

# Galaxy Zoo: Evidence for quenching caused by AGN feedback

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## ABSTRACT

A black hole resides at the centre of every galaxy whereby it co-evolves with its host. Despite its relatively small size, an active black hole (active galactic nucleus; AGN) can have an impact on the evolution of its host galaxy through the feedback of energy into the galaxy system. The largest fraction of AGN are commonly found in the ‘green valley’, suggesting a relation between the AGN and the suppression (quench) of star formation, causing the galaxy to transition from the star forming ‘blue cloud’ to the dead ‘red sequence’. Though observational evidence has been found for both positive and negative feedback caused by an AGN, the effect on the galaxy wide star formation history (SFH) due to the presence of an AGN has not been studied. Here we present the first observational population study of the SFH of AGN host galaxies, in comparison with a population inactive galaxies using a Bayesian method. We find evidence for an AGN host galaxy to have undergone a recent and rapid drop in its star formation rate. This result is not seen for the inactive galaxies whose SFHs are dominated by the effects of downsizing at earlier epochs; a secondary effect for the AGN host galaxies. We show that rapid quenching histories cannot account fully for the quenching of all the star formation across the population of AGN host galaxies and that slower quenching histories, attributed to non-violent processes of evolution are also key in their evolution. This is against the typically accepted merger driven scenario of the co-evolution of black holes and their galaxies. The availability, and ability to be replenished, of gas in the reservoirs of a galaxy is the key driver behind this co-evolution.

## 1 INTRODUCTION

Two of the most important issues in current astrophysical understanding are: (i) the co-evolution of galaxies and their central black holes and (ii) the effects, if any, of AGN feedback. There is an obvious relationship between the evolution of a central black hole and its host galaxy, observed multiple times and commonly referred to as the Maggorian relationship (Maggorrian et al. 1998; Marconi & Hunt 2003; Haring & Rix 2004). AGN feedback was first theorised as a mechanism for regulating star formation in simulations (Croton et al. 2006; Bower et al. 2006; Somerville et al. 2008) and some indirect evidence has been observed for both positive and negative feedback in various systems (see the comprehensive review from Fabian 2006).

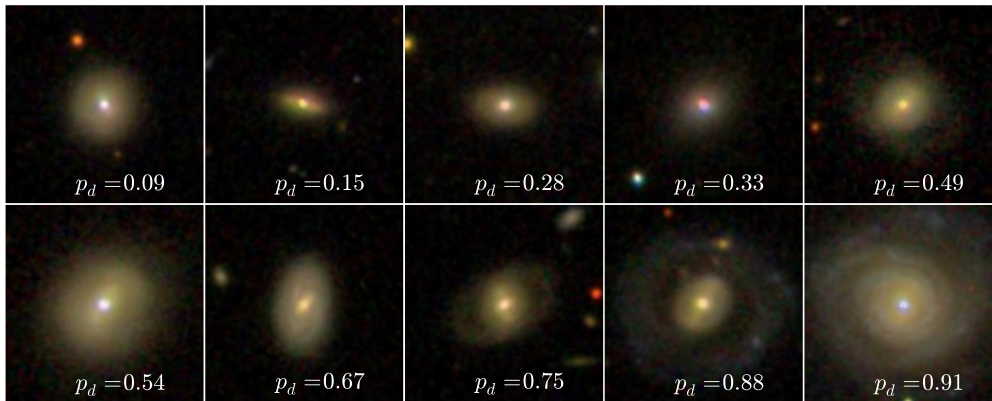
The strongest observational evidence for this feedback is that the largest fraction of AGN are found in the green valley (Cowie & Barger 2008; Hickox et al. 2009; Schawinski

et al. 2010), suggesting some link to the process of quenching star formation in order for a galaxy to progress from the blue cloud to the red sequence. However, the rate at which this quenching occurs and its effect on the galaxy population as a whole, has not been studied.

Here we present the first large observational population study of AGN host galaxies with the use of a new PYTHON routine, STARPY, implementing a Bayesian method to effectively model the SFH of a galaxy with two parameters given the observed near ultra-violet (NUV) & optical colours. We therefore aim to determine the following: (i) Are galaxies currently hosting an AGN undergoing quenching? (ii) If so, when and at what rate does this quenching occur?

