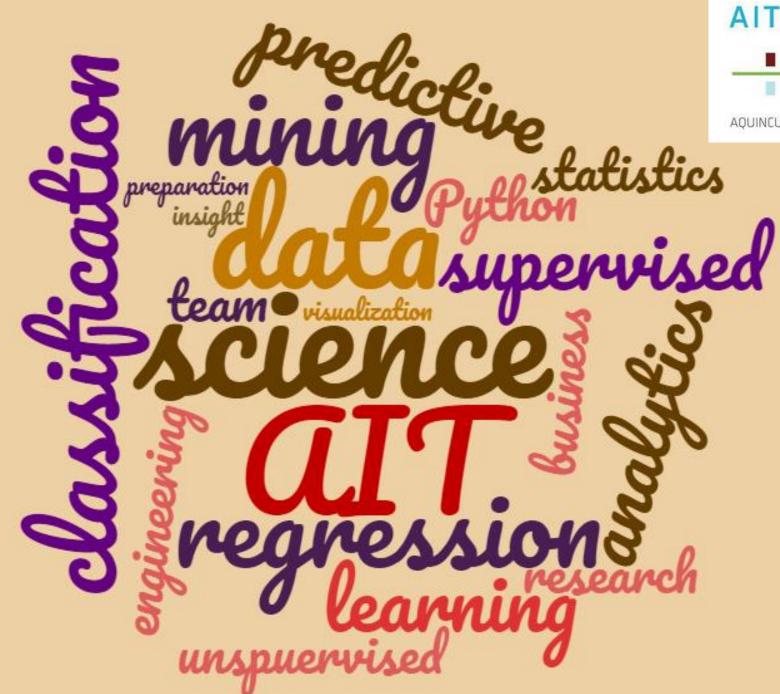
Data Science

April 28, 2028 Ensemble methods



AIT-BUDAPEST

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AQUINCUM INSTITUTE OF TECHNOLOGY

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### Schedule of the semester

	Monday midnight	Tuesday class	Friday class
W1 (02/06)			
W2 (02/13)		HW1 out	
W3 (02/20)			
W4 (02/27)	<b>HW1 deadline + TEAMS</b>	HW2 out	
W5 (03/06)			PROJECT PLAN
W6 (03/13)	HW2 deadline	HW3 out	
W7 (03/20)			MIDTERM
<b>SPRING BREAK</b>		SPRING BREAK	SPRING BREAK
W8 (04/03)	HW3 deadline		GOOD FRIDAY
W9 (04/10)	MILESTONE 1		
W10 (04/17)		HW4 out	
W11 (04/24)			
W12 (05/01)	HW4 deadline		
W13 (05/08)	MILESTONE 2		
W14 (05/15)		FINAL	-PROJECT presentations
W15 (05/22)		PROJECT presentations	

#### Milestone 2

- Three-page long report including:
  - Reviewing the related works
  - Data understanding and data preparation steps
  - Data analysis steps, implementing some models and evaluating them



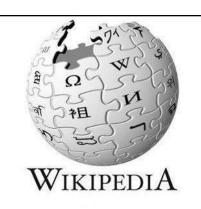
# Galton and the weight of an ox

- The story of Sir Francis Galton (1906)
  - English statistician, polymath
  - He visited a country fair where 800 people participated in a contest to estimate the weight of an ox
  - To his surprise, the median guess, 1207 pounds was accurate within 1% of the true weight of 1198 pounds
    - None of the experts were as accurate as the crowd itself
  - Several similar experiments have been conducted with similar results

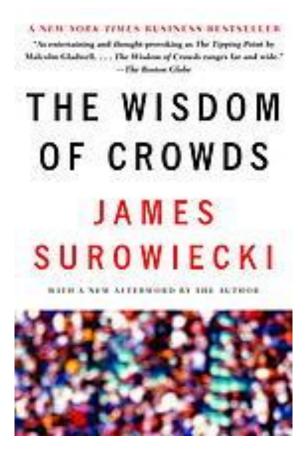


#### The wisdom of crowds

- Criteria required to form a wise crowd (collective intelligence)
  - Diversity of opinion
  - Independence
  - Decentralization, specialization
  - Appropriate aggregation







