# Towards an Understanding of the Correlations in Jet Substructure

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#### Abstract Abstract for BOOST2013 report

- 2 **Keywords** boosted objects · jet substructure ·
- $_{3}~$  beyond-the-Standard-Model physics searches  $\cdot$  Large
- 4 Hadron Collider

#### 5 1 Introduction

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The characteristic feature of collisions at the LHC is a center-of-mass energy, 7 TeV in 2010 and 2011, of 8 TeV in 2012, and near 14 TeV with the start of the second  $^{59}$ phase of operation in 2015, that is large compared to even the heaviest of the known particles. Thus these 10 particles (and also previously unknown ones) will often 11 be produced at the LHC with substantial boosts. As a 12 result, when decaying hadronically, these particles will  $^{64}\,$ not be observed as multiple jets in the detector, but  $^{\rm 65}$ rather as a single hadronic jet with distinctive internal 66 substructure. This realization has led to a new era of sophistication in our understanding of both standard  $^{68}$ 17 QCD jets and jets containing the decay of a heavy particle, with an array of new jet observables and detection 19 techniques introduced and studies. To allow the efficient 20 sharing of results from these jet substructure studies a 21 series of BOOST Workshops have been held on a yearly 22 basis: SLAC (2009,  $\cite{Mathematical Property}$ ), Oxford University (2010,  $\cite{Mathematical Property}$ ),  $\cite{Mathematical Property}$ Princeton University University (2011, [?]), IFIC Va-24 lencia (2012 [?]), University of Arizona (2013 [?]), and, 74 most recently, University College London (2014 [?]). Af-75 26 ter each of these meetings Working Groups have func-76 27 tioned during the following year to generate reports 77 28 highlighting the most interesting new results, includ-78 29 ing studies of ever maturing details. Previous BOOST 79 reports can be found at [?,?,?]. 31

This report from BOOST 2013 thus views the study  $_{\rm 81}$ and implementation of jet substructure techniques as a fairly mature field, and focuses on the question of the correlations between the plethora of observables that 82 have been developed and employed, and their dependence on the underlying jet parameters, especially the 83 jet radius R and jet  $p_T$ . Samples of quark-, gluon-, W- 84 and Top-initiated jets are reconstructed at the particle- 85 level using FastJet[REF], and the performance, in 86 terms of separating signal from background, of vari-87 ous groomed jet masses and jet substructure observ-88 ables investigated through Receiver Operating Char-89 acteristic (ROC) curves, which show the efficiency to 90 "tag" the signal as a function of the efficiency (or re-91 jection, being 1/efficiency) to "tag" the background. 92 We investigate the separation of a quark signal from 93 a gluon background (q/g tagging), a W signal from a 94

gluon background (W-tagging) and a Top signal from a mixed quark/gluon QCD background (Top-tagging). In the case of Top-tagging, we also investigate the performance of dedicated Top-tagging algorithms, the Hep-TopTagger[REF] and John Hopkins Tagger[REF]. Using multivariate techniques, we study the degree to which the discriminatory information provided by the observables and taggers overlaps, by examining in particular the extent to which the signal-background separation performance increases when two or more variables/taggers are combined, via a Boosted Decision Tree (BDT), into a single discriminant.

The report is organized as follows. In Section 2 we describe the generation of the Monte Carlo event samples that we use in the studies that follow. In Section 3 we detail the jet algorithms, observables and taggers investigated in each section of the report, and in Section 4 the multivariate techniques used to combine the one or more of the observables into single discriminants. In Section 5 we describe the q/g-tagging studies, in Section 6 we describe the W-tagging studies, and in Section 7 we describe the Top-tagging studies. Finally we offer some summary of the studies and general conclusions in Section 8.

# 2 Monte Carlo Samples

In the below sections the Monte Carlo samples used in the q/g tagging, W tagging and Top tagging sections of this report are described. Note that in all cases the samples used contain no additional proton-proton interactions beyond the hard scatter (no pile-up), and there is no attempt to emulate the degradation in angular and  $p_T$  resolution that would result when reconstructing the jets inside a real detector.

# 2.1 Quark/gluon and W tagging

Samples were generated at  $\sqrt{s}=8$  TeV for QCD dijets, and for  $W^+W^-$  pairs produced in the decay of a (pseudo) scalar resonance and decaying hadronically. The QCD events were split into subsamples of gg and  $q\bar{q}$  events, allowing for tests of discrimination of hadronic W bosons, quarks, and gluons.

Individual gg and  $q\bar{q}$  samples were produced at leading order (LO) using MadGraph5, while  $W^+W^-$  samples were generated using the JHU Generator to allow for separation of longitudinal and transverse polarizations. Both were generated using CTEQ6L1 PDFs[REF]. The samples were produced in exclusive  $p_T$  bins of width 100 GeV, with the slicing parameter chosen to be the  $p_T$  of any final state parton or W at LO. At

the parton-level the  $p_T$  bins investigated were 300-400<sub>139</sub> GeV, 500-600 GeV and 1.0-1.1 TeV. Since no match-140 ing was performed, a cut on any parton was equivalent.<sub>141</sub> The samples were then all showered through Pythia8<sub>142</sub> (version 8.176)[REF]using the default tune 4C[REF].

ED: Need to report the size of the samples used

103 2.2 Top tagging

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Samples were generated at  $\sqrt{s} = 14$  TeV. Standard 104 Model dijet and top pair samples were produced with 105 Sherpa 2.0.0[REF], with matrix elements of up to two<sup>143</sup> 106 extra partons matched to the shower. The top sam-144 107 ples included only hadronic decays and were generated  $^{145}$ 108 in exclusive  $p_T$  bins of width 100 GeV, taking as slic-<sup>146</sup> 109 ing parameter the maximum of the top/anti-top  $p_T$ .<sup>147</sup> The QCD samples were generated with a cut on the <sup>148</sup> 111 leading parton-level jet  $p_T$ , where parton-level jets are <sup>149</sup> 112 clustered with the anti- $k_t$  algorithm and jet radii of 150 113 R = 0.4, 0.8, 1.2. The matching scale is selected to be <sup>151</sup> 114  $Q_{\text{cut}} = 40,60,80 \text{ GeV} \text{ for the } p_{T \text{ min}} = 600,1000, \text{ and}^{152}$ 115 1500 GeV bins, respectively. **ED: Need to report the**<sup>153</sup> 116 size of the samples used

# 3 Jet Algorithms and Substructure Observables<sup>155</sup>

In this section, we define the jet algorithms and observables used in our analysis. Over the course of our study, we considered a larger set of observables, but for the final analysis, we eliminated redundant observables for presentation purposes. In Sections 3.1, 3.2, 3.3 and 3.4 we first describe the various jet algorithms, groomers, taggers and other substructure variables used in these studies.

#### 3.1 Jet Clustering Algorithms

Jet clustering: Jets were clustered using sequential jet clustering algorithms [REF] implemented in FAST-163 JET 3.0.3. Final state particles i, j are assigned a mutual distance  $d_{ij}$  and a distance to the beam,  $d_{iB}$ . The particle pair with smallest  $d_{ij}$  are recombined and the algorithm repeated until the smallest distance is instead the distance to the beam,  $d_{iB}$ , in which case i is set aside and labelled as a jet. The distance metrics are defined as

$$d_{ij} = \min(p_{Ti}^{2\gamma}, p_{Tj}^{2\gamma}) \frac{\Delta R_{ij}^2}{R^2}, \tag{1}_{166}$$

$$d_{iB} = p_{Ti}^{2\gamma}, (2)_{_{168}}^{^{167}}$$

where  $\Delta R_{ij}^2 = (\Delta \eta)^2 + (\Delta \phi)^2$ . In this analysis, we use the anti- $k_t$  algorithm  $(\gamma = -1)$ , the Cambridge/Aachem 170

(C/A) algorithm  $(\gamma = 0)[\mathbf{REF}]$ , and the  $k_t$  algorithm  $(\gamma = 1)[\mathbf{REF}]$ , each of which has varying sensitivity to soft radiation in defining the jet.

**Qjets:** We also perform non-deterministic jet clustering [**REF**]. Instead of always clustering the particle pair with smallest distance  $d_{ij}$ , the pair selected for combination is chosen probabilistically according to a measure

$$P_{ij} \propto e^{-\alpha (d_{ij} - d_{\min})/d_{\min}},\tag{3}$$

where  $d_{\rm min}$  is the minimum distance for the usual jet clustering algorithm at a particular step. This leads to a different cluster sequence for the jet each time the Qjet algorithm is used, and consequently different substructure properties. The parameter  $\alpha$  is called the rigidity and is used to control how sharply peaked the probability distribution is around the usual, deterministic value. The Qjets method uses statistical analysis of the resulting distributions to extract more information from the jet than can be found in the usual cluster sequence. We use  $\alpha=0.1$  and 25 trees per event for all the studies presented here.

#### 3.2 Jet Grooming Algorithms

**Pruning:** Given a jet, re-cluster the constituents using the C/A algorithm. At each step, proceed with the merger as usual unless both

$$\frac{\min(p_{Ti}, p_{Tj})}{p_{Tij}} < z_{\text{cut}} \text{ and } \Delta R_{ij} > \frac{2m_j}{p_{Tj}} R_{\text{cut}}, \tag{4}$$

in which case the merger is vetoed and the softer branch discarded. The default parameters used for pruning [REF]in this study are  $z_{\rm cut}=0.1$  and  $R_{\rm cut}=0.5$ . One advantage of pruning is that the thresholds used to veto soft, wide-angle radiation scale with the jet kinematics, and so the algorithm is expected to perform comparably over a wide range of momenta.

**Trimming:** Given a jet, re-cluster the constituents into subjets of radius  $R_{\rm trim}$  with the  $k_t$  algorithm. Discard all subjets i with

$$p_{Ti} < f_{\text{cut}} \, p_{TJ}. \tag{5}$$

The default parameters used for trimming [REF] in this study are  $R_{\text{trim}} = 0.2$  and  $f_{\text{cut}} = 0.03$ .

Filtering: [REF] Given a jet, re-cluster the constituents into subjets of radius  $R_{\rm filt}$  with the C/A algorithm. Redefine the jet to consist of only the hardest N subjets, where N is determined by the final state topology and

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is typically one more than the number of hard prongs in 207 the resonance decay (to include the leading final-state 208 gluon emission). **ED: Do we actually use filtering** 209 as described here anywhere? (BS: Yes, it is used 210 in the HEPTopTagger.)

**Soft drop:** Given a jet, re-cluster all of the constituents<sub>13</sub> using the C/A algorithm. Iteratively undo the last stage<sub>214</sub> of the C/A clustering from j into subjets  $j_1$ ,  $j_2$ . If

$$\frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} < z_{\text{cut}} \left(\frac{\Delta R_{12}}{R}\right)^{\beta}, \tag{6}$$

discard the softer subjet and repeat. Otherwise, take  $j_{220}$  to be the final soft-drop jet[**REF**]. Soft drop has  $two_{221}$  input parameters, the angular exponent  $\beta$  and the soft- $j_{222}$  drop scale  $j_{222}$  drop scale  $j_{223}$  drop actually functions as a tagger when  $j_{223}$  drop actually functions as a tagger when  $j_{223}$ 

#### 3.3 Jet Tagging Algorithms

Modified Mass Drop Tagger: Given a jet, re-cluster<sub>229</sub> all of the constituents using the C/A algorithm. Iteratively undo the last stage of the C/A clustering from  $j_{231}$  into subjets  $j_1$ ,  $j_2$  with  $m_{j_1} > m_{j_2}$ . If either

$$m_{j_1} > \mu \, m_j \text{ or } \frac{\min(p_{T1}^2, p_{T2}^2)}{m_j^2} \, \Delta R_{12}^2 < y_{\text{cut}},$$
 (7)<sub>234</sub>

then discard the branch with the smaller transverse<sup>236</sup> mass  $m_T = \sqrt{m_i^2 + p_{Ti}^2}$ , and re-define j as the branch<sup>237</sup> with the larger transverse mass. Otherwise, the jet is tagged. If de-clustering continues until only one branch<sup>239</sup> remains, the jet is untagged. In this study we use by<sup>240</sup> default  $\mu = 1.0$  and  $y_{\rm cut} = 0.1$ .

**Johns Hopkins Tagger:** Re-cluster the jet using the  $^{243}$ C/A algorithm. The jet is iteratively de-clustered, and at each step the softer prong is discarded if its  $p_{\rm T}$  is less than  $\delta_p p_{\mathrm{T\,jet}}$ . This continues until both prongs are <sup>244</sup> harder than the  $p_{\rm T}$  threshold, both prongs are softer than the  $p_{\rm T}$  threshold, or if they are too close ( $|\Delta \eta_{ij}|$  +  $|\Delta\phi_{ij}|<\delta_R$ ); the jet is rejected if either of the latter conditions apply. If both are harder than the  $p_{\rm T}$  threshold, the same procedure is applied to each: this results in 2, 3, or 4 subjets. If there exist 3 or 4 subjets, then the jet is accepted: the top candidate is the sum of the subjets, and W candidate is the pair of subjets closest to the W mass. The output of the tagger is  $m_t$ ,  $m_W$ , and  $\theta_h$ , a helicity angle defined as the angle, measured in the rest frame of the W candidate, between the top<sub>245</sub> direction and one of the W decay products. The two<sub>246</sub> free input parameters of the John Hopkins tagger in<sub>247</sub>

this study are  $\delta_p$  and  $\delta_R$ , defined above.

**HEPTopTagger:** Re-cluster the jet using the C/A algorithm. The jet is iteratively de-clustered, and at each step the softer prong is discarded if  $m_1/m_{12} > \mu$  (there is not a significant mass drop). Otherwise, both prongs are kept. This continues until a prong has a mass  $m_i < m$ , at which point it is added to the list of subjets. Filter the jet using  $R_{\text{filt}} = \min(0.3, \Delta R_{ij})$ , keeping the five hardest subjets (where  $\Delta R_{ij}$  is the distance between the two hardest subjets). Select the three subjets whose invariant mass is closest to  $m_t$ . The output of the tagger is  $m_t$ ,  $m_W$ , and  $\theta_h$ , a helicity angle defined as the angle, measured in the rest frame of the W candidate, between the top direction and one of the W decay products. The two free input parameters of the HEP-TopTagger in this study are m and  $\mu$ , defined above.

Top Tagging with Pruning: For comparison with the other top taggers, we add a W reconstruction step to the trimming algorithm described above. A W candidate is found as follows: if there are two subjets, the highest-mass subjet is the W candidate (because the W prongs end up clustered in the same subjet); if there are three subjets, the two subjets with the smallest invariant mass comprise the W candidate. In the case of only one subjet, no W is reconstructed.

Top Tagging with Trimming: For comparison with the other top taggers, we add a W reconstruction step to the trimming algorithm described above. A W candidate is found as follows: if there are two subjets, the highest-mass subjet is the W candidate (because the W prongs end up clustered in the same subjet); if there are three subjets, the two subjets with the smallest invariant mass comprise the W candidate. In the case of only one subjet, no W is reconstructed.

