

## Chapter 9

**Logistic regression** is a tool for building models when there is a categorical response variable with two levels, e.g., yes and no. Logistic regression is a type of **generalized linear model (GLM)** for response variables where regular multiple regression does not work very well. GLMs can be thought of as a two-stage modeling approach. First, model the response variable using a probability distribution, such as the binomial or Poisson distribution. Second, we model the parameter of the distribution using a collection of predictors and a special form of multiple regression. Ultimately, the application of a GLM will feel very similar to multiple regression, even if some of the details are different.

**Logistic Regression** is used to predict a binary outcome (1 / 0, Yes / No, True / False) given a set of independent variables. To represent binary / categorical outcome, we use dummy variables. You can also think of logistic regression as a special case of linear regression when the outcome variable is categorical, where we are using log of odds as dependent variable. In simple words, it predicts the probability of occurrence of an event by fitting data to a logit function.

The fundamental equation of generalized linear model is:

$$g(E(y)) = \alpha + \beta x_1 + \gamma x_2$$

Here,  $g()$  is the link function,  $E(y)$  is the expectation of target variable and  $\alpha + \beta x_1 + \gamma x_2$  is the linear predictor ( $\alpha, \beta, \gamma$  to be predicted). The role of link function is to 'link' the expectation of  $y$  to linear predictor.

Since probability must always be positive, we'll put the linear equation in exponential form. For any value of slope and dependent variable, exponent of this equation will never be negative.

$$\hat{p} = e^{(\beta_0 + \beta(\text{predictor}))} \text{ ----- (b)}$$

To make the probability less than 1, we must divide  $p$  by a number greater than  $p$ . This can simply be done by:

$$\hat{p} = \frac{e^{(\beta_0 + \beta(\text{predictor}))}}{e^{(\beta_0 + \beta(\text{predictor}))} + 1} \text{ ---- (c)}$$

Using (a), (b) and (c), we can redefine the probability as:

$$\hat{p} = \frac{e^y}{1 + e^y} \text{ --- (d)}$$

where  $\hat{p}$  is the probability of success. *This (d) is the Logit Function.*

If  $\hat{p}$  is the probability of success,  $1 - \hat{p}$  will be the probability of failure which can be written as:

$$\hat{q} = 1 - \hat{p} = 1 - \frac{e^y}{1+e^y} \quad \text{--- (e)}$$

where  $\hat{q}$  is the probability of failure.

On dividing, (d) / (e), we get,  $\left(\frac{\hat{p}}{1-\hat{p}}\right) = e^y$  **odds**

After taking log on both sides, we get  $\log\left(\frac{\hat{p}}{1-\hat{p}}\right) = y$

$\log\left(\frac{\hat{p}}{1-\hat{p}}\right)$  is the **link function**. Logarithmic transformation on the outcome variable allows us to model a non-linear association in a linear way.

After substituting value of y, we'll get:  $\log\left(\frac{\hat{p}}{1-\hat{p}}\right) = \beta_0 + \beta(\text{predictor})$  **log odds**

**Odds of winning**  
 $2:1$   
 $\hat{p}(\text{win}) = \frac{2}{3}$   
 $\hat{p}(\text{lose}) = \frac{1}{3}$

This is the equation used in Logistic Regression. Here  $(\hat{p}/1-\hat{p})$  is the odd ratio. Whenever the log of odd ratio is found to be positive, the probability of success is always more than 50%. A typical logistic model plot is shown below. You can see probability never goes below 0 and above 1.

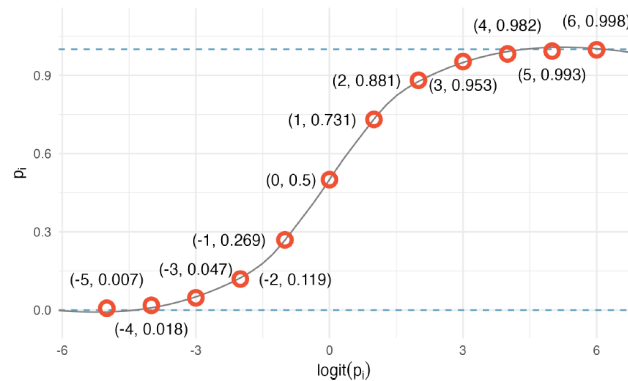
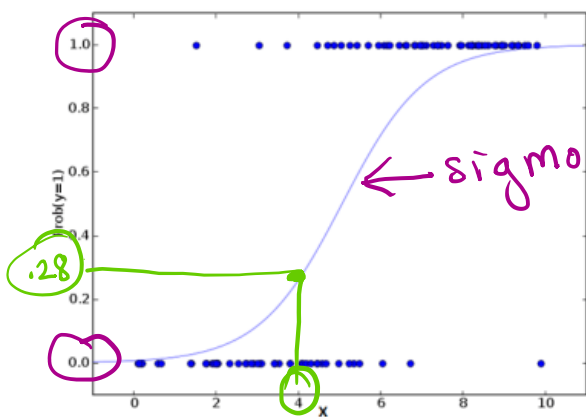


