Contents

1 Basic

1.1 Default

```cpp
#include <bits/stdc++.h>
using namespace std;

using ll = long long;
using ull = unsigned long long;
using ld = long double;
using uint = unsigned int;
using pii = pair<int, int>;
using pll = pair<ll, ll>;
using vi = vector<int>;
using vl = vector<ll>;
using vvi = vector<vector<int>>;
using vvl = vector<vector<ll>>;
#define pb push_back
#define F first
#define S second
#define mid ((LB+RB)/2)
#define mkp make_pair
#define iter(x) x.begin(),x.end()
#define aiter(a,n) a,a+n
#define REP(n) for (int ___=n > 0 ? n : 0;___--;)
#define REP0(i,n) for (int i=0,___=n;i<___;++i)
#define REP1(i,n) for (int i=1,___=n;i<=___;++i)
#define MEM(e,val) memset (e,val,sizeof(e))
const double EPS = 1e-8;
const int INF = 0x3F3F3F3F;
const ll LINF = 4611686018427387903;
const int MOD = 1e9+7;
const int maxn = 1e5 + 25;

signed main() { ios::sync_with_stdio(0); cin.tie(0);

}
```

1.2 vimrc

```
set nu rnu is ls=2 hls ts=4 sw=4 et sts=4 ai bs=2 et sc
     acd mouse=a encoding=utf-8
syn on
filetype plugin indent on
colo desert
nnoremap <C-a> ggVG
vnoremap <C-c> "+y
inoremap <C-v> <ESC>"+pa
nnoremap <C-s> :w<CR>
inoremap <C-s> <ESC>:w<CR>a
inoremap {<CR> {<CR>}<Esc>O
nnoremap <F8> :w <bar> !g++ -std=c++17 % -o %:r -O2<CR>
nnoremap <F9> :w <bar> !g++ -std=c++17 % -o %:r -Wall -
    Wextra -Wconversion -Wshadow -Wfatal-errors -
    fsanitize=undefined,address -g -Dmichan <CR>
nnoremap <F10> :!./%:r <CR>
```

1.3 Pragma

```cpp
#pragma GCC optimize("Ofast,no-stack-protector")
#pragma GCC optimize("no-math-errno,unroll-loops")
#pragma GCC target("sse,sse2,sse3,ssse3,sse4")
#pragma GCC target("popcnt,abm,mmx,avx,tune=native")
```

2 Data Structure

2.1 Black Magic

```cpp
template<typename T>
using pbds_tree = tree<T, null_type, less<T>,
   rb_tree_tag, tree_order_statistics_node_update>;
// find_by_order: like array accessing, order_of_key
```

2.2 Lichao Tree

```cpp
struct lichao { // maxn: range
  struct line {
    ll a, b;
    line(): a(0), b(0) { } // or LINF
    line(ll a, ll b): a(a), b(b) { }
    ll operator()(ll x) { return a * x + b; }
  } arr[maxn << 2];
  void insert(int l, int r, int id, line x) {
    int m = (l + r) >> 1;
    if(arr[id](m) < x(m))
      swap(arr[id], x);
    if(l == r - 1)
      return;
    if(arr[id].a < x.a)
      insert(m, r, id << 1 | 1, x);
    else
      insert(l, m, id << 1, x);
  } // change to > if query min
  void insert(ll a, ll b) { insert(0, N, 1, line(a, b))
    ; }
  ll que(int l, int r, int id, int p) {
    if(l == r - 1)
      return arr[id](p);
    int m = (l + r) >> 1;
    if(p < m)
      return max(arr[id](p), que(l, m, id << 1, p));
    return max(arr[id](p), que(m, r, id << 1 | 1, p));
  } // chnage to min if query min
  ll que(int p) { return que(0, N, 1, p); }
} tree;
```

2.3 Linear Basis

```cpp
template<int BITS>
struct linear_basis {
  array<uint64_t, BITS> basis;
  linear_basis() { basis.fill(0); }
  void insert(uint64_t x) {
    for(int i = BITS - 1; i >= 0; i--) if((x >> i) & 1)
     {
      if(basis[i] == 0) {
        basis[i] = x;
        return;
      }
      x ^= basis[i];
    }
  }
  bool valid(uint64_t x) {
    for(int i = BITS - 1; i >= 0; i--)
      if((x >> i) & 1) x ^= basis[i];
    return x == 0;
  }
  uint64_t operator[](int i) { return basis[i]; }
}; // max xor sum: greedy from high bit
  // min xor sum: zero(if possible) or min_element
```

