

Data Structure Using C

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Data Structure Using C

Topic:

Introduction To Data Structure

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INTRODUCTION TO DATA STRUCTURE:

Computer Science is the study of data, its representation and transformation by computer. For every data object, we consider the class of operations to be performed and then the way to represent the object so that these operations may be efficiently carried out. The two techniques required for this is :-

1) Devise alternative forms of data representation.

2) Analyze the algorithm which operates on the structure.

These includes data structures, data types and data representations.

Data :

- Data are simply values or set of values. data items refers to a single unit of values. By data we mean known facts that can be recorded and that help implicit meaning.

Datatype and its necessity :

- A datatype is a term which refers to the kind of data that a variable may hold. Every programming language has some built-in datatypes. This means that the language allows variables to name data of that type and provides a set of operations which meaningfully manipulate these variables.
- If an application needs to use a datatype other than the primitive datatypes of the language i.e. a datatype for which values and operations are not defined in the language itself, then it is programmer's responsibility to specify the values and operations for that datatype and implement it.

Abstract Data type :

- Abstract data type is a mathematical model or concept that defines a datatype logically. It specifies a set of data and collection of operations that can be performed on that data. This definition of ADT only mentions what operations are to be performed but not how these operations will be implemented. It does not specify how data will be organized in memory and what algorithms will be used for



implementing the operations. It is called abstract because it gives an implementation development view. The process of providing only the essentials and hiding the details is known as abstraction.

Data Structures :

1. The logical or mathematical model of a particular organization of data is called a data structure. Data structure is a programming construct used to implement an ADT. It is the physical implementation of ADT.
2. A data structure that is implementing an ADT consists of collection of variables for storing the data specified in the ADT and the algorithms for implementing the operations specified in ADT. Data structure is the actual representation of data and the algorithms to manipulate the data.

TYPES OF DATA STRUCTURES:

- 1. Data Structures are broadly classified into two categories.
 - a) Primitive (using basic datatypes)
 - b) Non Primitive (using derived datatype or user defined datatype).

a) Primitive Data Structures:

- The Primitive data structures are typically those data structures that directly operated upon the fundamental data types. e.g. int, char etc in case of 'C' language. So, the data structures that use primary datatype is of primitive type.

b) Non Primitive Data Structures:

- The data structures operated upon derived or user defined datatype is non primitive type. Non-primitive data structures can be represented in two categories.
 - i.e:- a) Linear type (Array, Linked List, Stack and Queues)
 - b) Non Linear type (Tree, Graph, Hash Table, Sets).

a) Linear Data Structures:

1. A data structure is said to be linear if its elements form a sequence or linear list, or a data structure which allows representing the data in sequential order and allows the operations accordingly, is of linear type. A list which shows the relationship of adjacency between elements is said to be linear data structure.
2. The linear data structures are, array, linked list, stack and queue. There are two basic ways of representing such linear structure in memory. i.e:- i) array and ii) linked list.
3. The linear relationship between the elements represented by means of sequential memory location. These linear structures are called array.
4. The linear relationship between the elements represented by means of pointer or links are called linked list.

Eg:- Suppose a table contains customers name and his/her sales person.

	Customer	Sales Person
1.	A	SMITH
2.	B	RAY
3.	C	JONES
4.	D	RAY
5.	E	SMITH
6.	F	JONES
7.	G	RAY

Figure - 1.

	Customer	Link	Sales Person
1.	A	3	JONE
2.	B	2	RAY
3.	C	1	SMITH
4.	D	2	
5.	E	3	
6.	F	1	
7.	G	2	

Figure - 2



	Customer	Link	Sales Person
1.	A	5	JONE
2.	B	4	RAY
3.	C	6	SMITH
4.	D	7	
5.	E	8	
6.	F	0	
7.	G	0	

Figure - 3 - Linked list representation

5. Stack is the last-in-first-out (LIFO) linear list in which insertion and deletion can take place only one end called top of the stack.



stack of dishes

New dishes are inserted only at the top of the stack and dishes can be deleted only from the top of the stack.

6. Queue is a first-in-first-out (FIFO) linear list in which deletion can take place only at one end of the list which is called front and the insertion can take place only at other end of the list called rear end.

Eg:- The first person in line is the first person to board the bus,

b. Non-Linear Data Structure:

- i. The data structure represented in non-sequential order is of non-linear type. The data structure that comes under non-linear type are trees and graphs.

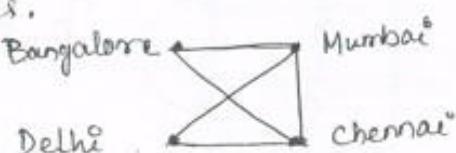
2. In tree, data frequently contains hierarchical relationship between the various elements. It consists of a special element called root and from root many elements are connected like branches, sub-branches and so on, upto leaf.

Eg:- Employee



3. Graph:- In Graph, data sometimes containing a relationship between pairs of elements, which is not necessarily hierarchical in nature. It maintains the random relationship between various elements.

Eg:- Suppose an airline flies, only between cities connected by lines.



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Algorithm:

1. An algorithm is any well formed defined computational procedure that takes set of values as input and produces set of values as output.
2. A well defined set of instructions to solve a particular problem in finite number of steps is called Algorithm.

Characteristics of Algorithm:

1. Every algorithm should have the following characteristics, i.e.
 - i) Input: Every algorithm should take zero or more input.
 - ii) Output: Every algorithm must yield at least one output.
 - iii) Definiteness: Every step of an algorithm should be very clear and unambiguous.
- iv) Finiteness: Every algorithm must end with a finite number of steps, i.e. Every algorithm must have countable numbers of steps.
- v) Effectiveness: The steps present in the algorithm should be such that one can implement it by taking the help of pen and paper.

Analyzing an algorithm:

1. Analysing of an algorithm means predicting resources that the algorithm requires. Resources such as:- memory, logic, gets etc. But most often analysing an algorithm is an computational time that we want to resource. The Space needed by each of these algorithm is seen to be the sum of the following components.

- a) A fixed part: It is independent of input and output, which includes the space for code, simple variable etc.
Eg:- Algorithm Rsum(a, n)
if $n \leq 0$ then return 0.0;
else
return Rsum(a, n-1) + a[n];

In fixed part, the space needed to store the program, variable 'n' always take fixed byte and 'a' is the array.



b) A Variable Part: It consist of the space needed by reference variable and recursion stack space.

Eg:- Suppose $a[5]$ is an array, then take $a[1] = 4, a[2] = 10, a[3] = 2, a[4] = 5, a[5] = 1$.

$Rsum(a, 5)$

\downarrow
 $Rsum(a, 4) + 1$

\downarrow
 $Rsum(a, 3) + 5$

\downarrow
 $Rsum(a, 2) + 20$

\downarrow
 $Rsum(a, 1) + 40$

\downarrow
 $Rsum(a, 0) + 4$

4
10
2
5
1

$$\begin{aligned} 4 + 10 &= 14 + 2 = 16 + 5 \\ &= 21 + 1 = 22 \end{aligned}$$

The time $T(p)$ taken by a program p is the sum of the compile time and the run time. But compile time is fixed for a program and run time is varient.

2. Once an algorithm is designed, there are two issue which are to be properly dealt with. One issue is validation of the algorithm that means whether the algorithm is valid or not and the other issue is evaluating the complexity of the algorithm.
3. It is necessary to show that designed algorithm yields correct output for all possible combination of input values. This is also called "program proving" or "program verification".
4. One important topic in the study of algorithms is to determine the amount of time and storage it may require for execution. These results are useful for comparing algorithms and predicting the performance of the algorithm in the best, worst and average case.
5. When a program is run on a computer, two of the most important considerations are:-
 - ii) Time Complexity
 - ii) Space Complexity.

Criteria for developing an algorithm:

1. It should correctly work under all possible conditions.
2. It should solve the problem according to the given conditions.
3. It should be clearly written by following the top down strategy.
4. It should be efficient to use the time and resources.
5. It should have sufficient documentation so that any one can understand it.
6. It should be easy to modify.
7. It should be independent of running on a particular computer.

Best Case and Average Case:

1. The Best case time complexity is the minimum amount of time that can required by an algorithm for an input of size n . Thus, it is the function defined by the minimum no. of steps taken on any instant of size n .
2. The Worst case time complexity is the function defined by the maximum amount of the time needed by an algorithm for an input size n .
3. The average case time complexity is the education of an algorithm having typical input data of size n , Thus it is the function defined by the minimum no. of steps taken on array instance of size n ,

Eq:- $\text{Sum}(a, n)$

$$\begin{aligned}
 & \left\{ \begin{array}{l} s=0; \\ \text{for } (i=1 \text{ to } n) \end{array} \right. - \Theta(1) \\
 & \quad \left\{ \begin{array}{l} s=s+a[i]; \\ \text{return } s; \end{array} \right. - n+1 \\
 & \quad \left. \begin{array}{l} \\ \end{array} \right. - n \\
 & \quad \left. \begin{array}{l} \\ \end{array} \right. - 1 \\
 & \quad \left. \begin{array}{l} \\ \end{array} \right. \hline
 & \quad \left. \begin{array}{l} \\ \end{array} \right. 2n + 3
 \end{aligned}$$



Asymptotic Notation:

1. The Notation, which we use to describe the asymptotic running time of an algorithm are defined in terms of functions, whose domains are the set of natural numbers and real numbers.

i) The Natural number set is denoted as:-

$$N = \{0, 1, 2, \dots\}$$

v) The positive integers set is denoted as :-

$$\mathbb{N}^+ = \{1, 2, 3, \dots\}$$

w) The real numbers set is denoted as \mathbb{R} .

x) The positive real numbers set is denoted as \mathbb{R}^+ .

y) The non-negative real set is denoted as \mathbb{R}^* .

2. The different types of notations are :-

v) Big oh (O) notation

w) Small oh (o) notation.

x) Big omega (Ω) notation.

y) Small omega (ω) notation.

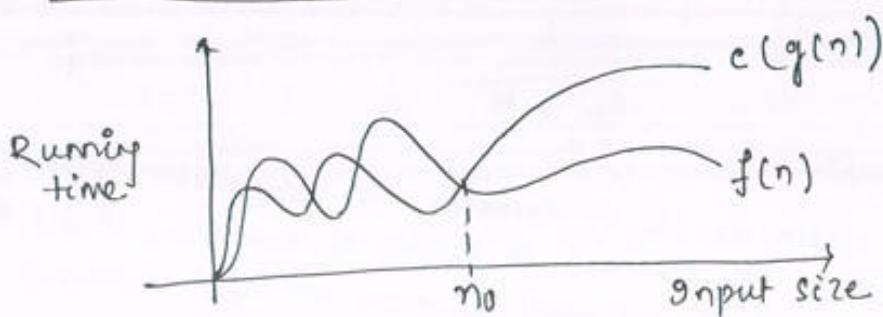
z) Theta (Θ) notation.

v) Big Oh (O) Notation :

1. The upper bound for the function is provided by the Big oh (O) notation. We can say, the running time of an algorithm $O(g(n))$, if whenever input size is equal to or exceeds, some threshold n_0 , its running time can be bounded by some positive constant c time $g(n)$.

2. Let $f(n)$ and $g(n)$ are two functions from set of natural numbers to set of non-negative real numbers and $f(n) \leq g(n)$ is said to be $O(g(n))$. That is, $f(n) = O(g(n))$, iff \exists a natural number n_0 and a positive constants $c > 0$, such that

$$f(n) \leq c(g(n)), \forall n > n_0$$



examples :-

1. $f(n) = 2n^2 + 7n - 10$
 $\Rightarrow f(n) = O(g(n))$, where $g(n) = n^2$

if $n=5, c=3$

$$\Rightarrow f(n) \leq c(g(n)) \Rightarrow 2n^2 + 7n - 10 \leq cn^2$$

$$\Rightarrow 2 \times 25 + 7 \times 5 - 10 \leq 3 \times 25 \Rightarrow 50 + 35 - 10 \leq 75$$

$$\Rightarrow 75 \leq 75.$$

So, it is $O(g(n)) = O(n^2)$.

if $n=4, c=3$

$$\Rightarrow f(n) \leq c(g(n)) \Rightarrow 2n^2 + 7n - 10 \leq cn^2$$

$$\Rightarrow 2 \times 16 + 7 \times 4 - 10 \leq 3 \times 16 \Rightarrow 32 + 28 - 10 \leq 48 \Rightarrow 50 \leq 48$$

So, it is not in $O(g(n))$

if $n=6, c=3$

$$\Rightarrow f(n) \leq c(g(n)) \Rightarrow 2n^2 + 7n - 10 \leq cn^2$$

$$\Rightarrow 2 \times 36 + 7 \times 6 - 10 \leq 3 \times 36 \Rightarrow 72 + 42 - 10 \leq 108$$

$$\Rightarrow 114 - 10 \leq 108 \Rightarrow 104 \leq 108.$$

So, $f(n) = O(g(n)) = O(n^2)$.

2. if $3n+2 = O(g(n))$

Here $f(n) = 3n+2$

$$3n+2 \leq c*n.$$

$$3n+2 \leq 4*n (\because c=4)$$

if $n=2$, then $6+2 \leq 8 \Rightarrow 8 \leq 8$.

So, $3n+2 = O(n)$, for $n \geq 2$.

if $10n^2 + 4n + 2 = O(g(n))$

$$10n^2 + 4n + 2 \leq c*n^2$$

$$\text{let } c=11, 10n^2 + 4n + 2 \leq 11*n^2$$

$$\text{if } n=5, 10 \times 25 + 4 \times 5 + 2 \leq 11 \times 25$$

$$= 250 + 20 + 2 \leq 275$$

$$= 272 \leq 275. \text{ So } 10n^2 + 4n + 2 = O(n^2), n \leq 5.$$





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3. $O(1)$ = A computing time ie:- constant.

$O(n)$ = linear

$O(n^2)$ = Quadratic

$O(n^3)$ = Cubic

$O(2^n)$ = Exponential

Several computing times in decreasing order

i.e:- $O(1), O(\log n), O(n), O(n \log n), O(n^2), O(n^3), O(2^n)$.

4. Small oh (\mathcal{O}) Notation:

- The functions in small oh (\mathcal{O}) notation are the smaller function in Big oh (\mathcal{O}) notation. We use small oh (\mathcal{O}) notation to denote an upper bound that is not asymptotically tight. This notation is defined as :- $f(n) = O(g(n))$ iff \exists any positive constant $c > 0$ and $n_0 > 0$, such that $f(n) \leq c(g(n)), \forall n > n_0$

- The definition of \mathcal{O} -notation and \mathcal{o} -notation are similar. The main difference is that in $f(n) = O(g(n))$, the bound $f(n) \leq c(g(n))$, holds for some constant $c > 0$, but in $f(n) = o(g(n))$, the bound $f(n) < c(g(n))$ hold for all constant $c > 0$.

- In this notation, the function $f(n)$ becomes insignificant relative to $g(n)$ as n approaches infinity.

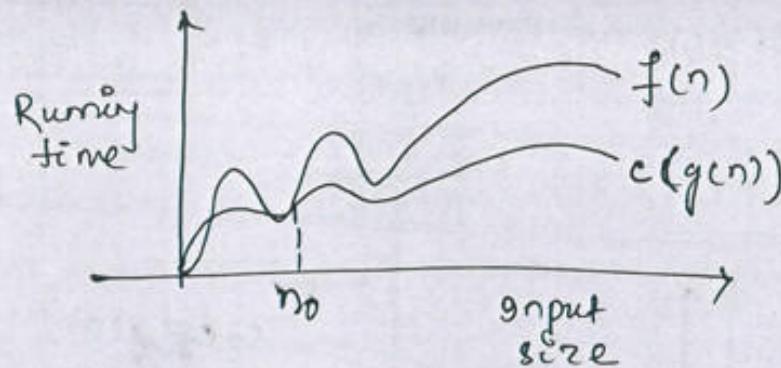
$$\text{i.e.} - \lim_{n \rightarrow \infty} \frac{f(n)}{g(n)} = 0$$

5. Big Omega (Ω) Notation:

- The lower bound for the function is provided by Big Omega (Ω) Notation. We can say, the running time of an algorithm $\Omega(g(n))$, if whenever input size is equal to or exceeds some thresholds value n_0 , its running time can be denoted by some positive constant 'c' times $g(n)$.

2. Let $f(n)$ and $g(n)$ are 2 functions from set of natural numbers to set of non-negative real numbers and $f(n)$ said to be $\Omega(g(n))$, i.e. $[f(n) \geq c_2 g(n)]$, iff \exists a natural number n_0 and a constant $c_2 > 0$, such that

$$[f(n) \geq c_2 g(n), \forall n \geq n_0]$$



Example:

$f(n) = n^2 + 3n + 4 \Rightarrow f(n) = \Omega(g(n))$, where $g(n) = n^2$
 let $c=1, n=1 \Rightarrow f(n) \geq c(g(n))$
 $\Rightarrow n^2 + 3n + 4 \geq n^2 \Rightarrow 1 + 3 + 4 \geq 1 \Rightarrow 8 \geq 1$
 $\Rightarrow f(n) = \Omega(g(n))$ (proved)



Ques) Small omega (w) Notation:

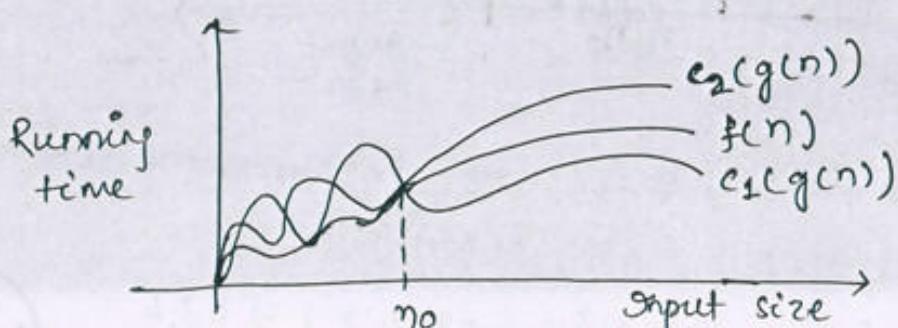
1. The function small omega (w) notation are the larger functions of Big omega (Ω) Notation. We use a notation to denote a lower bound that is not asymptotically tight, we define this notation as: $[f(n) = w(g(n))] \exists$ some positive constant $c > 0$ and $n_0 > 0$, such that $[f(n) \geq c(g(n)), \forall n \geq n_0]$.
 The relation $f(n) = w(g(n))$ implies that $\lim_{n \rightarrow \infty} \frac{f(n)}{g(n)} = \infty$

Ans) Theta (Θ) Notation:

1. For a given function $g(n)$ we denote by $\Theta(g(n))$, the set of functions $[f(n) = \Theta(g(n))]$, iff \exists some constant c_1, c_2 and n_0 such that $[c_1(g(n)) \leq f(n) \leq c_2(g(n)), \forall n \geq n_0]$

2. For all values of n to the right of n_0 , the values of $f(n)$ lie at or above $c_1(g(n))$ and at or below $c_2(g(n))$. In other words, $\forall n \geq n_0$, the function $f(n)$ is equal to $g(n)$ to within a constant factor. We say that $g(n)$ is asymptotically tight bound for $f(n)$.
3. The definition of $\Theta(g(n))$ requires that every member $f(n) \in \Theta(g(n))$ be asymptotically non-negative. i.e. that $f(n)$ be non-negative whenever n is sufficiently large.

$$\text{So, } f(n) = \Theta(g(n)) \Rightarrow \lim_{n \rightarrow \infty} \frac{f(n)}{g(n)} = \text{constant } c$$



Example:-

$$f(n) = 3n + 2$$

$$c_1(g(n)) \leq 3n + 2$$

$$\text{let } c_1 = 3, 3n \leq 3n + 2$$

$$\text{if } n=2, \text{ then } 3 \times 2 \leq 3 \times 2 + 2 \Rightarrow 6 \leq 8.$$

$$\therefore 3n \leq 3n + 2, n \leq 2,$$

$$3n + 2 \leq c_2(g(n))$$

$$3n + 2 \leq 4 \times n \quad (\because c_2 = 4)$$

$$\text{if } n=2, \text{ then } 3 \times 2 + 2 \leq 4 \times 2 \Rightarrow 8 \leq 8.$$

$$\therefore 3n + 2 \leq 4 \times n, n \leq 2.$$

Array:

1. An array is a collection of similar data elements present in continuous memory locations referred by a unique name. The datatype of the elements may be any valid datatype like char, int or float. The elements of array share the same variable name, but each element has a different index number known as subscript.
2. An array can be one dimensional array, two dimensional array and multidimensional array. Two dimensional array has 2 subscripts one for row and other one for column. It is also called matrix.

One dimensional array:

1. An array is defined as :-

datatype arrayname [size];

which has one subscript.

Eg:- int a[5];

The initialization of the array is :-

i) int a[5] = {1, 2, 3, 4, 5};

ii) int a[] = {1, 2, 3, 4, 5}.

2. A linear array is a list of a finite number 'n' of homogeneous data elements, such that
 - i) The elements of the array are referenced respectively by an index set consisting of 'n' consecutive numbers.
 - ii) The elements of the array are stored respectively in successive memory location.
3. The number 'n' of elements is called the length or size of the array. The length of an array can be obtained from the index by the formula:-

$$\boxed{\text{Length} = \text{Upperbound (UB)} - \text{Lowerbound (LB)} + 1}$$

where UB = Largest index called upper bound.

LB = Smallest index called lower bound

When lowerbound = 1, then $\boxed{\text{Length} = \text{Upperbound (UB)}} |$

Eg:-

3	5	6	7	9	10
0	1	2	3	4	5
(LB)					

 $\text{Length} = \text{UB} - \text{LB} + 1 = 5 - 0 + 1 = 6.$



Representation of Linear array in Memory / finding Address of an element in an 1-D array :

- Let 'LA' be a linear array in the memory of the computer.
- $\text{LOC(LA}[K]\text{)} = \text{Address of the element } LA[K]$ of the array LA.
- Base(LA) called the base address of the array LA. Elements of 'LA' are stored in successive memory cells. So, we need to keep track of the address of the 1st element of the array LA, which is the Base(LA) .
- Using this base address, the computer calculate the address of any element of 'LA' by the following formula :-

$$\text{LOC(LA}[K]\text{)} = \text{Base(LA)} + W(K - LB)$$

where $W = \text{no. of words per memory cell for an array LA.}$
or $\text{Size/Width of each element.}$

A[10]	0	1	2	3	4	K	6	7	8	9
5	9	2	11	3	8	7	6	4	1	
101	103	105	107	109	111	113	115	117	119	UB

Hence, base address $\text{Base(LA)} = 101$.

Lowerbound (LB) = 0, Upperbound (UB) = 9.

Size/Width of each element $W = 2 \text{ bytes}$,

'K' is the position = 5

So, Address of an element with index K :-

$$\begin{aligned} \text{Loc(LA}[K]\text{)} &= \text{Base(LA)} + W(K - LB) \\ &= 101 + 2 \times (5 - 0) \\ &= 111. \end{aligned}$$

So Address of $LA[5] = 111$,

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Operation on Data Structure:

- i) The operation performed on any linear structure whether it be an array or linked list include the following.
- ii) Creation : Creation of new data structures by considering a set of data.
- iii) Insertion : Adding a new data at various positions of existing data structure.
- iv) Deletion : Deleting an existing data from the data structure.
- v) Search : finding the existence and location of the elements with a given value or the records with a given key.
- vi) Traversal : Visiting each field present in the data structure exactly once for certain processing purpose.
- vii) Sorting : Arranging the data or records or elements in a particular order.
- viii) Merging : Joining or combining of records from multiple data structures to produce a single file in sorted order.

Memory Representation Data Structures:

- i) Any data structure can be represented in two ways in the memory, i.e. by Sequential representation and by linked representation.
- ii) Sequential Representation:
 - A sequential representation maintains the data in continuous memory locations which takes less time to retrieve the data but leads to time complexity during insertion and deletion operations. The major drawback of this is it takes much time for insertion and deletion operations unnecessarily and increasing the complexity of algorithm.
- iii) Linked Representation:
 - It maintains the list by means of a link or a pointer between the adjacent elements which need not be stored in continuous memory locations. During insertion and deletion operations, link will be created or removed between the elements which takes less time when compared to the corresponding operations of sequential representation. It takes more memory space, which is the drawback of this.



Entity :

1. An entity is a thing or object in the real world that is distinguishable from all other objects.
Eg:- Each person in an enterprise is an entity.
2. An entity is represented by a set of attributes.
3. An entity set is a set of entities of the same type that share the same properties or attributes.
Eg:- The set of all persons who are customers of a given bank can be defined as the entity set customer.
4. Each entity has a value for each of its attributes.
Eg:- 123 for customer ID is the attributes of the entity set.
5. For each attribute there is a set of permitted values called the domain or value set of the entity set.

Information :

1. Data with given attributes or meaningful and processed data is known as information. Field is the single elementary unit of information representing an attribute of an entity.

Record :

1. It is the collection of field values of a given entity.

File :

1. It is the collection of records of the entity in a given entity set.

Space Complexity and Time Complexity :

1. Space Complexity of an algorithm is the amount of memory, it needs to run to completion.
2. The time complexity of an algorithm is the amount of computer time, it needs to run to completion.



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Data Structure Using C

Topic:
Operations On Array

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Operations on One Dimensional Array :-

1. The operations on one dimensional array are :-

- i) Creation : Create or entering elements into array
- ii) Traversal : Processing each element
- iii) Search : Searching for an element.
- iv) Insertion : Inserting an element at required position.
- v) Deletion : Deletion of an element.

vi) Sorting : Arranging in ascending or descending order

vii) Merging : It is done in two ways

- a) Join/concatenate two ways into 3rd array and then sort.
- b) Merge directly into 3rd array where two arrays are already sorted.

viii) Creation of an array :-

Algorithm :-

CREATE(LA, LB, UB)

Step 1 : Let LA[10], LB, UB, K

Step 2 : LB := 1, UB := 10

Step 3 : Display "Enter 10 Elements"

Step 4 : Repeat, for K := LB to UB incremented by 1

 INPUT LA[K]

[End of For]

Step 5 : Exit..

The 'C' function for this is :-

/* assume LB and UB are declared as global variables */

Void CREATION(int LA[])

{

 Ent K;

 printf("Enter elements into array");

 for(K = LB; K <= UB; K++)

 scanf("%d", &LA[K]);

}



^Q Traversing an array:

Algorithm:

TRAVERSE (LA, LB, UB)

Step 1: Repeat for $K := LB$ to UB by 1
Apply PROCESS to $LA[K]$

[End of For]

Step 2: Exit.

Hence, PROCESS can be visiting each element and do calculation on it. In C language LB is 0 by default and UB is Last position of array.

The 'C' function for Traversing a linear array:-

/* UB representing Upper Bound or declared as global */
Void Traverse (int LA[])

```
{ int K;
for (K = LB; K <= UB; K++)
    {
        printf ("%d", LA[K]);
    }
}
```

^Q Searching for an element in an array:

Algorithm:

SEARCH (LA, LB, UB, ITEM)

Step 1: Let K, Set $K := LB$

Step 2: Repeat, while ($K \leq UB$)

Step 2.1: If $LA[K] = ITEM$, Then

Display "Item Found at", K

[End of if]

Step 2.2: Set $K := K + 1$

[End of While]

Step 3: Exit

The 'C'-function for this is :-

```

void search (int LA[], int ITEM)
{
    int K = 0;
    for (K = LB; K <= UB; K++)
    {
        if (LA[K] == ITEM)
        {
            printf ("Item found at %d", K);
        }
    }
}

```

Q) Insertion of new element in an array :-

1. Inserting an element at the end of the linear array can be easily done, provided the memory space allocated for the array is large enough to accomodate the additional element.
2. If we insert an element in the middle of the array, then on the average half of the element must be moved downward to new location to accomodate the new element and give the order of the other elements.

Algorithm:

INSERTION(LA, LB, UB, ITEM, POS)

Step 1: Set K

Step 2: Repeat, for $K := UB$ to POS, decreasing by 1
 $LA[K+1] := LA[K]$

[End of For]

Step 3: $LA[POS] := ITEM$

Step 4: Set $UB := UB + 1$.

