

# Introduction

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Hash Function :

- Input - String (Any Size)
- Output - Fixed Size (256 bits - Bitcoins)
- Efficiently computable (Real Time)

Security Properties of Hash Function :

- Collision Free  $\rightarrow x \neq y$  and  $H(x) = H(y)$  Collisions do exist

To find a collision -- Try  $2^{130}$  random inputs their is 99.8% probability that 2 inputs collide  
( No matter what hash function is ... )

No Hash function is collision free but the people have found that it is very hard to find collision and hence proved to be collision free.

Application : 1. Message Digest (Compare Files)

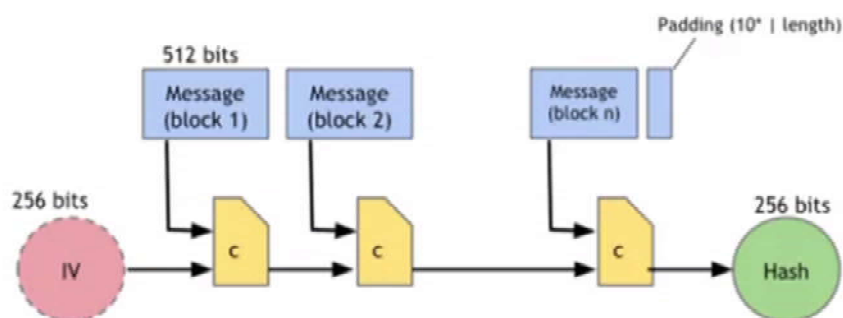
- Hiding  $\rightarrow$  Given  $H(x)$  no way to figure what is  $x$  --  $x$  has to be from a set that should be spread out (Not like Heads and Tails)  
Solution to this problem is to choose  $r$  from a probability distribution that has high min-entropy, then given  $H(r|x)$ , it is infeasible to find  $x$ .  
high min-entropy  $\rightarrow$  spread out

Security Properties :

- Hiding : Given commitment  $H(\text{key} | \text{msg})$  unable to find  $\text{msg}$
- Binding:  $\text{msg} \neq \text{msg}$  such that  $H(\text{key} | \text{msg}) = H(\text{key} | \text{msg})$
- Puzzle Friendly: For every possible  $y$ , if  $k$  is chosen from a distribution that has high min-entropy then it is infeasible to find  $x$  such that  $H(k | x) = y$   
Application : Search Puzzle (Bit coin mining) No way to find solution other than searching for solution

Hash Function that BIT COIN Uses : SHA - 256

## SHA-256 hash function



C is called compression function

IV is standard value that we look up

No collisions ever found