

Q2

Let us first formulate null hypothesis and alternative hypothesis.

$$H_0 : p = 0.03$$

$$H_1 : p \neq 0.03$$

a) $n = 50$

Our test statistic is $C = 0.6 * 50 = 3$

```
import scipy

p_value = scipy.stats.binomtest(3, 50, p=0.03).pvalue

print(p_value)
```

0.18920192463027882

At the 5% significance level, we fail to reject the hypothesis.

- b) Now let us repeat the proportion test for $n = 350$. For this larger sample size, we can use the asymptotic proportion test with the standardized test statistic

$$Z = (\hat{p} - p_0) / \sqrt{(p_0 * (1 - p_0)) / n}$$

Evaluating this results in:

```
import math

z = (0.06 - 0.03) / math.sqrt((0.03 * 0.97) / 350)

print(z)
```

3.290097607676896

The critical z-values for the two-tailed test at the 5% significance level are ± 1.96 . Since 3.29 is larger than that value, we reject the null hypothesis for $n = 350$.

To sum up; for $n = 50$ we fail to reject the null hypothesis that 3% of the products are faulty. For $n = 350$, we reject the null hypothesis, given that the observed proportion of faulty products in the sample is still 6%.