

There’s something about STARPIES

R. J. Smethurst,¹ C. J. Lintott,² et al.

¹ *School of Physics and Astronomy, The University of Nottingham, University Park, Nottingham, NG7 2RD, UK*

² *Oxford Astrophysics, Department of Physics, University of Oxford, Denys Wilkinson Building, Keble Road, Oxford, OX1 3RH, UK*

9 January 2018

ABSTRACT

We present STARPIES, an open source code written in *Python*, developed to infer a simple toy model of star formation history of a galaxy spectrum from the emission and absorption features. STARPIES utilises FSPS, the MaNGA DAP and *emcee* in order to provide the inferred $[Z, t_q, \tau]$ parameters with which to describe the exponentially declining quenching history of the input spectral features. This code was written for use on the MaNGA spectral data cubes but can be used for any scenario where a spectrum has been obtained, or spectral feature measurements have been provided.

Key words: software – description

1 INTRODUCTION

Whilst there are many codes which provide a full spectral fit to a galaxy spectrum in order to determine its SFH, there are few providing a simpler, quicker inference of a toy model of star formation history (SFH).

Here we present an open source *Python* software which can infer a simple toy model of SFH from the absorption and emission features of a galaxy (or IFU) spectrum.

We describe our SFH model (Section 2.1) and our code, STARPIES through generation (Section 2.2) and spectral fit of synthetic spectra (Section 2.3), using a Markov Chain Monte Carlo method (Section 2.5) and pruning methods (Section 2.6) outputs ‘best fit’ parameters to describe the SFH in Section 3. We also describe the rigorous testing procedures applied to STARPIES in Section 4.

2 DESCRIPTION OF CODE

2.1 Star Formation History Model

The SFH used in this code was first described in Smethurst et al. (2015). We have reproduced its description here. The quenched star formation history of a galaxy can be simply modelled as an exponentially declining star formation rate (SFR) across cosmic time as:

$$SFR = \begin{cases} I_{sfr}(t_q) & \text{if } t \leq t_q \\ I_{sfr}(t_q) \times \exp\left(\frac{-(t-t_q)}{\tau}\right) & \text{if } t > t_q \end{cases} \quad (1)$$

where t_q is the onset time of quenching, τ is the timescale over which the quenching occurs and I_{sfr} is an initial constant star formation rate dependent on t_q . A smaller τ value corresponds to a rapid quench, whereas a larger τ value corresponds to a slower quench. This model is clearly not a

fully hydrodynamical simulation, it is a deliberately simple model built in order to test our understanding of the evolution of galaxy populations. This SFH model has previously been shown to appropriately characterise quenching galaxies (Weiner et al. 2006; Martin et al. 2007; Noeske & et al. 2007; Schawinski et al. 2014). For galaxies which are still star forming, this model results in a constant SFR.

Here, I assume that all galaxies formed at a time $t = 0$ Gyr with an initial burst of star formation, $I_{sfr}(t_q)$. This initial constant star formation rate must be defined in order to ensure the ‘model’ galaxy has a reasonable stellar mass by $z \sim 0$. This value will be dependent on the epoch at which quenching is modelled to occur, hence the dependence of this initial star formation rate on quenching time in Equation 1. To tackle this problem, I looked to the literature; Peng & et al. (2010, Equation 1) define a relation between the average specific SFR ($sSFR = SFR/M_*$) and redshift by fitting to measurements of the mean $sSFR$ of blue star forming galaxies from SDSS, zCOSMOS and literature values from Elbaz et al. (2007) and Daddi et al. (2007) measured at increasing redshifts with data from the GOODS survey:

$$sSFR(m, t) = 2.5 \left(\frac{m}{10^{10} M_\odot} \right)^{-0.1} \left(\frac{t}{3.5 \text{ Gyr}} \right)^{-2.2} \text{ Gyr}^{-1}. \quad (2)$$

Beyond $z \sim 2$ the characteristic SFR flattens and is roughly constant back to $z \sim 6$. This flattening can be seen across similar observational data (Peng & et al. 2010; González et al. 2010; Béthermin et al. 2012); the cause is poorly understood but may reflect a physical limit to the $sSFR$ of a galaxy.

