

Mathematics

Quarter 1 – Module 1: Generating Patterns



Mathematics – Grade 10
Alternative Delivery Mode
Quarter 1 – Module 1: Generates Patterns
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Mathematics

Quarter 1 – Module 1:

Generating Patterns

Introductory Message

This Self-Learning Module (SLM) is prepared so that you, our dear learners, can continue your studies and learn while at home. Activities, questions, directions, exercises, and discussions are carefully stated for you to understand each lesson.

Each SLM is composed of different parts. Each part shall guide you step-by-step as you discover and understand the lesson prepared for you.

Pre-tests are provided to measure your prior knowledge on lessons in each SLM. This will tell you if you need to proceed on completing this module or if you need to ask your facilitator or your teacher's assistance for better understanding of the lesson. At the end of each module, you need to answer the post-test to self-check your learning. Answer keys are provided for each activity and test. We trust that you will be honest in using these.

In addition to the material in the main text, Notes to the Teacher are also provided to our facilitators and parents for strategies and reminders on how they can best help you on your home-based learning.

Please use this module with care. Do not put unnecessary marks on any part of this SLM. Use a separate sheet of paper in answering the exercises and tests. And read the instructions carefully before performing each task.

If you have any questions in using this SLM or any difficulty in answering the tasks in this module, do not hesitate to consult your teacher or facilitator.

Thank you.



What I Need To Know

This module was designed and written with you in mind. It is here to indulge you in discovering and generating patterns. The scope of this module permits it to be used in many different learning situations. Recognizing and extending patterns are important skills needed to the learning of concepts related to sequences. The arrangement of the lessons follows the standard sequence of the course. But the pacing in which you read and answer this module is dependent on your ability.

Primarily, the scope of this module is to develop your skill in generating patterns. While going through this module, you are expected to:

1. generate pattern from a given succession of objects, numbers, letters, or symbols;
2. find the n th term of a sequence; and
3. write the rule for the n th term of a sequence.



What I Know

Let us determine how much you already know about generating patterns. If you answer all the test items correctly in this pretest, then you may skip studying this learning material and proceed to the next learning module.

DIRECTION: Read and understand each item, then choose the letter of your answer and write it on your answer sheet.

1. Which of the following does not show a sequence?
A) K to 12 Curriculum C) Body temperature
B) Months of a year D) Counting numbers
2. Which of the following is a finite sequence?
A) negative even numbers C) even numbers greater than 1
B) even numbers below 100 D) even numbers between 10 and 50
3. What is the 9th term in the sequence $-1, 4, -9, 16, -25, \dots$?
A) 64 B) -81 C) -64 D) 81
4. Find the first four terms of the sequence $a_n = 5n - 1$.
A) 5, 10, 15, 20 C) 4, 9, 14, 19
B) 6, 11, 16, 21 D) 5, 9, 13, 17

5. What is the 20th term of the sequence $a_n = \frac{(-1)^n}{n^2}$?
- A) $\frac{1}{400}$ B) $-\frac{1}{400}$ C) $\frac{20}{400}$ D) $-\frac{20}{400}$

6. What rule will correctly describe the sequence: 2, 5, 10, 17, 26, 37, ...?
- A) $n + 1$ B) $2n$ C) $2n + 1$ D) $n^2 + 1$

7. Find the n^{th} term of the sequence $-\frac{1}{2}, \frac{1}{4}, -\frac{1}{6}, \frac{1}{8}, -\frac{1}{10}, \dots$
- A) $a_n = \frac{(-1)^n}{2n}$ C) $a_n = \frac{-1}{2n}$
 B) $a_n = \frac{(-1)^n}{2}$ D) $a_n = -\frac{1}{2n}$

8. What are the next four terms of the sequence 2, 3, 5, 8,?
- A) 12, 17, 23, 30 C) 13, 21, 34, 55
 B) 12, 20, 33, 54 D) 13, 18, 23, 28

9. Consider the figures below, what is the n^{th} term of the sequence?

A) $\frac{n+1}{n}$ B) $\frac{n(n+1)}{2}$ C) $\frac{2n}{n+1}$ D) $\frac{n^2+1}{2}$

10. Which numerical pattern follows the rule “the next term is obtained by alternately subtracting 2 and multiplying by 3”, when starting with 5?