## Ensemble methods in machine learning

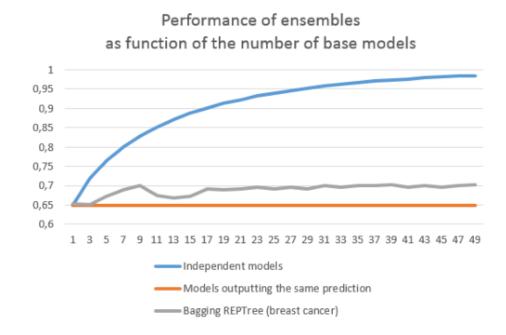
- Main idea: we combine multiple (simple) learning algorithms to have better performance
- Why is it good?
  - We have a binary classification task
  - We have 100 classification models
  - Assume that all of them misclassify a record with probability 0.4 (independently from each other)
  - The probability that more than half of the classifiers misclassify a single record is:

$$\sum_{k=50}^{100} {100 \choose k} \cdot 0.4^k \cdot 0.6^{100-k} \approx 0.027$$

• Using majority voting we assign the right class with probability 0.973 (or 97.3%)

#### Performance of ensembles

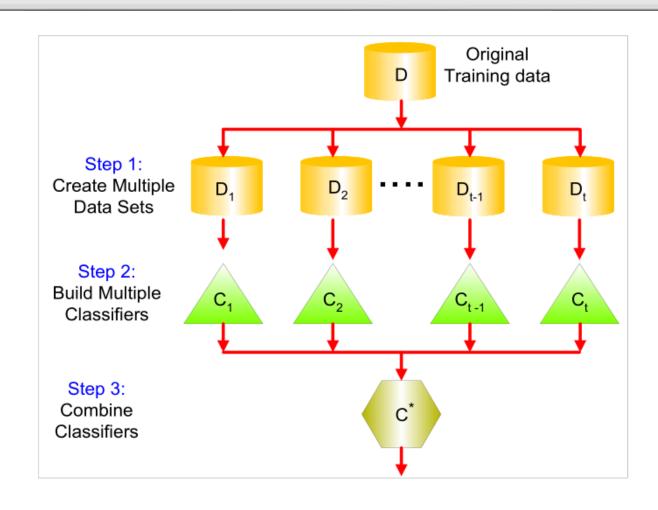
- In practice the increase in performance is not that sharp
  - In reality the models are not independent from each other
- But combining multiple classification algorithms usually results in better predictive performance than could be obtained from any of the composing learning algorithms alone
- It helps to reduce variance
- It helps to avoid overfitting



## Motivations for ensemble learning

- Statistical motivation
  - Using ensemble methods, the algorithm can average the different hypotheses and reduce the risk of choosing the wrong classifier
- Computational motivation:
  - Individual classifiers may be stuck in local optima, an ensemble algorithm may provide a better result
- Representational motivation:
  - Ensemble methods can expand the space of hypotheses searched by the individual learning algorithms

## Main idea of ensemble learning



## Multiple classifiers on a training set

- If the training set is very large: we partition the dataset into disjoint subsets, and we train an individual classifier on each subset
  - Usually the training set is not large enough to do that
- Bagging: random sampling with replacement
  - We create the samples independently from each other
  - The selection of all record is with equal probability
- Boosting: creating the sample in a sequential way, taking into account the previous classifier's success
  - After each training step the selection probabilities (weights) are redistributed
  - Misclassified data increases its weights to emphasize the most difficult cases

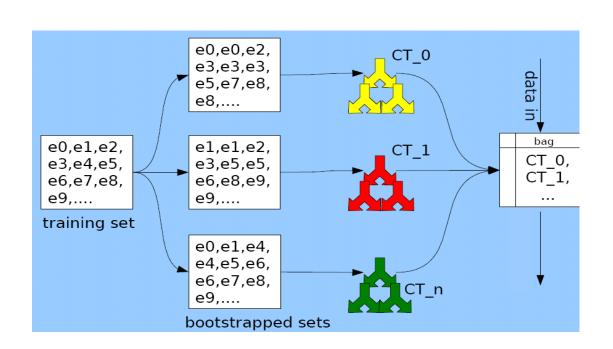
## Bagging

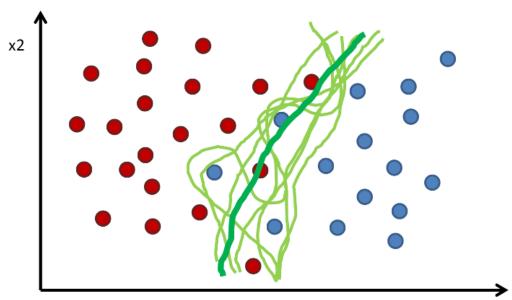
- Bagging (Bootstrap Aggregating)
- We train the individual models on random samples sampled with replacement