This letter proceeds as follows. Section 2 contains a description of the sample data, and details of the Bayesian analysis of an exponentially declining star formation history model. Section 3 contains the results produced by this analysis, with Section 4 providing a detailed discussion and a summary of the results obtained. The zero points of all ugriz magnitudes are in the AB system and where necessary we adopt the WMAP Seven-Year Cosmological parameters (Jarosik et al. 2011) with  $(\Omega_m, \Omega_\lambda, h) = (0.26, 0.73, 0.71)$ .

\* This investigation has been made possible by the participation of more than 250,000 users in the Galaxy Zoo project. Their contributions are individually acknowledged at <http://authors.galaxyzoo.org>



**Figure 1.** Randomly selected SDSS *gri* composite images from the sample of 984 Type 1 AGN showing the continuous probabilistic nature of the Galaxy Zoo sample from a redshift range  $0.040 < z < 0.05$ . The debiased ‘disc or featured’ vote fraction (see Willett et al. 2013) for each galaxy is shown. Note the bright point source of the AGN in the centre of each galaxy. The scale for each image is 0.099 arcsec/pixel.

## 2 DATA & METHODS

### 2.1 Galaxy Zoo 2

In this investigation we use visual classifications of galaxy morphologies from the Galaxy Zoo 2<sup>1</sup> citizen science project (Willett et al. 2013), which obtains multiple independent classifications for each optical galaxy image; the full question tree for each image is shown in Figure 1 of Willett et al. 2013.

The Galaxy Zoo 2 (GZ2) project consists of 304,022 images from the SDSS DR8 (a subset of those classified in Galaxy Zoo 1; GZ1) all classified by *at least* 17 independent users, with the mean number of classifications standing at  $\sim 42$ .

Further to this, we required NUV photometry from the GALEX survey, within which  $\sim 42\%$  of the GZ2 sample were observed, giving a total sample size of 126,316 galaxies. The completeness of this subsample of GZ2 matched to GALEX is shown in Figure 2 of Smethurst et al. (2015) with the *u*-band absolute magnitude against redshift for this sample compared with the SDSS data set. Typical Milky Way  $L_*$  galaxies with  $M_u \sim -20.5$  are still included in the GZ2 subsample out to the highest redshift of  $z \sim 0.25$ ; however dwarf and lower mass galaxies are only detected at the lowest redshifts.

### 2.2 STARPY

STARPY is a PYTHON code which allows the user to derive the quenched star formation history (SFH) of a galaxy through a Bayesian Markov Chain Monte Carlo method with the input of two observed photometric colours, a redshift, and the use of the SSP models of Bruzual & Charlot (2003). The star formation history template is an exponential decline of the SFR and is described by two parameters  $[t_q, \tau]$  where  $t_q$  is the time at which the onset of quenching begins [*Gyr*] and  $\tau$  is the exponential rate at which quenching occurs [*Gyr*]. Under the simplifying assumption that all galaxies formed

at  $t = 0$  Gyr with an initial burst of star formation, the SFH can therefore be described as:

$$SFR = \begin{cases} i_{sfr}(t_q) & \text{if } t < t_q \\ i_{sfr}(t_q) \times \exp\left(\frac{-(t-t_q)}{\tau}\right) & \text{if } t > t_q \end{cases} \quad (1)$$

where  $i_{sfr}$  is an initial constant star formation rate dependent on  $t_q$  (see Smethurst et al. 2015). A smaller  $\tau$  value corresponds to a rapid quench, whereas a larger  $\tau$  value corresponds to a slower quench. The output of STARPY is probabilistic in nature and provides the likelihood across the entirety of the two parameter space for each individual galaxy.

