

# Assignment

## WEEK 1

- Building Blocks for Problem Solving - Practice quiz on Sets (3 questions)

1. Let  $A = \{1, 3, 5\}$ . Is the following statement:  $3 \in A$ . True or false?

1 / 1 point

- True  
 False

 Correct

The symbol  $\in$  stands for "is an element of" and it is true that  $3$  is an element of  $A$ . The other two elements of  $A$  are  $1$  and  $5$ .

2. Let  $E = \{-1, -2, -3\}$ . Compute the cardinality  $|E|$  of  $E$ :

1 / 1 point

- 0
- $E$
- 3
- 3

 Correct

Recall that the cardinality of a set is the number of elements in it. Since  $E$  has three elements (which are  $-1, -2, -3$ ), the cardinality of  $E$  is  $|E| = 3$ .

3. Let  $A = \{1, 3, 5\}$  and  $B = \{3, 5, 10, 11, 14\}$ .

1 / 1 point

- Which of the following sets is equal to the intersection  $A \cap B$ ?
- $\{1, 3, 5\}$
  - $\{3, 5\}$
  - $\{3, 5, 10\}$
  - $\{3\}$

- The infinite World of Real Numbers - Practice quiz on the Number Line, including Inequalities (8 questions)

1. Which of the following real numbers is *not* an integer?

1 / 1 point

- 3
- 7
- 4.3
- 0

 Correct

4.3 is a decimal that is between two consecutive integers (4 and 5).

2. Which of the following is the absolute value  $|-7|$  of the number  $-7$ ?

1 / 1 point

- 7
- 1
- 0
- 7

 Correct

The absolute value of a number  $x$  is the distance along the number line from  $x$  to 0. In this case,  $-7$  is 7 units away from 0, and so  $|-7| = 7$ .

3. Suppose I tell you that  $x$  and  $y$  are two real numbers which make the statement  $x < y$  true. Which pair of numbers **cannot** be values for  $x$  and  $y$ ?

1 / 1 point

- $x = 5$  and  $y = 3.3$
- $x = -17.3$  and  $y = -17.1$
- $x = -1$  and  $y = 0$
- $x = 1$  and  $y = 7.3$

 **Correct**

The statement  $x < y$  means that  $x$  is to the left of  $y$  on the real number line. Since 5 is to the right of 3.3, these cannot be values for  $x$  and  $y$ .

4. Suppose I tell you that  $w$  is a real number which makes both of the following statements true:  $w > 1$  and  $w < 1.2$ . Which of the following numbers could be  $w$ ?

1 / 1 point

- $w = 1.2$
- $w = 11$
- $w = 1.05$
- $w = 0$

5. Suppose that  $x$  and  $y$  are two real numbers which satisfy  $x + 3 = 4y + 1$ . Which of the following statements are false?

1 / 1 point

- $x = 4y$
- $x = 4y - 2$
- $x + 2 = 4y$
- $2x + 6 = 8y + 2$

 Correct

The equation  $x = 4y$  cannot be derived from the given equation.

6. Which of the following real numbers is in the open interval  $(2, 3)$ ?

1 / 1 point

- 2.1
- 1
- 3
- 2

 Correct

7. Which of the following real numbers are in the open ray  $(3.1, \infty)$ ?

1 / 1 point

- 0
- 3.1
- 4.75
- 5

 Correct

Recall that  $(3.1, \infty) = \{x \in \mathbb{R} \mid x > 3.1\}$ . Since  $4.75 > 3.1$  is true,  $4.75 \in (3.1, \infty)$ .

8. Which of the following values for  $x$  solves the equation  $-3x + 2 = -4$

1 / 1 point

- All values of  $x$  such that  $x \leq 2$
- $x = \frac{2}{3}$
- $x = 2$
- $x = -2$

 Correct

First we subtract 2 from both sides of the given equation, to obtain  $-3x = -6$ . Finally, to isolate  $x$  we divide both sides of the equation by -3 to obtain  $x = 2$ .

- That Jagged S Symbol - Practice quiz on Simplification Rules and Sigma Notation (6 questions)

1. Which of the numbers below is equal to the following summation:  $\begin{aligned} \text{\displaystyle}\sum_{i=1}^3 i^2 \end{aligned}$

1 / 1 point

- 30
- 14
- 1
- 9

 Correct

We compute  $\sum_{i=1}^3 i^2 = 1^2 + 2^3 + 3^2 = 14$

2. Suppose that  $A = \sum_{k=1}^{100} k^4$  and  $B = \sum_{j=1}^{100} j^4$

1 / 1 point

Which of the following statements is true?

- There is not enough information to do the problem
- $B > A$
- $A > B$
- $A = B$

3. Which of the numbers below is equal to the summation  $\sum_{i=1}^{10} 7$ ?

1 / 1 point

- 70
- 7
- 55
- 0

 Correct

According to one of our Sigma notation simplification rules, this summation is just equal to 10 copies of the number 7 all added together, and so we get  $10 \times 7 = 70$ .

4. Suppose that  $X = \sum_{i=1}^5 i^3$  and  $Y = \sum_{i=1}^5 i^4$ .

1 / 1 point

Which of the following expressions is equal to the summation  $\sum_{i=1}^5 (2i^3 + 5i^4)$ ?

- 3375
- 7
- $2X + 5Y$
- $X + Y$

5. Which of the following numbers is the mean  $\mu_Z$  of the set  $Z = \{-2, 4, 7\}$ ?

1 / 1 point

- 9
- $\begin{aligned} &\text{\frac{13}{3}} \end{aligned}$
- 4
- 3

 Correct

To get the mean of a set of numbers, you need to perform two steps: first add them all up (in this case getting  $-2 + 4 + 7 = 9$ ), and then divide by the number of elements in the set (in this case that number is 3).

So you should obtain  $\mu_Z = \begin{aligned} &\text{\frac{9}{3}} \\ &= 3 \end{aligned}$ , which you did!

6. Suppose the set  $X$  has five numbers in it:  $X = \{x_1, x_2, x_3, x_4, x_5\}$ . Which of the following expression represents the mean of the set  $X$ ?

1 / 1 point

- $\sum_{i=1}^5 x_i$
- $\begin{aligned} &\text{\frac{1}{5} [\sum_{i=1}^5 (x_i - \mu_X)^2]} \end{aligned}$
- $\begin{aligned} &\text{\frac{1}{5} [\sum_{i=1}^5 x_i]} \end{aligned}$
- $\begin{aligned} &\text{\frac{1}{N} [\sum_{i=1}^N x_i]} \end{aligned}$

- That Jagged S Symbol - Graded quiz on Sets, Number Line, Inequalities, Simplification, and Sigma Notation (13 questions)

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LATEST SUBMISSION GRADE

100%

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1. Let  $B = \{3, 5, 10, 11, 14\}$ . Is the following statement true or false:  $3 \notin B$

1 / 1 point

- False  
 True

 Correct

The symbol  $\notin$  stands for "is not an element of." Since 3 is in an element of the set  $B$ , the given statement is not true.