#### 3.4 Other Jet Substructure Observables

**Qjet mass volatility:** As described above, Qjet algorithms re-cluster the same jet non-deterministically to obtain a collection of interpretations of the jet. For each jet interpretation, the pruned jet mass is computed with the default pruning parameters. The mass volatility,  $\Gamma_{\text{Qjet}}$ , is defined as

$$\Gamma_{\text{Qjet}} = \frac{\sqrt{\langle m_J^2 \rangle - \langle m_J \rangle^2}}{\langle m_J \rangle},$$
(8)

where averages are computed over the Qjet interpretations. 248

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N-subjettiness: N-subjettiness[**REF**]quantifies how<sub>270</sub> well the radiation in the jet is aligned along N direc-<sub>271</sub> tions. To compute N-subjettiness,  $\tau_N^{(\beta)}$ , one must first<sub>272</sub> identify N axes within the jet. Then,

$$au_{N} = rac{1}{d_{0}} \sum_{i} p_{Ti} \min\left(\Delta R_{1i}^{\beta}, \dots, \Delta R_{Ni}^{\beta}\right),$$
 (9)<sub>275</sub>

where distances are between particles i in the jet and<sub>277</sub> the axes.

$$d_0 = \sum_i p_{Ti} R^{\beta} \tag{10}_{279}$$

and R is the jet clustering radius. The exponent  $\beta$  is  $_{1281}$  a free parameter. There is also some choice in how the axes used to compute N-subjettiness are determined. The optimal configuration of axes is the one that  $\min_{282}$  imizes N-subjettiness; recently, it was shown that the "winner-takes-all" (WTA) axes can be easily computed and have superior performance compared to other  $\min_{284}$  imization techniques [REF]. We use both the WTA and one-pass  $k_t$  optimization axes in our analyses.

A more powerful discriminant is often the ratio,

$$\tau_{N,N-1} \equiv \frac{\tau_N}{\tau_{N-1}}.\tag{11}_{289}^{288}$$

While this is not an infrared-collinear (IRC) safe observable, it is calculable [**REF**] and can be made IRC<sup>291</sup> safe with a loose lower cut on  $\tau_{N-1}$ .

**Energy correlation functions:** The transverse mo-<sup>294</sup> mentum version of the energy correlation functions are<sup>295</sup> defined as [**REF**]:

$$ECF(N,\beta) = \sum_{i_1 < i_2 < \dots < i_N \in j} \left( \prod_{a=1}^{N} p_{Ti_a} \right) \left( \prod_{b=1}^{N-1} \prod_{c=b+1}^{N} \Delta R_{i_b i_c} \right)$$

where i is a particle inside the jet. It is preferable to work in terms of dimensionless quantities, particularly the energy correlation function double ratio:

$$C_N^{(\beta)} = \frac{\text{ECF}(N+1,\beta) \, \text{ECF}(N-1,\beta)}{\text{ECF}(N,\beta)^2}.$$
 (13)<sup>303</sup>

This observable measures higher-order radiation from<sup>305</sup> leading-order substructure.

# 4 Multivariate Analysis Techniques

Multivariate techniques are used to combine variables into an optimal discriminant. In all cases variables are combined using a boosted decision tree  $(BDT)_{313}$  as implemented in the TMVA package [?]. We use the BDT implementation including gradient boost. An example of the BDT settings are as follows:

- NTrees=1000
- BoostType=Grad
- Shrinkage=0.1
- UseBaggedGrad=F
- nCuts=10000
- MaxDepth=3
- UseYesNoLeaf=F
- nEventsMin=200

Exact parameter values are chosen to best reduce the effect of overtraining. **ED:** Can we describe a bit more the tests we do to ensure that we are not suffering from overtraining?

#### 5 Quark-Gluon Discrimination

In this section, we examine the differences between quarkand gluon-initiated jets in terms of substructure variables, and to determine to what extent these variables are correlated. Along the way, we provide some theoretical understanding of these observables and their performance. The motivation for these studies comes not only from the desire to "tag" a jet as originating from a quark or gluon, but also to improve our understanding of the quark and gluon components of the QCD backgrounds relative to boosted resonances. While recent studies have suggested that quark/gluon tagging efficiencies depend highly on the Monte Carlo generator used[REF], we are more interested in understanding the scaling performance with  $p_T$  and R, and the correlations between observables, which are expected to be treated consistently within a single shower scheme.

5.1 Methodology

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These studies use the qq and gg MC samples, described previously in Section 2. The showered events were clustered with FASTJET 3.03[REF]using the anti- $k_T$  algorithm[REF]with jet radii of  $R=0.4,\,0.8,\,1.2$ . In both signal (quark) and background (gluon) samples, an upper and lower cut on the leading jet  $p_T$  is applied after showering/clustering, to ensure similar  $p_T$  spectra for signal and background in each  $p_T$  bin. The bins in leading jet  $p_T$  that are considered are 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV, for the 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV parton  $p_T$  slices respectively. Various jet grooming approaches are applied to the jets, as described in Section 3.4. Only leading and subleading jets in each sample are used. The following observables are studied in this section:

- The ungroomed jet mass, m.

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– 1-subjettiness,  $\tau_1^{\beta}$  with  $\beta=1,\,2.$  The N-subjettiness<sub>367</sub> axes are computed using one-pass  $k_t$  axis optimiza-368 tion.

- 1-point energy correlation functions,  $C_1^{(\beta)}$  with  $\beta = 370$ 1, 2.
- The pruned Qjet mass volatility,  $\Gamma_{\rm Qjet}$ .
- The number of constituents ( $N_{\text{constits}}$ ).

# 5.2 Single Variable Discrimination

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Figure 1 shows the mass of jets in the quark and gluon samples when using different groomers, and the ungroomed jet mass, for jets with R=0.8 and in the  $p_T = ^{379}$  500 - 600 GeV bin. Qualitatively, the application of grooming shifts the mass distributions towards lower values when compared to the ungroomed mass, as expected. No clear gain in discrimination can be seen, and for certain grooming parameters, such as the use of soft drop with  $\beta = -1$  a clear loss in discrimination power is observed; this is because the soft-drop condition for  $\beta = -1$  discards collinear radiation, and the differences between quarks and gluons are manifest in the collinear structure (spin, splitting functions, etc.).

The quark and gluon distributions of different sub-structure variables are shown in Figure 2. Among those considered, one can see by eye that  $n_{\text{constits}}$  provides the highest separation power, followed by  $C_1^{\beta=0}$  and  $C_1^{\beta=1}$ , as was also found by the CMS and ATLAS Collaborations [**REF**].

To more quantitatively study the power of each ob-396 servable as a discriminator for quark/gluon tagging,  $^{\rm 397}$ ROC curves are built by scanning each distribution and plotting the background efficiency (to select gluon jets) vs. the signal efficiency (to select quark jets). Fig-400 ure 3 shows these ROC curves for all of the substructure  $^{\scriptscriptstyle 401}$ variables shown in Figure 2, along with the ungroomed 402 mass, representing the best performing mass variable,  $^{403}$ for R=0.4, 0.8 and 1.2 jets in the  $p_T = 300 - 400 \text{ GeV}^{404}$ bin. In addition, the ROC curve for a tagger built from  $^{405}\,$ a BDT combination of all the variables (see Section 4)  $^{406}\,$ is shown. Clearly,  $n_{\rm constits}$  is the best performing variable for all Rs, even though  $C_1^{\beta=0}$  is close, particularly for R=0.8. Most other variables have similar perfor- $^{409}$ mance, except  $\Gamma_{\mathrm{Qjet}}$ , which shows significantly worse<sup>410</sup> discrimination (this may be due to our choice of rigid-  $^{411}\,$ ity  $\alpha=0.1,$  with other studies suggesting that a smaller  $^{\mbox{\tiny 412}}$ value, such as  $\alpha = 0.01$ , produces better results [**REF**]). The combination of all variables shows somewhat better<sub>413</sub> discrimination.

We now examine how performance of masses and  $^{414}$  substructure observables changes with  $p_T$  and R. For  $^{415}$  jet masses, few variations are observed as the radius pa- $^{416}$  rameter of the jet reconstruction is increased in the two  $^{417}$ 

highest  $p_T$  bins; this is because the radiation is more collimated and the dependence on R is consequently smaller. However, for the 300-400 GeV bin, the use of small-R jets produces a shift in the mass distributions towards lower values, so that large-R jet masses are more stable with  $p_T$  and small-R jet masses are smaller at low- $p_T$  as expected from the spatial constraints imposed by the R parameter. These statements are explored more quantitatively later in this section. (BS: Do we have plots for this?)

The evolution of some of the substructure variable distributions with  $p_T$  and R is less trivial than for the jet masses. In particular, changing the R parameter at high  $p_T$  changes significantly the  $C_a^\beta$  for  $\beta>0$  and the  $n_{\rm constits}$  distributions, while leaving all other distributions qualitatively unchanged. This is illustrated in Figure 4 for  $\beta=0$  and  $\beta=1$  using a=1 in both cases for jets with  $p_T=1.0-1.1$  TeV.

The shift towards lower values with changing R is evident for the  $C_1^{\beta=1}$  distributions, while the stability of  $C_1^{\beta=0}$  can also be observed. These features are present in all  $p_T$  bins studied, but are even more pronounced for lower  $p_T$  bins. The shape of the Q-jet volatility distribution shows some non-trivial shape that deserves some explanation. Two peaks are observed, one at low volatility values and one at mid-volatility. These peaks are generated by two somewhat distinct populations. The high volatility peak arises from jets that get their mass primarily from soft (and sometimes wide-angle) emissions. The removal of some of the constituents when building Q-jets thus changes the mass significantly, increasing the volatility. The lower volatility peak corresponds to jets for which mass is generated by a hard emission, which makes the fraction of Q-jets that change the mass significantly to be smaller. Since the probability of a hard emission is proportional to the colour charge (squared), the volatility peak is higher for gluon jets by about the colour factor  $C_A/C_F$ .

In summary, the overall discriminating power between quarks and gluons decreases with increasing R due to the reduction in the amount of out-of-cone radiation differences and and increased contamination from the underlying event (**BS: is this ok?**). The broad performance features discussed for this  $p_T$  bin also apply to the higher  $p_T$  bins. These is further quantified in the next section.

#### 5.3 Combined Performance and Correlations

The quark/gluon tagging performance can be further improved over cuts on single observables by combining multiple observables in a BDT; due to the challenging nature of q/g-tagging, any improvement in per-

Boosted objects at the LHC

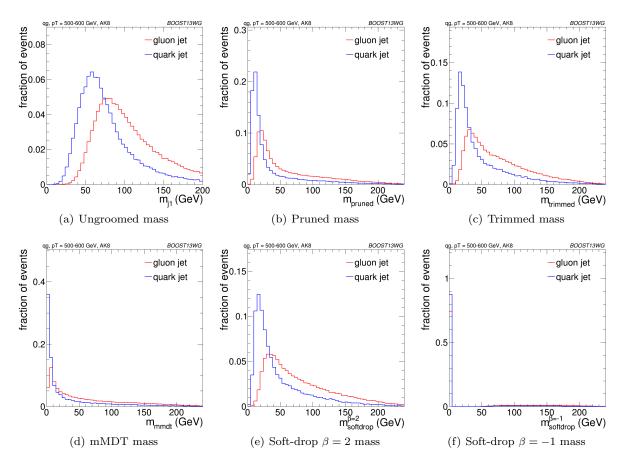


Fig. 1 Comparisons of ungroomed and groomed quark and gluon mass distributions for leading jets in the  $p_T = 500 - 600$  GeV bin using the anti- $k_{\rm T}$  R=0.8 algorithm.

formance with multivariable techniques could be crit-440 ical for certain analyses, and the improvement could441 be more substantial in data than the marginal benefit442 found in MC and shown in Fig. 3. Furthermore, insight443 can be gained into the features allowing for quark/gluon444 discrimination if the origin of the improvement is un-445 derstood. To quantitatively study this improvement, we446 build quark/gluon taggers from every pair-wise combi-447 nation of variables studied in the previous section for448 comparison with the all-variable combination.

In order to quantitatively study the value of each variable for quark/gluon tagging, we study the gluon variable for quark/gluon tagging, we study the gluon rejection, defined as  $1/\epsilon_{\rm gluon}$ , at a fixed quark selection for efficiency of 50% using jets with  $p_T=1-1.1$  TeV and or different R parameters. Figure 5 shows the gluon rejection for each pair-wise combination. The pair-wise gluon rejection at 50% quark efficiency can be compared to the single-variable values shown along the diagonal. The gluon rejection for the BDT all-variable combination is also shown on the bottom right of each plot. As already observed in the previous section,  $n_{\rm constits}$  is the most powerful single variable and  $C_1^{(\beta=0)}$  follows closely.

However, the gains are largely correlated; the combined performance of  $n_{\rm constits}$  and  $C_1^{(\beta=0)}$  is generally poorer than combinations of  $n_{\rm constits}$  with other jet substructure observables, such as  $\tau_1$ . Interestingly, in spite of the high correlation between  $n_{\rm constits}$  and  $C_1^{(\beta=0)}$ , the two-variable combinations of  $n_{\rm constits}$  generally fare worse than two-variable combinations with  $C_1^{(\beta=0)}$ . In particular, the combinations of  $\tau_1^{\beta=1}$  or  $C_1^{(\beta=1)}$  with  $n_{\rm constits}$  are capable of getting very close to the rejection achievable through the use of all variables for R=0.4 and R=0.8.

