

H22 院試 (情報科学研究科) ① (藤原由来)

① アルゴリズム

※ 選択 ⑧ ⑨

論理学 計算理論

(1) 71, 77-1

(2) 1回目 30 10 20 40 70 80 60 50

3回目 10 20 30 40 70 80 60 50

37 20 40 60 80 10 50 30 70

(4) (4-1) $2(n-1)+1 = 2n-1$ (4-2) $O(n^2)$

(4-3) 最悪ケース

② 論理回路

(1) (1-1)

a, a_0	b, b_0	$S=0(\text{Max})$ C_1, C_0	$S=1(\text{Min})$ C_1, C_0
0 0	0 0	0 0	0 0
0 0	0 1	0 1	0 0
0 0	1 0	1 0	0 0
0 0	1 1	1 1	0 0
0 1	0 0	0 1	0 0
0 1	0 1	0 1	0 1
0 1	1 0	1 0	0 1
0 1	1 1	1 1	0 1
1 0	0 0	1 0	0 0
1 0	0 1	1 0	0 1
1 0	1 0	1 0	1 0
1 0	1 1	1 1	1 0
1 1	0 0	1 1	0 0
1 1	0 1	1 1	0 1
1 1	1 0	1 1	1 0
1 1	1 1	1 1	1 1

ポイント:
下から順に
求めていく

20	40	60	80	10	50	30	70
20	40	60	80	10	50	30	70
20	40	60	80	10	50	30	70
20	40	60	80	10	50	30	70
20	40	60	80	10	50	30	70
20	40	60	80	10	50	30	70
20	40	60	80	10	50	30	70
20	40	60	80	10	50	30	70

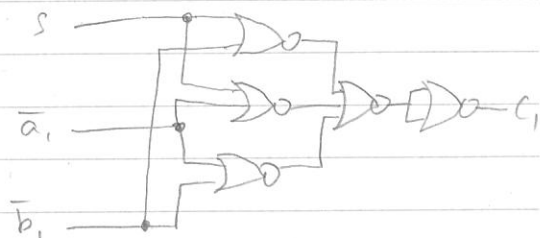
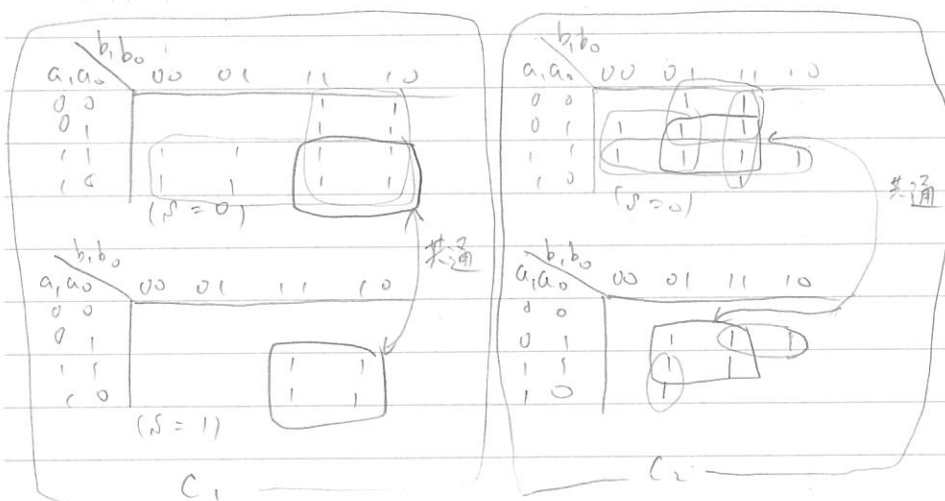
斜線: 終わったやつ

