

# CSE 4102

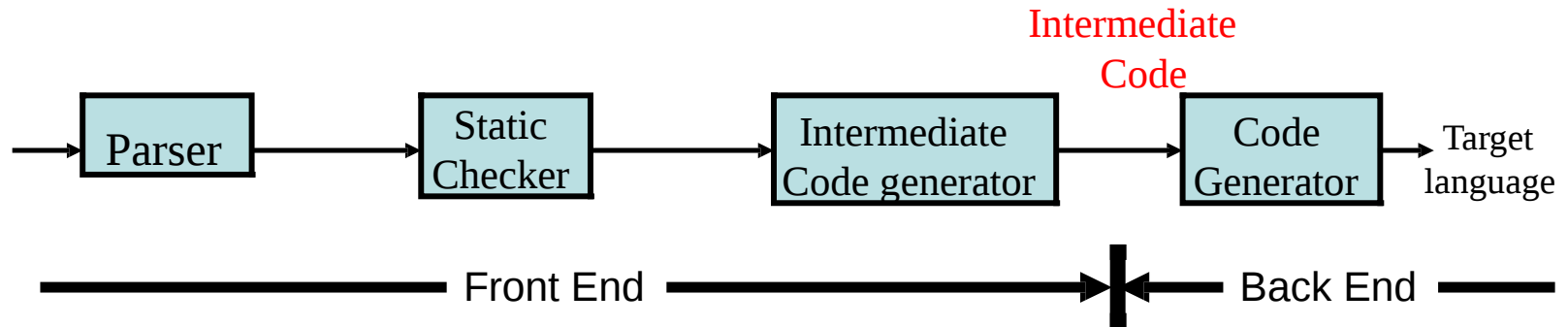
## Intermediate Code Generation

Compilers principles, techniques, & tools-

ULLMAN

Chapter 06

# Compiler Architecture



- $m \times n$  compilers can be built by writing  $m$  front ends and  $n$  back ends – save considerable amount of effort
- We assume parsing, static checking and IC generation is done sequentially
  - These can be combined and done during parsing
- Static checking
  - Operator operand compatibility
  - Proper placement of break/continue keywords etc.

# Intermediate Code (IC)

- The given program in a source language is converted to an equivalent program in an intermediate language by the IC generator.
- Ties the front and back ends together
- Language and Machine neutral
- Many forms
- Level depends on how being processed
- More than one intermediate language may be used by a compiler

# Intermediate Representations

- In most compilers, the parser builds an *intermediate representation* of the program
- Rest of the compiler transforms the IR to “improve” (optimize) it and eventually translates it to final code
  - Often will transform initial IR to one or more different IRs along the way

# IR Design

- Decisions affect speed and efficiency of the rest of the compiler
- Desirable properties
  - Easy to generate
  - Easy to manipulate
  - Expressive
  - Appropriate level of abstraction
- Different tradeoffs depending on compiler goals
- Different tradeoffs in different parts of the same compiler

# Types of IRs

- Three major categories
  - Structural
  - Linear
  - Hybrid
- Some basic examples now; more when we get to later phases of the compiler

# Levels of Abstraction

- Key design decision: how much detail to expose
  - Affects possibility and profitability of various optimizations
  - Structural IRs are typically fairly high-level
  - Linear IRs are typically low-level
  - But these generalizations don't always hold

# Intermediate language levels

- **High**

$T1 \leftarrow a[i,j+2]$

- **Medium**

$t1 \leftarrow j + 2$

$t2 \leftarrow i * 20$

$t3 \leftarrow t1 + t2$

$t4 \leftarrow 4 * t3$

$t5 \leftarrow \text{addr } a$

$t6 \leftarrow t5 + t4$

$t7 \leftarrow *t6$

- **Low**

$r1 \leftarrow [fp-4]$

$r2 \leftarrow r1 + 2$

$r3 \leftarrow [fp-8]$

$r4 \leftarrow r3 * 20$

$r5 \leftarrow r4 + r2$

$r6 \leftarrow 4 * r5$

$r7 \leftarrow fp - 216$

$f1 \leftarrow [r7+r6]$



# Intermediate Languages Types

- Graphical IRs:
  - Syntax trees
  - Abstract Syntax trees
  - Directed Acyclic Graphs (DAGs)
  - Control Flow Graphs
- Linear IRs:
  - Stack based (postfix)
  - Three address code (quadruples)