Figure 9.1: Values of  $p_i$  against values of  $\text{logit}(p_i)$ .

We will use the **resume** dataset from openintro (<https://openintro.org/data/index.php?data=resume>)

## Which resume attributes drive job callbacks?

This experiment data comes from a study that sought to understand the influence of race and gender on job application callback rates. The study monitored job postings in Boston and Chicago for several months during 2001 and 2002 and used this to build up a set of test cases. Over this time period, the researchers randomly generating resumes to go out to a job posting, such as years of experience and education details, to create a realistic-looking resume. They then randomly assigned a name to the resume that would communicate the applicant's gender and race. The first names chosen for the study were selected so that the names would predominantly be recognized as belonging to black or white individuals. For example, Lakisha was a name that their survey indicated would be interpreted as a black woman, while Greg was a name that would generally be interpreted to be associated with a white male.

## The Dataset

The first names that were used and randomly assigned in this experiment were selected so that they would predominantly be recognized as belonging to Black or White individuals; other races were not considered in this study. While no name would definitively be inferred as pertaining to a Black individual or to a White individual, the researchers conducted a survey to check for racial association of the names; names that did not pass this survey check were excluded from usage in the experiment. You can find the full set of names that did pass the survey test and were ultimately used in the study in Table 9.1 (textbook). For example, Lakisha was a name that their survey indicated would be interpreted as a Black woman, while Greg was a name that would generally be interpreted to be associated with a White male.

Table 9.2: Descriptions of nine variables from the `resume` dataset. Many of the variables are indicator variables, meaning they take the value 1 if the specified characteristic is present and 0 otherwise.

variable	description
<code>received_callback</code>	Specifies whether the employer called the applicant following submission of the application for the job.
<code>job_city</code>	City where the job was located: Boston or Chicago.
<code>college_degree</code>	An indicator for whether the resume listed a college degree.
<code>years_experience</code>	Number of years of experience listed on the resume.
<code>honors</code>	Indicator for the resume listing some sort of honors, e.g. employee of the month.
<code>military</code>	Indicator for if the resume listed any military experience.
<code>has_email_address</code>	Indicator for if the resume listed an email address for the applicant.
<code>race</code>	Race of the applicant, implied by their first name listed on the resume.
<code>sex</code>	Sex of the applicant (limited to only and in this study), implied by the first name listed on the resume.

The outcome (response variable) we will explore is “`received_callback`”.

### Notation for a logistic regression model.

The outcome variable for a GLM is denoted by  $Y_i$ , where the index  $i$  is used to represent observation  $i$ . In the resume application,  $Y_i$  will be used to represent whether resume  $i$  received a callback ( $Y_i = 1$ ) or not ( $Y_i = 0$ ).

## The Full Regression Model

```

              Estimate Std. Error z value Pr(>|z|)
(Intercept)  -2.53494    0.18531  -13.679  < 2e-16 ***
job_cityChicago -0.41782    0.11468   -3.643  0.000269 ***
years_experience  0.01962    0.01010    1.942  0.052188 .
honors         0.75131    0.18473    4.067  4.76e-05 ***
military       -0.32473    0.21563   -1.506  0.132087
has_email_address 0.26879    0.11663    2.305  0.021193 *
racewhite      0.43709    0.10810    4.043  5.27e-05 ***
gendermale     -0.23905    0.13737   -1.740  0.081814 .
computer_skills -0.24205    0.13963   -1.733  0.083011 .
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

    Null deviance: 2726.9  on 4869  degrees of freedom
Residual deviance: 2656.6  on 4861  degrees of freedom
AIC: 2674.6