A) 5, 7, 21, 69 C) 5, 9, 14, 36
 B) 5, 3, 6, 4, 12 D) 5, 3, 9, 7, 21

11. Which is the next ordered pair in the pattern (1, 6), (3, 18), (5, 30)?

A) (7, 49) B) (7, 42) C) (8, 56) D) (8, 64)

12. In the sequence, $a_n = \frac{(-1)^{n+1}(n-1)(n+2)}{n}$, what is a_5 ?
- A) $\frac{28}{5}$ B) $-\frac{24}{5}$ C) $\frac{30}{5}$ D) $-\frac{26}{5}$

13. If x represents the number of terms, what is the rule for this pattern?

1st term: 32, 2nd term: 36, 3rd term: 40

A) $4x$ B) $x + 4$ C) $4x + 28$ D) $4x + 32$

14. Which of the following patterns shows infinite sequence?

A) 6, 12, 18, 24, 30 C) First 20 whole numbers
 B) English Alphabets D) 100, 50, 25, 12.5, ...

15. Madison has the number pattern {5, 3, 8, 6, 11} for a homework problem. She says that the number pattern is alternately adding 5 and subtracting 2. Did Madison correctly describe the pattern?

- A) No, the pattern is alternately adding 5 and subtracting 2.
- B) No, the pattern is alternately subtracting 2 and adding 5.
- C) No, the pattern is alternately subtracting 3 and adding 4.
- D) Yes, Madison's description of the pattern is correct.

Lesson

Generating Patterns



What's In

When you were in grade 8, you learned about concepts related to generating patterns like Inductive Reasoning. The knowledge and skills you acquired are very important for you to understand how to generate patterns and sequences. Hence, let us review inductive reasoning and perform the activities that follow.

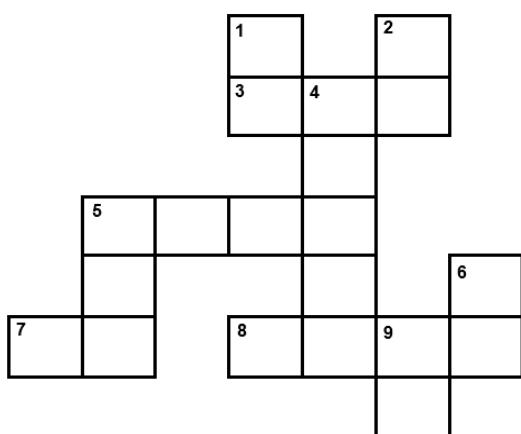
review

Inductive Reasoning is the process of observing data, recognizing patterns, and making generalizations (conjecture) from observations. A **conjecture** is a conclusion made from observing data or an educated guess based on patterns.

Activity 1. Complete Me!

Direction: Make a conjecture about each pattern. Then use your conjecture to draw or write the next term in the pattern.

- A) Complete the puzzle below by providing the needed term/s in each pattern.



ACROSS

- 3) 1, 8, 27, 64, 125, ____
- 5) 4, 20, 100, 500, ____
- 7) 1, 1, 2, 3, 5, 8, ____
- 8) J, F, M, A, M, J, J, A, ___, ___, ___, ____

DOWN

- 1) 2, 4, 6, 8 10, ____
- 2) 128, 64, 32, ____
- 4) 1, 10, 100, 1000, ____
- 5) 3, 9, 27, 81, ____
- 6) 1A, 2B, 3C, ____
- 9) O, T, T, F, F, S, S, E, ___, ____

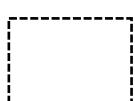
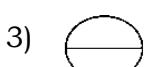
B) Draw the next object in each picture pattern.



4)



5)



6)



What's New

At this point of the module, you are about to learn the Introduction to Sequences and Patterns. To understand better how to generate patterns, you will have to perform the simple activity below.

Activity 2. Let's Discover!

Direction: Read, understand, and perform the given instructions below then answer the questions asked.

Materials: string, pair of scissors

- 1) Prepare five (5) strings with equal lengths.
- 2) Cut the first string once. (a) How many pieces are there? _____
Cut the second string twice. (b) How many pieces are there? _____
Cut the third string thrice. (c) How many pieces are there? _____
Cut the fourth string four times. (d) How many pieces are there? _____
Cut the fifth string five times. (e) How many pieces are there? _____
- 3) Based from your answers, complete the table below.

Number of cuts (x)	1	2	3	4	5
Number of pieces (y)					

- 4) Without cutting a string 6 times, how many pieces are there? _____
- 5) Have you seen a pattern? If yes, describe the pattern and state your conjecture. Use a formula or equation in your conjecture, where y is the number of pieces and x is the number of cuts.
- 6) Using your conjecture, how many pieces of strings can be made from (a) 12 cuts? (b) 24 cuts? (c) 35 cuts? and (d) 42 cuts? Show your solutions.