Step 5: EXIT

The 'C'-function for this is :-

```

void insertion (int LA[], int ITEM, int POS)

```

```

{
    int K;
    for (K = UB; K = POS; K--)
    {
        LA[K+1] = LA[K];
    }
    LA[POS] = ITEM;
    UB + 1;
}

```



Deletion of an element from an array:

1. Deletion of an element in the middle of the array or somewhere at the array would required that each subsequent element be moved one location upward in order to fill up the array.

Algorithm:

1. Deletion of an element when the position is given is:-

DELETION-POS (LA, LB, UB, POS)

Step 1: Let K

Step 2: Repeat for $K := \text{POS}$ to UB incremented by 1.
 $LA[K] := LA[K+1]$

[End of For]

Step 3: $UB := UB - 1$

Step 3: Exit

The C-function for this is:-

void DELETION-POS(int LA[], int POS)

{ int K;

for ($K = \text{POS}; K <= \text{UB}; K++$)

{ $LA[K] := LA[K+1];$

}

$UB--;$

}

2. Deletion of an element when the item is given,

DELETION-ITEM (LA, LB, UB, ITEM)

Step 1: Let $K, S = 0, T$

Step 2: Repeat for $K := LB$ to UB incremented by 1.

Step 2.1: If ($LA[K] = \text{ITEM}$), Then

Step 2.1.1: Display "Item found at", K.

Step 2.1.2: Repeat for $T := K$ to UB , incremented by 1

Step 2.1.2.1: $LA[T] := LA[T+1]$

[End of For]

Step 2.1.3: $UB := UB - 1$.

Step 2.1.4: $S = 1$

[End of If]

Step 3: [End of For]

Step 3: If ($S = 0$), Then

Step 3.1: Display "Item to be deleted is not found".

Step 4: [End of If]

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The 'C'-function for this is :-

```
void DELETION-ITEM (int LA[], int ITEM)
{
    int K, S = 0, T;
    for (K = LB; K <= UB; K++)
    {
        if (LA[K] == ITEM)
        {
            printf ("Item found at %d", K);
            for (T = K; T <= UB; T++)
            {
                LA[T] = LA[T + 1];
            }
            UB--;
            S = 1;
        }
        if (S == 0)
        {
            printf ("Item to be deleted is not found");
        }
    }
}
```

Sorting the elements of an array:

Algorithm:

SORTING (LA, LB, UB)

Step 1: Let I, J, K, T

Step 2: Set I := 1, J := 2.

Step 3: Repeat for K := UB - 1 to 1 by decrementing by 1.

Step 3.1: Repeat for I := 1, J := 2 to K by 1.

Step 3.1.1: If LA[I] > LA[J], then

T := LA[I]
LA[I] := LA[J]
LA[J] := T

Step 4: Exit
[End of FOR]
[End of IF]



The C-function for this is :-

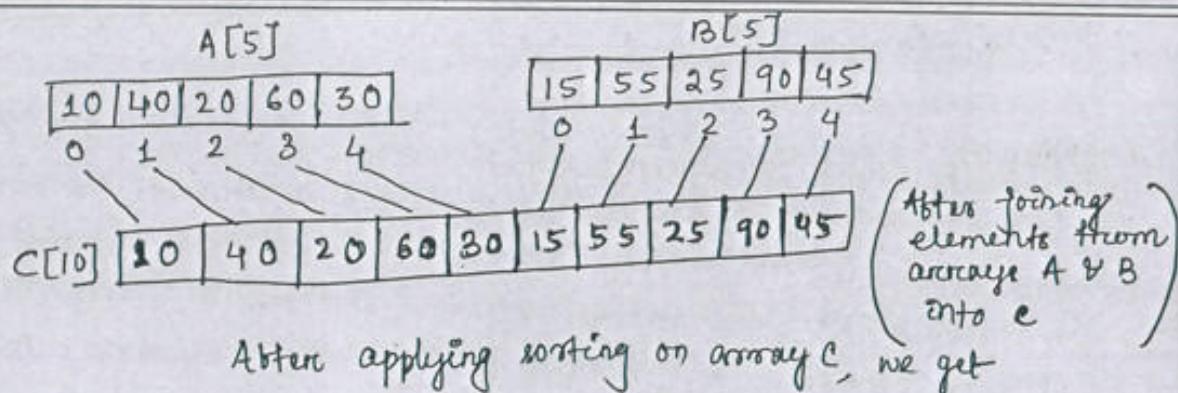
```

void SORTING(Ent LA[ ] )
{
    int I, J, K, T;
    for (K = UB - 1; K > 0, K--)
    {
        for (I = 0, J = 1; J <= K; I++, J++)
        {
            if (LA[I] > LA[J])
            {
                T = LA[I];
                LA[I] = LA[J];
                LA[J] = T;
            }
        }
    }
}

```

Merging of Two Arrays:

1. Merging means storing the elements of two or more arrays together into 3rd array in sorted array. It is an operation when we need to compact the elements from two different arrays into a single array.
2. Merging is possible in two ways. That is :-
 - (i) when the elements of two arrays given are in unsorted manner.
 - (ii) when the elements of two arrays given are in sorted manner.
3. When the elements of two arrays given are in unsorted manner :
 Hence we need to join the elements of both the arrays into 3rd array and then apply sorting method to the 3rd array or resultant array.
4. Let us consider A[5] contains {10, 40, 20, 60, 30} and B[5] contains {15, 55, 25, 90, 45}.
 Assuming C[10] is the resultant array, we need to join all the elements of array A and B together to store in third array. i.e C[10] now contains {10, 40, 20, 60, 30, 15, 55, 25, 90, 45}, as shown in the figure.



10	15	20	25	30	40	45	55	60	90
0	1	2	3	4	5	6	7	8	9

Algorithm : (Method - I)

MERGE (A, B, C, LB1, UB1, LB2, UB2, LB3, UB3)

Step 1: Let I, K

Step 2: Set K := LB3

Step 3: Repeat for I := LB1 to UB1 incrementing by 1

C[K] := A[I]

K := K + 1

[End of For]

Step 4: Repeat for I = LB2 to UB2 incrementing by 1

C[K] := B[I]

K := K + 1

[End of For]

Step 5: Call SORTING (C, LB3, UB3)

Step 6: Exit

The C function for this is :-

void MERGE (int A[], int B[])

```

    {
        int C[10], I, K;
        K = 0;
        for (I = 0; I < 5; I++)
        {
            C[K] = A[I];
            K++;
        }
        for (I = 0; I < 5; I++)
        {
            C[K] = B[I];
            K++;
        }
    }

```



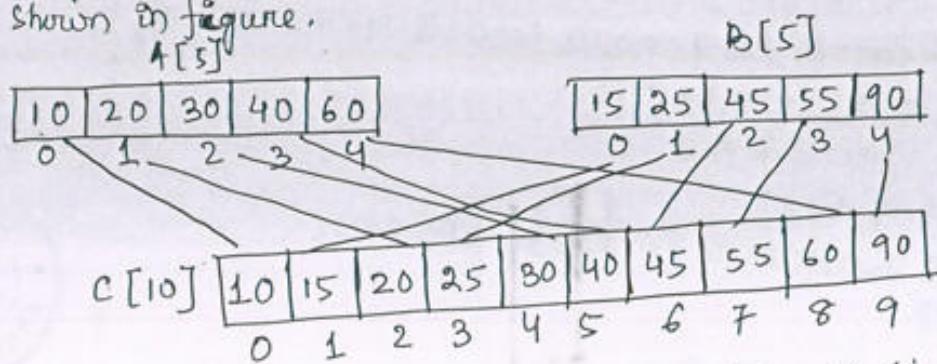
3) SORTING (C, 10);

- Q) When the elements of two arrays given are in sorted manner:
- Assume two arrays A and B are given with elements in sorted order. We need to compare elements between both arrays A & B, and always store the smaller element into the 3rd array. Hence if some elements are retained either in array A or in B, then they need to be stored directly into the at the end of 3rd array.

Eg:- Let us consider $A[5] = \{10, 20, 30, 40, 60\}$ and $B[5] = \{15, 25, 45, 55, 90\}$

Now we need to compare the elements of array 'A' with elements of array 'B' and the smaller element will be copied into array C. If any element are left out from either array A or array B, they will be copied into array 'C' at the end. So, finally we get the elements in array C in sorted order.

They are :- $C[10] = \{10, 15, 20, 25, 30, 40, 45, 55, 60, 90\}$ as shown in figure.



By comparing the elements of array 'A' with 'B', always smaller elements is stored into array 'C'. Finally left over element i.e. 90 is stored directly into array 'C'.

Algorithm:

MERGE (A, B, C, LB1, UB1, LB2, UB2, LB3, UB3)

Step 1: Let I, J, K.

Step 2: Set I := LB1, J := LB2, K := LB3

Step 3: Repeat While I <= UB1 AND J <= UB2

Step 3.1: If A[I] < B[J], then

C[K] := A[I]

K := K + 1

I := I + 1

Else

C[K] := B[J]

J := J + 1

K := K + 1

[End of IF]

[End of While]

Step 4: Repeat While I <= UB1

C[K] := A[I]

K := K + 1, I := I + 1.

[End of While]

Step 5: Repeat, while J <= UB2

C[K] := B[J]

K := K + 1, J := J + 1

[End of While]

Step 6: Exit

The 'C' - function for this :-

void MERGE (int A[], int B[])

{ int C[10], I, J, K;

I = 0, J = 0, K = 0;

while (I < 5 && J < 5)

{ if (A[I] < B[J])

{ C[K] = A[I];





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```
K++;
I++;

else
{
    C[K] = B[J];
    K++;
    J++;
}

while (I < 5)
{
    C[K] = A[I]; /* To copy rest of the elements left out in array A */
    I++;
    K++;
}

while (J < 5)
{
    C[K] = B[J]; /* To copy rest of the elements left out in array B */
    J++;
    K++;
}

for (K = 0; K < 10; K++)
{
    printf("%d", C[K]);
}
```

Multidimensional Array:

1. While discussing Multidimensional array, we will concentrate on the concepts related to 2-D array or matrix. In general, a two dimensional array is row and column arrangement of elements.
2. A two dimensional MxN array, 'A' is the collection of MxN data elements. If each element is specified by a pair of integers such as i, j called subscript with the property that $1 \leq i \leq M$ and $1 \leq j \leq N$.

Memory Representation of 2-D Array:

- The programming language will store the array 'A' in two different ways, that is:- i) Row-Major Order (Row by Row) and ii) Column Major Order (column by column)

i) Row-Major Order (Row by Row):

- In Row-Major order, elements of 2D array are stored on a row-by-row basis beginning from first row, i.e. the majority is given to the rows present in the matrix.

7	9	20	1	11	5	2	17	13	15	21	19
0,0	0,1	0,2	0,3	1,0	1,1	1,2	1,3	2,0	2,1	3,2	2,3

[Row Major Order Representation]

- Address of an element when represented in row-major order can be calculated by using the following formula :-

$$\text{Address of } A[i][j] = B + W * [(N * (i - LBR)) + (j - LBC)]$$

Eg:- Address of $A[1][3]$

$$\begin{aligned} &= 100 + 2 * (4 * 1 - 0) + (3 - 0) \\ &= 100 + 2 * [(4 * 1) + 3] \\ &= 100 + 2 * 7 \\ &= 114 \end{aligned}$$

In C language as $LBR = 0$ and $LBC = 0$, so the above formula can also be represented as per the following :-

$$\text{Address } A[i][j] = B + W * (N * i + j)$$

ii) Column Major Order (Column by column):

- In column-Major order, elements of 2D array are stored on a column by column basis beginning from first column, i.e. the majority is given to the columns present in the matrix.

Eg:- The representation of column-major order is:-

7	11	13	9	5	15	20	2	21	1	17	19
0,0	0,1	0,2	1,0	1,1	1,2	2,0	2,1	2,2	3,0	3,1	3,2

[Column-Major Order Representation]



2. Address of an element when represented in column-major order can be calculated by using the following formula :-

$$\boxed{\text{Address of } A[i][j] = B + w * [(i - LBR) + M * (j - LBC)]}$$

e.g:- Address of $A[1][3]$

$$\begin{aligned} &= 100 + 2 * [(1 - 0) + 3 * (3 - 0)] \\ &= 100 + 2 * [1 + 9] \\ &= 100 + 20 \\ &= 120 \end{aligned}$$

In C language, when $LBR = 0$ and $LBC = 0$, then

$$\boxed{\text{Address of } A[i][j] = B + w * [i + M * j]}$$

A table that shows the address of each location of matrix A in row major order and in column major order is given below.

Row Major Order	Address	Column Major Order	Address
$A[0][0]$	100	$A[0][0]$	100
$A[0][1]$	102	$A[1][0]$	102
$A[0][2]$	104	$A[2][0]$	104
$A[0][3]$	106	$A[0][1]$	106
$A[1][0]$	108	$A[1][1]$	108
$A[1][1]$	110	$A[2][1]$	110
$A[1][2]$	112	$A[0][2]$	112
$A[1][3]$	114	$A[1][2]$	114
$A[2][0]$	116	$A[2][2]$	116
$A[2][1]$	118	$A[0][3]$	118
$A[2][2]$	120	$A[1][3]$	120
$A[2][3]$	122	$A[2][3]$	122

Sparse Matrix:

1. A matrix with relatively high proportion of zero or null entries is called sparse matrix. A $M \times N$ matrix is said to be sparse matrix if many of its elements are zero.

eg:-

$$\begin{bmatrix} 0 & 0 & 0 & 24 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 9 & 0 & 0 \\ 0 & 0 & 0 & 0 & 18 & 0 & 0 \\ 0 & 0 & 0 & 0 & 8 & 0 & 0 \end{bmatrix}$$

It is a sparse matrix of 6×7 order with 5 non-zero elements out of 42 entries.



2. A matrix that is not sparse is called dense matrix. The diagonal, trigonal, lower triangular and upper triangular matrices fits into the category of sparse matrix.

$$\begin{bmatrix} 2 & 0 & 0 & 0 \\ 0 & 5 & 0 & 0 \\ 0 & 0 & 7 & 0 \\ 0 & 0 & 0 & 9 \end{bmatrix}$$

Diagonal matrix

$$\begin{bmatrix} 2 & 1 & 0 & 0 \\ 8 & 5 & 8 & 0 \\ 0 & 6 & 7 & 2 \\ 0 & 0 & 4 & 2 \end{bmatrix}$$

Trigonal matrix

$$\begin{bmatrix} 2 & 0 & 0 & 0 \\ 3 & 5 & 0 & 0 \\ 8 & 6 & 7 & 0 \\ 4 & 1 & 4 & 9 \end{bmatrix}$$

Lower triangular matrix

$$\begin{bmatrix} 2 & 1 & 8 & 6 \\ 0 & 5 & 3 & 4 \\ 0 & 0 & 7 & 2 \\ 0 & 0 & 0 & 9 \end{bmatrix}$$

Upper triangular matrix

Array Representation of Sparse Matrix:

1. The alternate data structure that we consider to represent a sparse matrix is a triplet. The triplet is a two dimensional array having $t+1$ rows and 3 columns, where 't' is the total number of non-zero entries.
2. The first row of the triplet contains number of rows, columns and non-zero entries available in the matrix in its 1st, 2nd and 3rd column respectively.
3. In addition, we need to record the size of matrix ie:- no. of rows and no. of columns and non-zero elements, for this purpose, the first element of array of triplets is used where the first field stores no. of rows and 2nd field stores no. of columns and 3rd field stores no. of non-zero elements.

4. The possible operations on a sparse matrix are :-

- i) To store the non-zero entries of a sparse matrix into alternate triplet representation.
- ii) To display the original matrix from a given triplet representation of matrix.
- iii) To store transpose of the triplet representation.
- iv) To display the transpose of original sparse matrix using transpose of triplet.

e.g.: - Consider a matrix $A[5][6]$, which contains zeros and non-zeros. Let NZ be a variable containing nonzeros count.

		J			
		1	2	3	4
0	0	55	0	0	0
88	0	0	0	99	0
0	0	44	66	0	0
0	0	0	0	0	11
0	0	0	22	0	0

Sparse matrix
 $A[5][6]$

5	6	7
0	2	55
1	0	88
1	4	99
2	2	44
2	3	66
3	5	11
4	3	33

Triplet matrix
 $SP[8][3]$

6	5	7
0	1	88
2	0	55
2	2	44
3	2	66
3	4	33
4	1	99
5	3	11

Transpose of
triplet matrix
 $TP[8][3]$

0	88	0	0	0
0	0	0	0	0
55	0	44	0	0
0	0	66	0	22
0	99	0	0	0
0	0	0	11	0

Transpose of
original
matrix.

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Algorithm for operations on a Sparse matrix %

Step 1: Let $A[10][10]$, $SP[50][3]$, $TP[50][3]$, I, J, M, N, NZ

Step 2: $NZ = 0$

Step 3: Display "Enter the row and column size"

Step 4: Input M, N .

Step 5: Repeat, for $I = 0$ to $M-1$ incremented by 1.

Step 5.1: Repeat for $J = 0$ to $N-1$ incremented by 1:

 Input $A[I][J]$

 If $A[I][J] \neq 0$, then

$NZ = NZ + 1$

 [End of if]

[End of Step 5.1]

Step 6: If $NZ >= (M+N)/2$, then Display "Matrix is not sparse"

Step 7: else Display "Matrix is sparse".

[Calling the procedure to store Non-Zero elements from Matrix A into alternate data structure Triplet Matrix SP]

Step 7.1: CALL ALTERNATE (A, SP, M, N, NZ)

[Calling the procedure to display original matrix using Triplet Matrix SP]

Step 7.2: CALL DISPLAY-ORIGINAL (SP, M, N)

[Calling procedure to transpose of Triplet Matrix SP into alternate Matrix TP]

Step 7.3: CALL TRANPOSE (SP, TP, NZ, N)

[Calling procedure to display transpose of original matrix using triplet TP]

Step 7.4: CALL DISPLAY-TRANPOSE (TP, M, N, NZ)

[End of Step- 6]

Step 8: Exit.



Algorithm to Represent a Sparse Matrix in Triplet Format:

ALTERNATE (A , SP , M , N , NZ)

Step 1: Let $I, J, K := 1$.

Step 2: $SP[0][0] := M$, $SP[0][1] := N$, $SP[0][2] := NZ$.

Step 3: Repeat for $I := 0$ to $M-1$ incremented by 1.

Step 3.1: Repeat for $J := 0$ to $N-1$ incremented by 1.

If $A[I][J] \neq 0$ then

$SP[K][0] := I$

$SP[K][1] := J$

$SP[K][2] := A[I][J]$

$K := K + 1$.

[End of If]

[End of Step 3.1]

Step 4: Repeat, for $K := 0$ to NZ incremented by 1

Display $SP[K][0], SP[K][1], SP[K][2]$

[End of For]

Step 5: Exit.

C-function:

```
Void Alternate (int A[10][10], int SP[50][3])
```

{ int I, J, K = 1;

SP[0][0] = M, SP[0][1] = N, SP[0][2] = NZ;

for (I = 0; I < M; I++)

{ for (J = 0; J < N; J++)

{ if (A[I][J] != 0)

{ SP[K][0] = I;

SP[K][1] = J;

SP[K][2] = A[I][J];

K++;

for (K = 0; K < NZ; K++)

{ printf("%d %d %d\n", SP[K][0], SP[K][1], SP[K][2]);

{ }

Algorithm to Display Original Matrix Using Triplet (SP) :

DISPLAY-ORIGINAL(SP, M, N)

Step 1 : Let I, J, K

Step 2 : K := 1

Step 3 : Repeat For I := 0 to M-1 Increased by 1.

Step 3.1 : Repeat for J := 0 to N-1 Increased by 1.

If (SP[K][0] = I AND SP[X][1] = J), then

Display SP[K][2].

K := K + 1.

Else

Display "0".

[End of if]

[End of for step 3.1]

[End of for - step 3]

Step 4 : Exit.

C-Function:

void Display-original (int SP[50][3])

{ Ent I, J, K;

 K = 1;

 for (I = 0; I < M; I++)

 { for (J = 0; J < N; J++)

 { if (SP[K][0] == I && SP[K][1] == J)

 { printf("%d", SP[K][2]);

 K++;

 else

 { printf("0");

 { printf("\n");

}

}



Algorithm to find transpose of triplet matrix (SP) into alternate matrix (TP) :

TRANSPOSE (SP, TP, NZ, N)

Step 1: Let J, K, T := 1.

Step 2: TP[0][0] := SP[0][1], TP[0][1] := SP[0][0].
 $TP[0][2] := SP[0][2]$.

Step 3: Repeat for J := 0 to N-1 incremented by 1.

If ($SP[KJ[1] = J$), then

$TP[TJ[0] := SP[XJ[1]$

$TP[TJ[1] := SP[XJ[0]$

$TP[TJ[2] := SP[XJ[2]$

$T := T + 1$

[End of if]

[End of for - step 3-1]

[End of for - step 3]

Step 4: Repeat for T := 0 to NZ-1 incremented by 1.

Display $TP[TJ[0], TP[TJ[1], TP[TJ[2]$

[End of for]

Step 5: Exit.

C-function:

void Transpose (int SP[50][3], int TP[50][3])

{ int J, K, T = 1;

$TP[0][0] = SP[0][1];$

$TP[0][1] = SP[0][0];$

$TP[0][2] = SP[0][2];$

for (J = 0; J < N; J++)

{ for (K = 1; K < NZ; K++)

{ if ($SP[KJ[1] = J$)

{ $TP[TJ[0] = SP[KJ[1];$

$TP[TJ[1] = SP[KJ[0];$

$TP[TJ[2] = SP[KJ[2];$

}

}

T++;

for ($T=0$; $T \leq NZ$; $T++$)

{ printf("%d.%d.%d", TP[T][0], TP[T][1], TP[T][2]);

}

3.

Algorithm to display transpose of original matrix using transpose of triplet (TP):

DISPLAY-TRANSPOSE(TP, M, N, NZ)

Step 1: Let I, J, T.

Step 2: $T := 1$

Step 3: Repeat for $J := 0$ to $N - 1$ incremented by 1.

Step 3.1: Repeat for $I := 0$ to $M - 1$ incremented by 1.

If ($TP[T][0] = J$ AND $TP[T][1] = I$) then

Display $TP[T][2]$

$T := T + 1$.

else

Display "0"

[End of if]

[End of for-step 3.1]

[End of for-step 3]

Step 4: Exit.

C-function:

Void Display-Transpose (int TP[50][3])

{ int I, J, T;

$T = 1$;

for (J=0; J < N; J++)

{ for (I=0; I < M; I++)

{ if ((TP[T][0] == J) && (TP[T][1] == I))

{ printf("%d", TP[T][2]);

$T++$;

else

{ printf("0");





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{ Pointf("\n");

Complete C-program for operations on Sparse Matrix;

```
#include<stdio.h>
void Alternate(int A[10][10], int SP[50][3]);
void Display-Original(int SP[50][3]);
void Transpose(int SP[50][3], int TP[50][3]);
void Display-Transpose(int TP[50][3]);
int M, N, NZ;
```

main()

{ int A[10][10], SP[50][3], TP[50][3], I, J;

NZ = 0;

Pointf("Enter row and column size of matrix");

scanf("%d %d", &M, &N);

Pointf("Enter elements now");

for(I = 0; I < M; I++)

{ for(J = 0; J < N; J++)

{ scanf("%d", &A[I][J]);

if(A[I][J] != 0)

{ NZ++;

}

} }

if(NZ >= (M * N) / 2)

{ Pointf("Matrix is not sparse");

exit(0);

else

{ Pointf("Matrix is sparse");

/* calling the function to store Non-Zero elements from
Matrix A into alternate Triplet Matrix SP/

Alternate(A, SP);

/* calling the procedure to display original matrix using
Triplet Matrix SP */

Display-Original(SP);

/* calling the function to transpose of Triplet Matrix SP into alternate matrix TP */

Transpose (SP, TP);

/* calling function to display transpose of original matrix using Triplet TP */

Display - Transpose (TP);

3

void Alternate (int A[10][10], int SP[5][3])

{ int I, J, K = 1;

SP[0][0] = M, SP[0][1] = N, SP[0][2] = NZ;

for (I = 0; I < M; I++)

{ for (J = 0; J < N; J++)

{ if (A[I][J] != 0)

{ SP[K][0] = I;

SP[K][1] = J;

SP[K][2] = A[I][J];

K++;

y y y

for (K = 0; K <= NZ; K++)

{ printf ("%d %d %d\n", SP[K][0], SP[K][1], SP[K][2]);

y y

void Display_Original (int SP[50][3])

{ int I, J, K;

K = 1;

for (I = 0; I < M; I++)

{ for (J = 0; J < N; J++)

{ if (SP[K][0] == I && SP[K][1] == J)

{ printf ("%d", SP[K][2]);

y K++;



```

    , else
    {
        printf("0");
    }
    printf("\n");

3 void Transpose (int SP[50][3], int TP[50][3])
{
    int J, K, T = 1;
    TP[0][0] = SP[0][1];
    TP[0][1] = SP[0][0];
    TP[0][2] = SP[0][2];
    for (J = 0; J < N; J++)
    {
        for (K = 1; K < NZ; K++)
        {
            if (SP[K][1] == J)
            {
                TP[T][0] = SP[K][1];
                TP[T][1] = SP[K][0];
                TP[T][2] = SP[K][2];
                T++;
            }
        }
    }
    for (T = 0; T < = NZ; T++)
    {
        printf("1.0 1.0 1.0\n"), TP[T][0], TP[T][1], TP[T][2]);
    }
}

3 void Display_Transpose (int TP[50][3])
{
    int I, J, T;
    T = 1;
    for (J = 0; J < N; J++)
    {
        for (I = 0; I < M; I++)
        {
            if ((TP[T][0] == J) && (TP[T][1] == I))
            {
                printf("1.0\n"), TP[T][2];
                T++;
            }
            else
            {
                printf("0");
            }
        }
        printf("\n");
    }
}

```



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Data Structure Using C

Topic:
Stack

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Stack:

- It is a non-primitive Linear data structure, which works on the concept of Last In First Out (LIFO). It is an ordered list, where insertion and deletion can be done at one end only, which is called TOP element of the stack.

e.g:- A stack of plates one above the other.

A stack of books kept one above the others.

Operations of Stack:

- There are various operation done in stack. That is:-

PUSH: Insertion of an element at the TOP of the stack.

POP: Deletion of an element from the TOP of the stack.

PEEP: If we want to know about the information stored at some location in the stack then PEEP operation is required.

Memory Representation of Stack: Array Representation

- An one dimensional array can be considered for representing a stack in memory. While representing a stack in the form of an array we take a variable Top that identifies top most element of the stack.

- Initially, when the stack is empty $\text{TOP} = -1$. The operation of pushing an ITEM into a stack and the operation of removing an ITEM from the stack is done by PUSH and POP.

- In executing the procedure PUSH, one must first test whether there is room in the stack for new ITEM, if not then we have the condition known as "OVERFLOW". The condition for overflow is $\text{TOP} = \text{size} - 1$, where size is the maximum number of elements that can be held by the array that represents the stack in memory.

- In executing the procedure POP, we must first test whether there is an element in the stack to be deleted, if not then we have the condition known as "UNDERFLOW". The condition for UNDERFLOW is $\text{TOP} = -1$.



Linked Representation of Stack :-

The concept of dynamic memory allocation is implemented by using linked list to represent stack in linked format.

Algorithm for PUSH Operation :-

Let $\text{STACK}[\text{size}]$ is an array, TOP = topmost element and ITEM = element to be pushed into the stack. Then the algorithm for PUSH operation is :-

PUSH(STACK, TOP, SIZE, ITEM)

Step 1: if ($\text{TOP} = \text{SIZE} - 1$), then
Display "Overflow"
EXIT

Step 2: else

$\text{TOP} := \text{TOP} + 1$
 $\text{STACK}[\text{TOP}] := \text{ITEM}$
[End of If]

Step 3: EXIT

Algorithm for POP Operation :-

Step 1: Let ITEM

Step 2: if ($\text{TOP} < 0$), then
Display "Underflow"
EXIT.

Step 3: else

$\text{ITEM} := \text{STACK}[\text{TOP}]$
Display "popped item is 'g' ITEM"

$\text{TOP} := \text{TOP} - 1$

[End of If]

Step 4: EXIT.

Algorithm for PEEP :

Step 1 : If $\text{TOP} = -1$, then print "underflow" and return.

Step 2 : Read the location value ' i '

Step 3 : Return the i th element from the top of the stack

$\text{Return}(\text{STACK}(K[\text{TOP}-i+1]))$

Algorithm for Update :

When the content of some location in a stack is to be changed "update" operation is required.

$\text{Update}(\text{STACK}, \text{ITEM})$

Step 1 : If $\text{TOP} = -1$, then print "Underflow" and return.

Step 2 : Read the location value ' i '.

Step 3 : $\text{STACK}[\text{TOP}-i+1] = \text{ITEM}$

Step 4 : Return.

C- Program for stack operation :

#include<stdio.h>

#define SIZE 10.

int stack[SIZE], TOP = -1, i;

void push();

void pop();

void display();

main()

{ int ch;

do

printf("[1]. push [2]. pop [3]. Display [4]. Exit");

printf("\nEnter your choice [1-4]:");

scanf("%d", &ch);

switch(ch)

{

case 1 :

push();
break;

case 2 :

pop();
break;

case 3 :

display();
break;

case 4 :

break;

default:

printf("Invalid option");

} while(ch != 4);