(1-2)

$$C_1 = \overline{S} a_1 \vee \overline{S} b_1 \vee a_1 b_1$$

$$= \overline{S} a_1 \vee \overline{S} b_1 \vee a_1 b_1$$

$$= (\overline{S} \vee a_1) \vee (\overline{S} \vee b_1) \vee a_1 b_1$$



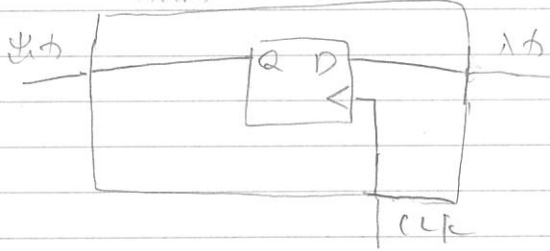
$$C_1 = \overline{S} a_1 \vee \overline{S} b_1 \vee a_1 b_1$$

$$C_2 = \overline{S} a_0 b_1 \vee \overline{S} a_1 b_0 \vee \overline{S} a_0 b_0 \vee \overline{S} b_1 b_0 \vee a_0 b_0 \vee S a_1 \overline{b_1} b_0 \vee S \overline{a_1} a_0 b_1$$

H22 (2) (解原)

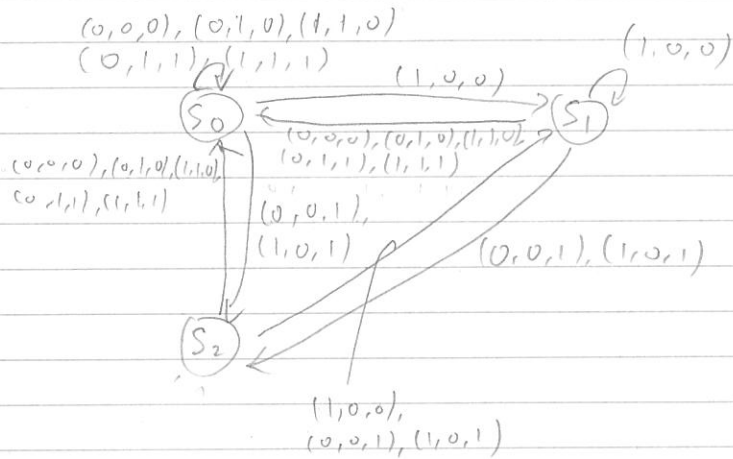
[2] (2) (2-1)

表示素子の制御回路

(2-2) (2-2-1) 入力: (In, R, c)

次状態

現状態	入力	$(R, c) = (0, 0)$	$(R, c) = (1, 0), (1, 1)$	$(R, c) = (0, 1)$
Q_1, Q_0	In	Q_1^+, Q_0^+	Q_1^+, Q_0^+	Q_1^+, Q_0^+
0 0	0	0 0	0 0	1 0
0 0	1	0 1	0 0	1 0
0 1	0	0 0	0 0	1 0
0 1	1	0 1	0 0	1 0
1 0	0	0 0	0 0	0 1
1 0	1	0 1	0 0	0 1
1 1	0	d d	d d	d d
1 1	1	d d	d d	d d



現状態

 Q_1, Q_0

出力

Q_1, Q_0	出力
0 0	0
0 1	1
1 0	0
1 1	d

(2-2-2)

 $Out = Q_0$

(2-2-3)

 $D_1 = \bar{R} C \bar{Q}_1$ $D_0 = \bar{R} \bar{C} In \vee \bar{R} C Q_1$

H22 院試 (3)

[3] 計算機システム・システム工学

(1) (1-1)

$x_1: 0101$

$x_2: 1010$

$y_1: -2^{n-1} + 1$

$y_2: 2^{n-1} - 1$

$x_3: 0101$

$x_4: 1011$

$y_3: -2^{n-1}$

$y_4: 2^{n-1} - 1$

(1-2) (1-2-1) $C_1 = a_0 \cdot b_0 + (a_0 + b_0) \cdot C_0$

(1-2-2) $G_0 = g_1 + g_0 \cdot P_1$

$P_0 = P_1 \cdot P_0$

(1-2-3) $C_0: 3T$

$T_0: 2T$

(1-2-4) C_1

1段目の $g_i, P_i: T$

2段目の (L_1, L_2) の $G_0: 2T$

3段目の (L_1) の $C_2: 2T$

以上より C_2 の累積遅延は $T + 2T + 2T = 5T$

(1-3) $z_1: \text{ア}$

$z_2: \text{イ}$

$z_3: \text{オ}$

$z_4: \text{エ}$

$z_5: \text{ウ}$

$z_6: \text{シ}$

(2) (2-1)

