

Input : X : attribute set; Γ : set of implications

Output: X^+ : the closure of X with respect to Γ ; Γ' : the simplified set of implications

$\Gamma' := \Gamma \cup \{\emptyset \Rightarrow X\}$

$X_{\text{new}} := X$

$X_{\text{old}} := X$

repeat

 Replace $\{\emptyset \Rightarrow X_{\text{old}}\}$ with $\{\emptyset \Rightarrow X_{\text{new}}\}$ in Γ'

$X_{\text{old}} = X_{\text{new}}$

for *each* $A \Rightarrow B \in \Gamma' \setminus \{\emptyset \Rightarrow X_{\text{new}}\}$ **do**

if $A \subseteq X_{\text{new}}$ **then**

 Replace $\{\emptyset \Rightarrow X_{\text{new}}\}$ with $\{\emptyset \Rightarrow X_{\text{new}} \cup B\}$

$X_{\text{new}} := X_{\text{new}} \cup B$

end

if $B \subseteq X_{\text{new}}$ **then**

 Remove $A \Rightarrow B$ from Γ'

end

if $A \cap X_{\text{new}} \neq \emptyset$ *or* $B \cap X_{\text{new}} \neq \emptyset$ **then**

 Replace $A \Rightarrow B$ with $A \setminus X_{\text{new}} \Rightarrow B \setminus X_{\text{new}}$

end

end

until $X_{\text{old}} = X_{\text{new}}$

return X^+ *and* Γ'