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Were you able to complete the task? If yes, you may proceed to the next page. If no, take time to finish for you to better understand the next discussions.



What Is It

How did you find activity 2? Have you given idea on how to generate a pattern? Let us process your answers.

- Based from the task, the complete solution is shown in the table below:

Number of cuts (x)	1	2	3	4	5	6
Number of pieces (y)	2	3	4	5	6	7

- From the table, notice that the number of pieces (y) of strings is one more than the number of cuts (x). Thus, we can state our conjecture as, “The number of pieces (y) when a string is cut x times can be computed using the formula $y = x + 1$.”
- Using the formula $y = x + 1$, we can now solve the number of pieces of strings that can be made from 12 cuts? 24 cuts? 35 cuts? and 42 cuts?
 - 12 cuts, $x = 12$ $y = 12 + 1 = \mathbf{13}$
 - 24 cuts, $x = 24$ $y = 24 + 1 = \mathbf{25}$
 - 35 cuts, $x = 35$ $y = 35 + 1 = \mathbf{36}$
 - 42 cuts, $x = 42$ $y = 42 + 1 = \mathbf{43}$

Were you able to get the same answers? If yes, very good! If no, I hope you were able to understand the discussions above. Based from the given activity, the number of pieces, $y = x + 1$, when a string is cut x times represents a sequence. Thus, the values of y which are 2, 3, 4, 5, 6, 7, ... is an example of a sequence.

The word **sequence** means an order in which one thing follows another in succession. A sequence is an ordered list. For another example, if we write $x, 2x^2, 3x^3, 4x^4, 5x^5, ?$, what would the next term in the sequence be - the one where the question mark now stands? The answer is $6x^6$.

definition

A **sequence** is a set of objects which is listed in a specific order, one after another. Each member or element in the sequence is called **term**. The terms in a sequence can be written as $a_1, a_2, a_3, a_4, \dots, a_n, \dots$ which means a_1 is the first term, a_2 is the second term, a_3 is the third term, ..., a_n is the n^{th} term, and so on.

Sequences are classified as finite and infinite. A **finite** sequence contains a limited number of terms. This means it has an end or last term. Consider the examples below.

- a) Days of the week: {Sunday, Monday, Tuesday, ..., Saturday}
- b) First 10 positive perfect squares: {1, 4, 9, 16, 25, 36, 49, 64, 81, 100 }

On the other hand, an **infinite** sequence contains a countless number of terms. The number of terms of the sequence continues without stopping or it has no end term. The ellipsis (...) at the end of the following examples shows that the sequences are infinite. Consider the examples below.

- a) Counting numbers: {1, 2, 3, 4, 5, ...}
- b) Multiples of 5: {5, 10, 15, 20, 25, ...}

Sometimes a pattern in the sequence can be obtained and the sequence can be written using a **general term**. In the previous example $x, 2x^2, 3x^3, 4x^4, 5x^5, 6x^6, \dots$, each term has the same exponent and coefficient. We can write this sequence as $a_n = nx^n$ where $n = 1, 2, 3, 4, 5, 6, \dots$, and a_n is called the **general** or ***n*th term**.

A. Finding several terms of a sequence, given the general term:

Example 1.

Find the first four terms of the sequence $a_n = 2n - 1$.

Solution: To find the first term, let $n = 1$

$$a_n = 2n - 1 \quad \text{use the given general term}$$

$$a_1 = 2(1) - 1 \quad \text{substitute } n \text{ by 1}$$

$$a_1 = 2 - 1 \quad \text{perform the operations}$$

$$a_1 = 1 \quad \text{simplify}$$

Repeat the same process for the second to the fourth terms.

$$\text{Find the second term, } n = 2 \qquad a_2 = 2(2) - 1 = 4 - 1 = 3$$

$$\text{Find the third term, } n = 3 \qquad a_3 = 2(3) - 1 = 6 - 1 = 5$$

$$\text{Find the fourth term, } n = 4 \qquad a_4 = 2(4) - 1 = 8 - 1 = 7$$

Therefore, the first four terms of the sequence are **1, 3, 5, 7**.

Example 2.

Find the 5th to the 8th terms of the sequence $b_n = \frac{(-1)^n}{n+1}$.