2. Let  $A = \{1, 3, 5\}$  and  $B = \{3, 5, 10, 11, 14\}$ . Which of the following sets is equal to the union  $A \cup B$ ?

1 / 1 point

- $\{1, 10, 18\}$   
  $\{3, 5, 10, 11, 14\}$   
  $\{1, 3, 5, 10, 11, 14\}$   
  $\{1, 3, 5, 3, 5, 10, 11, 14\}$

3. How many real numbers are there between the integers 1 and 4?

1 / 1 point

- Infinitely many
- None
- 4
- 2

 Correct

There are in fact infinitely many real numbers between any pair of distinct integers, or indeed any pair of distinct real numbers!

4. Suppose I tell you that  $x$  and  $y$  are two real numbers which make the statement  $x \geq y$  true. Which pair of numbers cannot be values for  $x$  and  $y$ ?

1 / 1 point

- $x = 2$  and  $y = 1$
- $x = 10$  and  $y = 10$
- $x = -1$  and  $y = 0$
- $x = 5$  and  $y = 3.3$

5. Suppose that  $z$  and  $w$  are two positive numbers with  $z < w$ . Which of the following inequalities is false?

1 / 1 point

- $z + 3 < w + 3$
- $-z > -w$
- $-5z < -5w$
- $w - 7 > z - 7$

 Correct

If we start with  $z < w$  and multiply both sides by  $-5$ , we need to flip the less-than sign, which would give  $-5z > -5w$ . For an example, try  $z = 1$  and  $y = 2$  and see what happens!

6. Find the set of all  $x$  which solve the inequality  $-2x + 5 \leq 7$

1 / 1 point

- $x \geq -1$
- $x \geq -6$
- $x \leq -1$
- $x = -1$

7. Which of the following real numbers is not in the closed interval  $[2, 3]$

1 / 1 point

- 1
- 2.1
- 2
- 3

 Correct

Recall that the closed interval  $[2, 3]$  consists of all real numbers  $x$  which satisfy  $2 \leq x \leq 3$ . Since  $2 \leq 1$  is false,  $1 \notin [2, 3]$

8. Which of the following intervals represents the set of all solutions to:

1 / 1 point

$$-5 \leq x + 2 < 10?$$

- $[-7, 8)$
- $[-7, 8]$
- $[-5, 10)$
- $(7, 8)$

9. Which of the numbers below is equal to the following summation:  $\sum_{k=2}^5 2k$ ?

1 / 1 point

- 28
- 14
- 4
- 10

 Correct

We compute  $\sum_{k=2}^5 2k = 4 + 6 + 8 + 10 = 28$ .

10. Suppose we already know that  $\sum_{k=1}^{20} k = 210$ . Which of the numbers below is equal to  $\sum_{k=1}^{20} 2k$ ?

1 / 1 point

- 40
- 210
- 2
- 420

11. Which of the numbers below is equal to the summation  $\sum_{i=2}^{10} 7$ ?

1 / 1 point

- 7
- 63
- 70
- 48

 Correct

According to one of our Sigma notation simplification rules, this summation is just equal to 9 copies of the number 7 all added together, and so we get  $9 \cdot 7 = 63$ .

12. Which of the following numbers is the variance of the set  $Z = \{-2, 4, 7\}$ ?

1 / 1 point

- $\sqrt{14}$
- 42
- 14
- 69

13. Which of the following sets does *not* have zero variance? (hint: don't do any calculation here, just think!)

1 / 1 point

- $\{5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5\}$
- $\{0, 0, 0, 0, 0, 0, 0\}$
- $\{1, 1, 1, 1\}$
- $\{2, 5, 9, 13\}$

## WEEK 2

- Descartes Was Really Smart - Practice quiz on the Cartesian Plane (5 questions)

1. Which of the following points in the Cartesian Plane is on the  $y$ -axis?

1 / 1 point

- (0, -5)
- (-5, 0)
- (5, 0)
- (1, 1)

 Correct

The  $y$ -axis is defined to be all points in the Cartesian plane with zero as  $x$ -coordinate. The point (0, -5) meets that requirement.

2. Find the distance between the points  $A = (2, 2)$  and  $C = (3, 3)$ :

1 / 1 point

- 0
- 2
- 1
- $\sqrt{2}$

3. Find the point-slope form of the equation of the line that goes between  $A = (1, 1)$  and  $B = (5, 3)$ : 1 / 1 point

- $y - 1 = \frac{1}{2}(x - 1)$
- $y - 1 = \frac{1}{2}(x - 5)$
- $y = \frac{1}{2}x$
- $y - 3 = \frac{1}{2}(x - 1)$

**Correct**

The point-slope form for the equation of a line with slope  $m$  that goes through the point  $(x_0, y_0)$  is  $y - y_0 = m(x - x_0)$

In this case, the slope  $m = \frac{3-1}{5-1} = \frac{1}{2}$

We can choose either  $A$  or  $B$  for the point on the line, but in neither case do we get this chosen answer.

4. Which of the following points is on the line with equation:

1 / 1 point

$$y - 1 = 2(x - 2)?$$

- (0, 0)
- (2, 1)
- (2, 3)
- (3, 2)

 Correct

If we plug in 1 for  $y$  and 2 for  $x$  in the equation of the line, we make a true statement,  $0 = 0$ , so this point lies on the line.

5. Suppose that a line  $\ell$  has slope 2 and goes through the point  $(-1, 0)$ . What is the  $y$ -intercept of  $\ell$ ?

1 / 1 point

- 1
- 1
- 2
- 0

- Input-Output Machines - Practice quiz on Types of Functions (6 questions)

1. Suppose that  $A = \{1, 2, 10\}$  and  $B = \{4, 8, 40\}$ . Which of the following formulae do **not** define a function  $f : A \rightarrow B$ ? 1 / 1 point

- $f(1) = 4, f(2) = 4$ , and  $f(10) = 4$ .
- $f(a) = 4a$ , for each  $a \in A$
- $f(1) = 4, f(2) = 40$ , and  $f(10) = 8$ .
- $f(1) = 5, f(2) = 8$ , and  $f(10) = 40$ .

**Correct**

A function  $f : A \rightarrow B$  is a rule which assigns an element  $f(a) \in B$  to each  $a \in A$ . In this case, unfortunately,  $f(1) = 5 \notin B$ .

2. Suppose that  $A$  contains every person in the VBS study (see the second video in the course if you're confused here!). Suppose that  $Y = \{+, -\}$  and  $Z = \{H, S\}$  1 / 1 point

Suppose that  $T : A \rightarrow Y$  is the function which gives  $T(a) = +$  if person  $a$  tests positive and  $T(a) = -$  if they test negative.

Suppose that  $D : A \rightarrow Z$  is the function which gives  $D(a) = H$  does not actually have VBS and  $D(a) = S$  if the person actually has VBS.

