

# 8PUZZLE PROBLEM

Pietro Ciciari,  
Mario Choto,  
Israel Sanchez,  
Raj Kumar,  
Armon Lee,  
Venkat Sairam Ravala



# CONTENT

VARIOUS ALGORITHMS CAN SOLVE THIS PROBLEM:

The 8-puzzle problem involves arranging 8 tiles on a 3x3 grid so they are in numerical order.

- Breadth-First Search (BFS)
- Depth-First Search (DFS)
- A\* Search Algorithm
- Greedy Best-First Search
- Iterative Deepening Search

# FORMALIZING THE PROBLEM

THE 8-PUZZLE PROBLEM CAN BE DEFINED AS:

- Initial State: A starting configuration of the grid.
- Goal State: The target configuration (1 to 8, with empty space at the end).
- Actions: Move the empty space (up, down, left, right).
- Transition Model: Defines the result of a move.
- Action Cost: Uniform cost for each move (typically 1).



# ALGORITHMS OVERVIEW

WE EXPLORED THE FOLLOWING  
ALGORITHMS:

**1**

**BREADTH-FIRST SEARCH  
(BFS)**

**2**

**DEPTH-FIRST SEARCH(DFS)**

**3**

**A\* SEARCH ALGORITHM**

**4**

**GREEDY BEST-FIRST SEARCH**

**5**

**ITERATIVE DEEPENING  
SEARCH**

# BREADTH-FIRST SEARCH (BFS)



# DEPTH-FIRST SEARCH (DFS)

1

EXPLORES AS FAR AS  
POSSIBLE ALONG ONE  
BRANCH BEFORE  
BACKTRACKING.



2

MAY NOT FIND THE  
SHORTEST PATH.



3

LOWER MEMORY  
USAGE COMPARED  
TO BFS.



4

TIME COMPLEXITY:  
 $O(B^M)$

# A\* SEARCH ALGORITHM

1

USES HEURISTICS TO  
GUIDE THE SEARCH  
TOWARDS THE GOAL.



2

OFTEN FINDS THE  
OPTIMAL SOLUTION  
QUICKLY.



3

TIME COMPLEXITY:  
 $O(B^D)$  WITH  
HEURISTIC  
IMPROVEMENTS.



4

BEST BALANCE OF  
SPEED AND  
ACCURACY.

# GREEDY BEST-FIRST SEARCH

1

EXPANDS THE NODE  
CLOSEST TO THE GOAL  
USING A HEURISTIC.



2

FAST BUT MAY NOT  
FIND THE OPTIMAL  
PATH.



3

USES HEURISTICS  
LIKE MANHATTAN  
DISTANCE.



4

CAN GET STUCK IN  
LOCAL MINIMA.



# ITERATIVE DEEPENING SEARCH (IDS)

1

COMBINES  
DEPTH-FIRST AND  
BREADTH-FIRST  
SEARCH



2

MEMORY EFFICIENT  
AND GUARANTEES  
OPTIMAL SOLUTION.



3

REPEATS  
DEPTH-FIRST SEARCH  
WITH INCREASING  
DEPTH LIMITS.

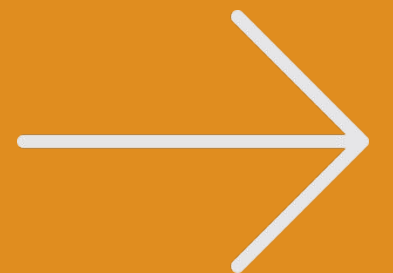


4

EFFICIENTLY  
BALANCES DEPTH  
EXPLORATION WITH  
SOLUTION  
OPTIMALITY.

# PERFORMANCE ANALYSIS

- A\* consistently outperforms other algorithms in terms of speed and path optimality.
- BFS is thorough but slow and memory-intensive.
- DFS is fast but not always reliable for finding the optimal path.
- Greedy Best-First is fast but may miss the optimal path.
- Iterative Deepening combines BFS and DFS benefits.



# CONCLUSION

- A\* Search Algorithm is the most effective method for solving the 8-puzzle problem.
- Its use of heuristics makes it a powerful and efficient choice.
- Future improvements could focus on refining heuristics for even better performance.