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clc; clear; close all;

### **ME 456 CLT Project Code**

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#### **Number of Plies**

n = # plies vv = variable volume fraction 'yes' or 'no'
[n, vv] = numplies;

# **Engineering Parameters**

E1 = modulus 1 for each layer (Pa) E2 = modulus 2 for each layer G12 = shear modulus for each layer v12 = major poissons ratio for each layer t = thickness of each layer t =

[E1,E2,G12,v12,t,f,theta] = eparam(n,vv);

#### **Stiffness Tensors**

Q = stiffness tensor for each layer Qbar = stiffness tensor in global frame for each layer

[Q,Qbar,S] = Qcalc(n,E1,E2,G12,v12,theta);

#### **Macro Stiffness Constants**

A = laminate extensional stiffnesses (Pa m) B = laminate coupling stiffnesses (Pa m $^2$ ) A = laminate bending stiffnesses (Pa m $^3$ ) z =

```
[A,B,D,z] = macrostiffness(Qbar,t,n);
ABBD = [A B; B D];
```

# **Applied Forces**

[M,N] = appforces;

# **Display Values**

```
disp('IMLS matrix, HMS fiber, 0.75 vf')
disp('Q (GPa)')
disp(Q(:,:,1))
disp(['Qbar (GPa), rotation ', num2str(theta), ' degrees'])
disp(Qbar(:,:,1))
IMLS matrix, HMS fiber, 0.75 vf
Q (GPa)
  285.4521
                             0
            1.3448
    1.3448 5.3260
                             0
         0
                  0
                        4.0342
Qbar (GPa), rotation 45 degrees
   77.4011 69.3327
                       70.0315
   69.3327
             77.4011
                       70.0315
   70.0315
             70.0315
                       72.0221
```

### **Function numplies**

```
function [n, vv] = numplies
% Prompts user to input number of plies and then select yes or no for
% variable volume fraction
    prompt='Input number of plies:';
    name='Number of Plies';
    numlines=1;
    definput= {'1'};
    options.Resize= 'on';
    n = str2double(inputdlg(prompt, name, numlines, definput, options));
    vvf = questdlg({'Variable volume fraction?',...
        '(Yes allows user to input volume fraction)'},...
        'Input', 'Yes', 'No', 'Yes');
    switch vvf
        case 'No'
            vv = 0;
        case 'Yes'
            vv = 1;
    end
end
```