Motivated by these observations, the relation defined in Peng & et al. (2010) is taken up to a cosmic time of $t = 3$ Gyr ($z \sim 2.3$) and prior to this the value of the $sSFR$ at $t = 3$ Gyr is used. At the point of quenching, t_q , the SFH

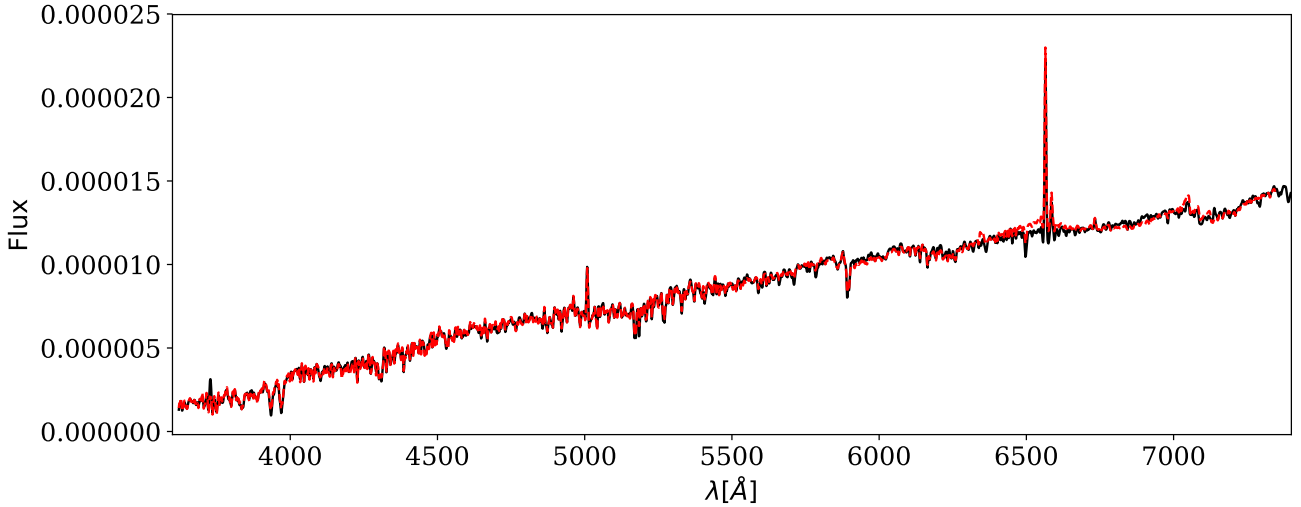


Figure 1. Example synthetic spectra constructed using FSPS, shown by the black solid line, along with the fit returned by the MaNGA DAP (i.e. ppxf, emission lines and absorption features) shown by the red dashed line.

models are therefore defined to have an $I_{sfr}(t_q)$ which lies on this relationship for the sSFR, for a galaxy with mass, $m = 10^{10.27} M_{\odot}$. This choice of $I_{sfr}(t_q)$ is an important one, however does not impact on the predicted spectral features output by the model as it is merely a normalisation factor on the SFH. $[t_q, \tau]$, which set the shape of the SFH, and Z which can affect the strength of a spectral feature are the crucial parameters.

2.2 Synthetic spectra generation

We then employ stellar population synthesis models (SPS) in order to construct synthetic spectra with known SFHs as defined in Section 2.1.

2.3 Measuring the synthetic spectral features

2.4 Choosing which spectral features to use

2.5 Markov Chain Monte Carlo Methods

2.6 Pruning

After running STARPIES and upon inspection of the walker positions it became apparent that the walkers of *emcee* would often get stuck in local minima. We therefore implemented a pruning method, as described in Hou et al. (2012), in order to remove those walkers in local minima leaving only the global minima from which to derive inferred SFH parameters. The method outlined in Hou et al. (2012) is a simple one dimensional clustering method wherein the average negative log-likelihood for each walker is collected. This results in L numbers:

$$\bar{l}_k = \frac{1}{T} \sum_{t=1}^T l(\vec{\theta}_k(t)|D), \quad (3)$$

where T is the total number of steps each walker, k , takes. These L numbers, \bar{l}_k are therefore characteristic of the well which walker k is in, so that walkers in the same well will

have similar \bar{l}_k (see Figure 3 in which walkers are coloured by their characteristic $\bar{l}_{(k)}$ value).