# Graphical IRs

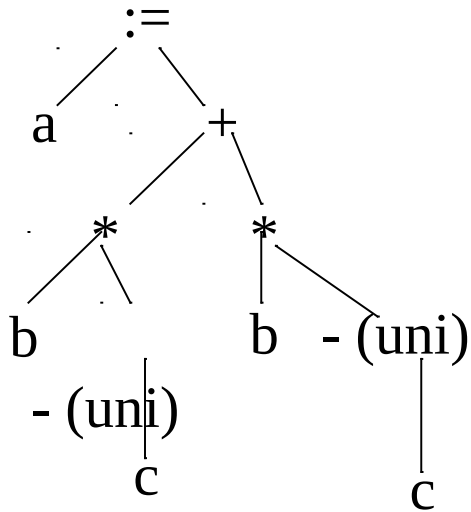
- Concrete Syntax Trees
- Abstract Syntax Trees (AST) – retain essential structure of the parse tree, eliminating unneeded nodes.
- Directed Acyclic Graphs (DAG) – compacted AST to avoid duplication – smaller footprint as well
- Control flow graphs (CFG) – explicitly model control flow

# Structural IRs

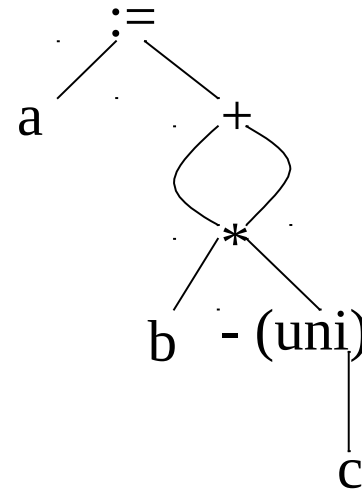
- *Typically reflect source (or other higher-level) language structure*
- *Tend to be large*
- Examples: syntax trees, DAGs
- Particularly useful for source-to-source transformations
- The full grammar is needed to guide the parser, but contains many extraneous details
- Typically the full syntax tree does not need to be used explicitly