```

$$\log\left(\frac{\hat{p}}{1-\hat{p}}\right) = -2.535 - 0.418(\text{job\_city}_{\text{chicago}}) + 0.0196(\text{years\_experience}) + 0.751(\text{honors}) - 0.325(\text{military}) \\ + 0.269(\text{has\_email\_address}) + 0.437(\text{race}_{\text{white}}) - 0.239(\text{gender}_{\text{male}}) - 0.242(\text{computer\_skills})$$

**Example:** Use this model summarized in Table 9.4 to estimate the probability of receiving a callback for: *a job in Chicago where the candidate lists 14 years’ experience, no honors, no military experience, includes an email address, has computer skills, and has a first name that implies they are a White male.*

$$\log\left(\frac{\hat{p}}{1-\hat{p}}\right) = -2.535 - 0.418 + 0.0196(14) + 0.751(0) - 0.325(0) + 0.269(1) + 0.437(1) - 0.239(1) - 0.242(1)$$

$$\log\left(\frac{\hat{p}}{1-\hat{p}}\right) = -2.4536$$

$$\frac{.08598}{1 + .08598} \frac{e^{-2.4536}}{1 + e^{-2.4536}} = 0.07918 = 7.92\% \text{ chance of receiving a callback}$$

## Load library tidyverse and resume dataset

Set your working directory to find the saved dataset and use “head” to view the variables in the dataset

```
library(tidyverse)
library(tidymodels)
setwd("C:/Users/rsaidi/Dropbox/Rachel/MontColl/Datasets/Datasets")
resume <- read_csv("resume.csv")
head(resume)
```

# A tibble: 6 × 30

	job_ad_id	job_city	job_industry	job_type	job_fed_contractor
	<dbl>	<chr>	<chr>	<chr>	<dbl>
1	384	Chicago	manufacturing	supervisor	NA
2	384	Chicago	manufacturing	supervisor	NA
3	384	Chicago	manufacturing	supervisor	NA
4	384	Chicago	manufacturing	supervisor	NA
5	385	Chicago	other_service	secretary	0
6	386	Chicago	wholesale_and_retail_trade	sales_rep	0

#

```
# college_degree <dbl>, honors <dbl>, worked_during_school <dbl>,
# years_experience <dbl>, computer_skills <dbl>, special_skills <dbl>, ...
```

## List all variables in the dataset

```
names(resume)
```

```
[1] "job_ad_id"          "job_city"          "job_industry"
[4] "job_type"           "job_fed_contractor" "job_equal_opp_employer"
[7] "job_ownership"      "job_req_any"        "job_req_communication"
[10] "job_req_education"  "job_req_min_experience" "job_req_computer"
[13] "job_req_organization" "job_req_school"      "received_callback"
[16] "firstname"          "race"              "gender"
[19] "years_college"      "college_degree"     "honors"
[22] "worked_during_school" "years_experience"    "computer_skills"
[25] "special_skills"     "volunteer"          "military"
[28] "employment_holes"   "has_email_address"  "resume_quality"
```

## Visualizing the data

Let's start by looking at whether an applicant received a callback based on years experience.

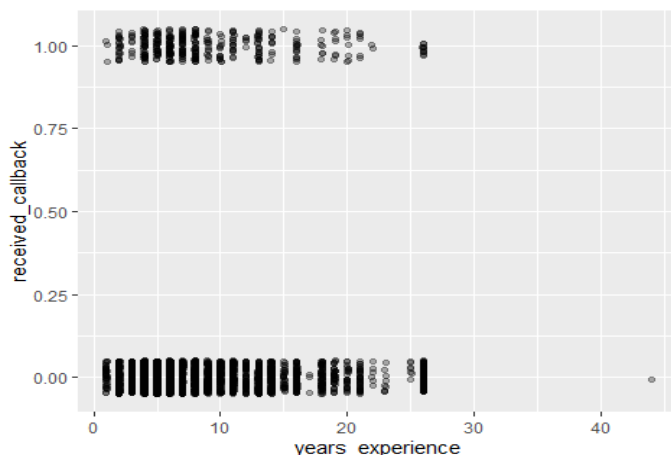
### Ensure the response variable is binary

Check out **received\_callback** to be sure that the values are zeros or ones. In our case, we are fine. If they are not, you can use the code below to change it.

```
data <- data %>% mutate(newvar = ifelse(oldvar == "yes", 1, 0))
```

Note that in the plot below, we use the **geom\_jitter()** function to create the illusion of separation in our data. Because the y value is categorical, all of the points would either lie exactly on "dead" or "alive", making the individual points hard to see. To counteract this, **geom\_jitter()** will move the points a small random amount up or down.

