

Number System

Types of numbers

Real

Rational (Non-Terminating & repeating) $\frac{p}{q} \neq 0$

Irrational (Non Terminating & non repeating)
($\pi, \sqrt{2}, \sqrt{3}$)

Co-Prime numbers - Set of two numbers having HCF = 1
Ex - (2, 3), (5, 7), etc.

Perfect number -

Ex. $6 = 1, 2, 3, 6$

Adding factor sum $= 1 + 2 + 3 = 6$

Ex - $21.2\bar{5}$

Sol $\frac{2125 - 212}{90}$

Ex - $1.2555\ldots = 1.2\bar{5} = \frac{125 - 12}{90} = \frac{113}{90}$

$$1.2\bar{56} = \frac{1256 - 12}{990} = \frac{1244}{990} = \frac{622}{495}$$

$$1.256256\ldots = 1.\overline{256} = \frac{1256 - 1}{999} = \frac{1255}{999}$$

$$0.2333\ldots = 0.\bar{23} = \frac{23 - 2}{90} = \frac{21}{90} = \frac{7}{30}$$

Divisibility rule

for 7 -

$$79(8)_{\times 2}$$

$$\begin{array}{r} 79 \\ -16 \\ \hline 63 \end{array}$$

11 \rightarrow (Sum - Sum
odd posi. even posi.) \rightarrow It should be 0 or 11

$$10593$$

$$9-9=0$$

• $88 - 11 \times 8$

• $12 - 4 \times 3$

\rightarrow Remainder theorem

$$\text{Dividend} = (\text{Divisor} \times \text{Quotient}) + \text{remainder}$$

$$\begin{array}{r} \text{Divisor} - 6 \quad \begin{array}{r} 4 - \text{Quotient} \\ \overline{) 25} \rightarrow \text{dividend} \\ 24 \\ \hline 1 \rightarrow \text{remainder} \end{array} \end{array}$$

{ remainder < Divisor }

$$= (5x \times x) + 3x$$

$$= 25 \times 5 + 3 \times 5$$

$$= 125 + 15$$

$$= 140$$

$$\begin{aligned} 8x &= 15 \\ x &= 5 \end{aligned}$$

• Remainder of -

$$\frac{123 \times 120}{11} = 2 \times 10 = \frac{20}{11} = 9$$

Q. What is the remainder when 3^7 is divided by 8?

• Negative Remainder

$$\overset{+2}{123} \times \overset{-1}{120} = -2 = 11 - 2 = 9$$

Factors - The values that divides the no. completely

$$i) N = 2^a \times 3^b \times 7^d = (a+1)(b+1)(d+1) \quad \left. \vphantom{N} \right\} \text{No. of Factors}$$

$$\begin{aligned} 300 &= 2^2 \times 3^1 \times 5^2 \\ &= (2+1)(1+1)(2+1) \\ &= 3 \times 2 \times 3 \\ &= 18 \end{aligned}$$

$$\begin{array}{r|l} 2 & 300 \\ \hline 2 & 150 \\ \hline 3 & 75 \\ \hline 5 & 25 \\ \hline 5 & 5 \\ \hline & 1 \end{array}$$

$$ii) \text{ Odd No. of factors} = (b+1)(d+1)$$

$$iii) \text{ Even No. of factors} = 2a(b+1)(d+1)$$

$$iv) \text{ Sum of all the factors} =$$

$$300 = (2^0 + 2^1 + 2^2)(3^0 + 3^1)(5^0 + 5^1 + 5^2)$$

$$= (1+2+4)(1+3)(1+5+25)$$

$$= 7 \times 4 \times 31$$

$$a^0 + a^1 + a^2 + \dots + a^n = \frac{a^{n+1} - 1}{a - 1} = \left(\frac{2^{a+1} - 1}{2 - 1} \right)$$

$$v) \text{ Product of the factors} = (N)^{\frac{\text{Total no. of factors} - 1}{2}}$$

