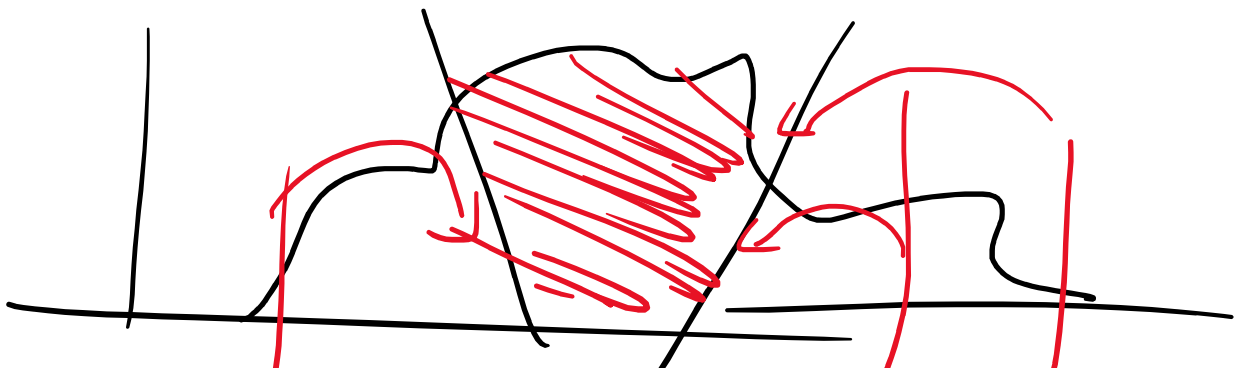


=> Measures of Dispersion



~~1 1 1 1 1 1 1~~

→ Standard Deviation, Variance

⇒ Standard Deviation

Deviation = Error

⇒ Population: Entire Data  $N$

⇒ Sample: Derived Sub-space  $n$

1400000000

1.4B

200M ~ 15M Min

250M ~ UP

180M ~ RJ

1400

200M ~ 15M Min

250 UP

180 RJ

⇒ Deviation  $\rightarrow \frac{N}{n} ( \dots )$

∴ Deviation

$$\rightarrow \sum_{i=1}^N (x_i - \bar{x})$$

$$(x_1 - \bar{x}) + (x_2 - \bar{x}) + (x_3 - \bar{x}) - \dots - (x_N - \bar{x})$$

$$\sqrt{\sum_{i=1}^N (x_i - \bar{x})^2} \sim \text{Deviation (Normalized)}$$

Population S.D

$$\sigma = \sqrt{\frac{\sum_{i=1}^N (x_i - \bar{x})^2}{N}}$$

Sample S.D

$$s = \sqrt{\frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}}$$

∴ Variance :

Pop Variance

$$\sigma^2 = \frac{\sum_{i=1}^N (x_i - \bar{x})^2}{N}$$

Sample Variance

$$s^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

⇒ Covariance

$$Cov(x, y) = \frac{\sum (x_i - \bar{x}) \cdot (y_i - \bar{y})}{N-1}$$

N - Population

n - Sample (N-1)

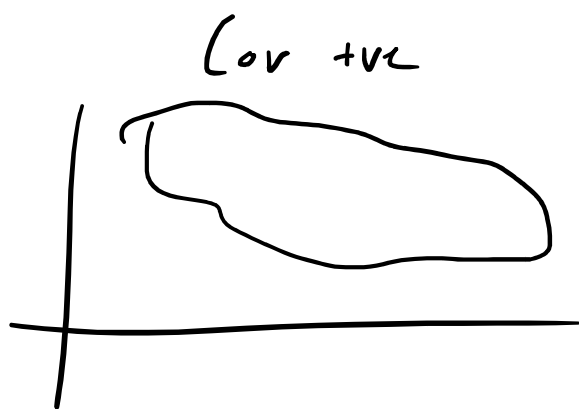
⇒  $x(2, 4, 6, 8, 10)$  &  $y(3, 7, 10, 14, 17)$

x	y	$x_i - \bar{x}$	$y_i - \bar{y}$	$(x_i - \bar{x}) \cdot (y_i - \bar{y})$
2	3	-4	-2.2	8.8
4	7	-2	-3.2	6.4
6	10	0	-0.2	0
8	14	2	3.8	7.6
10	17	4	6.8	27.2
<u>2</u>	<u>4</u>			<u>27.2</u>