# ASTs and DAGs:

$a := b * -c +$   
 $b * -c$



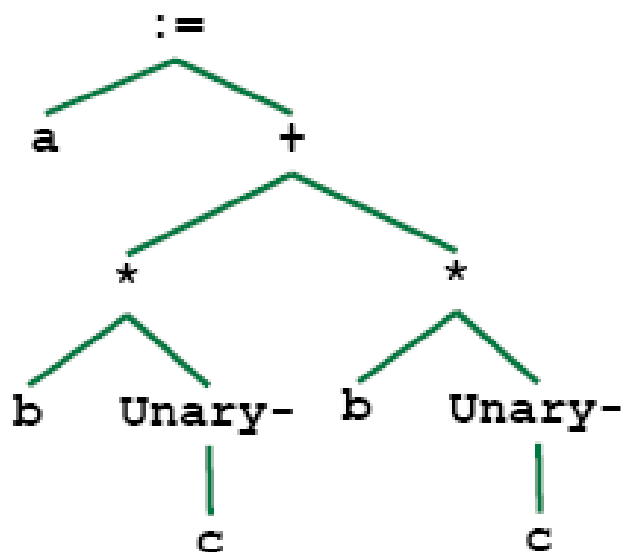
AST



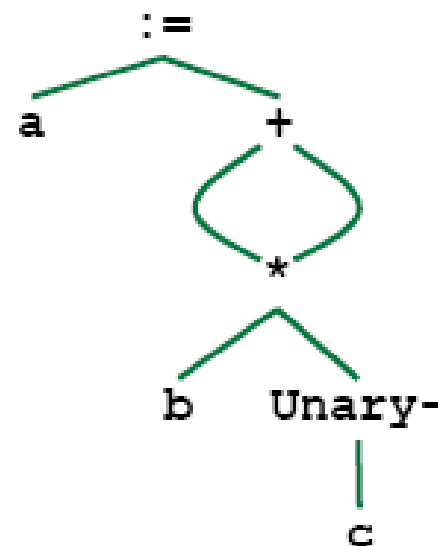
DAG

# Implementation of DAG/AST: Value Number Method

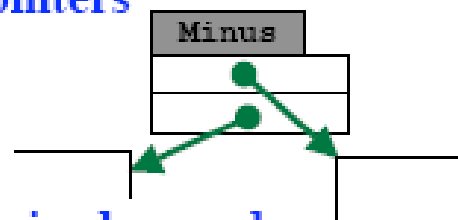
Tree:



DAG:



Structures and Pointers



An array of fixed-sized records

Q: How to build DAG's (i.e., trees with shared, common parts)?

A: When you are about to allocate a new node; look to see if you already have one with the same info.

0	id	b	-
1	id	c	-
2	unary-	1	-
3	mult	0	2
4	id	b	-
5	id	c	-
6	unary-	5	-
7	mult	4	6
8	add	3	7
9	id	a	-
10	assign	9	8

# Three-Address code

- Many different representations
- General form:  $x \leftarrow y \text{ (op) } z$ 
  - One operator
  - Maximum of three names
- Example:  $x = 2 * (n + m)$ ; becomes
  - $t1 \leftarrow n + m$
  - $t2 \leftarrow 2 * t1$
  - $x \leftarrow t2$

# Three Address Code (cont)

- Advantages
  - Resembles code for actual machines
  - Explicitly names intermediate results
  - Compact
  - Often easy to rearrange
- Various representations
  - Quadruples, triples, SSA
  - Much more later...

# Three-Address Code

- A three-address code is:

$x := y \text{ } \mathbf{op} \text{ } z$

where  $x$ ,  $y$  and  $z$  are names, constants or compiler-generated temporaries;  $\mathbf{op}$  is any operator.

- But we may also the following notation for three-address code (it looks like a machine code instruction)

$\mathbf{op} \quad y, z, x$

apply operator  $\mathbf{op}$  to  $y$  and  $z$ , and store the result in  $x$ .

- We use the term **“three-address code”** because **each statement usually contains three addresses** (two for operands, one for the result).



# Linearized Representation of DAG/AST

- Source Code
  - $a = b * -c + b * -c$
- Three address code

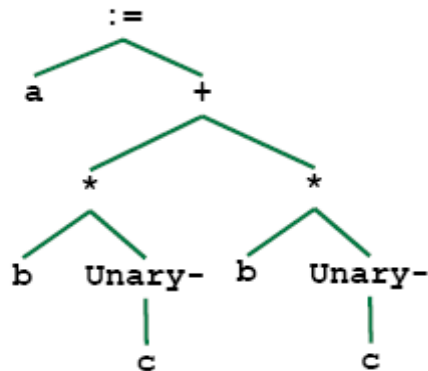
Each instruction has (up to) 3 operands.

```
t1 := -c
t2 := b * t1
t3 := -c
t4 := b * t3
t5 := t2 + t4
a := t5
```

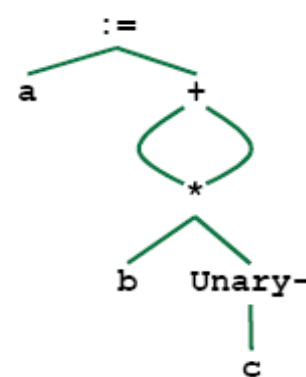
```
neg    c    ⇒ t1
mult   b,t1  ⇒ t2
neg    c    ⇒ t3
mult   b,t3  ⇒ t4
add    t2,t4 ⇒ t5
move   t5    ⇒ a
```

- Tree Representation

Tree:



DAG:



# Three-Address Statements

**Binary Operator:**  $\text{op } y, z, \text{result}$  or  
 $\text{result} := y \text{ op } z$

where  $\text{op}$  is a binary arithmetic or logical operator. This binary operator is applied to  $y$  and  $z$ , and the result of the operation is stored in  $\text{result}$ .