$$(300)^{18/2} = (300)^9$$

• Perfect Square -

$$N = 2^5 \times 3^6 \times 5^3$$

$$(2^0, 2^2, 2^4) (3^0, 3^2, 3^4, 3^6) (5^0, 5^2)$$

$$3 \times 4 \times 2 = 24$$

• Perfect Cube - $(2^0, 2^3) (3^0, 3^3, 3^6) (5^0, 5^3)$

$$2 \times 3 \times 2 = 12$$

Note -

$$36 = 3^2 \times 2^2 = 9$$

$$(36)^{9/2} = (36)^{8/2} \times \sqrt{36}$$

Multiples -

$$30 = 2^1 \times 3^1 \times 5^1$$

$$\underline{\underline{Q.}} \quad \frac{(17)^{20}}{9} = \frac{(8)^{20}}{9} = \frac{(-1)^{20}}{9} = 1$$

$$\begin{array}{r} 9 \overline{) 17} \\ -18 \\ \hline -1 \end{array}$$

$$\underline{\underline{Q.}} \quad \frac{44 \times 43 \times 46 \times 47}{9} = \frac{-1 \times -2 \times 1 \times 2}{9} = 4$$

$$\underline{\underline{Q.}} \quad \frac{2^{30}}{7} = \frac{(2^3)^{10}}{7} = \frac{8^{10}}{7} = 1$$

$$\underline{\underline{Q.}} \quad \frac{3^{80}}{80} = \frac{(3^4)^{20}}{80} = \frac{(81)^{20}}{80} = \frac{(1)^{20}}{80} = 1$$

Unit digits - Right most digit of a no. is called Unit digit.

1 Simple Product type

2 Power Type

$$\text{Ex - } 278 \times 623$$

24 → Unit digit

$$\begin{array}{r} 6 \\ 49 \\ 27 \\ \hline 343 \end{array}$$

$$(127)^{23} \rightarrow (127)^{12\frac{3}{4}} \rightarrow (+3) \rightarrow \text{Remainder}$$

$$7^3 \rightarrow 343$$

Cyclicity No.

$$[4, 9] \rightarrow 2$$

$$\begin{array}{ll} u^1 \rightarrow 4 & q^1 \rightarrow 9 \\ u^2 \rightarrow 16 & q^2 \rightarrow 81 \\ u^3 \rightarrow 64 & q^3 \rightarrow 729 \\ u^4 \rightarrow 256 & \end{array}$$

$$[2, 3, 7, 8] \rightarrow 4$$

$$\begin{array}{l} 2^1 \rightarrow 2 \\ 2^2 \rightarrow 4 \\ 2^3 \rightarrow 8 \\ 2^4 \rightarrow 16 \\ 2^5 \rightarrow 32 \\ 2^6 \rightarrow 64 \\ 2^7 \rightarrow 128 \\ 2^8 \rightarrow 256 \end{array}$$

$$2^9 \rightarrow 2^{9/4} \xrightarrow{+1 \rightarrow \text{Rem.}} 2^1 \rightarrow 2$$

Cyclicity of ~~2~~ 4 is applicable in every scenario.

Ex

$$(2354)^{1048} \rightarrow$$

$$(248)^{1587} \rightarrow (248)^{\frac{1587}{4} \rightarrow 39} \rightarrow (8)^3 \rightarrow 8^2 \times 8^1$$

$$(456)^{87} \times (307)^{42}$$

$$6 \times (307)^{\frac{42}{4}} \rightarrow 6 \times 7^2 \times 49 \rightarrow 59 \rightarrow \text{Unit digit}$$

$$3 \rightarrow \text{Unit digit} \quad \frac{42}{4} + 2$$

$$\begin{array}{r} 38 \\ 32 \\ \hline 57 \\ 4 \\ \hline 17 \\ 16 \\ \hline 1 \end{array}$$