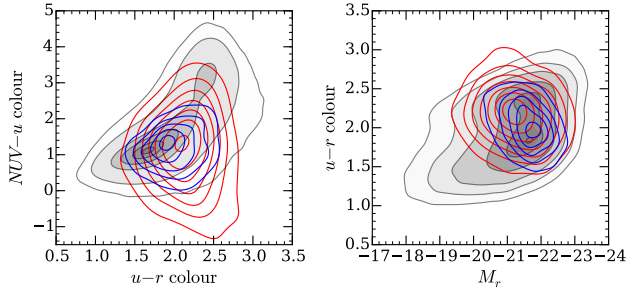
The probabilistic fitting methods to this SFH for an observed galaxy are described in full detail in Smethurst et al. (2015) wherein the STARPY code was run on a volume limited sample ( $0.01 < z < 0.25$ ) of 126,316 galaxies of the Galaxy Zoo 2 project from SDSS DR8 (York et al. 2009; Aihara et al. 2011). This will be referred to as the GZ2-STARPY sample.

### 2.3 AGN Sample

We utilise a new sample of type 1 AGN selected by Oh et al. (2015) who built on the selection techniques of the OSSY catalogue<sup>2</sup> (Oh et al. 2011). To search for broad line region (BLR) AGN Oh et al. (2015) used a flux ratio between two regions near the  $H\alpha$  emission line in SDSS DR7 spectra. The two regions were  $6460 - 6480\text{\AA}$  and  $6523 - 6543\text{\AA}$  to give a flux ratio,  $F_{6533}/F_{6470}$ ; which identified, if high, those candidate AGN host galaxies. Each spectra was fit using the IDL PPXF and GANDALF programs with the Bruzual & Charlot (2003) and MILES stellar libraries using the Levenberg Marquardt minimisation method (Markwardt et al. 2009). From the measured continuums and emission line widths, Type 1 AGN were selected

<sup>1</sup> <http://zoo2.galaxyzoo.org/>

<sup>2</sup> <http://gem.yonsei.ac.kr/ossy/>



**Figure 2.** Optical-NUV colour-colour diagram (left panel) and optical colour-magnitude diagram (right panel) showing the inactive sample of galaxies (grey filled contours) in comparison to those for the AGN host galaxies with disc morphologies (blue contours;  $p_d > 0.5$ ) and smooth morphologies (red contours;  $p_d > 0.5$ ) with magnitudes corrected for the AGN flux contribution.

with the following criteria: (i)  $0.00 < z < 0.20$ , (ii) FWHM of  $H\alpha > 800 \text{ km s}^{-1}$  and (iii) A/N of broad  $H\alpha > 3$ .

This resulted in a sample of 9,671 Type 1 AGN identified by Oh et al. (2015) with broad line and luminosity measurements provided in the published catalogue. This sample was then matched to the GZ2-STARPY sample to give 984 galaxies currently hosting AGN. This will be referred to as the AGN-HOST sample.

As the optical and NUV photometry are required by STARPY to predict the most likely star formation history of these galaxies, we removed the flux contribution from the AGN at the centre of each galaxy to obtain only the stellar flux contribution. Note bright central point sources of the AGN in each galaxy of Figure 1 which mandate this approach necessary.

This was achieved using the petrosian and PSF magnitudes provided by SDSS and the ‘AUTO’ and ‘aperture 3’ magnitudes provided by GALEX. The GALEX PSF size is quoted at  $5 - 6''$  therefore in order to ensure that the entirety of the flux contribution from the AGN was removed, the  $7''$  ‘aperture 3’ was selected (as opposed to the smaller  $4.5''$  ‘aperture 2’ provided by GALEX). A check was made to ensure that this  $7''$  aperture did not encompass the entire galaxy using the SDSS u-band Petrosian 90% Flux Radius, doubled to give a more accurate size of the galaxy due to the effects of the AGN point source on the Petrosian Flux estimation. 17% of the AGN host galaxies appeared to lay below this  $7''$  radius, however upon inspection were the most luminous AGN. Therefore further visual inspection of the size ensured they were in fact larger than  $7''$ .

The newly corrected stellar magnitudes were k-corrected to  $z = 0$  with the routine provided in Chilingarian et al. (2010) and extinction corrected using the dust maps of Schlegel et al. (1998)<sup>3</sup> and optical and NUV values of  $A/E(B - V)$  from Schlafly & Finbeiner (2011) and Seibert et al. (2005) respectively.