Ex:

$\text{add } a, b, c$

$\text{gt } a, b, c$

$\text{addr}$

$a, b, c$

$\text{addi } a, b, c$

**Unary Operator:**  $\text{op } y, \text{result}$  or  
 $\text{result} := \text{op } y$

where  $\text{op}$  is a unary arithmetic or logical operator. This unary operator is applied to  $y$ , and the result of the operation is stored in  $\text{result}$ .

Ex:

$\text{uminus}$

$a, , c$

# Three-Address Code

- Two concepts
  - Address
  - Instruction
- Address
  - Name: source-program names to appear as addresses
  - Constant: Different types of constants
  - Compiler Generated temporary:

# Three-Address Instruction

**Assignment Type 1:**  $x \quad := \quad y \quad op \quad z$

$op$  is a binary arithmetic or logical operation

$x$ ,  $y$  and  $z$  are addresses

**Assignment Type 2:**  $x \quad := \quad op \quad z$

$op$  is a unary arithmetic or logical operation

$x$  and  $z$  are addresses

**Copy Instruction:**  $x \quad := \quad y$

$x$  and  $z$  are addresses and  $x$  is assigned the value of  $y$

# Three-Address Instructions

## Unconditional Jump: `goto L`

We will jump to the three-address code with the label L, and the execution continues from that statement.

```
Ex:      goto    L1      // jump to L1
         jmp     7        // jump to the statement 7
```

## Conditional Jump 1: `if x goto L and if False x goto L`

We will jump to the three-address code with the label L if x is TRUE and FALSE, respectively. Otherwise, the following three-address instruction in sequence is executed next.

## Conditional Jump 2: `if x relop y goto L`

We will jump to the three-address code with the label L if the result of y *relop* z is true, and the execution continues from that statement. If the result is false, the execution continues from the statement following this conditional jump statement.

# Three-Address Statements (cont.)

**Procedure Parameters:** `param x`

**Procedure Calls:** `call p, n`

where  $x$  is an actual parameter, we invoke the procedure  $p$  with  $n$  parameters.

Ex:

`param  $x_1$`

`param  $x_2$`

`.....`

`param  $x_n$`

`call p, n,`

$\rightarrow p(x_1, \dots, x_n)$

$\leftarrow$   $n$  is necessary because call  
can be nested

`f( $x+1$ ,  $y$ )`  $\rightarrow$  `add x, 1, t1`  
`param t1,,`  
`param y,,`  
`call f, 2,`

# Three-Address Statements (cont.)

## Indexed Assignments:

$x := y[i]$

sets  $x$  to the value in location  $i$  memory units beyond location  $y$

$y[i] := x$

sets contents of the location  $i$  memory units beyond location  $y$  to the value of  $x$

## Address and Pointer Assignments:

$x := \&y$

sets the **r-value** of  $x$  to **l-value** of  $y$

$x := *y$  where  $y$  is a pointer whose **r-value** is a location

sets the **r-value** of  $x$  equal to the contents of that location

$*x := y$

sets the **r-value** of the object pointed by  $x$  to the **r-value** of  $y$

# Three address code example

do  $i=i+1$ ; while ( $a[i] < v$ )

L:       $t_1=i+1$   
  
         $i=t_1$   
         $t_2=i*8$   
         $t_3=a[t_2]$   
        if  $t_3 < v$  goto L