Solution: To find the 5th term, let $n = 5$

$$b_n = \frac{(-1)^n}{n+1} \quad \text{use the given general term}$$

$$b_5 = \frac{(-1)^5}{5+1} \quad \text{substitute } n \text{ by 5}$$

$$b_5 = \frac{-1}{6} = -\frac{1}{6} \quad \text{simplify } (-1 \text{ raised to an odd number power is always negative})$$

Repeat the same process for the 6th to the 8th terms.

$$\text{Find the 6th term, } n = 6 \quad b_6 = \frac{(-1)^6}{6+1} = \frac{1}{7}$$

$$\text{Find the 7th term, } n = 7 \quad b_7 = \frac{(-1)^7}{7+1} = \frac{-1}{8} = -\frac{1}{8}$$

$$\text{Find the 8th term, } n = 8 \quad b_8 = \frac{(-1)^8}{8+1} = \frac{1}{9}$$

Therefore, the 5th to the 8th terms of the sequence are $-\frac{1}{6}, \frac{1}{7}, -\frac{1}{8}, \frac{1}{9}$.

B. Finding the general term, given several terms of the sequence:

Example 3.

Write the general term of the sequence 5, 12, 19, 26, 33, ...

Solution: Notice that each term is 7 more than the previous term. We can search the pattern using a tabular form.

Term	Given	Pattern
1	5	5
2	12	$5 + 7$
3	19	$5 + 7 + 7$
4	26	$5 + 7 + 7 + 7$
5	33	$5 + 7 + 7 + 7 + 7$
n	a_n	$5 + 7 + 7 + 7 + 7 + \dots + 7$
		$5 + 7(n - 1)$

In the pattern, the number of times that 7 is added to 5 is one less than the n^{th} term ($n - 1$). Thus,

$$a_n = 5 + 7(n - 1) \quad \text{equate } a_n \text{ and } 5 + 7(n - 1)$$

$$a_n = 5 + 7n - 7 \quad \text{apply distributive property of multiplication}$$

$$a_n = 7n - 2 \quad \text{combine similar terms}$$

Therefore, the n^{th} term of the sequence is $a_n = 7n - 2$, where $n = 1, 2, 3, 4, 5, \dots$

Example 4.

Write the general term of the sequence 2, 4, 8, 16, 32, ...

Solution: Notice that each term is 2 times the previous term. We can search the pattern using a tabular form.

Term	Given	Pattern	
1	2	2	2^1
2	4	$2(2)$	2^2
3	8	$2(2)(2)$	2^3
4	16	$2(2)(2)(2)$	2^4
5	32	$2(2)(2)(2)(2)$	2^5
n	a_n	$2(2)(2)(2)(2)\dots(2)$	2^n

Therefore, the n^{th} term of the sequence is $a_n = 2^n$, where $n = 1, 2, 3, 4, 5, \dots$

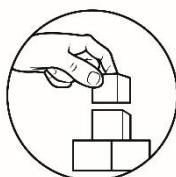
Example 5.

Find the general term of the sequence $1, \frac{1}{4}, \frac{1}{9}, \frac{1}{16}, \frac{1}{25}, \dots$

Solution: $\frac{1}{1}, \frac{1}{4}, \frac{1}{9}, \frac{1}{16}, \frac{1}{25}, \dots$ write 1 as $\frac{1}{1}$

$\frac{1}{1^2}, \frac{1}{2^2}, \frac{1}{3^2}, \frac{1}{4^2}, \frac{1}{5^2}, \dots, \frac{1}{n^2}$ notice each denominator is an integer squared

Therefore, the n^{th} term of the sequence is $a_n = \frac{1}{n^2}$, where $n = 1, 2, 3, 4, 5, \dots$

**What's More**

Now, it's your turn to apply the concepts on sequences and patterns to find the specified terms of a sequence when given its general term and vice versa.

Activity 3. Your Turn!

Direction: Answer what is asked in each set of exercises on a separate sheet of paper

- In Exercises 1 – 4, write the first four terms of each sequence. Assume n starts at 1.

1) $a_n = n$

2) $a_n = \frac{n}{n+1}$

3) $a_n = (-1)^{n+1} n^2$

4) $a_n = \frac{n(n+1)}{2}$

- In Exercises 5 – 8, find the indicated term of each sequence given.

5) $a_n = \left(\frac{1}{2}\right)^n$ $a_9 = ?$

6) $a_n = \frac{(n+1)^2}{n-9}$ $a_{14} = ?$

7) $a_n = \frac{(-1)^{n+1}(n-1)(n+2)}{n}$ $a_7 = ?$

8) $a_n = \left(\frac{n}{9} - 12\right)^n$ $a_{99} = ?$

- In Exercises 9 – 12, write an expression for the n^{th} term of the given sequence. Assume n starts at 1.