The colours calculated from these corrected magnitudes

are shown in Figure 2 in comparison to those of the GZ2-STARPY inactive galaxy sample. We can see that the AGN-HOST galaxies typically lie between the red sequence and blue cloud populations of galaxies in the area commonly known as the green valley, an observation that also supports the findings of Cowie & Barger (2008); Hickox et al. (2009) and Schawinski et al. (2010).

The AGN-HOST sample is studied in three different mass bins with 112 (11%) low mass ( $M_* < 10.25 M_\odot$ ), 572 (58%) medium mass ( $10.25 < M_* [M_\odot] < 10.75$ ) and 300 (31%) high mass ( $M_* > 10.75 M_\odot$ ) galaxies and is compared to the larger GZ2-STARPY sample of 125,332 galaxies in the three different mass bins defined above, with 41,698 (33%) low mass, 47,391 (38%) medium mass and 36,243 (29%) high mass galaxies.

The GZ2-STARPY sample will contain some obscured AGN, Seyfert’s, LINERS etc. however these types of active galaxies are a minimal ( $\sim 10\%$ ) proportion of the local galaxy population (Eastman et al. 2007; Haggard et al. 2010; Aird et al. 2010). Due to the high numbers of galaxies in this sample, the effects of these minority galaxies will get washed out and the ‘typical’ galaxy which is representative of each population will dominate the likelihoods of the population SFHs. To remove them completely with a BPT diagram would have also removed quiescent galaxies and given a sample of purely star forming galaxies which would not be representative of the galaxy population. We therefore utilise the GZ2-STARPY sample as a control sample of inactive galaxies against the agn-host sample.

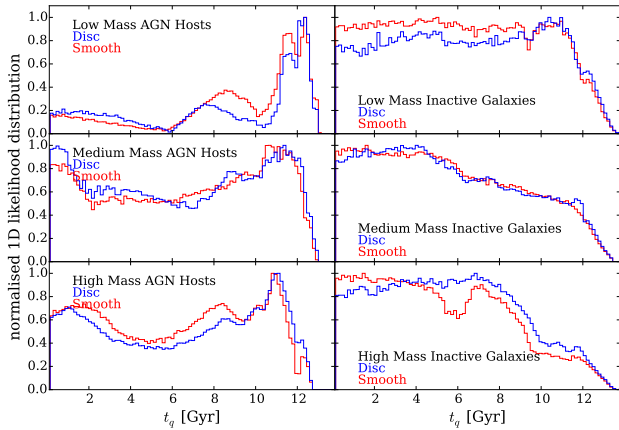
### 3 RESULTS

Each galaxy was run through STARPY to obtain a 2D likelihood distribution across the  $[t_q, \tau]$  parameter space. The individual likelihood distributions of each galaxy were combined across the three mass bins defined in Section 2.3 for the AGN-HOST and GZ2-STARPY galaxies. Here we utilise the GZ2 morphologies to weight by the vote fractions to split the sample into smooth and disc dominated populations. We stress that this portion is purely for visualisation purposes and is no longer a Bayesian method.

These 2D likelihoods are summed across each parameter axis and normalised to produce the one dimensional histograms shown in Figures 3 and 4 for the quenching time,  $t_q$  and quenching rate  $\tau$  respectively. In each figure the summed 1D normalised probability distribution across the given parameter is shown for smooth (red) and disc (blue) galaxies split into the three mass bins; low (top), medium (middle) and high (bottom) mass galaxies for the AGN host (left) and inactive galaxies (right). In Figure 4 the percentage likelihood in each region of quenching rate shown by the dashed lines for rapid ( $\tau < 1 \text{ Gyr}$ ), intermediate ( $1 < \tau [\text{Gyr}] < 2$ ) and slow ( $\tau > 2 \text{ Gyr}$ ) quenching timescales.