Original Data	1	2	3	4	5	6	7	8	9	10
Bagging (Round 1)	7	8	10	8	2	5	10	10	5	9
Bagging (Round 2)	1	4	9	1	2	3	2	7	3	2
Bagging (Round 3)	1	8	5	10	5	5	9	6	3	7

- The probability of selecting a record:  $1 \left(1 \frac{1}{n}\right)^n \to 1 \frac{1}{e} \approx 0.632$
- The final result is aggregated using majority voting or averaging (for regression)

## Bagging - examples





### Bagging for attributes

- Attribute bagging (random subspace method)
- Here the difference between the models is not due to sampling the training set but sampling the feature set
- We create (not necessarily disjoint) random samples of the features and train individual models using the sampled feature set

# Using meta-models (stacking)

- The results of the individual (base-level) models are combined using a meta-classifier or meta-regressor
  - More sophisticated than just using majority voting or averaging
- The training set is partitioned into two disjoint sets:  $S_1$  and  $S_2$ 
  - On  $S_1$  the base classifiers are trained
  - The records of set  $S_2$  are classified using the base models, the meta-model is trained on the outputs of the base level models as features

### Boosting

- Boosting: creating the sample in a sequential way, taking into account the previous classifier's success
  - After each training step the selection probabilities (weights) are redistributed
  - Misclassified data increases its weights to emphasize the most difficult cases
    - In the example record 4 seems to be a difficult one

Original Data	1	2	3	4	5	6	7	8	9	10
Boosting (Round 1)	7	3	2	8	7	9	4	10	6	3
<b>Boosting (Round 2)</b>	5	4	9	4	2	5	1	7	4	2
Boosting (Round 3)	(4)	(4)	8	10	4	5	(4)	6	3	(4)

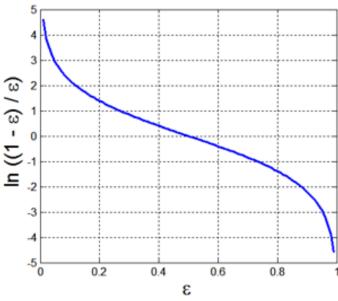
#### AdaBoost

- Adaptive boosting algorithms
- Base classifiers:  $C_1$ ,  $C_2$ , ...,  $C_T$
- In step j classifier  $C_j$  is trained, and in step j the record i has weight  $w_i^{(j)}$
- The error rate of classifier  $C_i$ :

$$\varepsilon_{j} = \frac{1}{N} \sum_{i=1}^{N} w_{i} \delta(C_{j}(x_{i}) \neq y_{i})$$

• The importance of classifier  $C_i$ :

$$\alpha_{j} = \frac{1}{2} \ln \left( \frac{1 - \varepsilon_{j}}{\varepsilon_{j}} \right)$$



#### AdaBoost II.

Updating the weights

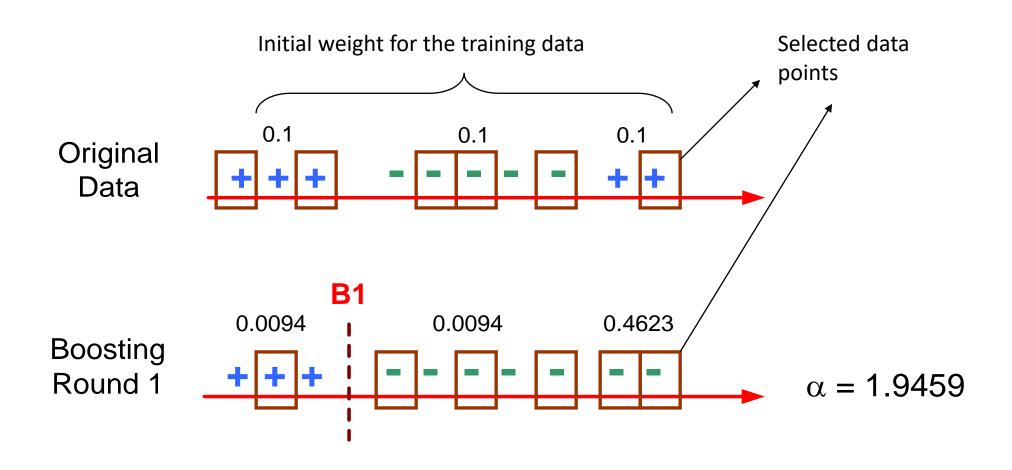
$$w_i^{(j+1)} = \frac{w_i^{(j)}}{Z_j} \begin{cases} e^{-\alpha_j} & \text{if } C_j(x_i) = y_i \\ e^{\alpha_j} & \text{if } C_j(x_i) \neq y_i \end{cases}$$

where  $Z_j$  is the normalizing factor to ensure that the sum of the weights is equal to 1