$$= 2^4 \times 3^2 \times 5^2$$

$$= 5 \times 3 \times 3$$

$$= 45$$

$$\begin{aligned} 3600 &= 36 \times 100 \\ &\quad \swarrow \quad \searrow \\ &2^2 \times 3^2 \times 2^2 \times 5^2 \\ &= 2^4 \times 3^2 \times 5^2 \\ &= 5 \times 3 \times 3 \\ &= 45 \end{aligned}$$

$$\begin{aligned} 330 &= 33 \times 10 \\ &\quad \swarrow \quad \searrow \\ &3 \times 11 \times 2 \times 5 \\ &= 2 \times 2 \times 2 \times 2 \\ &= 16 \end{aligned}$$

$$\begin{aligned} &= (2^0 \times 2^1 \times 2^2 \times 2^3) (3^0 \times 3^1 \times 3^2) (5^0 \times 5^1 \times 5^2) \\ &= (1 \times 2 \times 4 \times 8) (1 \times 3 \times 9) (1 \times 5 \times 25) \\ &= \end{aligned}$$

$$3600 = \frac{2^5-1}{2-1} \times \frac{3^3-1}{3-1} \times \frac{5^3-1}{5-1}$$

$$= \frac{32-1}{1} \times \frac{26}{2} \times \frac{124}{4}$$

$$= 31 \times 13 \times 31$$

$$= 12493$$

$$\begin{aligned} (3600)^{45/2} &= (3600)^{22} \times \sqrt{3600} \\ &= (3600)^{22} \times (3600)^{1/2} \\ &= \times 60 \end{aligned}$$

$$\begin{array}{r} 2 \overline{) 3600} \\ 2 \overline{) 1800} \\ 2 \overline{) 900} \\ 2 \overline{) 450} \\ 3 \overline{) 225} \\ 3 \overline{) 75} \\ 5 \overline{) 25} \\ 5 \overline{) 5} \\ 1 \end{array}$$

$$\begin{array}{r} 15 \\ \times 2 \\ \hline 30 \end{array}$$

$$\begin{array}{r} 8 \\ 3 \overline{) 24} \\ 3 \overline{) 75} \\ 2 \overline{) 436} \\ 2 \overline{) 872} \\ 4 \overline{) 436} \\ 5 \overline{) 436} \\ 4 \overline{) 436} \\ 10 \end{array}$$

$$\begin{array}{r} 3 \overline{) 330} \\ 2 \overline{) 160} \end{array}$$

$$\begin{array}{r} 31 \\ \times 31 \\ \hline 31 \\ 93 \\ \hline 961 \\ \times 13 \\ \hline 2883 \\ 961 \\ \hline 12493 \end{array}$$

even factor =

• Trail
→ zer
an

Q.
sol

$$\begin{aligned} \text{even factor} &= 4 \times 3 \times 3 \\ &= 4 \times 9 \\ &= 36 \end{aligned}$$

$$\begin{aligned} &= 2 \times 2 \times 5 \times 17 \\ &= 2^2 \times 5 \times 17 \\ &= 2 \times 2 \times 2 \\ &= 8 \end{aligned}$$

$$\begin{array}{r} 2 \overline{) 340} \\ \underline{17} \\ 17 \\ \underline{17} \\ 0 \end{array}$$

• Trailing Zeros (Number of zeros at the end)
 → zero can be produced when we have a pair of 2 and 5.

201!

$$\begin{array}{r} 5 \overline{) 201} \\ \underline{5} \\ 5 \\ \underline{5} \\ 1 \end{array} \rightarrow 4 \text{ zeros}$$

$$\begin{array}{r} 5 \overline{) 20} \\ \underline{5} \\ 5 \\ \underline{5} \\ 0 \end{array} \rightarrow 4 \text{ zeros}$$

$$\begin{array}{r} 5 \overline{) 100} \\ \underline{5} \\ 5 \\ \underline{5} \\ 0 \end{array} \rightarrow 24 \text{ zeros}$$

$$\begin{array}{r} 5 \overline{) 56} \\ \underline{5} \\ 1 \\ \underline{2} \\ 0 \end{array} \rightarrow 13 \text{ zeros}$$

