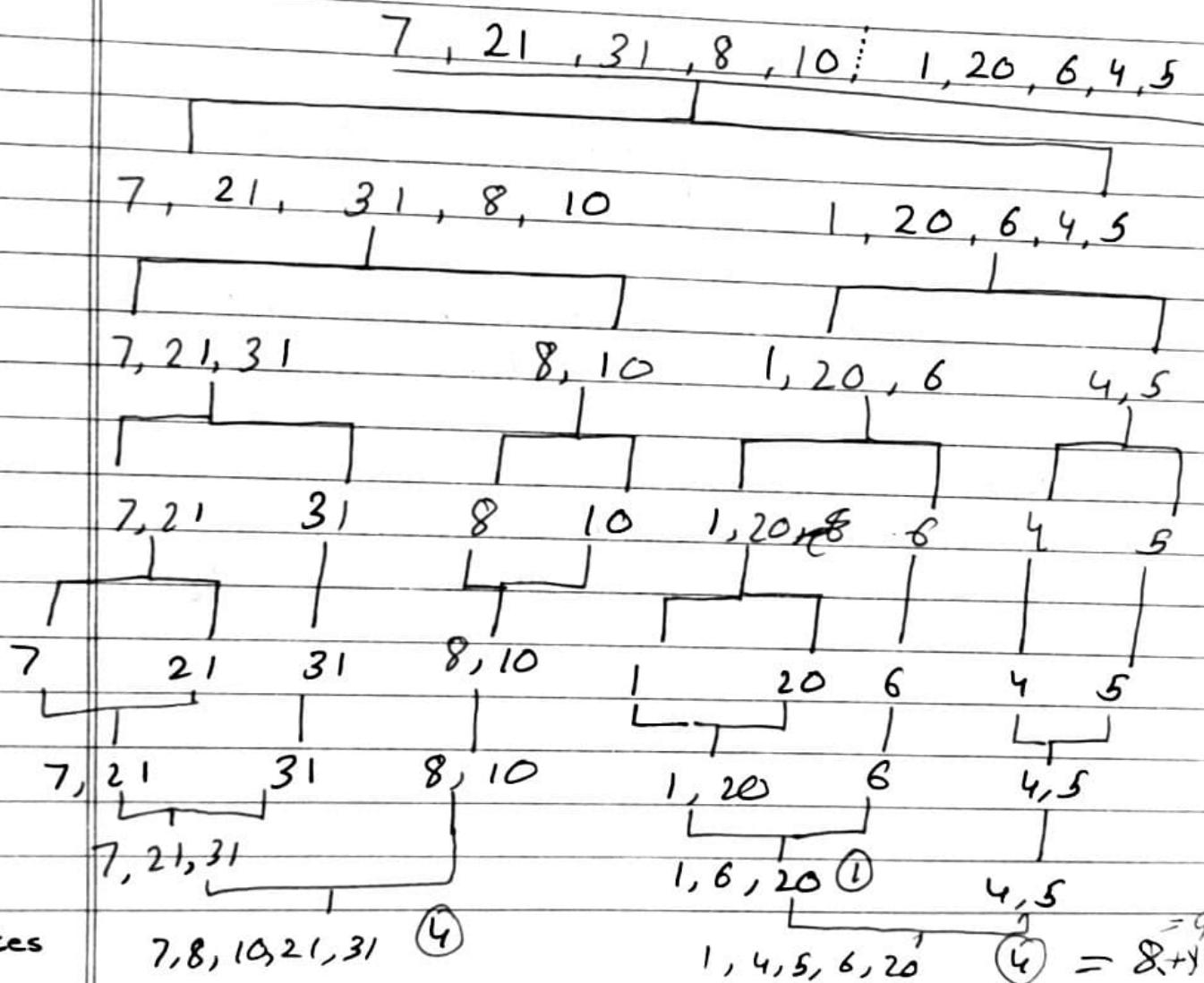
Inversions

Number of inversion means how many element is shifted before placing new element at its prescribed location.

