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## Model Adaptation

- An on-line  $K$ -Means approx: to update  $\mathcal{N}(\cdot)$ s
  - Why? Stationary pixel process (time-invariant)? EM for time window (costly) Lighting & scene changes reduce past dependence
  - Either: matches one of the  $K$  Gaussians  $\sim 2.5\sigma$
  - Or: doesn't match any Gaussians  $\sim 2.5\sigma$
- If match with one of the  $K$  Gaussians  $\sim 2.5\sigma$ 
  - Update the 3 sets of parameters  $\mu_j, \Sigma_j, \pi_j$ :
  - $\mu_j, \Sigma_j$ : linear combo of old & new evidence:
    - \*  $\mu_j^{\tau+1} = (1 - \rho)\mu_j^{\tau} + \rho\mathbf{x}^{\tau+1}$
    - \*  $\Sigma_j^{\tau+1} = (1 - \rho)\Sigma_j^{\tau} + \rho(\mathbf{x}^{\tau+1} - \mu_j^{\tau+1})^T(\mathbf{x}^{\tau+1} - \mu_j^{\tau+1})$
    - \* Assume diagonal Cov, ind & same variances

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- $\rho \triangleq \alpha \mathcal{N}(\mathbf{x}^{\tau+1} | \boldsymbol{\mu}_j^\tau, \boldsymbol{\Sigma}_j^\tau)$ 
  - \*  $\alpha$ : learning rate.  $\alpha = 0 \implies$  no learning,  $\rho = 0$
  - \*  $\boldsymbol{\mu}_j^{\tau+1} = \boldsymbol{\mu}_j^\tau; \boldsymbol{\Sigma}_j^{\tau+1} = \boldsymbol{\Sigma}_j^\tau$
- Prior weights of *all* Gaussians adjusted:
  - $\pi_j^{\tau+1} = (1 - \alpha) \pi_j^\tau + \alpha \delta_{j, \text{top match}}^{\tau+1}$ 
    - \*  $\delta_{j, \text{top match}}^{\tau+1} = 1$ : matching Gaussian, 0 otherwise
  - Renormalise all weights  $\pi_j^{\tau+1}$  (only if  $> 1$  best. Grey levels: 2 best equidistant on each side)
    - \*  $\alpha = 0 \implies \pi_j^{\tau+1} = \pi_j^\tau$ : no learning
    - \*  $\alpha = 1 \implies \pi_j^{\tau+1} = 1$ : matching Gauss'n, 0 otherwise
- If  $\mathbf{x}^{\tau+1}$  doesn't match any  $\sim 2.5\sigma \implies$  something new coming up at this pixel, needs to be put in
  - Least prob ( $\sim \pi/\sigma$ ) replaced with a new one
  - New one:  $\boldsymbol{\mu}_j^{\tau+1} = \mathbf{x}^{\tau+1}$ ,  $\boldsymbol{\Sigma}_j = \text{high}$ ,  $\pi_j = \text{low}$