$$\begin{array}{r} 10 \\ \hline \bar{x} \\ = 6 \end{array} \quad \begin{array}{r} 17 \\ \hline \bar{y} \\ = 10.2 \end{array} \quad \begin{array}{r} 4 \\ \hline \end{array} \quad \begin{array}{r} 6.8 \\ \hline \end{array} \quad \begin{array}{r} 27.2 \\ \hline \Sigma = \underline{\underline{70}} \end{array}$$

$$\text{Cov}(x, y) = \frac{\sum (x_i - \bar{x}) \cdot (y_i - \bar{y})}{N - 1}$$

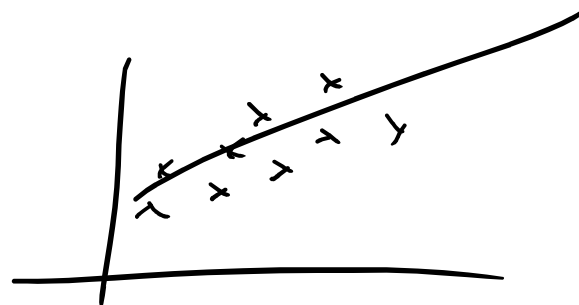
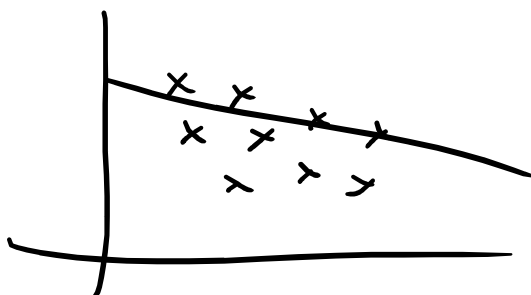
$$= \frac{70}{5-1} = \frac{70}{4} = \underline{\underline{17.5}}$$

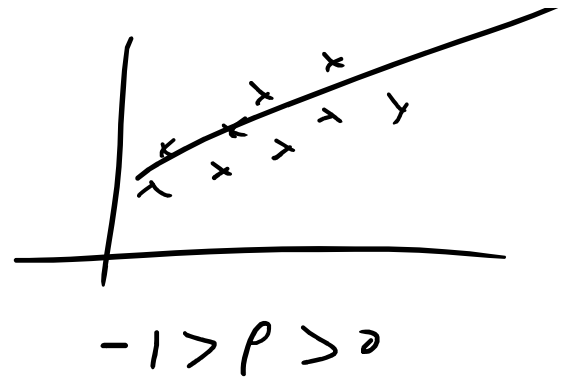
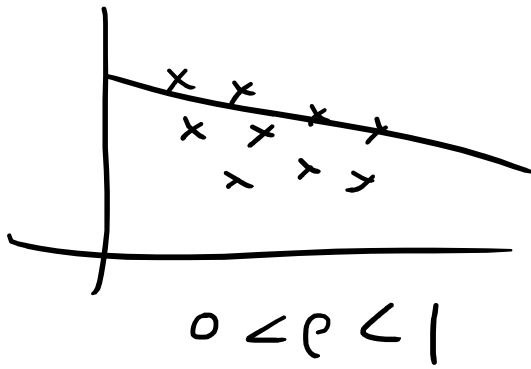


$\Rightarrow$  Karl Pearson's Correlation Coefficient

Pop =  $\rho$

Sample :  $r$





$\rho, \rho^2$

$$\rho = \frac{N \sum xy - \sum x \cdot \sum y}{\sqrt{[N \sum x^2 - (\sum x)^2] \cdot [N \sum y^2 - (\sum y)^2]}}$$

$$x = 1, 2, 3, 4, 5, 6$$

$$y = 2, 4, 7, 5, 12, 19$$

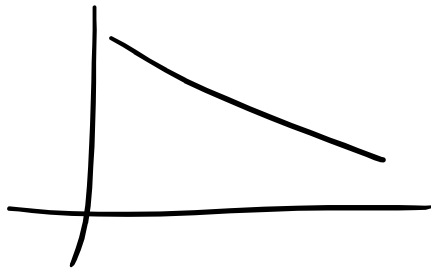
$x$	$y$	$xy$	$x^2$	$y^2$
21	48	211	91	450

$$\rho = \frac{6 \times 211 - 21 \times 48}{\sqrt{[6 \times (91) - (21)^2] \cdot [6 \times (450) - (48)^2]}}$$

$$\rho = \underline{\underline{0.998}} \approx \underline{\underline{99.8\%}}$$

1

Verdict: Data is . . .



Verdict: Data is  
positively correlated