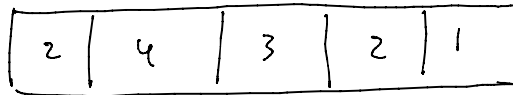
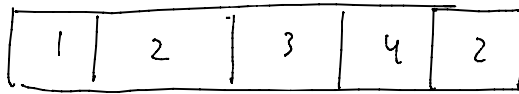
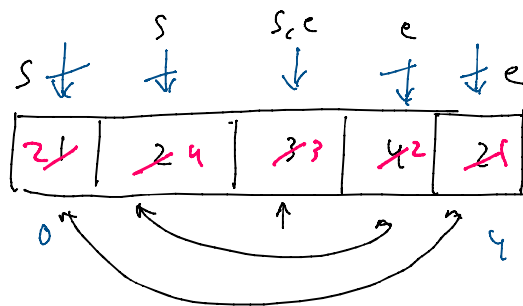


4. Problems on Functional Recursion

① Reverse an Array



Naive Approach



for loop/while

$s = 0$

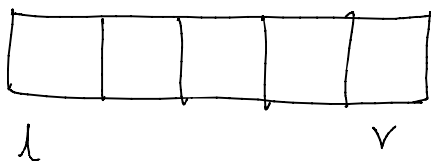
$e = n - 1$

$\text{swap}(s, e)$

$s++$

$e--$

Recursion Using Two Pointer :