Tagger performance is generally better at small R. The overall loss in performance with increasing R can be seen in most single variables we study; this is expected, since more of the parton radiation is captured in the jet and more contamination from underlying event occurs, suppressing the differences between q/g jets. The principal exceptions are  $C_1^{(\beta=0)}$  and the Q-jet mass volatility, which are both quite resilient to increasing R. For  $C_1^{(\beta=0)}$ , this is due to the fact that the exponent on  $\Delta R$  is zero, and so soft radiation at the periphery of the jet does not substantially change the distribution;

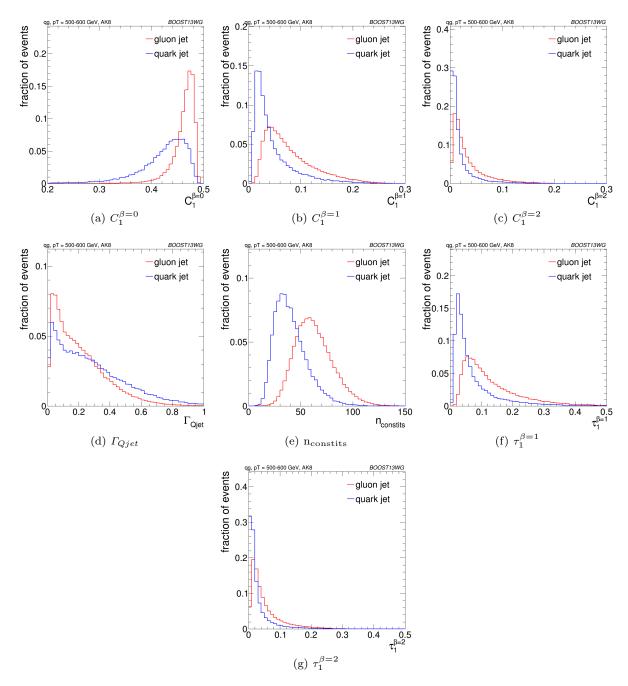


Fig. 2 Comparisons of quark and gluon distributions of different substructure variables for leading jets in the  $p_T = 500 - 600$  GeV bin using the anti- $k_T$  R=0.8 algorithm.

as a result, the performance is largely independent of  $R_{.470}$  Similarly, the soft radiation distant from the jet centre<sub>471</sub> will be vetoed during pruning regardless of the cluster<sub>472</sub> sequence, and so the R-dependence of  $\Gamma_{\rm Qjet}$  is not sig- $_{473}$  nificant. (BS: Check my logic?) Their combination, $_{,474}$  however, does perform slightly worse at larger R. (BS: $_{475}$  I don't understand this, but it is a  $\sim 10\%$  ef- $_{476}$  fect, so maybe not too significant?). By contrast, $_{,477}$ 

 $\tau_1^{(\beta=2)}$  and  $C_1^{(\beta=2)}$  are particularly sensitive to increasing R since, for  $\beta=2$ , large-angle emissions are given a larger weight.

These observations are qualitatively similar across all ranges of  $p_T$ . Quantitatively, however, there is a loss of rejection power for the taggers made of a combination of variables as the  $p_T$  decreases. This can be observed in Fig. 6 for anti- $k_T$  R=0.4 jets of different  $p_T$ s. Clearly, most single variables retain their gluon rejec-

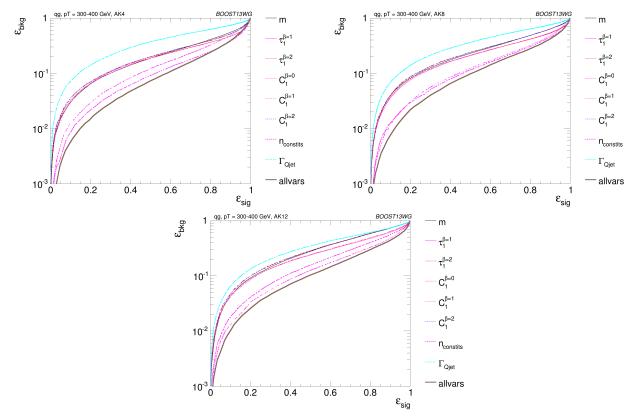


Fig. 3 The ROC curve for all single variables considered for quark-gluon discrimination in the  $p_T$  300-400 GeV bin using the anti- $k_T$  R=0.4, 0.8 and 1.2 algorithm.**ED: Hard to tell the lines on the plots apart** 

tion potential at lower  $p_T$ . However, when combined with other variables, the highest performing pairwise combinations lose ground with respect to other pairwise combinations. This is also reflected in the rejection of the tagger that uses a combination of all variables, which is lower at lower  $p_T$ s. [do we understand this?] (BS: This is a bit of a guess, but could it be that there is typically less radiation for low  $p_T$ , and so you're more sensitive to fluctuations; since you have less access to information, combinations of observables perform less well than at high  $p_T$ .)

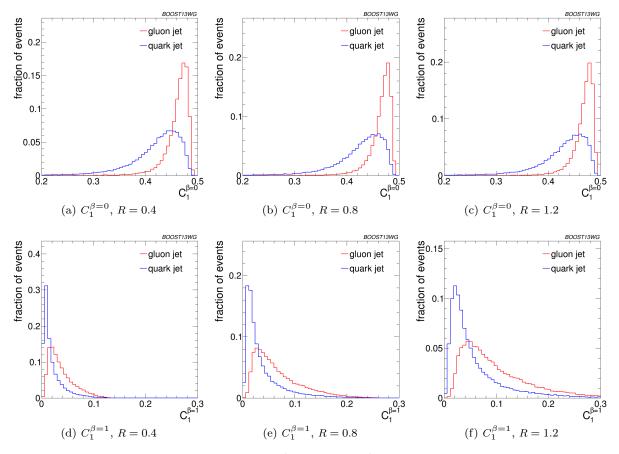


Fig. 4 Comparisons of quark and gluon distributions of  $C_1^{\beta=0}$  (top) and  $C_1^{\beta=1}$  (bottom) for leading jets in the  $p_T = 1-1.1$  TeV bin using the anti- $k_T$  algorithm with R = 0.4, 0.8 and 1.2.

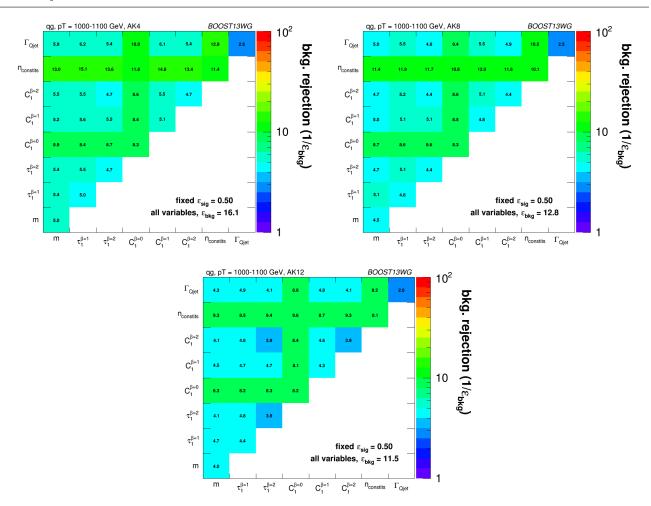


Fig. 5 Gluon rejection defined as  $1/\epsilon_{\rm gluon}$  when using each 2-variable combination as a tagger with 50% acceptance for quark jets. Results are shown for jets with  $p_T=1-1.1$  TeV and for (left) R=0.4; (centre) R=0.8; (right) R=1.2. The rejection obtained with a tagger that uses all variables is also shown in the plots.

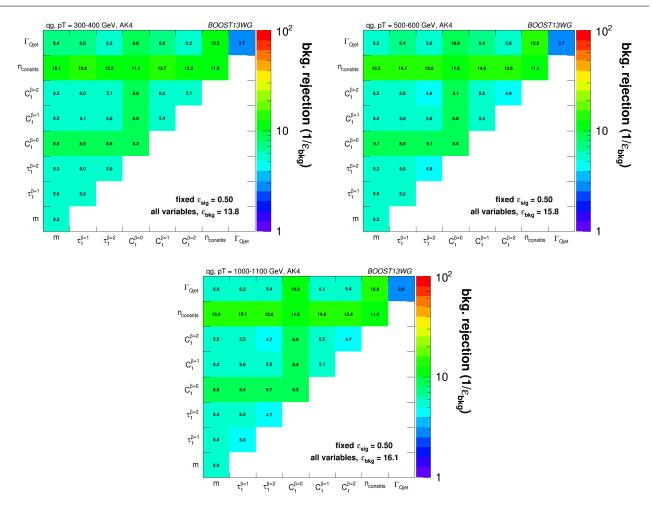


Fig. 6 Gluon rejection defined as  $1/\epsilon_{\rm gluon}$  when using each 2-variable combination as a tagger with 50% acceptance for quark jets. Results are shown for R=0.4 jets with  $p_T=300-400$  GeV,  $p_T=500-600$  GeV and  $p_T=1-1.1$  TeV. The rejection obtained with a tagger that uses all variables is also shown in the plots.

#### 6 Boosted W-Tagging

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#### 6.1 Methodology

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These studies use the WW samples as signal and the dijet gg as background, described previously in Section 2. Whilst only gluonic backgrounds are explored here, the conclusions as to the dependence of the performance and correlations on the jet boost and radius have been verified to hold also for qq backgrounds. ED: To be checked!

As in the q/g tagging studies, the showered events were clustered with FASTJET 3.03 using the anti- $k_{\rm T}$  algorithm with jet radii of R = 0.4, 0.8, 1.2. In both signal and background samples, an upper and lower cut on the leading jet  $p_T$  is applied after showering/clustering, to ensure similar  $p_T$  spectra for signal and background in each  $p_T$  bin. The bins in leading jet  $p_T$  that are considered are 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV, for the 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV parton  $p_T$ slices respectively. The jets then have various grooming approaches applied and substructure observables reconstructed as described in Section 3.4. The substructure observables studied in this section are:

- The ungroomed, trimmed  $(m_{\text{trim}})$ , and pruned  $(m_{\text{prun}})$ jet masses.
- The mass output from the modified mass drop tagger  $(m_{\text{mmdt}})$ .
- The soft drop mass with  $\beta=-1, 2$   $(m_{\rm sd})$ . 2-point energy correlation function ratio  $C_2^{\beta=1}$  (we also studied  $\beta=2$  but do not show its results because it showed poor discrimination power).
- N-subjettiness ratio  $\tau_2/\tau_1$  with  $\beta=1$   $(\tau_{21}^{\beta=1})$  and with axes computed using one-pass  $k_t$  axis optimization (we also studied  $\beta=2$  but did not show its results because it showed poor discrimination power).
- The pruned Qjet mass volatility,  $\Gamma_{\text{Qjet}}$ .

# 6.2 Single Variable Performance

In this section we will explore the performance of the various groomed jet mass and substructure variables in terms of discriminating signal and background, and how this performance changes depending on the kinematic bin and jet radius considered.

Figure 7 the compares the signal and background in terms of the different groomed masses explored for the anti- $k_{\rm T}$  R=0.8 algorithm in the  $p_T$  500-600 bin. One can clearly see that in terms of separating signal and background the groomed masses will be significantly more performant than the ungroomed anti- $k_{\rm T}$  R=0.8 mass. Figure 8 compares signal and background in the different substructure variables explored for the same jet radius and kinematic bin.

541 In this section, we study the discrimination of a boosted  $_{\!\scriptscriptstyle{543}}$ hadronically decaying W signal against a gluon background, comparing the performance of various groomed jet masses, substructure variables, and BDT combina-544 tions of groomed mass and substructure. We produce ROC curves that elucidate the performance of the vari-545 ous groomed mass and substructure variables. A ranges46 of different distance parameters R for the anti- $k_{\rm T}$  jets47 algorithm are explored, as well as a variety of kine-548 matic regimes (lead jet  $p_T$  300-400 GeV, 500-600 GeV, 549 1.0-1.1 TeV). This allows us to determine the perfor-550 mance of observables as a function of jet radius and jet<sub>551</sub> boost, and to see where different approaches may break552 down. The groomed mass and substructure variables<sub>553</sub> are then combined in a BDT as described in Section 4,554 and the performance of the resulting BDT discriminant<sub>555</sub> explored through ROC curves to understand the degree<sub>556</sub> to which variables are correlated, and how this changes<sub>557</sub> with jet boost and jet radius.

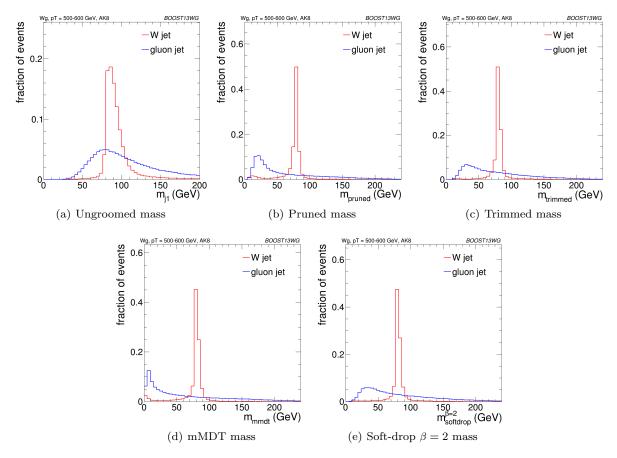


Fig. 7 Comparisons of the QCD background to the WW signal in the  $p_T$  500-600 GeV bin using the anti- $k_T$  R=0.8 algorithm: leading jet mass distributions.

Figures 9, 10 and 11 show the single variable ROC<sub>581</sub> curves compared to the ROC curve for a BDT combi-<sub>582</sub> nation of all the variables (labelled "allvars"), for each<sub>583</sub> of the anti- $k_{\rm T}$  distance parameters considered in each<sub>584</sub> of the kinematic bins. One can see that, in all cases<sub>,585</sub> the "allvars" option is considerably better performant than any of the individual single variables considered than any of the individual single variables considered that there is considerable complementarity between the variables, and this will be explored further the next section.

Although the ROC curves give all the relevant in-591 formation, it is hard to compare performance quanti-592 tatively. In Figures 12, 13 and 14 are shown matrices593 which give the background rejection for a signal effi-594 ciency of 70% when two variables (that on the x-axis595 and that on the y-axis) are combined in a BDT. These596 are shown separately for each  $p_T$  bin and jet radius597 considered. In the final column of these plots are shown598 the background rejection performance for three-variable599 BDT combinations of  $m_{sd}^{\beta=2} + C_2^{\beta=1} + X$ . These results500 will be discussed later in Section 6.3.3. The diagonal of501 these plots correspond to the background rejections for502

a single variable BDT, and can thus be examined to get a quantitative measure of the individual single variable performance, and to study how this changes with jet radius and momenta.

One can see that in general the most performant single variables are the groomed masses. However, in certain kinematic bins and for certain jet radii,  $C_2^{\beta=1}$  has a background rejection that is comparable to or better than the groomed masses.

By comparing Figures 12(a), 13(a) and 14(b), we can see how the background rejection performance evolves as we increase momenta whilst keeping the jet radius fixed to R=0.8. Similarly, by comparing Figures 12(b), 13(b) and 14(c) we can see how performance evolves with  $p_T$  for R=1.2. For both R=0.8 and R=1.2 the background rejection power of the groomed masses increases with increasing  $p_T$ , with a factor 1.5-2.5 increase in rejection in going from the 300-400 GeV to 1.0-1.1 TeV bins. ED: Add some of the 1-D plots comparing signal and bkgd in the different masses and pT bins here? However, the  $C_2^{\beta=1}$ ,  $\Gamma_{Qjet}$  and  $\tau_{21}^{\beta=1}$  substructure variables behave somewhat differently. The background

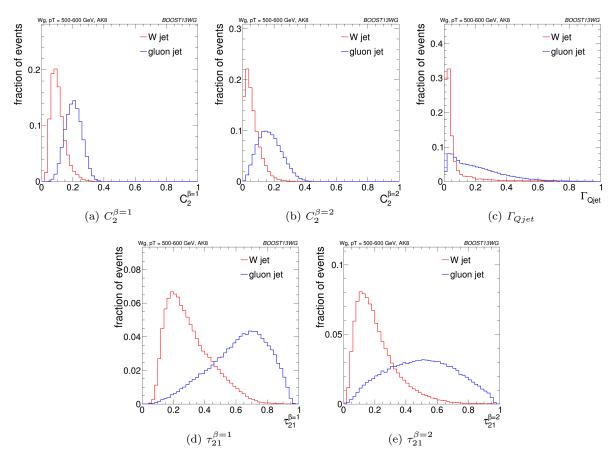


Fig. 8 Comparisons of the QCD background to the WW signal in the  $p_T$  500-600 GeV bin using the anti- $k_T$  R=0.8 algorithm: substructure variables.

