Contents

1 Basic

1.1 Pragma

```cpp
#pragma GCC optimize("Ofast,no-stack-protector")
#pragma GCC optimize("no-math-errno,unroll-loops")
#pragma GCC target("sse,sse2,sse3,ssse3,sse4")
#pragma GCC target("popcnt,abm,mmx,avx,tune=native")
```

2 Data Structure

2.1 Black Magic

```cpp
template<typename T>
using pbds_tree = tree<T, null_type, less<T>,
  rb_tree_tag, tree_order_statistics_node_update>;
// find_by_order: like array accessing, order_of_key
```

2.2 Lichao Tree

```cpp
struct lichao { // maxn: range
  struct line {
    ll a, b;
    line(): a(0), b(0) { } // or LINF
    line(ll a, ll b): a(a), b(b) { }
    ll operator()(ll x) { return a * x + b; }
  } arr[maxn << 2];
  void insert(int l, int r, int id, line x) {
    int m = (l + r) >> 1;
    if(arr[id](m) < x(m))
      swap(arr[id], x);
    if(l == r - 1)
      return;
    if(arr[id].a < x.a)
      insert(m, r, id << 1 | 1, x);
    else
      insert(l, m, id << 1, x);
  } // change to > if query min
  void insert(ll a, ll b) { insert(0, N, 1, line(a, b))
    ; }
  ll que(int l, int r, int id, int p) {
    if(l == r - 1)
      return arr[id](p);
    int m = (l + r) >> 1;
    if(p < m)
      return max(arr[id](p), que(l, m, id << 1, p));
    return max(arr[id](p), que(m, r, id << 1 | 1, p));
  } // chnage to min if query min
  ll que(int p) { return que(0, N, 1, p); }
} tree;
```

2.3 Linear Basis

```cpp
template<int BITS>
struct linear_basis {
  array<uint64_t, BITS> basis;
  linear_basis() { basis.fill(0); }
  void insert(uint64_t x) {
    for(int i = BITS - 1; i >= 0; i--) if((x >> i) & 1)
    {
      if(basis[i] == 0) {
        basis[i] = x;
        return;
      }
      x ^= basis[i];
    }
  }
  bool valid(uint64_t x) {
    for(int i = BITS - 1; i >= 0; i--)
      if((x >> i) & 1) x ^= basis[i];
    return x == 0;
  }
  uint64_t operator[](int i) { return basis[i]; }
}; // max xor sum: greedy from high bit
   // min xor sum: zero(if possible) or min_element
```

3 Graph

3.1 Bridge CC

```cpp
namespace bridge_cc {
  vector<int> tim, low;
  stack<int, vector<int>> st;
  int t, bcc_id;
  void dfs(int u, int p, const vector<vector<pair<int,
    int>>> &edge, vector<int> &pa) {
    tim[u] = low[u] = t++;
    st.push(u);
    for(const auto &[v, id] : edge[u]) {
      if(id == p)
        continue;
      if(tim[v])
        low[u] = min(low[u], tim[v]);
      else {
        dfs(v, id, edge, pa);
        if(low[v] > tim[u]) {
          int x;
          do {
            pa[x = st.top()] = bcc_id;
            st.pop();
          } while(x != v);
          bcc_id++;
        }
        else
          low[u] = min(low[u], low[v]);
      }
    }
  }
  vector<int> solve(const vector<vector<pair<int, int
    >>> &edge) { // (to, id)
    int n = edge.size();
    tim.resize(n);
    low.resize(n);
    t = bcc_id = 1;
    vector<int> pa(n);

    for(int i = 0; i < n; i++) {
      if(!tim[i]) {
        dfs(i, -1, edge, pa);
        while(!st.empty()) {
          pa[st.top()] = bcc_id;
          st.pop();
        }
        bcc_id++;
      }
    }
    return pa;
  } // return bcc id(start from 1)
};
```