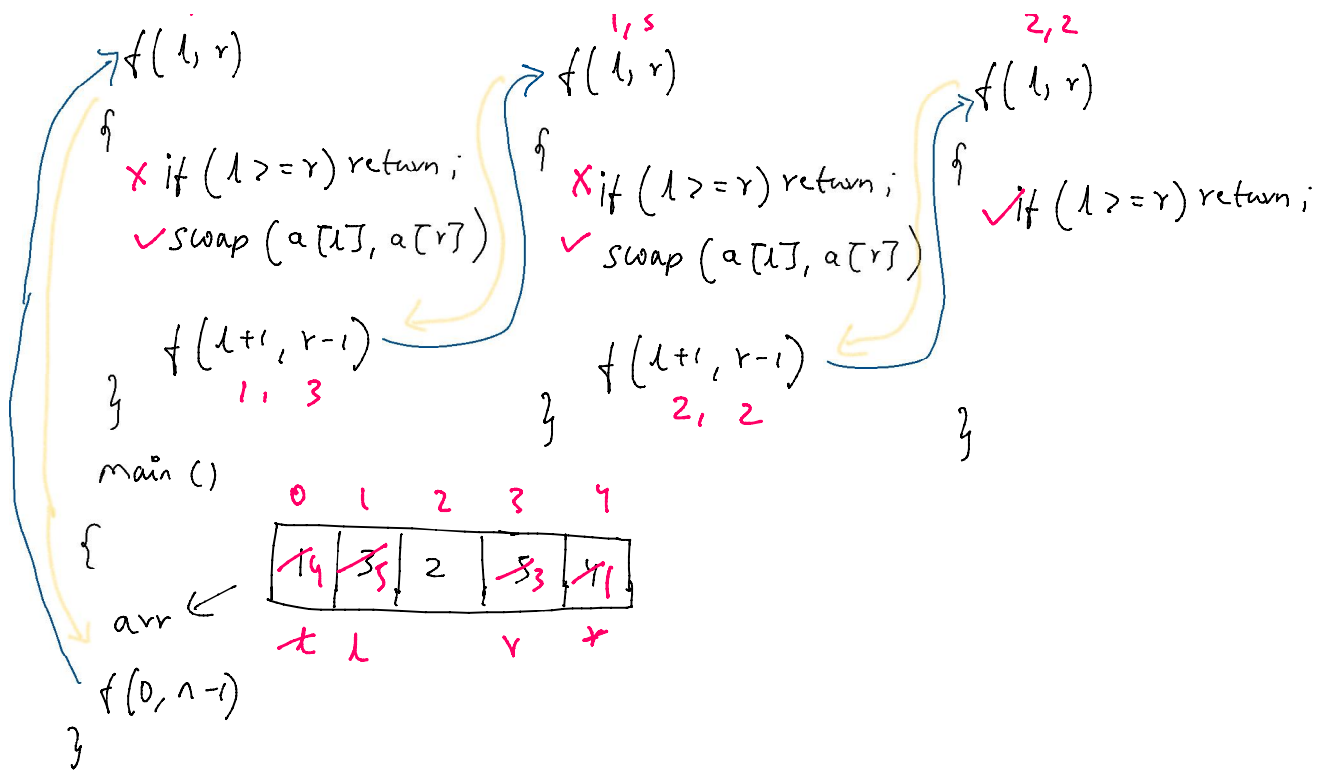


\Rightarrow Recursion job is to swap and $l++$ and $r--$

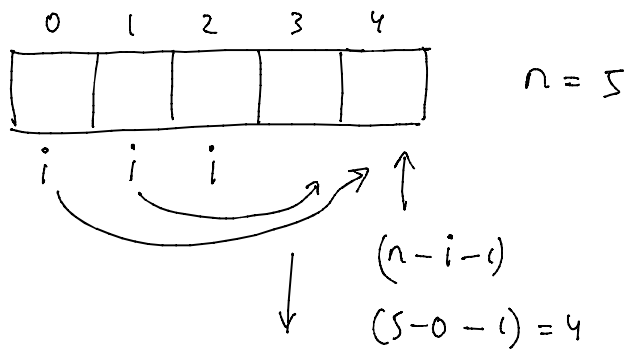
$0, 4$
 $\rightarrow f(l, r)$

$1, 3$
 $\rightarrow f(l, r)$

$2, 2$
 $\rightarrow f(l, r)$



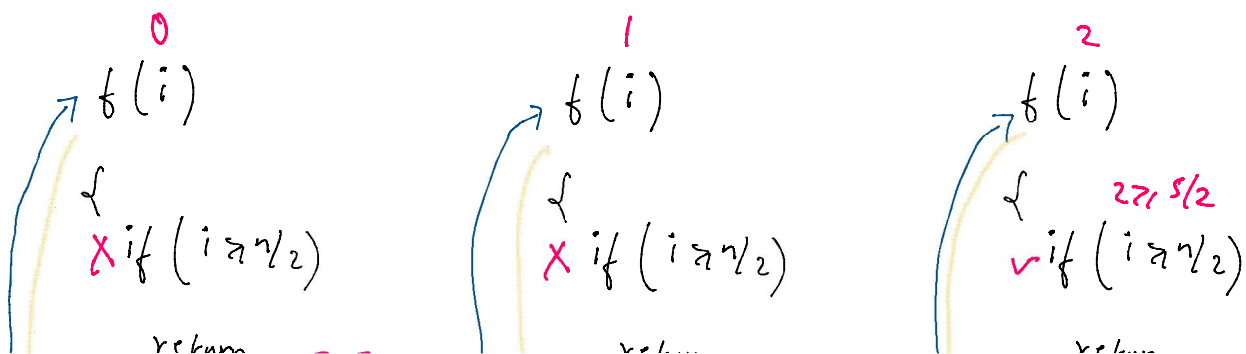
Can you solve this using single pointer?



$$\begin{aligned}
 &(n-i-1) \\
 &5-1-1 \\
 &= 3
 \end{aligned}
 \quad \text{swap}(i, n-i-1)$$

How long?

$(i \geq n/2)$ until middle



```

    if (i < n/2)
        return
        a[i], a[n-i-1];
    swap(a[i], a[n-i-1]);
    f(i+1);
}

main()
{
    arr;
    f(0);
}

```

```

    if (i < n/2)
        return
        a[i], a[n-i-1];
    swap(a[i], a[n-i-1]);
    f(i+1);
}

```

```

    if (i < n/2)
        return
        swap(a[i], a[n-i-1]);
    f(i+1);
}

```

```

#include<bits/stdc++.h>
using namespace std;
void reverse(int i, int arr[], int n){
    //base
    if(i >= n/2) return;
    swap(arr[i], arr[n-i-1]);
    reverse(i+1, arr, n);
}

int main(){
    int n;
    cin >> n;
    int arr[n];
    for(int i = 0; i < n; i++)
        cin >> arr[i];
    reverse(0, arr, n);
    for(int i = 0; i < n; i++)
        cout << arr[i] << " ";
    return 0;
}

```

```

1 5
2 1 2 3 4 5

```

```

1 5 4 3 2 1

```

② Palindrome :

Check if a string is palindrome or not

"MADAM" $\xrightarrow{\text{reverse}}$ "MADAM" (true)

