

## COVER PAGE

### STAT 608 Homework 06 Summer 2017

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NAME: RAJAN KAPOOR

EMAIL: r.kapoor@tanu.edu.

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**STATISTICS 608**

**Homework 608 S17 06**

**Due:** 11:59 PM, July 17, 2017

**Question 1** [ $4+4+4+4+2+2=20$ ]

Work Exercise 3 on page 261 in the textbook.

**Question 2** [ $2+4=6$ ]

Work Exercise 8.3.1, page 294, in the textbook.

## Solution 1

(a) All possible subsets

	$R^2_{adj}$	AIC	AICc	BIC
1	0.25107	-63.126	-63.0018	-56.57053
2	0.48577	-135.85	-135.6493	-126.0244
3	0.53819	-155.31	-154.94498	-142.1983
4	0.54278	-156.291	-155.8468	-139.9004
5	0.54585	-156.6416	-156.0459	-136.9729
6	0.54366	-154.7307	-153.9606	-131.7839
7	0.54124	-152.7355	-151.7677	-126.5105

Optimal Model acc to BIC

$$\log(\text{PrizeMoney}) \sim \text{GIR} + \text{BirdieConversion} + \text{Scrambling} \quad (x_2 + x_4 + x_6) \text{ or}$$

Optimal model acc to AIC, AICc,  $R^2_{adj}$

$$\log(\text{PrizeMoney}) \sim \text{GIR} + \text{BirdieConversion} + \text{SandSaves} + \text{Scrambling} + \text{Putts per Round} \quad \text{or } (x_2 + x_4 + x_5 + x_6 + x_7)$$

(b) Backward selection AIC

$$\log(Y) \sim \text{GIR} + \text{BirdieConversion} + \text{SandSaves} + \text{Scrambling} + \text{Putts per Round}$$

$$\text{or } (x_2 + x_4 + x_5 + x_6 + x_7)$$

Backward selection BIC

$$\log(Y) \sim \text{Scrambling} + \text{GIR} + \text{BirdieConversion}$$

$$\text{or } (x_6 + x_2 + x_4)$$

AIC is  
(R-notation)

(c) Forward Selection AIC

$$\log(Y) \sim \text{GIR} + \text{Putts per Round} + \text{Birdie Conversion} + \text{Scrambling} + \text{Sand save}$$

(in R-notation)

$$\text{or } (x_2 + x_7 + x_4 + x_6 + x_5)$$

Forward selection BIC

$$\log(Y) \sim \text{GIR} + \text{Putts per Round} + \text{Birdie Conversion} + \text{Scrambling}$$

(in R-notation)

$$\text{or } (x_2 + x_7 + x_4 + x_6)$$

(d) In Backward selection, all predictors in subset 5 are present in subset 6 and subset 7. So when elimination starts from subset 7 and stops at subset 5 same result as (a) is obtained for AIC. Similar argument can be given for BIC in (b) and (c).

On the other hand, when starting from 1 predictor in forward selection, Putts per Round is present in subset 2 predictors but not in subset 3 predictors. Since in forward selection, once a predictor is added, it cannot be removed in following steps, BIC fails to consider the 3-predictor <sup>sub-</sup>sets without putts per Round predictor and different result from (a) is obtained.

Forward selection AIC gives same result because it does not stop at 3 predictor set.

e) The 3-predictor model has all 3 regression coeff as statistically highly significant while 5 predictor model has only 3 of 5 coefficients statistically significant. Final Recommended model is selected using partial F test.

$$\underline{M1}: \log(Y) \sim x_2 + x_4 + x_6$$

$$\text{or } \log(Y) = \beta_0 + \beta_2 x_2 + \beta_4 x_4 + \beta_6 x_6$$

$$M2: \log(Y) \sim x_2 + x_4 + x_6 + x_7 + x_5$$

Using partial F-test in anova,

- the p-value is found to be significant

⇒ cannot reject reduced model M1.

∴ final Recommended model is

$$\log(Y) = \beta_0 + \beta_2 x_2 + \beta_4 x_4 + \beta_6 x_6$$

(f) The mmp plots show quite a variation when compared with non linear models. Yes, we should be cautious in using the results literally..

2 (a) <sup>①</sup> The variable Playoff Appearances is discrete. It is based on series of yes/no responses which ideally follow a binomial distribution, not Gaussian as assumed by the linear model. The variance in such case is not constant and thus validity of model is in question.

② From histogram, the predictor Population appears to be right skewed. As such, some sort of transformation or inclusion of  $\log(\text{Population})$  is expected.

③ Using logistic regression of Playoff Appearances on  $\log(\text{Population})$  results in regression coeff

$$\beta_0 = -1.8525$$

$$\beta_1 = 0.5606$$