$$\begin{array}{r} 50000 \\ \underline{5} \\ 0 \end{array}$$

Q. $100! + 200!$

Sol. 24 zeros

Ex -
$$\begin{array}{r} 157210 \\ \underline{20400} \\ 610 \end{array}$$

• LCM and HCF

LCM (Least Common Multiple)

$$\begin{aligned} \text{LCM} &= 2^3 \times 3^2 \times 5 \\ &= 8 \times 9 \times 5 \\ &= 360 \end{aligned}$$

$$\text{LCM} = 80$$

$$\begin{array}{r|rrrr} 8 & 8, 16, 40, 80 \\ 2 & 1, 2, 5, 10 \\ 5 & 1, 1, 5, 5 \\ \hline & 1, 1, 5, 1 \end{array}$$

$$\begin{array}{r|rrrr} 2 & 24, 36, 40 \\ 2 & 12, 18, 20 \\ 2 & 6, 9, 10 \\ 3 & 3, 9, 5 \\ 3 & 1, 3, 5 \\ 5 & 1, 5, 5 \\ \hline & 1, 1, 1 \end{array}$$

HCF (Highest Common factor)

360

$$\begin{aligned} &700 \\ &385 \\ &1285 \end{aligned}$$

Q. Four bells ring at an interval 3min, 4min, 5min and 6min. respectively. If all the four bells ring at 9am first, when will it ring again?

Sol

$$\begin{array}{r|rrrr} 2 & 3, 4, 5, 6 \\ 2 & 3, 2, 5, 3 \\ 3 & 3, 1, 5, 3 \\ 5 & 1, 1, 5, 1 \\ \hline & 1, 1, 1, 1 \end{array}$$

$$\begin{aligned} &= 2^2 \times 3 \times 5 \\ &= 60 \text{ min} \end{aligned}$$

Q. HCF of $9/10, 12/25, 18/35$ and $21/40$ is?

Sol

$$\begin{array}{l} \text{HCF} \rightarrow \frac{4}{10} \quad \frac{12}{25} \quad \frac{18}{35} \quad \frac{21}{40} = \frac{3}{1400} \\ \text{LCM} \rightarrow \end{array}$$

Q. of LCM of $\frac{4}{10} \quad \frac{12}{25} \quad \frac{18}{35} \quad \frac{21}{40}$?

$$\begin{array}{l} \text{LCM} \rightarrow \frac{4}{10} \quad \frac{12}{25} \quad \frac{18}{35} \quad \frac{21}{40} = \\ \text{HCF} \rightarrow \end{array}$$

Q. Ratio of two numbers is $3:4$ and their H.C.F is 4 .
Their L.C.M is

Sol

$$\begin{array}{l} 3x \times 4x = 4 \times \text{LCM} \\ 12x = 4 \times \text{LCM} \\ \quad \quad \quad \div 4 \end{array}$$

$$3 \times 4 = 12$$

$$4 \times 4 = 16$$

$$\text{LCM} = 48$$

Q. The least no., which divided by 12, 15, 20 & 54 leaves in each case a remainder of 8 is:

Sol

$$\text{LCM of } 12, 15, 20 \& 54$$

$$\text{LCM} = 540$$

$$\begin{array}{r} 540 \\ + 8 \\ \hline 548 \text{ Ans} \end{array}$$

Q. Find the smallest no., which when divided by 3, 4 & 5 leaves remainders 1, 2 and 3 respectively?

Sol

$$\text{LCM} = 60$$

$$\text{Divisor } 3 \quad 4 \quad 5 \rightarrow 60$$

$$\begin{array}{r} \text{Remainder } 1 \quad 2 \quad 3 \\ \hline 2 \quad 2 \quad 2 \end{array}$$

$$\begin{array}{r} 60 \\ - 2 \\ \hline 58 \text{ Ans} \end{array}$$

Q. The greatest no. which on dividing 1657 and 2037 leaves remainders 6 and 5 respectively, is:

Sol

$$\begin{array}{r} 1657 \\ - 6 \\ \hline 1651 \end{array}$$

$$\begin{array}{r} 2037 \\ - 5 \\ \hline 2032 \end{array}$$

HCF of 1651 & 2032 is 127 Ans

Q. Find the greatest no. which on dividing divide 43, 91 and 183 so as to leave the same remainder in each case.

Sol

$$\begin{array}{r} 48 \quad 92 \\ \underbrace{43, 91 \text{ and } 183} \\ 140 \end{array}$$