(A) Symbolic Labels

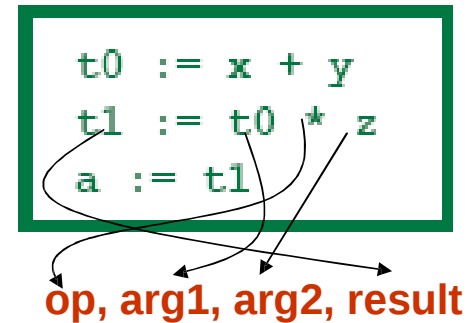
100:  $t_1 = i + 1$   
  
101:  $i = t_1$   
102:  $t_2 = i * 8$   
103:  $t_3 = a[t_2]$   
104: if  $t_3 < v$  goto 100

(B) Position Numbers



# Representing 3-Address Statements

- Quadruples (“Quads”)
- Triples
- Indirect Triples



- **x = minus y**
  - Does not use arg2
- **x = y**
  - Op is =
- **param a1**
  - Uses neither arg2 nor result
- Conditional/Unconditional jumps
  - Put the target label in result

# Quadruples

- $a = b * -c + b * -c$

```
t1 := -c
t2 := b * t1
t3 := -c
t4 := b * t3
t5 := t2 + t4
a := t5
```

Instr	Operation	Arg 1	Arg 2	Result
(0)	uminus	c		$t_1$
(1)	mult	b	$t_1$	$t_2$
(2)	add	a	$t_2$	$t_3$
(3)	move	$t_3$		a

# Quadruples

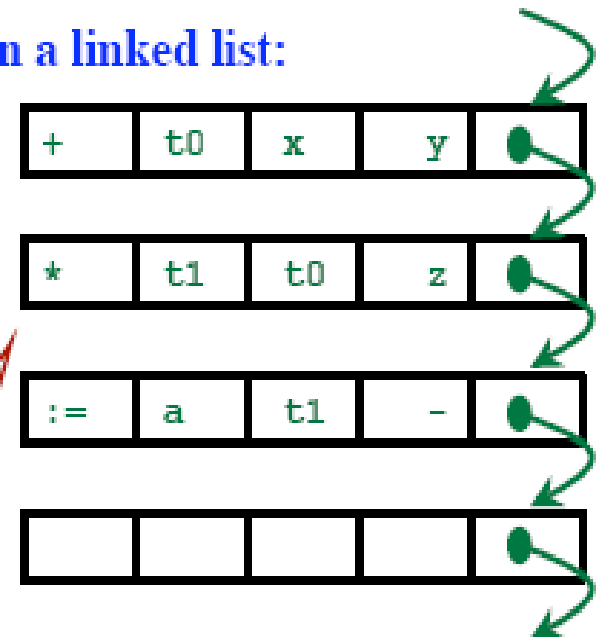
- Store each fields directly

... In an array:

0	+	t1	x	y
1	*	t2	t1	z
2	:=	a	t2	-
3				

*Less Space*

... In a linked list:



*Easier to re-order*

# Triples

Don't store the result directly.

Implicitly associate a temporary result with each triple.

```
t0 := x + y
t1 := t0 * z
a := t1
```

Avoids creating the temporaries.

Saves storage.

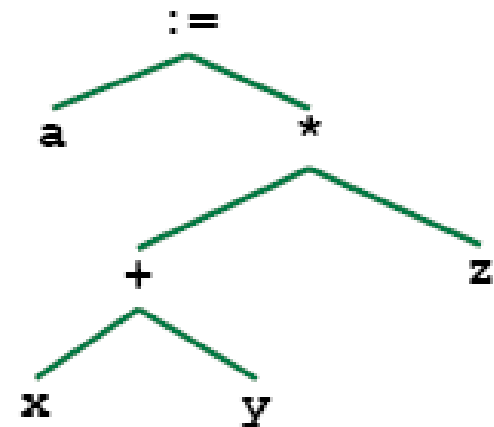
Difficult to re-order instructions.