The walkers are all then ranked in order of decreasing average log likelihood, $\bar{l}_{(k)}$, or increasing $-\log \bar{l}_{(k)}$. If there are big jumps in the $-\log \bar{l}_{(k)}$, these are easy to spot and are indicative of areas where walkers have got stuck in local minima. The difference in $-\log \bar{l}_{(k)}$ for every adjacent pair of walkers is then calculated. The first pair whose difference is a certain amount times bigger than the average difference previously is then identified like so:

$$-\log \bar{l}_{(j+1)} + \log \bar{l}_{(j)} > Const \frac{\log \bar{l}_{(j)} + \log \bar{l}_{(1)}}{j-1}. \quad (4)$$

All the walkers with $k > j$ are thrown away and only the ones with $k \leq j$ are kept after being identified as part of the global minimum. This can be seen in Figure 4 wherein the walker positions at each step before pruning in the burn-in phase are shown in comparison to those after pruning in the main run stage.

3 OUTPUT OF CODE

4 TESTING

4.1 Testing precision

In order to test that STARPIES can find the correct quenched SFH model for a given set of spectral features, 25 synthesised galaxy spectra were created with known SFHs (i.e. known values of $\theta = [Z, t_q, \tau]$) from which spectral features were generated using the FSPS models (see Section 2.2. These were input into STARPIES to test whether the known values of θ were reproduced, within error, for each of the 25 synthesised galaxies. Figure 6 shows the results for each of these synthesised galaxies, with the known values of θ shown by the red lines. In only one case for the τ parameter this red line does not fall within the 16th and 84th percentile values shown by the blue dashed lines (see bottom right panel). However, on inspection, this SFH was a constant SFR that

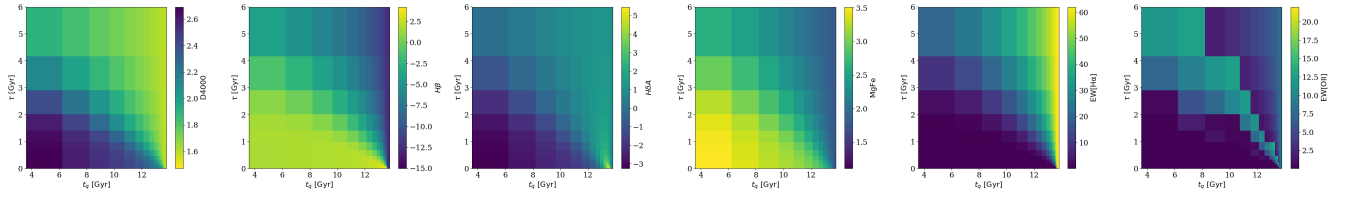


Figure 2. The variation of model spectral features across the logarithmically binned two dimensional $[t_q, \tau]$ parameter space measured at $t_{obs} = 13.6\text{Gyr}$ and solar metallicity, $Z = Z_\odot$. The features shown from left to right are the $D4000$, $H\beta$, $H\delta_A$ and $MgFe'$ spectral absorption indices and the equivalent width of both $H\alpha$ and $[OII]$ emission lines. This figure shows how each feature is sensitive to the changing SFH and how they can be used to break the degeneracies that plague photometric studies of SFH.

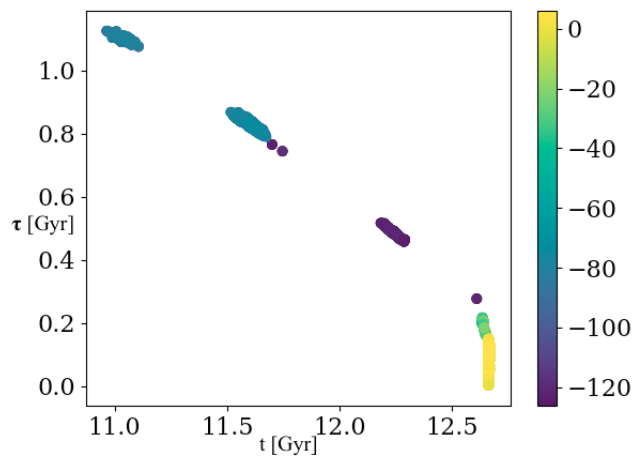


Figure 3. This figure shows the walker positions marginalized over the Z dimension into the two dimensional model $[t_q, \tau]$ space and coloured by their log probability value. The higher the value of their log probability, the more likely the model is. The lower values of log probability for some groups of walkers suggests that these are indeed stuck in local minima. These clusters of walkers in local minima can be ‘pruned’ (see Section 2.6) away to leave only the global minimum in the final output.

had not yet quenched and so the posterior probability function returned for the τ parameter is very broad as STARPIES does not have any information with which to constrain this parameter. In all cases the intersection of the red lines (i.e. the known or true values input) resides within the parameter space explored by the walkers left over after pruning, which trace the global minimum of the posterior probability. Therefore STARPIES succeeds in precisely locating the true parameter values within the degeneracies of the SFH model for known values.