3.2 Dinic

```cpp
template<typename T> // maxn: edge/node counts
struct dinic{ // T: int or ll, up to range of flow
  const T IN_INF = (is_same_v<T, int>) ? INF : LINF;
```

```cpp
struct E{
  int v; T c; int r;
  E(int v, T c, int r):
    v(v), c(c), r(r){}
};
vector<E> adj[maxn];
pair<int, int> is[maxn]; // counts of edges
void add_edge(int u, int v, T c, int i){
  is[i] = {u, adj[u].size()};
  adj[u].pb(E(v, c, (int) adj[v].size()));
  adj[v].pb(E(u, 0, (int) adj[u].size() - 1));
}
int n, s, t;
void init(int nn, int ss, int tt){
  n = nn, s = ss, t = tt;
  for(int i = 0; i <= n; ++i)
    adj[i].clear();
}
int le[maxn], it[maxn];
int bfs(){
  fill(le, le + maxn, -1); le[s] = 0;
  queue<int> q; q.push(s);
  while(!q.empty()){
    int u = q.front(); q.pop();
    for(auto [v, c, r]: adj[u]){
      if(c > 0 && le[v] == -1)
        le[v] = le[u] + 1, q.push(v);
    }
  }
  return ~le[t];
}
int dfs(int u, int f){
  if(u == t) return f;
  for(int &i = it[u]; i < (int) adj[u].size(); ++i){
    auto &[v, c, r] = adj[u][i];
    if(c > 0 && le[v] == le[u] + 1){
      int d = dfs(v, min(c, f));
      if(d > 0){
        c -= d;
        adj[v][r].c += d;
        return d;
      }
    }
  }
  return 0;
}
T flow(){
  T ans = 0, d;
  while(bfs()){
    fill(it, it + maxn, 0);
    while((d = dfs(s, IN_INF)) > 0) ans += d;
  }
  return ans;
}
T rest(int i) {
  return adj[is[i].first][is[i].second].c;
}
};
```

3.3 Min Cost Max Flow

```cpp
struct cost_flow { // maxn: node count
  static const int64_t INF = 1029384756102938471LL;
  struct Edge {
    int v, r;
    int64_t f, c;
    Edge(int a,int b,int _c,int d):v(a),r(b),f(_c),c(d)
    { }
  };
  int n, s, t, prv[maxn], prvL[maxn], inq[maxn];
  int64_t dis[maxn], fl, cost;
  vector<Edge> E[maxn];
  void init(int _n, int _s, int _t) {
    n = _n; s = _s; t = _t;
    for (int i = 0; i < n; i++) E[i].clear();
    fl = cost = 0;
  }
  void add_edge(int u, int v, int64_t f, int64_t c) {
    E[u].push_back(Edge(v, E[v].size() , f, c));
    E[v].push_back(Edge(u, E[u].size()-1, 0, -c));
  }
  pair<int64_t, int64_t> flow() {
    while (true) {
```

```cpp
      for (int i = 0; i < n; i++) {
        dis[i] = INF;
        inq[i] = 0;
      }
      dis[s] = 0;
      queue<int> que;
      que.push(s);
      while (!que.empty()) {
        int u = que.front(); que.pop();
        inq[u] = 0;
        for (int i = 0; i < E[u].size(); i++) {
          int v = E[u][i].v;
          int64_t w = E[u][i].c;
          if (E[u][i].f > 0 && dis[v] > dis[u] + w) {
            prv[v] = u; prvL[v] = i;
            dis[v] = dis[u] + w;
            if (!inq[v]) {
              inq[v] = 1;
              que.push(v);
            }
          }
        }
      }
      if (dis[t] == INF) break;
      int64_t tf = INF;
      for (int v = t, u, l; v != s; v = u) {
        u = prv[v]; l = prvL[v];
        tf = min(tf, E[u][l].f);
      }
      for (int v = t, u, l; v != s; v = u) {
        u = prv[v]; l = prvL[v];
        E[u][l].f -= tf;
        E[v][E[u][l].r].f += tf;
      }
      cost += tf * dis[t];
      fl += tf;
    }
    return {fl, cost};
  }
};
```