0	+	x	y
1	*	0	z
2	:=	a	1
3			

The following instruction is difficult

```
x[i] := y
```

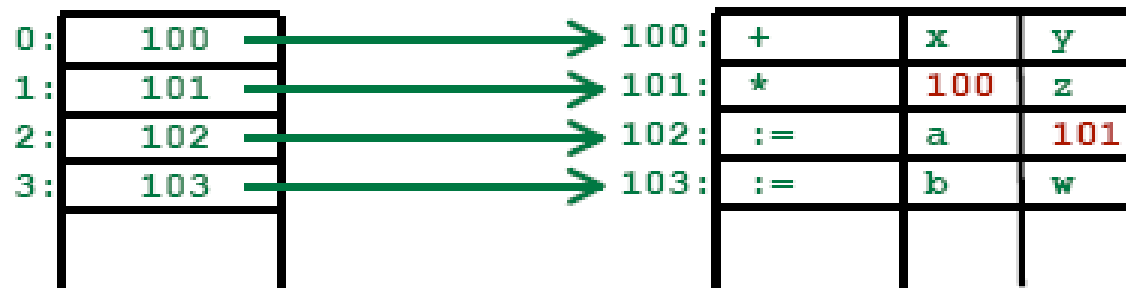
It takes 2 triples.



	op	arg1	arg2
0	[ ]=	x	i
1	:=	0	y

# Indirect Triples

Get around the re-ordering problem  
... by introducing another data structure.



## Quadruples

- Less indirection, simpler
- Easier to manipulate, reorder

## Triples

## Indirect Triples

- About same amount of space as quadruples
- May save space when lots of shared sub-expressions
- More complex

# Goal

Take a source statement and produce a sequence of IR quads:

## Example:

```
x := y + z;
```

## IR Quads:

```
t1 := y + z  
x := t1
```

## Example:

```
x := (y + z) * (u + v);
```

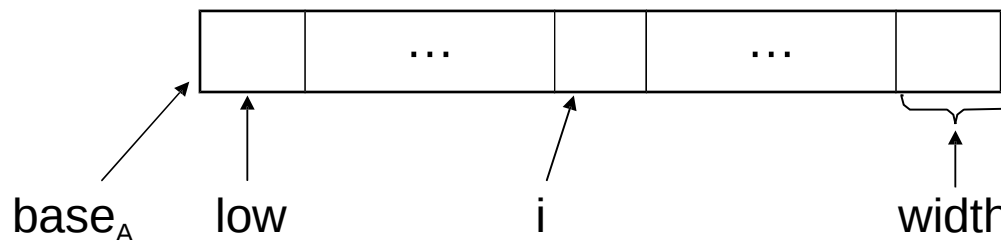
## IR Quads:

```
t1 := y + z  
t2 := u + v  
t3 := t1 * t2  
x := t3
```

# Addressing Array Elements

- Elements of arrays can be accessed quickly if the elements are stored in a block of consecutive locations.

A one-dimensional array **A**:



**base<sub>A</sub>** is the address of the first location of the array **A**,  
**width** is the width of each array element. **low** is the  
index of the first array element

$$\text{location of } A[i] \rightarrow \text{base}_A + (i - \text{low}) * \text{width}$$