(a) ア

(b) イ

(c) ウ

(d) エ

(e) オ

(f) カ

(g) キ

(h) ク

(i) ケ

(j) コ

(k) サ

(l) シ

(m) セ

(n) ソ

(2-2) 手法 1: ① ③ ③

2: ① ③

3: ① ② ③

(4: ① ② ③) ← 解答用紙の解答例

H22 院試④ (藤原)

[8] (1)

$$(1-1) \quad P(a) \rightarrow \forall x P(x) = \neg P(a) \vee \forall x P(x)$$

(b) (真) $D: \{1\}$ $C: a = 1$ $F: \text{なし}$ $P: P(x): \text{「} x = 1 \text{」}$ (偽) $D: \{0, 1\}$ $C, F, P: \text{同上}$

$$(1-2) \quad (\forall x P(x)) \rightarrow \forall x P(f(x)) = \exists x \neg P(x) \vee \forall x P(f(x))$$

(a)

$$(1-3) \quad (\exists x P(x)) \rightarrow \forall x P(x) = \forall x \neg P(x) \vee \forall x P(x)$$

(b) (真) $D: \{1\}$ $C, F: \text{なし}$ $P: P(x): \text{「} x = 1 \text{」}$ (偽) $D: \{0, 1\}$ $C, F: \text{なし}$ $P: P(x): \text{「} x = 1 \text{」}$

$$(1-4) \quad (\forall x \exists y P(x, y)) \rightarrow \exists y \forall x P(x, y)$$

$$= \exists x (\forall y \neg P(x, y) \vee \exists y \forall x P(x, y)) = \exists y \forall x (\neg P(y, x) \vee \forall x P(x, y))$$

(b) (真) $D: \{1\}$ $C, F: \text{なし}$ $P: p(x, y): \text{「} x = y \text{」}$ (偽) $D: \text{非負整数全体}$ $C, F: \text{なし}$ $P: p(x, y): \text{「} x \leq y \text{」}$

$$(1-5) \quad (\exists y \forall x (P(x, y) \rightarrow \forall x \exists y P(x, y))) \rightarrow \forall x \exists y P(x, y)$$

$$= \forall y \exists x (\neg P(x, y) \vee \forall x \exists y P(x, y))$$

$$= \forall x \exists y (\neg P(y, x) \vee \forall x \exists y P(x, y))$$

(a)

H22 院試⑤ (藤原)

[8] (2) (2-1)

$$\neg A = p(a, b)$$

$$\wedge \forall x \forall y \exists z (\neg p(x, y) \vee p(g(x, z), y))$$

$$\wedge \forall x \forall y (\neg p(x, y) \vee p(y, x))$$

$$\wedge \forall z \forall w \neg p(g(g(z, w), w), a)$$

$$= \forall x \forall y \exists z \forall w (p(a, b)$$

$$\wedge (\neg p(x, y) \vee p(g(x, z), y))$$

$$\wedge (\neg p(x, y) \vee p(y, x))$$

$$\wedge (\neg p(g(g(x, y), w), a))$$

(2-2) z は $\lambda x - \lambda y. P(g(x, y))$ に対して $f(x, y)$ は $f(x, y) = z$ である。