Which of the following must be true of person  $a$  if we have a false positive?

- $T(a) = +$  and  $D(a) = H$
- $T(a) = +$  and  $D(a) = S$
- $T(a) = -$  and  $D(a) = S$
- $T(a) = -$  and  $D(a) = H$

**Correct**

Recall that a false positive is a positive test result (so  $T(a) = +$ ) which is misleading because the person actually does not have the disease ( $D(a) = H$ )

3. Consider the function  $g : \mathbb{R} \rightarrow \mathbb{R}$  defined by  $g(x) = x^2 - 1$ . Which of the following points are *not* on the graph of  $g$ ?

1 / 1 point

- (2, -1)
- (1, 0)
- (-1, 0)
- (0, -1)

 Correct

Recall that the graph of  $g$  consists of all points  $(x, y)$  such that  $y = g(x)$ . Here  $g(2) = 3 \neq -1$ , so the point  $(2, -1)$  is *not* on the graph of  $g$ .

4. Let the point  $A = (2, 4)$ . Which of the following graphs does *not* contain the point  $A$ ?

1 / 1 point

- The graph of  $g(x) = x + 2$
- The graph of  $f(x) = 2x$
- The graph of  $h(x) = x - 1$
- The graph of  $s(x) = x^2$

5. Suppose that  $h(x) = -3x + 4$ . Which of the following statements is true?

1 / 1 point

- $h$  is neither a strictly increasing function nor a strictly decreasing function.
- $h$  is a strictly increasing function
- All statements are correct
- $h$  is a strictly decreasing function



Correct

A function  $h$  is called strictly decreasing if whenever  $a < b$ , then  $h(a) > h(b)$

Since the graph of  $h$  is a line with negative slope, this is in fact true!

6. Suppose that  $f : \mathbb{R} \rightarrow \mathbb{R}$  is a strictly increasing function, with  $f(3) = 15$

1 / 1 point

Which of the following is a possible value for  $f(3.7)$ ?

- 3
- 3
- 14.7
- 17

- Input-Output Machines - Graded quiz on Cartesian Plane and Types of Function (13 questions)

1. Which of the following points in the Cartesian Plane have positive  $x$ -coordinate and negative  $y$ -coordinate?

1 / 1 point

- (0, 0)
- (-4, 5)
- (7, -1)
- (5, 7)



Correct

The  $x$ -coordinate, 7, is positive, and the  $y$ -coordinate, -1, is negative.

2. Which of the following points is in the first quadrant of the Cartesian Plane?

1 / 1 point

- (5, -1)
- (7, 11)
- (-4, -7)
- (-5, 1)

 Correct

The first quadrant is defined to be all points in the Cartesian plane whose coordinates are both positive.

3. Let  $A, B, C, D$  be points in the Cartesian Plane, and let the set  $S = \{B, C, D\}$

1 / 1 point

Suppose that the distances from  $A$  to  $B, C, D$  are 5.3, 2.1, and 11.75, respectively.

Which of the following points is the nearest neighbor to the point  $A$  in the set  $S$ ?

- C
- D
- A
- B

4. Find the distance between the points  $A = (2, 2)$  and  $B = (-1, -2)$ .

1 / 1 point

- 25
- 25
- 1
- 5

 Correct

Recall that the distance between points  $(a, b)$  and  $(c, d)$  is  $\sqrt{(c - a)^2 + (d - b)^2}$

In this case we have:

$$\sqrt{(-1 - 2)^2 + (-2 - 2)^2} = \sqrt{(-3)^2 + (-4)^2} = \sqrt{25} = 5$$

5. Find the slope of the line segment between the points  $A = (0, 1)$  and  $B = (1, 0)$ .

1 / 1 point

- 1
- 1
- $\sqrt{2}$
- 0

6. Find the point-slope form of the equation of the line with slope  $-2$  that goes through the point  $(5, 4)$ .

1 / 1 point

- $y - 4 = -2(x - 5)$
- $y - 5 = -2(x - 4)$
- $(5, 4)$
- $y - 4 = 2(x - 5)$

 Correct

The point-slope form for the equation of a line with slope  $m$  that goes through the point  $(x_0, y_0)$  is  $y - y_0 = m(x - x_0)$ .

In this case, the slope  $m = -2$  is given and the point  $(5, 4)$  on the line is given.

7. Which of the following equations is for a line with the same slope as  $y = -3x + 2$ ?

1 / 1 point

- $y = 5x$
- $y = 5x + 2$
- $y = 8x - 3$
- $y = -3x - 8$

 Correct

The slope-intercept formula for a line is  $y = mx + b$ , where  $m$  is the slope and  $b$  is the  $y$ -coordinate of the point where the line hits the  $y$ -axis.

This line has slope  $m = -3$  which is the same slope as the given line.

8. Which of the following equations is for a line with the same  $y$ -intercept as  $y = -3x + 2$ ?

1 / 1 point

- $y = -3x - 8$
- $y = 5x + 2$
- $y = 5x$
- $y = 8x - 3$

 Correct

The slope-intercept formula for a line is  $y = mx + b$ , where  $m$  is the slope and  $b$  is the  $y$ -coordinate of the point where the line hits the  $y$ -axis. This line has a  $y$ -intercept of 2 which is the same as the given line.

9. How many lines contain both the point  $A = (1, 1)$  and the point  $B = (2, 2)$ ?

1 / 1 point

- None
- infinitely many
- 1
- 2



Correct

The line with equation  $y = x$  is the one and only line that meets the stated requirements.

10. Suppose that we have two sets,  $A = \{a, b\}$  and  $Z = \{x, y\}$ . How many different functions  $F : A \rightarrow Z$  are possible?

1 / 1 point

- There are infinitely many
- There are none
- 4
- 1

11. How many graphs contain both the point  $A = (0, 0)$  and the point  $B = (1, 1)$

0 / 1 point

- 2
- Infinitely many
- None
- 1

! Incorrect

Here are at least two functions whose graphs contain both  $A$  and  $B$ :  $f(x) = x$  and  $g(x) = x^2$

12. Suppose that  $g : \mathbb{R} \rightarrow \mathbb{R}$  is a continuous function whose graph intersects the  $x$ -axis more than once. Which of the following statements is true?

1 / 1 point

- All of the above.
- $g$  is neither strictly increasing nor strictly decreasing.
- $g$  is strictly decreasing.
- $g$  is strictly increasing.

13. Find the slope of the line segment between the points  $A = (1, 1)$  and  $B = (5, 3)$ .

1 / 1 point

- 4
- 2
- $\frac{1}{2}$
- $\sqrt{20}$

✓ Correct

The slope of this line segment is  $\frac{3-1}{5-1} = \frac{1}{2}$ , where  $3 - 1$  is the rise and  $5 - 1$  is the run.