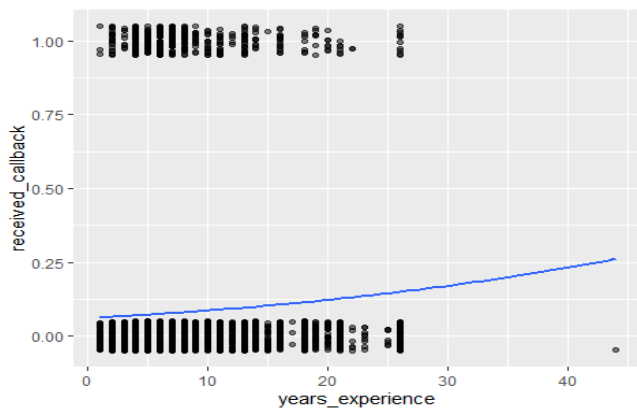
```
ggplot(data = resume, aes(x = years_experience, y = received_callback)) +
  geom_jitter(width = .05, height = 0.05, alpha = 0.3)
```



## Fit a logistic regression model

Start with the simple premise above, that years experience is associated with the likelihood of receiving a callback.

```
plot_log <- ggplot(data = resume, aes(y = received_callback, x = years_experience)) +  
  geom_jitter(width = 0, height = 0.05, alpha = 0.5) +  
  geom_smooth(method = "glm", se = FALSE, method.args = list(family = "binomial"))  
plot_log  
  
`geom_smooth()` using formula = 'y ~ x'
```



`geom_smooth(method = "glm")` creates a **sigmoid** curve, like a stretched-out S. This curve fits to the binary values (zeros and ones plotted). It shows the predicted probabilities of receiving a callback, based on years experience. You can see that even a candidate with 20 years of experience has about a 12.5% chance of receiving a callback.

## Odds scale

To combat the problem of the scale of the y variable, we can change the scale of the variable on the y-axis. Instead of thinking about the probability of receiving a callback, we can think about the odds. While these two concepts are often conflated, they are not the same. They are however, related by the simple formula below. The odds of a binary event are the ratio of how often it happens, to how often it doesn't happen.

$$\text{odds}(\hat{y}) = \frac{\hat{y}}{1 - \hat{y}} = \exp(\beta_0 + \beta_1 x)$$

Thus, if the probability of receiving a callback is 10%, then the odds of receiving a callback are  $.1/(1-.1) = 1:9$

Odds are commonly used to express uncertainty in a variety of contexts.

## Use the Tidymodels package to create a model

### Create the testing and training data by splitting

```
# convert received_callback to categorical variable  
resume$received_callback <- as.factor(resume$received_callback)  
set.seed(123)
```

```
#initial_split creates a single binary split of the data into a training set and testing
set (the default is 75% training 25% testing)

res_splits<- initial_split(resume, strata = received_callback)

callback_train <- training(res_splits)
callback_test  <- testing(res_splits)
```

## Calculate training set proportions by callbacks

```
callback_train |>
  group_by(received_callback) |>
  tally() |>
  mutate(prop = n/sum(n))

# A tibble: 2 × 3
  received_callback     n   prop
  <fct>             <int> <dbl>
1 0                 3364 0.921
2 1                  288 0.0789
```

We see that in the training set, 8% of applicants did receive callbacks.

## logistic model

```
logit_fit <-
  logistic_reg(mode = "classification") |>
  set_engine(engine = "glm") |>
  fit(received_callback ~ years_experience, data = callback_train)
```

## Prediction

To get predicted values we use the function **predict**.

```
## get prediction on train set
pred_logit_train <- predict(logit_fit, new_data = callback_train)
## get prediction on test set
pred_logit_test <- predict(logit_fit, new_data = callback_test)
## get probabilities on test set
prob_logit_test <- predict(logit_fit, new_data = callback_test, type="prob")
```

## Model performance

**yardstick** is a package to get metrics on model performance. By default on classification problem `yardstick::metrics` returns accuracy and kappa.

```
library(yardstick)
metrics(bind_cols(callback_test, pred_logit_test), truth = received_callback, estimate =
.pred_class)

# A tibble: 2 × 3
  .metric .estimator .estimate
  <chr>    <chr>      <dbl>
```

1	accuracy	binary	0.915
2	kap	binary	0

The accuracy is 91.4% - very close to the original data (1- p\_hat).