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### **Function eparam**

```
function [E1,E2,G12,v12,t,f,theta] = eparam(n,vv)
% Calculates layer properties for variable and nonvariable volume fraction
% Fiber material properties. E values in GPa
listfib = { 'Boron', 'HMS', 'AS', 'T300', 'KEV', 'S-G', 'E-G'};
Ef1a = [400 379 213.7 221 152 85.5 73.1];
Ef2a = [400 \ 6.21 \ 13.8 \ 13.8 \ 4.14 \ 85.5 \ 73.1];
vf12a = [0.2 \ 0.2 \ 0.2 \ 0.35 \ 0.2 \ 0.22];
Gf12a = [167 \ 7.58 \ 13.8 \ 8.96 \ 2.9 \ 35.6 \ 30.1];
% Matrix material properties. E values in GPa
listmat = {'LM','IMLS','IMHS','HM','Polyimide','PMR'};
Ema = [2.21 \ 3.45 \ 3.45 \ 5.17 \ 3.45 \ 3.24];
vma = [0.43 \ 0.41 \ 0.35 \ 0.35 \ 0.35 \ 0.36];
Gma = Ema./(2.*(1+vma));
% Composite material properties. E values in GPa
listcom = {'Boron/5505 boron/epoxy','AS/3501 carbon/epoxy',...
         'IM7/8551-7 carbon/epoxy', 'AS4/APC2 carbon/PEEK', 'B4/6061 boron/
aluminum',...
         'Kevlar 49/934 aramid/epoxy', 'Scotchply 1002 E-glass/epoxy',...
         'E-glass/470-36/vinyl ester'};
Ec1 = [204 \ 139 \ 162 \ 131 \ 235 \ 75.8 \ 38.6 \ 24.4];
Ec2 = [18.5 \ 9 \ 8.34 \ 8.7 \ 137 \ 5.5 \ 8.27 \ 6.87];
Gc12 = [5.59 \ 6.9 \ 2.07 \ 5 \ 47 \ 2.3 \ 4.14 \ 2.89];
vc12 = [0.23 \ 0.3 \ 0.34 \ 0.28 \ 0.3 \ 0.34 \ 0.26 \ 0.32];
fc = [0.5 \ 0.65 \ 0.6 \ 0.58 \ 0.5 \ 0.65 \ 0.45 \ 0.3];
% Preallocating arrays
f = zeros(1,n);
E1 = zeros(1,n);
v12 = zeros(1,n);
E2 = zeros(1,n);
G12 = zeros(1,n);
    if vv == 0 % no variable vf
         % Choose composite for all layers
         [composite] = choosecomposite;
         for i = 1:n
             E1(i) = Ec1(composite);
             v12(i) = vc12(composite);
             E2(i) = Ec2(composite);
             G12(i) = Gc12(composite);
             f(i) = fc(composite);
         end
    elseif vv == 1 % yes variable vf
         % Choose matrix for all layers
         [matrix] = choosematrix;
         for i = 1:n
```

```
% Choose fiber material for each layer
            [fiber] = choosefiber(i);
            % Fiber/matrix properties for chosen materials
            Ef1 = Ef1a(fiber);
            Ef2 = Ef2a(fiber);
            vf12 = vf12a(fiber);
            Gf12 = Gf12a(fiber);
            Em = Ema(matrix);
            vm = vma(matrix);
            Gm = Gma(matrix);
            % volume fraction input for each layer
            definput= {'0.5'};
            options.Resize= 'on';
            f(i) = str2double(inputdlg(['Input fiber volume fraction between 0
 and 1 for layer ', num2str(i)]...
            ,'Volume Fraction',1,definput,options));
            if f(i) < 0 \mid \mid f(i) > 1
                f(i) = 0.5;
            end
            % Properties for each layer calculated
            E1(i) = Ef1*f(i) + Em*(1-f(i));
            v12(i) = vf12*f(i) + vm*(1-f(i));
            E2(i) = Em*((1-sqrt(f(i)))+(sqrt(f(i))/(1-(sqrt(f(i)))*(1-(Em/(i))))
Ef2)))));
            G12(i) = Gm*((1-sqrt(f(i)))+(sqrt(f(i)))/(1-(sqrt(f(i)))*(1-(Gm/sqrt(f(i))))
Gf12)))));
        end
    end
    % Thickness of each layer (mm)
    t = zeros(1,n);
    for i = 1:n
        definput= {'0.25'};
        options.Resize= 'on';
        t(i) = str2double(inputdlg(['Input thickness (mm) for layer
 ',num2str(i)]...
        ,'Thickness',1,definput,options));
        if t(i) <= 0
            t(i) = 0.0025;
        end
    end
    % Orientation angle for each layer
    theta = zeros(1,n);
    for i = 1:n
        definput= {'0'};
        options.Resize= 'on';
        theta(i) = str2double(inputdlg(['Input orientation angle (-90 to 90)
 for layer ', num2str(i)]...
        ,'Orientation',1,definput,options));
        if theta(i) < -90 || theta(i) > 90
            theta(i) = 0;
        elseif theta(i) == -90
            theta(i) = 90;
```

```
end
end
```