## WEEK 3

- This is about that derivative stuff - Practice quiz on Tangent Lines to Functions (2 questions)

1. Suppose that  $f : \mathbb{R} \rightarrow \mathbb{R}$  is a function. Which of the following expressions corresponds to  $f'(2)$ , the slope of the tangent line to the graph of  $f(x)$  at  $x = 2$ ?

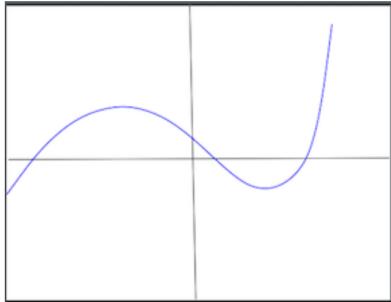
1 / 1 point

- $f'(2) = \lim_{h \rightarrow 0} \frac{f(a+h)-f(a)}{h}$
- $f'(2) = 2$
- $f'(2) = mx + b$
- $f'(2) = \lim_{h \rightarrow 0} \frac{f(2+h)-f(2)}{h}$

 **Correct**

This expression can be obtained from the first screen of our video by plugging in 2 for  $a$ .

2. Suppose that  $h : \mathbb{R} \rightarrow \mathbb{R}$  is a function whose graph is shown as the blue curve in the figure. For how many values of  $a$  is  $h'(a) = 0$ ? 1 / 1 point



- 3
- Never
- Always
- 2

**Correct**

$h'(a)$  gives the slope of the tangent line to the graph of  $h$  at the point  $x = a$ .

When  $h'(a) = 0$ , this means that the tangent line is horizontal.

There are two places (one on each side of the  $y$ -axis) where this tangent line is horizontal, so this answer is correct.

- Fast Growth, Slow Growth - Practice quiz on Exponents and Logarithms (12 questions)

1. Re write the number  $784 = 2 \times 2 \times 2 \times 2 \times 7 \times 7$  using exponents.

1 / 1 point

- $(16^4)(49^2)$
- $(2^4)(7^2)$
- $(2^6)(7^6)$
- $(2 \times 7)^6$



Correct

For this type of problem, count the number of times each relevant factor appears in the product. That number is the exponent for that factor.

2. What is  $(x^2 - 5)^0$ ?

1 / 1 point

- $(x^2)$
- $(x^2) - 5$
- $-4$
- $1$



Correct

Any real number (except zero) raised to the "zeroith" power = 1.

3. Simplify  $((x - 5)^2)^{-3}$

1 / 1 point

- $(x - 5)^{-6}$
- $(x - 5)^{-1}$
- $(x - 5)^{-5}$
- $(x - 5)$

 Correct

By Rule 2, "Power to a Power," multiply the exponents and get:

$$(x - 5)^{(2 \times -3)} = (x - 5)^{-6}$$

By the definition of negative exponents, this is equal to  $\frac{1}{(x - 5)^6}$

4. Simplify  $\left(\frac{8^2}{8^7}\right)^2$

1 / 1 point

- $8^{-10}$
- $8^{-4}$
- $8^{-5}$
- $8^{-1}$

 Correct

We can first simplify what is inside the parenthesis to  $8^{-5}$  using the Division and Negative Powers Rule.

Then apply division and negative powers-- the result is the same.  $\frac{8^4}{8^{14}} = 8^{-10}$

5.  $\log 35 = \log 7 + \log x$

1 / 1 point

Solve for  $x$

- 28
- 7
- 5
- 4

✓ correct

$$\log(x) = \log 35 - \log 7$$

$$\log(x) = \log \begin{aligned} & \left( \frac{35}{7} \right) \end{aligned}$$

By the Quotient Rule  $\log x = \log 5$

6.  $\log_2(x^2 + 5x + 7) = 0$

1 / 1 point

Solve for  $x$

- $x = 2$
- $x = 3$
- $x = -2 \text{ or } x = -3$
- $x = 2 \text{ or } x = 3$

 Correct

We use the property that  $\log_b a = c \Rightarrow b^c = a$

Use both sides as exponent for 2.

$$2^{\log_2 x^2 + 5x + 7} = 2^0$$

$$x^2 + 5x + 7 = 1$$

$$x^2 + 5x + 6 = 0$$

$$(x + 3)(x + 2) = 0$$

$$x = -3 \text{ OR }$$

$$x = -2$$

7. Simplify  $\log_2 72 - \log_2 9$

1 / 1 point

- $\log_2 63$
- 4
- $\log_2 4$
- 3

 Correct

By the quotient rule, this is  $\log_2 \begin{aligned} &\frac{72}{9} \\ &= \log_2 2^3 \\ &= 3 \end{aligned}$

8. Simplify  $\log_3 9 - \log_3 3 + \log_3 5$

1 / 1 point

- 15
- 8
- $\log_3 8$
- $\log_3 15$

 Correct

By the Quotient and Product Rules, this is  $\log_3 \begin{aligned} &\frac{9 \times 5}{3} \\ &= \log_3 15 \end{aligned}$

9. Simplify  $\log_2(3^8 \times 5^7)$

1 / 1 point

- (8 × log<sub>2</sub> 3) + (7 × log<sub>2</sub> 5)
- 15 × log<sub>2</sub> 56
- (5 × log<sub>2</sub> 3) + (8 × log<sub>2</sub> 5)
- 56 × log<sub>2</sub> 15

 Correct

We first apply the Product Rule to convert to the sum:  $\log_2(3^8) + \log_2(5^7)$ . Then apply the power and root rule.

10. If  $\log_{10} y = 100$ , what is  $\log_2 y = ?$

1 / 1 point

- 500
- 20
- 332.19
- 301.03

 Correct

Use the change of base formula,  $\log_a b = \frac{\log_x b}{\log_x a}$

Where the "old" base is  $x$  and the "new" base is  $a$ .

So  $\frac{100}{\log_{10}(2)} = \frac{100}{0.30103} = 332.19$

11. A tree is growing taller at a continuous rate. In the past 12 years it has grown from 3 meters to 15 meters. What is its rate of growth per year?

1 / 1 point

- 11.41%
- 12.41%
- 10.41%
- 13.41%

 Correct

$$\frac{\ln(15/3)}{12} = 0.1341$$

12. Bacteria can reproduce exponentially if not constrained. Assume a colony grows at a continually compounded rate of 400% per day. How many days before a colony with initial mass of  $6.25 \times 10^{-10}$  grams weights 1000 Kilograms?

1 / 1 point

- 87.5 days
- 0.875 days
- 875 days
- 8.75 days

 Correct

$$6.25 \times 10^{-10} \times e^{4t} = 10^6$$

$$4t = \ln\left(\frac{10^6}{6.25 \times 10^{-10}}\right) = 35.00878$$

$$t = \frac{35.00878}{4} = 8.752195$$

- Fast Growth, Slow Growth - Graded quiz on Tangent Lines to Functions, Exponents and Logarithms (13 questions)

1. Convert  $\begin{aligned}\frac{1}{49}\end{aligned}$  to exponential form, using 7 as the factor.

1 / 1 point

- $\begin{aligned}\frac{1}{49} = \frac{1}{7^2}\end{aligned}$
- $49^{-1}$
- $(7^2)$
- $7^{-2}$

 Correct

The rule for a factor to a Negative exponent is to divide by the same factor to a positive exponent with the same absolute value.