4.2 Testing accuracy

We have shown in the previous section that STARPIES is precise in returning known values for SFHs, however how can we be sure that it is returning an accurate result?

4.3 Testing performance with different known SFHs

Obviously, not all galaxies will be accurately described by an exponentially quenching SFH. In special use cases (for

example studying post starburst galaxies) a different SFH may be defined by the user by replacing the `expsfh` function with their own.

However, we have also tested how STARPIES behaves when known SFHs of different shapes to the exponentially quenching model it assumes are input. We tested a constant, burst, many burst, normal and log-normal models of SFH (see Figure 7) all of which are often used in the literature to model simple SFHs.

We found that STARPIES was always sensitive to the most recent epoch of star formation or quenching. For the constant SFR model, STARPIES returned a very recent t_q and a very large τ , i.e. a galaxy which has had constant SFR up until very recently at which point it started to decline very slowly. For the burst and many-burst models, STARPIES returns a constant SFR up until the peak of the last burst at which point quenching happens very rapidly. Similarly for the log normal and normal SFHs, STARPIES returns a best fit SFH with constant SFR until the peak of the normal and which point it declines at a rate comparable to the drop off of the Gaussian SFH.

4.4 Testing against previously derived SFHs

5 CONCLUSIONS

REFERENCES

- B  thermin M., Daddi E., Magdis G., Sargent M. T., Hezaveh Y., Elbaz D., Le Borgne D., Mullaney J., Pannella M., Buat V., Charmandaris V., Lagache G., Scott D., 2012, *ApJ*, 757, L23
- Daddi E., Dickinson M., Morrison G., Chary R., Cimatti A., Elbaz D., Frayer D., Renzini A., Pope A., Alexander D. M., Bauer F. E., Gialalisco M., Huynh M., Kurk J., Mignoli M., 2007, *ApJ*, 670, 156
- Elbaz D., Daddi E., Le Borgne D., Dickinson M., Alexander D. M., Chary R.-R., Starck J.-L., Brandt W. N., Kitzbichler M., MacDonald E., Nonino M., Popesso P., Stern D., Vanzella E., 2007, *A&A*, 468, 33
- Gonz  lez V., Labb   I., Bouwens R. J., Illingworth G., Franx M., Kriek M., Brammer G. B., 2010, *ApJ*, 713, 115
- Hou F., Goodman J., Hogg D. W., Weare J., Schwab C., 2012, *ApJ*, 745, 198
- Martin D. C., Wyder T. K., Schiminovich D., Barlow T. A., Forster K., Friedman P. G., Morrissey P., Neff S. G., Seibert M., Small T., Welsh B. Y., Bianchi L., Donas J., Heckman T. M., Lee Y.-W., Madore B. F., Milliard B., Rich R. M., Szalay A. S., Yi S. K., 2007, *ApJS*, 173, 342