HCF of 48 92 140 is 4 // Ans
~~140~~

• Arithmetic Progression

$$a_n = a + (n-1)d$$

Q. 1, 3, 5, 7, ... which term of this AP is 55?

$$a_{55} = 1 + (55-1)2$$

$$55 = 1 + 108(n-1)2$$

$$54 = 216(n-1)$$

$$54 = 216(n-1)$$

$$n-1 = \frac{54}{216}$$

$$n-1 = 27$$

$$n = 28$$

Q. Find 5th term of Series 20, 15, 10, ---

$$a_5 = 20 + (5-1) \times (-5)$$

$$= 20 + 4 \times (-5)$$

$$= 20 - 20 = 0$$

• Average

$$\text{Averages} = \frac{\text{Sum of Observation}}{\text{No. of Observation}}$$

Q. 80. 85 90 95 100

$$\frac{80+100}{2} = \frac{180}{2} = 90$$

Q. 75 80 85 90 95 100 (Middle term)

$$S/2 = 2.5$$

$$85 + 2.5 = 87.5$$

$$90 - 2.5 = 87.5$$

Formulae

Numbers

$$\text{Sum} = \frac{n(n+1)}{2}$$

$$\text{Average} = \frac{\text{Sum}}{n} = \frac{(n+1)}{2}$$

First n natural no.

First n odd no.

$$n^2$$

$$n$$

First n even no.

$$n(n+1)$$

$$(n+1)$$

First n natural no.

$$\frac{n(n+1)(2n+1)}{6}$$

$$\frac{(n+1)(2n+1)}{6}$$

Consecutive no.

Or Numbers in A.P

$$\frac{n(\text{First term} + \text{Last term})}{2}$$

$$\frac{(\text{First term} + \text{Last term})}{2}$$

Q. The the

- i.) 22
- ii.) 23
- iii.) 24
- iv.) 25

• Average

• Average

Q. The

Sum
Ass.

Actual

Q. The average of 5 consecutive numbers is 21. Find the largest number.

- i.) 22
- ii.) 23
- iii.) 24
- iv.) 25

19 20 21 22 23

• Average of 100 ^{whole} ~~natural~~ no.
0, 1, 2, ..., 99

$$\frac{99}{2} = 49.5$$

• Average of 100 even no.

2, 4, ..., 200

$$\frac{22}{2} = 11$$

Q. The average of first 17 multiples of 5?

5, 10, 15, ..., 85

$$\frac{90}{2} = 45$$

Sum → 0 20 19 17 23 25
 -1 -3 +3 +5 → 4

Ass. Avg → 20

$$\frac{4}{5} = 0.8$$

Actual Avg → $20 + 0.8 = 20.8$

Combined Average

	No	x Avg	= Sum
Gr I	30	80	= 2400
Gr II	20	50	= 1000
	<u>50</u>		<u>3400</u>
			50
			= 68

Q. A $\begin{array}{r} 36 \\ 24 \\ \hline 60 \end{array}$ B $\begin{array}{r} 30 \\ 40 \\ \hline 70 \end{array}$

Q The average of marks obtained by 120 Candidates was 35. If the average of passed Candidate was 39, and that of failed Candidate was 15, the no. of Candidates who passed the examination is?

Sol

α	30				
15	No	x	Avg	= Sum	
			35	= 4200	
Overall	120		30	= 39x	
Pass	x		(120-x)	= 15(120-x)	
fail	fail		15		
	(120-x)				

Q. A man goes from home to his office at Speed = of 40 km/h and return from office to home at a Speed of 60 km/h. Find the Average Speed during whole journey.