# Addressing Array Elements (cont.)

$\text{base}_A + (i - \text{low}) * \text{width}$

can be re-written as

$i * \text{width}$

should be computed  
at run-time

$+ (\text{base}_A - \text{low} * \text{width})$

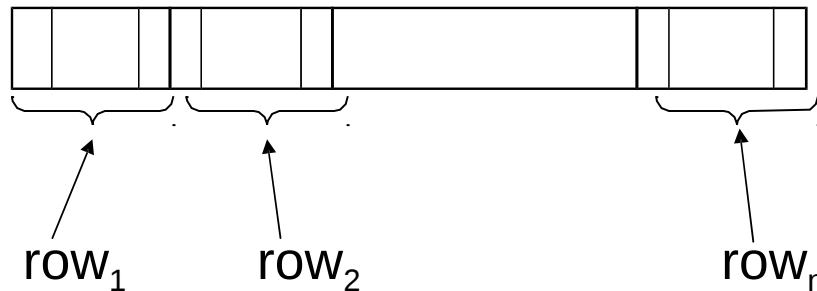
can be computed  
at compile-time

- So, the location of  $A[i]$  can be computed at the run-time by evaluating the formula  $i * \text{width} + c$  where  $c$  is  $(\text{base}_A - \text{low} * \text{width})$  which is evaluated at compile-time.
- Intermediate code generator should produce the code to evaluate this formula  $i * \text{width} + c$  (one multiplication and one addition operation).

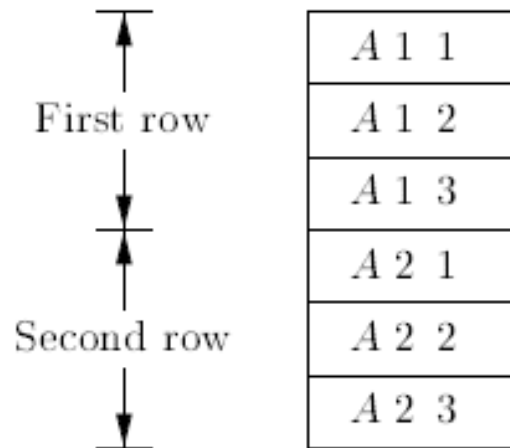


# Two-Dimensional Arrays

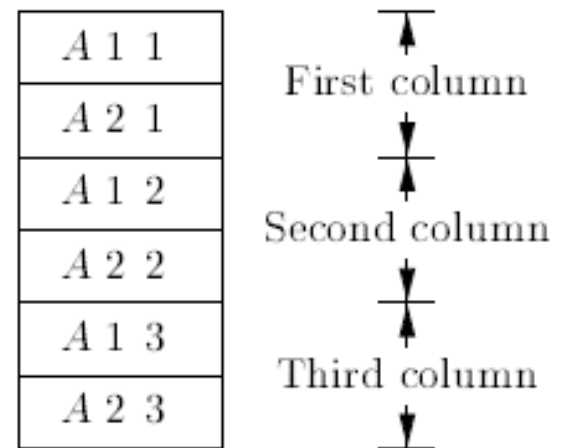
- A two-dimensional array can be stored in
  - either **row-major** (*row-by-row*) or
  - **column-major** (*column-by-column*).
- Most of the programming languages use **row-major** method.
- Row-major representation of a two-dimensional array:



# Layout of Two-Dimensional Arrays



a Row Major



b Column Major

# Two-Dimensional Arrays (cont.)

- The location of  $A[i_1, i_2]$  is

$$\text{base}_A + ((i_1 - \text{low}_1) * n_2 + i_2 - \text{low}_2) * \text{width}$$

$\text{base}_A$  is the location of the array  $A$ .

$\text{low}_1$  is the index of the first row

$\text{low}_2$  is the index of the first column

$n_2$  is the number of elements in each row

$\text{width}$  is the width of each array element

- Again, this formula can be re-written as

$$\underbrace{((i_1 * n_2) + i_2) * \text{width}}_{\substack{\text{(should be computed} \\ \text{at run-time)}}} + \underbrace{(\text{base}_A - \text{low}_1 * n_2 + \text{low}_2 * \text{width})}_{\substack{\text{can be computed} \\ \text{at compile-time}}}$$