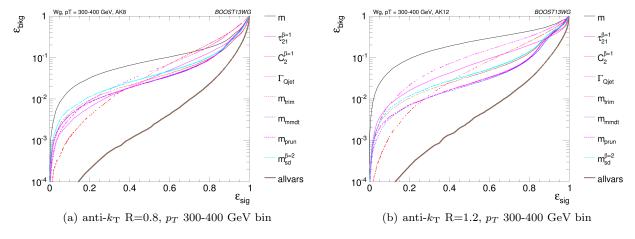


Fig. 9 The ROC curve for all single variables considered for W tagging in the  $p_T$  300-400 GeV bin using the anti- $k_T$  R=0.8 algorithm and R=1.2 algorithm.

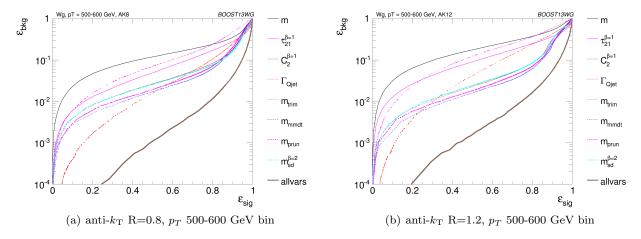


Fig. 10 The ROC curve for all single variables considered for W tagging in the  $p_T$  500-600 GeV bin using the anti- $k_T$  R=0.8 algorithm and R=1.2 algorithm.

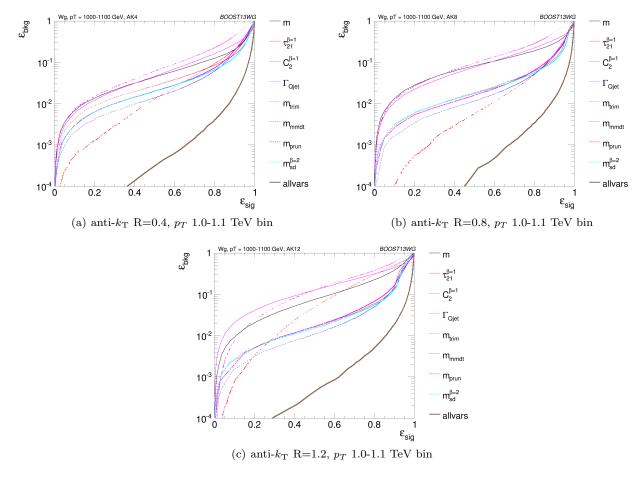


Fig. 11 The ROC curve for all single variables considered for W tagging in the  $p_T$  1.0-1.1 TeV bin using the anti- $k_T$  R=0.4 algorithm, anti- $k_T$  R=0.8 algorithm and R=1.2 algorithm.

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rejection power of the  $\Gamma_{Qjet}$  and  $\tau_{21}^{\beta=1}$  variables both<sub>653</sub> decrease with increasing  $p_T$ , by up to a factor two<sub>554</sub> in going from the 300-400 GeV to 1.0-1.1 TeV bins.<sub>655</sub> Conversely the rejection power of  $C_2^{\beta=1}$  dramatically<sub>656</sub> increases with increasing  $p_T$  for R=0.8, but does not<sub>657</sub> improve with  $p_T$  for the larger jet radius R=1.2. **ED**:<sub>658</sub> Can we explain this? Again, should we add some<sub>559</sub> of the 1-D plots?

and 14 we can see how the background rejection perfor-662 mance depends on jet radius within the same  $p_T$  bin.663 To within  $\sim 25\%$ , the background rejection power of 664 the groomed masses remains constant with respect to 665 the jet radius. However, we again see rather different666 behaviour for the substructure variables. In all  $p_T$  bins 667 considered the most performant substructure variable,  $C_2^{\beta=1}$ , performs best for an anti- $k_{\rm T}$  distance parameter of R=0.8. The performance of this variable is dramatically worse for the larger jet radius of R=1.2 (a $_{669}$ factor seven worse background rejection in the  $1.0\text{-}1.1_{\scriptscriptstyle 670}$ TeV bin), and substantially worse for R=0.4. For the  $_{671}$ other jet substructure variables considered,  $\Gamma_{Qjet}$  and  $_{672}$  $au_{21}^{\beta=1}$ , their background rejection power also reduces for  $au_{672}^{\beta=1}$ larger jet radius, but not to the same extent. **ED:**  $In_{-674}$ sert some nice discussion/explanation of why jet<sub>675</sub> substructure power generally gets worse as we<sub>676</sub> go to large jet radius, but groomed mass perfor-677 mance does not. Probably need the 1-D figures<sub>678</sub> for this.

# 6.3 Combined Performance

The off-diagonal entries in Figures 12, 13 and 14 can be used to compare the performance of different BDT685 two-variable combinations, and see how this varies as a function of  $p_T$  and R. By comparing the background rejection achieved for the two-variable combinations to be the background rejection of the "all variables" BDT,689 one can understand how much more discrimination is possible by adding further variables to the two-variable BDTs.

One can see that in general the most powerful two-693 variable combinations involve a groomed mass and a694 non-mass substructure variable  $(C_2^{\beta=1}, \Gamma_{Qjet} \text{ or } \tau_{21}^{\beta=1})$ .695 Two-variable combinations of the substructure variables96 are not powerful in comparison. Which particular mass697 + substructure variable combination is the most pow-698 erful depends strongly on the  $p_T$  and R of the jet, as699 discussed in the sections that follow.

There is also modest improvement in the background $_{01}$  rejection when different groomed masses are combined, $_{702}$  compared to the single variable groomed mass perfor- $_{703}$ 

mance, indicating that there is complementary information between the different groomed masses. In addition, there is an improvement in the background rejection when the groomed masses are combined with the ungroomed mass, indicating that grooming removes some useful discriminatory information from the jet. These observations are explored further in the section below.

Generally one can see that the R=0.8 jets offer the By comparing the individual sub-figures of Figures 12; 13best two-variable combined performance in all  $p_T$  bins 14 we can see how the background rejection perfor-662 explored here. This is despite the fact that in the highnce depends on jet radius within the same  $p_T$  bin.663 explored here. This is despite the fact that in the highest 1.0-1.1 GeV  $p_T$  bin the average separation of the
quarks from the W decay is much smaller than 0.8,
and well within 0.4. This conclusion could of course be
susceptible to pile-up, which is not considered in this
aviour for the substructure variables. In all  $p_T$  bins667

# $6.3.1\ Mass + Substructure\ Performance$

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As already noted, the largest background rejection at 70% signal efficiency are in general achieved using those two variable BDT combinations which involve a groomed mass and a non-mass substructure variable. For both R=0.8 and R=1.2 jets, the rejection power of these two variable combinations increases substantially with increasing  $p_T$ , at least within the  $p_T$  range considered here.

For a jet radius of R=0.8, across the full  $p_T$  range considered, the groomed mass + substructure variable combinations with the largest background rejection are those which involve  $C_2^{\beta=1}$ . For example, in combination with  $m_{sd}^{\beta=2}$ , this produces a five-, eight- and fifteen-fold increase in background rejection compared to using the groomed mass alone. In Figure 15 the low degree of correlation between  $m_{sd}^{\beta=2}$  versus  $C_2^{\beta=1}$  that leads to these large improvements in background rejection can be seen. One can also see that what little correlation exists is rather non-linear in nature, changing from a negative to a positive correlation as a function of the groomed mass, something which helps to improve the background rejection in the region of the W mass peak.

However, when we switch to a jet radius of R=1.2 the picture for  $C_2^{\beta=1}$  combinations changes dramatically. These become significantly less powerful, and the most powerful variable in groomed mass combinations becomes  $\tau_{21}^{\beta=1}$  for all jet  $p_T$  considered. Figure 16 shows the correlation between  $m_{sd}^{\beta=2}$  and  $C_2^{\beta=1}$  in the  $p_T$  1.0 - 1.2 TeV bin for the various jet radii considered. Figure 17 is the equivalent set of distributions for  $m_{sd}^{\beta=2}$  and  $\tau_{21}^{\beta=1}$ . One can see from Figure 16 that, due to the sensitivity of the observable to to soft, wide-angle radiation, as the jet radius increases  $C_2^{\beta=1}$  increases and becomes more and more smeared out for both signal and background, leading to worse discrimination power.

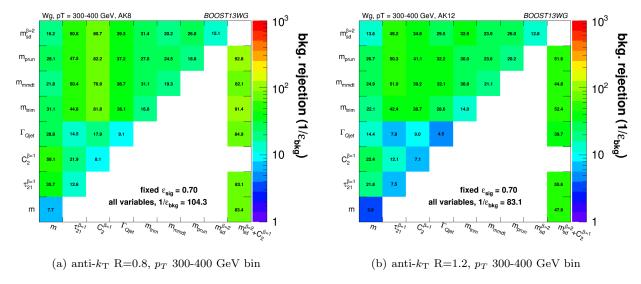


Fig. 12 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the  $p_T$  300-400 GeV bin using the anti- $k_T$  R=0.8 algorithm and R=1.2 algorithm. Also shown is the background rejection for a BDT combination of all of the variables considered.

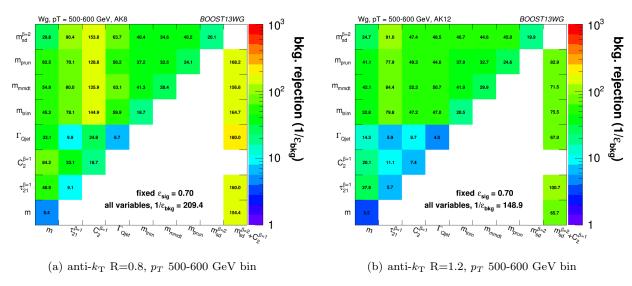


Fig. 13 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the  $p_T$  500-600 GeV bin using the anti- $k_T$  R=0.8 algorithm and R=1.2 algorithm. Also shown is the background rejection for a BDT combination of all of the variables considered.

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This does not happen to the same extent for  $\tau_{21}^{\beta=1}$ . We<sub>711</sub> can see from Figure 17 that the negative correlation between  $m_{sd}^{\beta=2}$  and  $\tau_{21}^{\beta=1}$  that is clearly visible for R=0.4712 decreases for larger jet radius, such that the groomed<sup>713</sup> mass and substructure variable are far less correlated<sup>714</sup> and  $\tau_{21}^{\beta=1}$  offers improved discrimination within a  $m_{sd}^{\beta=2}$ <sub>715</sub> mass window.

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# $6.3.2\ Mass\ +\ Mass\ Performance$

The different groomed masses and the ungroomed mass are of course not fully correlated, and thus one can always see some kind of improvement in the background rejection (relative to the single mass performance) when two different mass variables are combined in the BDT. However, in some cases the improvement can be dramatic, particularly at higher  $p_T$ , and particularly for combinations with the ungroomed mass. For example, in Figure 14 we can see that in the  $p_T$  1.0-1.1 TeV bin

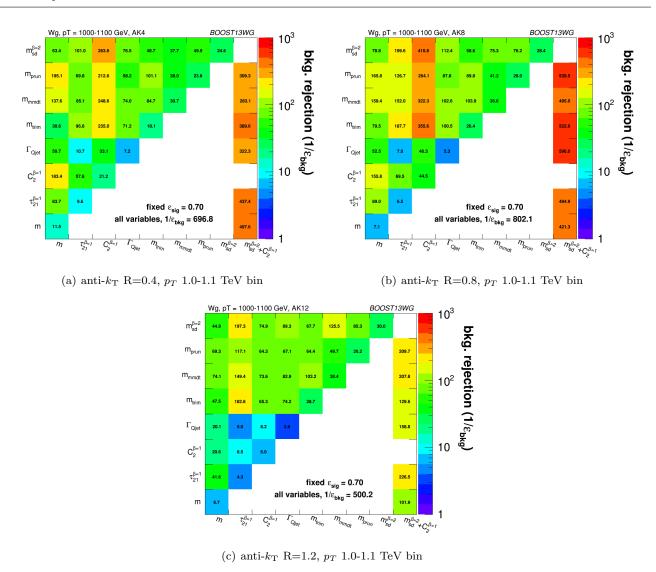


Fig. 14 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the  $p_T$  1.0-1.1 TeV bin using the anti- $k_T$  R=0.4, R=0.8 and R=1.2 algorithm. Also shown is the background rejection for a BDT combination of all of the variables considered.

the combination of pruned mass with ungroomed mass<sub>736</sub> produces a greater than eight-fold improvement in the<sub>737</sub> background rejection for R=0.4 jets, a greater than five-<sub>738</sub> fold improvement for R=0.8 jets, and a factor  $\sim$ two im-<sub>739</sub> provement for R=1.2 jets. A similar behaviour can be<sub>740</sub> seen for mMDT mass. In Figures 18, 19 and 20 is shown<sub>741</sub> the 2-D correlation plots of the pruned mass versus the<sub>742</sub> ungroomed mass separately for the WW signal and  $gg_{743}$  background samples in the  $p_T$  1.0-1.1 TeV bin, for the<sub>744</sub> various jet radii considered. For comparison, the corre-<sub>745</sub> lation of the trimmed mass with the ungroomed mass<sub>,746</sub> a combination that does not improve on the single mass<sub>,747</sub> as dramatically, is shown. In all cases one can see that<sub>,748</sub> there is a much smaller degree of correlation between<sub>749</sub> the pruned mass and the ungroomed mass in the back-<sub>750</sub>

grounds sample than for the trimmed mass and the ungroomed mass. This is most obvious in Figure 18, where the high degree of correlation between the trimmed and ungroomed mass is expected, since with the parameters used (in particular  $R_{trim}=0.2$ ) we cannot expect trimming to have a significant impact on an R=0.4 jet. The reduced correlation with ungroomed mass for pruning in the background means that, once we have made the requirement that the pruned mass is consistent with a W (i.e.  $\sim 80$  GeV), a relatively large difference between signal and background in the ungroomed mass still remains, and can be exploited to improve the background rejection further. In other words, many of the background events which pass the pruned mass requirement do so because they are shifted to lower mass (to

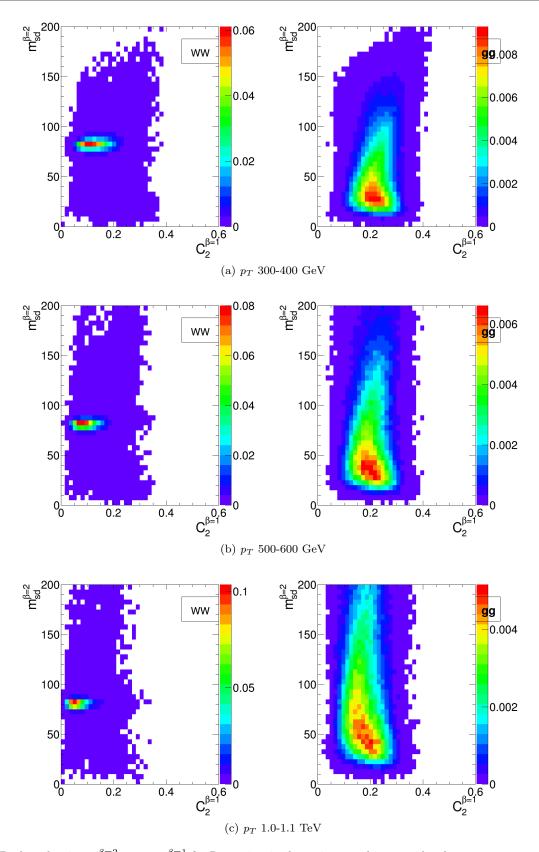


Fig. 15 2-D plots showing  $m_{sd}^{\beta=2}$  versus  $C_2^{\beta=1}$  for R=0.8 jets in the various  $p_T$  bins considered.