3 Graph

3.1 Bridge CC

```
namespace bridge_cc {
  vector<int> tim, low;
  stack<int, vector<int>> st;
  int t, bcc_id;
  void dfs(int u, int p, const vector<vector<pair<int,
    int>>> &edge, vector<int> &pa) {
    tim[u] = low[u] = t++;
    st.push(u);
    for(const auto &[v, id] : edge[u]) {
      if(id == p)
        continue;
      if(tim[v])
        low[u] = min(low[u], tim[v]);
      else {
        dfs(v, id, edge, pa);
        if(low[v] > tim[u]) {
          int x;
          do {
            pa[x = st.top()] = bcc_id;
            st.pop();
          } while(x != v);
          bcc_id++;
        }
        else
          low[u] = min(low[u], low[v]);
      }
    }
  }
  vector<int> solve(const vector<vector<pair<int, int
    >>> &edge) { // (to, id)
    int n = edge.size();
    tim.resize(n);
    low.resize(n);
    t = bcc_id = 1;
    vector<int> pa(n);

    for(int i = 0; i < n; i++) {
      if(!tim[i]) {
        dfs(i, -1, edge, pa);
        while(!st.empty()) {
          pa[st.top()] = bcc_id;
          st.pop();
        }
        bcc_id++;
      }
    }
    return pa;
  } // return bcc id(start from 1)
};
```

3.2 Dinic

```
template<typename T> // maxn: edge/node counts
struct dinic{ // T: int or ll, up to range of flow
  const T IN_INF = (is_same_v<T, int>) ? INF : LINF;
  struct E{
    int v; T c; int r;
    E(int v, T c, int r):
      v(v), c(c), r(r){}
  };
  vector<E> adj[maxn];
  pair<int, int> is[maxn]; // counts of edges
  void add_edge(int u, int v, T c, int i){
    is[i] = {u, adj[u].size()};
    adj[u].pb(E(v, c, (int) adj[v].size()));
    adj[v].pb(E(u, 0, (int) adj[u].size() - 1));
  }
  int n, s, t;
  void init(int nn, int ss, int tt){
    n = nn, s = ss, t = tt;
    for(int i = 0; i <= n; ++i)
      adj[i].clear();
  }
  int le[maxn], it[maxn];
  int bfs(){
    fill(le, le + maxn, -1); le[s] = 0;
    queue<int> q; q.push(s);
    while(!q.empty()){
      int u = q.front(); q.pop();
      for(auto [v, c, r]: adj[u]){
        if(c > 0 && le[v] == -1)
          le[v] = le[u] + 1, q.push(v);
      }
    }
    return ~le[t];
  }
  int dfs(int u, int f){
    if(u == t) return f;
    for(int &i = it[u]; i < (int) adj[u].size(); ++i){
      auto &[v, c, r] = adj[u][i];
      if(c > 0 && le[v] == le[u] + 1){
        int d = dfs(v, min(c, f));
        if(d > 0){
          c -= d;
          adj[v][r].c += d;
          return d;
        }
      }
    }
    return 0;
  }
  T flow(){
    T ans = 0, d;
    while(bfs()){
      fill(it, it + maxn, 0);
      while((d = dfs(s, IN_INF)) > 0) ans += d;
    }
    return ans;
  }
  T rest(int i) {
    return adj[is[i].first][is[i].second].c;
  }
};
```

3.3 Min Cost Max Flow

```
struct cost_flow { // maxn: node count
  static const int64_t INF = 102938475610293847LL;
  struct Edge {
    int v, r;
    int64_t f, c;
    Edge(int a,int b,int _c,int d):v(a),r(b),f(_c),c(d)
    { }
  };
  int n, s, t, prv[maxn], prvL[maxn], inq[maxn];
  int64_t dis[maxn], fl, cost;
  vector<Edge> E[maxn];
  void init(int _n, int _s, int _t) {
    n = _n; s = _s; t = _t;
    for (int i = 0; i < n; i++) E[i].clear();
    fl = cost = 0;
  }
  void add_edge(int u, int v, int64_t f, int64_t c) {
    E[u].push_back(Edge(v, E[v].size() , f, c));
    E[v].push_back(Edge(u, E[u].size()-1, 0, -c));
  }
  pair<int64_t, int64_t> flow() {
    while (true) {
      for (int i = 0; i < n; i++) {
        dis[i] = INF;
        inq[i] = 0;
      }
      dis[s] = 0;
      queue<int> que;
      que.push(s);
      while (!que.empty()) {
        int u = que.front(); que.pop();
        inq[u] = 0;
        for (int i = 0; i < E[u].size(); i++) {
          int v = E[u][i].v;
          int64_t w = E[u][i].c;
          if (E[u][i].f > 0 && dis[v] > dis[u] + w) {
            prv[v] = u; prvL[v] = i;
            dis[v] = dis[u] + w;
            if (!inq[v]) {
              inq[v] = 1;
              que.push(v);
            }
          }
        }
      }
      if (dis[t] == INF) break;
      int64_t tf = INF;
      for (int v = t, u, l; v != s; v = u) {
        u = prv[v]; l = prvL[v];
        tf = min(tf, E[u][l].f);
```

```
      }
      for (int v = t, u, l; v != s; v = u) {
        u = prv[v]; l = prvL[v];
        E[u][l].f -= tf;
        E[v][E[u][l].r].f += tf;
      }
      cost += tf * dis[t];
      fl += tf;
    }
    return {fl, cost};
  }
};
```