```

void push()
{
    if (TOP == SIZE - 1)
    {
        printf ("stack overflow");
        return;
    }
    else
    {
        TOP++;
        printf ("enter the element to push");
        scanf ("%d", &stack[TOP]);
    }
}

void pop()
{
    if (TOP == -1)
    {
        printf ("stack underflow");
        return;
    }
    printf ("the pop element is : %d", stack[TOP]);
    TOP--;
}

void display()
{
    if (TOP == -1)
    {
        printf ("stack is empty or underflow");
        return;
    }
    printf ("The elements in stack are : %d", TOP);
    for (i = TOP; i >= 0; i--)
        printf ("%d", stack[i]);
}

```

Application of stack:

- Stacks are used to pass parameters between functions or in a call to a function the parameters and local variable are stored on a stack.
- High level programming language, such as 'pascal', 'c', that provides for recursion used stack for book keeping. That is:- in each recursive call, there is need to save the current values of parameters local variables and return address.

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Conversion and Evaluation of Arithmetic Expressions:

Arithmetic Expression Notations:

1. In any arithmetic expression, each operator is placed in between two operands i.e. mathematical representation, then this way of representing the arithmetic expression is called as infix expression e.g. $A + B$.
2. Apart from usual mathematical representation of an arithmetic expression, an expression can also be represented in the following two ways.
 - i. e. by Polish or Prefix Notation.
 - ii. by Reverse Polish or Postfix Notation.

by Polish or Prefix Notation:

→ The notation, in which the operator symbol is placed before its operands, is referred as polish or prefix notation, e.g.: - $+AB$

by Reverse Polish or Postfix Notation:

→ The notation, in which the operator symbol is placed after its operands, is referred as reverse polish or postfix notation. e.g.: - $AB+$.

Mathematical Procedure for Conversion:

1. The possible conversions are :-

- i) Infix to Prefix
- ii) Prefix to Infix
- iii) Infix to Postfix
- iv) Postfix to Infix
- v) Prefix to Postfix
- vi) Postfix to prefix.



2. Standard Arithmetic Operators and Precedence levels are :-

\wedge (exponentiation) → higher level
 $\times, /, \%$ → middle level
 $+, -$ → lower level.

i) Infix to Prefix :

- Identify the innermost brackets.
- Identify the operator according to the priority of evaluation.
- Represent the operator and corresponding operator in prefix notation.
- Continue this process until the equivalent prefix expression is achieved.

$$\text{eg:- } (A + B * (C - D^E) / F)$$

$$\begin{aligned} &= (A + B * (C - [^DE])) / F \\ &= (A + B * [-C^DE]) / F \\ &= (A + [*B - C^DE]) / F \\ &= A + [/ * B - C^DEF] \\ &= + A / * B - C^DEF. \end{aligned}$$

ii) Prefix to Infix :

- Identify the operator from right to left order.
- The two operands which immediately follows the operator are for evaluation.
- Represent the operator and operands in infix notation.
- Continue this process until the equivalent infix expression is achieved.
- If the priority of a scanned operator is less than any operators available with [], then put them within ().

$$\text{eg:- } + A / * B - C^DEF$$

$$\begin{aligned} &= + A / * B - C [D^E] F \\ &= + A / * B [C - D^E] F \\ &= + A / [B * (C - D^E)] F \\ &= + A [B * (C - D^E) / F] \\ &= A + B * (C - D^E) / F. \end{aligned}$$

Ques 1) Infix to Postfix :

- Identify the inner most branches.
- Identify the operators according to the priority of evaluation.
- Represent the operators and corresponding operator in postfix notation.
- Continue this process until the equivalent postfix expression is achieved.

$$\begin{aligned}
 \text{eg:- } & (A + B * (C - D^E) / F) \\
 & = (A + B * (C - [DE^]) / F) \\
 & = (A + B * [CDE^ -] / F) \\
 & = (A + [BCDE^ - *] / F) \\
 & = A + [BCDE^ - * F /] \\
 & = ABCDE^ - * F /
 \end{aligned}$$

Ques 2) Postfix to Infix :

- Identify the operators from left to right order.
- The two operands which immediately precede the operator are for evaluation.
- Represent the operators and operands in infix notation.
- Continue this process until the equivalent infix expression is achieved.
- If the priority of a scanned operator is less than any operators available with [], then put them within () .

$$\begin{aligned}
 \text{eg:- } & ABCDE^ - * F / \\
 & = AB[C[DAE] - * F /] \\
 & = AB[C - D^E] * F / \\
 & = A[B * (C - D^E)] F / \\
 & = A[B * (C - D^E) / F] + \\
 & = A + B * (C - D^E) / F .
 \end{aligned}$$



v) Prefix to Postfix:

- Identify the operators from left to right order.
- The two operands which immediately follows the operator are for evaluation.
- Represent the operator and operands in postfix notation.
- Continue this process until the equivalent postfix expression is achieved.
- If the priority of a scanned operator is less than any operators available with [], then put them within () .

$$\begin{aligned}
 \text{Eg:- } & + A / * B - C ^ D E F \\
 & = + A / * B - C [D E ^] F \\
 & = + A / * B [C D E ^ -] F \\
 & = + A / [B C D E ^ - *] F \\
 & = + A [B C D E ^ - * F /] \\
 & = A B C D E ^ - * F / +
 \end{aligned}$$

vi) Postfix to Prefix:

- Identify the operators from left to right order
- The two operands which immediately precedes the operator are for evaluation.
- Represent the operator and operands in prefix notation.
- Continue this process until the equivalent prefix expression is achieved.
- If the priority of a scanned operator is less than any operators available with [], then put them within () .

$$\begin{aligned}
 \text{Eg:- } & A B C D E ^ - * F / + \\
 & = A B C [^ D E] - * F / + \\
 & = A B [- C ^ D E] * F / + \\
 & = A [* B - C ^ D E] F / + \\
 & = A [/ * B - C ^ D E F] + \\
 & = + A / * B - C ^ D E F .
 \end{aligned}$$

Importance of Postfix Expression :-

1. INFIX notation which is rather complex as using this notation one has to remember a set of rules. The rules include BODMAS and ASSOCIATIVITY.
2. In case of POSTFIX notation, the expression, which is easier to work or evaluate the expression as compared to the INFIX expression. In a POSTFIX expression, operands appear before the operators, there is no need to follow the operator precedence and any other rules.

Conversion of an INFIX expression into Postfix expression using Stack :-



Algorithm :-

[Assume Q is an Infix expression and P is the corresponding Postfix Notation]

Step 1: PUSH ("onto STACK and Add") at the end of Q.

Step 2: Repeatedly scan from Q Until STACK is empty.

Step 2.1: If Q[I] is an operand, Then Add it to P[J],

Step 2.2: Else if Q[I] is '(', Then PUSH Q[I] onto STACK.

Step 2.3: Else if Q[I] is an operator, Then

Step 2.3.1: While STACK [TOP] is an operator and has higher or equal priority compared to Q[I].

pop operators from STACK and add to P[J].

[End of while]

Step 2.3.2: Push operator Q[I] onto STACK

Step 2.4: Else if Q[I] is an ')', Then

Step 2.4.1: Repeatedly pop operators from STACK and add to P[J] until ')' is encountered.

Step 2.4.2: Remove ')' from STACK.

Step 3: Exit. [End of step-2]



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Procedure for Conversion:

$$\text{Eg:- } A = (B * C - (D / E ^ F))$$

Symbol Scanned from A	Stack	Postfix Expression P
((
B	(B
*	(*	B
C	(*	BC
-	(-	BC*
((-	BC*
D	(-()	BC*D
/	(-()	BC*D
E	(-()	BC*DE
^	(-()^	BC*DE
F	(-()^	BC*DEF
)	(-)	BC*DEFN/
)	.	BC*DEFN/-

Evaluation:

Evaluation of Postfix expression using Stack:

[Assume 'P' is a postfix expression]

Step 1: Add ')' at the end of P.

Step 2: Repeatedly scan P from left to right until ')' encountered.

Step 2.1: If $P[i:j]$ is an operand, then
 Push the operand onto STACK

Step 2.2: else if $P[i:j]$ is an operator \otimes then

Step 2.2.1: Pop two elements from stack
 (1st element is A and 2nd is B)

Step 2.2.2 : Evaluate $B \otimes A$

Step 2.2.3 : Push result back to STACK

[End of If]

[End of step 2]

Step 3 : VALUE := STACK[TOP]

Step 4 : Display VALUE

Step 5 : EXIT

Eg:- Evaluate the following Postfix expression using stack:-

$$P = B C * D E F ^ / -$$

where $B = 5, C = 6, D = 24, E = 2, F = 3.$

$$\text{So, } P = 5, 6, *, 24, 2, 3, ^, /, -$$



Symbol scanned from Postfix Notation	Stack	A	B	$B \otimes A$
5	5			
6	5, 6			
*	30	6	5	$5 * 6 = 30$
24	30, 24			
2	30, 24, 2			
3	30, 24, 2, 3			
^	30, 24, 8	3	2	$2^3 = 8$
/	30, 3	8	24	$24 / 8 = 3$
-	27	3	30	$30 - 3 = 27$

c - program for conversion of an infix expression to postfix expression:

```
#include<stdio.h>
int top = -1;
void push(char);
char pop(void);
int op(char);
int priority(char);
char Q[100], P[100], S[100];
main()
{
    int i, j, k, r;
    printf("enter a string");
    scanf("%s", Q);
    for (i=0; Q[i] != '\0'; i++)
        Q[i] = ')';
    top++;
    S[top] = '(';
    i = 0; j = 0;
    while (top != -1)
    {
        /* if an operand is found */
        else if (op(Q[i]) == 2)
            push(Q[i]);
        /* if an operator is found at Q[i] then repeatedly
           pop from the top of stack for each operator which
           has same or higher precedence than the operator found */
        else if (op(Q[i]) == 3)
        {
            while (op(S[top]) == 3 && priority(L[top]) > priority(R[i]))
            {
                P[j] = pop();
                j++;
            }
            push(Q[i]);
        }
    }
}
```

1 * If a right parenthesis is found, then repeatedly pop from stack and add it to 'p' until a left parenthesis is found. Remove it from the stack and do not add it to p */

else if ($op(A[i]) == 4$)

{ while ($op(S[top]) != 2$)

{ $P[j] = pop();$

$j++;$

$top--;$

$i++;$

$P[j] = '\backslash 0';$

printf("\n\t%.c\t", S[i-1]);

for ($r=0; r <= top; r++$)

 printf("-%c-", S[r]);

 printf("\t-%c", P[r]);

}

int op(char x)

{ if ($x == '('$)

 return 2;

else if ($x == ')' || x == '-' || x == '*' || x == '/' || x == '^'$)

 return 3;

else if ($x == ')'$)

 return 4;

else

 return 1;

int priority (char x)

{ if ($x == '+' || x == '-'$)

 return 1;



```

else if (x == '*' || x == '/')
    return 2;
else
    return 3;
}

void push(char x)
{
    top++;
    S[top] = x;
}

char pop(void)
{
    char x;
    x = S[top];
    top--;
    return x;
}

```

C - program for Post-fix Evaluation :-

```

#include <stdio.h>
#include <math.h>
int op(char);
void push(int);
int pop(void);
int top = -1;
int stack[100], A, B, R, Value;
char p[100];
main()
{
    int i, j;
    printf("enter the post-fix expression");
    scanf("%s", p);
    for (i = 0; p[i] != '\0'; i++)
        p[i] = 'j';
    for (i = 0; p[i] != '\0'; i++)
    {

```

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```
#include <stdio.h>
#include <stack.h>

void push(int x)
{
    stack.push(x);
}

int pop()
{
    int R;
    R = stack.pop();
    return R;
}

int op(char x)
{
    if (x == '+' || x == '-' || x == '*' || x == '/')
        return 3;
    else
        return 1;
}

int calculate()
{
    stack s;
    int A, B, C;
    char op;
    float R;
    int top = -1;
    float stack[10];
    int i = 0;
    char str[100];
    gets(str);

    while (str[i] != '\0')
    {
        if (str[i] >='0' && str[i] <='9')
            push(str[i] - '0');
        else if (str[i] == '+' || str[i] == '-')
            op = str[i];
        else if (str[i] == '*' || str[i] == '/')
            op = str[i];
        else if (str[i] == '(')
            push(str[i]);
        else if (str[i] == ')')
            R = pop();
        else if (op == '+')
            R = pop() + pop();
        else if (op == '-')
            R = pop() - pop();
        else if (op == '*')
            R = pop() * pop();
        else if (op == '/')
            R = pop() / pop();
        else
            R = pop();
        push(R);
    }
    R = pop();
    printf("Result estd: %f", R);
}
```



Conversion of infix expression to prefix expression using stack.

Assume 'Q' is an infix expression. Consider there are two stacks S1 and S2 exist. The following algorithm converts the infix expression into its equivalent prefix notation,

Algorithm:

Step 1: Add left parenthesis '(' at the beginning of the expression 'Q'.

Step 2: Push ')' onto stack S1.

Step 3: Repeatedly scan Q from right to left order, until stack S1 is empty.

Step 3.1: If $Q[i]$ is an operand, then push it onto stack S2.

Step 3.2: Else if $Q[i] =)$, then push it onto stack S1.

Step 3.3: Else if $Q[i]$ is an operator (OP), then

Step 3.3.1: Set $x := \text{pop}(S1)$

Step 3.3.2: Repeat while x is an operator AND
(precedence(x) > precedence(OP))

push(x) onto stack S2

Set $x := \text{pop}(S1)$

[End of while - Step 3.3.2]

Step 3.3.3: push(x) onto stack S1

Step 3.3.4: push(OP) onto stack S1.

Step 3.4: Else if $Q[i]$ is '(', then

Step 3.4.1: Set $x := \text{pop}(S1)$

Step 3.4.2: Repeat, while ($x \neq)$ (until right parenthesis found)

Step 3.4.2.1: push(x) onto stack S2

Step 3.4.2.2: Set $x := \text{pop}(S1)$

[End of while - Step 3.4.2]

[End of if - Step 3.1]

[End of loop - step 3]

Step 4: Repeat, while stack S2 is not empty.

Step 4.1: Set $x := \text{pop}(S2)$

Step 4.2: Display x.

[End of while]

Step 5: Exit.

Procedure of Conversion :-

$$\text{eg} :- Q = (A + B * C * (M + N ^ P + T) - G) + H$$

Symbol Scanned from Q	Stack S1	Stack S2.
H)	H
+) +	H
G) +	H G
-) + -	H G
)) + -)	H G P
T) + -) +	H G T P
+) + -) +	H G T
P) + -) +	H G T P
^) + -) + ^	H G T P
N) + -) + ^	H G T P N
*) + -) + * ^	H G T P N ^
M) + -) + * ^ M	H G T P N ^ M
() + -	H G T P N ^ M * +
*) + - * ^	H G T P N ^ M * +
C) + - * ^ C	H G T P N ^ M * + C
*) + - * ^ C	H G T P N ^ M * + C
B) + - * ^ C B	H G T P N ^ M * + C B
+) + - +	H G T P N ^ M * + C B * +
A) + - + A	H G T P N ^ M * + C B * + A
C		H G T P N ^ M * + C B * + A + -

So, the prefix Notation, We can get by popping all the symbols from stack S2. i.e:- + - + A * * B C + ^ M ^ N P T G H .

Evaluation of prefix expression:

[Assume P is a Prefix Expression]

Step 1: Add '(' at beginning of the prefix expression.

Step 2: Repeatedly scan from P in right to left order until ')' encountered.

Step 2.1: If $P[i]$ is an operand, then
push the operand onto STACK

Step 2.2: Else if $P[i]$ is operator (OP), then

Step 2.2.1: Pop two elements from STACK

(1st element is A and 2nd element is B)

Step 2.2.2: Evaluate A (OP) B.

Step 2.2.3: Push result back to STACK

[End of If]

[End of loop - step-2]

Step 3: VALUE := STACK[Top]

Step 4: Display VALUE

Step 5: Exit.

Example:

Evaluate the following prefix expression using stack:

$$P = (-, *, 3, +, 16, 2, /, 12, 6)$$

Symbol scanned from prefix expression in Right to Left order	Stack	A	B	$A(OP)B$
6	6			
12	6, 12			
/	2	12	6	$12/6=2$
2	2, 2			
16	2, 2, 16			
+	2, 18	16	2	$16+2=18$
3	2, 18, 3			
*	2, 54	3	18	$3*18=54$
-	52	54	2	$54-2=52$

finally, the value in the stack is 52.

C program for conversion from infix to prefix expression:-

```
#include<stdio.h>
char S[50], S2[50], Q[50], P[50];
int t1 = -1, t2 = -1;
void S1 push(char);
void S1 pop(void);
void S2push(char);
char S2pop(void);
int op(char);
int priority(char);
main()
{
    int i, K, r;
    char x;
    clrscr();
    printf("enter a string");
    scanf("%s", Q);
    for (i=0; Q[i] != '\0'; i++)
        for (j = i; Q[j] == Q[i]; j++)
            Q[i+1] = Q[j];
    Q[0] = ' ';
    printf("%s", Q);
    t1 = 0;
    S1[t1] = ')';
    for (i=0; Q[i] != '\0'; i++)
        if (Q[i] == ')')
            while (t1 != -1)
                if (op(Q[i]) == 1)
                    S2push(Q[i]);
                else if (op(Q[i]) == 4)
                    S1push(Q[i]);
            t1--;
        else if (Q[i] == '(')
            t1++;
        else if (Q[i] == '+' || Q[i] == '-')
            if (op(Q[i]) > op(Q[i-1]))
                S1push(Q[i]);
            else
                S2push(Q[i]);
        else if (Q[i] == '*' || Q[i] == '/')
            if (op(Q[i]) > op(Q[i-1]))
                S1push(Q[i]);
            else
                S2push(Q[i]);
        else
            S2push(Q[i]);
}
```





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1. If arr operator is found //
else if ($op(a[i]) == 3$)
{
 $x = s1.pop();$
 while ($op(x) == 3 \text{ && } priority(x) > priority(a[i])$)
 {
 $s2.push(x);$
 $x = s1.pop();$
 }
 $s1.push(x);$
 $s1.push(a[i]);$
 }
}

1. If left parenthesis found //
else if ($op(a[i]) == 2$)
{
 while ($op(s1[t]) != 4$)
 {
 $x = s1.pop();$
 $s2.push(x);$
 }
 $s1.pop();$
 }
 $i--;$
}
printf("In In In the prefix notation is ");
while ($t2 != -1$)
{
 $x = s2.pop();$
 printf("-%c", x);
}

int op(char x)
{
 if ($x == '('$)
 return 2;
 else if ($x == '+' || x == '-' || x == '*' || x == '/' || x == '^'$)
 return 3;
 else if ($x == ')'$)
 return 4;
}

```

    else return 1;
}

int priority (char x)
{
    if (x == '+' || x == '-')
        return 1;
    else if (x == '*' || x == '/')
        return 2;
    else
        return 3;
}

void s1push(char x)
{
    t1++;
    s1[t1] = x;
}

char s1pop(void)
{
    char x;
    x = s1[t1];
    t1--;
    return x;
}

void s2push(char x)
{
    t2++;
    s2[t2] = x;
}

char s2pop(void)
{
    char x;
    x = s2[t2];
    t2--;
    return x;
}

```



'C' program for prefix Evaluation :

```

#include <stdio.h>
#include <math.h>
int op(char);
int calc(char, int, int);
void push(int);
int pop(void);
char S[50];
char P[50];
int top = -1;
main()
{
    int E, k, a, b, c;
    printf("Enter prefix notation");
    scanf("%s", P);
    for(i=0; P[i] != '\0'; i++)
        for(j = 0; j < i; j++)
            if(P[i+1] == P[j])
                P[i+1] = P[i];
    P[0] = '(';
    for(i=0; P[i] != '\0'; i++)
        if(P[i] == ')')
            i--;
        while(P[i] != '(')

```

if $\text{op}(\text{P}[\varepsilon]) = 2$

```
{ printf(" enter the value of t.c, p[?]);
```

`score('a', d, 8K);`

```
push(K);
```

25

else

6

```
a = pop();
```

```
b = pop();
```

$c = \text{calc}(p[i], b, a);$

```
push(c);
```

α \rightarrow $i - j$

printf(" the evaluated value is %d", s[top]);

8

int op(char x)

{

if (x == '+' || x == '-' || x == '*' || x == '/' || x == '^')

return 1;

else if (x == '(')

return 3;

else return 2; .

9

int calc(char x, int a, int b)

{

int c;

switch(x)

{

case '+': c = b + a; break;

case '-': c = b - a; break;

case '*': c = b * a; break;

case '/': c = b / a; break;

case '^': c = pow(b, a); break;

}

return c;

10

void push(int x)

{

top++;

s[top] = x;

11

int pop(void)

{

int t;

t = s[top];

top--;

return t;

12





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Data Structure Using C

Topic:

Queue

Contributed By:

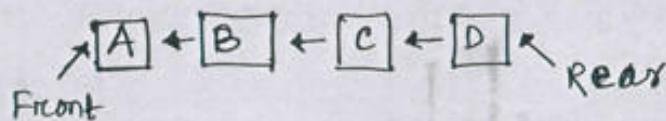
Nihar Ranjan Rout

Gandhi Institute For Technology, GIFT

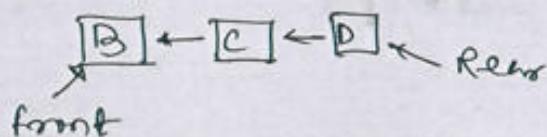
Queue:

1. Queue is a linear non-primitive data structure, works on the concept First in first out (FIFO), where insertion takes place at one end called REAR end and Deletion takes place at other end called Front end.

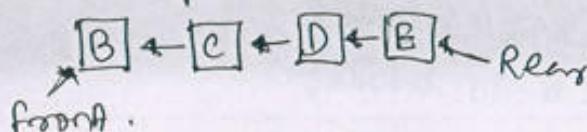
Eg :- Consider below a list of elements exist.



After deleting an element from Front end :-



After inserting element 'E' at Rear end :-



Memory Representation of Queue:

1. Array Representation :-

The concept of static memory allocation can be implemented by using ~~linked list~~ to represent a one dimensional array to represent a queue in memory. We consider two variables FRONT and REAR which holds the index of front and rear end of the queue.

2. Linked Representation :-

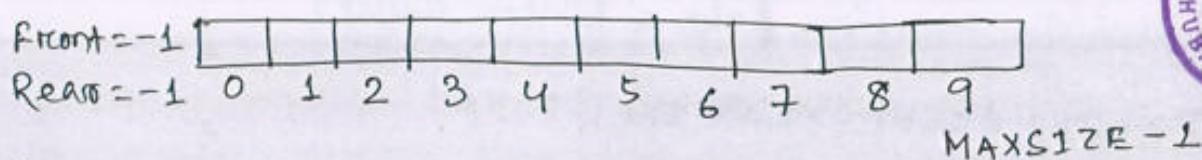
The concept of dynamic memory allocation is implemented by using linked list to represent queue in linked format.

Types of Queues :

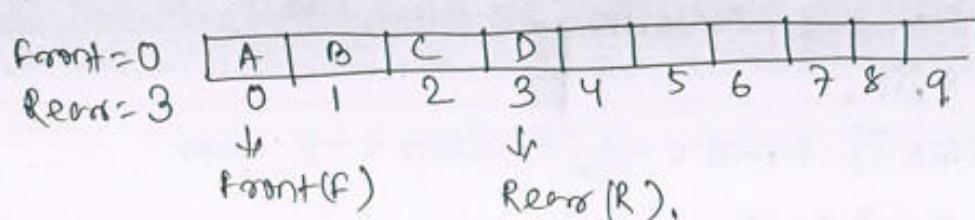
1. Linear Queue : Insertion Operation and Deletion operation :

1. In the Queue, while inserting a new element, one must test whether there is a room available at Rear end or not if room is available then the element can be inserted, otherwise Overflow situation occurs i.e.: Queue is full.
2. Deletion of an element can be done from the room that is identified by FRONT and FRONT will identify the next room of the queue. Underflow situation occurs when no element is present in the queue, i.e. when front and rear identified NULL and deletion operation is performed on it.

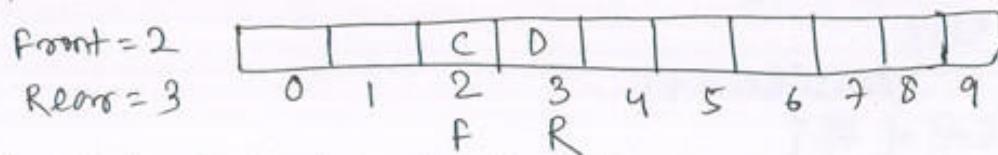
Eg:- Let $Q[\text{MAXSIZE}]$ is an array that represents a queue in the memory and at the beginning, it is empty, and $\text{MAXSIZE} = 10$, i.e.: $\text{Front} = \text{Rear} = \text{NULL} \text{ or } -1$.



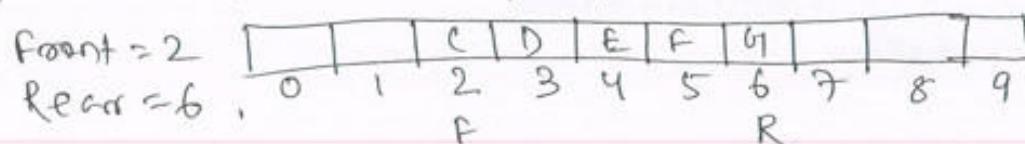
i) Insert 4 elements A, B, C, D.



ii) Delete 2 elements



iii) Insert 3 elements E, F, G.



From the example, it is clear that-

i) for each insertion in the queue the value of REAR is incremented by 1 ie:- $\text{REAR} = \text{REAR} + 1$.

ii) for each deletion in the queue the value of front is incremented by 1 ie:- $\text{FRONT} = \text{FRONT} + 1$.

Note :-

1. After all the elements inserted into the Queue, Rear will identify position at MAXSIZE - 1. ie:- Queue is full.
2. Even though the memory locations are vacant at FRONT end, where Rear identified MAXSIZE - 1 position, we can't insert a new element.
3. When Front = Rear = Null (ie:- queue is empty), we can't perform deletion operation.
4. When Front = Rear only one element is present in Queue.
5. When Front is at MAXSIZE - 1, means Queue having one element. After deletion Front need to be reset to NULL.

Algorithm for insertion into a Linear Queue:

QINSERT (QUEUE[MAXSIZE], ITEM)

Step 1: If Rear = MAXSIZE - 1, then

 Display "Overflow Or Queue Full"
 Exit.

Step 2: Else if front = -1, or Rear = -1, then

 front := 0

 Rear := 0

Step 3: Else

 Rear := Rear + 1

 [End of if]

Step 4: QUEUE[Rear] := ITEM

Step 5: Exit.