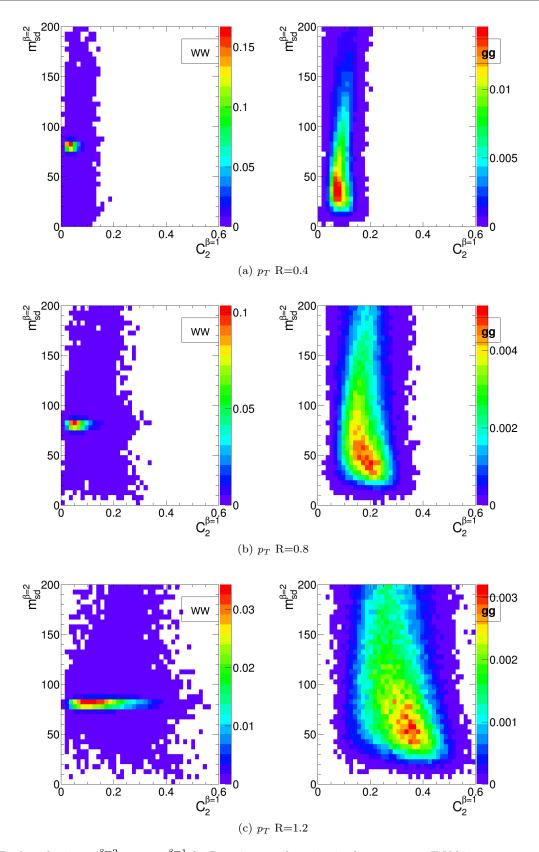


Fig. 16 2-D plots showing  $m_{sd}^{\beta=2}$  versus  $C_2^{\beta=1}$  for R=0.4, 0.8 and 1.2 jets in the  $p_T$  1.0-1.1 TeV bin.

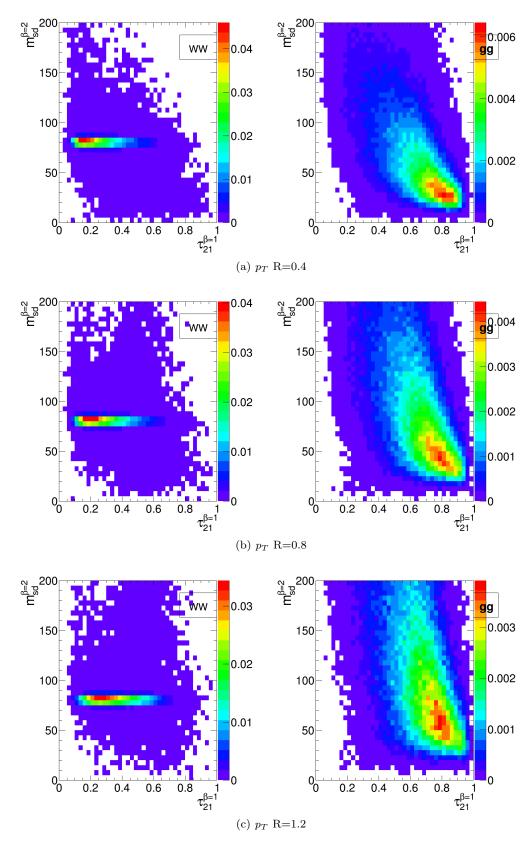


Fig. 17 2-D plots showing  $m_{sd}^{\beta=2}$  versus  $\tau_{21}^{\beta=1}$  for R=0.4, 0.8 and 1.2 jets in the  $p_T$  1.0-1.1 TeV bin.

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be within a signal mass window) by the grooming, but<sub>802</sub> these events still have the property that they look very<sub>803</sub> much like background events before the grooming. A<sub>804</sub> single requirement on the groomed mass only does not<sub>805</sub> exploit this. Of course, the impact of pile-up, not con-<sub>806</sub> sidered in this study, could significantly limit the degree<sub>307</sub> to which the ungroomed mass could be used to improve<sub>308</sub> discrimination in this way.

#### 6.3.3 "All Variables" Performance

As well as the background rejection at a fixed 70% sig- $_{811}$ nal efficiency for two-variable combinations, Figures 12, 13 and 14 also report the background rejection achieved<sub>813</sub> by a combination of all the variables considered into  $a_{_{\!814}}$ single BDT discriminant. One can see that, in all cases,  $_{\imath_{815}}$ the rejection power of this "all variables" BDT is signif-  $_{816}$ icantly larger than the best two-variable combination.  $_{817}$ This indicates that beyond the best two-variable com-818 bination there is still significant complementary infor-  $_{819}$ mation availiable in the remaining variables in order to  $_{820}$ improve the discrimination of signal and background. $_{821}$ How much complementary information is available ap-  $_{822}$ pears to be  $p_T$  dependent. In the lower  $p_T$  300-400 and<sub>823</sub> 500-600 GeV bins the background rejection of the "all  $_{824}$ variables" combination is a factor  $\sim 1.5$  greater than<sub>825</sub> the best two-variable combination, but in the highest  $_{826}$  $p_T$  bin it is a factor  $\sim 2.5$  greater.

The final column in Figures 12, 13 and 14 allows<sub>828</sub> us to explore the all variables performance a little further. It shows the background rejection for three variable BDT combinations of  $m_{sd}^{\beta=2}+C_2^{\beta=1}+X$ , where X is the variable on the y-axis. For jets with R=0.4<sub>832</sub> and R=0.8, the combination  $m_{sd}^{\beta=2}+C_2^{\beta=1}$  is the best<sub>833</sub> performant (or very close to the best performant) two-  $_{834}$ variable combination in every  $p_T$  bin considered. For<sub>835</sub> R=1.2 this is not the case, as  $C_2^{\beta=1}$  is superceded by<sub>836</sub>  $au_{21}^{\beta=1}$  in performance, as discussed earlier. Thus, in considering the three-variable combination results it is best $_{838}$ to focus on the R=0.4 and R=0.8 cases. Here we see, that, for the lower  $p_T$  300-400 and 500-600 GeV bins,  $p_{3840}$ adding the third variable to the best two-variable com-  $_{841}$ bination brings us to within  $\sim$  15% of the "all variables"  $_{\mbox{\tiny 842}}$ background rejection. However, in the highest  $p_T$  1.0-843 1.1 TeV bin, whilst adding the third variable does im-  $_{844}$ prove the performance considerably, we are still  $\sim 40\%_{\rm \tiny 845}$ from the observed "all variables" background rejection, 2846 and clearly adding a fourth or maybe even fifth vari-  $_{847}$ able would bring considerable gains. In terms of which  $_{\! {\tt 848}}$ variable offers the best improvement when added to the  $m_{sd}^{\beta=2}+C_2^{\beta=1}$  combination, it is hard to see an obvious pattern; the best third variable changes depending on the  $p_T$  and R considered.

In conclusion, it appears that there is a rich and complex structure in terms of the degree to which the discriminatory information provided by the set of variables considered overlaps, with the degree of overlap apparently decreasing at higher  $p_T$ . This suggests that in all  $p_T$  ranges, but especially at higher  $p_T$ , there are substantial performance gains to be made by designing a more complex multivariate W tagger.

#### 6.4 Conclusions

We have studied the performance, in terms of the degree to which a hadronically decaying W boson can be separated from a gluonic background, of a number of groomed jet masses, substructure variables, and BDT combinations of the above. We have used this to build a picture of how the discriminatory information contained in the variables overlaps, and how this complementarity between the variables changes with  $p_T$  and anti- $k_T$  distance parameter R.

In terms of the performance of individual variables, we find that, in agreement with other studies [REF], in general the groomed masses perform best, with a background rejection power that increases with increasing  $p_T$ , but which is more constant with respect to changes in R. Conversely, the performance of other substructure variables, such as  $C_2^{\beta=1}$  and  $\tau_{21}^{\beta=1}$  is more susceptible to changes in radius, with background rejection power decreasing with increasing R.

The best two-variable performance is obtained by combining a groomed mass with a substructure variable. Which particular substructure variable works best in combination is strongly dependent on  $p_T$  and R.  $C_2^{\beta=1}$  offers significant complimentarity to groomed mass at smaller R, owing to the small degree of correlation between the variables. However, the sensitivity of  $C_2^{\beta=1}$  to soft, wide-angle radiation leads to worse discrimination power at large R, where  $\tau_{21}^{\beta=1}$  performs better in combination. Our studies also demonstrate the potential for enhanced discrimination by combining groomed and ungroomed mass information, although the use of ungroomed mass in this may in practice be limited by the presence of pile-up that is not considered in these studies.

By examining the performance of a BDT combination of all the variables considered, it is clear that there are potentially substantial performance gains to be made by designing a more complex multivariate W tagger, especially at higher  $p_T$ .

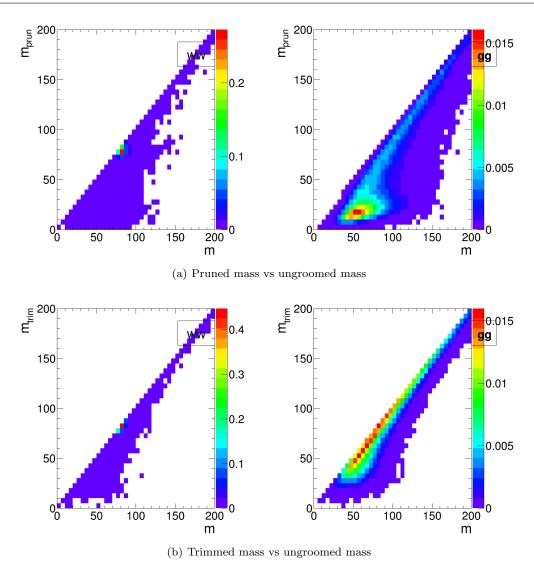


Fig. 18 2-D plots showing the correlation between groomed and ungroomed mass for WW and gg events in the  $p_T$  1.0-1.1 TeV bin using the anti- $k_T$  R=0.4 algorithm.

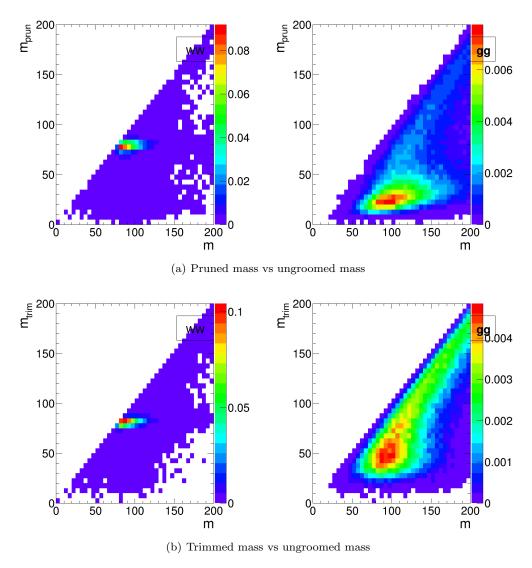


Fig. 19 2-D plots showing the correlation between groomed and ungroomed mass for WW and gg events in the  $p_T$  1.0-1.1 TeV bin using the anti- $k_T$  R=0.8 algorithm.

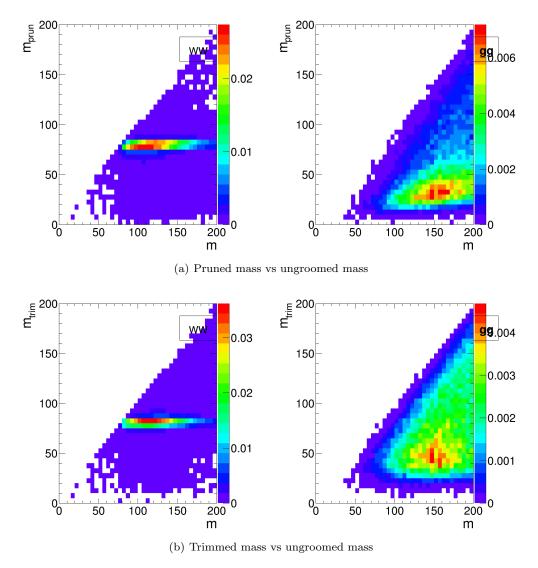


Fig. 20 2-D plots showing the correlation between groomed and ungroomed mass for WW and gg events in the  $p_T$  1.0-1.1 TeV bin using the anti- $k_T$  R=1.2 algorithm.

# <sup>49</sup> 7 Top Tagging

In this section, we study the identification of boosted top quarks at Run II of the LHC. Boosted top quarks result in large-radius jets with complex substructure, containing a b-subjet and a boosted W. The additional kinematic handles coming from the reconstruction of the W mass and b-tagging allows a very high degree of discrimination of top quark jets from QCD back-888 grounds.

We consider top quarks with moderate boost (600- $^{907}$  1000 GeV), and perhaps most interestingly, at high<sub>908</sub> boost ( $\gtrsim 1500$  GeV). Top tagging faces several chal<sub>-909</sub> lenges in the high- $p_T$  regime. For such high- $p_T$  jets,<sub>910</sub> the *b*-tagging efficiencies are no longer reliably known.<sub>911</sub> Also, the top jet can also accompanied by additional<sub>912</sub>

radiation with  $p_T \sim m_t$ , leading to combinatoric ambiguities of reconstructing the top and W, and the possibility that existing taggers or observables shape the background by looking for subjet combinations that reconstruct  $m_t/m_W$ . To study this, we examine the performance of both mass-reconstruction variables, as well as shape observables that probe the three-pronged nature of the top jet and the accompanying radiation pattern.