3.4 Stoer Wagner Algorithm

```
// return globale min cut in O(n^3)
struct SW { // 1-based
  int edge[maxn][maxn], wei[maxn], n;
  bool vis[maxn], del[maxn];
  void init(int _n) {
    n = _n; MEM(edge, 0); MEM(del, 0);
  }
  void add_edge(int u, int v, int w) {
    edge[u][v] += w; edge[v][u] += w;
  }
  void search(int &s, int &t) {
    MEM(wei, 0); MEM(vis, 0);
    s = t = -1;
    while(true) {
      int mx = -1;
      for(int i = 1; i <= n; i++) {
        if(del[i] || vis[i]) continue;
        if(mx == -1 || wei[mx] < wei[i])
          mx = i;
      }
      if(mx == -1) break;
      vis[mx] = true;
      s = t; t = mx;
      for(int i = 1; i <= n; i++)
        if(!vis[i] && !del[i])
          wei[i] += edge[mx][i];
    }
  }
  int solve() {
    int ret = INF;
    for(int i = 1; i < n; i++) {
      int x, y;
      search(x, y);
      ret = min(ret, wei[y]);
      del[y] = true;
      for(int j = 1; j <= n; j++) {
        edge[x][j] += edge[y][j];
        edge[j][x] += edge[y][j];
      }
    }
    return ret;
  }
} sw;
```

4 Geometry

4.1 Basic

```
using pt = pair<ll, ll>;
using ptf = pair<ld, ld>;
pt operator+(pt a, pt b)
{ return pt {a.F + b.F, a.S + b.S}; }
pt operator-(pt a, pt b)
{ return pt {a.F - b.F, a.S - b.S}; }
ptf to_ptf(pt p) { return ptf {p.F, p.S}; }
int sign(ll x) { return (x > 0) - (x < 0); }
ll dot(pt a, pt b) { return a.F * b.F + a.S * b.S; }
ll cross(pt a, pt b) { return a.F * b.S - a.S * b.F; }
ld abs2(ptf a) { return dot(a, a); }
ld abs(ptf a) { return sqrtl(dot(a, a)); }
int ori(pt a, pt b, pt c)
{ return sign(cross(b - a, c - a)); }
bool operator<(pt a, pt b)
{ return a.F != b.F ? a.F < b.F : a.S < b.S; }
```

4.2 2D Convex Hull

```
// returns a convex hull in counterclockwise order
// for a non-strict one, change cross >= to >
vector<pt> convex_hull(vector<pt> p) {
 sort(iter(p));
 if (p[0] == p.back()) return {p[0]};
 int n = p.size(), t = 0;
 vector<pt> h(n + 1);
 for (int _ = 2, s = 0; _--; s = --t, reverse(iter(p)))
  for (pt i : p) {
   while (t > s + 1 && cross(i, h[t-1], h[t-2])>=0)
    t--;
   h[t++] = i;
  }
 return h.resize(t), h;
} // not tested, but trust ckiseki!
```

5 String

5.1 KMP

```
vector<int> kmp(const string &s) {
  int n = s.size();
  vector<int> dp(n);
  for(int i = 1, j = 0; i < n; i++) {
    while(j && s[i] != s[j])
      j = dp[j - 1];
    if(s[i] == s[j])
      j++;
    dp[i] = j;
  }
  return dp;
}
```