C-function:

```
void insertion (int Q[], int item)
{
    if (rear == maxsize - 1)
    {
        printf ("In queue overflow");
        exit (0);
    }
    else if (front == -1 || rear == -1)
    {
        front = 0;
        rear = 0;
    }
    else
    {
        rear = rear + 1;
    }
    Q[rear] = item;
}
```



Algorithm for deletion in a linear queue:

Assume QUEUE[MAXSIZE] is an array which represents a queue, FRONT and REAR identifies the index of front and rear end respectively. ITEM holds the element to be deleted from queue.

QDELETE (QUEUE[MAXSIZE])

Step 1: Get ITEM

Step 2: If front = -1 or rear = -1, then

Display "Underflow" or Queue empty"

Exit

[End of If]

Step 3: ITEM := QUEUE[front]

Step 4: Display "Deleted Item is", ITEM

Step 5: Else If front = rear, then [when queue has only one element]

front := -1

rear := -1

Step 6: Else

front := front + 1.

Step 7: Exit.

SUBJECT:- DATA STRUCTURE

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C-function:

```
void deletion(int A[])
{
    int item;
    if (front == -1 || rear == -1)
        printf("In queue underflow");
    exit(0);
    item = A[front];
    if (front == rear)
    {
        front = -1;
        rear = -1;
    }
    else
    {
        front = front + 1;
        printf("In deleted item is %.d", item);
    }
}
```

C-Program for implementing Linear queue:

```
#include<stdio.h>
#include<process.h>
#define maxsize 10
int A[maxsize], front = -1, rear = -1, item;
void insertion(int [], int);
void deletion(int []);
void display(int []);
main()
{
    int option;
    do
    {
        printf("\n 1. insert\n 2. delete\n 3. display\n 4. exit\n\n");
        scanf("%d", &option);
    }
```

```
switch(option)
```

```
{ case 1: printf("\n enter item");
    scanf("%d", &item);
    insertion(Q, item);
```

```
    break;
```

```
case 2: deletion(Q);
    break;
```

```
case 3: display(Q);
    break;
```

```
case 4: exit(0);
    break;
```

```
default: printf("In Invalid entry");
```

```
}
```

```
while(option != 4);
```

```
void insertion(int Q[], int item)
```

```
{ if(rear == maxsize - 1)
```

```
{ printf("\n queue overflow");
    exit(0); }
```

```
else if(front == -1 || rear == -1)
```

```
{ front = 0;
    rear = 0; }
```

```
else { rear = rear + 1;
    Q[rear] = item; }
```

```
}
```



`void deletion(int Q[])`

{ int item;

if (front == -1 || rear == -1)

{ printf("In Queue Underflow");
exit(0);

{ item = Q[front];

if (front == rear)

{ front = -1;

rear = -1;

else { front = front + 1;

printf("In deleted item is %d", item);

`void display(int Q[])`

{ int i;

if (front != -1)

{ printf("Elements at queue\n");

for (i = front; i <= rear; i++)

printf(" %d", Q[i]);

.

Circular Queue:

1. It is a queue of circular nature, in which it is possible to insert a new element at the front location, when the last location of the queue is occupied.

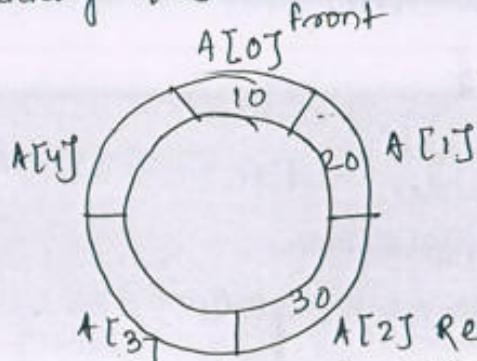
In other words, if an $A[\text{MAXSIZE}]$ represents a circular queue, then after inserting an element at $(\text{MAXSIZE} - 1)^{\text{th}}$ location of the array, the next element will be inserted at the very first location at index 0.

Advantage of circular queue over linear queue:

→ In case of linear queue, if Rear is at $\text{MAXSIZE} - 1$, then queue is considered as full. Here even though memory locations are vacant at beginning still we can not use them, as for each insertion rear is incremented and here REAR goes out of bounds. This drawback can be overcome by circular queue representation.

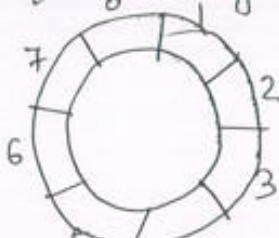
Circular Queue Representation:

Eg:- Let an array $A[5]$ is maintained in form of circular queue.

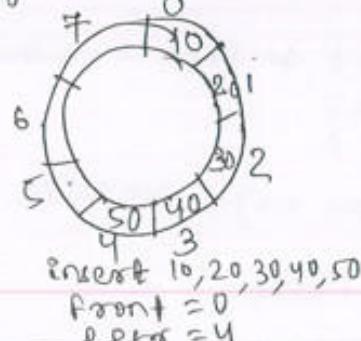


Here overflow situation arises only when Rear is before the front position.

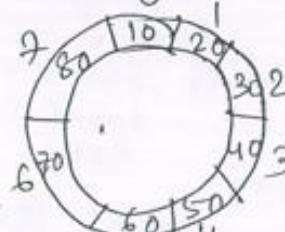
Eg:- When Queue is empty, the front = NULL or -1 and when Queue is full, the front = 0 and Rear = MAXSIZE - 1. When the queue having a single element the front = Rear.



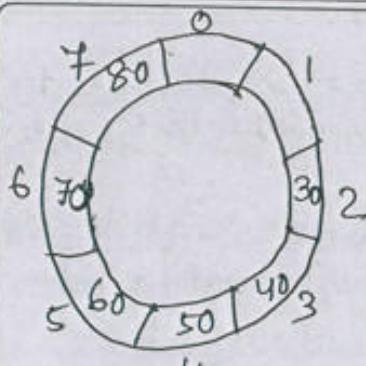
Queue is empty
Front = Rear = -1.



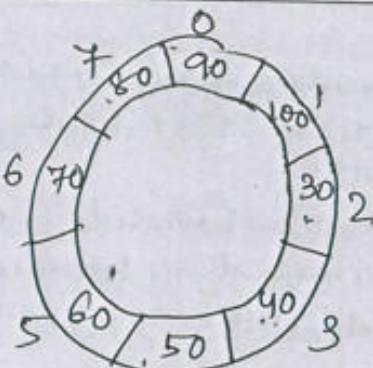
insert 10, 20, 30, 40, 50
front = 0
rear = 4



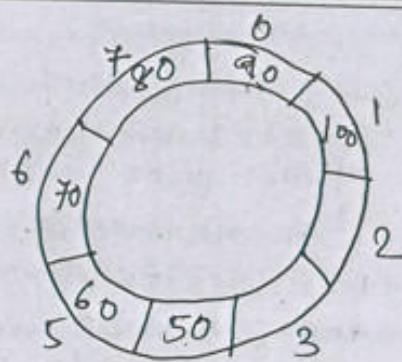
insert 60, 70, 80
front = 0 rear = 7
queue is full.



Delete two elements
front = 2
Rear = 7



Insert 90 and 100
front = 2
Rear = 1.



Delete 2 elements
front = 4
Rear = 1.

i) If Rear = MAXSIZE - 1, and free locations exist, then
 Rear = 0.

ii) If front = MAXSIZE - 1 and Rear is less than N, then
 front = 0.

During each insertion, to find the next Rear the
formula is :-

$$\text{Rear} = (\text{Rear} + 1) \% \text{MAXSIZE}$$

Similarly during each deletion to find the next front
position the formula is:-

$$\text{front} = (\text{front} + 1) \% \text{MAXSIZE}.$$

Algorithm for Insertion in a Circular Queue:

CGINSERT(QUEUE[MAXSIZE], ITEM)

Step 1: If (front = 0 and Rear = MAXSIZE - 1) or

(front = (Rear + 1) \% MAXSIZE), then

Display "Overflow"

Exit.

Step 2: Else if front = -1 or Rear = -1 then

front = 0

Rear = 0.

Step 3: Else

Rear = (Rear + 1) \% MAXSIZE

[End of if]
Step 4: QUEUE[Rear] = ITEM

Step 5: Exit.



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SUBJECT:- DATA STRUCTURE

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C - function:

void insertion(int A[], int item)

{ if ((front == 0) || rear == maxsize - 1) || (front == (rear + 1) % maxsize))

{ printf("In Queue overflow");
return;

else if (front == -1 || rear == -1)

{ front = 0;
rear = 0;

else

{ rear = (rear + 1) % maxsize;

A[rear] = item;

Algorithm for deletion in a circular queue:

(DELETION(QUEUE, FRONT, REAR))

Step 1: Let ITEM

Step 2: If Front = -1 or Rear = -1, then

Display "Queue is empty or Underflow"

Exit

[End of If]

Step 3: ITEM := QUEUE[Front]

Step 4: Display "Deleted Item is", ITEM.

Step 5: If front := Rear, then

front := -1

Rear := -1

Step 6: Else

front := (front + 1) % MAXSIZE

[End of If]

Step 7: Exit.



c-function:

```
void deletion(int A[])
{
    int item;
    if(front == -1 || rear == -1)
```

```
    printf("In Queue Underflow");
    return;
```

```
    item = A[front];
```

```
    if(front == rear)
```

```
        front = -1;
        rear = -1;
```

```
    else
```

```
        front = (front + 1) % maxsize;
```

```
    printf("The deleted item is %d", item);
```

```
}
```

C- Program implementing circular queue and its operation:

```
#include <stdio.h>
```

```
#define maxsize 5
```

```
int A[maxsize], front = -1, rear = -1, item;
```

```
void insertion(int [], int);
```

```
void deletion (int []);
```

```
void display (int []);
```

```
main()
```

```
{ int option;
```

```
do
```

```
{ printf("1. insert\n2. delete\n3. display\n4. exit\nEnter option");
```

```
scanf("%d", &option);
```

```
switch(option)
```

```
{ case 1: printf("Enter item");
```

```
scanf("%d", &item);
```

```
insertion(A, item);
```

```
break;
```

```

case 2: deletion();
break;
case 3: display();
break;
case 4: exit(0);
break;
default: printf("In Invalid option");
}

while(option != 4);

void insertion(int a[], int item)
{
    if((front == 0 || rear == maxsize - 1) || (front == (rear + 1) % maxsize))
    {
        printf("In queue overflow");
        return;
    }
    else if(front == -1 || rear == -1)
    {
        front = 0;
        rear = 0;
    }
    else
    {
        rear = (rear + 1) % maxsize;
        a[rear] = item;
    }
}

void deletion(int a[])
{
    int item;
    if(front == -1 || rear == -1)
    {
        printf("In Queue Underflow");
        return;
    }
    item = a[front];
    if(front == rear)
    {
        front = -1;
        rear = -1;
    }
}

```



else

{

front = (front + 1) % maxsize;

{

printf("In deleted item = %d", item);

{

void display(int A[])

{

int i;

{if (front == -1)}

{

{if (front == rear)}

{

printf("No items at queue\n");

for (i = front; i <= rear; i++)

printf("\t% d", A[i]);

{

else

{

printf("No items at queue\n\n");

for (i = front; i < maxsize; i++)

printf("\t% d", A[i]);

for (i = 0; i <= rear; i++)

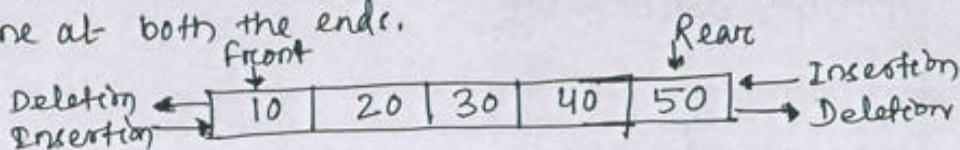
printf("\t% d", A[i]);

{}

{}

Double Ended Queue (DEQUE)

1. It is a kind of queue, in which the elements can be added or removed at either ends but not in the middle. In other words, it is a linear list in which insertion and deletion can be done at both the ends.



2. There are 2 forms of Deques such as:-
 a) Input Restricted Deque and b) Output Restricted Deque

a) Input Restricted Deque

- It is a deque, which restricts insertion at only one end, but allows deletion at both ends of the list. So in input-restricted deque, the following operations are possible:-

- i) Deletion at front end
- ii) Deletion at rear end
- iii) Insertion at front or Rear end.

b) Output Restricted Deque

- It is a deque, which restricts deletion at only end but allows insertion at both ends of the list. So, in output-restricted deque, the following operations are possible:-

- i) Insertion at front end
- ii) Insertion at Rear end
- iii) Deletion at front or Rear end.

3. As insertion and deletion is allowed at both end of deque, so the operations possible in deque are:-

- i) Insertion at Rear end (similar to linear queue)
- ii) Deletion at front end (similar to DLL)
- iii) Insertion at front end
- iv) Deletion at rear end.



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'C'-function for insertion at rear end of deque:

void dqinsert_rear (int A[], int ITEM)

{ if (rear == Maxsize - 1)

{ printf ("deque is full");

}

else

{ rear = rear + 1;

A[rear] = ITEM;

}

}

'C'-function for insertion at front end of deque:

void dqinsert_front (int A[], int front, int Rear, int ITEM, int maxsize)

{ if (front == 0)

{ printf ("deque is full");

}

else

{ front = front - 1;

A[FRONT] = ITEM;

}

}

'C'-function for deletion at front end of deque:

void dqdelete_front (int A[])

{ int ITEM;

{ if (front == -1)

{ printf ("deque is empty");

}

else if (front == Rear)

{ ITEM = A[front];

front = rear = -1;

printf ("Deleted item is %d", ITEM);

}

```
else ~
```

```
{ ITEM = Q[Front];
  Front = front + 1;
  printf("Deleted item is %d", ITEM);
```

y

C-function for deletion at rear end of deque :

```
void dqDeleteRear(int Q[])
```

{

```
int ITEM;
if (front == -1 || Rear == -1)
```

{

```
printf("Dequeue is empty");
```

```
exit(0);
```

y

```
ITEM = Q[Rear];
```

```
if (front == Rear)
```

{

```
front = Rear = -1;
```

y

```
else
```

{

```
Rear = Rear - 1;
```

y

```
printf("Deleted item is %d", ITEM);
```

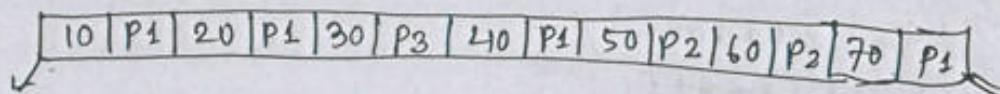
y

Priority Queue :

A priority queue is a collection of elements such that each element has a priority level and according to the priority level, the elements are deleted. In the queue, an element of higher priority is processed before any element of lower priority. When two or more elements have same priority levels then they are processed according to the order in which they



are added to the queue.



Deletion :

Insertion,

2. Priority queues are classified into two categories.
They are :-

i) Ascending priority queue.

ii) Descending priority queue.

Ascending priority queue : It is a collection of elements in which the items or elements are inserted randomly and from which the smallest element can be deleted.

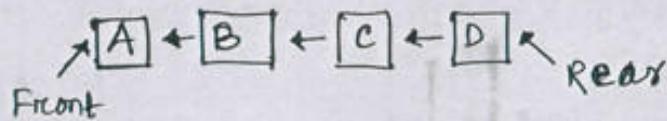
Descending priority queue : It is a collection of elements in which the items or elements are inserted randomly and from which the largest element can be deleted.

-X-

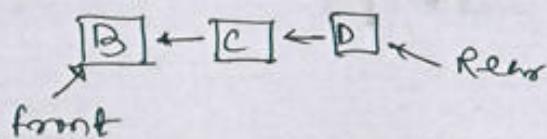
Queue:

1. Queue is a linear non-primitive data structure, works on the concept First in first out (FIFO), where insertion takes place at one end called REAR end and Deletion takes place at other end called Front end.

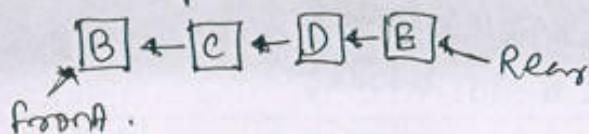
Eg :- Consider below a list of elements exist.



After deleting an element from Front end :-



After inserting element 'E' at Rear end :-



Memory Representation of Queue:

1. Array Representation :-

The concept of static memory allocation can be implemented by using ~~linked list~~ to represent a one dimensional array to represent a queue in memory. We consider two variables FRONT and REAR which holds the index of front and rear end of the queue.

2. Linked Representation :-

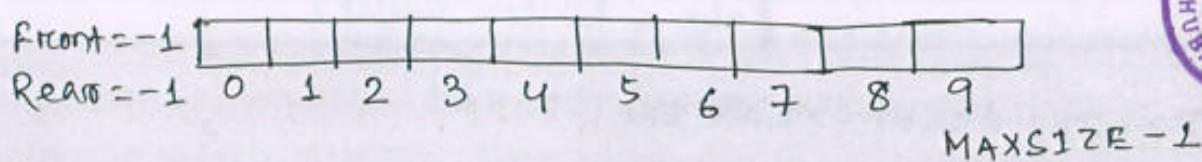
The concept of dynamic memory allocation is implemented by using linked list to represent queue in linked format.

Types of Queues :

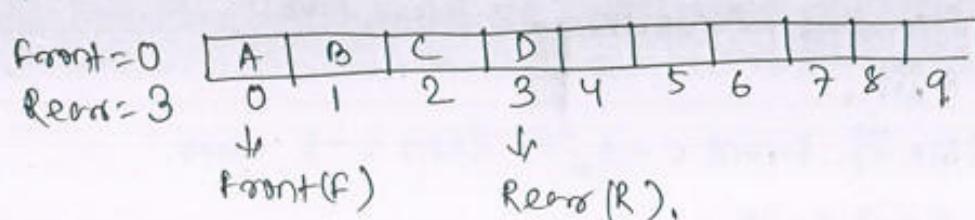
1. Linear Queue : Insertion Operation and Deletion operation :

1. In the Queue, while inserting a new element, one must test whether there is a room available at Rear end or not if room is available then the element can be inserted, otherwise Overflow situation occurs i.e.: Queue is full.
2. Deletion of an element can be done from the room that is identified by FRONT and FRONT will identify the next room of the queue. Underflow situation occurs when no element is present in the queue, i.e. when front and rear identified NULL and deletion operation is performed on it.

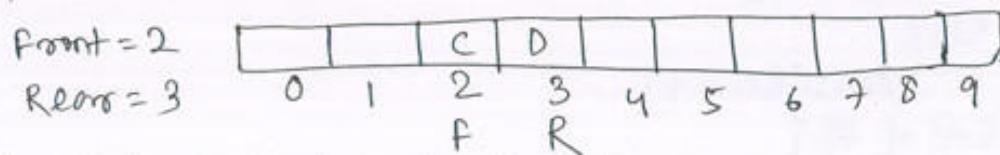
Eg:- Let $Q[\text{MAXSIZE}]$ is an array that represents a queue in the memory and at the beginning, it is empty, and $\text{MAXSIZE} = 10$, i.e.: $\text{Front} = \text{Rear} = \text{NULL} \text{ or } -1$.



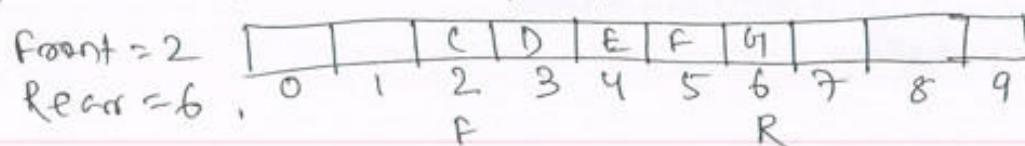
i) Insert 4 elements A, B, C, D.



ii) Delete 2 elements



iii) Insert 3 elements E, F, G.





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From the example, it is clear that-

i) For each insertion in the queue the value of REAR is incremented by 1 i.e.: $REAR = REAR + 1$.

ii) For each deletion in the queue the value of FRONT is incremented by 1 i.e.: $FRONT = FRONT + 1$.

Note :-

1. After all the elements inserted into the Queue, Rear will identify position at $MAXSIZE - 1$. i.e.- Queue is full.
2. Even though the memory location are vacant at FRONT end, where Rear identified $MAXSIZE - 1$ position, we can't insert a new element.
3. When $Front = Rear = \text{Null}$ (i.e.- queue is empty), we can't perform deletion operation.
4. When $Front = Rear$ only one element is present in Queue.
5. When Front is at $MAXSIZE - 1$, means Queue having one element. After deletion Front need to be reset to NULL.

Algorithm for insertion into a Linear Queue:

QINSERT (QUEUE[MAXSIZE], ITEM)

Step 1: If $Rear = MAXSIZE - 1$, then
Display "Overflow Or Queue Full"
Exit.

Step 2: Else If $front = -1$, or $Rear = -1$, then

$front := 0$

$Rear := 0$

Step 3: Else

$Rear := Rear + 1$

[End of if]

Step 4: $QUEUE[Rear] := ITEM$

Step 5: Exit.

C-function:

```
void insertion (int Q[], int item)
{
    if (rear == maxsize - 1)
    {
        printf ("In queue overflow");
        exit (0);
    }
    else if (front == -1 || rear == -1)
    {
        front = 0;
        rear = 0;
    }
    else
    {
        rear = rear + 1;
    }
    Q[rear] = item;
}
```



Algorithm for deletion in a linear queue:

Assume QUEUE[MAXSIZE] is an array which represents a queue, FRONT and REAR identifies the index of front and rear end respectively. ITEM holds the element to be deleted from queue.

QDELETE (QUEUE[MAXSIZE])

Step 1: Get ITEM

Step 2: If front = -1 or rear = -1, then

Display "Underflow" or Queue empty"

Exit

[End of If]

Step 3: ITEM := QUEUE[front]

Step 4: Display "Deleted Item is", ITEM

Step 5: Else If front = rear, then [when queue has only one element]

front := -1

rear := -1

Step 6: Else

front := front + 1.

Step 7: Exit.

C-function:

```
void deletion(int A[])
{
    int item;
    if (front == -1 || rear == -1)
        printf("In queue underflow");
    exit(0);
    item = A[front];
    if (front == rear)
    {
        front = -1;
        rear = -1;
    }
    else
    {
        front = front + 1;
        printf("In deleted item is %d", item);
    }
}
```

C-Program for implementing Linear queue:

```
#include<stdio.h>
#include<process.h>
#define maxsize 10
int A[maxsize], front = -1, rear = -1, item;
void insertion(int[], int);
void deletion(int[]);
void display(int[]);
main()
{
    int option;
    do
    {
        printf("1. insert\n2. delete\n3. display\n4. exit\n");
        scanf("%d", &option);
        switch(option)
        {
            case 1:
                insertion(A, rear);
                break;
            case 2:
                deletion(A);
                break;
            case 3:
                display(A);
                break;
            case 4:
                exit(0);
        }
    } while(option != 4);
}
```

```
switch(option)
```

```
{ case 1: printf("\n enter item");
    scanf("%d", &item);
    insertion(Q, item);
```

```
    break;
```

```
case 2: deletion(Q);
    break;
```

```
case 3: display(Q);
    break;
```

```
case 4: exit(0);
    break;
```

```
default: printf("In Invalid entry");
```

```
}
```

```
while(option != 4);
```

```
void insertion(int Q[], int item)
```

```
{ if(rear == maxsize - 1)
```

```
{ printf("\n queue overflow");
    exit(0); }
```

```
else if(front == -1 || rear == -1)
```

```
{ front = 0;
    rear = 0; }
```

```
else { rear = rear + 1;
    Q[rear] = item; }
```

```
}
```



`void deletion(int Q[])`

{ int item;

if (front == -1 || rear == -1)

{ printf("In Queue Underflow");
exit(0);

{ item = Q[front];

if (front == rear)

{ front = -1;

rear = -1;

else { front = front + 1;

printf("In deleted item is %d", item);

`void display(int Q[])`

{ int i;

if (front != -1)

{ printf("Elements at queue\n");

for (i = front; i <= rear; i++)

printf(" %d", Q[i]);

.

SUBJECT:- DATA STRUCTURE

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Circular Queue:

1. It is a queue of circular nature, in which it is possible to insert a new element at the first location, when the last location of the queue is occupied.

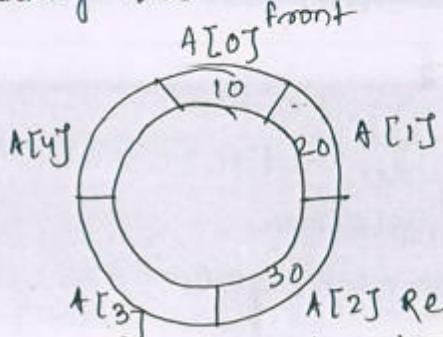
In other words, if an $A[0:MAXSIZE]$ represents a circular queue, then after inserting an element at $(MAXSIZE - 1)^{th}$ location of the array, the next element will be inserted at the very first location at index 0.

Advantage of circular queue over linear queue:

→ In case of linear queue, if Rear is at $MAXSIZE - 1$, then queue is considered as full. Here even though memory locations are vacant at beginning still we can not use them, as for each insertion rear is incremented and here REAR goes out of bounds. This drawback can be overcome by circular queue representation.

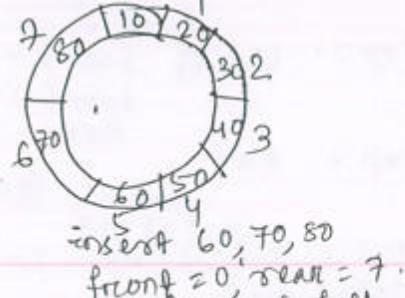
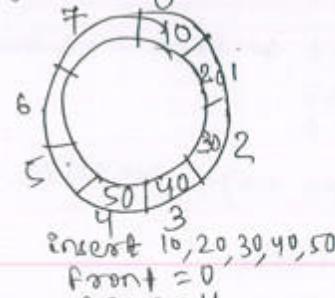
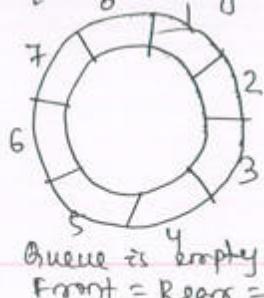
Circular Queue Representation:

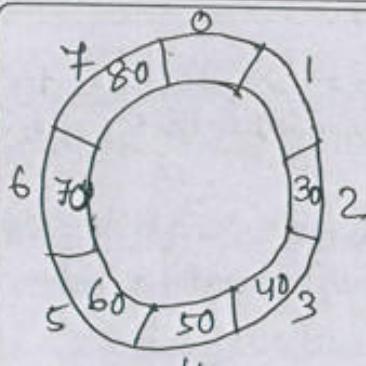
Eg:- Let an array $A[5]$ is maintained in form of circular queue.



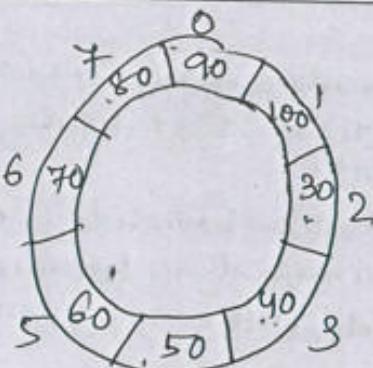
Here overflow situation arises only when Rear is before the front position.

Eg:- When Queue is empty, the front = NULL or -1 and when Queue is full, the front = 0 and Rear = MAXSIZE - 1. When the queue having a single element the front = Rear.

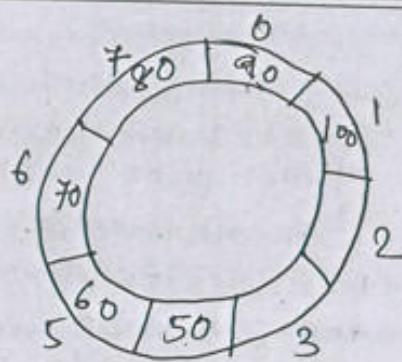




Delete two elements
front = 2
Rear = 7



Insert 90 and 100
front = 2
Rear = 1.