# Multi-Dimensional Arrays

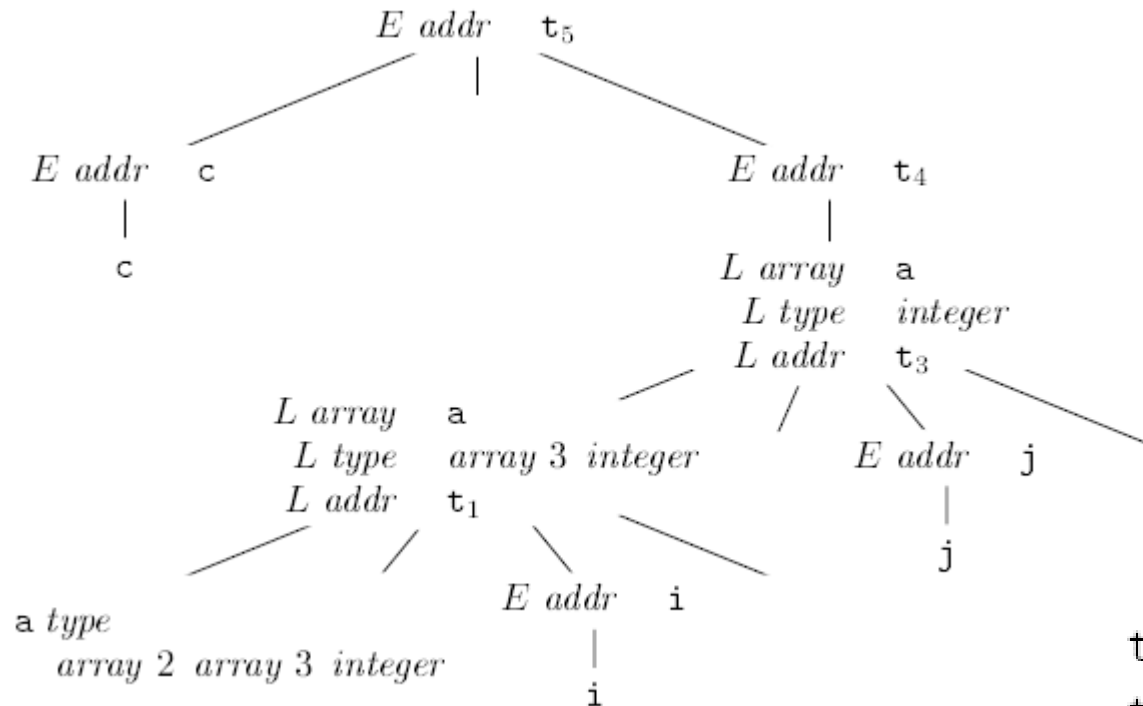
- In general, the location of  $A[i_1, i_2, \dots, i_k]$  is
- $(( \dots ((i_1 * n_2) + i_2) \dots) * n_k + i_k) * \text{width} + (\text{base}_A - ((\dots ((\text{low}_1 * n_1) + \text{low}_2) \dots) * n_k + \text{low}_k) * \text{width}))$
- So, the intermediate code generator should produce the codes to evaluate the following formula (to find the location of  $A[i_1, i_2, \dots, i_k]$ ) :
- $(( \dots ((i_1 * n_2) + i_2) \dots) * n_k + i_k) * \text{width} + c$
- To evaluate the  $(( \dots ((i_1 * n_2) + i_2) \dots) * n_k + i_k)$  portion of this formula, we can use the recurrence equation:
- $e_1 = i_1$
- $e_m = e_{m-1} * n_m + i_m$

# Translation of Array Elements

- One dimensional
  - $\text{base} + i \times w$
  - $w$ : width of each array element
- Two Dimensional
  - $\text{base} + i_1 \times w_1 + i_2 \times w_2$
  - $w_1$ : width of a row
  - $w_2$ : width of an element in a row
- $k$  dimensional (generalized)
  - $\text{base} + i_1 \times w_1 + i_2 \times w_2 + \dots + i_k \times w_k$

- Let  $a$  denote a 2x3 array of integers, and let  $c, i, j$  all integers. Then, type of  $a$  is  $\text{array}(2, \text{array}(3, \text{integer}))$ .

$W = 12 \text{ var} = 1$



$t_1$	$i$	12
$t_2$	$j$	4
$t_3$	$t_1$	$t_2$
$t_4$	$a$	$t_3$
$t_5$	$c$	$t_4$

*Any Question?*