## The null model

It will be useful to have our null model stored as a model object. We can create such an object using tidymodels by specifying a logistic regression model with no explanatory variables. The computational engine is glm because glm() is the name of the R function that actually fits vocab("generalized linear models") (of which logistic regression is a special case).

```
mod_null <- logistic_reg(mode = "classification") |>
  set_engine("glm") |>
  fit(received_callback ~ 1, data = callback_train)
```

## Compute the accuracy of the null model

According to Wikipedia, *accuracy* is how close a given set of measurements (observations or readings) are to their true value.

```
pred <- callback_train |>
  select(received_callback, years_experience) |>
  bind_cols(predict(mod_null, new_data = callback_train, type = "class")) |>
  rename(mod_null = .pred_class)
accuracy(pred, received_callback, mod_null)

# A tibble: 1 × 3
  .metric .estimator .estimate
  <chr>    <chr>      <dbl>
1 accuracy binary      0.921
```

The accuracy estimate of this null model is almost the same: = 92.1%.

## Create a confusion matrix

This is a two-way table that counts how often our model made the correct prediction. Note that there are two different types of mistakes that our model can make: predicting receiving a callback when a callback was not received (a Type I error), and predicting not receiving a callback when the callback was received (a Type II error).

**Confusion Matrix** is nothing but a tabular representation of Actual vs Predicted values. This helps us to find the accuracy of the model and avoid overfitting. This is how it looks like:



		Predicted	
		Good	Bad
Actual	Good	True Positive {d}	False Negative {c}
	Bad	False Positive {b}	True Negative {a}

You can calculate the **accuracy** of your model with:

$$\frac{\text{True Positive} + \text{True Negatives}}{\text{True Positive} + \text{True Negatives} + \text{False Positives} + \text{False Negatives}}$$

From the confusion matrix, **Specificity and Sensitivity** can be derived as illustrated below:

$$\left. \begin{aligned} \text{True Negative Rate (TNR), specificity} &= \frac{A}{A+B} \\ \text{False Positive Rate (FPR), } 1 - \text{specificity} &= \frac{B}{A+B} \end{aligned} \right\} \text{sum to 1}$$

$$\left. \begin{aligned} \text{True Positive Rate (TPR), sensitivity} &= \frac{D}{C+D} \\ \text{False Negative Rate (FNR)} &= \frac{C}{C+D} \end{aligned} \right\} \text{sum to 1}$$

Specificity and Sensitivity plays a crucial role in deriving ROC curve.

```
confusion_null <- pred |>
  conf_mat(truth = received_callback, estimate = mod_null)
confusion_null
```

```
      Truth
Prediction 0    1
0    3364  288
1      0    0
```

Note that the null model predicts that *NONE* do not receive a callback (`receives_callback = 0`), so it makes many *Type II errors* (false negatives) and *NONE* receive a callback (`receives_callback = 1`) *Type I errors* (false positives).

## Build Logit Models and Predict

Start by building the logit model using training data

Beating the null model shouldn't be hard. Our first attempt will be to employ a simple logistic regression model. First, we'll fit the model using only one explanatory variable: `years_experience`. It stands to reason that more experienced people are more likely to get a job offer.

```
mod_log_1 <- logistic_reg(mode = "classification") |>
  set_engine("glm") |>
  fit(received_callback ~ years_experience, data = callback_train)
```