Delete 2 elements
front = 4
rear = 1.

ii) If Rear = MAXSIZE - 1, and free locations exist, then
 Rear = 0.

iii) If front = MAXSIZE - 1 and rear is less than N, then
 front = 0.

During each insertion, to find the next Rear the
formula is :-

$$\text{Rear} = (\text{Rear} + 1) \% \text{MAXSIZE}$$

Similarly during each deletion to find the next front
position the formula is:-

$$\text{front} = (\text{front} + 1) \% \text{MAXSIZE}.$$

Algorithm for Insertion in a Circular Queue:

CGINSERT(QUEUE[MAXSIZE], ITEM)

Step 1: If (front = 0 and Rear = MAXSIZE - 1) or

(front = (Rear + 1) \% MAXSIZE), then

Display "Overflow"

Exit.

Step 2: Else if front = -1 or Rear = -1 then

front = 0

Rear = 0.

Step 3: Else

Rear = (Rear + 1) \% MAXSIZE

Step 4: QUEUE[Rear] = ITEM
[End of if]

Step 5: Exit.

C - function:

```

void insertion(int A[], int item)
{
    if ((front == 0 && rear == maxsize - 1) || (front == (rear + 1) % maxsize))
        printf("In Queue overflow");
    return;
}
else if (front == -1 && rear == -1)
{
    front = 0;
    rear = 0;
}
else
{
    rear = (rear + 1) % maxsize;
}
A[rear] = item;
}

```

Algorithm for deletion in a circular queue:

(DELETION(QUEUE, FRONT, REAR))

Step 1: Let ITEM

Step 2: If Front = -1 or Rear = -1, then

Display "Queue is empty or Underflow"

Exit

[End of if]

Step 3: ITEM := QUEUE[Front]

Step 4: Display "Deleted Item is", ITEM.

Step 5: If front := Rear, then

Front := -1

Rear := -1

Step 6: Else

front := (front + 1) % MAXSIZE

[End of if]

Step 7: Exit.



c-function:

```
void deletion(int A[])
{
    int item;
    if (front == -1 || rear == -1)
```

```
    printf("In Queue Underflow");
    return;
```

```
    item = A[front];
```

```
    if (front == rear)
```

```
        front = -1;
        rear = -1;
```

```
    else
```

```
        front = (front + 1) % maxsize;
```

```
    printf("The deleted item is %d", item);
```

```
}
```

C- Program implementing circular queue and its operation:

```
#include <stdio.h>
```

```
#define maxsize 5
```

```
int A[maxsize], front = -1, rear = -1, item;
```

```
void insertion(int [], int);
```

```
void deletion (int []);
```

```
void display (int []);
```

```
main()
```

```
{ int option;
```

```
do
```

```
{ printf("1. insert\n2. delete\n3. display\n4. exit\nEnter option");
```

```
scanf("%d", &option);
```

```
switch(option)
```

```
{ case 1: printf("Enter item");
```

```
scanf("%d", &item);
```

```
insertion(A, item);
```

```
break;
```

```

case 2: deletion();
break;
case 3: display();
break;
case 4: exit(0);
break;
default: printf("In Invalid option");
}

while(option != 4);

void insertion(int a[], int item)
{
    if((front == 0 || rear == maxsize - 1) || (front == (rear + 1) % maxsize))
    {
        printf("In queue overflow");
        return;
    }
    else if(front == -1 || rear == -1)
    {
        front = 0;
        rear = 0;
    }
    else
    {
        rear = (rear + 1) % maxsize;
        a[rear] = item;
    }
}

void deletion(int a[])
{
    int item;
    if(front == -1 || rear == -1)
    {
        printf("In Queue Underflow");
        return;
    }
    item = a[front];
    if(front == rear)
    {
        front = -1;
        rear = -1;
    }
}

```





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SUBJECT:- DATA STRUCTURE

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else

{
 front = (front + 1) % maxsize;
 printf ("In deleted item = %d", item);
}

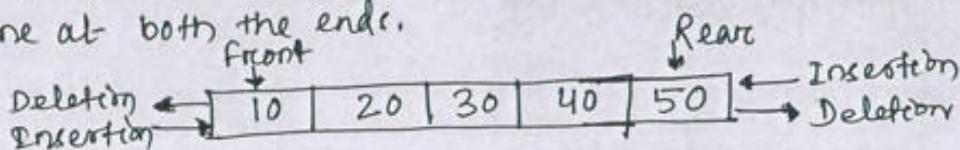
void display (int A[])

{
 int i;
 if (front == -1)
 {
 if (front == rear)
 {
 printf ("No items at queue\n");
 for (i = front; i <= rear; i++)
 printf ("\t%d", A[i]);
 }
 }
}

else
{
 printf ("No items at queue\n");
 for (i = front; i < maxsize; i++)
 printf ("\t%d", A[i]);
 for (i = 0; i <= rear; i++)
 printf ("\t%d", A[i]);
}

Double Ended Queue (DEQUE)

1. It is a kind of queue, in which the elements can be added or removed at either ends but not in the middle. In other words, it is a linear list in which insertion and deletion can be done at both the ends.



2. There are 2 forms of Deques such as:-
 a) Input Restricted Deque and b) Output Restricted Deque

a) Input Restricted Deque

- It is a deque, which restricts insertion at only one end, but allows deletion at both ends of the list. So in input-restricted deque, the following operations are possible:-

- i) Deletion at front end
- ii) Deletion at rear end
- iii) Insertion at front or Rear end.

b) Output Restricted Deque

- It is a deque, which restricts deletion at only end but allows insertion at both ends of the list. So, in output-restricted deque, the following operations are possible:-

- i) Insertion at front end
- ii) Insertion at Rear end
- iii) Deletion at front or Rear end.

3. As insertion and deletion is allowed at both end of deque, so the operations possible in deque are:-

- i) Insertion at Rear end (similar to linear queue)
- ii) Deletion at front end (similar to all linear queue)
- iii) Insertion at front end
- iv) Deletion at rear end.



C - function for insertion at rear end of deque :

```
void dqinsert_rear (int A[], int ITEM)
```

```
{ if (rear == Maxsize - 1)
```

```
{ printf ("deque is full");
```

```
}
```

```
else
```

```
{ Rear = Rear + 1;
```

```
A[Rear] = ITEM;
```

```
}
```

C - function for insertion at front end of deque :

```
void dqinsert_front (int A[], int front, int Rear, int ITEM, int maxsize)
```

```
{ if (front == 0)
```

```
{ printf ("deque is full");
```

```
}
```

```
else
```

```
{
```

```
front = front - 1;
```

```
A[FRONT] = ITEM;
```

```
}
```

C - function for deletion at front end of deque :

```
void dqdelete_front (int A[])
```

```
{ int ITEM;
```

```
if (front == -1)
```

```
{ printf ("deque is empty");
```

```
}
```

```
else if (front == Rear)
```

```
{ ITEM = A[front];
```

```
front = Rear = -1;
```

```
printf ("Deleted item is o.d.", ITEM);
```

```
}
```

```
else ~
```

```
{ ITEM = Q[Front];
  Front = front + 1;
  printf("Deleted item is %d", ITEM);
```

y

C-function for deletion at rear end of deque :

```
void dqDeleteRear(int Q[])
```

{

```
int ITEM;
if (front == -1 || Rear == -1)
```

{

```
printf("Dequeue is empty");
```

```
exit(0);
```

y

```
ITEM = Q[Rear];
```

```
if (front == Rear)
```

{

```
front = Rear = -1;
```

y

```
else
```

{

```
Rear = Rear - 1;
```

y

```
printf("Deleted item is %d", ITEM);
```

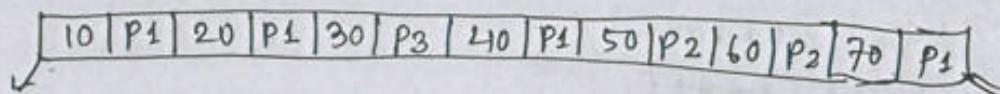
y

Priority Queue :

A priority queue is a collection of elements such that each element has a priority level and according to the priority level, the elements are deleted. In the queue, an element of higher priority is processed before any element of lower priority. When two or more elements have same priority levels then they are processed according to the order in which they



are added to the queue.



Deletion :

Insertion,

2. Priority queues are classified into two categories.
They are :-

i) Ascending priority queue.

ii) Descending priority queue.

Ascending priority queue : It is a collection of elements in which the items or elements are inserted randomly and from which the smallest element can be deleted.

Descending priority queue : It is a collection of elements in which the items or elements are inserted randomly and from which the largest element can be deleted.

-X-



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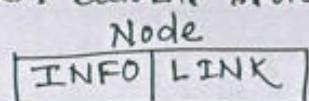
Data Structure Using C

Topic:
Linked List

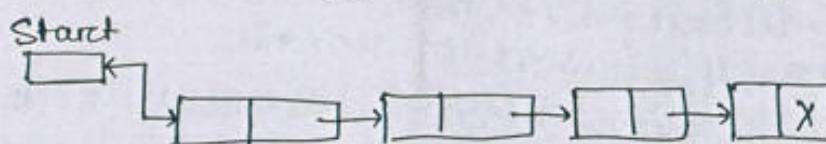
Contributed By:
Nihar Ranjan Rout
Gandhi Institute For Technology, GIFT

LINKED LIST:

1. Linked List is a linear collection of data elements called nodes, each of which is a memory location that contains two parts. That is:-
- i) Information of element or data.
 - ii) Link field contains the address of next node or points to the next element stored in the list.



[Structure of a node in linked list]



2. Here start is an external pointer which identifies address of 1st Node. i.e. the beginning of the linked list. The address of Link part of last node contains NULL as no further nodes exist.
3. The INFO part contains the value and the link points to the next node. To create a node of linked list, self referential structure is needed.

Dynamic Storage Management:iii) static Memory Allocation:

static memory allocation is the one in which the required memory is allocated at compile time.
e.g:- arrays are the best example of static memory allocation.

Drawbacks of static memory allocation:

Static memory allocation has the following drawbacks.

i) Size is fixed before execution.

ii) Insertion and deletion is a time taking process as the elements need to be shifted towards left or right.

iii) There may be a possibility that memory may get wasted or memory is deficit.



iii) Dynamic Memory Allocation:

Dynamic memory allocation in which the required memory is allocated at runtime. Eg:- linked lists are the best example of dynamic memory allocation. The drawbacks of static memory allocation can be overcome by dynamic memory allocation.

Advantages of Linked List:

1. A Linked List has the following advantages over arrays.
 - i) The allocated size can be increased or decreased as per the requirement at runtime.
 - ii) Memory can be utilized efficiently as the programmer can choose exact amount of memory needed.
 - iii) The operations like insertion and deletion are less time consuming as compared to arrays.

Disadvantages of Linked List:

1. A linked list has few disadvantages. They are:-
 - i) It takes more memory space because each node contains a link or address part.
 - ii) Moving to a specific node directly like array is not possible.

How to declare structure of a node in C:

struct node

```
{ int info;
  struct node *link; // self referencing
};
```

```
struct node *P;
P = (struct node*) malloc(sizeof(struct node));
```

Note: If a pointer to a structure is declared as a structure element of same structure, called self referencing structure.

Basic Operations on Linked List :

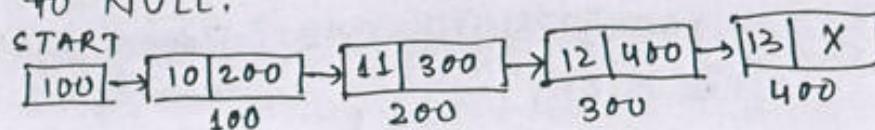
→ The basic operations that can be performed on a linked list are as follows:-

- i) Creation
- ii) Insertion
- iii) Deletion
- iv) Traversing
- v) Searching
- vi) Sorting
- vii) Concatenation

Types of Linked List :

i. Singly Linked List :

1. It is a collection of nodes where each node contains the address of next node. It is also referred as one-way list as traversing is possible in only one direction i.e.: - from START to NULL.



Memory Allocation:

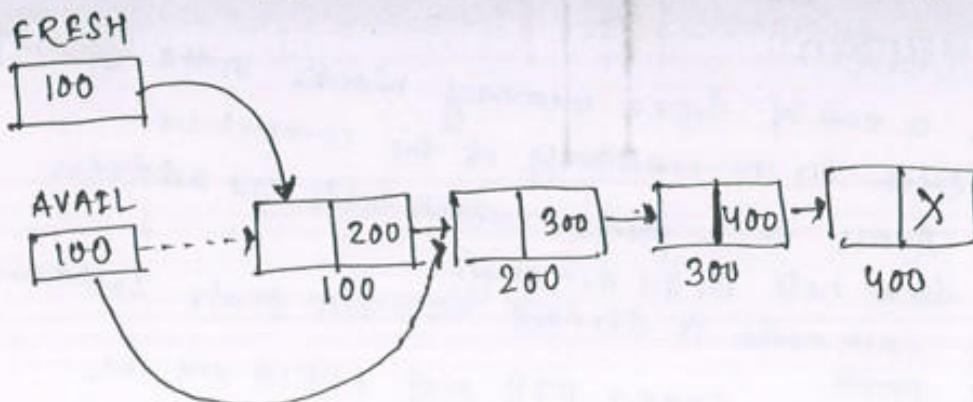
1. Assume a set of free memory blocks in the form of nodes exist in the memory of the computer.
2. Assume AVAIL is a pointer which holds the address first free node in the memory.
3. Assume each node is divided into two parts INFO and LINK parts.
Suppose START, PTR and FRESH are the pointers where,
 - i) START identifies the address of first node of linked list
 - ii) FRESH identifies the new node to be added to a linked list.
 - iii) PTR will be used to move between linked lists,



- When $AVAIL = \text{NULL}$, it indicates that no free memory blocks exist in the memory. At this point of time, if we try to create a new node overflow situation occurs.
 - When $START = \text{NULL}$, it indicates that linked list has no nodes or linked list doesn't exist. At this point of time if we try to delete a node from linked list it leads to underflow situation.
4. The following pseudocode checks for availability of memory and a new node is prepared if free memory is available otherwise displays an overflow message.

Step 1: If $AVAIL = \text{NULL}$, Then
 Display "Insufficient Memory or Overflow"
 Exit.

Step 2: Else
 $FRESH := AVAIL$ [FRESH is assigned with node as pointed by AVAIL]
 $AVAIL := \text{LINK}[AVAIL]$ [AVAIL now holds address of next available free node]
 $\text{INFO}[FRESH] := ITEM$ [INFO part of FRESH is updated with ITEM]
 $\text{LINK}[FRESH] := \text{NULL}$ [Address of LINK part is assigned with NULL]
 [End of IF]



SUBJECT:- **DATA STRUCTURE**

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Operations on a single linked list :-

1. Insertion of a node in a single linked list.

- a) Insertion at the beginning
- b) Insertion at the end
- c) Insertion at a specific location
- d) Insertion after a specific location
- e) Insertion after specified node.

2. Deletion of a node in a single linked list.

- a) Deletion at the beginning
- b) Deletion at the end
- c) Deletion of a node at specific location.
- d) Deletion of a node based on a given item or INFO

3. Searching for a node based on given item

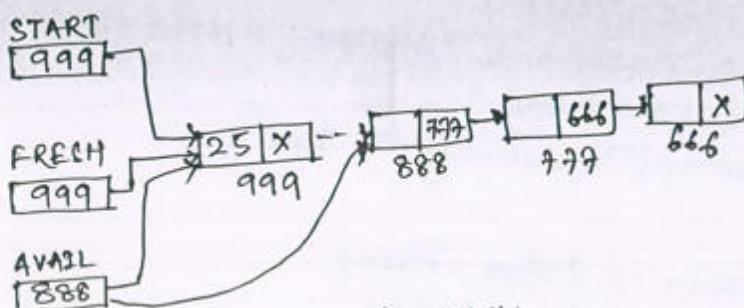
4. Concatenation of two linked lists.

5. Sorting the node INFO in a single linked list.

6. Reversing the single linked list.

1. Insertion of a node in a single linked list :-

a) Insertion at the beginning (when list is empty) :-



START initially contains NULL

After creation operation :-

- i) START points to node with address 999
- ii) AVAIL points to the next free node with address 888



Algorithm:

CREATION (AVAIL, INFO, LINK, START, FRESH, ITEM)

Step 1: If AVAIL = NULL, Then

Display "Insufficient Memory or Overflow"

Exit.

Step 2: Else

FRESH := AVAIL

AVAIL := LINK[AVAIL]

INFO[FRESH] := ITEM

LINK[FRESH] := NULL

START := FRESH

[End of IF]

Step 3: Exit

C-function:

struct node *create_list (struct node *start)

{ struct node *fresh;

int item;

printf("Enter item:");

scanf("%d", &item);

fresh = (struct node *) malloc (sizeof(struct node));

if (fresh == NULL)

printf("Memory is full");

else

{ fresh -> info = item;

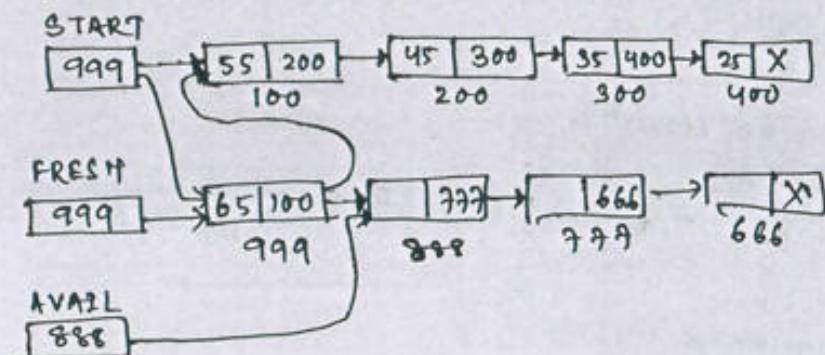
fresh -> link = NULL;

start = fresh;

} return start;

}

b) Insertion at the beginning (when linked list has one or more nodes):



START initially contains the 1st node address i.e.: - 100,
After insertion operation :-

- i) START points to node with address 999
- ii) Node with address 999 points to the address 100
- iii) AVAIL points to the next free node with address 888.

Algorithm:

INSERTFIRST(INFO, LINK, START, AVAIL, ITEM)

Step 1: If AVAIL = NULL, Then

Display "Memory insufficient or overflow"

Exit.

[End of If]

Step 2: If START = NULL, Then

START := FRESH

Step 3: Else

FRESH := AVAIL

AVAIL := LINK[AVAIL]

INFO[FRESH] := ITEM

LINK[FRESH] := START.

START := FRESH

[End of If]

Step 3: Exit.



c-function :-

struct node * insert - first (struct node * start)

{ struct node * fresh;

int item;

printf (" \n enter an item ");

scanf ("%d", &item);

fresh = (struct node *) malloc (sizeof (struct node));

if (fresh == NULL)

printf (" \n memory is full ");

else

{ fresh -> info = item;

fresh -> link = NULL;

if (start == NULL)

{ start = fresh;

}

else

{ fresh -> link = start;

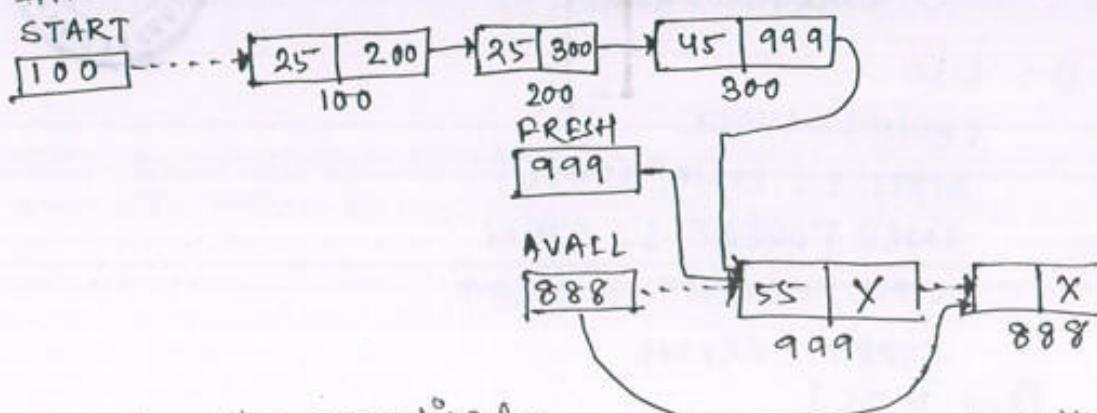
start = fresh;

}

return start;

}

c) Insertion at the end of a single linked list :-



After insertion operation :-

The last node with address 300 points to node with address 999 sets to NULL
999 and link part of Node with address 999 sets to NULL
and AVAIL points to the next free node with address 888.

Algorithm:

INSERTEND (INFO, LINK, START, AVAIL, ITEM)

Step 1 : Let PTR

Step 2 : If AVAIL = NULL, then display "Memory Insufficient or overflow".
Exit.

Step 3 : Else

FRESH := AVAIL

AVAIL := LINK[AVAIL]

INFO[FRESH] := ITEM

LINK[FRESH] := NULL

Step 3.1 : If START = NULL, then
 START := FRESH

Step 3.2 : else

PTR := START

Repeat while LINK[PTR] != NULL
 PTR := LINK[PTR]

[End of while]

LINK[PTR] := FRESH

[End of step 3.1]

[End of step 2]

Step 4 : Exit.

C-function:

struct node *insert_last(struct node *start)

{ struct node *fresh, *ptr;

int item;

printf("\n enter item");

scanf("%d", &item);

fresh = (struct node *) malloc(sizeof(struct node));

If(fresh == NULL)

 printf("\n memory is full");

else

 fresh->info = item;

 fresh->link = NULL;

 If(start == NULL)

 start = fresh;

 else
 for (ptr = start; ptr->link != NULL; ptr = ptr->link);

 ptr->link = fresh;

 return start;



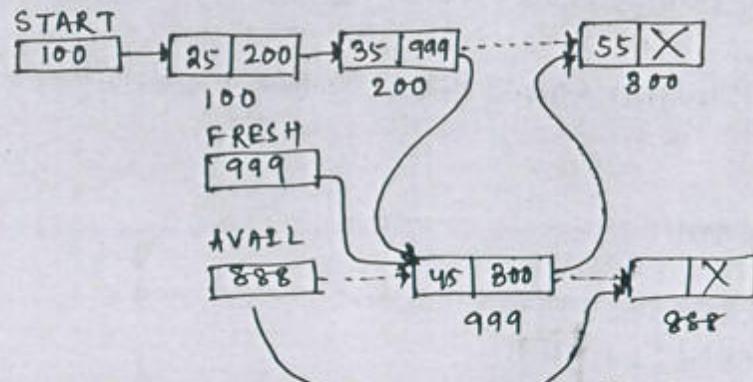


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SUBJECT:- DATA STRUCTURE

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a) Insertion at specific location of a Single Linked List :



When Loc = 3, after insertion operation :-

if the 2nd node with address 200 points to new node with address 999 and the link part of node with address 999 points to node with address 300. So, now the new node is inserted at location 3 and AVAIL points to the next free node having address 888.

Algorithm :-

`INSERTLOC(INFO, LINK, START, AVAIL, LOC, ITEM, PTR, PREV)`

Step 1 :- Let I := 1

Step 2 :- If AVAIL = NULL, then display "Memory insufficient"
 Exit.

Step 3 :- Else

 FRESH := AVAIL

 AVAIL := LINK[AVAIL]

 INFO[FRESH] := ITEM

 LINK[FRESH] := NULL

Step 3.1 :- If START = NULL, then display "List doesn't exist"

Step 3.2 :- Else

 Step 3.2.1 :- PTR := START

 Step 3.2.2 :- Repeat, while [LOC AND PTR] = NULL

 PREV := PTR

 PTR := LINK[PTR]

 I := I + 1

[End of while]

Step 3.2.3 :- If PTR = NULL, then display "Location not found"

Step 3.2.4 :- Else if PTR = START, then

 LINK[FRESH] := START

 START := FRESH

Step 3.2.5 : else

LINK[PREV] := PREV

LINK[FRESH] := PTR

[End of IF - Step 3.2.3]

[End of Step-3.1]

[End of Step-2]

Step 4 : Exit.

C-function :

```
struct node *insert_loc(struct node *start)
```

```
{ struct node *frosh, *ptr, *prev;
```

```
int item, loc, i;
```

```
frosh = (struct node *) malloc(sizeof(struct node));
```

```
if(frosh == NULL)
```

```
{ printf("In memory is full");
```

```
}
```

```
else
```

```
{ printf("Enter item and location for insertion");
```

```
scanf("%d%d", &item, &loc);
```

```
frosh->info = item;
```

```
frosh->link = NULL;
```

```
if(start == NULL)
```

```
{ printf("List does not exist");
```

```
}
```

```
else
```

```
{ ptr = start;
```

```
i = 1;
```

```
while(i < loc && ptr != NULL)
```

```
{ prev = ptr;
```

```
ptr = ptr->link;
```

```
i++;
```

```
if(ptr == NULL)
```

```
{ printf("Invalid entry of location");
```

```
}
```



```

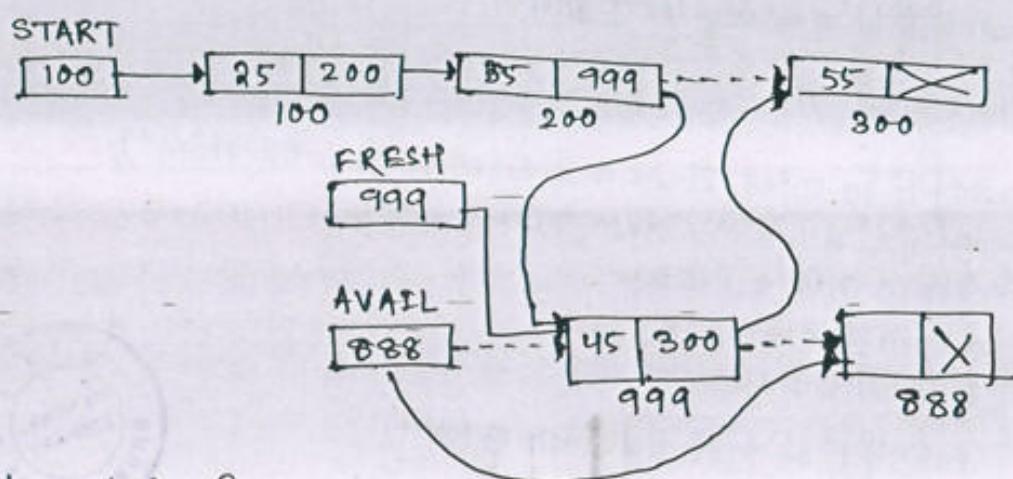
else if (ptr == start)
{
    // insertion at beginning
    fresh->link = ptr;
    start = fresh;
}

else
{
    prev->link = fresh;
    fresh->link = ptr;
}

return start;
}

```

e) Insertion after specific location in a single linked list :-



When loc = 2,

After insertion operation :-

The 2nd node with address 200 points to new node with address 999 and the link part of node with address 999 points to node with address 300. So, now the new node inserted after location 2 and AVAIL points to the next free node with address 888.

Algorithm :-

INSERTAFTERLOC(INFO, LINK, START, AVAIL, LOC, ITEM, PTR)

Step 1 : Let I.

Step 2 : If AVAIL = NULL, then Display "Memory Insufficient"
Exit.

Step 3 : Else

FRESH := AVAIL

AVAIL := LINK[AVAIL]

INFO[FRESH] := ITEM

LINK[FRESH] := NULL

Step 3. 1 : If START = NULL, then Display "list does not exist".

Step 3. 2 : Else

Step 3. 2. 1 : PTR := START

Step 3. 2. 2 : Repeat for I = 1 to LOC - 1 increasing by 1.
PTR := LINK[PTR]

[End of FOR]

Step 3. 2. 3 : If PTR = NULL, Then

Display "Invalid entry for location"

Step 3. 2. 4 : else

LINK[FRESH] := LINK[PTR]

LINK[PTR] := FRESH

[End of IF - Step 3. 2. 3]

else [End of IF 3. 1 step]

[End of IF - step 2]

Step 4 : Exit.

