

Lab 9 – Pamela the Pediatrician

In 2017, a Pamela the Pediatrician was interested in the heights of children (measured in cm). She collected three random samples from three populations according to birth month and did a one-way ANOVA analysis with the data.

Pamela wanted to test this hypothesis: $H_0: \mu_1 = \mu_2 = \mu_3$

	Group 1 born Mar. 2013	Group 2 born Dec. 2012	Group 3 born Sept. 2012
	104	106	110
	106	101	114
	105	107	115
	102	106	110
	99	109	118
		101	118
			113
sample size	5	6	7
sample mean	103.2	105	114
sample variance	7.7	10.8	11

Find \bar{X} , the overall mean among all 18 observations in the study. Since the sample sizes are not all equal to each other, \bar{X} will not simply equal the average of the three sample means!

Compute SSA by hand. Use a calculator, but show your work.

Compute SSE by hand. Use a calculator, but show your work.

Complete the ANOVA table:

Source	d.o.f.	SS	MS	F
Treatment	$k - 1$	SSA	$MSA = \frac{SSA}{k-1}$	$F = \frac{MSA}{MSE}$
Error	$n - k$	SSE	$MSE = \frac{SSE}{n-k}$	
Total	$n - 1$	SS Total		

Source	d.o.f.	SS	MS	F
Treatment				
Error				
Total				

Draw the Rejection Region on the appropriate curve and label the critical value ($\alpha = .05$).

Did Pamela have significant evidence that $H_0: \mu_1 = \mu_2 = \mu_3$ is false?

Use both SAS and R to confirm your previous answers (see SAS10 and R10 handouts). The data is in a file named pamela.csv

$$\text{Fisher's Least Significant Difference} = \text{LSD} = t_{n-k, \alpha/2} \cdot \sqrt{\text{MSE}} \cdot \sqrt{\frac{1}{n_i} + \frac{1}{n_j}}$$

Find Fisher's LSD for each pair of sample means ($\alpha = .05$). Notice that since the three sample sizes are different, Fisher's LSD will be slightly different for each pair.

LSD for \bar{X}_1 and \bar{X}_2 :

$$\bar{X}_1 - \bar{X}_2 =$$

Are \bar{X}_1 and \bar{X}_2 significantly different?

LSD for \bar{X}_1 and \bar{X}_3 :

$$\bar{X}_1 - \bar{X}_3 =$$

Are \bar{X}_1 and \bar{X}_3 significantly different?

LSD for \bar{X}_2 and \bar{X}_3 :

$$\bar{X}_2 - \bar{X}_3 =$$

Are \bar{X}_2 and \bar{X}_3 significantly different?

Draw an underline summary for the three sample means and identify which pair(s) of means are significantly different from each other:

**After you have completed this handout,
complete the Canvas quiz titled:
Lab 08 – Pamela the Pediatrician**