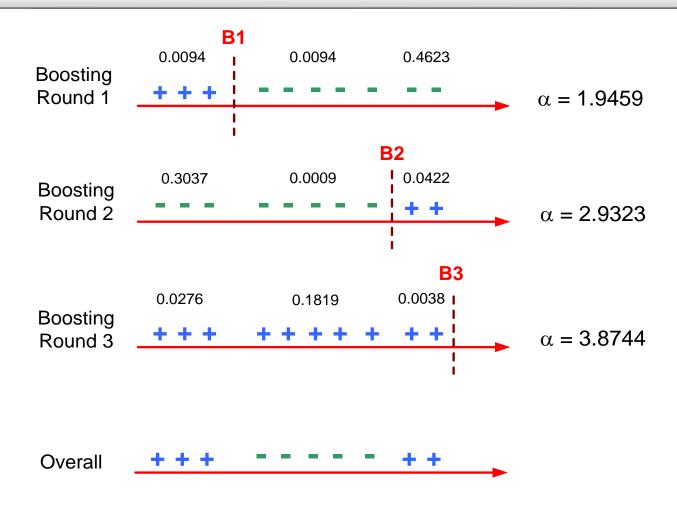
Classification

$$C*(x) = \underset{y}{\operatorname{arg max}} \sum_{j=1}^{T} \alpha_{j} \delta(C_{j}(x) = y)$$

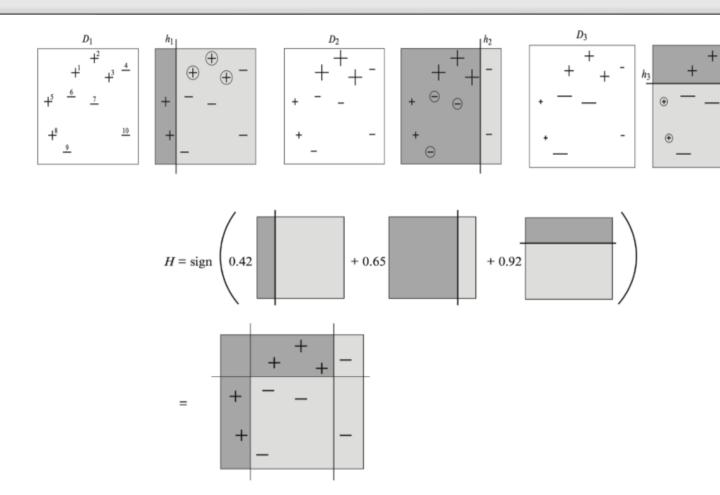
## AdaBoost - example



## AdaBoost – example II.

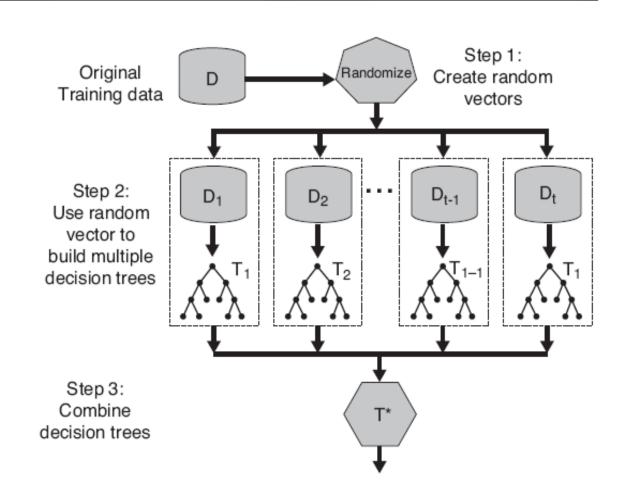


## AdaBoost – another example



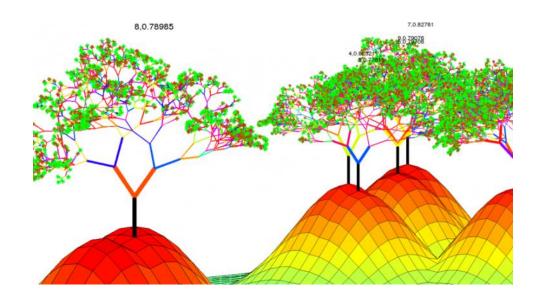
#### Random forest

- We build multiple decision trees in such a way that
  - We create random samples from the training set using bagging method
  - We use attribute bagging for the features for training the individual trees
    - the feature set for an individual tree is much smaller than the original feature set