3.4 Stoer Wagner Algorithm

```cpp
// return globale min cut in O(n^3)
struct SW { // 1-based
  int edge[maxn][maxn], wei[maxn], n;
  bool vis[maxn], del[maxn];
  void init(int _n) {
    n = _n; MEM(edge, 0); MEM(del, 0);
  }
  void add_edge(int u, int v, int w) {
    edge[u][v] += w; edge[v][u] += w;
  }
  void search(int &s, int &t) {
    MEM(wei, 0); MEM(vis, 0);
    s = t = -1;
    while(true) {
      int mx = -1;
      for(int i = 1; i <= n; i++) {
        if(del[i] || vis[i]) continue;
        if(mx == -1 || wei[mx] < wei[i])
          mx = i;
      }
      if(mx == -1) break;
      vis[mx] = true;
      s = t; t = mx;
      for(int i = 1; i <= n; i++)
        if(!vis[i] && !del[i])
          wei[i] += edge[mx][i];
    }
  }
  int solve() {
    int ret = INF;
    for(int i = 1; i < n; i++) {
      int x, y;
      search(x, y);
      ret = min(ret, wei[y]);
      del[y] = true;
      for(int j = 1; j <= n; j++) {
        edge[x][j] += edge[y][j];
        edge[j][x] += edge[y][j];
      }
    }
```

```
      return ret;
    }
} sw;
```

3.5 Hopcroft Karp Algorithm

```
// Find maximum bipartite matching in O(Esqrt(V))
// g: edges for all nodes at left side
vector<int> hopcroft_karp(vector<vector<int>> g, int l,
      int r) {
  vector<int> match_l(l, -1), match_r(r, -1);
  vector<int> dis(l);
  vector<bool> vis(l);
  while(true) {
    queue<int> que;
    for(int i = 0; i < l; i++) {
      if(match_l[i] == -1)
        dis[i] = 0, que.push(i);
      else
        dis[i] = -1;
      vis[i] = false;
    }
    while(!que.empty()) {
      int x = que.front();
      que.pop();
      for(int y : g[x])
        if(match_r[y] != -1 && dis[match_r[y]] == -1) {
          dis[match_r[y]] = dis[x] + 1;
          que.push(match_r[y]);
        }
    }
    auto dfs = [&](auto dfs, int x) {
      vis[x] = true;
      for(int y : g[x]) {
        if(match_r[y] == -1) {
          match_l[x] = y;
          match_r[y] = x;
          return true;
        }
        else if(dis[match_r[y]] == dis[x] + 1
            && !vis[match_r[y]]
            && dfs(dfs, match_r[y])) {
          match_l[x] = y;
          match_r[y] = x;
          return true;
        }
      }
      return false;
    };
    bool ok = true;
    for(int i = 0; i < l; i++)
      if(match_l[i] == -1 && dfs(dfs, i))
        ok = false;
    if(ok)
      break;
  }
  return match_l;
} // 0-based
```

3.6 General Matching

```
// Find max matching on general graph in O(|V|^3)
vector<int> max_matching(vector<vector<int>> g) {
  int n = g.size();
  vector<int> match(n + 1, n), pre(n + 1, n), que;
  vector<int> s(n + 1), mark(n + 1), pa(n + 1);
  function<int(int)> fnd = [&](int x) {
    if(x == pa[x]) return x;
    return pa[x] = fnd(pa[x]);
  };
  auto lca = [&](int x, int y) {
    static int tk = 0;
    tk++;
    x = fnd(x);
    y = fnd(y);
    for(;; swap(x, y))
      if(x != n) {
        if(mark[x] == tk)
          return x;
        mark[x] = tk;
        x = fnd(pre[match[x]]);
      }
  };
  auto blossom = [&](int x, int y, int l) {
```

```
    while(fnd(x) != l) {
      pre[x] = y;
      y = match[x];
      if(s[y] == 1)
        que.push_back(y), s[y] = 0;
      if(pa[x] == x) pa[x] = l;
      if(pa[y] == y) pa[y] = l;
      x = pre[y];
    }
  };
  auto bfs = [&](int r) {
    fill(s.begin(), s.end(), -1);
    iota(pa.begin(), pa.end(), 0);
    que = {r}; s[r] = 0;
    for(int it = 0; it < que.size(); it++) {
      int x = que[it];
      for(int u : g[x]) {
        if(s[u] == -1) {
          pre[u] = x;
          s[u] = 1;
          if(match[u] == n) {
            for(int a = u, b = x, lst;
                b != n; a = lst, b = pre[a]) {
              lst = match[b];
              match[b] = a;
              match[a] = b;
            }
            return;
          }
          que.push_back(match[u]);
          s[match[u]] = 0;
        }
        else if(s[u] == 0 && fnd(u) != fnd(x)) {
          int l = lca(u, x);
          blossom(x, u, l);
          blossom(u, x, l);
        }
      }
    }
  };
  for(int i = 0; i < n; i++)
    if(match[i] == n) bfs(i);
  match.resize(n);
  for(int i = 0; i < n; i++)
    if(match[i] == n) match[i] = -1;
  return match;
} // 0-based
```