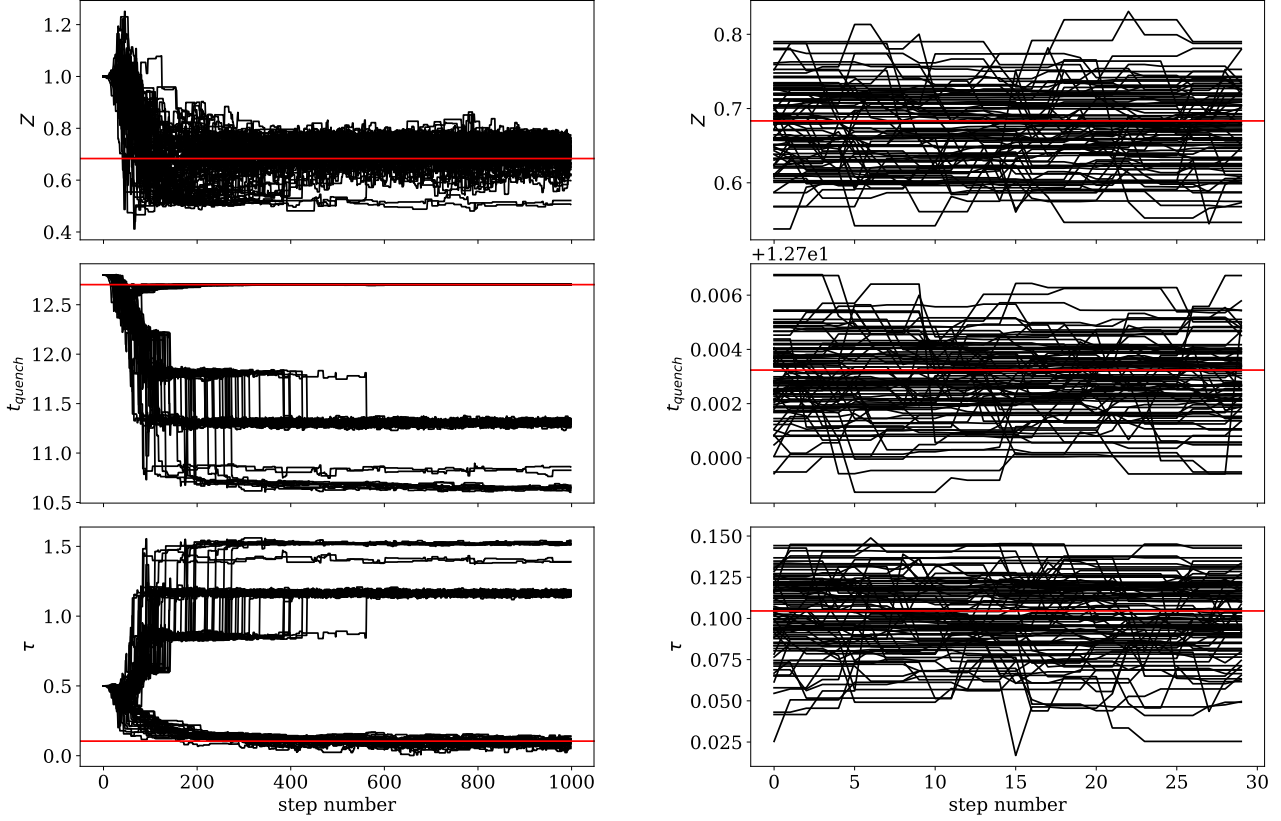


Figure 4. The positions traced by the *emcee* walkers with step number (i.e. time) in each of the $[Z, t_q, \tau]$ dimensions during the burn in phase before pruning (left) and the post burn-in phase after pruning (right). The red lines show the known true values in each panel. Walkers have got stuck in local minima (see Figure3) but some have managed to find the global minimum which can be seen more clearly in the right hand panels.

Noeske K. G., et al. 2007, *ApJ*, 660, L43
 Peng Y.-j., et al. 2010, *ApJ*, 721, 193
 Schawinski K., Urry C. M., Simmons B. D., Fortson L., Kaviraj S., Keel W. C., Lintott C. J., Masters K. L., Nichol R. C., Sarzi M., Skibba R., Treister E., Willett K. W., Wong O. I., Yi S. K., 2014, *MNRAS*, 440, 889
 Smethurst R. J., Lintott C. J., Simmons B. D., Schawinski K., Marshall P. J., Bamford S., Fortson L., Kaviraj S., Masters K. L., Melvin T., Nichol R. C., Skibba R. A., Willett K. W., 2015, *MNRAS*, 450, 435
 Weiner B. J., Willmer C. N. A., Faber S. M., Harker J., Kassin S. A., Phillips A. C., Melbourne J., Metevier A. J., Vogt N. P., Koo D. C., 2006, *ApJ*, 653, 1049