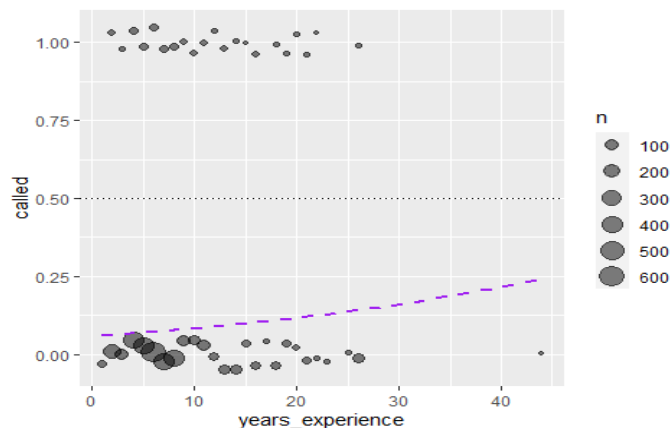
## Illustrate the predicted probability

Illustrate how the predicted probability of dying varies in our simple logistic regression model with respect to a person's age. Notice the sigmoid curve (in purple) - this is the shape of a logistic curve.

```
train_plus <- callback_train |>
  mutate(called = as.integer(received_callback == 1))

ggplot(train_plus, aes(x = years_experience, y = called)) +
  geom_count(
    position = position_jitter(width = 0, height = 0.05),
    alpha = 0.5 ) +
  geom_smooth(method = "glm", method.args = list(family = "binomial"),
    color = "purple", lty = 2, se = FALSE) +
  geom_hline(aes(yintercept = 0.5), linetype = 3)

`geom_smooth()` using formula = 'y ~ x'
```



This still looks very similar to the original plot.

## ROC - Receiver Operating Characteristics

Receiver Operating Characteristics Curve traces the percentage of true positives accurately predicted by a given logit model as the prediction probability cutoff is lowered from 1 to 0. For a good model, as the cutoff is lowered, it should mark more of actual 1's as positives and lesser of actual 0's as 1's. So for a good model, the curve should rise steeply, indicating that the TPR (Y-Axis) increases faster than the FPR (X-Axis) as the cutoff score decreases.

## AUC - Area under the curve

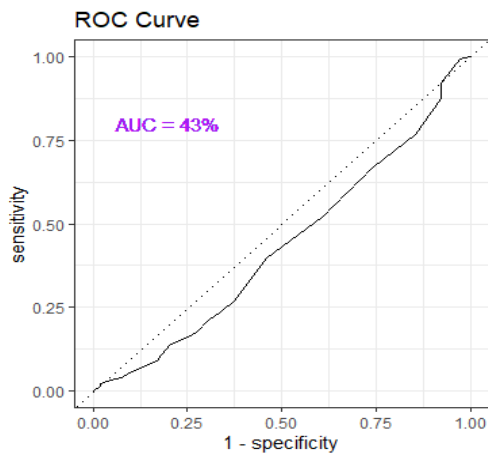
The greater the area under the ROC curve, better the predictive ability of the model

```
roc_auc(bind_cols(callback_test, prob_logit_test), truth = received_callback, .pred_1)

# A tibble: 1 × 3
  .metric .estimator .estimate
  <chr>    <chr>      <dbl>
1 roc_auc binary      0.433
```

The AUC estimate is 43.3% - this is VERY low, meaning the model is not great for predicting probabilities.

```
roc_data <- roc_curve(bind_cols(callback_test, prob_logit_test), truth = received_callback, .pred_1)
roc_data |>
  ggplot(aes(x = 1 - specificity, y = sensitivity)) +
  geom_path() +
  geom_abline(lty = 3) +
  coord_equal()+
  ggtitle("ROC Curve")+
  theme_bw()+
  geom_text(x=0.2, y=.8, label="AUC = 43%", color ="purple")
```



## The Full Regression Model

Computing the full logistic regression model will feel similar to the process for computing the full multiple linear regression model. We will use **GLM** to replace **LM** and we need to include **family = binomial()**

```
log_mod1 <- glm(data=resume, received_callback ~ job_city + college_degree + years_experience + honors + military + has_email_address + race + gender + computer_skills + resume_quality, family = binomial())
summary(log_mod1)
```