2. A light-year (the distance light travels in a vacuum in one year) is 9,460 trillion meters. Express in scientific notation.

0 / 1 point

- $0.946 \times 10^{16}$
- $9.46 \times 10^{15}$  meters.
- $9460 \times 10^{12}$  meters
- $9.46 \times 10^{15}$  kilometers

 Incorrect

9,460 is  $(9.4 \times 10^3)$  meters and one trillion meters is  $10^{12}$  meters.  $(9.4 \times 10^3)(10^{12}) = 9.4 \times 10^{15}$ . A kilometer is 1000 meters.

3. Simplify  $(x^8)(y^3)(x^{-10})(y^{-2})$

1 / 1 point

- $(x^2)(y)$
- $(x)(y^{-2})$
- $(x^{-80})(y^{-6})$
- $(x^{-2})(y)$

 Correct

By the Division and Negative Powers Rule, this is  $(x^{(8-10)})(y^{(3-2)})$

4. Simplify  $[(x^4)(y^{-6})]^{-1}$

1 / 1 point

- $\{\backslash large \begin{aligned} \frac{(x^{-4})(y^6)}{} \end{aligned}\}$
- $\{\backslash large \begin{aligned} \frac{(x^4)(y^{-6})}{} \end{aligned}\}$
- $(x^3)(y^{-7})$
- $(x^{-4})(y^6)$

 Correct

By the Power to a Power Rule, each of the exponents is multiplied by  $(-1)$

5. Solve for  $x$ :

1 / 1 point

$$\log_2(39x) - \log_2(x - 5) = 4$$

- $\backslash begin{aligned} \frac{23}{80} \end{aligned}$
- $\backslash begin{aligned} \frac{80}{38} \end{aligned}$
- $\backslash begin{aligned} \frac{39}{23} \end{aligned}$
- $\backslash begin{aligned} \frac{-80}{23} \end{aligned}$

6. Simplify this expression:

1 / 1 point

$$(x^{\frac{1}{2}})^{\frac{-3}{2}}$$

- $x^{-1}$
- $x^{\frac{-3}{4}}$
- $x^{\frac{4}{3}}$
- $x^{\frac{1}{3}}$

 Correct

We use the Power to a Power Rule -- multiply exponents:

$$x^{\frac{1}{2} \times \frac{-3}{2}} = x^{\frac{-3}{4}}$$

7. Simplify  $\log_2 8 - \log_2 4 - (\log_3 4.5 + \log_3 2)$

1 / 1 point

- 1
- 2
- 1
- 0

 Correct

This is equivalent to:

$$\log_2\left(\frac{8}{4}\right) - \log_3(4.5 \times 2) = 1 - 2 = -1$$

8. If  $\log_3 19 = 2.680$ , what is  $\log_9 19$ ?

1 / 1 point

- 0.8934
- 0.4347
- 5.216
- 1.304

 Correct

To convert from  $\log_3$  to  $\log_9$ , divide by  $\log_3 9$ . Which is equal to 2, so the answer is 1.34

9. If  $\log_{10} b = 1.8$  and  $\log_a b = 2.5752$ , what is  $a$ ?

1 / 1 point

- 4
- 6
- 5
- 3

 Correct

To solve for  $a$  in the formula;

$$\log_a b = \frac{\log_x b}{\log_x a}$$

$$\log_a b = 2.5752 \text{ and } \log_{10} b = 1.8$$

Therefore,  $\log_{10} a$  must equal to  $\frac{1.8}{2.5752} = 0.69897$

Treating both sides of equation  $\log_{10} a = 0.69897$  as exponents of 10 gives  $a = 10^{0.69897} = 5$

10. An investment of 1,600 is worth 7,400 after 8.5 years. What is the continuously compounded rate of return of this investment?

1 / 1 point

- 19.01%
- 20.01
- 18.02%
- 17.01%

 Correct

$$\ln\left(\frac{7400}{1600}\right)/8.5 = 0.18017$$

11. A pearl grows in an oyster at a continuously compounded rate of .24 per year. If a 25-year old pearl weighs 1 gram, what did it weigh when it began to form?

0 / 1 point

- 0.002478
- 0.02478
- 0.2478
- 0.0002478

!

Incorrect

$$e^{(0.24 \times 25)} = \frac{1}{x}$$

$$\text{\large x}=\begin{aligned} \frac{1}{\text{e}^{(0.24 \times 25)}} \end{aligned}$$

$$x = \frac{1}{403.4288}$$

$x = ?$  Look over your math and try again. You can do this!

12.  $\log_2 z = 6.754$ . What is  $\log_{10}(z)$ ?

1 / 1 point

- 0.82956
- 1.3508
- 2.03316
- 0.49185

✓

Correct

$$\frac{\log_2 z}{\log_2 10} =$$

$$(\log_{10} z) \times (\log_2 10) = 3.321928$$

Therefore,  $\log_{10} z = \frac{6.754}{3.321928} = 2.03316$

13. Suppose that  $g : \mathbb{R} \rightarrow \mathbb{R}$  is a function, and that  $g(1) = 10$ . Suppose that  $g'(a)$  is negative for every single value of  $a$ . Which of the following could possibly be  $g(1.5)$ ?

0 / 1 point

- $g(1.5) = 103.4$
- $g(1.5) = 11$
- $g(1.5) = 9.7$
- $g(1.5) = 10.1$

! Incorrect

Since the slope of the tangent line to the graph of  $g$  is negative everywhere on the graph, we know that  $g$  is a *decreasing* function! And therefore we must have  $g(1.5) < g(1)$ . That is not the case here!

## WEEK 4

- Basic Probability Definitions - Practice quiz on Probability Concepts (9 questions)

1. If  $x = \text{"It is raining,"}$  what is  $\sim(\sim x)$ ?

1 / 1 point

- "It is never raining"
- "It is not raining"
- "It is always raining"
- "It is raining"

 Correct

The second negation cancels out the first one.

Similarly  $\sim(\sim(\sim x)) = \sim x$

2. If the statement "I am 25 years old" is assigned probability 0, what probability is assigned to the statement "I am not 25 years old"?

1 / 1 point

- Unknown
- 1
- 0
- 1

 Correct

It is always the case that  $p(x) + p(\sim x) = 1$ .

3. If I assign to the statement  $x$  = "it will rain today" a probability of  $p(x) = 0.35$ , what probability must I assign to the statement "it will not rain today?"