Sol

$$\frac{2xy}{x+y} = \frac{2 \times 40 \times 60}{40+60} = \frac{2 \times 2400}{100} = \frac{4800}{100} = 48$$

• Equal Distribution of Data

Q. If the avg. weight of 10 Students in a Class is 30 kg, when weight of teacher is also included new average becomes 33. Find weight of teacher.

No	x	Avg	= Sum
10		30	= 300
		33	<u>363</u>
			63

$\frac{33-30}{33} = \frac{3}{33} = \frac{1}{11}$

Q. The avg. weight of a Class of 24 students is 30 kg when weight of the Teacher is also included the average weight is increases by 1 kg. what is the weight of teacher in kg

No	Avg	Sum
24	30	720
25	31	<u>775</u>
		55

Q. What is the remainder when 3^7 is divided by 8?

Sol $\frac{3^7}{8} = \frac{(3^2)^3 \times 3^1}{8} = \frac{9^3 \times 3}{8}$
 $= \frac{(+1)^3 \times 3}{8} = \frac{3}{8} \rightarrow \text{Divisor} > \text{Rem.}$
 $= 3$

Q. $\frac{3^7}{10} = \frac{(3^2)^3 \times 3^1}{10} = \frac{(-1)^3 \times 3}{10}$
 $= \frac{-3}{10}$
 $= 10 - 3$
 $= 7$

Q. $\frac{3^{10}}{10} = \frac{(3^2)^5}{10} = \frac{(-1)^5}{10} = \frac{-1}{10}$
 $= 10 - 1 = 9$

Q. $\frac{3^{13}}{9} =$

Q. $\frac{2^{33}}{9} = \frac{2^{32} \times 2}{9} = \frac{(2^3)^{16} \times 2}{9}$
 $= \frac{(8)^{16}}{9} = \frac{(8)^{10} \times 8}{9}$
 $= \frac{(-1)^{10} \times 8}{9} = \frac{-8}{9}$
 $= -8 + 9 = 1$

by

$$\begin{aligned} \text{Q. } \frac{2^{34}}{9} &= \frac{(2^3)^{11} \times 2^1}{9} = \frac{-1 \times 2}{9} = \frac{-2}{9} \\ &= 9 - 2 = 7 \end{aligned}$$

$$\begin{aligned} \text{Q. } \frac{2^{99}}{10} &= \frac{2^{98} \times 2}{10} = 8 \frac{(2^3)^{33}}{10} \\ &= \frac{(8)^{33}}{10} = \frac{(-2)^{33}}{10} = \frac{(-2^3)^{11}}{10} \\ &= \frac{2^{99}}{2 \times 5} = \frac{2^{98}}{5} = \frac{(2^2)^{49}}{5} \\ &= \frac{(4)^{49}}{5} = (-1)^{49} = -1 + 5 = 4 \end{aligned}$$

But

$$4 \times 2 = 8 \text{ Ans (Because } \frac{2^{98} \times 2}{5 \times 2}$$

Q. The average weight of 8 person increase by 2.5 kg when a new person comes in place of one of them weighting 65 kg. what might be the weight of the new person?

Sol

No.	Avg	Sum
8	+2.5	+20
		65
		<u>85</u>

Q. A teacher while calculating the avg. marks of 30 students of an examination by mistake enters a student's marks as 68, instead of 86 and obtained the average as 58. Find the actual average.

Sol

No	Avg.	Sum	Wrong	Correct
30	58 + A	+ 18	68	86

$30 \times (A + 18)$
 $A = \frac{18}{30}$
 $= 0.6$

Actual average = $58 + 0.6$
 $= 58.6$

Q. A student's marks were wrongly entered as 83 instead of 63. Due to that the average marks of the class got ~~decreased~~ ^{increased} by 2. The no. of students in class is?