$$\forall x \forall y \forall w (p(a, b)$$

$$\wedge (\neg p(x, y) \vee p(g(x, f(x, y)), y))$$

$$\wedge (\neg p(x, y) \vee p(y, x))$$

$$\wedge (\neg p(g(g(x, y), w), a))$$

$$C_1 = p(a, b)$$

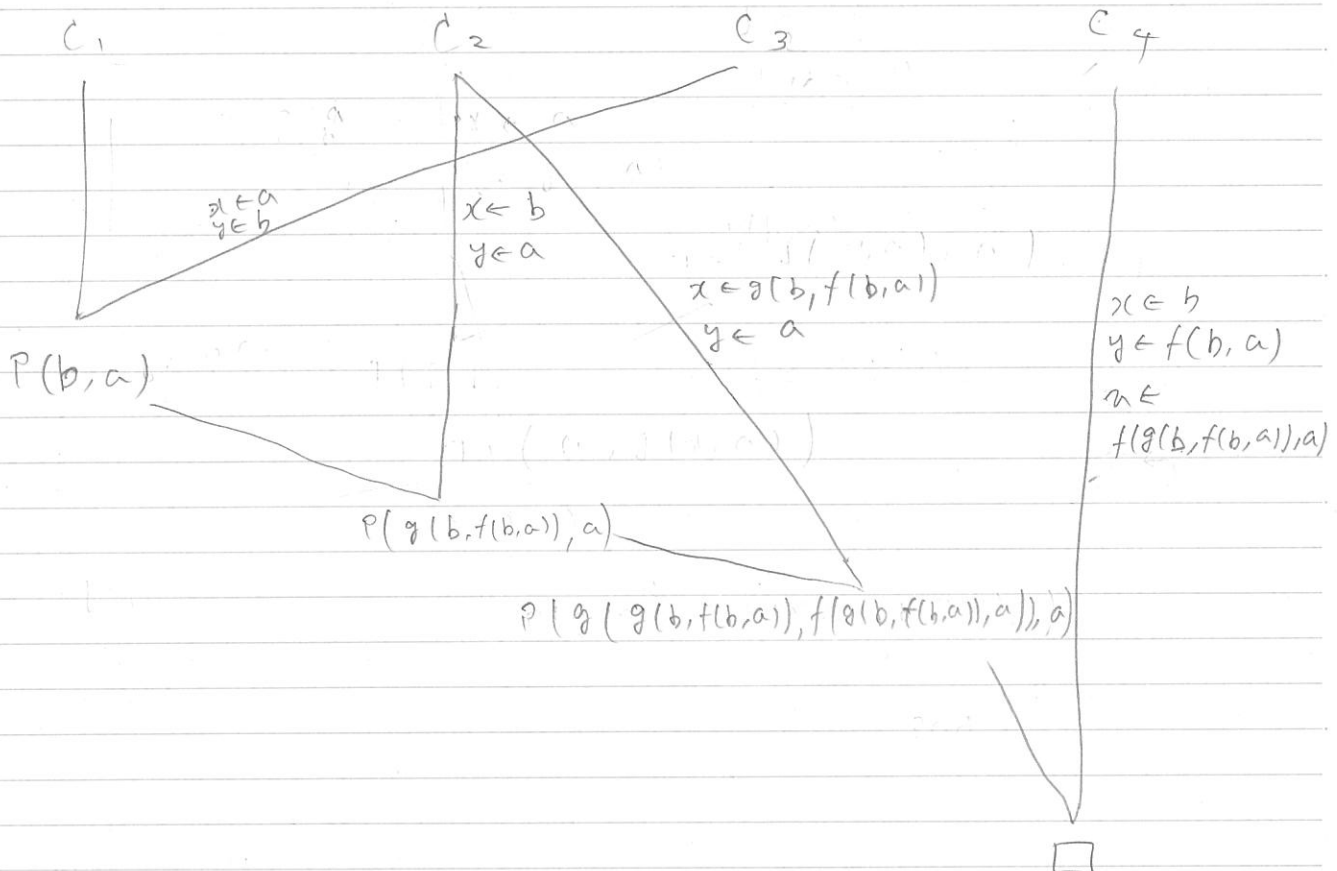
$$C_2 = \neg p(x, y) \vee p(g(x, f(x, y)), y)$$

$$C_3 = \neg p(x, y) \vee p(y, x)$$

$$C_4 = \neg p(g(g(x, y), w), a)$$

と C_1

(2-3)