4 Geometry

4.1 Basic

```
using pt = pair<ll, ll>;
using ptf = pair<ld, ld>;
pt operator+(pt a, pt b)
{ return pt {a.F + b.F, a.S + b.S}; }
pt operator-(pt a, pt b)
{ return pt {a.F - b.F, a.S - b.S}; }
ptf to_ptf(pt p) { return ptf {p.F, p.S}; }
int sign(ll x) { return (x > 0) - (x < 0); }
ll dot(pt a, pt b) { return a.F * b.F + a.S * b.S; }
ll cross(pt a, pt b) { return a.F * b.S - a.S * b.F; }
ld abs2(ptf a) { return dot(a, a); }
ld abs(ptf a) { return sqrtl(dot(a, a)); }
int ori(pt a, pt b, pt c)
{ return sign(cross(b - a, c - a)); }
bool operator<(pt a, pt b)
{ return a.F != b.F ? a.F < b.F : a.S < b.S; }
```

4.2 2D Convex Hull

```
// returns a convex hull in counterclockwise order
// for a non-strict one, change cross >= to >
vector<pt> convex_hull(vector<pt> p) {
 sort(iter(p));
 if (p[0] == p.back()) return {p[0]};
 int n = p.size(), t = 0;
 vector<pt> h(n + 1);
 for (int _ = 2, s = 0; _--; s = --t, reverse(iter(p)))
  for (pt i : p) {
   while (t > s + 1 && cross(i, h[t-1], h[t-2])>=0)
    t--;
   h[t++] = i;
```

```
  }
 return h.resize(t), h;
} // not tested, but trust ckiseki!
```

5 String
5.1 KMP
```cpp
vector<int> kmp(const string &s) {
  int n = s.size();
  vector<int> dp(n);
  for(int i = 1, j = 0; i < n; i++) {
    while(j && s[i] != s[j])
      j = dp[j - 1];
    if(s[i] == s[j])
      j++;
    dp[i] = j;
  }
  return dp;
}
```

5.2 Suffix Array
```cpp
int sa[maxn], tmp[2][maxn], c[maxn];
void get_sa(const string &s) { // m: char set
  int *x = tmp[0], *y = tmp[1], m = 256, n = s.size();
  for(int i = 0; i < m; i++) c[i] = 0;
  for(int i = 0; i < n; i++) c[x[i] = s[i]]++;
  for(int i = 1; i < m; i++) c[i] += c[i - 1];
  for(int i = n - 1; i >= 0; --i) sa[--c[x[i]]] = i;
  for(int k = 1; k < n; k <<= 1) {
    for(int i = 0; i < m; i++) c[i] = 0;
    for(int i = 0; i < n; i++) c[x[i]]++;
    for(int i = 1; i < m; i++) c[i] += c[i - 1];
    int p = 0;
    for(int i = n - k; i < n; i++) y[p++] = i;
    for(int i = 0; i < n; i++)
      if(sa[i] >= k) y[p++] = sa[i] - k;
    for(int i = n - 1; i >= 0; --i) sa[--c[x[y[i]]]] =
y[i];
    y[sa[0]] = p = 0;
    for(int i = 1; i < n; i++) {
      int a = sa[i], b = sa[i - 1];
      if(x[a] == x[b] && a + k < n && b + k < n && x[a
+ k] == x[b + k]);
      else p++;
      y[sa[i]] = p;
    }
    if(n == p + 1)
      break;
    swap(x, y);
    m = p + 1;
  }
} // sa[i]: index which ranks i
int rk[maxn], lcp[maxn]; // lcp[i] : lcp with i-1
void get_lcp(const string &s) {
  int n = s.size(), val = 0;
  for(int i = 0; i < n; i++) rk[sa[i]] = i;
  for(int i = 0; i < n; i++) {
    if(rk[i] == 0) lcp[rk[i]] = 0;
    else {
      if(val) val--;
      int p = sa[rk[i] - 1];
      while(val + i < n && val + p < n && s[val + i] ==
s[val + p])
        val++;
      lcp[rk[i]] = val;
    }
  }
}
```