#### Random forest II.

- The base classifiers are decision trees
  - Trained on random samples (bagging)
  - For an individual tree we restrict the feature space for a much smaller number of features
  - The individual trees grow according to a decision tree algorithm
- The random forest uses majority voting on the results of the individual trees

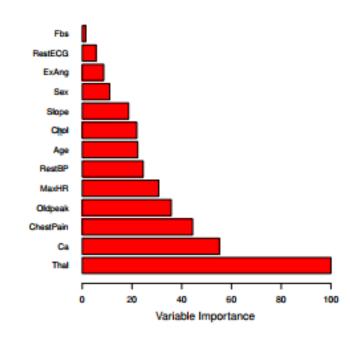


## Efficiency of random forest

- Usually we generate a high number of decision trees
- The efficiency of RF model depends on the followings:
  - Number of generated trees (the more trees, the better result)
  - The correlation between the trees (the higher correlation, the worse result)
  - BUT: The more tree we have, the higher the correlation is
  - The more attributes we let the decision trees to split on, the higher the correlation between the trees is
  - We can optimize for these parameters:
    - number of trees
    - used number of features for each tree

#### Evaluation of random forest

- The interpretability of the model is worse than for a simple decision tree
- Fast, easy to parallelize
- It can be used to measure the feature importance
  - How many times the decision trees use a certain attribute to split on
- Reduce overfitting
- Can handle high dimension
- Small number of parameters (number of trees, cardinality of the reduced feature space)

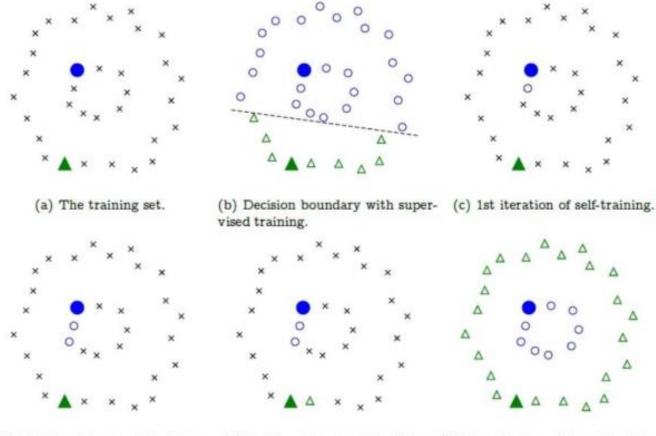


## Semi-supervised learning

- We use this method if the training set is small or non-representative
- Procedure
  - We classify the object whose label we are the most confident in
  - We add the previously classified object (with the predicted label) to the training set
  - We retrain the model, and repeat the procedure on the unlabeled data points
- Computationally expensive
- The algorithm is able to take into consideration the structure of the unlabeled data points

# Example – semi supervised learning

- kNN classifier
  - Two classes
  - The filled objects mark the records with known labels



(d) 2nd iteration of self-training.

(e) 3rd iteration of self-training. (f) Classification with self-training.

# Classifying imbalanced data

- Goal: balancing the class distribution
- Methods:
  - Under-sampling, sub-sampling:
     we reduce the size of the frequent class by
     eliminating the objects that are easy to
     classify (that are far away from the decision
     boundary)

The Problem:

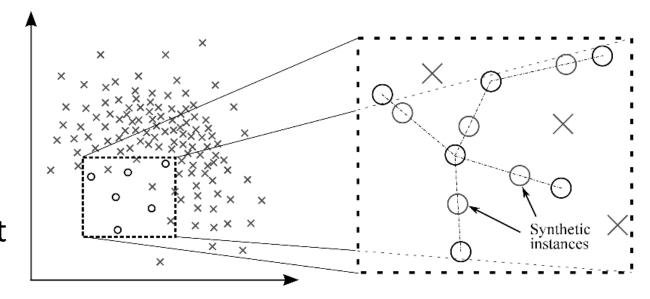
Oversample:

Subsample:

- Disadvantage: we lose data
- Over-sampling: synthetically supplementing the training data of the minority class
  - We won't have more information on the minority class, still it can help to improve the performance of classifiers

#### **SMOTE**

- SMOTE (Synthetic Minority Over-sampling Technique)
- The most common oversampling procedure
- For all instances from the minority class we consider their k nearest neighbors from the minority class.
- To create a synthetic data point by taking a random point on the segment between the neighbor and current data point



## Acknowledgement

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