It is immediately apparent from Figures 3 and 4 that there is a distinct difference between the distribution of likelihood for AGN hosts (left panels) and inactive galaxies (right panels) for both parameters. For the inactive galaxies, the likelihood for quenching at later times decreases with increasing mass, whereas for the lower mass galaxies the quenching is roughly constant with time for both smooth and disc dominated populations. This is observational ev-

<sup>3</sup> Software for extracting the  $E(B - V)$  values from the Schlegel et al. (1998) dust maps is available at [github.com/rjismethurst/ebvpy](https://github.com/rjismethurst/ebvpy)



**Figure 3.** 1D summed distribution of 2D likelihood in quenching time for AGN (left) host and inactive (right) galaxies, split into low (top), medium (middle) and high (bottom) mass galaxies for smooth (red) and disc (blue) galaxies. A low value of  $t_q$  corresponds to the early Universe and a high value to the recent Universe.

idence of downsizing across the generic galaxy population whereby stars in massive galaxies form first and subsequent star formation at later times is suppressed therefore there is no star formation to quench (Cowie et al. 1996; Thomas et al. 2010).

The distribution of likelihood for AGN host galaxies across the quenching time  $t_q$  parameter (left panels of Figure 3), is very obviously different from that of the inactive galaxies (right panels of Figure 3). Recent quenching is the most dominant history across all three mass bins, particularly for low mass galaxies. However, this effect is dampened in higher mass galaxies where quenching at earlier times also has significant likelihood.

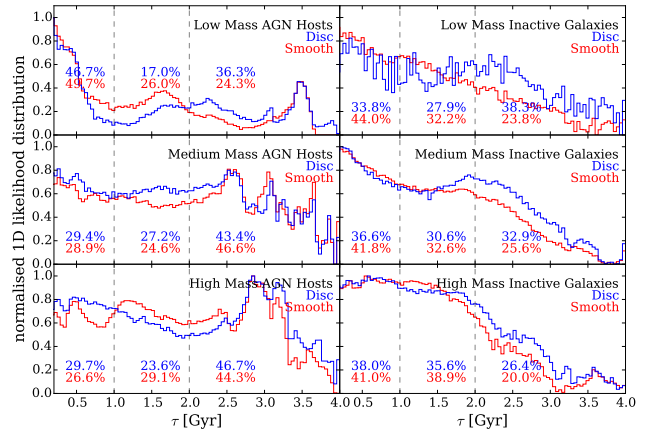
The distribution of likelihoods for the rate of quenching,  $\tau$ , in Figure 4, show once again the AGN host (left panels) and inactive (right panels) galaxies distributions are vastly different. The likelihood for rapid quenching ( $\tau < 1$  Gyr) increases for inactive galaxies of increasing mass (see percentage likelihoods in the left hand panels of Figure 4) and the likelihood for slow quenching ( $\tau > 2$  Gyr) also increases for inactive disc galaxies with increasing mass.

However, the distribution of likelihood of the rate of quenching for the AGN host galaxies is in fact the opposite to that seen for inactive galaxies. The likelihood for rapid quenching decreases with increasing mass for both smooth and disc dominated populations, whereas for slow quenching rates the likelihood increases with increasing mass for the disc dominated population.

## 4 DISCUSSION

The vast differences between the distribution of likelihood for the AGN host and inactive galaxy populations reveals that AGN have a significant effect on the SFH of their host galaxy and can be associated with both recent rapid quenching and earlier, slower quenching histories.

As well as the clear evidence for downsizing in the inactive galaxy population in Figure 3, we can also see it's effect



**Figure 4.** 1D summed distribution of 2D likelihood in quenching rate for AGN (left) host and inactive (right) galaxies, split into low (top), medium (middle) and high (bottom) mass galaxies for smooth (red) and disc (blue) galaxies. The dashed lines show the separation between rapid ( $\tau < 1.0$  Gyr), intermediate ( $1.0 < \tau < 2.0$  Gyr) and slow ( $\tau > 2.0$  Gyr) quenching timescales with the fraction of the likelihood distribution in each region shown. A small (large) value of  $\tau$  corresponds to a rapid (slow) quenching rate.

on the AGN host galaxies. Although recent quenching is the dominant history, quenching at earlier times also has significant likelihood with increasing mass. These galaxies may have undergone downsizing earlier in life with the current AGN also having an effect on the SFR through feedback, causing a recent, rapid quench of any residual star formation.