9) 2, 4, 6, 8, 10, ...

10) 1, -1, 1, -1, 1, ...

11) 3, 9, 27, 81, ...

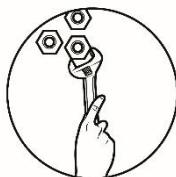
12) $\frac{1}{2 \cdot 1}, \frac{1}{3 \cdot 2}, \frac{1}{4 \cdot 3}, \frac{1}{5 \cdot 4}, \frac{1}{6 \cdot 5}, \dots$



What I Have Learned

Great! You have reached this part of the module. To ensure your full understanding on the concepts related to generating patterns, it's important that you are able to complete each statement below.

- 1) A sequence is _____.
- 2) A term is _____.
- 3) A finite sequence contains _____ while infinite sequence contains _____.
- 4) To find the specified term/s of a sequence when given the general term, _____.
- 5) To write the general term of a sequence when given some terms, _____.



What I Can Do

Generating patterns is a vital concept in performing any mathematical investigation. Similar to the previous activity on the number of pieces when a string is cut x times, a sequence is formed when a repeated process following a certain rule is employed. To perform a simple mathematical investigation, perform the task below.

Activity 4. Let's Investigate!

Direction: Given the figures below, perform a mathematical investigation by following the given steps.



Figure 1



Figure 2



Figure 3



Figure 4

Step 1. To investigate, you are going to make your own problem to solve. Based from the figures above, what do you think could be a probable problem to investigate?

Step 2. Identify your variables (dependent and independent variables). For example, number of pieces of strings, a_n , and number of cuts n . Then list your data.

Step 3. Present your data in a tabular form.

Term	Sequence	Pattern
1		
2		
3		
4		
n	a_n	

Step 4. State your conjecture using a general or n^{th} term.

Step 5. Test your conjecture. Using your derived formula or general term, find the first four terms of your sequence if it matches.

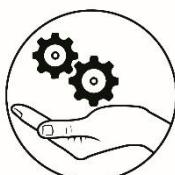


Assessment

Let us determine how much you have learned from this module. Read and understand each item, then choose the letter of your answer and write it on your answer sheet.

1. Which of the following shows a pattern?
A) 3, 2, 3, 2, 3, 2 C) A, G, M, T, O, 9
B) 5, 7, 2, T, 6, Y D) smooth, long, wall, sing
2. Which of the following defines infinite sequence?
A) days of the week C) every other day
B) teenage life D) first Fridays of July 2020
3. What are the next three terms of the sequence 1, 11, 22, 34, ...?
A) 46, 60, 75 B) 47, 61, 76 C) 42, 54, 66 D) 44, 60, 74
4. What is the 25th term of the sequence $a_n = \frac{(-1)^n}{n^2}$?
A) $\frac{1}{625}$ B) $-\frac{1}{625}$ C) $\frac{25}{625}$ D) $-\frac{25}{625}$
5. What is the 11th term in the sequence -1, 4, -9, 16, -25, ...?
A) 100 B) -100 C) 121 D) -121
6. Find the first four terms of the sequence $a_n = 3n + 2$.
A) 5, 7, 11, 14 B) 5, 8, 11, 15 C) 5, 8, 11, 14 D) 5, 9, 13, 17
7. Which numerical pattern follows the rule “the next term is obtained by alternately subtracting 3 and multiplying by 2”, when starting with 5?
A) 5, 10, 20, 40, 50 C) 5, 2, -1, -4, -7
B) 5, 2, 4, 1, 2 D) 5, 8, 16, 19, 38
8. What rule will correctly describe the sequence: 2, 6, 12, 20, 30, ...?
A) $n + 1$ B) $n^2 + 1$ C) $2n + 1$ D) $n^2 + n$
9. Find the n^{th} term of the sequence $\frac{1}{2}, -\frac{1}{4}, \frac{1}{6}, -\frac{1}{8}, \frac{1}{10}, \dots$
A) $a_n = \frac{-1}{2n}$ B) $a_n = \frac{(-1)^{(n+1)}}{2}$ C) $a_n = \frac{(-1)^{(n+1)}}{2n}$ D) $a_n = -\frac{1}{2n}$