5.3 Booth Algorithm
```cpp
// return start index of minimum rotation in O(|s|)
int min_rotation(string s) {
  s += s;
  int k = 0;
  vector<int> f(s.size(), -1);
  for(int j = 1; j < s.size(); j++) {
    int i = f[j - k - 1];
    for(i = f[j - k - 1];
        i != -1 && s[j] != s[i + k + 1]; i = f[i])
      if(s[k + i + 1] > s[j])
        k = j - i - 1;
```

```cpp
    if(i == -1 && s[j] != s[k + i + 1]) {
      if(s[j] < s[k + i + 1])
        k = j;
      f[j - k] = -1;
    }
    else
      f[j - k] = i + 1;
  }
  return k;
}
```

5.4 Manacher Algorithm
```cpp
vector<int> manacher_algorithm(string s) {
  int n = 2 * s.size() + 1;
  string t(n, 0);
  vector<int> len(n);//len[i]: max length when mid at i
  for(int i = 0; i < n; i++) {
    if(i & 1)
      t[i] = s[i / 2];
  }
  for(int i = 0, l = 0, r = -1; i < n; i++) {
    len[i] = (i <= r ? min(len[2 * l - i], r - i) : 0);
    while(i - len[i] >= 0 && i + len[i] < n && t[i -
        len[i]] == t[i + len[i]])
      len[i]++;
    len[i]--;
    if(i + len[i] > r)
      l = i, r = i + len[i];
  }
  return len;
}
```

6 Math
6.1 Extgcd
```cpp
// return (d, x, y) s.t. ax+by=d=gcd(a,b)
template<typename T>
tuple<T, T, T> extgcd(T a, T b) {
  if(!b) return make_tuple(a, 1, 0);
  auto [d, x, y] = extgcd(b, a % b);
  return make_tuple(d, y, x - (a / b) * y);
} // not tested
```

6.2 Linear Sieve
```cpp
int least_prime_divisor[maxn];
vector<int> pr;
void linear_sieve() {
  for(int i = 2; i < maxn; i++) {
    if(!least_prime_divisor[i]) {
      pr.push_back(i);
      least_prime_divisor[i] = i;
    }
    for(int p : pr) {
      if(1LL * i * p >= maxn) break;
      least_prime_divisor[i * p] = p;
      if(i % p == 0) break;
    }
  }
}
```

6.3 Miller Rabin
```cpp
bool is_prime(ull x) { // need modular pow(mpow)
  static auto witn = [](ull a, ull u, ull n, int t) {
    if(!a) return false;
    while(t--) {
      ull a2 = __uint128_t(a) * a % n;
      if(a2 == 1 && a != 1 && a != n - 1) return true;
      a = a2;
    }
    return a != 1;
  };
  if(x < 2) return false;
  if(!(x & 1)) return x == 2;
  int t = __builtin_ctzll(x - 1);
  ull odd = (x - 1) >> t;
  for(ull m:
      {2, 325, 9375, 28178, 450775, 9780504,
      1795265022})
    if(witn(mpow(m % x, odd, x), odd, x, t))
      return false;
  return true;
}
```

6.4 Pollard's Rho

```cpp
ull f(ull x, ull k, ull m) {
  return (__uint128_t(x) * x + k) % m;
}
// does not work when n is prime
// return any non-trivial factor
ull pollard_rho(ull n) {
  if(!(n & 1)) return 2;
  mt19937 rnd(120821011);
  while(true) {
    ull y = 2, yy = y, x = rnd() % n, t = 1;
    for(ull sz = 2; t == 1; sz <<= 1, y = yy) {
      for(ull i = 0; t == 1 && i < sz; ++i) {
        yy = f(yy, x, n);
        t = __gcd(yy > y ? yy - y : y - yy, n);
      }
    }
    if(t != 1 && t != n) return t;
  }
}
```