Tortora et al. (2009) find by modelling the effects of negative AGN feedback on a typical early type (i.e. smooth) galaxy the time between the current galaxy age,  $t_{gal}$  and the time that the feedback began  $t_{AGN}$ , peaks at  $t_{gal} - t_{AGN} \sim 0.85$  Gyr. This is in agreement with the location of the peak in Figure 3 for the low mass galaxies, where the difference between the peak of the likelihood and the average age of the population (calculated from the redshift and assuming all galaxies form at  $t = 0$ ) is  $\sim 0.83$  Gyr for both smooth and disc dominated populations. This suggests that this dominant recent quenching history is caused directly by negative AGN feedback.

If a slowly ‘dying’ or ‘dead’ galaxy has an infall of gas either through a minor merger, galaxy interaction or environmental change, this can trigger further star formation and feed the central black hole, igniting an AGN. In turn this AGN can then quench the recent boost in star formation. This track is similar to the evolution history theorised for blue ellipticals (Kaviraj et al. 2013; McIntosh et al. 2014; Haines et al. 2015). As for the disc galaxies, it also follows from the ideas of previously isolated discs evolving slowly by the Kennicutt-Schmidt (KS; Schmidt 1959; Kennicutt 1997) law which can then undergo an interaction or merger to reinvigorate star formation and feed the central black hole.

The difference between the AGN host and inactive galaxies distribution of likelihood in Figure 4 for the rate of quenching,  $\tau$ , tells a story of gas reservoirs. Smethurst et al. (2015) speculated that rapid quenching rates could be attributed to mergers of galaxies, therefore we expect

the trend of increasing likelihood for rapid quenching rates with increasing mass for the inactive galaxies, as mergers are thought to be responsible for creating the most massive smooth galaxies (Conselice et al. 2003; Springel, Di Matteo & Hernquist 2005; Hopkins et al. 2008). Similarly we also expect the trend of increasing likelihood for slow quenching rates with increasing mass as Smethurst et al. (2015) attributed slower quenching histories to secular (non-violent) evolution of isolated galaxies (Kormendy & Kennicutt 2004; Cisternas et al. 2011) which are often lower in mass (Varela et al. 2004; Bamford et al. 2009) due to their isolation from other galaxies and therefore any potential gas reservoirs.

The trends with likelihood of  $\tau$  in Figure 4 are reversed however for the AGN host galaxies. The likelihood for rapid quenching decreases with increasing mass for both smooth and disc dominated populations and for slow quenching increases with increasing mass disc galaxies. It appears that the most massive disc galaxies, therefore with the most massive gas reservoirs evolve with a slow quench of star formation through the KS law and also have enough gas to feed the central black hole to trigger a current AGN (Varela et al. 2004; Emsellem et al. 2015). Conversely, a rapid quench, possibly caused by the AGN itself through negative feedback, is only the most dominant history for low mass galaxies with lower gravitational potentials which allow gas to be expelled more easily (or heated by the AGN) across the entire galaxy (Tortora et al. 2009). This rapid quenching is still apparent but at a lower likelihood across the smooth and disc populations in higher mass galaxies, which have larger potentials, making it more difficult for the AGN to have an impact on the galaxy wide SFR (Ishibashi et al. 2012; Zinn et al. 2013).

We have used morphological classifications from the Galaxy Zoo 2 project to determine the morphology-dependent star formation histories of AGN host galaxies in comparison to a ‘typical’ inactive galaxy population via a Bayesian analysis of an exponentially declining star formation quenching model. We determined the most likely parameters for the quenching onset time,  $t_q$  and quenching timescale  $\tau$  and find clear differences in the combined population likelihoods between inactive and AGN host galaxies. We find evidence for a link between a galaxy currently hosting an AGN and its SFR. We find evidence of downsizing in massive inactive galaxies, which appears as a secondary effect in AGN host galaxies with the dominant quenching occurring at recent times. There is also evidence of negative feedback from AGN in lower mass galaxies from dominant rapid quenching tracks.

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