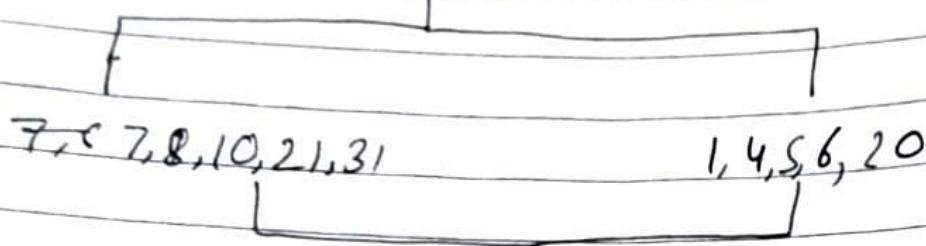
for eg →

~~1, 2, 7, 10, 12, 13~~ has to accomodate 4

1, 2, 4, 7, 10, 12, 13 — inversion = 4

Merge Sort

last ↴



$$1, 4, 5, 7, 8, 10, 20, 21, 31 \rightarrow 5 + 5 + 5 + 2 = 17$$

$$\text{Total} = 17 + 9 = 26$$

10. Quick Sort

Best $\rightarrow O(n \log n)$ ↴

Condition \rightarrow pivot is exactly the middle element

Worst $\rightarrow O(n^2)$ ↴

Condition \rightarrow pivot is either first or last element.

Average $\rightarrow O(n \log n)$ ↴

Condition \rightarrow Array is roughly divided in equally half subarrays

12. S Table Quick Sort

```
void SQS(vector<pair<int, int> &arr) {
    /* first element holds value second holds
       occurrence */
    int n = arr.size() - 1;

    for (int i = 0; i < n; i++) {
        int min_idx = i;
        for (int j = i + 1; j < n; j++) {
            if (arr[j].first < arr[min_idx].first)
                min_idx = j;
        }

        pair<int, int> key = arr[min_idx];
        while (min_idx > i) {
            arr[min_idx] = arr[min_idx - 1];
            min_idx--;
        }

        arr[i] = key;
    }
}
```

13.

Bubble sort without scanning whole array -

~~Beside double check loop we can use single loop in which one element is at i position and others is at $i+1$. if $a[i] < a[i+1]$ then go for next comparison if not then call bubble sort for i to n indices.~~

Comparison Code

```
void bs(int a[], int l, int u) {
    if (l
```

13. Bubble sort after sorting -

This can be achieved by pairing element with boolean data type. if it is sorted then it will store true else false. If true is found at 0^{th} index break the condition and come out else iterate for bubble sort.

Code

```
void bs(&vector<int, bool>& arr) {
    int n = arr.size() - 1;
```

```

for(i=0; i<n; i++)
{
    if (arr[0].second == true)
        break;
    else
    {
        for(j=i+1; j<n; j++)
            if (arr[j] < arr[i])
            {
                Swap(i, j);
                Swap(arr, i, j);
            }
    }
}
arr[0].second = true; // after first call turns arr[0] true.

```

Note ** → if array is of size n , i.e $n \geq n$
 & then if a element is added after sorting
 array will ~~be~~ not able to sort again.
 to achieve capability to sort again, while
 including a element change $\text{arr}[0].\text{second}$ to
 false again.

Merging of data greater than available memory

We can't sort data of 4GB in 2GB memory to do so we have to use External Sorting methods like External merge sort or External quick sort.

~~St~~

External Sorting → It is sorting in which data is sorted and stored in slower memory for a while. Then it is retrieved from file to sort with other data. This chunking of data allows us to sort large data with less resource usage.

Internal Sorting → It is sorting in which less memory is directly used and no secondary memory is used. It can only accommodate chunk smaller than available memory.

Speed Comparison

Internal > ~~External~~ external

Storage can be sorted

External > internal