We use the top quark MC samples described in Section 2.2. The analysis relies on FASTJET 3.0.3 for jet clustering and calculation of jet substructure observables. Jets are clustered using the anti- $k_t$  algorithm. An upper and lower  $p_T$  cut are applied after jet clustering to each sample to ensure similar  $p_T$  spectra in each bin. The bins in leading jet  $p_T$  that are investigated for top tagging are 600-700 GeV, 1-1.1 TeV, and 1.5-1.6 TeV. Jets are clustered with radii R=0.4, 0.8, and 1.2; R=0.4 jets are only studied in the 1.5-1.6 TeV bin because for top quarks with this boost, the top decay products are all contained within an R=0.4 jet.

#### 7.1 Methodology

We study a number of top-tagging strategies, in particular:

- 1. HEPTopTagger
- 2. Johns Hopkins Tagger (JH)
- 3. Trimming
- 4. Pruning

The top taggers have criteria for reconstructing a top and W candidate, and a corresponding top and W mass, as described in Section 3.3, while the grooming algorithms (trimming and pruning) do not incorporate a W-identification step. For a level playing field, where grooming is used we construct a W candidate mass,  $m_W$ , from the three leading subjets by taking the mass of the pair of subjets with the smallest invariant mass; in the case that only two subjets are reconstructed, we take the mass of the leading subjet. The top mass,  $m_t$ , is the mass of the groomed jet. All of the above taggers and groomers incorporate a step to remove pile-up and other soft radiation.

We also consider the performance of the following jet shape observables:

- The ungroomed jet mass.
- N-subjettiness ratios  $\tau_2/\tau_1$  and  $\tau_3/\tau_2$  with  $\beta=1$  and the "winner-takes-all" axes.
- 2-point energy correlation function ratios  $C_2^{\beta=1}$  and  $C_3^{\beta=1}$ .

- The pruned Qjet mass volatility,  $\Gamma_{\text{Qjet}}$ .

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In addition to the jet shape performance, we combine <sup>964</sup> the jet shapes with the mass-reconstruction methods <sup>965</sup> described above to determine the optimal combined <sup>966</sup> performance.

For determining the performance of multiple variables, we combine the relevant tagger output observables and/or jet shapes into a boosted decision tree 
(BDT), which determines the optimal cut. Additionally, because each tagger has two input parameters, as 
described in Section 3.3, we scan over reasonable values 
of the parameters to determine the optimal value that 
gives the largest background rejection for each top tagging signal efficiency. This allows a direct comparison of 
the optimized version of each tagger. The input values 
scanned for the various algorithms are:

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 \begin{array}{ll} - \ \mathbf{HEPTopTagger:} \ m \in [30, 100] \ \mathrm{GeV}, \ \mu \in [0.5, 1] \\ - \ \mathbf{JH} \ \mathbf{Tagger:} \ \delta_p \in [0.02, 0.15], \ \delta_R \in [0.07, 0.2] \\ - \ \mathbf{Trimming:} \ f_{\mathrm{cut}} \in [0.02, 0.14], \ R_{\mathrm{trim}} \in [0.1, 0.5] \\ - \ \mathbf{Pruning:} \ z_{\mathrm{cut}} \in [0.02, 0.14], \ R_{\mathrm{cut}} \in [0.1, 0.6] \end{array}
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# 7.2 Single-observable performance

We start by investigating the behaviour of individual <sup>987</sup> jet substructure observables. Because of the rich, three- <sup>988</sup> pronged structure of the top decay, it is expected that <sup>990</sup> combinations of masses and jet shapes will far out- <sup>991</sup> perform single observables in identifying boosted tops. <sup>991</sup> However, a study of the top-tagging performance of sin- <sup>992</sup> gle variables facilitates a direct comparison with the  $W^{993}$  tagging results in Section 6, and also allows a straight- <sup>994</sup> forward examination of the performance of each observ- <sup>995</sup> able for different  $p_T$  and jet radius.

Fig. 21 shows the ROC curves for each of the top-997 tagging observables, with the bare (ungroomed) jet mass<sup>998</sup> also plotted for comparison. The jet shape observables<sup>999</sup> all perform substantially worse than jet mass, unlike  $W^{\!\scriptscriptstyle{000}}$ tagging for which several observables are competitive out with or perform better than jet mass (see, for exam<sup>1002</sup> ple, Fig. 7). To understand why this is the case, con<sup>1003</sup> sider N-subjettiness. The W is two-pronged and the  $^{004}$ top is three-pronged; therefore, we expect  $\tau_{21}$  and  $\tau_{32}^{1005}$ to be the best-performant N-subjettiness ratio, respec<sup>1006</sup> tively. However,  $au_{21}$  also contains an implicit cut on the  $^{007}$ denominator,  $\tau_1$ , which is strongly correlated with jet 008 mass. Therefore,  $\tau_{21}$  combines both mass and shape in  $^{1009}$ formation to some extent. By contrast, and as is cleat  $^{\!010}$ in Fig.21(a), the best shape for top tagging is  $\tau_{32}$ , which on contains no information on the mass. Therefore, it is un±012 surprising that the shapes most useful for top tagging013 are less sensitive to the jet mass, and under-perform rel<sub>±014</sub> ative to the corresponding observables for W tagging. 1015

Of the two top tagging algorithms, we can see from Figure 21 that the Johns Hopkins (JH) tagger outperforms the HEPTopTagger in terms of its signal-tobackground separation power in both the top and Wcandidate masses. In Figure 22 we show the histograms for the top mass output from the JH and HEPTopTagger for different R in the  $p_T$  1.5-1.6 TeV bin, and in Figure 23 for different  $p_T$  at at R =0.8, optimized at a signal efficiency of 30%. One can see from these figures that the likely reason for the better performance of the JH tagger is that, in the HEPTopTagger algorithm, the jet is filtered to select the five hardest subjets, and then three subjets are chosen which reconstruct the top mass. This requirement tends to shape a peak in the QCD background around  $m_t$  for the HEPTopTagger, while the JH tagger has no such requirement. It has been suggested by Anders et al. [?] that performance in the HEPTopTagger may be improved by selecting the three subjets reconstructing the top only among those that pass the W mass constraints, which somewhat reduces the shaping of the background. The discrepancy between the JH and HEPTopTaggers is more pronounced at higher  $p_T$  and larger jet radius (see Figs. 26 and 29). Note that both the JH tagger and the HEP-TopTagger are superior to the grooming algorithms at using the W candidate inside of the top for signal discrimination; this is because the the pruning and trimming algorithms do not have inherent W-identification steps and are not optimized for this purpose.

In Figures 24 and 26 we directly compare ROC curves for jet shape observable performance and top mass performance respectively in the three different  $p_T$ bins considered whilst keeping the jet radius fixed at R=0.8. The input parameters of the taggers, groomers and shape variables are separately optimized in each  $p_T$  bin. One can see from Figure 24 that the tagging performance of jet shapes do not change substantially with  $p_T$ . The observables  $\tau_{32}^{(\beta=1)}$  and Qjet volatility  $\Gamma$ have the most variation and tend to degrade with higher  $p_T$ , as can be seen in Figure 25. This makes sense, as higher- $p_T$  QCD jets have more, harder emissions within the jet, giving rise to substructure that fakes the signal. By contrast, from Figure 26 we can see that most of the top mass observables have superior performance at higher  $p_T$  due to the radiation from the top quark becoming more collimated. The notable exception is the HEPTopTagger, which degrades at higher  $p_T$ , likely in part due to the background-shaping effects discussed earlier.

In Figures 27 and 29 we directly compare ROC curves for jet shape observable performance and top mass performance respectively for the three different jet radii considered within the  $p_T$  1.5-1.6 TeV bin. Again,

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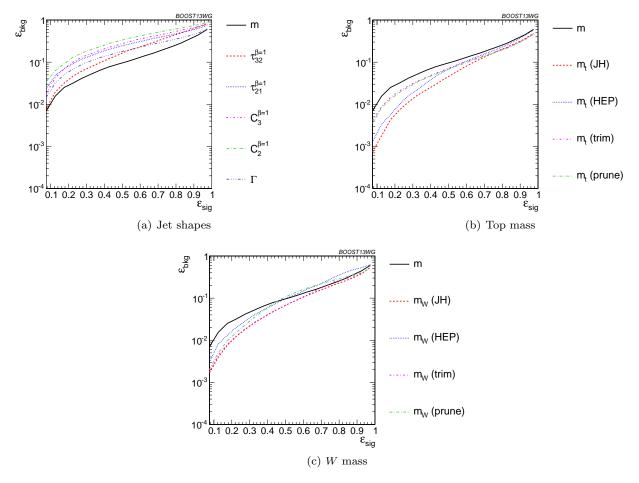


Fig. 21 Comparison of single-variable top-tagging performance in the  $p_T = 1-1.1$  GeV bin using the anti- $k_T$ , R=0.8 algorithm.

the input parameters of the taggers, groomers and shap@37 variables are separately optimized for each jet radius<sub>1038</sub> We can see from these figures that most of the top tag<sub>±039</sub> ging variables, both shape and reconstructed top mass<sub>1040</sub> perform best for smaller radius. This is likely because<sub>1,041</sub> at such high  $p_T$ , most of the radiation from the top<sub>042</sub> quark is confined within R = 0.4, and having a larger<sub>043</sub> jet radius makes the observable more susceptible to con+044 tamination from the underlying event and other uncorto45 related radiation. In Figure 28, we compare the individ<sub>±046</sub> ual top signal and QCD background distributions for<sub>047</sub> each shape variable considered in the  $p_T$  1.5-1.6 TeV<sub>048</sub> bin for the various jet radii. One can see that the distributions for both signal and background broaden with increasing R, degrading the discriminating power. For  $^{1049}$  $C_2^{(\beta=1)}$  and  $C_3^{(\beta=1)}$ , the background distributions are shifted upward as well. Therefore, the discriminating  $^{050}$ power generally gets worse with increasing R. The main  $^{1051}$ exception is for  $C_3^{(\beta=1)}$ , which performs optimally at  $^{052}$ R = 0.8; in this case, the signal and background coinci<sup>1053</sup> dentally happen to have the same distribution around  $^{054}\,$ 

R=0.4, and so R=0.8 gives better discrimination. ED: Should we also include 1-D plots comparing signal vs bkgd in the top mass, and how this varies with radius? Having said that, there a a lot of 1-D plots here already, might want to try and cut down. (How about now? I've added them to Fig. 26, 27, and removed some other plots. We should decide if we want them; if we do, we need to explain about how the optimization at  $\epsilon_S=0.3-0.35$  prefers an aggressive trimmer which suppresses the background mass but also tends to give a spurious peak around  $m_W$ .

# 7.3 Performance of multivariable combinations

We now consider various BDT combinations of the observables from Section 7.2, using the techniques described in Section 4. In particular, we consider the performance of individual taggers such as the JH tagger and HEPTopTagger, which output information about the top and W candidate masses and the helicity an-

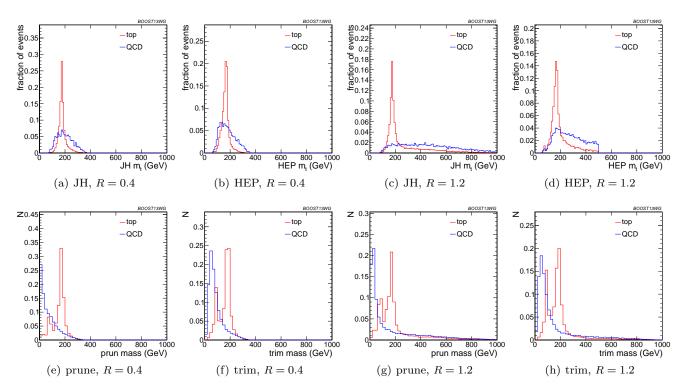


Fig. 22 Comparison of top mass reconstruction with the Johns Hopkins (JH), HEPTopTaggers (HEP), pruning, and trimming at different R using the anti- $k_{\rm T}$  algorithm,  $p_{\rm T}=1.5-1.6$  TeV. Each histogram is shown for the working point optimized for best performance with  $m_t$  in the 0.3-0.35 signal efficiency bin, and is normalized to the fraction of events passing the tagger. In this and subsequent plots, the HEPTopTagger distribution cuts off at 500 GeV because the tagger fails to tag jets with a larger mass.

gle; groomers, such as trimming and pruning, whichoso remove soft, uncorrelated radiation from the top cantosi didate to improve mass reconstruction, and to whichose we have added a W reconstruction step; and the comtosi bination of the outputs of the above taggers/groomers, both with each other, and with shape variables such as N-subjettiness ratios and energy correlation ratios. Forosall observables with tuneable input parameters, we scanos and optimize over realistic values of such parameters, as described in Section 7.1.

In Figure 30, we directly compare the performance of the HEPTopTagger, the JH tagger, trimming, and pruning, in the  $p_T = 1 - 1.1$  TeV bin using jet radius R=0.8, where both  $m_t$  and  $m_W$  are used in the groomers Generally, we find that pruning, which does not naturo rally incorporate subjets into the algorithm, does not perform as well as the others. Interestingly, trimming which does include a subjet-identification step, performs range, possibly due to the BertopTagger over much of the range, possibly due to the background-shaping observed in Section 7.2. By contrast, the JH tagger outperforms to the other algorithms. To determine whether there is complementary information in the mass outputs from different top taggers, we also consider in Figure 30 and

multivariable combination of all of the JH and HEP-TopTagger outputs. The maximum efficiency of the combined JH and HEPTopTaggers is limited, as some fraction of signal events inevitably fails either one or other of the taggers. We do see a 20-50% improvement in performance when combining all outputs, which suggests that the different algorithms used to identify the top and W for different taggers contains complementary information.