Call:

```
glm(formula = received_callback ~ job_city + college_degree + years_experience + honors + military + has_email_address + race + gender + computer_skills + resume_quality, family = binomial(), data = resume)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-0.8721	-0.4330	-0.3785	-0.3268	2.6204

Coefficients:

	Estimate	Std. Error	z value	Pr(> z )	
(Intercept)	-2.47003	0.33302	-7.417	1.20e-13	***
job_cityChicago	-0.42156	0.11493	-3.668	0.000245	***
college_degree	-0.06682	0.12244	-0.546	0.585214	
years_experience	0.01896	0.01037	1.828	0.067475	.
honors	0.75741	0.18539	4.085	4.40e-05	***
military	-0.32315	0.21597	-1.496	0.134577	
has_email_address	0.25501	0.23523	1.084	0.278320	
racewhite	0.43659	0.10811	4.038	5.38e-05	***
genderm	-0.22604	0.13996	-1.615	0.106289	
computer_skills	-0.24265	0.14064	-1.725	0.084476	.
resume_qualitylow	-0.01140	0.23602	-0.048	0.961473	

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 2726.9 on 4869 degrees of freedom  
Residual deviance: 2656.3 on 4859 degrees of freedom  
AIC: 2678.3

Number of Fisher Scoring iterations: 5

## Performance of Logistic Regression Model

To evaluate the performance of a logistic regression model, we must consider few metrics: AIC and p-values.

AIC (Akaike Information Criteria) – The analogous metric of adjusted  $R^2$  in logistic regression is AIC. AIC is the measure of fit which penalizes model for the number of model coefficients. Therefore, we always prefer model with **minimum** AIC value.

## Assessing our full model

1. The AIC is 2678
2. The largest p-values come from college\_degree and resume\_quality

Remove college\_degree and resume\_quality and re-run the model

```
log_mod2 <- glm(data=resume, received_callback ~ job_city + years_experience + honors + m  
ilitary + has_email_address + race + gender + computer_skills, family = binomial())  
summary(log_mod2)
```

Call:

```
glm(formula = received_callback ~ job_city + years_experience +  
    honors + military + has_email_address + race + gender + computer_skills,  
    family = binomial(), data = resume)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-0.8580	-0.4329	-0.3732	-0.3276	2.6244

Coefficients:

```
      Estimate Std. Error z value Pr(>|z|)
(Intercept)  -2.53494    0.18531 -13.679  < 2e-16 ***
job_cityChicago -0.41782    0.11468  -3.643 0.000269 ***
years_experience  0.01962    0.01010   1.942 0.052188 .
honors          0.75131    0.18473   4.067 4.76e-05 ***
military       -0.32473    0.21563  -1.506 0.132087
has_email_address 0.26879    0.11663   2.305 0.021193 *
racewhite       0.43709    0.10810   4.043 5.27e-05 ***
genderm        -0.23905    0.13737  -1.740 0.081814 .
computer_skills -0.24205    0.13963  -1.733 0.083011 .
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

(Dispersion parameter for binomial family taken to be 1)

```
Null deviance: 2726.9 on 4869 degrees of freedom
Residual deviance: 2656.6 on 4861 degrees of freedom
AIC: 2674.6
```

Number of Fisher Scoring iterations: 5

The AIC decreased to 2675 and all p-values are relatively low.

## VIF - Variance Inflation Factor

Like in case of linear regression, we should check for multicollinearity in the model.

One way to measure multicollinearity is the variance inflation factor (VIF), which assesses how much the variance of an estimated regression coefficient increases if your predictors are correlated.

A VIF between 5 and 10 indicates high correlation that may be problematic. And if the VIF goes above 10, you can assume that the regression coefficients are poorly estimated due to multicollinearity.

```
#install.packages("car") #car package will calculate the VIF
library(car)
vif(log_mod2)
```

	job_city	years_experience	honors	military
	1.162480	1.176885	1.057478	1.189503
		race	gender	computer_skills
has_email_address	1.204211	1.001827	1.126755	1.159797

All X variables in the model have VIF well below 4, so log\_mod2 model does not appear to have multicollinearity.

## Example for predicting

Use this model (log\_mod2) to estimate the probability of receiving a callback for: a job in Chicago where the candidate lists 14 years' experience, no honors, no military experience, includes an email address, has computer skills, and has a first name that implies they are a White male.

```
# the log odds value of the above characteristics
-2.535-0.418+0.0196*14+0.269+0.437-0.239-0.242

[1] -2.4536

# calculate the probability using the above value
exp(-2.4536)/(1+exp(-2.4536))

[1] 0.07917569
```

The probability of receiving a callback for a candidate looking at a job in Chicago with 14 years' experience, no honors, no military experience, included an email address, has computer skills, and has a first name that implies they are White male is 7.92%

### Overall

Although this tutorial goes through many concepts that are involved with logistic regression, one of the take-aways is that there are many components involved in building the model and then testing the model.

## Homework Chapter 9

1. Review section 9.5 (the chapter review)
2. **Suggested:** from textbook section 9.6 exercises: 3,4,5,6,8
3. **Suggested:** Unit 3 Tutorial Regression Modeling:  
9 - [Logistic regression](#)