# **Activity 9**

## ORIECTIVE

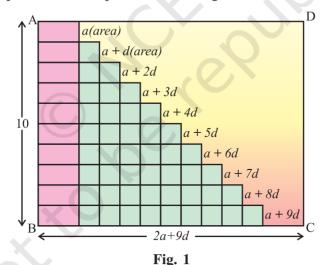
To establish a formula for the sum of first n terms of an Arithmetic Progression.

# MATERIAL REQUIRED

Cardboard, coloured drawing sheets, white paper, cutter, adhesive.

#### METHOD OF CONSTRUCTION

- 1. Take a rectangular cardboard of a convenient size and paste a white paper on it. Draw a rectangle ABCD of length (2a+9d) units and breadth 10 units.
- 2. Make some rectangular strips of equal length a units and breadth one unit and some strips of length d units and breadth 1 unit, using coloured drawing sheets.
- 3. Arrange/paste these strips on the rectangle ABCD as shown in Fig. 1.



## **DEMONSTRATION**

- 1. The strips so arranged look like a stair case.
- 2. The first stair is of length a units, the second stair is of length a+d (units), third of a+2d units and so on and each is of breadth 1 unit. So, the areas (in sq. units) of these strips are a, a + d, a + 2d, ...., a+9d, respectively.

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- 3. This arrangement of strips gives a pattern a, a + d, a + 2d, a + 3d, ... which is an AP with first term a and the common difference d.
- 4. The sum of the areas (in square units) of these strips  $= a + (a + d) + (a + 2d) + \dots + (a + 9d) = 10a + 45d \tag{1}$
- 5. Area of the designed formed by the stair case =  $\frac{1}{2}$  (area of rectangle ABCD)

$$= \frac{1}{2}(10)(2a+9d)$$

= (10a + 45d), which is the same as obtained in (1) above.

This shows that the sum of first 10 terms of the AP =  $\frac{1}{2}(10)(2a+9d)$ 

$$= \frac{1}{2}(10) \left[2a + (10 - 1)d\right]$$

This can be further generalised to find the sum of first n terms of an AP as

$$S_n = \frac{n}{2} \left[ 2a + (n-1)d \right]$$

# OBSERVATION

On actual measurement:

So, 
$$S_n = \frac{n}{2} [-+(n-1)-]$$
.

## **APPLICATION**

This result may be used to find the sum of first n terms of the list of numbers :

1. 
$$1^2$$
,  $2^2$ ,  $3^2$ , ...

2. 
$$1^3$$
,  $2^3$ ,  $3^3$ , ...

to be studied in Class XI.

# Activity 10

## ORIECTIVE

To verify the distance formula by graphical method.

# MATERIAL REQUIRED

Cardboard, chart paper, graph paper, glue, pen/pencil and ruler.

## METHOD OF CONSTRUCTION

- 1. Paste a chart paper on a cardboard of a convenient size.
- 2. Paste the graph paper on the chart paper.
- 3. Draw the axes X'OX and Y'OY on the graph paper [see Fig. 1].
- 4. Take two points A(a, b) and B(c,d) on the graph paper and join them to get a line segment AB [see Fig. 2].

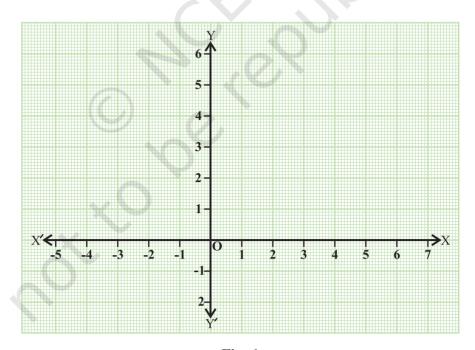


Fig. 1

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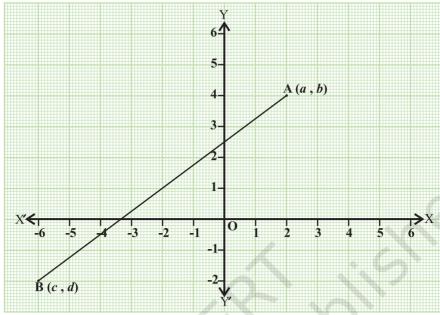


Fig. 2

## DEMONSTRATION

- 1. Calculate the distance AB using distance formula.
- 2. Measure the distance between the two points A and B using a ruler.
- 3. The distance calculated by distance formula and distance measured by the ruler are the same.

## **OBSERVATION**

- Coordinates of the point A are \_\_\_\_\_\_.
  Coordinates of the point B are \_\_\_\_\_\_.
- 2. Distance AB, using distance formula is \_\_\_\_\_\_.
- 3. Actual distance AB measured by ruler is \_\_\_\_\_\_
- 4. The distance calculated in (2) and actual distance measured in (3) are \_\_\_\_\_.

#### APPLICATION

The distance formula is used in proving a number of results in geometry.