Sol

No	Avg	Sum
N.	2	20

$= \frac{20}{2}$
 $= 10$

Q.

No.	Avg	Sum
12	Avg	36

$$= \frac{36}{12}$$

$$= 3$$

Q. The average of a family is 24 yrs which is consisting of 5 members, out of which the youngest being 6 yrs old. What would be the avg. age of family just before his birth?

Sol

No.	Avg	Sum
5	24	120
4		$\frac{-30}{90} = 22.5$
		$\frac{4}{4}$

Q. The average age of 10 members in a Committee is increased by 3 yrs when two men whose age are 25 yrs and 35 yrs are replaced by two new men. Find the average age of two new men.

10	+3	$\frac{+30}{60}$
		$\frac{90}{2} = 45$

Q. If the average weight of 10 students in a class is 30 kg, when weight of teacher is also included new average becomes 33. Find weight of teacher.

No	Avg	Sum
10	30	300
11	33	363
		<u>63 kg</u>

Q. The avg. marks of some students is 40 and 10 of them get 60 marks instead of 40 marks by mistake. After Correction, the new average becomes 50. Find no. of students.

Sol

No	Avg	Sum
40 x	40	40x
10	+30	+300

x 50

$$50x = 40x + 300$$

$$10x = 300$$

$$x = 30$$

Q. ~~The avg.~~ In a hostel there are 30 students and if the no. of students increased by 5 then the expense is increased by 40 per day. But the average expenditure diminishes by 3. Find the original expenditure.

Sol

No	Avg	Sum
30	x	$30x$
35	$x-3$	$30x+40$

$$35x - 105 = 30x + 40$$

$$x = 29$$

$$30 \times 29 = 870$$

Q. A batsman has a certain average of runs for 16 innings. In the 17th inning, he makes a score of 85 runs there by increasing the average by 3. What is the avg. of 17 innings?

Sol

No	Avg	Sum
16	A	$16A$
17	$A+3$	$16A+85$

$$17(A+3) = 16A + 85$$

$$A = 34$$

17th inning

$$= A + 3$$

$$= 34 + 3 = 37$$

Q. If a batsman score 36 runs in his 18th innings so that his average is reduced by 3 run. Find the average of batsman upto 18th inning.

No	Avg	Sum
17	A	17A
18	A-3	17A+36

$$18A - 54 = 17A + 36$$

$$A = 90$$

$$A - 3 = 90 - 3$$

$$= 87$$

Q. A baller whose balling Average is 12.4 runs/wicket. He played his next match and takes 5 wickets for 26 runs; therefore his average is reduced by 0.4. Find the total no. of wickets taken by the baller.

Sol

No	Avg	Sum
x	12.4	12.4x
x+5	12.4-0.4 = 12	12x+60 12.4x+26

$$12x + 60 = 12.4x + 26$$

$$0.4x = 34$$

$$x = \frac{340}{0.4}$$

$$= 85$$

$$x + 5 = 85 + 5 = 90$$

Q. The average temp. in Delhi for the first four days of the month was reported as 58°C . It reported as 60°C for 2nd, 3rd, 4th and 5th days. The ratio of the temperature of 1st and 5th day was 7:8. Find the temperature on the first day.

No	Avg	Sum
1, 2, 3, 4	58	232
2, 3, 4, 5	60	240
1, 5		$\frac{240 - 232}{4} = 8^{\circ}\text{C}$

$7:8$
 $7 \rightarrow 8 \times 7 = 56$
 $8 \rightarrow 64^{\circ}\text{C}$

• If $\frac{3}{2} \rightarrow 8^{\circ}\text{C}$
 $3 \rightarrow \frac{8}{2} \times 3 = 12^{\circ}\text{C}$
 $5 \rightarrow \frac{8}{2} \times 5 = 20^{\circ}\text{C}$

Q. 6 friends went to a hostel for taking their lunch. 5 of them spend Rs 32 each while the 6th person spend 80 more than the average expenditure of all the 6 person. Find the total money spend on lunch.