C-function :-

struct node *insert-after-loc(struct node *start)

{ struct node *frosh, *ptr;

Ent item, loc, i;

frosh = (struct node *) malloc(sizeof(struct node));

If (frosh == NULL)

{ printf("Memory is full");

}



```

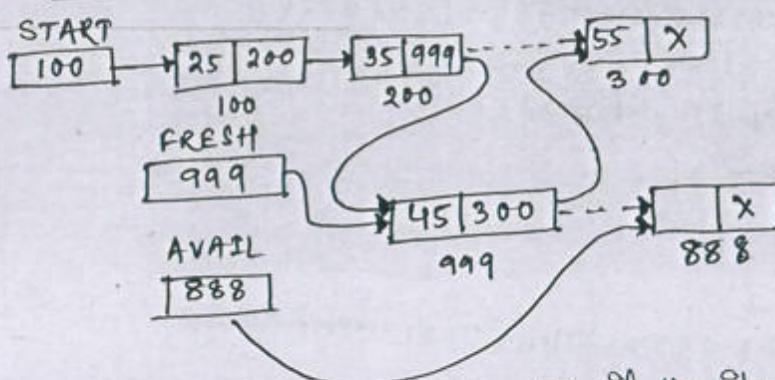
else
{
    printf("\n enter item");
    scanf("%d", &item);
    printf("\n enter location");
    scanf("%d", &loc);
    foresh->info = item;
    foresh->link = NULL;
    if (start == NULL)
        printf("list doesn't exist");
    else
        {
            ptrs = start;
            i = 1;
            while (i < loc || ptrs == NULL)
                {
                    ptrs = ptrs->link;
                    i++;
                }
            if (ptrs == NULL)
                printf("\n Invalid entry of location");
            else
                {
                    foresh->link = ptrs->link;
                    ptrs->link = foresh;
                }
        }
    return start;
}

```

SUBJECT:- DATA STRUCTURE

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f) Insertion of a node After specified node in single linked list :-



while searching for an item 85, if the item is available then insertion after that node is accomplished as follows :-
 Hence, the node with address 200 contains item ie:- 35, so node with address 200 points to new node with address 999 and the link part of node with address 999 points to the node with address 300. So, now the new node is inserted after the node having info part with value 35, and AVAIL points to the next free node with address 888.

Algorithm :-

INSERTAFTERNODE (INFO, LINK, START, ITEM, PTR, AVAIL, NEWITEM, FRESH)

Step 1 : START

Step 2 : If AVAIL = NULL, then Display "memory insufficient or Overflow"
 Exit

Step 3 : ELSE

FRESH := AVAIL

AVAIL := LINK[AVAIL]

INFO[FRESH] := NEWITEM

LINK[FRESH] := NULL

Step 3.1 : If START = NULL, then Display "list doesn't exist"

Step 3.2 : ELSE

Step 3.2.1 : PTR := START

Step 3.2.2 : Repeat while PTR != NULL AND ITEM != INFO[PTR]
 PTR := LINK[PTR]

[End of while]

Step 3.2.3 : If PTR = NULL then

Display "Item doesn't exist".



Step 3.2.4 : Else

LINK[FRESH] = LINK[PTR]

LINK[PTR] = FRESH

{End of If - step 3.1}

[End of If - step 2]

Step 4 : Exit.

C - Program:

```
struct node * insert_after_item(struct node * start)
```

```
{ struct node * fresh, * ptr;
```

```
int item, newItem;
```

```
fresh = (struct node *) malloc(sizeof(struct node));
```

```
if (fresh == NULL)
```

```
    printf("\n memory is full");
```

```
else
```

```
    printf("\n enter item to search and new item to insert").
```

```
scanf("%d %d", &item, &newItem);
```

```
fresh->info = newItem;
```

```
fresh->link = NULL;
```

```
if (start == NULL)
```

```
{ printf("\n list doesn't exist");
```

```
else
```

```
{
```

```
ptr = start;
```

```
while (item != ptr->info && ptr != NULL)
```

```
{ ptr = ptr->link;
```

```
}
```

```
if (ptr == NULL)
```

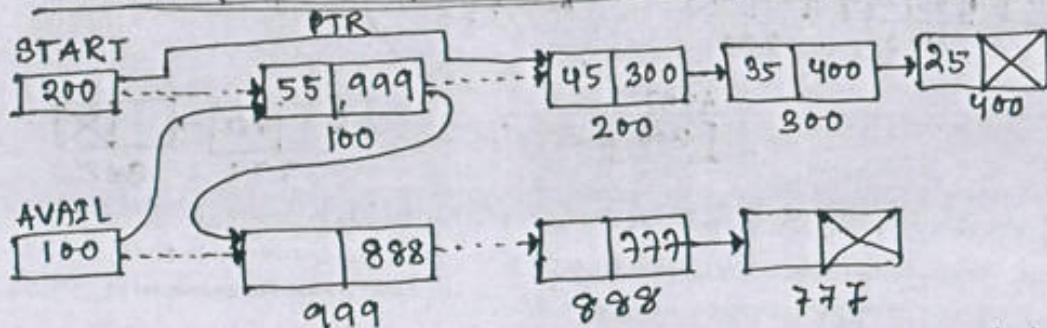
```
{ printf("\n item to search not exist");
```

```
else
```

```
{ fresh->link = ptr->link;
```

```
ptr->link = fresh;
```

```
return start;
```

2. Deletion from a Linked List :a) Deletion of first node from a single linked list :

Here the first node i.e. node with address 100 to be deleted. So, START will be updated with address of 2nd node which is present in the link part of first node as pointed by START. PTR is a pointer that points to first node with address 100 is added to the free or avail list at the beginning by updating link part of PTR with address of node as pointed by AVAIL and AVAIL is assigned with the address 100 as pointed by PTR}.

Algorithm:

DELETION FIRST(INFO, LINK, START, AVAIL, PTR)

Step 1: If START = NULL, Then
Display "List does not exist or Underflow"

Step 2: Else

PTR := START
START := LINK[PTR]
LINK[PTR] := AVAIL
AVAIL := PTR

[End of IF]

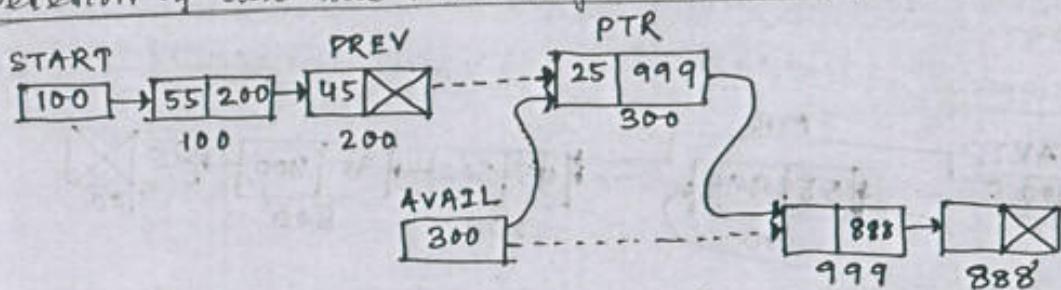
Step 3: Exit.

C-function:

```
struct node * delete_first( struct node * start )
{
    struct node * ptr;
    if( start == NULL )
        printf("\n memory underflow - list is empty");
    else
        ptr = start;
        start = start->link;
        free(ptr);
    return start;
}
```



b) Deletion of last node from single linked list :



Hence, the last node is pointed by PTR and last but one node is pointed by PREV. As the node pointed by PREV will become the last node, the link part of PREV with address 200 is updated with NULL. The node with address 300 as pointed by PTR is added at the beginning of free or avail list.

Algorithm 8

DELETIONEND(START, LINK, INFO, PTR, PREV, AVAIL)
 Step 1 : If START = NULL, then Display "List is empty".

Step 2 Else

Step 2.1 : PTR := START.

Step 2.2 : Repeat while LINK[PTR] != NULL

 PREV := PTR

 PTR := LINK[PTR]

[End of While]

Step 2.3 : LINK[PREV] := NULL

Step 2.4 : LINK[PTR] := AVAIL

Step 2.5 : AVAIL := PTR

[End of If]

Step 3 : Exit .

C - function :

struct node * delete - last (struct node * start)

{ struct node *ptr, *prev;

 if (start == NULL)

 printf ("\n memory underflow - list is empty");

 else {

 ptr = start;

 while (ptr->link != NULL)

 prev = ptr;

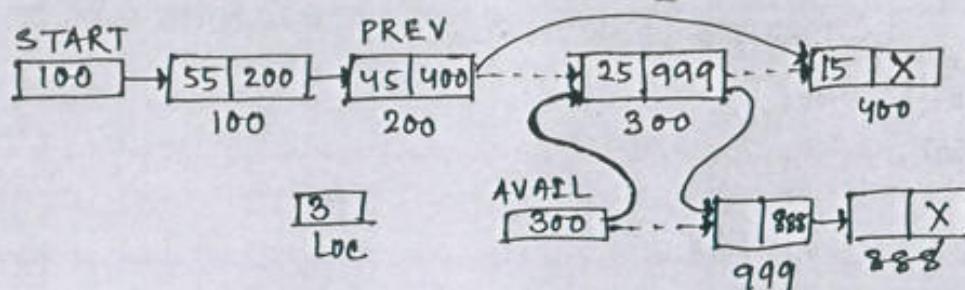
 ptr = ptr->link;

 prev->link = NULL;

 }

 return start;

c) Deletion of node from a specific location.



Hence loc is 3, i.e., node with address 300 is to be deleted. The link part of node with address 200 is updated with the link part of node with address 300 i.e., 400. Now the node pointed by PTR is added at the beginning of AVAIL list.

Algorithm:

DELETION LOC (INFO, LINK, START, PTR, PREV, LOC)

Step 1 : Let I := 1

Step 2 : PTR := START

Step 3 : Repeat, while $I < LOC \text{ AND } PTR \neq \text{NULL}$

 PREV := PTR

 PTR := LINK[PTR]

 I := I + 1

[End of While]

Step 4 : If PTR = NULL, then Display "Location Doesn't exist".

Step 5 : Else if PTR = START, then START := LINK[PTR]

Step 6 : Else LINK[PREV] := LINK[PTR]

[END of IF]

Step 7 : LINK[PTR] := AVAIL

Step 8 : AVAIL := PTR

Step 9 : Exit.

C-function:

struct node *delete_loc (struct node *start)

{ struct node *ptr, *prev;

int loc, i;

If (start == NULL)

{ printf ("In memory underflow - list is empty");

}





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SUBJECT:- DATA STRUCTURE

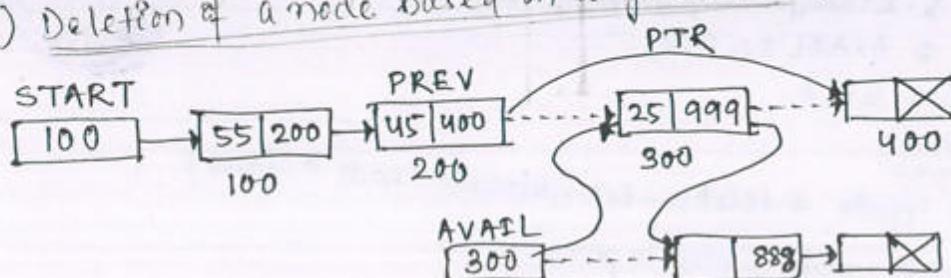
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```

else
{
    printf("Enter the location or node no. for deletion");
    scanf("%d", &loc);
    ptr = start;
    i = 1;
    while (i < loc && ptr != NULL)
    {
        pprev = ptr;
        ptr = ptr->link;
        i++;
    }
    if (ptr == NULL)
        printf("Location entered not exist");
    else if (ptr == start)
    {
        start = start->link;
        free(ptr);
    }
    else
    {
        pprev->link = ptr->link;
        free(ptr);
    }
}
return start;
}

```

d) Deletion of a node based on a given item :



Here we want to delete a node whose info part contains the value 25. PTR is pointing to the node with address 300 whose info part contains the item given i.e. 25 and PREV is pointing to node with address 200. The link part of node as pointed by PREV is updated with link part of node as pointed by PTR. Now, the node with address 300 as pointed by PTR is added at the beginning of free or avail list.

Algorithm :-

DELETION ITEM (LINK, INFO, START, PTR, PREV, AVAIL, ITEM)

Step 1 : PTR := START

Step 2 : Repeat While PTR != NULL AND ITEM != INFO[PTR]

 PREV := PTR

 PTR := LINK[PTR]

[End of While]

Step 3 : If PTR = NULL, Then Display "Item Not found"

Step 4 : Else If PTR = START, Then START := LINK[PTR]

Step 5 : Else LINK[PREV] := LINK[PTR]

[End of If]

Step 6 : LINK[PTR] := AVAIL

Step 7 : AVAIL := PTR

Step 8 : EXIT.

C-function :-

struct node * delete_item (struct node * start)

{ struct node *ptr, *prev;

int item;

if (start == NULL)

{ printf ("\n memory underflow - list is empty");

else

{ printf ("\n enter the item for deletion");

scanf ("%d", &item);

ptr = start;

while (item != ptr->info && ptr != NULL)

{ prev = ptr;

ptr = ptr->link;

if (ptr == NULL)

 printf ("\n location entered not exist");

else if (ptr == start)

{ start = start->link;

 free(ptr);



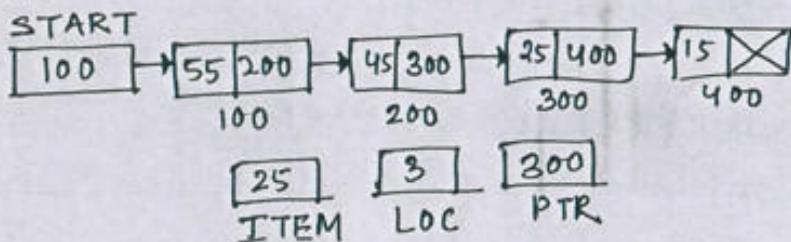
```

else
{
    pprev->link = ptr->link;
    free(ptr);
}

return start;
}

```

3. Search of a Node in a Single Linked List :-



Algorithm :-

SEARCHNODE(INFO, LINK, START, PTR, ITEM)

Step 1 : Let LOC := 0, F := 0

Step 2 : PTR := START

Step 3 : Repeat while PTR != NULL

 Step 3.1 : Set LOC := LOC + 1

 Step 3.2 : If ITEM == INFO[PTR], then

 F := 1

 BREAK

[END OF IF]

PTR := LINK[PTR]

[END OF WHILE]

Step 4 : If F == 0, Then Display "Item Not Found"

Step 5 : Else Display "Item Found at Location", LOC

[End of If]

Step 6 : Exit.

C-function :-

void searching(struct node *start)

{ int item, loc = 1;

struct node *ptr;

printf("In enter the item to search:");

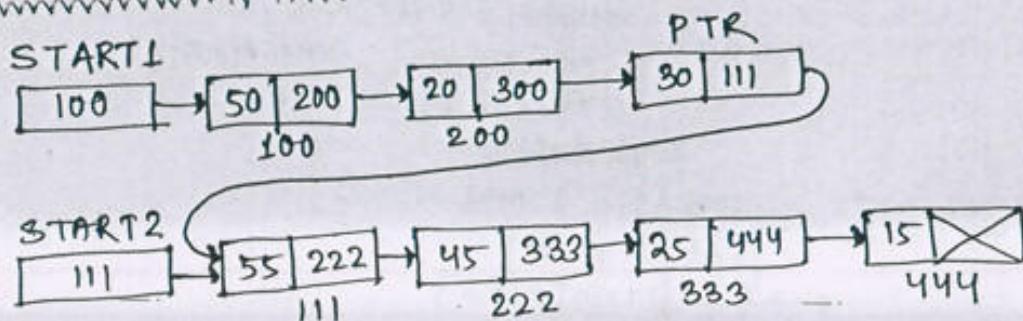
scanf("%d", &item);

```

ptr = start;
while (ptr != NULL && item != ptr->info)
{
    ptr = ptr->link;
    loc++;
}
if (ptr == NULL)
    printf("\n Item not found");
else
{
    printf("\n Item found at location = %d", loc);
}

```

4. Concatenation of two single linked lists:



Algorithm:

Step 1: Let PTR
 Step 2: PTR = START 1
 Step 3: Repeat While LINK[PTR] != NULL
 PTR = LINK[PTR]
 [End of While]

Step 4: LINK[PTR] = START 2
 Step 5: START2 = NULL
 Step 6: EXIT.

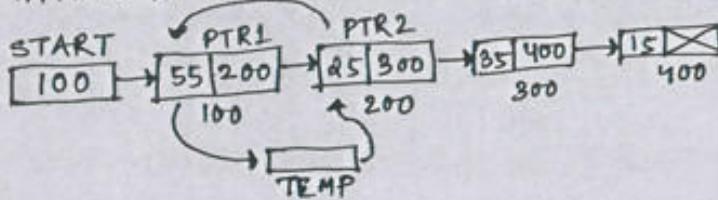
C function:
 struct node* concatenate (struct node *start1, struct node *start2)

```

{
    struct node *ptr;
    ptr = start1;
    while (ptr->link != NULL)
    {
        ptr = ptr->link;
        ptr->link = start2;
        start2 = NULL;
    }
    return start1;
}
```



5. Sorting of a single linked list :



Algorithm:

Sorting(START, INFO, LINK)

Step 1: Let PTR1, PTR2, TEMP

Step 2: PTR1 := START

Step 3: Repeat while LINK[PTR1] != NULL

Step 3.1: PTR2 := LINK[PTR1]

Step 3.2: Repeat while PTR2 != NULL

Step 3.2.1: If INFO[PTR1] > INFO[PTR2], then

TEMP := INFO[PTR1]

INFO[PTR1] := INFO[PTR2]

INFO[PTR2] := TEMP

[End of IF]

PTR2 := LINK[PTR2]

[End of while]

PTR1 := LINK[PTR1]

[End of while]

Step 4: Exit

C-function:

void sorting(struct node *start)

{ struct node *ptr1, *ptr2;

int temp;

ptr1 = start;

while (ptr1 → link != NULL)

{ ptr2 = ptr1 → link;

while (ptr2 != NULL)

{ if (ptr1 → info > ptr2 → info)

{ temp = ptr1 → info;

ptr1 → info = ptr2 → info;

ptr2 → info = temp;

{ ptr2 = ptr2 → link;

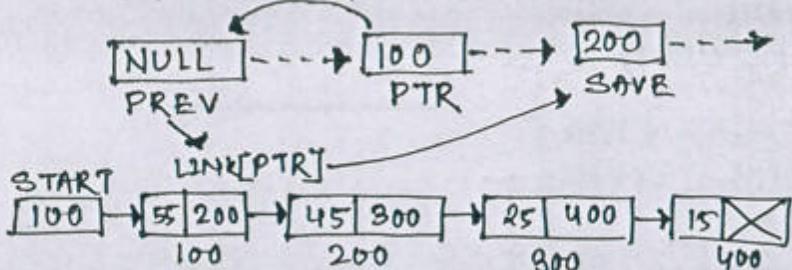
{ ptr1 = ptr1 → link;

SUBJECT:- DATA STRUCTURE

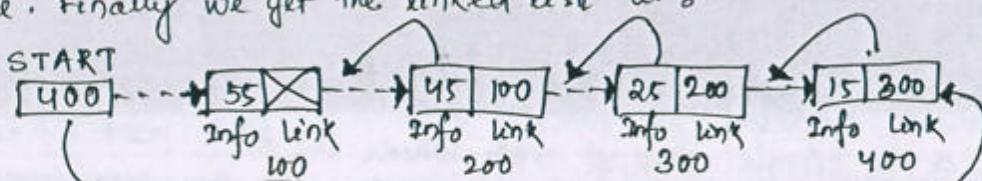
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6. Reversing a single Linked List :

- Reversing of single linked list means pointing the START pointer to the last node, then the last node link part have to point to its previous node and that node have to point to its previous node and so on till 1st node, whence the 1st node link part will point to NULL.



- Here for each node identified by PTR we need to connect it in reverse orders e.g. When PTR = 100, LINK[PTR] points to NULL as it becomes last node. Then PTR = SAVE to point to the next node. finally we get the linked list as :-



Algorithm :-

REVERSE(START, INFO, LINK)

Step 1 % Let PREV, SAVE, PTR

Step 2 % PTR % = START;

Step 3 % PREV % = NULL

Step 4 % Repeat while PTR != NULL

 SAVE % = LINK[PTR]

 LINK[PTR] % = PREV

 PREV % = PTR

 PTR % = SAVE

 [End of while]

Step 5 % START % = PREV

Step 6 % Exit ,



'C'- function:

```
struct node *reverse(struct node *start)
```

```
{ struct node *prev, *ptr, *save;
```

```
ptr = start;
```

```
prev = NULL;
```

```
while(ptr != NULL)
```

```
{ save = ptr->link;
```

```
ptr->link = prev;
```

```
prev = ptr;
```

```
ptr = save;
```

```
}
```

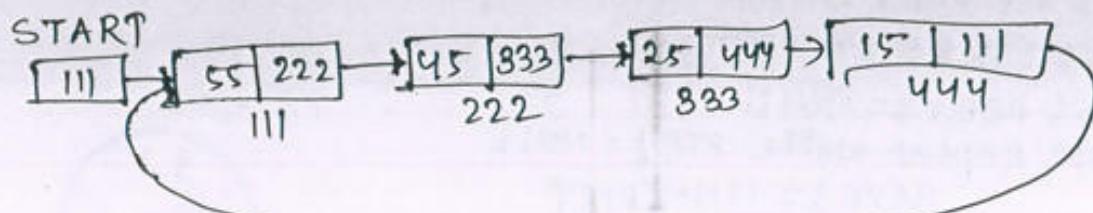
```
start = prev;
```

```
return start;
```

```
}
```

Circular Singly Linked List:

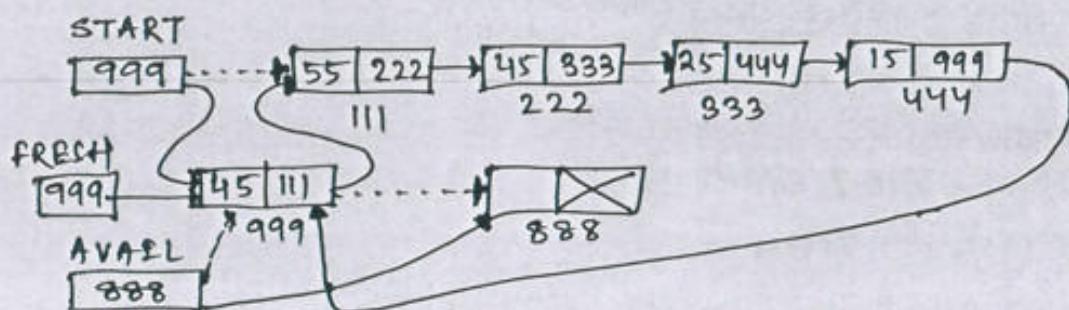
It is a single linked list where the link part of last node contains the address of first node. In other words, when we traverse a circular singly linked list, the first node can be visited after the last node.



Operations on Circular Singly Linked List :-

1. Insertion at the beginning
2. Insertion at the end
3. Deletion at the beginning
4. Deletion at the end.

1. Insertion of a node at the beginning:



Here, the FRESH node with address 999 is to be inserted. The INFO part of fresh node is updated with 111 which will become the 2nd node. The LINK part of last node i.e. node with address 444 is updated with address of fresh node 999. START is assigned with the address of fresh node 999.

Algorithm:

INSERTFIRST(START, INFO, LINK, AVAIL, FRESH, ITEM)

Step 1% if AVAIL=NULL, then display "memory Insufficient"

Step 2% ELSE

FRESH := AVAIL

AVAIL := LINK[AVAIL]

INFO[FRESH] := ITEM

LINK[FRESH] := NULL

Step 2.1% of START=NULL Then

START := FRESH

LINK[FRESH] := START

Step 2.2% ELSE

LINK[FRESH] := START

PTR := START

Repeat While LINK[PTR] != START

PTR := LINK[PTR]

[End of while]

LINK[PTR] := FRESH

START := FRESH

Step 3% Exit [End of IF]



C²- Functions :-

```
struct node *insertFirst(struct node *start)
```

```
{ struct node *first, *ptr;
```

```
int item;
```

```
printf("Enter an Item");
```

```
scanf("%d", &item);
```

```
first = (struct node *) malloc(sizeof(struct node));
```

```
if(first == NULL)
```

```
{ printf("Memory is full - overflow");
```

```
exit(0);
```

Y

```
else
```

```
{ first->info = item;
```

```
first->link = NULL;
```

```
if(start == NULL)
```

```
{ start = first;
```

```
first->link = start;
```

Y

```
else
```

```
{
```

```
for(ptr = start; ptr->link != start; ptr = ptr->link),
```

```
ptr->link = first;
```

```
first->link = start;
```

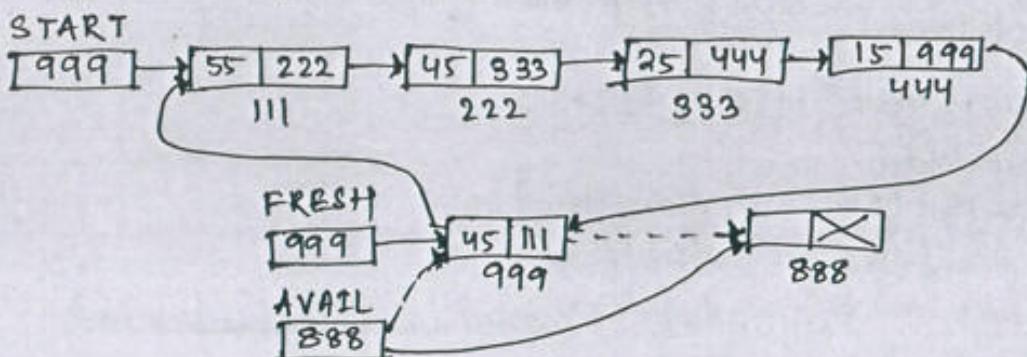
```
start = first;
```

Y

```
return start;
```

Y

2. Insertion of a node at the end :



Algorithm:

INSERTEND(START, INFO, LNK, AVAIL, FRESH, ITEM)

Step 1 : If AVAIL = NULL, then Display "Memory Insufficient"

Step 2 : Else

 FRESH := NULL

 AVAIL := LINK[AVAIL]

 INFO[FRESH] := ITEM

 LINK[FRESH] := NULL

Step 2.1 : If START = NULL, then

 START := FRESH

 LINK[FRESH] := START

Step 2.2 : Else

 PTR := START

 Repeat while LINK[PTR] != START

 PTR := LINK[PTR]

 [End of While]

 LINK[PTR] := FRESH

 LINK[FRESH] := START.

 [End of If - Step 2.1]

 [End of Else If - Step 2]

Step 3 : Exit.





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SUBJECT:- DATA STRUCTURE

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C - function:

struct node * insert_last (struct node * start)

{ struct node * fresh, * ptr;

int item;

printf ("\n enter an item");

scanf ("%d", &item);

fresh = (struct node *) malloc (sizeof (struct node));

if (fresh == NULL)

printf ("In memory is full"),

else

{ fresh -> info = item;

fresh -> link = NULL;

if (start == NULL)

{ start = fresh;

fresh -> link = start;

}

else

{

for (ptr = start; ptr -> link != start; ptr = ptr -> link)

ptr -> link = fresh;

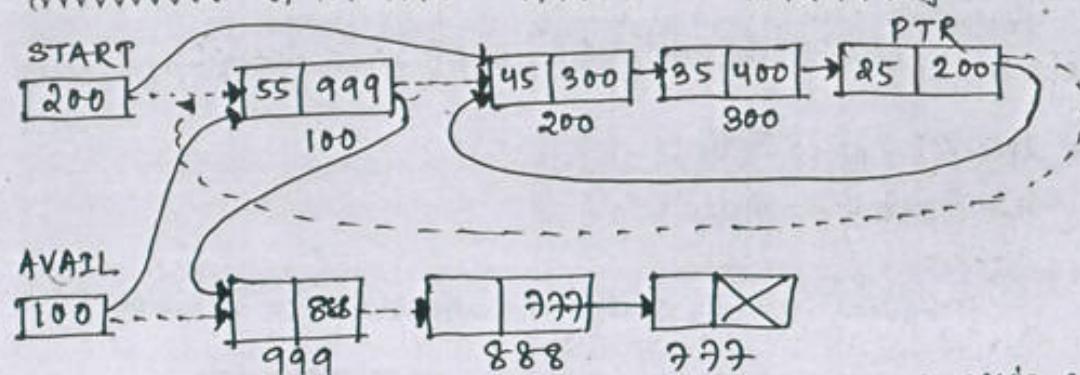
fresh -> link = start;

}

return start;

.

3. Deletion of a node from the beginning:



Hence, the link part of 1st node is 200 which is assigned to START and by moving to the last node, the link part of last node updated with address 200 as pointed by START. Now the 1st node with address 100 is added at the beginning of free or avail list.

Algorithm:

DELETE FIRST (START, INFO, LINK, AVAIL)

Step 1: If $START = \text{NULL}$, Then

Display "List does not exist".

Step 2: Else if $START = \text{LINK}[START]$, then

$\text{LINK}[START] := \text{AVAIL}$

$\text{AVAIL} := \text{START}$.

$\text{START} := \text{NULL}$

Step 3: Else

$\text{PTR} := \text{START}$

Repeat While $\text{LINK}[\text{PTR}] != \text{START}$.

$\text{PTR} := \text{LINK}[\text{PTR}]$

[End of While]

$\text{LINK}[\text{PTR}] := \text{LINK}[\text{START}]$

$\text{PTR} := \text{START}$

$\text{START} := \text{LINK}[\text{START}]$

$\text{LINK}[\text{PTR}] := \text{AVAIL}$

$\text{AVAIL} := \text{PTR}$

[End of IF]

Step 4: Exit.



C - function :-

```
struct node * delete - first (struct node * start)
```

```
{ struct node *ptr;
```

```
if (start == NULL)
```

```
{ printf ("In memory underflow - list is empty");
```

```
}
```

```
else
```

```
{ ptr = start;
```

```
while (ptr->link != start)
```

```
{
```

```
ptr = ptr->link;
```

```
ptr->link = start->link;
```

```
ptr = start;
```

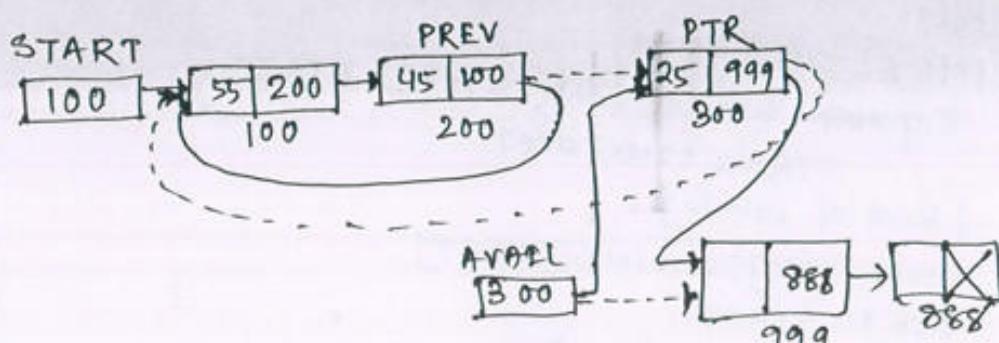
```
start = start->link;
```

```
free (ptr);
```

```
}
```

```
return start;
```

4. Deletion of a node from the end :-



Hence, the link part of last but one node as pointed by PREV with address 200 is updated with address of first node 100. Now the last node as pointed by PTR is added at the beginning of free or avail list.

Algorithm :-

```

~~~~~ DELETE END (START, INFO, LINK, AVAIL)
Step 1: If START = NULL, Then Display "List Not Exist"
Step 2: Else If START = LINK[START], Then
        LINK[START] := AVAIL
        AVAIL := START
        START := NULL
Step 3: Else
        PTR := START
        Repeat, while LINK[PTR] != START
            PREV := PTR
            PTR := LINK[PTR]
        [End of while]
        LINK[PREV] := START
        LINK[PTR] := AVAIL
        AVAIL := PTR
    [End of If]
Step 4: EXIT.