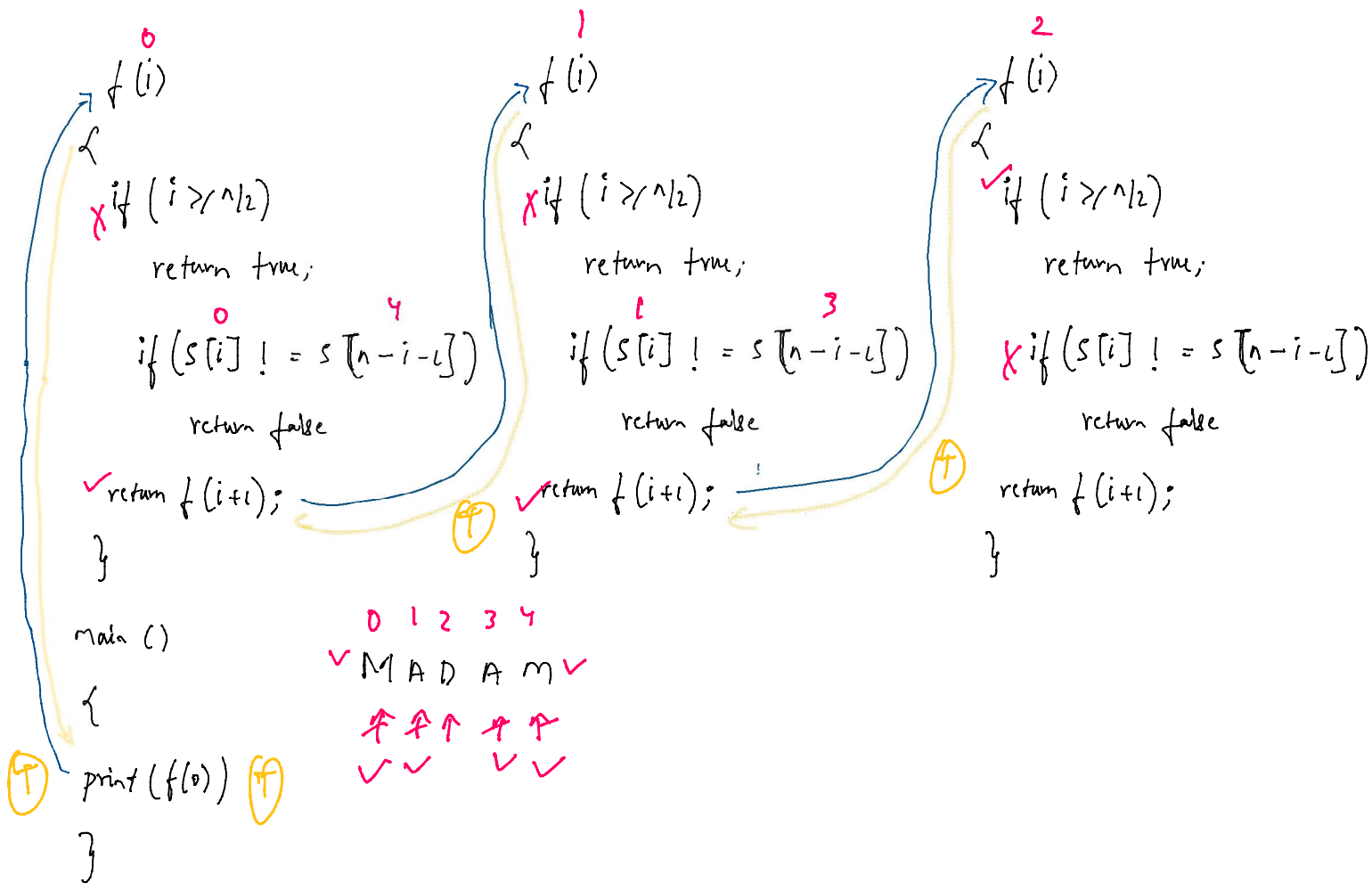
"11211" $\xrightarrow{\text{reverse}}$ "11211" (true)

"123" $\xrightarrow{\text{reverse}}$ "321" (false)

* It's same like reversing, the left half and the right half

should be same.

↓ ↓ ↓ ↓ ↓
M A D A M



```

#include<bits/stdc++.h>
using namespace std;
bool f(int i, string &s) {
    if(i >= s.size() / 2) return true;
    if(s[i] != s[s.size() - i - 1]) return false;
    return f(i+1, s);
}
int main() {
    #ifndef ONLINE_JUDGE
    freopen("input.txt", "r", stdin);
    freopen("output.txt", "w", stdout);
    #endif
    string s = "madam";
    cout << f(0, s);
    return 0;
}

```

True

T.C $\Rightarrow O(n/2)$ // till half you are going

S.C $\Rightarrow O(n/2)$