No	Avg	Sum
5	32	160
6	A	$160 + 80 = 240 + A$

$$\begin{aligned}
 6A &= 160 + A + 80 \\
 5A &= 240 \\
 A &= 48 \\
 6 \times A &= 48 \times 6 = 288
 \end{aligned}$$

• Digit Sum

1.

$$\begin{array}{rcl}
 58 & \times & 96 & \times & 62 \\
 \downarrow & & \downarrow & & \downarrow \\
 13 & & 15 & & 8 \\
 \downarrow & & \downarrow & & \\
 4 & & 6 & & \\
 & \swarrow & & \searrow & \\
 & 24 & & 48 & \\
 & \downarrow & & \downarrow & \\
 & 6 & & 12 & \\
 & & & \downarrow & \\
 & & & 3 &
 \end{array}$$

→ If Sum is 9 then ignore it.

a) ~~343248~~ ×

b) ~~345026~~

c) ~~348216~~ → 3

d) 345236

two options
 • If both give same answer than use unit digit rule.

$$\begin{array}{rcl}
 728 & \times & 456 & \times & 827 \\
 \downarrow & & \downarrow & & \downarrow \\
 17 & & 15 & & 17 \\
 \downarrow & & \downarrow & & \downarrow \\
 8 & & 6 & & 8 \\
 & \swarrow & & \searrow & \\
 & 48 & & 24 & \\
 & \downarrow & & \downarrow & \\
 & 12 & & 6 & \\
 & \downarrow & & & \\
 & 3 & & &
 \end{array}$$

a) 274467536

b) 275537536

c) 274567536

d) ~~274537536~~ → 15
 6

4. $43751 + 25653 + 35433 + 2567 + 342 = ?$

a) 107546

b) 106646

c) 107846

d) 107746

$$\begin{array}{r} 20 + 21 + 20 \\ \sqrt{} \quad \sqrt{} \quad \sqrt{} \\ 2 \quad 3 \quad 2 \\ \hline 5 \quad 7 \end{array}$$

6. $12.25 \times 7.2 + 84.33 = ?$
 $1 \times 0 + 0 = 0$

a) 182.51

b) 177.44

c) 173.33

d) 172.53

7. $6205 \div 73 \times 13 - 376 = A^2$

$$\begin{array}{r} 13 \quad 10 \quad 4 \quad 7 \\ 6205 \div 73 \\ \underline{4} \quad \underline{16} \quad \underline{42} \\ 4 \quad 6 \quad 6 \end{array}$$

7. $6205 \div 73 \times 13 - 346 = A^2$

$$\begin{array}{r} 4 \quad 1 \quad 4 \quad 7 \\ \underline{} \quad \underline{} \quad \underline{} \quad \underline{} \\ 7 \quad 0 \rightarrow 9 \end{array}$$

a) 29

b) 28

c) $27 \rightarrow 9^2 \rightarrow 81 \rightarrow 9$

d) 26

8. $6205 \div 23 \times 13 - 376$

$$\frac{4}{5} \times 4 - 7$$

$$\frac{4 \times 2}{5 \times 2} \times 4 - 7$$

$$\frac{8}{10} \times 4 - 7 \Rightarrow -2 + 9 \Rightarrow +7$$

$$10. 113 \times 114 - 1127 \div 23 + 100 = ?$$

Sol

$$5 \times 6 - 11 \div 5 + 1$$

Handwritten calculations showing intermediate steps:

- $5 \times 6 = 30$
- $11 \div 5 = 2$ (with remainder 1)
- $30 - 2 = 28$
- $28 + 1 = 29$

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$$3 - 4 + 1 = 0$$

a) 12743

b) 12823

c) 12933

d) 12464

9. $88\% \text{ of } 370 + 24\% \text{ of } 210 - ? = 118$

Handwritten calculations for percentages:

- $88\% \text{ of } 370 = 325.6$
- $24\% \text{ of } 210 = 50.4$

$$7 + 0 - x = 1$$

$$x = 6$$