```

C- Functions :-

```

~~~~~ struct node * delete - last (struct node * start)

```

```

{
    struct node * pptr, * pprev;
    if (start == NULL)
        printf ("\n memory underflow - list is empty");
    else if (start == start -> link)
        {
            pptr = start;
            start = NULL;
            free (ptr);
        }
    else
        {
            pptr = start;
            while (ptr -> link != start)
                {
                    pprev = pptr;
                    pptr = pptr -> link;
                    pprev -> link = start;
                }
            free (ptr);
        }
    return start;
}

```



Advantages of circular singly linked list :-

i) Nodes can be accessed easily

ii) Deletion of nodes is easier

iii) Concatenation and splitting of circular linked list can be done efficiently.

Disadvantages of circular singly linked list :-

i) It may enter into an infinite loop.

ii) Head node is required to indicate the START or END of the circular linked list.

iii) Backward traversing is not possible.



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Data Structure Using C

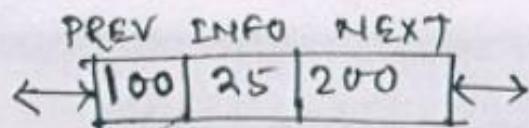
Topic:
Doubly Linked List

Contributed By:
Nihar Ranjan Rout
Gandhi Institute For Technology, GIFT

Doubly Linked List :-

A doubly linked list is a collection of nodes where each node contains the address of next as well as address of previous node along with INFO part to hold the information. In other words, it is also referred as two-way list as traversing is possible in both the directions.

Eg:-



2. The structure of a node in 'C' is -

struct node

{
 int info

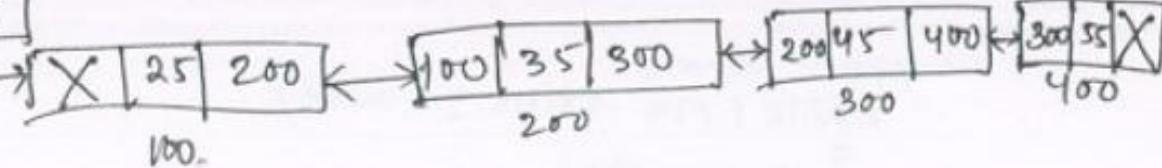
 struct node *prev, *next;

};

Eg:-

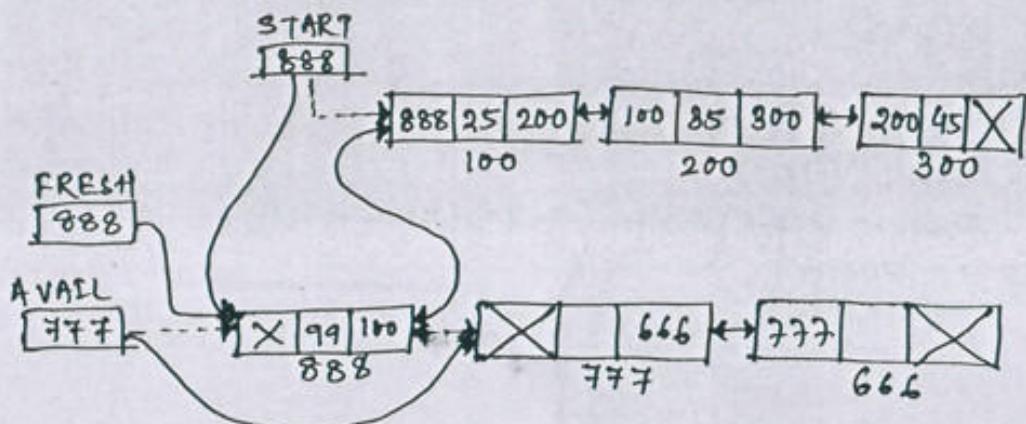
START

100



Operations on doubly linked list :

1. Insertion of a node at the beginning :



Hence, the fresh node with address 888 is inserted at the beginning of the doubly linked list. The NEXT part of fresh node is updated with the address contained in START. i.e., 100 and START is updated with 888, the address of fresh node.

Algorithm:

INSERT FIRST(START, INFO, NEXT, PREV, FRESH, AVAIL)

Step 1 : If AVAIL = NULL, then Display "Insufficient Memory"

Step 2 : Else

 FRESH := AVAIL

 AVAIL := NEXT[AVAIL]

 PREV[AVAIL] := NULL

 NEXT[FRESH] := NULL

 PREV[FRESH] := NULL

 INFO[FRESH] := ITEM

Step 2.1 : If START = NULL, then START := FRESH

Step 2.2 : Else

 NEXT[FRESH] := START

 PREV[START] := FRESH

 START := FRESH

[End. of IF - Step 2.1]

[End of IF - Step-1]

Step-3 : Exit



c-function:

struct node *insert-first(struct node *start)

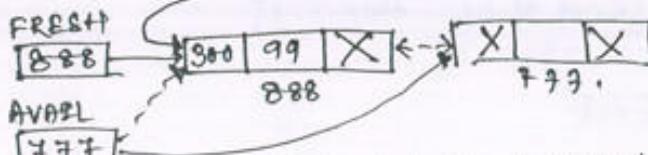
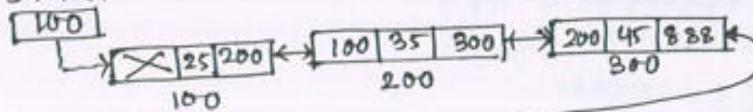
```

2 struct node *first;
int item;
printf("Enter item");
scanf("%d", &item);
first = (struct node*) malloc(sizeof(struct node));
if(first == NULL)
    printf("Memory is full");
else
{
    first->info = item;
    first->next = NULL;
    first->prev = NULL;
    if(start == NULL)
    {
        start = first;
    }
    else
    {
        first->next = start;
        start->prev = first;
        start = first;
    }
}
return start;

```

2. Insertion of a node at the end:

START



Here, the fresh node with address 888 is to be inserted at the end. Now the NEXT PTR is made to point the last node with address 300. Now the PTR is assigned with next part of node with address 300 as pointed by PTR is assigned with address of fresh ie:- 888 and PREV part of fresh node is updated with address 800 as pointed by PTR.

Algorithm :-

INSERT END (START, INFO, NEXT, PREV, FRESH, AVAIL, PTR)

Step 1 :- If AVAIL = NULL, Then Display "Insufficient Memory"

Step 2 :- Else

FRESH := AVAIL

AVAIL := NEXT[AVAIL]

PREV[FRESH] := ITEM

NEXT[FRESH] := NULL

PREV[FRESH] := NULL

INFO[FRESH] := ITEM

Step 2.1 :- If START = NULL, Then START := FRESH

Step 2.2 :- Else

PTR := START

while NEXT[PTR] != NULL

PTR := NEXT[PTR]

[End of while]

NEXT[PTR] := FRESH

PREV[FRESH] := PTR

[End of IF - Step 2.1]

[End of If - Step 1]

Step 3 :- Exit

C- Program :-

struct node *insertLast (struct node *start)

{ struct node *fresh, *ptr;

int item;

printf("Enter an item");

scanf("%d", &item);

fresh = (struct node *) malloc(sizeof(struct node));

If (fresh == NULL)

printf("Memory is full");

else

{ fresh->info = item;

fresh->next = NULL;

fresh->prev = NULL;

If (start == NULL)

{ start = fresh;

}



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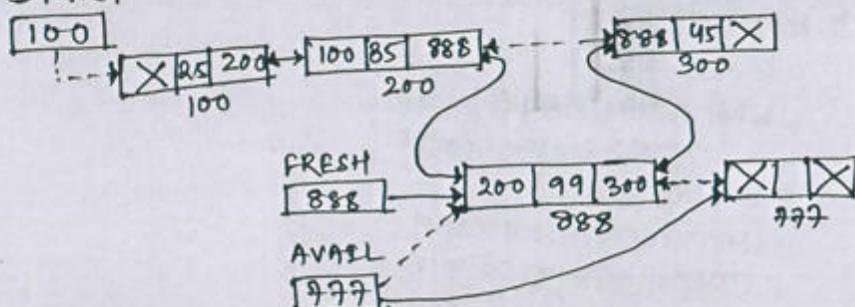
```

else
{
    for( ptr = start; ptr->next != NULL, &ptr = ptr->next)
        ptr->next = fresh;
    fresh->prev = ptr;
}
return start;
}

```

3. Insertion of a node at specific location :

START



Algorithm :

~~~~~  
 INSERT-AT-LOC (START, INFO, NEXT, PREV, FRESH, AVAIL, PTR)

Step 1 : If AVAIL = NULL, Then Display "Insufficient Memory".

Step 2 : ELSE

```

        FRESH = AVAIL
        AVAIL := NEXT[AVAIL]
        PREV[AVAIL] := NULL
        NEXT[FRESH] := NULL
        PREV[FRESH] := NULL
        INFO[FRESH] := ITEM
    
```

Step 2.1 : If START = NULL, Then START := FRESH

Step 2.2 : ELSE

Step 2.2.1 : Set I := 1, PTR1 := START

Step 2.2.2 : Repeat While I < LOC AND PTR1 != NULL

Set PTR := PTR1

Set PTR1 := NEXT[PTR1]

Set I := I + 1

[End of while]

Step 2.2.3 : If PTR1 = NULL, Then  
Display "Location does not exist".

Step 2.2.4 : Else if PTR1 = START, Then  
NEXT[FRESH] := START  
PREV[START] := FRESH

Step 2.2.5 : Else  
NEXT[PTR] := FRESH  
PREV[FRESH] := PTR  
NEXT[FRESH] := PTR1  
PREV[PTR1] := FRESH

[End of If - step 2.2.3]

[End of If - step 2.1]

[End of If - step 1]

Step 3 : Exit.

C-function:

```
struct node *insert_loc (struct node *start)
```

```
{ struct node *frosh, *ptr, *ptr1;  
int item, loc, i;
```

```
frosh = (struct node*) malloc(sizeof(struct node));
```

```
if (frosh == NULL)
```

```
{ printf("\n memory is full");
```

```
else
```

```
{ printf("\nEnter item and location for insertion");
```

```
scanf("%d %d", &item, &loc);
```

```
frosh->info = item;
```

```
frosh->next = NULL;
```

```
frosh->prev = NULL;
```

```
if (start == NULL)
```

```
{ printf("\n list doesn't exist");
```

```
}
```

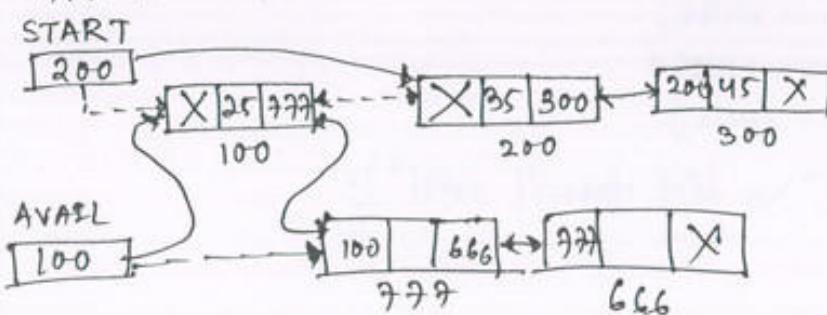


```

else
{
    ptr1 = start;
    i = 1;
    while(i < loc && ptr1 != NULL)
    {
        ptr = ptr1;
        ptr1 = ptr1->next;
        i++;
    }
    if(ptr1 == NULL)
        printf("Invalid entry of location");
    else if(ptr1 == start)
    {
        // insertion at beginning
        fresh->next = ptr;
        ptr->prev = fresh;
        start = fresh;
    }
    else
    {
        ptr->next = fresh;
        fresh->prev = ptr;
        fresh->next = ptr1;
        ptr1->prev = fresh;
    }
}
return start;
}

```

4. Deletion of a node from the beginning:



Algorithm :-

DELETE FIRST(START, PREV, NEXT, PTR, AVAIL)

Step 1: If START = NULL, Then

Display "Linked List Doesn't Exist or Underflow".

Step 2: Else

PTR := START

START := NEXT[PTR]

NEXT[PTR] := AVAIL

PREV[AVAIL] := PTR

AVAIL := PTR

Step-3: [End of If]

Step-3: Exit.

C-function:

```
struct node *delete-first(struct node *start)
```

{ struct node \*ptr;

if (start == NULL)

printf("In memory underflow - List is empty");

}

else

ptr = start;

start = start → next;

start → prev = NULL;

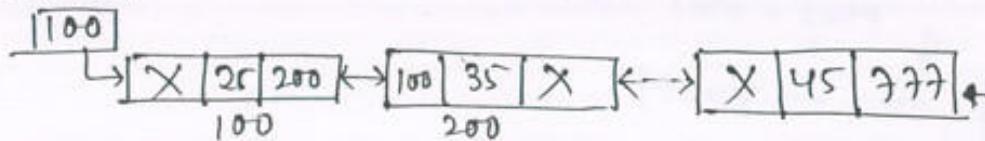
free(ptr);

return start;

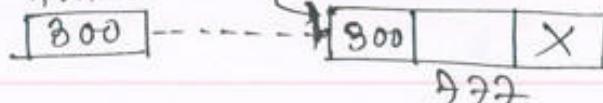


### 5. Deletion of a node from the end :

START



AVAIL



Algorithm:

DELETEEND(START, PREV, NEXT, PTR, PTR1, AVAIL)

Step 1: If START = NULL, then

Display "Linked List Doesn't Exist or Underflow"

Step 2: Else

Step 2.1: PTR1 = START

Step 2.2: Repeat while NEXT[PTR1] != NULL

Set PTR2 = PTR1

Set PTR1 := NEXT[PTR1]

[End of while]

Step 2.3: NEXT[PTR1] := NULL

PREV[PTR1] := NULL

NEXT[PTR1] := AVAIL

PREV[AVAIL] := PTR1

AVAIL := PTR1

[End of If]

Step 3: Exit

C-function:

struct node \* deleteLast(struct node \*start)

{ struct node \*ptr, \*ptr1;

if (start == NULL)

{ printf("In memory underflow - list is empty");

else

{ ptr1 = start;

while (ptr1->next != NULL)

{ ptr2 = ptr1;

ptr1 = ptr1->next;

if (ptr1 == start)

{ start = NULL;

}



---

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else  
    ptr->next = NULL;

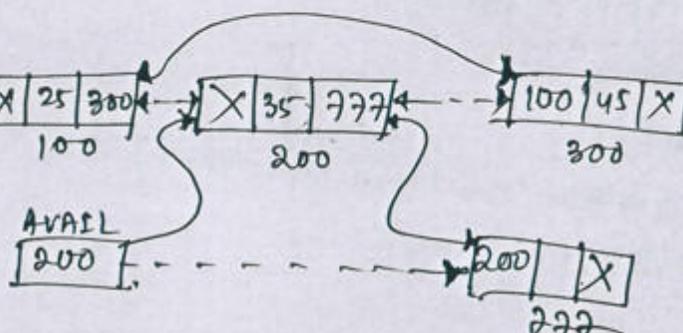
    free(ptr);

    return start;

6. Deletion of a node from Specific position:

START

200



Algorithm:

DELETE POS (START, LOC, PTR, PTR1, ITEM, AVAIL)

Step 1: Let I := 1

Step 2: If START = NULL, then Display "List not exist"

Step 3: Else

    Step 3.1: PTR1 := START

    Step 3.2: Repeat while I < LOC AND PTR1 != NULL

        PTR := PTR1

        PTR1 := NEXT[PTR1]

        I := I + 1

[End of while]

Step 3.3: If PTR1 = NULL, then

        Display "Location entered not exist"

Step 3.4: Else if PTR1 = START, then

        START := NEXT[START]

        PREV[START] := NULL

Step 3.5: Else if NEXT[PTR1] = NULL, then

        NEXT[PTR1] := NULL

Step 3.6 Else

$$\text{NEXT[PTR]} := \text{NEXT[PTR1]}$$

$$\text{PREV[NEXT[PTR1]]} := \text{PTR}$$

[End of step 3.3]

Step 3.7 :  $\text{NEXT[PTR1]} := \text{AVAIL}$   
 $\text{PREV[AVAIL]} := \text{PTR1}$   
 $\text{PREV[PTR1]} := \text{NULL}$   
 $\text{AVAIL} := \text{PTR1}$

[End of step-2]

Step 4 : Exit.

C-function :

```
struct node * delete_loc (struct node * start)
```

```
{ struct node *ptr, *ptr1;
```

```
int loc, i;
```

```
if (start == NULL)
```

```
{ printf ("In memory underflow - list is empty");
```

```
else
```

```
{ printf ("Enter the location/node no. for deletion");
```

```
- scanf ("%d", &loc);
```

```
ptr1 = start;
```

```
i = 1;
```

```
while (i < loc && ptr1 != NULL)
```

```
{
```

```
ptr = ptr1;
```

```
ptr1 = ptr1 -> next;
```

```
i++;
```

```
if (ptr1 == NULL)
```

```
printf ("In location entered not exist");
```

```
else if (ptr1 == start)
```

```
{
```

```
start = start -> next;
```

```
start -> prev = NULL;
```

```
free (ptr1);
```

```
else if (ptr1 -> next == NULL)
```

```
ptr1 -> next = NULL;
```

```

else
    {
        ptr->next = ptr->next;
        ptr->next->prev = ptr;
        free(ptr);
    }
}
return start;

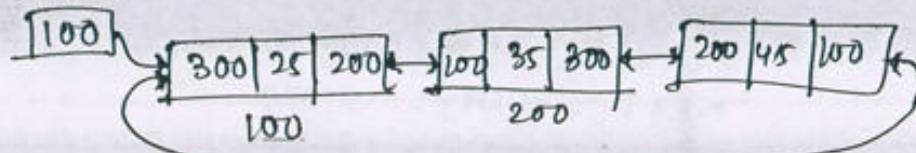
```

3.

### Circular Linked List & Doubly

- The doubly linked list of circles in nature is referred as circular doubly linked list i.e. In a circular doubly linked list, the NEXT part of last node contains the address of first node and the PREV part of first node contains address of last node.

START

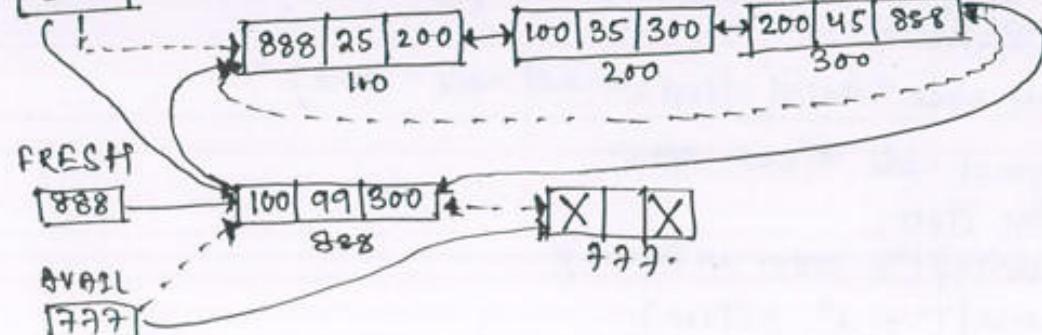


### Operations on circular doubly linked list :-

1. Insertion of a node at the beginning :-

START

300



Algorithm<sup>o</sup>  
~~~~~

INSERT-FIRST(START, FRESH, INFO, PREV, NEXT, PTR, AVAIL)
Step 1: If AVAIL = NULL, then Display "Insufficient memory or
overflow".

Step 2: Else

Step 2.1: FRESH := AVAIL
AVAIL := NEXT[AVAIL]
PREV[AVAIL] := NULL
PREV[FRESH] := NULL
NEXT[FRESH] := NULL

Step 2.2: If START = NULL, then

START := FRESH
PREV[FRESH] := START
NEXT[FRESH] := START

Step 2.3: Else

PTR := PREV[START]
NEXT[PTR] := FRESH
PREV[FRESH] := PTR
NEXT[FRESH] := START
PREV[START] := FRESH
START := FRESH

[End of IF]

[END of IF]

Step 3: Exit.

C-function:

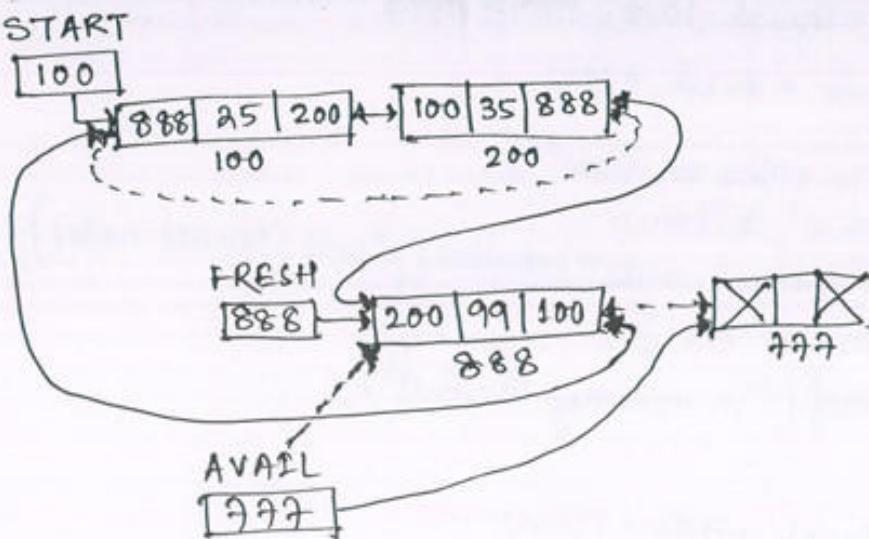
```
struct node *Insert-first(struct node *start)
{
    struct node *fresh, *ptr;
    int item;
    printf("In enter an item");
    scanf("%d", &item);
    fresh = (struct node *) malloc(sizeof(struct node));
    if (fresh == NULL)
    {
        printf("In memory is full");
    }
}
```

```

else
{
    fresh->info = item;
    fresh->next = NULL;
    fresh->prev = NULL;
    if (start == NULL)
    {
        start = fresh;
        start->prev = start;
        start->next = start;
    }
    else
    {
        ptr = start->prev;
        ptr->next = fresh;
        fresh->prev = ptr;
        fresh->next = start;
        start->prev = fresh;
        start = fresh;
    }
}
return start;
}

```

2. Insertion of a node at the end :



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Algorithm:

INSERTEND(START, FRESH, INFO, PREV, NEXT, PTR, AVAIL)

Step 1: If AVAIL = NULL, then display "Insufficient memory or Overflow"

Step 2: Else

Step 2.1: FRESH := AVAIL

AVAIL := NEXT[AVAIL]

PREV[AVAIL] := NULL

PREV[FRESH] := NULL

NEXT[FRESH] := NULL

Step 2.2: If START = NULL, Then

START := FRESH

PRBV[FRESH] := START

NEXT[FRESH] := START

Step 2.3: Else

PTR := PREV[START]

NEXT[PTR] := FRESH

PREV[FRESH] := PTR

NEXT[FRESH] := START

PREV[START] := FRESH

[End of IF]

[End of IF]

Step 3: Exit.

C-function:

struct node *insertLast(struct node *start)

{ struct node *fresh, *ptr;

int item;

printf("\n Enter an item");

scanf("%d", &item);

fresh = (struct node *) malloc(sizeof(struct node));

If (fresh == NULL)

{ printf("\n Memory is full");

}

else

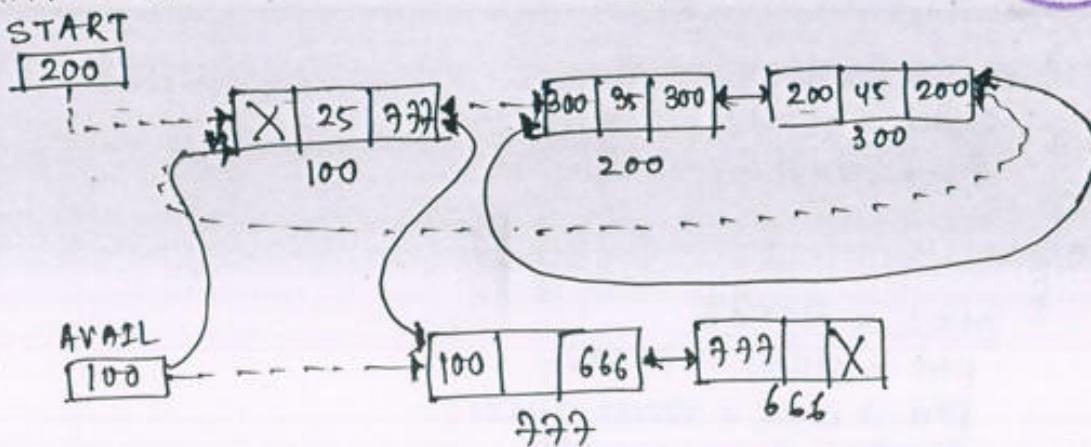
{ fresh->info = item;

