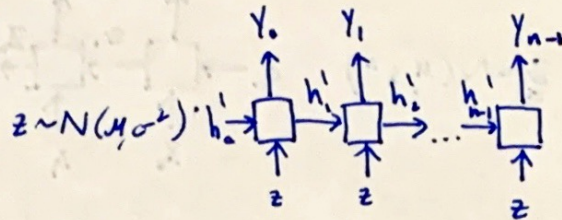
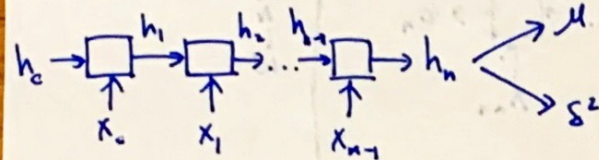


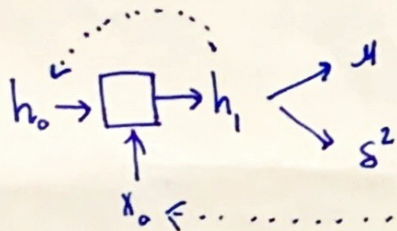
Variational RNN Architecture 1

ENCODER

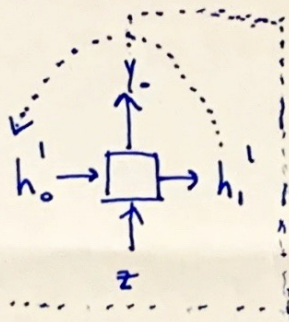


DECODER

TRAIN



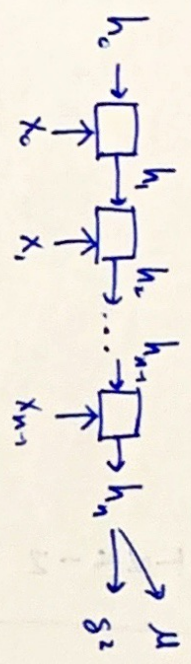
$$z \sim N(\mu, \sigma^2)$$



TEST

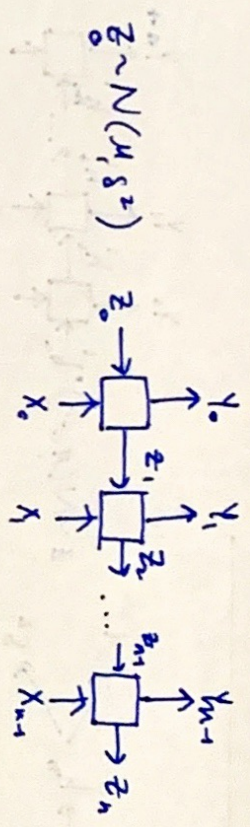
at next t , $h_0 = h_1$
 $h'_0 = h'_1$
 $x_0 = y_0$

Variational RNN Architecture 2

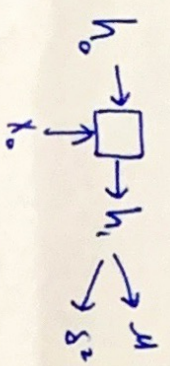


ENCODER

DECODER

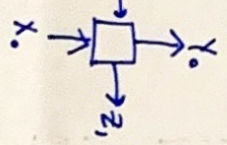


$T \in \mathbb{R}^{n \times 2}$



ENCODER

DECODER



at next timestep,

$$h_0 = h_1$$

$$z_0 = z_1$$

$$x_0 = y_0$$

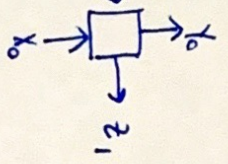
then, there is no need for the encoder after the 1st timestep.

we could modify the decoder

$$z'_0 = \text{random}$$

$$z_0 \sim N(\mu, \sigma^2)$$

$$f(z_0, z'_0) \rightarrow z_1$$

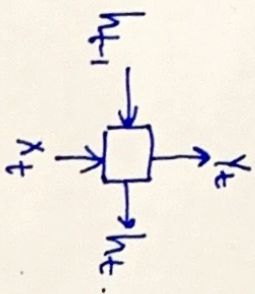


$$z'_0 = z_1$$

$$z_0 \sim N(\mu, \sigma^2) \text{ from encoder.}$$

TRUE VARIATIONAL RNN.

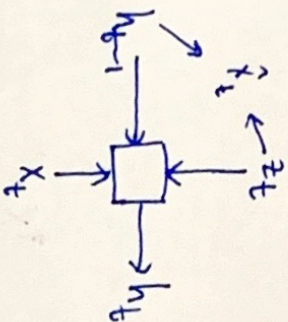
Let's look at a vanilla RNN.



$$h_t = f(x_t, h_{t-1}) \quad f \text{ is the transition function.}$$

$$y_t = g(h_t).$$

In a variational seq2seq Autoencoder, we would do this:



$$h_t = f(x_t, z_t, h_{t-1}).$$

encoder: $z_t | x_t$

$$x_t, h_{t-1} \xrightarrow{\mathcal{M}} s^z \quad z_t \sim \mathcal{N}(\mu, s^z)$$

decoder: $x_t | z_t$

$$z_t, h_{t-1} \xrightarrow{\mathcal{M}} s^x \quad \hat{x}_t \sim \mathcal{N}(\mu, s^x)$$

in the case of supervised learning,

$$\hat{x}_t = y_t$$