In Figure 31 we present the results for multivariable combinations of the top tagger outputs with and without shape variables. We see that, for both the HEP-TopTagger and the JH tagger, the shape observables contain additional information uncorrelated with the masses and helicity angle, and give on average a factor 2-3 improvement in signal discrimination. We see that, when combined with the tagger outputs, both the energy correlation functions  $C_2 + C_3$  and the N-subjettiness ratios  $\tau_{21} + \tau_{32}$  give comparable performance, while the Qjet mass volatility is slightly worse; this is unsurprising, as Qjets accesses shape information in a more indirect way from other shape observables. Combining all shape observables with a single top tagger provides even greater enhancement in discrimi-

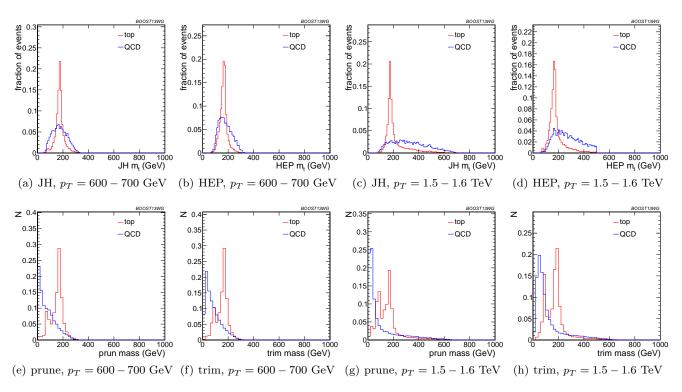


Fig. 23 Comparison of top mass reconstruction with the Johns Hopkins (JH), HEPTopTaggers (HEP), pruning, and trimming at different  $p_T$  using the anti- $k_T$  algorithm, R = 0.8. Each histogram is shown for the working point optimized for best performance with  $m_t$  in the 0.3 - 0.35 signal efficiency bin, and is normalized to the fraction of events passing the tagger.

nation power. We directly compare the performance of 128 the JH and HEPTopTaggers in Figure 31(c). Combin 129 ing the taggers with shape information nearly erases the difference between the tagging methods observed in Figure 30; this indicates that combining the shape information with the HEPTopTagger identifies the differences between signal and background missed by the tagger alone. This also suggests that further improvement to discriminating power may be minimal, as various multivariable combinations are converging to within a factor of 20% or so.

In Figure 32 we present the results for multivari<sup>1140</sup> able combinations of groomer outputs with and without<sup>141</sup> shape variables. As with the tagging algorithms, com<sup>1142</sup> binations of groomers with shape observables improves<sup>143</sup> their discriminating power; combinations with  $\tau_{32} + \tau_{21}$ <sup>1144</sup> perform comparably to those with  $C_3 + C_2$ , and both<sup>145</sup> of these are superior to combinations with the mass<sup>146</sup> volatility,  $\Gamma$ . Substantial improvement is further possi<sup>1147</sup> ble by combining the groomers with all shape observe<sup>1148</sup> ables. Not surprisingly, the taggers that lag behind in<sup>149</sup> performance enjoy the largest gain in signal-background<sup>150</sup> discrimination with the addition of shape observables<sup>1151</sup> Once again, in Figure 32(c), we find that the differ<sup>1152</sup>

ences between pruning and trimming are erased when combined with shape information.

Finally, in Figure 33, we compare the performance of each of the tagger/groomers when their outputs are combined with all of the shape observables considered. One can see that the discrepancies between the performance of the different taggers/groomers all but vanishes, suggesting perhaps that we are here utilising all available signal-background discrimination information, and that this is the optimal top tagging performance that could be achieved in these conditions.

Up to this point we have just considered the combined multivariable performance in the  $p_T$  1.0-1.1 TeV bin with jet radius R=0.8. We now compare the BDT combinations of tagger outputs, with and without shape variables, at different  $p_T$ . The taggers are optimized over all input parameters for each choice of  $p_T$  and signal efficiency. As with the single-variable study, we consider anti- $k_T$  jets clustered with R=0.8 and compare the outcomes in the  $p_T=500-600$  GeV,  $p_T=1-1.1$  TeV, and  $p_T=1.5-1.6$  TeV bins. The comparison of the taggers/groomers is shown in Figure 34. The behaviour with  $p_T$  is qualitatively similar to the behaviour of the  $m_t$ observable for each tagger/groomer shown in Figure 26; this suggests that the  $p_T$  behaviour of the

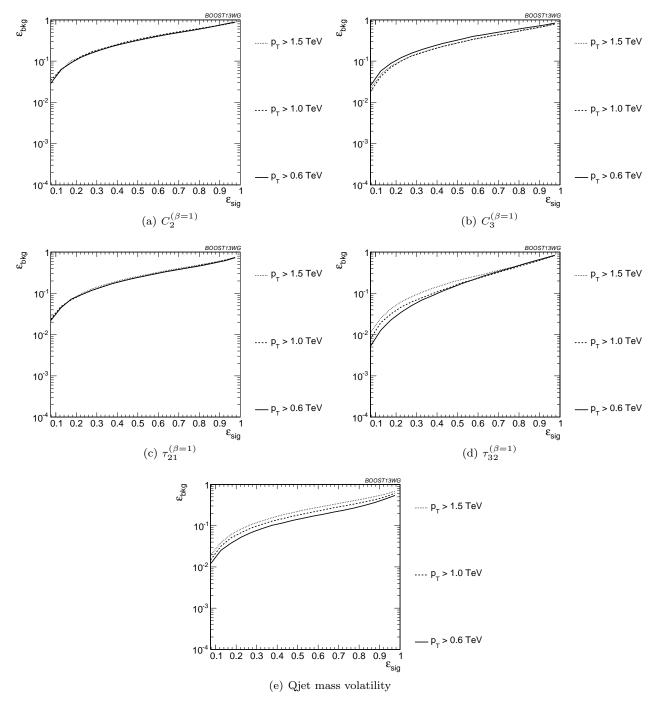


Fig. 24 Comparison of individual jet shape performance at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm.

taggers is dominated by the top mass reconstruction  $_{161}$  As before, the HEPTopTagger performance degrades  $_{162}$  slightly with increased  $p_T$  due to the background shap  $_{163}$  ing effect, while the JH tagger and groomers modestly  $_{164}$  improve in performance.

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In Figure 35, we show the  $p_T$  dependence of BDT<sup>166</sup> combinations of the JH tagger output combined with<sup>167</sup> shape observables. We find that the curves look nearly<sup>168</sup>

identical: the  $p_T$  dependence is dominated by the top mass reconstruction, and combining the tagger outputs with different shape observables does not substantially change this behaviour. The same holds true for trimming and pruning. By contrast, HEPTopTagger ROC curves, shown in Figure 36, do change somewhat when combined with different shape observables; due to the suboptimal performance of the HEPTopTagger at high

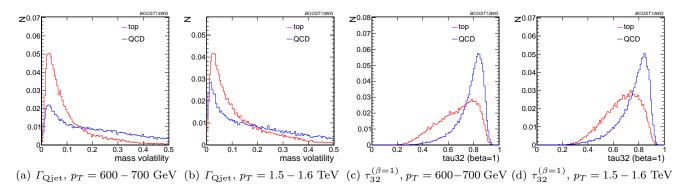


Fig. 25 Comparison of  $\Gamma_{\text{Qjet}}$  and  $\tau_{32}^{\beta=1}$  at R=0.8 and different values of the  $p_T$ . These shape observables are the most sensitive to varying  $p_T$ .

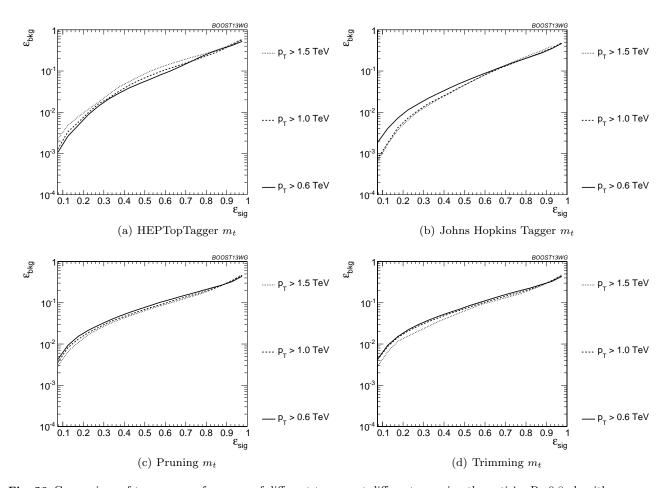


Fig. 26 Comparison of top mass performance of different taggers at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm.

 $p_T$  , we find that combining the HEPTopTagger with  $C_3^{(\beta=1)},$  which in Figure 24(b) is seen to have some mod  $_{117}$  est improvement at high  $p_T$  , can improve its perfor  $_{1178}$  mance. Combining the HEPTopTagger with multiple  $_{179}$  shape observables gives the maximum improvement in  $_{1180}$  performance at high  $p_T$  relative to at low  $p_T$  .

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In Figure 37 we compare the BDT combinations of tagger outputs, with and without shape variables, at different jet radius R in the  $p_T = 1.5 - 1.6$  TeV bin. The taggers are optimized over all input parameters for each choice of R and signal efficiency. We find that, for all taggers and groomers, the performance is always best at small R; the choice of R is sufficiently large to

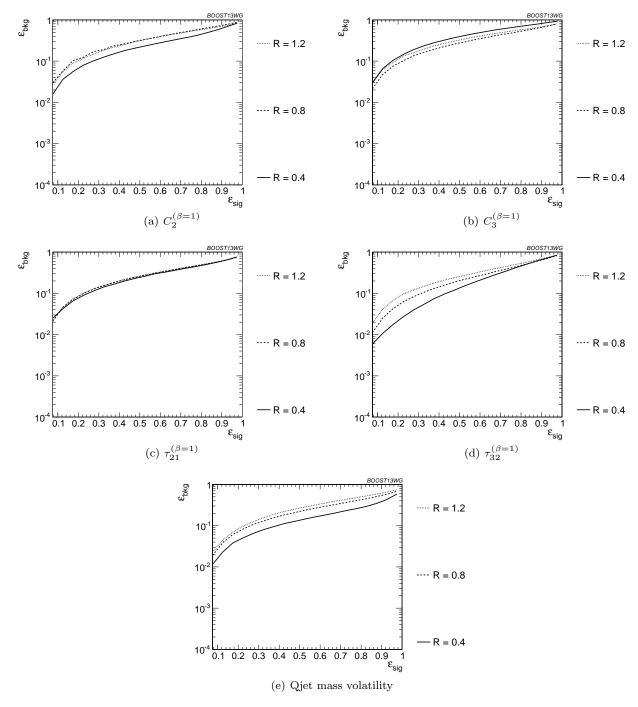


Fig. 27 Comparison of individual jet shape performance at different R in the  $p_T = 1.5 - 1.6$  TeV bin.

admit the full top quark decay at such high  $p_T$ , buting is small enough to suppress contamination from additional radiation. This is not altered when the taggers are combined with shape observable. For example, in Figure 38 is shown the depedence on R of the JH tag<sub>1192</sub> ger when combined with shape observables, where one can see that the R-dependence is identical for all com<sub>1193</sub>

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binations. The same holds true for the HEPTopTagger, trimming, and pruning.

# 7.4 Performance at Sub-Optimal Working Points

Up until now, we have re-optimized our tagger and groomer parameters for each  $p_T$ , R, and signal efficiency

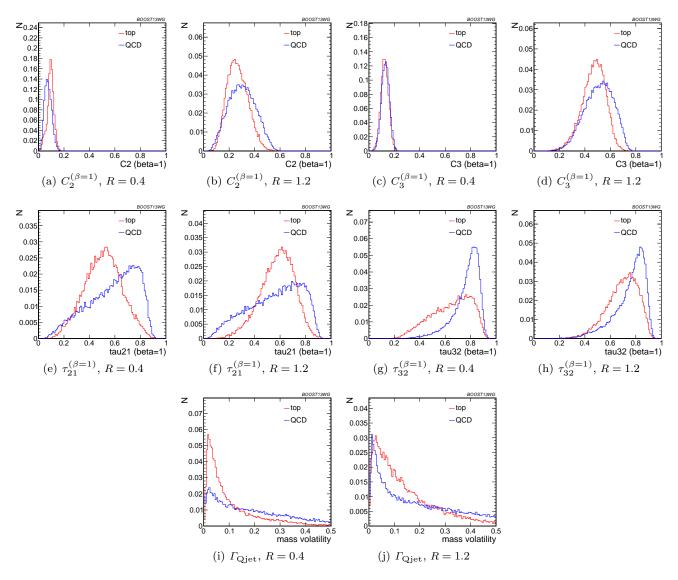


Fig. 28 Comparison of various shape observables in the  $p_T = 1.5 - 1.6$  TeV bin and different values of the anti- $k_T$  radius R.

working point. In reality, experiments will choose a fi $_{1211}$  nite set of working points to use. How do our results $_{212}$  hold up when this is taken into account? To address this $_{213}$  concern, we replicate our analyses, but only optimize $_{214}$  the top taggers for a particular  $p_T/R$ /efficiency and ap $_{1215}$  ply the same parameters to other scenarios. This allows $_{216}$  us to determine the extent to which re-optimization is $_{217}$  necessary to maintain the high signal-background dis $_{1218}$  crimination power seen in the top tagging algorithms $_{219}$  we study. The shape observables typically do not have $_{220}$  any input parameters to optimize. Therefore, we focuse on the taggers and groomers, and their combination $_{222}$  with shape observables, in this section.

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Optimizing at a single  $p_T$ : We show in Figure 39<sup>224</sup> the performance of the top taggers, using just the recon<sup>1225</sup> structed top mass as the discriminating variable, with <sup>226</sup>

all input parameters optimized to the  $p_T = 1.5 - 1.6$ TeV bin, relative to the performance optimized at each  $p_T$ . We see that while the performance degrades by about 50% when the high- $p_T$  optimized points are used at other momenta, this is only an order-one adjustment of the tagger performance, with trimming and the Johns Hopkins tagger degrading the most. The jagged behaviour of the points is due to the finite resolution of the scan. We also observe a particular effect associated with using suboptimal taggers: since taggers sometimes fail to return a top candidate, parameters optimized for a particular efficiency  $\varepsilon_S$  at  $p_T = 1.5 - 1.6$  TeV may not return enough signal candidates to reach the same efficiency at a different  $p_T$ . Consequently, no point appears for that  $p_T$  value. This is not often a practical concern, as the largest gains in signal discrimination and signif-

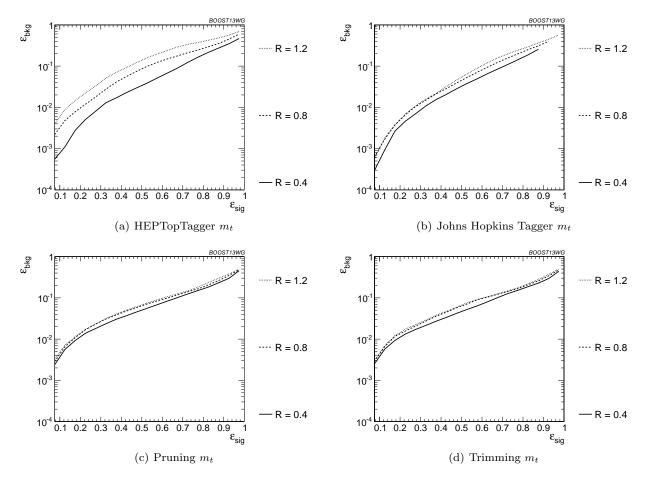


Fig. 29 Comparison of top mass performance of different taggers at different R in the  $p_T = 1.5 - 1.6$  TeV bin.