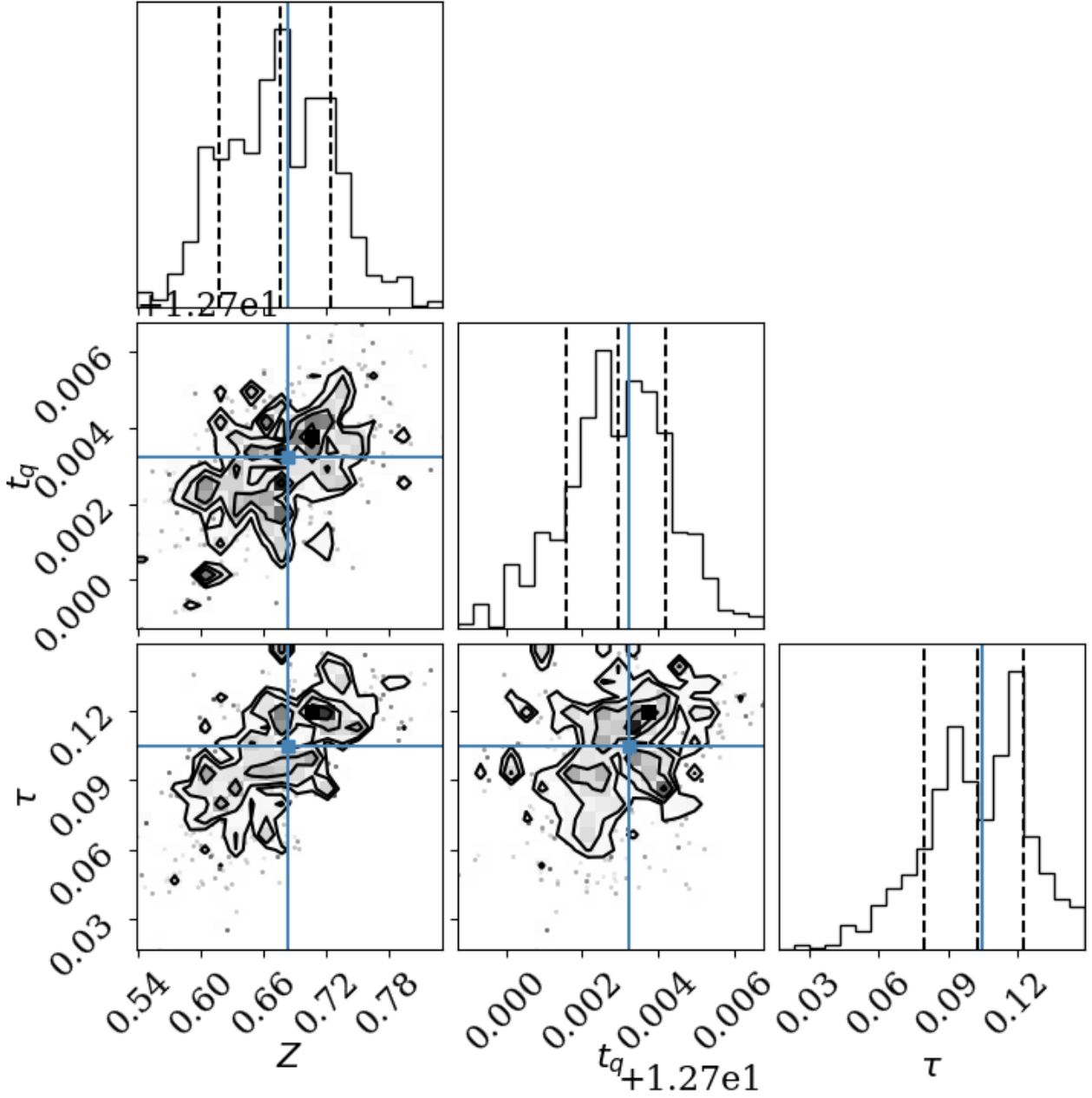


Figure 5. Example output from STARPIES showing the posterior probability function traced by the MCMC walkers across the three dimensional parameter space $[Z, t_q, \tau]$. Dashed lines show the 18th, 50th and 64th percentile of each distribution function which can be interpreted as the ‘best fit’ with 1σ . The blue lines show the known true values which STARPIES has managed to recover.