```

fresh → next = NULL;
fresh → prev = NULL;
if (start == NULL)
{
    start = fresh;
    start → prev = start;
    start → next = start;
}
else
{
    ptr = start → prev;
    ptr → next = fresh;
    fresh → prev = ptr;
    fresh → next = start;
    start → prev = fresh;
}
return start;

```

3. Deletion of a node from the beginning:



Algorithm:

```

DELETEFIRST(START, PTR, PTR1, PREV, NEXT, AVAIL)
Step 1: If START = NULL, then Display "list Not Exist"
Step 2: Else If NEXT[START] = START, then
        PTR = START
        START = NULL
        NEXT[PTR] = AVAIL
        PREV[AVAIL] = PTR
        AVAIL = PTR

```

Step 3: Else

PTR₀ = PREV[START]

PTR₁ = START

NEXT[PTR]₀ = NEXT[PTR₁]

START₀ = NEXT[PTR₁]

PREV[START] = PTR₀

NEXT[PTR₁] = AVAIL

PREV[AVAIL] = PTR₁

AVAIL = PTR₁

[End of If]

Step 4: Exit.

C-function:

```
struct node *delete-first(struct node *start)
```

```
{ struct node *ptr, *ptr1;
```

```
if (start == NULL)
```

```
{ printf("In memory underflow - list is empty");
```

```
else if (start == start->next)
```

```
{ ptr = start;
```

```
start = NULL;
```

```
free(ptr);
```

```
}
```

```
else
```

```
{ ptr1 = start;
```

```
ptr = start->prev;
```

```
ptr->next = start->next;
```

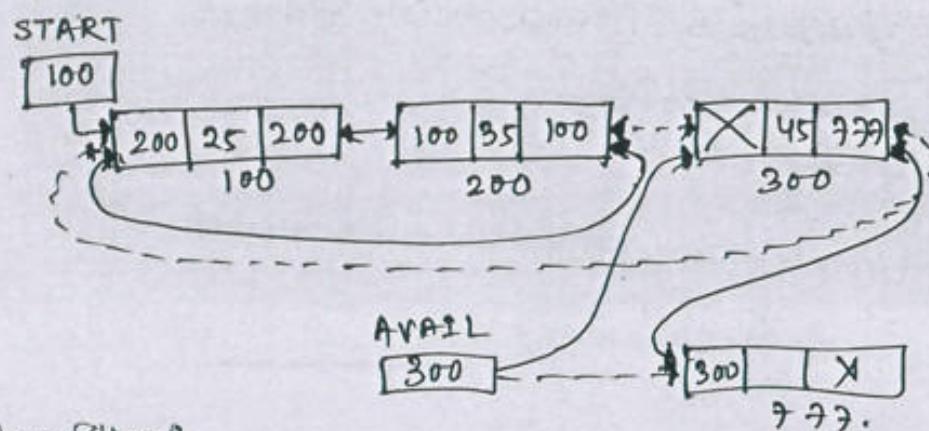
```
start = start->next;
```

```
start->prev = ptr;
```

```
free(ptr1);
```

```
return start;
```

3

4. Deletion of a node from the end :Algorithm:

DELETE END(START, PTR, PTR1, PREV, NEXT, AVAIL)

Step 1 : If START = NULL, Then Display "List not exist"

Step 2 : Else If START = NEXT[START], Then

PTR := START

START := NULL

NEXT[PTR] := AVAIL

PREV[AVAIL] := PTR

AVAIL := PTR

Step 3 : Else

PTR1 := PREV[START]

PTR := PREV[PTR1]

NEXT[PTR] := START

PREV[START] := PTR

NEXT[PTR1] := AVAIL

PREV[AVAIL] := PTR1

AVAIL := PTR1.

[End of IF]

Step 4 : Exit.



c-function:

```

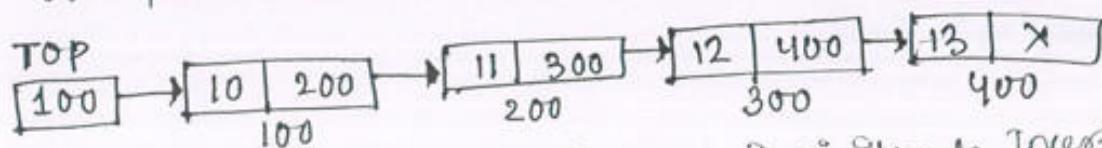
struct node *deleteLast(struct node *last)
{
    struct node *ptr1, *ptr2;
    if (start == NULL)
    {
        printf("\n memory underflow - list is empty");
    }
    else if (start == start->next)
    {
        ptr1 = start;
        start = NULL;
        free(ptr1);
    }
    else
    {
        ptr1 = start->prev;
        ptr2 = ptr1->prev;
        ptr2->next = start;
        start->prev = ptr2;
        free(ptr1);
    }
    return start;
}

```

Applications of linked list:

1. Linked Stack:

→ When the concept of stack is implemented using singly linked list, it is referred as linked stack. In linked stack, assume TOP is the pointer that identifies starting stack, or topmost node.



→ PUSH operation in a linked stack is similar to insertion of a node at the beginning of single linked list. POP operation in a linked stack is similar to deletion of a node from the beginning of a single linked list.

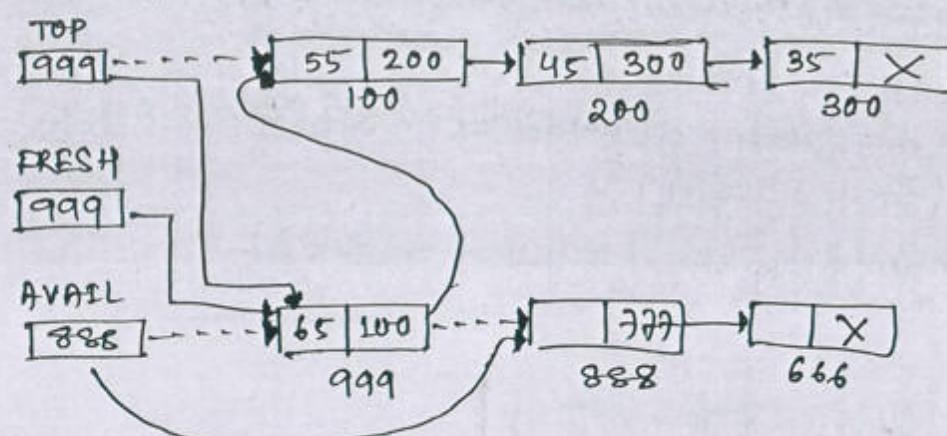


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a) Push operation in a linked stack:



Here node with address 999 is to be pushed onto the stack. Initially Top holds the address of node 100. In order to push the fresh node 999, the link part of it is updated with 100 and Top is assigned with the address of fresh 999.

Algorithm:

PUSH(AVAIL, FRESH, LINK, INFO, TOP)

Step 1: If AVAIL = NULL, Then Display "Insufficient memory or Overflow"

Step 2: Else

 FRESH := AVAIL

 AVAIL := LINK[AVAIL]

 LINK[FRESH] := NULL

 INFO[FRESH] := ITEM

Step 2.1:

 If TOP = NULL, Then TOP := FRESH

Step 2.2:

 Else

 LINK[FRESH] := TOP

 TOP := FRESH

 [End of If - Step 2.1]

 [End of If - Step 1]

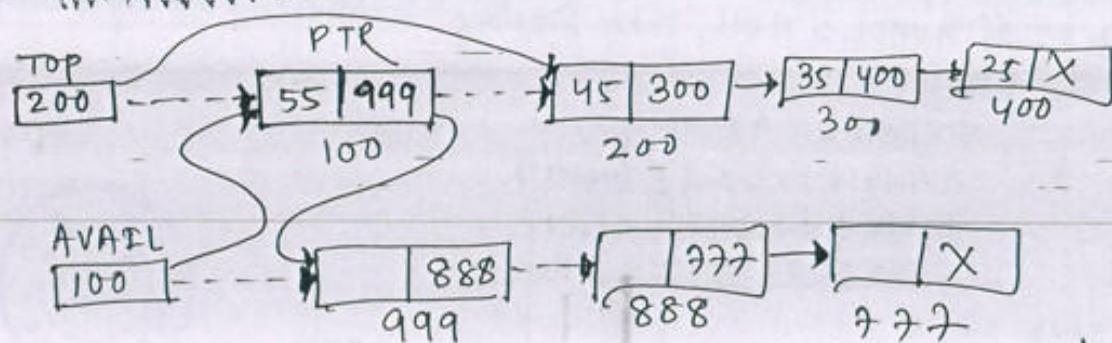
Step 3: Exit.



c) function :-

```
struct node *push(struct node **top, int item)
{
    struct node *frosh;
    frosh = (struct node *) malloc (sizeof (struct node));
    if (frosh == NULL)
        printf ("In stack is full or overflow");
    else
    {
        frosh->info = item;
        frosh->link = *top;
        *top = frosh;
    }
    return *top;
}
```

b) Pop operation on a linked stack :-



Hence, the top node with address 100 is to be popped. The TOP is updated with address 200. The node 100 is added at the beginning of free or avail list.

Algorithm :-

POP(TOP, PTR, LINK, AVAIL)

Step 1 :- If TOP = NULL, then display "Underflow"

Step 2 :- Else

PTR :- = TOP

TOP :- = LINK[TOP]

LINK[PTR] :- = AVAIL

AVAIL :- = PTR

[End of If]

Step 3 :- Exit.

C. functions:

```

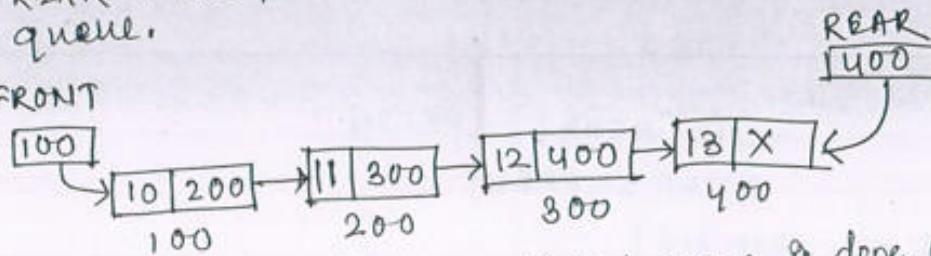
struct node *pop(struct node *top)
{
    struct node *ptr;
    int pitem;
    if (top == NULL)
    {
        printf("In stack is empty or underflow");
    }
    else
    {
        pitem = top->info;
        printf("In popped item is %d", pitem);
        ptr = top;
        top = top->link;
        free(ptr);
    }
    return top;
}

```



2. Linked Queue:
- When the concept of queue is implemented using singly linked list, it is referred as linked queue. In linked queue, assume FRONT is the pointer that identifies first node and REAR is the pointer that identifies the last node of linked queue.

FRONT

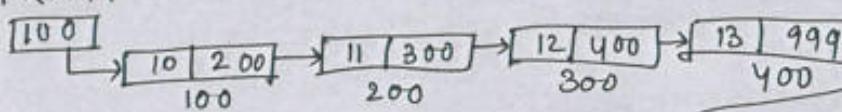


- Insertion operation in a linked queue is done at the rear end of the linked queue. Insertion operation in a linked queue is similar to insertion at the end of singly linked list.
- Deletion operation in a linked queue is done at the front end of linked queue. Deletion operation in a linked queue is similar to deletion from the beginning of the singly linked list.
- A linked queue can be traversed from the node as pointed by FRONT to node as pointed by REAR.

Q) Insertion operation in a linked queue:

FRONT

100



FRESH

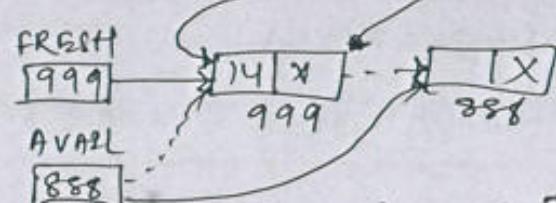
999

AVAIL

888

REAR

400



Assume node 999 is inserted onto the linked queue. The link part of REAR node is updated with the address of fresh node 999 and REAR is made to point to fresh node 999.

Algorithm:

LINKED-BQUEUE_INSERTION(AVAIL, FRESH, LINK, FRONT, REAR, INFO, ITEM)

Step 1: If AVAIL = NULL, then display "overflow"

Step 2: Else

 FRESH := AVAIL

 AVAIL := LINK[AVAIL]

 LINK[FRESH] := NULL

 INFO[FRESH] := ITEM

Step 2.1: If FRONT = NULL AND REAR = NULL, then

 FRONT := FRESH

 REAR := FRESH

Step 2.2: Else

 LINK[REAR] := FRESH

 REAR := FRESH

[End of if - step 2.1]

[End of if - step 1]

Step 3: Exit.

C function:

void insertion(int item)

{ struct node *frosh;

 frosh = (struct node *) malloc (sizeof(struct node));

 if (frosh == NULL)

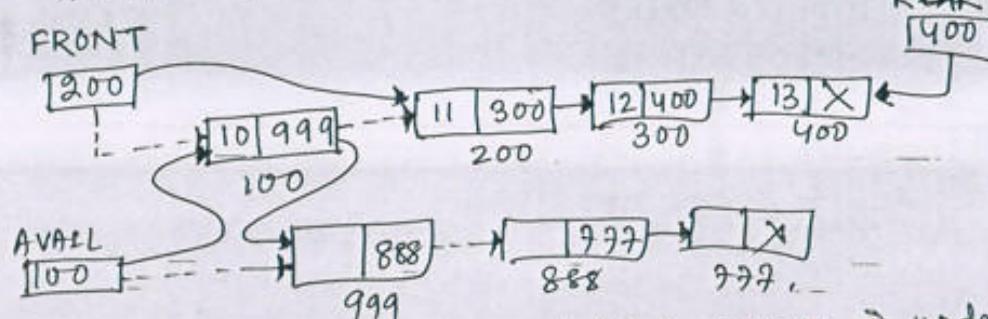
 {

```

printf("In queue is full or overflow");
}
else
{
    front->info = item;
    front->link = NULL;
    if (front == NULL && rear == NULL)
    {
        front = rear = front;
    }
    else
    {
        rear->link = front;
        rear = front;
    }
}
}

```

b) Deletion operation in a linked queue:



Hence front node 100 is to be deleted. FRONT is updated with address 200. Now node 100 is added at the beginning of free list or avail list.

Algorithm:

LINKED-QUEUE-DELETION (AVAIL, LINK, FRONT, REAR, PTR)

Step 1: If FRONT = NULL AND REAR = NULL, then
Display "Underflow"

Step 2: Else If FRONT = REAR, then
FRONT := NULL
REAR := NULL

Step 3: Else
PTR := FRONT
FRONT := LINK[FRONT]
LINK[PTR] := AVAIL
AVAIL := PTR

Step 4: End of If

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C-function:

void deletion(void)

{ struct node *ptr;

int pitem;

if (front == NULL)

{ printf("In queue or empty or underflow");

}

else

{ pitem = front->info;

printf("In deleted item is %d", pitem);

ptr = front;

if (front == rear)

{ front = NULL;

rear = NULL;

}

else

{

front = front->link;

free(ptr);

} }

Polynomial Representation Using Linked List :

1. A single linked list can be used to represent and manipulate polynomials. A polynomial expression is a collection of polynomial terms, where each term contains a coefficient, base and exponent.

Representation of a polynomial term:

1. A node that can be used to represent a polynomial term with one variable, is divided into 3 parts such as:- Coefficient

Point, Exponent Point and Link.

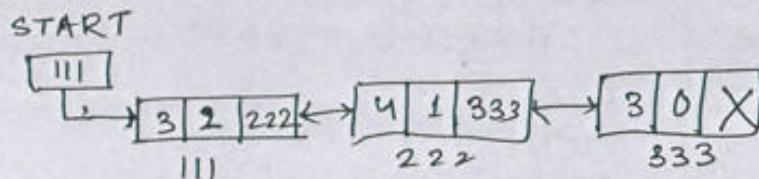
e.g:- To represent a polynomial term $3x^2$, the structure of nod

e.g:-

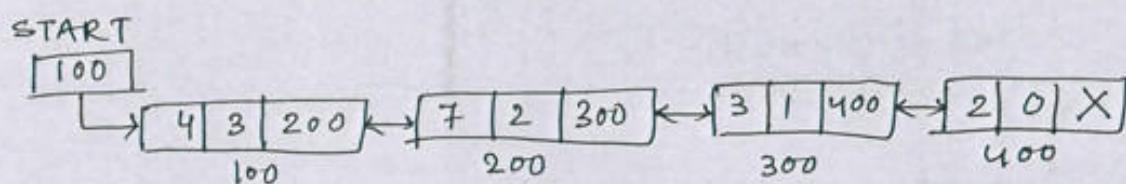
3	2	200
---	---	-----

Example: Represent the following polynomial expression in linked list format

$$\text{i)} 3x^2 + 4x + 3$$



$$\text{ii)} 4x^3 + 7x^2 + 3x + 2$$



Creating a polynomial using linked list:

Algorithm:

CREATE POLY(START, AVAIL, CO, EXP, LINK, FRESH, PTR, PTR1)

Step 1: If AVAIL = NULL, then Display "Memory insufficient"

Step 2: Else

FRESH := AVAIL

AVAIL := LINK[AVAIL]

LINK[FRESH] := NULL

Display "Enter Co-efficient & Exponent Value"

READ CO[FRESH], EXP[FRESH]

Step 2.1: If START = NULL, then START = FRESH

Step 2.2: Else PTR1 := START

Step 2.2.1: Repeat while PTR1 = NULL

If EXP[PTR1] < EXP[FRESH], then
BREAK

[End of If]

PTR := PTR1

PTR1 := LINK[PTR1]

[End of while]



Step 2.2.2: If PTR1 = START, then

LINK[FRESH] := PTR1

START := FRESH

Step 2.2.3: Else if PTR1 = NULL, then

LINK[PTR] := FRESH

Step 2.2.4: Else

LINK[PTR] := FRESH

LINK[FRESH] := PTR1.

[End of If - step 2.2.2]

[End of If - step 2.1]

Step 3: EXIT.

C-functions:

```
struct node *createpoly (struct node *start)
```

```
{ struct node *ptr, *ptrs1, *avail, *fresh;
```

```
char ch;
```

```
do
```

```
{ avail = (struct node *) malloc (sizeof (struct node));
```

```
if (avail == NULL)
```

```
{ printf (" overflow");
```

```
y
```

```
else
```

```
{ fresh = avail;
```

```
avail = avail->link;
```

```
fresh->link = NULL;
```

```
printf ("\n enter co-efficient & exponent : ");
```

```
scanf ("%d %d", &fresh->co, &fresh->exp);
```

```
if (start == NULL)
```

```
start = fresh;
```

```
else
```

```
{ ptrs1 = start;
```

```
while (ptrs1 != NULL && ptrs1->exp == fresh->exp)
```

```
{ ptrs = ptrs1;
```

```
y ptrs = ptrs1->link;
```

```

if (ptr == start)
{
    forest → link = ptr;
    start = forest;
}

else if (ptr == NULL)
{
    ptr → link = forest;
}

else
{
    ptr → link = forest;
    forest → link = ptr;
}

printf("add more (y/n)?");
fflush(stdin);
scanf("%c", &ch);
}
while (ch == 'y');
return start;
}

```



Polynomial Addition:

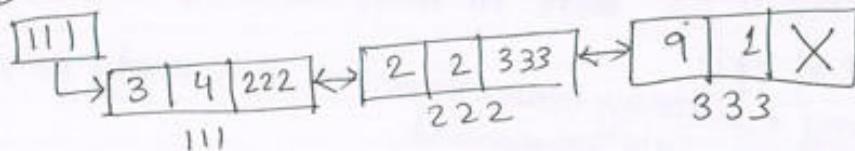
Assume P₁, P₂ are two polynomial expressions given. P₃ is the resultant polynomial which represents sum of P₁ and P₂.

$$P_1 = 3x^4 + 2x^3 + 9x$$

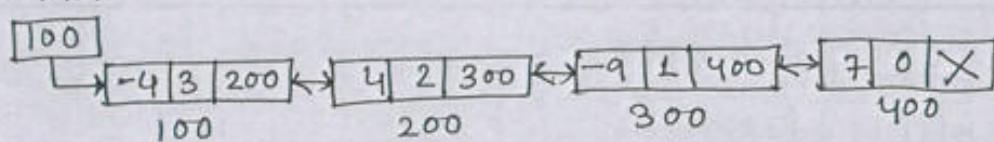
$$P_2 = -4x^3 + 4x^2 - 9x + 7$$

$$P_3 = 3x^4 + (-4x^3) + 6x^2 + 7.$$

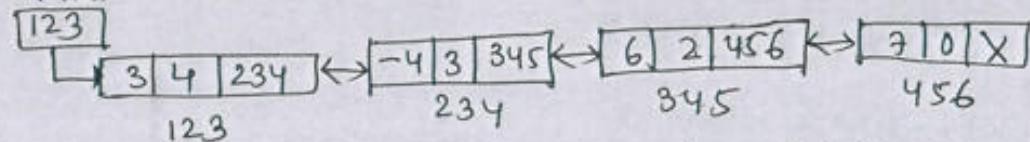
START



START



START



Procedure for addition of two polynomials :-

[Assume P1 and P2 are two polynomial expressions and P3 is the resultant polynomial]

Step 1 : Repeat while P1 and P2 are Not NULL repeat step 2,3 and 4.

Step 2 : If exponent parts of two terms of P1 and P2 are equal and if the co-efficient terms do not cancel to 0, then

Step 2.1 : Find sum of the co-efficient terms and insert SUM polynomial P3

Step 2.2 : Move to next term of P1

Step 2.3 : Move to next term of P2.

Step 3 : Else if the exponent of the term in first polynomial > exponent of the term in second polynomial, Then insert the term from first polynomial in the SUM polynomial.

Step 3.1 : Move to next term of P1.

Step 4 : Else

Step 4.1 : Insert the term from the 2nd polynomial into SUM polynomial

Step 4.2 : Move to Next term of P2.

[End of If]

Step 5 : Copy remaining terms from the non-empty polynomials into the SUM polynomial.

Step 6 : Exit.



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Algorithm for polynomial addition:

GET-NODE(AVAIL): This procedure used to allocate memory for a new node

INSERT-AT-END(P3,FRESH): This procedure need to insert FRESH node at the end of linked list.

ADD-POLY(P1,P2,P3): Hence P1 identifies first term of 1st polynomial, P2 identifies first term of 2nd polynomial and P3 identifies first term of the resultant polynomial.

GET-NODE(AVAIL)

Step 1: Let PTR

Step 2: If AVAIL = NULL, then Display "Overflow"

Step 3: Else

PTR := AVAIL

AVAIL := LINK[AVAIL]

LINK[PTR] := NULL

[End of If]

Step 4: RETURN(PTR)

Step 5: Exit



INSERT-AT-END(P3, FRESH)

Step 1: Set PTR

Step 2: If P3 = NULL, then P3 := FRESH

Step 3: Else

Step 3.1: Set PTR := P3

Step 3.2: Repeat while LINK[PTR] != NULL
PTR := LINK[PTR]

[End of While]

Step 3.3: LINK[PTR] := FRESH

Step 4: Exit

ADD-POLY(P1,P2,P3)

Step 1: Let PTR1, PTR2, FRESH

Step 2: P3 := NULL

Step 3: PTR1 := P1

Step 4: PTR2 := P2

Step 5: Repeat while $PTR1 = \text{NULL}$ AND $PTR2 = \text{NULL}$

Step 5.1: If $\text{EXP}[PTR1] > \text{EXP}[PTR2]$, then

$FRESH := \text{GET-NODE}(\text{AVAIL})$

$\text{EXP}[FRESH] := \text{EXP}[PTR1]$

$CO[FRESH] := CO[PTR1]$

$\text{INSERT-AT-END}(P3, FRESH)$

$PTR1 := \text{LINK}[PTR1]$

Step 5.2: Else If $\text{EXP}[PTR2] > \text{EXP}[PTR1]$, then

$FRESH := \text{GET-NODE}(\text{AVAIL})$

$\text{EXP}[FRESH] := \text{EXP}[PTR2]$

$CO[FRESH] := CO[PTR2]$

$\text{INSERT-AT-END}(P3, FRESH)$

$PTR2 := \text{LINK}[PTR2]$

Step 5.3: Else

$FRESH := \text{GET-NODE}(\text{AVAIL})$

$\text{EXP}[FRESH] := \text{EXP}[PTR1]$

$CO[FRESH] := CO[PTR1] + CO[PTR2]$

Step 5.3.1: If $CO[FRESH] = 0$, then

$\text{INSERT-AT-END}(P3, FRESH)$

[End of If - Step 5.3.1]

$PTR1 := \text{LINK}[PTR2]$

$PTR2 := \text{LINK}[PTR2]$

[End of If - Step 5.3.1]

[End of While - Step 5]

Step 6: Repeat while $PTR2 \neq \text{NULL}$

$FRESH := \text{GET-NODE}(\text{AVAIL})$

$\text{EXP}[FRESH] := \text{EXP}[PTR2]$

$CO[FRESH] := CO[PTR2]$

$\text{INSERT-AT-END}(P3, FRESH)$

$PTR2 := \text{LINK}[PTR2]$

[End of While - Step 6]

Step 7: Repeat while $PTR1 \neq \text{NULL}$

$FRESH := \text{GET-NODE}(\text{AVAIL})$

$\text{EXP}[FRESH] := \text{EXP}[PTR1]$

$CO[FRESH] := CO[PTR1]$

$\text{INSERT-AT-END}(P3, FRESH)$

$PTR1 := \text{LINK}[PTR1]$

[End of While - Step 7]

Step 8: RETURN ($P3$)

Step 9: EXIT.



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Data Structure Using C

Topic:

Dynamic Storage Management

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Dynamic Storage Management :-

i. Basic task of any program is to manipulate data. These data should be stored in memory during their manipulation. There are two memory management schemes for the storage allocations of data :-

ii) Static Storage Management

iii) Dynamic Storage Management.

2. In case of static storage management scheme, the net amount of memory for various data for a program are allocated before the starting of the executing of the program. Once memory is allocated, it neither can be extended nor can be returned to the memory bank for the use of other programs at the same time.
3. The dynamic storage management scheme allows the user to allocate and reallocate memory as per the necessity during the execution of programs.
4. Principles of dynamic memory management scheme :-
- i) Allocation scheme :- A request for a memory block will be serviced. There are two strategies. i.e. - a) fixed block allocation and b) variable block allocation (First fit and its variant, Next fit, Best fit, Worst fit)
 - ii) Reallocation scheme :- How to return memory block to the memory bank whenever it is no more required.
That is:- a) Random reallocation and b) Order Reallocation.



Garbage Collection:

1. Suppose some memory space becomes reusable, a node is deleted from a list or an entire list is deleted from a program. The operating system of a computer may periodically collect all the deleted space onto the free storage list.
2. Any technique which does this collection is called Garbage collection.
 a) Garbage collection usually takes place in two steps. That is-
 - i) First the computer runs through all list, tagging those cells which are currently in use.
 - ii) Then the computer runs through the memory collecting all untagged space into the free storage list.
3. The Garbage collection may take place when there is only some minimum amount of space or no space at all left in free storage list or when the CPU has the time to do the collection.

Compaction:

1. It is a technique for reclaiming the memory is unused for longer period by introducing a program to accomplish this task. The allocation problem becomes simple after compaction process.
 2. Compaction works by actually moving one block of data from one location of memory to another. So, as to collect all the free blocks into one large block.
- x—



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