H22 院試 (6) (藤原)

9 (1) (1-1) 1c 等価性文字列

k=1 0 1

p q s t u v r

00 00 00 01 00 01 01

k=2 0 1 2

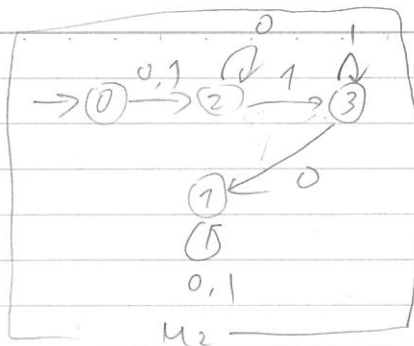
p q s u t v r

11 00 00 00 12 12 02

k=3 0 1 2 3

p q s u t v r

22 11 11 11 23 23 13



(1-2) M3: (e)

M4: (b)

M5: (h)

(?)

M3

$$p = 0p + 1r + \epsilon - (1)$$

$$q = 0p + 1r - (2)$$

$$r = 0q + 1r - (3)$$

$$(3) \text{より } r = 1 * 0q$$

$$q = 0p + 1 * 0q$$

$$q = (11 * 0) * 0p$$

$$p = 0p + 1 * 0(11 * 0) * 0p + \epsilon$$

$$p = (0 + 11 * 0(11 * 0) * 0) * \epsilon$$

$$= (0 * 11 * 0(11 * 0) * 0) * \epsilon \quad (?)$$

M4

$$p = 0p + 1q + \epsilon - (1)$$

$$q = 0q + 1r - (2)$$

$$r = 0p + 1r - (3)$$

$$(3) \text{より } r = 1 * 0p$$

$$(3) \text{より } q = 0 * 1r = 0 * 1 * 0p$$

$$p = (0 + 10 * 1 * 0) p + \epsilon$$

$$p = (0 + 10 * 1 * 0) *$$

$$M5 \begin{cases} p = 0p + 1r + \epsilon - (1) \\ q = 0p + 1s - (2) \\ r = 0q + 1s - (3) \\ s = 1s + 1q - (4) \end{cases}$$

$$(4) \text{より } s = 0 * 1q$$

$$(4) \text{より } q = 0p + 10 * 1q$$

$$q = (10 * 1)q + 0p$$

$$q = (10 * 1) * 0p$$

$$r = (0 + 10 * 1)q$$

$$= (0 + 10 * 1)(10 * 1) * 0p$$

$$p = (0 + 1(0 + 10 * 1)(10 * 1) * 0) p + \epsilon$$

$$p = (0 + 1(0 + 10 * 1)(10 * 1) * 0) *$$

(1-3) (1) (0, A) / AAA

(2) (1, A) / A

(3) (0, A) / \epsilon

H22 院試 ⑦ (藤原)

[9] (2/ (2-1)) $G_2 (V_1, T_1, P_2, S_1)$

$$P_2 = \{ \begin{array}{l} S \rightarrow A | AB, \\ A \rightarrow AD | ACD | ABD | ABCD, \\ B \rightarrow C, B \rightarrow b, \\ C \rightarrow B, C \rightarrow c, D \rightarrow d \end{array} \}$$

(2-2) 生成規則が

$$A \rightarrow a \text{ か } A \rightarrow BC.$$

の形しかとる文法。(a: 終端記号, A, B, C: 非終端記号)

(2-3) $G_4 (V_4, T_3, P_4, S_3)$

$$V_4 = \{ S, A, B, C, D, E \}$$

$$P_3 = \{ \begin{array}{l} S \rightarrow CB, B \rightarrow b, \\ C \rightarrow DA, \\ D \rightarrow AE, E \rightarrow a, \\ A \rightarrow AA, A \rightarrow a \end{array} \}$$