1 / 1 point

- .5
- .65
- .35
- 0

 Correct

$$p(x) + p(\sim x) = 1$$

4. Is the following collection of statements a probability distribution?

1 / 1 point

- 1. I own a Toyota pickup truck
- 2. I do not own a Toyota pickup truck
- 3. I own a non-Toyota pickup truck
- 4. I do not own a non-Toyota pickup truck

- Yes
- No

5. I don't know what it means to be "ingenuous." What probability would I assign to the statement, "I am ingenuous OR I am not ingenuous"?

1 / 1 point

- 1
- 1
- 0
- .5

 Correct

It is always the case, regardless of the content of the statement  $x$ , that  $p(x \text{ or } \sim x) = 1$

6. A friend of mine circumscribes a circle inside a square, so that the diameter of the circle and the edge of the square are the same length. He asks me to close my eyes and pick a point at random inside the square. He says the probability that my point will also be inside the circle is  $\frac{\pi}{4}$

1 / 1 point

Is this correct?

Yes

No

 Correct

Probabilities can be any real number between 0 and 1. They do not need to be rational numbers – a numerator that is a transcendental number like Pi is acceptable.

Note that the correct probability does not depend on the length  $r$  of the circle's radius. For a circle with any radius  $r$  to be circumscribed inside a square, the square must have sides each of length  $2r$ . The area of the circle is  $\pi r^2$  and the area of the square is  $(2r)^2 = 4r^2$ . The probability of landing in a circle of area  $\pi r^2$  when it is known that one is in the area of the square is equal to the ratio of the area of the circle to the area of the square in which it is circumscribed, or  $\pi r^2 / 4r^2$ , which equals  $\pi/4$ .

7. The probability of drawing a straight flush (including a Royal Flush) in a five-card poker hand is 0.0000153908

1 / 1 point

What is the probability of **not** drawing a straight flush?

.9999846092

.9996582672

.9967253809

.9999745688

8. What is the probability that a fair, six-sided die will come up with a prime number? (Recall that prime numbers are positive integers other than 1 that are divisible only by themselves and 1)

1 / 1 point

- $\begin{aligned} \frac{1}{2} \end{aligned}$
- $\begin{aligned} \frac{1}{6} \end{aligned}$
- $\begin{aligned} \frac{1}{3} \end{aligned}$
- $\begin{aligned} \frac{2}{3} \end{aligned}$

 Correct

The faces with 2, 3 and 5 satisfy the condition – which makes 3 relevant outcomes out of the “universe” of 6 outcomes =  $\begin{aligned} \frac{3}{6} = \frac{1}{2} \end{aligned}$

9. The joint probability  $p$  (the die will come up 5, the next card will be a heart) is equal to the joint probability:

1 / 1 point

- $p$  (the die will **not** come up 5, the next card will **not** be a heart)
- $p$  (the next card will **not** come up 5, the next card will be a heart)
- $p$  (the next card will be a heart, the die will **not** come up 5)
- $p$  (the next card will be a heart, the die will come up 5)

 Correct

In joint probabilities, the order does not change the probability:  $p(A, B) = p(B, A)$

- Problem Solving Methods - Practice quiz on Problem Solving (9 questions)

1. I am given the following 3 joint probabilities:

1 / 1 point

$$p(\text{I am leaving work early, there is a football game that I want to watch this afternoon}) = .1$$

$$p(\text{I am leaving work early, there is not a football game that I want to watch this afternoon}) = .05$$

$$p(\text{I am not leaving work early, there is not a football game that I want to watch this afternoon}) = .65$$

What is the probability that there is a football game that I want to watch this afternoon?

- .1
- .35
- .2
- .3



Correct

Getting the answer is a two-step process. First, recall that the sum of probabilities for a probability distribution must sum to 1. So the “missing” joint distribution

$$p(\text{I am not leaving work early, there is a football game I want to watch this afternoon}) \text{ must be } 1 - (0.1 + 0.05 + 0.65) = 0.2$$

By the sum rule, the marginal probability  $p(\text{there is a football game that I want to watch this afternoon}) = \text{the sum of the joint probabilities}$

$$P(\text{I am leaving work early, there is a football game that I want to watch this afternoon}) + P(\text{I am not leaving work early, there is a football game I want to watch this afternoon}) = .1 + .2 = .3$$

2. The Joint probability of my summiting Mt. Baker in the next two years AND publishing a best-selling book in the next two years is .05. If the probability of my publishing a best-selling book in the next two years is 10%, and the probability of my summiting Mt. Baker in the next two years is 30%, are these two events dependent or independent?

1 / 1 point

- Independent
- Dependent



Correct

We know this because the joint distribution of 5% does not equal the product distribution of  $(0.1) \times (0.3) = 3\%$ . If I summit Mt. Baker, I am more likely to publish a best-selling book, and vice versa.

3. The joint probability of my summittng Mt. Baker in the next two years AND my publishing a best-selling book in the next two years is .05.

1 / 1 point

If the probability of my publishing a best-selling book in the next two years is 10%, and the probability of my summittng Mt. Baker in the next two years is 30%, what is the probability that (sadly) in the next two years I will neither summit Mt. Baker nor publish a best-selling book?

.95

.65

.9

.25

 Correct

Set A = I will summit Mt. Baker in the next two years

Set B = I will publish a best-selling book in the next two years.

Since  $p(A) = 0.3$  and  $p(A, B) = 0.05$ , by the SUM RULE we know that  $p(A, \sim B) = (0.3 - 0.05) = 0.25$

Since  $p(B) = 0.1, p(\sim B) = 0.9$

Since  $p(\sim B) = 0.9$  and  $p(A, \sim B) = 0.25$  and again by the SUM RULE,  $p(\sim A, \sim B) = 0.9 - 0.25 = .65$

4. I have two coins. One is fair, and has a probability of coming up heads of .5. The second is bent, and has a probability of coming up heads of .75. If I toss each coin once, what is the probability that *at least* one of the coins will come up heads?

1 / 1 point

- .875
- 1.0
- .625
- .375

 Correct

We apply the rule  $p(A \text{ or } B \text{ or both})$

$$= 1 - (p(\sim A)p(\sim B))$$

$$= 1 - ((1 - .5)(1 - .75))$$

$$= 1 - .125$$

$$=.875$$

5. What is  $\begin{aligned} \frac{11!}{9!} \end{aligned}$ ?

1 / 1 point

- 554,400
- 110,000
- 110
- 4,435,200

 Correct

$$\begin{aligned} \frac{11!}{9!} = 11 \times 10 = 110 \end{aligned}$$

6. What is the probability that, in six throws of a die, there will be exactly one each of “1” “2” “3” “4” “5” and “6”?

1 / 1 point

- .01543210
- .01176210
- .01432110
- .00187220

 Correct

There are  $6! = 720$  permutations where each face occurs exactly once.

There are  $6 \times 6 \times 6 \times 6 \times 6 \times 6 = 46656$  total permutations of 6 throws.

The probability is therefore  $\begin{aligned} \frac{720}{46656} = 0.01543210 \end{aligned}$

7. On 1 day in 1000, there is a fire and the fire alarm rings.

1 / 1 point

On 1 day in 100, there is no fire and the fire alarm rings (false alarm)

On 1 day in 10,000, there is a fire and the fire alarm does not ring (defective alarm).