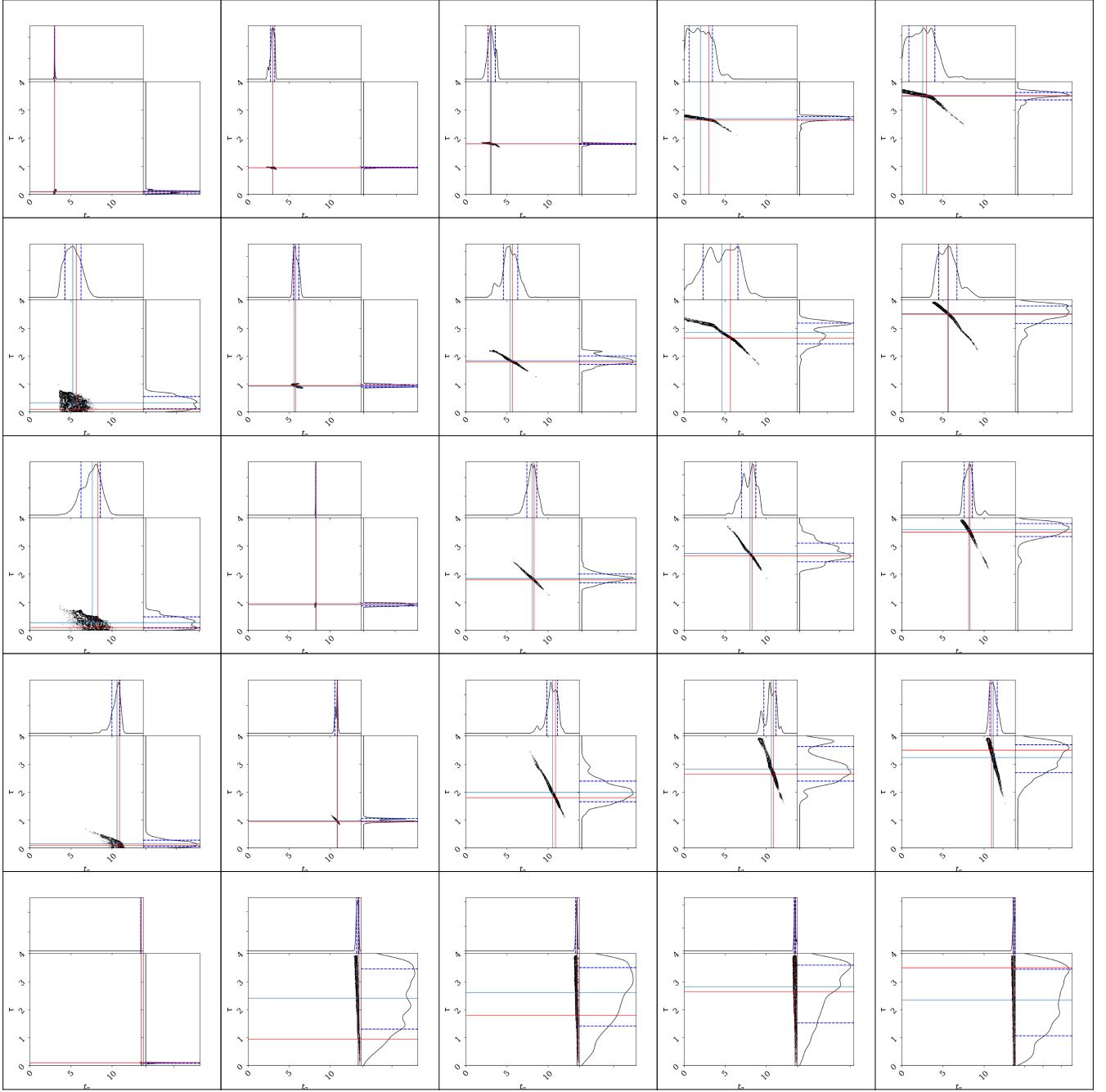


Figure 6. Results from STARPIES for an array of synthesised galaxies with known true $[Z, t_q, \tau]$ values (marked by the solid red lines) assuming an error on the input spectral measurements of the average error on the measured MaNGA spectra measurements. **Pruning has been applied?** In each case STARPIES has succeeded in locating the true parameter values within the degeneracies of the star formation history model.

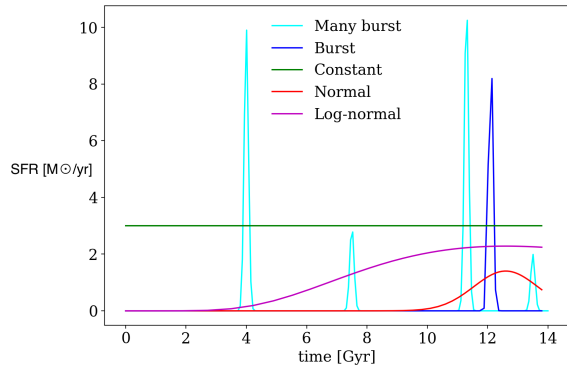


Figure 7. The shapes of the different known SFHs input into STARPIES.