5.2 Suffix Array

```
int sa[maxn], tmp[2][maxn], c[256];
void get_sa(const string &s) {
  int *x = tmp[0], *y = tmp[1], m = 256, n = s.size();
  for(int i = 0; i < m; i++) c[i] = 0;
  for(int i = 0; i < n; i++) c[x[i] = s[i]]++;
  for(int i = 1; i < m; i++) c[i] += c[i - 1];
  for(int i = n - 1; i >= 0; --i) sa[--c[x[i]]] = i;
  for(int k = 1; k < n; k <<= 1) {
    for(int i = 0; i < m; i++) c[i] = 0;
    for(int i = 0; i < n; i++) c[x[i]]++;
    for(int i = 1; i < m; i++) c[i] += c[i - 1];
    int p = 0;
    for(int i = n - k; i < n; i++) y[p++] = i;
    for(int i = 0; i < n; i++)
      if(sa[i] >= k) y[p++] = sa[i] - k;
    for(int i = n - 1; i >= 0; --i) sa[--c[x[y[i]]]] =
    y[i];
    y[sa[0]] = p = 0;
    for(int i = 1; i < n; i++) {
      int a = sa[i], b = sa[i - 1];
      if(x[a] == x[b] && a + k < n && b + k < n && x[a
    + k] == x[b + k]);
      else p++;
      y[sa[i]] = p;
    }
    if(n == p + 1)
      break;
    swap(x, y);
    m = p + 1;
  }
} // sa[i]: index which ranks i
int rk[maxn], lcp[maxn];
void get_cp(const string &s) {
  int n = s.size(), val = 0;
  for(int i = 0; i < n; i++) rk[sa[i]] = i;
  for(int i = 0; i < n; i++) {
    if(rk[i] == 0) lcp[rk[i]] = 0;
    else {
      if(val) val--;
      int p = sa[rk[i] - 1];
      while(val + i < n && val + p < n && s[val + i] ==
     s[val + p])
        val++;
      lcp[rk[i]] = val;
    }
  }
} // get_sa and get_lcp are not tested
```

6 Math

6.1 Extgcd

```
// return (d, x, y) s.t. ax+by=d=gcd(a,b)
template<typename T>
tuple<T, T, T> extgcd(T a, T b) {
  if(!b) return make_tuple(a, 1, 0);
  auto [d, x, y] = extgcd(b, a % b);
  return make_tuple(d, y, x - (a / b) * y);
} // not tested
```

6.2 Linear Sieve

```
int least_prime_divisor[maxn];
vector<int> pr;
void linear_sieve() {
  for(int i = 2; i < maxn; i++) {
    if(!least_prime_divisor[i]) {
      pr.push_back(i);
      least_prime_divisor[i] = i;
    }
    for(int p : pr) {
      if(1LL * i * p >= maxn) break;
      least_prime_divisor[i * p] = p;
      if(i % p == 0) break;
    }
  }
}
```

6.3 Miller Rabin

```
bool is_prime(ull x) { // need modular pow(mpow)
  static auto witn = [](ull a, ull u, ull n, int t) {
    if(!a) return false;
    while(t--) {
      ull a2 = __uint128_t(a) * a % n;
      if(a2 == 1 && a != 1 && a != n - 1) return true;
      a = a2;
    }
    return a != 1;
  };
  if(x < 2) return false;
  if(!(x & 1)) return x == 2;
  int t = __builtin_ctzll(x - 1);
  ull odd = (x - 1) >> t;
  for(ull m:
      {2, 325, 9375, 28178, 450775, 9780504,
    1795265022})
    if(witn(mpow(m % x, odd, x), odd, x, t))
      return false;
  return true;
}
```

6.4 Pollard's Rho

```
ull f(ull x, ull k, ull m) {
  return (__uint128_t(x) * x + k) % m;
}
// does not work when n is prime
// return any non-trivial factor
ull pollard_rho(ull n) {
  if(!(n & 1)) return 2;
  mt19937 rnd(120821011);
  while(true) {
    ull y = 2, yy = y, x = rnd() % n, t = 1;
    for(ull sz = 2; t == 1; sz <<= 1, y = yy) {
      for(ull i = 0; t == 1 && i < sz; ++i) {
        yy = f(yy, x, n);
        t = __gcd(yy > y ? yy - y : y - yy, n);
      }
    }
    if(t != 1 && t != n) return t;
  }
}
```