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### **Function choosecomposite**

```
function [composite] = choosecomposite
% Allows user to select from premade composite materials for all layers
    list = {'Boron/5505 boron/epoxy','AS/3501 carbon/epoxy',...
        'IM7/8551-7 carbon/epoxy', 'AS4/APC2 carbon/PEEK', 'B4/6061 boron/
aluminum',...
        'Kevlar 49/934 aramid/epoxy', 'Scotchply 1002 E-glass/epoxy',...
        'E-glass/470-36/vinyl ester'};
    [indx,tf] = listdlg('ListString',list,'PromptString',...
        'Select a composite material for all layers', 'SelectionMode',...
        'single','Name','Composite Material','ListSize',[250 115]);
    if tf == 0
        composite = 1;
    else
        composite = indx;
    end
end
```

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### **Function choosematrix**

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#### **Function choosefiber**

```
function [fiber] = choosefiber(i)
```

```
% Allows user to select fiber material from 7 different materials
   list = {'Boron', 'HMS', 'AS', 'T300', 'KEV', 'S-Glass', 'E-Glass'};
   [indx,tf] = listdlg('ListString', list, 'PromptString',...
        ['Select a fiber material for layer ',num2str(i)], 'SelectionMode',...
        'single', 'Name', 'Fiber Material', 'ListSize', [250 100]);
   if tf == 0
        fiber = 1;
   else
        fiber = indx;
   end
end
```

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#### **Function Qcalc**

```
function [Q,Qbar,S] = Qcalc(n,E1,E2,G12,v12,theta)
% Preallocate matrices
    Q = zeros(3,3,n);
    Qbar = zeros(3,3,n);
    S = zeros(3,3,n);
    for i = 1:n
        % Compliance value calculations
        S(1,1,i) = 1/E1(i);
        S(2,2,i) = 1/E2(i);
        S(1,2,i) = -v12(i)/E1(i);
        S(2,1,i) = S(1,2,i);
        S(3,3,i) = 1/G12(i);
        % Stiffness value calculations, fill Q matrix
        Q(1,1,i) = S(2,2,i)/(S(1,1,i)*S(2,2,i) - S(1,2,i)^2);
        Q(1,2,i) = -S(1,2,i)/(S(1,1,i)*S(2,2,i) - S(1,2,i)^2);
        Q(2,1,i) = Q(1,2,i);
        Q(2,2,i) = S(1,1,i)/(S(1,1,i)*S(2,2,i) - S(1,2,i)^2);
        Q(3,3,i) = 1/S(3,3,i);
        % Transformation matrix calculations
        s = sind(theta(i));
        c = cosd(theta(i));
        T = [c^2 s^2 2*c*s; s^2 c^2 -2*c*s; -c*s c*s c^2-s^2];
        T2 = [T(1,1) T(1,2) T(1,3)/2;...
            T(2,1) T(2,2) T(2,3)/2; 2*T(3,1) 2*T(3,2) T(3,3);
        % Qbar calculations: inv(T)*Q*T2
        Qbar(:,:,i) = TQ(:,:,i)*T2;
    end
end
```

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#### **Function macrostiffness**

```
function [A,B,D,z] = macrostiffness(Qbar,t,n)
% A,B,D macrostiffness matrix calculations (eqns: 7.41, 7.42, 7.43)
    % Distances z (mm)
    z = zeros(1,n+1);
    z(1) = -sum(t, 'all')/2;
    for i = 1:n
        z(i+1) = z(i) + t(i);
    end
    % Initialize A,B,D matrices
    A = zeros(3);
    B = zeros(3);
    D = zeros(3);
    for i = 1:n
        for r = 1:3
            for c = 1:3
                % A (laminate extensional stiffness) (GPa mm)
                A(r,c) = Qbar(r,c,i)*(z(i+1)-z(i)) + A(r,c);
                % B (laminate coupling stiffnesses) (GPa mm^2)
                B(r,c) = Qbar(r,c,i)*(z(i+1)^2-z(i)^2) + B(r,c);
                % D (laminate bending stiffnesses) (GPa mm^3)
                D(r,c) = Qbar(r,c,i)*(z(i+1)^3-z(i)^3) + D(r,c);
            end
        end
    end
    % Constants after summation (eqns: 7.42, 7.43)
    B = B/2;
    D = D/3;
end
```

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