

## Question: 1

*Solution:*

## Question: 3

Let  $f(1) = 3$  and  $f(n + 1) = 3^{f(n)}$ . Find the last two digits of  $f(2012)$ .

**Solution:** We claim that  $3^{20} \equiv 1 \pmod{100}$ , which is trivially shown by Fermat's or Euler's. As such, we take the exponent  $\pmod{20}$  to find the last two digits in this cyclic