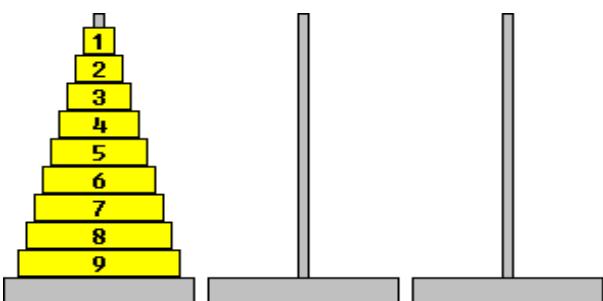
10. Which is the next ordered pair in the pattern $(2, 1)$, $(4, 4)$, $(6, 9)$?
- A) $(8, 12)$ B) $(7, 16)$ C) $(8, 16)$ D) $(7, 12)$
11. What is the 8th term in the sequence $9, 4, -1, -6, -11, \dots$?
- A) -21 B) -26 C) -31 D) -36
12. In the sequence, $a_n = \frac{(-1)^{n+1}(n-1)(n+2)}{n}$, what is a_{10} ?
- A) $\frac{108}{10}$ B) $-\frac{54}{5}$ C) $\frac{52}{5}$ D) $-\frac{104}{10}$
13. Which of the following patterns shows finite sequence?
- A) $6, 12, 18, 24, 30, \dots$ C) First 20 whole numbers
 B) multiples of 6 D) $100, 50, 25, 12.5, \dots$
14. Find the general term of the sequence $3, 9, 27, 81, \dots$
- A) $3n$ B) n^3 C) 3^n D) $n + 3$
15. Write the first four terms of the sequence $a_n = n^2 - 1$.
- A) $0, 3, 8, 15$ B) $1, 3, 5, 7$ C) $1, 5, 10, 16$ D) $0, 2, 7, 12$



Additional Activities

Awesome! Before we end this module, let me introduce a puzzle game called Tower of Hanoi. Are you familiar with this game? If not, allow me to introduce it to you.

In the **Tower of Hanoi** puzzle a player attempts to move a large pile of disks, known as the **Tower**, from the leftmost peg to the rightmost on the puzzle board. The rules of the puzzle state that the player can only move one disk per turn and can never place a larger disk onto a smaller one at any time.

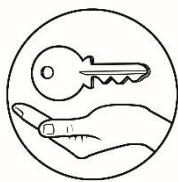


If you are interested to play the puzzle, you can search it on the internet. For the meantime, I just want to use the puzzle game for the purpose of applying sequences and generating patterns.

Situation: In playing the game, you can choose the number of disks of your tower and play with the least possible moves. The least number of moves when playing the puzzle with respect to the number of disks are as follows:

<i>Number of Disks</i>	Number of Moves	<i>Number of Disks</i>	Number of Moves
1	1	5	31
2	3	6	63
3	7	7	127
4	15	9	255

Task: Based on the above data, find the general term in finding the number of moves with respect to the number of disks in playing the tower of Hanoi.



Answer Key

The least possible number of moves, a_n , with respect to the number of disks (n) can be computed using the general term $a_n = 2^n - 1$.

Additional Activities

Assessment	(1) A	(4) B	(7) B	(10) C	(9) C	(12) B	(15) A
	(2) C	(5) D	(8) D	(11) B	(14) C	(13) C	
	(3) B	(6) C	(10) C	(11) B	(14) C	(12) B	
	(14) C	(13) C	(15) A	(12) B	(11) B	(10) C	

No. of Hexagons (n)	No. of Triangles (an)	Pattern	Conjecture:
1	6	6 + 4(0)	$6 + 4(n-1)$ or $4n + 2$
2	10	6 + 4(1)	
3	14	6 + 4 + 4	
4	18	6 + 4 + 4 + 4	
			$6 + 4 + 4 + \dots + 4$
			$a_n = 6n + 2$

What Can I Do (Activity 4)

1) a set of objects which is listed in a specific order.	2) each member or element in the sequence.	3) limited number of terms; countless number of terms
4) answer may vary	5) answer may vary	

What I Have Learned

1) 1, 2, 3, 4	4) 1, 3, 6, 10	7) $\frac{5}{4}$	10) $a_n = (-1)^{n+1}$	11) $a_n = 3^n$	5) $\frac{1}{512}$	6) 45	9) $a_n = 2^n$	12) $a_n = \frac{(n+1)\cdot n}{1}$	3) 1, -4, 9, -16

What's More (Activity 3)

1)	2)	3)	4)	5)	6)	7)	8)	9)	10)

What's In (Activity 1)

1) C	4) C	7) A	10) D	9) B	6) D	5) A	8) A	11) B	12) A	13) C	14) D	15) B

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