6.5 Fast Fourier Transform

```cpp
using cplx = complex<double>;
const double pi = acos(-1);
cplx omega[maxn * 4];
void prefft(int n) {
 for(int i = 0; i <= n; i++)
  omega[i] = cplx(cos(2 * pi * i / n),
    sin(2 * pi * i / n));
}
void fft(vector<cplx> &v, int n) {
  int z = __builtin_ctz(n) - 1;
  for(int i = 0; i < n; i++) {
    int x = 0, j = 0;
    for(; (1 << j) < n; j++) x ^= (i >> j & 1) << (z -
j);
    if(x > i) swap(v[x], v[i]);
  }
  for(int s = 2; s <= n; s <<= 1) {
    int z = s >> 1;
    for(int i = 0; i < n; i += s) {
      for(int k = 0; k < z; k++) {
        cplx x = v[i + z + k] * omega[n / s * k];
        v[i + z + k] = v[i + k] - x;
        v[i + k] = v[i + k] + x;
      }
    }
  }
}
void ifft(vector<cplx> &v, int n) {
  fft(v, n); reverse(v.begin() + 1, v.end());
  for(int i = 0; i < n; i++) v[i] = v[i] * cplx(1.0 / n
    , 0);
}
vl convolution(const vl &a, const vl &b) {
  // Should be able to handle N <= 10^5, C <= 10^4
  int sz = 1, tot = a.size() + b.size() - 1;
  while(sz < tot) sz <<= 1;
  prefft(sz);
  vector<cplx> v(sz);
  for(int i = 0; i < sz; i++) {
    double re = i < a.size() ? a[i] : 0;
    double im = i < b.size() ? b[i] : 0;
    v[i] = cplx(re, im);
  }
  fft(v, sz);
  for(int i = 0; i <= sz / 2; i++) {
    int j = (sz - i) & (sz - 1);
    cplx x = (v[i] + conj(v[j])) * (v[i] - conj(v[j]))
      * cplx(0, -0.25);
    if(j != i) v[j] = (v[j] + conj(v[i])) * (v[j] -
    conj(v[i])) * cplx(0, -0.25);
    v[i] = x;
  }
  ifft(v, sz);
  vl c(sz);
  for(int i = 0; i < sz; i++)c[i] = round(v[i].real());
  c.resize(tot);
  return c;
}
```

6.6 3 Primes NTT

```cpp
// MOD: arbitrary prime
const int M1 = 998244353;
const int M2 = 1004535809;
const int M3 = 2013265921;
int super_big_crt(int64_t A, int64_t B, int64_t C) {
  static_assert(M1 <= M2 && M2 <= M3);
  ll r12 = mpow(M1, M2 - 2, M2);
  ll r13 = mpow(M1, M3 - 2, M3);
  ll r23 = mpow(M2, M3 - 2, M3);
  ll M1M2 = 1LL * M1 * M2 % MOD;
  B = (B - A + M2) * r12 % M2;
  C = (C - A + M3) * r13 % M3;
  C = (C - B + M3) * r23 % M3;
  return (A + B * M1 + C * M1M2) % MOD;
} // return ans % MOD
```

6.7 Number Theory Transform

```cpp
/* mod | g | maxn possible values:
998244353 | 3 | 8388608
1004535809 | 3 } 2097152
2013265921 | 31 | 134217728 */
template <int mod, int G, int maxn>
struct NTT {
  ll mpow(ll a, ll b) {
    ll res = 1;
    for(; b; b >>= 1, a = a * a % mod)
      if(b & 1)
        res = res * a % mod;
    return res;
  }
  static_assert(maxn == (maxn & -maxn));
  int roots[maxn];
  NTT() {
    ll r = mpow(G, (mod - 1) / maxn);
    for(int i = maxn >> 1; i; i >>= 1) {
      roots[i] = 1;
      for(int j = 1; j < i; j++)
        roots[i + j] = roots[i + j - 1] * r % mod;
      r = r * r % mod;
    }
  }
  // n must be 2^k, and 0 <= f[i] < mod
  void operator()(vector<ll> &f, int n, bool inv =
    false) {
    for(int i = 0, j = 0; i < n; i++) {
      if(i < j) swap(f[i], f[j]);
      for(int k = n >> 1; (j ^= k) < k; k >>= 1);
    }
    for(int s = 1; s < n; s *= 2) {
      for(int i = 0; i < n; i += s * 2) {
        for(int j = 0; j < s; j++) {
          ll a = f[i + j];
          ll b = f[i + j + s] * roots[s + j] % mod;
          f[i + j] = (a + b) % mod;
          f[i + j + s] = (a - b + mod) % mod;
        }
      }
    }
    if(inv) {
      int invn = mpow(n, mod - 2);
      for(int i = 0; i < n; i++)
        f[i] = f[i] * invn % mod;
      reverse(f.begin() + 1, f.end());
    }
  }
};
```