

**TABLE 2-3**  
Laws of Boolean  
Algebra

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Operations with 0 and 1:

1.  $X + 0 = X$

2.  $X + 1 = 1$

Idempotent laws:

3.  $X + X = X$

Involution law:

4.  $(X')' = X$

Laws of complementarity:

5.  $X + X' = 1$

Commutative laws:

6.  $X + Y = Y + X$

Associative laws:

7.  $(X + Y) + Z = X + (Y + Z)$   
 $= X + Y + Z$

Distributive laws:

8.  $X(Y + Z) = XY + XZ$

DeMorgan's laws:

9.  $(X + Y)' = X'Y'$

1D.  $X \cdot 1 = X$

2D.  $X \cdot 0 = 0$

3D.  $X \cdot X = X$

5D.  $X \cdot X' = 0$

6D.  $XY = YX$

7D.  $(XY)Z = X(YZ) = XYZ$

8D.  $X + YZ = (X + Y)(X + Z)$

9D.  $(XY)' = X' + Y'$

**TABLE 2-4**  
Theorems of  
Boolean Algebra  
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Uniting theorems:

$$1. XY + XY' = X$$

$$1D. (X + Y)(X + Y') = X$$

Absorption theorems:

$$2. X + XY = X$$

$$2D. X(X + Y) = X$$

Elimination theorems:

$$3. X + X'Y = X + Y$$

$$3D. X(X' + Y) = XY$$

Duality:

$$4. (X + Y + Z + \dots)^U = XYZ \dots$$

$$4D. (XYZ \dots)^U = X + Y + Z + \dots$$

Theorems for multiplying out and factoring:

$$5. (X + Y)(X' + Z) = XZ + X'Y$$

$$5D. XY + X'Z = (X + Z)(X' + Y)$$

Consensus theorems:

$$6. XY + YZ + X'Z = XY + X'Z$$

$$6D. (X + Y)(Y + Z)(X' + Z) = (X + Y)(X' + Z)$$