On 9,889 days out of 10,000, there is no fire and the fire alarm does not ring.

If the fire alarm rings, what is the (conditional) probability that there is a fire?

Written  $p(\text{there is a fire} \mid \text{fire alarm rings})$

- 1.1%
- 9.09%
- 90.9%
- 1.12%

 Correct

10 days out of every 10,000 there is fire and the fire alarm rings.

100 days out of every 10,000 there is no fire and the fire alarm rings.

110 days out of every 10,000 the fire alarm rings.

The probability that there is a fire, given that the fire alarm rings, is  $\begin{aligned}\frac{10}{110} = \\ 9.09\%\end{aligned}$

8. On 1 day in 1000, there is a fire and the fire alarm rings.

1 / 1 point

On 1 day in 100, there is no fire and the fire alarm rings (false alarm)

On 1 day in 10,000, there is a fire and the fire alarm does not ring (defective alarm).

On 9,889 days out of 10,000, there is no fire and the fire alarm does not ring.

If the fire alarm does not ring, what is the (conditional) probability that there is a fire?

$p(\text{there is a fire} \mid \text{fire alarm does not ring})$

- 0.01011%
- .10011%
- 1.0001%
- .01000%

✓ Correct

On  $(1 + 9,889) = 9,890$  days out of every 10,000 the fire alarm does not ring.

On 1 of those 10,000 days there is a fire.

$$\begin{aligned} \frac{1}{9890} &= 0.01011\% \end{aligned}$$

9. A group of 45 civil servants at the State Department are newly qualified to serve as Ambassadors to foreign governments. There are 22 countries that currently need Ambassadors. How many distinct groups of 22 people can the President promote to fill these jobs?

0 / 1 point

- $= 2.429 * (10^{-13})$
- $8.2334 \times (10^{12})$
- $= 1.06 * (10^{35})$
- $\$4.1167 \times (10^{12})$

! Incorrect

$$\binom{45}{22}$$

$$= 45! / (23!)(22!)$$

$$\begin{aligned} &= \frac{45!}{23! \times 22!} \end{aligned}$$

- Applying Bayes Theorem and the Binomial Theorem - Practice quiz on Bayes Theorem and the Binomial Theorem (9 questions)

1. A jewelry store that serves just one customer at a time is concerned about the safety of its isolated customers.

1 / 1 point

The store does some research and learns that:

- 10% of the times that a jewelry store is robbed, a customer is in the store.
- A jewelry store has a customer on average 20% of each 24-hour day.
- The probability that a jewelry store is being robbed (anywhere in the world) is 1 in 2 million.

What is the probability that a robbery will occur while a customer is in the store?

- $\begin{aligned} &\frac{1}{500000} \end{aligned}$
- $\begin{aligned} &\frac{1}{2000000} \end{aligned}$
- $\begin{aligned} &\frac{1}{4000000} \end{aligned}$
- $\begin{aligned} &\frac{1}{5000000} \end{aligned}$



Correct

What is known is:

$$A: \text{"a customer is in the store," } P(A) = 0.2$$

$$B: \text{"a robbery is occurring," } P(B) = \frac{1}{2,000,000}$$

$$P(\text{a customer is in the store} \mid \text{a robbery occurs}) = P(A \mid B)$$

$$P(A \mid B) = 10\%$$

What is wanted:

$$P(\text{a robbery occurs} \mid \text{a customer is in the store}) = P(B \mid A)$$

By the product rule:

$$\begin{aligned} P(B \mid A) &= \frac{P(A \cap B)}{P(A)} \\ &= \frac{P(A) \cdot P(B \mid A)}{P(A)} \end{aligned}$$

$$\text{and } P(A, B) = P(A \mid B)P(B)$$

Therefore:

$$\begin{aligned} P(B \mid A) &= \frac{P(A \mid B)P(B)}{P(A)} \\ &= \frac{(0.1) \left( \frac{1}{2,000,000} \right)}{0.2} \\ &= \frac{1}{4000000} \end{aligned}$$

2. If I flip a fair coin, with heads and tails, ten times in a row, what is the probability that I will get exactly six heads?

1 / 1 point

- 0.021
- 0.187
- 0.2051
- 0.305

 Correct

By Binomial Theorem, equals

$$\begin{aligned} \binom{10}{6} \left(0.5^6\right) \end{aligned}$$

$$\begin{aligned} &= \left(\frac{10!}{6!4!}\right) \left(\frac{1}{1024}\right) \\ &\approx 0.2051 \end{aligned}$$

3. If a coin is bent so that it has a 40% probability of coming up heads, what is the probability of getting exactly 6 heads in 10 throws?

1 / 1 point

- 0.0974
- 0.1045
- 0.1115
- 0.1219

 Correct

$$\binom{10}{6} \times 0.4^6 \times 0.6^4 = 0.1115$$

4. A bent coin has 40% probability of coming up heads on each independent toss. If I toss the coin ten times, 1 / 1 point  
what is the probability that I get at least 8 heads?

- 0.0123
- 0.0132
- 0.0213
- 0.0312

**Correct**

The answer is the sum of three binomial probabilities:

$$\left(\binom{10}{8} \times (0.4^8) \times (0.6^2)\right) + \left(\binom{10}{9} \times (0.4^9) \times (0.6^1)\right) + \\ \left(\binom{10}{10} \times (0.4^{10}) \times (0.6^0)\right)$$

5. Suppose I have a bent coin with a 60% probability of coming up heads. I throw the coin ten times and it comes up heads 8 times. 1 / 1 point

What is the value of the "likelihood" term in Bayes' Theorem -- the conditional probability of the data given the parameter.

- 0.122885
- 0.168835
- 0.043945
- 0.120932

**Correct**

Bayesian "likelihood" --- the  $p(\text{observed data} \mid \text{parameter})$  is

$$p(8 \text{ of } 10 \text{ heads} \mid \text{coin has } p = .6 \text{ of coming up heads})$$

$$\binom{10}{8} \times (0.6^8) \times (0.4^2) = 0.120932$$

6. We have the following information about a new medical test for diagnosing cancer.

1 / 1 point

Before any data are observed, we know that 5% of the population to be tested actually have Cancer.

Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer. The other 10% get a false test result of "Negative" for Cancer.

Of the people who do not have cancer, 90% of them get an accurate test result of "Negative" for cancer. The other 10% get a false test result of "Positive" for cancer.

**What is the conditional probability that I have Cancer, if I get a "Positive" test result for Cancer?**

\*\*Formulas in the feedback section are very long, and do not fit within the standard viewing window. Therefore, the font is a bit smaller and the word "positive test" has been abbreviated as PT.