6.5 Fast Fourier Transform

```
using cplx = complex<double>;
const double pi = acos(-1);
cplx omega[maxn * 4];
void prefft(int n) {
 for(int i = 0; i <= n; i++)
  omega[i] = cplx(cos(2 * pi * i / n),
     sin(2 * pi * i / n));
}
void fft(vector<cplx> &v, int n) {
  int z = __builtin_ctz(n) - 1;
  for(int i = 0; i < n; i++) {
    int x = 0, j = 0;
    for(; (1 << j) < n; j++) x ^= (i >> j & 1) << (z -
    j);
    if(x > i) swap(v[x], v[i]);
  }
  for(int s = 2; s <= n; s <<= 1) {
    int z = s >> 1;
    for(int i = 0; i < n; i += s) {
      for(int k = 0; k < z; k++) {
        cplx x = v[i + z + k] * omega[n / s * k];
        v[i + z + k] = v[i + k] - x;
        v[i + k] = v[i + k] + x;
      }
    }
  }
}
void ifft(vector<cplx> &v, int n) {
  fft(v, n); reverse(v.begin() + 1, v.end());
  for(int i = 0; i < n; i++) v[i] = v[i] * cplx(1.0 / n
    , 0);
}
vl convolution(const vl &a, const vl &b) {
  // Should be able to handle N <= 10^5, C <= 10^4
  int sz = 1, tot = a.size() + b.size() - 1;
  while(sz < tot) sz <<= 1;
  prefft(sz);
  vector<cplx> v(sz);
  for(int i = 0; i < sz; i++) {
    double re = i < a.size() ? a[i] : 0;
    double im = i < b.size() ? b[i] : 0;
    v[i] = cplx(re, im);
  }
  fft(v, sz);
  for(int i = 0; i <= sz / 2; i++) {
    int j = (sz - i) & (sz - 1);
    cplx x = (v[i] + conj(v[j])) * (v[i] - conj(v[j]))
    * cplx(0, -0.25);
    if(j != i) v[j] = (v[j] + conj(v[i])) * (v[j] -
    conj(v[i])) * cplx(0, -0.25);
    v[i] = x;
  }
  ifft(v, sz);
  vl c(sz);
  for(int i = 0; i < sz; i++)c[i] = round(v[i].real());
  c.resize(tot);
  return c;
}
```

6.6 3 Primes NTT

```
// MOD: arbitrary prime
const int M1 = 998244353;
const int M2 = 1004535809;
const int M3 = 2013265921;
int super_big_crt(int64_t A, int64_t B, int64_t C) {
  static_assert(M1 <= M2 && M2 <= M3);
  ll r12 = mpow(M1, M2 - 2, M2);
  ll r13 = mpow(M1, M3 - 2, M3);
  ll r23 = mpow(M2, M3 - 2, M3);
  ll M1M2 = 1LL * M1 * M2 % MOD;
  B = (B - A + M2) * r12 % M2;
  C = (C - A + M3) * r13 % M3;
  C = (C - B + M3) * r23 % M3;
  return (A + B * M1 + C * M1M2) % MOD;
} // return ans % MOD
```

6.7 Number Theory Transform

```
/* mod | g | maxn possible values:
998244353 | 3 | 8388608
1004535809 | 3 } 2097152
2013265921 | 31 | 134217728 */
template <int mod, int G, int maxn>
struct NTT {
  ll mpow(ll a, ll b) {
    ll res = 1;
    for(; b; b >>= 1, a = a * a % mod)
      if(b & 1)
        res = res * a % mod;
    return res;
  }
  static_assert(maxn == (maxn & -maxn));
  int roots[maxn];
  NTT() {
```

```
    ll r = mpow(G, (mod - 1) / maxn);
    for(int i = maxn >> 1; i; i >>= 1) {
      roots[i] = 1;
      for(int j = 1; j < i; j++)
        roots[i + j] = roots[i + j - 1] * r % mod;
      r = r * r % mod;
    }
  }
  // n must be 2^k, and 0 <= f[i] < mod
  void operator()(vector<ll> &f, int n, bool inv =
    false) {
    for(int i = 0, j = 0; i < n; i++) {
      if(i < j) swap(f[i], f[j]);
      for(int k = n >> 1; (j ^= k) < k; k >>= 1);
    }
    for(int s = 1; s < n; s *= 2) {
      for(int i = 0; i < n; i += s * 2) {
        for(int j = 0; j < s; j++) {
          ll a = f[i + j];
          ll b = f[i + j + s] * roots[s + j] % mod;
          f[i + j] = (a + b) % mod;
          f[i + j + s] = (a - b + mod) % mod;
        }
      }
    }
    if(inv) {
      int invn = mpow(n, mod - 2);
      for(int i = 0; i < n; i++)
        f[i] = f[i] * invn % mod;
      reverse(f.begin() + 1, f.end());
    }
  }
};
```