- 67.9%
- 4.5%
- 32.1% probability that I have cancer
- 9.5%



Correct

I still have a more than  $\frac{2}{3}$  probability of not having cancer

Posterior probability:

$p(\text{I actually have cancer} \mid \text{receive a "positive" Test})$

By Bayes Theorem:

$$= \frac{(\text{chance of observing a PT if I have cancer})(\text{prior probability of having cancer})}{(\text{marginal likelihood of the observation of a PT})}$$

$$= \frac{p(\text{receiving positive test} \mid \text{has cancer})p(\text{has cancer} \mid \text{before data is observed})}{p(\text{positive} \mid \text{has cancer})p(\text{has cancer}) + p(\text{positive} \mid \text{no cancer})p(\text{no cancer})}$$

$$= (90\%)(5\%) / ((90\%)(5\%) + (10\%)(95\%)$$

$$= 32.1\%$$

7. We have the following information about a new medical test for diagnosing cancer.

1 / 1 point

Before any data are observed, we know that 8% of the population to be tested actually have Cancer.

Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer.

The other 10% get a false test result of "Negative" for Cancer.

Of the people who do not have cancer, 95% of them get an accurate test result of "Negative" for cancer.

The other 5% get a false test result of "Positive" for cancer.

What is the conditional probability that I have cancer, if I get a "Negative" test result for Cancer?

- 0.9%
- 99.1%
- 88.2%
- .80%

✓ Correct

$$p(\text{cancer} \mid \text{negative test}) =$$

$$\frac{p(\text{negative test} \mid \text{Cancer}) p(\text{Cancer})}{p(\text{negative test} \mid \text{cancer}) p(\text{cancer}) + p(\text{negative test} \mid \text{no cancer}) p(\text{no cancer})}$$

$$\frac{(10\%)(8\%)}{(10\%)(8\%) + (95\%)(92\%)}$$

$$\frac{0.8\%}{0.8\% + 87.4\%}$$

$$\frac{0.8\%}{88.2\%}$$

$$= 0.9\%$$

8. An urn contains 50 marbles - 40 blue and 10 white. After 50 draws, exactly 40 blue and 10 white are observed.

1 / 1 point

You are not told whether the draw was done "with replacement" or "without replacement."

What is the probability that the draw was done with replacement?

- 13.98%
- 12.27%
- 1
- 87.73%

 Correct

$p(40 \text{ blue and } 10 \text{ white} \mid \text{draws without replacement}) = 1$  [this is the only possible outcome when 50 draws are made without replacement]

$p(40 \text{ blue and } 10 \text{ white} \mid \text{draws with replacement})$

$$S = 40$$

$$N = 50$$

$P = .8$  [for draws with replacement] because 40 blue of 50 total means  $p(\text{blue}) = 40/50 = .8$

$$\left(\binom{50}{40}\right)(0.8^{40})(0.2^{10})$$

$$= 13.98\%$$

By Bayes' Theorem:

$p(\text{draws with replacement} \mid \text{observed data}) =$

$$\frac{13.98\%(.5)}{(13.98\%)(.5)+(1)(.5)}$$

$$= \frac{0.1398}{1.1398}$$

$$= 12.27\%$$

9. According to Department of Customs Enforcement Research: 99% of people crossing into the United States are not smugglers.

1 / 1 point

The majority of all Smugglers at the border (65%) appear nervous and sweaty.

Only 8% of innocent people at the border appear nervous and sweaty.

If someone at the border appears nervous and sweaty, what is the probability that they are a Smuggler?

- 92.42%
- 8.57%
- 7.58%
- 7.92%



Correct

By Bayes' Theorem, the answer is

$$\begin{aligned} & \frac{(0.65)(0.01)}{((0.65)(0.01) + (0.08)(0.99))} \\ & = 7.58\% \end{aligned}$$

- Applying Bayes Theorem and the Binomial Theorem - Probability (basic and Intermediate) Graded Quiz (12 questions)

1. What additional statement, added to the three below, forms a probability distribution?

1 / 1 point

(1) I missed only my first class today

(2) I missed only my second class today

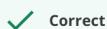
(3) I missed both my first and second class today



Correct

2. My friend takes 10 cards at random from a 52-card deck, and places them in a box. Then he puts the other 42 cards in a second, identical box. He hands me one of the two boxes and asks me to draw out the top card. What is the probability that the first card I draw will be the Ace of Spades?

1 / 1 point



Correct

3. I will go sailing today if it does not rain. Are the following two statements Independent or dependent?

1 / 1 point

(1) "I will go sailing today"

(2) "It will not rain today"

 Correct

4. The probability that I will go sailing today AND the fair six-sided die will come up even on the next roll is .3.

1 / 1 point

If these events are independent, what is the probability that I will go sailing today?

 Correct

5. I have two coins. One is fair, and has a probability of coming up heads of .5.

1 / 1 point

The second is bent, and has a probability of coming up heads of .75. \begin{aligned}\text{If I toss each coin once, what is the probability that at least one of the coins will come up tails?}\end{aligned}

 Correct

6. What is the probability, when drawing 5 cards from a fair 52-card deck, of drawing a "full house" (three of a kind and a pair) in the form AAABB?

1 / 1 point

 Correct

7. If it rains, I do not go sailing. It rains 10% of days; I go sailing 3% of days.

1 / 1 point

If it does not rain, what is the (conditional) probability that I go sailing?

Written " $p(I \text{ go sailing} | \text{ it does not rain})$ "?

 Correct

8. I am at my office AND not working 2% of the time. I am at my office 10% of the time. What is the conditional probability that I am not working, if I am at my office?

1 / 1 point

 Correct

9. The factory quality control department discovers that the conditional probability of making a manufacturing mistake in its precision ball bearing production is 4% on Tuesday, 4% on Wednesday, 4% on Thursday, 8% on Monday, and 12% on Friday.

1 / 1 point

The Company manufactures an equal amount of ball bearings (20%) on each weekday. What is the probability that a defective ball bearing was manufactured on a Friday?

 Correct

10. An Urn contains two white marbles and one black marble. A marble is drawn from the Urn without replacement and put aside without my seeing it. Then a second marble is drawn, and it is white.

0 / 1 point

What is the probability that the unknown removed marble is white, and what is the probability that it is black?

 Incorrect



You passed this course! Your grade is 88.10%.

Item	Status	Due	Weight	Grade
 <a href="#">Graded quiz on Sets, Number Line, Inequalities, Si...</a> Quiz	Passed	Oct 11 11:59 PM PDT	25%	<b>100%</b>
 <a href="#">Graded quiz on Cartesian Plane and Types of Funct...</a> Quiz	Passed	 Oct 18 11:59 PM PDT	25%	<b>92.30%</b>
 <a href="#">Graded quiz on Tangent Lines to Functions, Expone...</a> Quiz	Passed	Oct 25 11:59 PM PDT	25%	<b>76.92%</b>
 <a href="#">Probability (basic and Intermediate) Graded Quiz</a> Quiz	Passed	Nov 1 10:59 PM PST	25%	<b>83.33%</b>