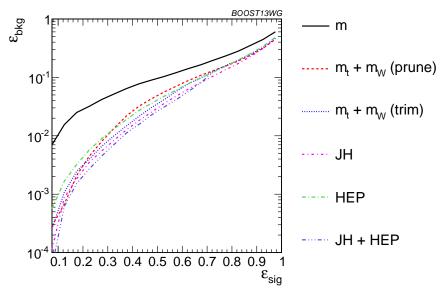


Fig. 30 The performance of the various taggers in the  $p_T = 1 - 1.1$  TeV bin using the anti- $k_T$  R=0.8 algorithm. For the groomers a BDT combination of the reconstructed  $m_t$  and  $m_W$  are used. Also shown is a multivariable combination of all of the JH and HEPTopTagger outputs. The ungroomed mass performance is shown for comparison.

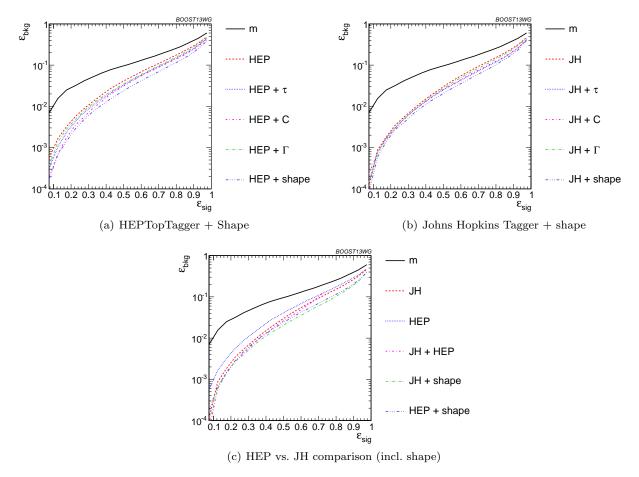


Fig. 31 The performance of BDT combinations of the JH and HepTopTagger outputs with various shape observables in the  $p_T=1-1.1$  TeV bin using the anti- $k_T$  R=0.8 algorithm. Taggers are combined with the following shape observables:  $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$ ,  $C_2^{(\beta=1)} + C_3^{(\beta=1)}$ ,  $\Gamma_{\rm Qjet}$ , and all of the above (denoted "shape").

icance are for smaller values of  $\varepsilon_S$ , but it is something<sup>247</sup> that must be considered when selecting benchmark tag<sub>7248</sub> ger parameters and signal efficiencies.

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The degradation in performance is more pronounced<sup>250</sup> for the BDT combinations of the full tagger outputs;<sup>251</sup> shown in Figure 40), particularly at very low signal effi<sup>1252</sup> ciency where the optimization picks out a cut on the tail<sup>253</sup> of some distribution that depends precisely on the  $p_T/R^{254}$  of the jet. Once again, trimming and the Johns Hop<sup>1255</sup> kins tagger degrade more markedly. Similar behaviout<sup>256</sup> holds for the BDT combinations of tagger outputs plus all shape observables.

Optimizing at a single R: We perform a similar anal<sub>1259</sub> ysis, optimizing tagger parameters for each signal ef<sub>1260</sub> ficiency at R=1.2, and then use the same parame<sub>1261</sub> ters for smaller R, in the  $p_T$  1.5-1.6 TeV bin. In Fig<sub>1262</sub> ure 41 we show the ratio of the performance of the<sub>263</sub> top taggers, using just the reconstructed top mass as<sub>264</sub> the discriminating variable, with all input parameters<sub>265</sub>

optimized to the R=1.2 values compared to input parameters optimized separately at each radius. While the performance of each observable degrades at small  $\epsilon_{\rm sig}$  compared to the optimized search, the HEPTop-Tagger fares the worst as the observed is quite sensitive to the selected value of R. It is not surprising that a tagger whose top mass reconstruction is susceptible to background-shaping at large R and  $p_T$  would require a more careful optimization of parameters to obtain the best performance.

The same holds true for the BDT combinations of the full tagger outputs, shown in Figure 42). The performance for the sub-optimal taggers is still within an O(1)factor of the optimized performance, and the HEPTop-Tagger performs better with the combination of all of its outputs relative to the performance with just  $m_t$ . The same behaviour holds for the BDT combinations of tagger outputs and shape observables.

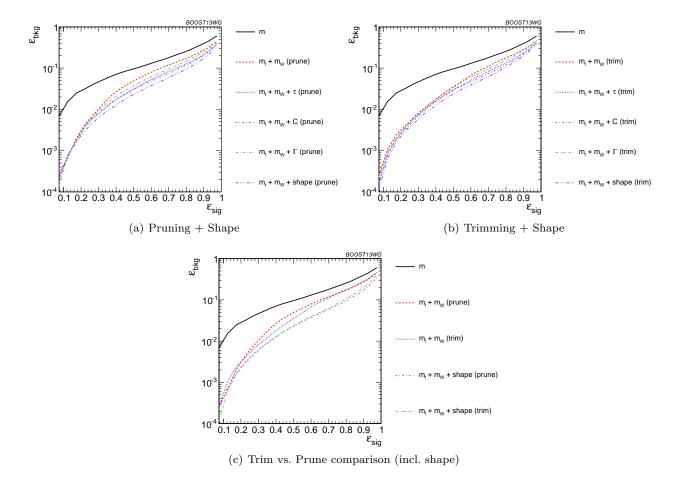


Fig. 32 The performance of the BDT combinations of the trimming and pruning outputs with various shape observables in the  $p_T = 1 - 1.1$  TeV bin using the anti- $k_T$  R=0.8 algorithm. Groomer mass outputs are combined with the following shape observables:  $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$ ,  $C_2^{(\beta=1)} + C_3^{(\beta=1)}$ ,  $\Gamma_{\text{Qjet}}$ , and all of the above (denoted "shape").

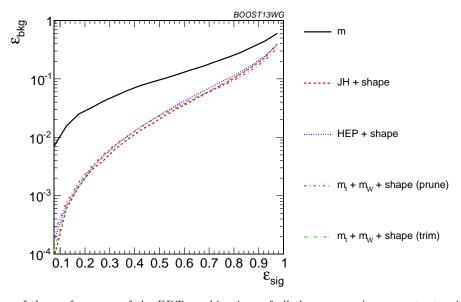


Fig. 33 Comparison of the performance of the BDT combinations of all the groomer/tagger outputs with all the available shape observables in the  $p_T = 1-1.1$  TeV bin using the anti- $k_T$  R=0.8 algorithm. Tagger/groomer outputs are combined with all of the following shape observables:  $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$ ,  $C_2^{(\beta=1)} + C_3^{(\beta=1)}$ ,  $\Gamma_{\text{Qjet}}$ .

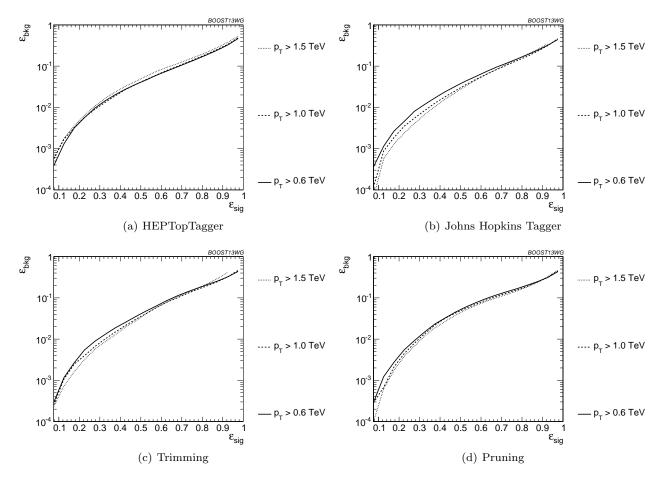


Fig. 34 Comparison of BDT combination of tagger performance at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm.

Optimizing at a single efficiency: The strongest as<sub>1288</sub> sumption we have made so far is that the taggers can<sub>289</sub> be reoptimized for each signal efficiency point. This is<sub>290</sub> useful for making a direct comparison of the power of<sub>291</sub> different top tagging algorithms, but is not particularly practical for the LHC analyses. We now consider the effects when the tagger inputs are optimized once, in<sub>292</sub> the  $\varepsilon_S = 0.3 - 0.35$  bin, and then used to determine the full ROC curve. We do this in the  $p_T 1 - 1.1$  TeV bin<sub>293</sub> and with R = 0.8.

The performance of each tagger, normalized to its<sub>295</sub> performance optimized in each bin, is shown in Fig<sub>1296</sub> ure 43 for cuts on the top mass and W mass, and in<sub>297</sub> Figure 44 for BDT combinations of tagger outputs and<sub>298</sub> shape variables. In both plots, it is apparent that op<sub>1299</sub> timizing the taggers in the 0.3-0.35 efficiency bin gives<sub>300</sub> comparable performance over efficiencies ranging from<sub>301</sub> 0.2-0.5, although performance degrades at small and<sub>302</sub> large signal efficiencies. Pruning appears to give espe<sub>1303</sub> cially robust signal-background discrimination without<sub>304</sub> re-optimization, possibly due to the fact that there are<sub>305</sub> no absolute distance or  $p_T$  scales that appear in the<sub>306</sub>

algorithm. Figures 43 and 44 suggest that, while optimization at all signal efficiencies is a useful tool for comparing different algorithms, it is not crucial to achieve good top-tagging performance in experiments.

## 7.5 Conclusions

We have studied the performance of various jet substructure observables, groomed masses, and top taggers to study the performance of top tagging at different  $p_T$  and jet radius parameter. At each  $p_T$ , R, and signal efficiency working point, we optimize the parameters for those observables with tuneable inputs. Overall, we have found that these techniques, individually and in combination, continue to perform well at high  $p_T$ , which is important for future LHC running. In general, the John Hopkins tagger performs best, while jet grooming algorithms under-perform relative to the best top taggers due to the lack of an optimized W-identification step. Tagger performance can be improved by a further factor of 2-4 through combination with jet substructure

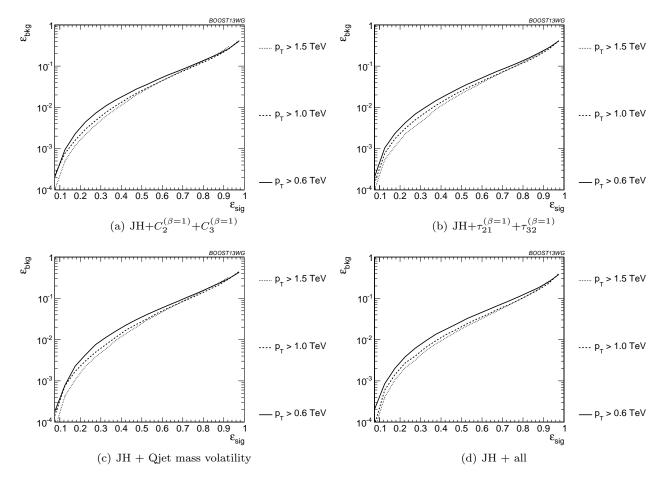


Fig. 35 Comparison of BDT combination of JH tagger + shape at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm.

observables such as  $\tau_{32}$ ,  $C_3$ , and Qjet mass volatility;<sup>328</sup> when combined with jet substructure observables, the<sup>329</sup> performance of various groomers and taggers becomes;<sup>330</sup> very comparable, suggesting that, taken together, the<sup>331</sup> observables studied are sensitive to nearly all of the<sup>332</sup> physical differences between top and QCD jets. A small;<sup>333</sup> improvement is also found by combining the Johns Hop<sup>334</sup> kins and HEPTopTaggers, indicating that different tag<sup>335</sup> gers are not fully correlated.

Comparing results at different  $p_T$  and R, top tag<sup>1338</sup> ging performance is generally better at smaller R due<sup>339</sup> to less contamination from uncorrelated radiation. Sim<sup>1340</sup> ilarly, most observables perform better at larger  $p_T$  due to the higher degree of collimation of radiation. Some observables fare worse at higher  $p_T$ , such as the N-subjettiness ratio  $\tau_{32}$  and the Qjet mass volatility  $\Gamma$ , as higher- $p_T$  QCD jets have more, harder emissions that fake the top jet substructure. The HEPTopTagger is also worse at large  $p_T$  due to the tendency of the tagger to shape backgrounds around the top mass. The  $p_T$ -and R-dependence of the multivariable combinations is

dominated by the  $p_T$ - and R-dependence of the top mass reconstruction component of the tagger/groomer.

Finally, we consider the performance of various observable combinations under the more realistic assumption that the input parameters are only optimized at a single  $p_T$ , R, or signal efficiency, and then the same inputs are used at other working points. Remarkably, the performance of all observables is typically within a factor of 2 of the fully optimized inputs, suggesting that while optimization can lead to substantial gains in performance, the general behaviour found in the fully optimized analyses extends to more general applications of each variable.

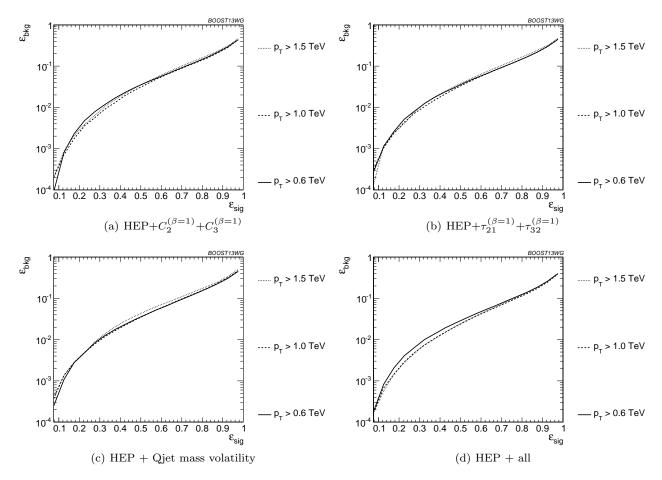


Fig. 36 Comparison of BDT combination of HEP tagger + shape at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm.

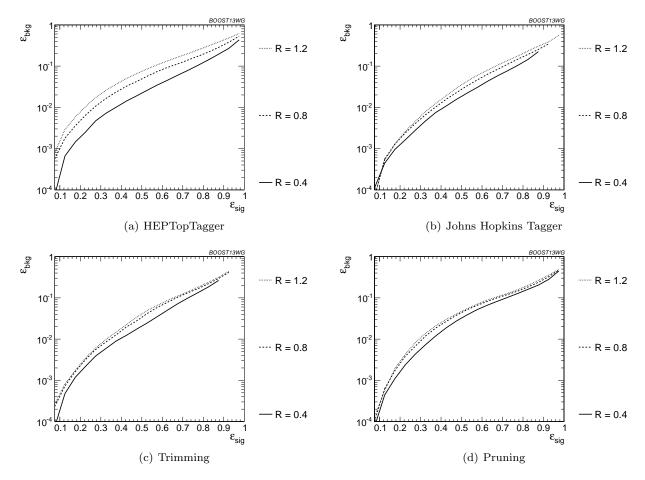


Fig. 37 Comparison of tagger and jet shape performance at different radius at  $p_T = 1.5$ -1.6 TeV.

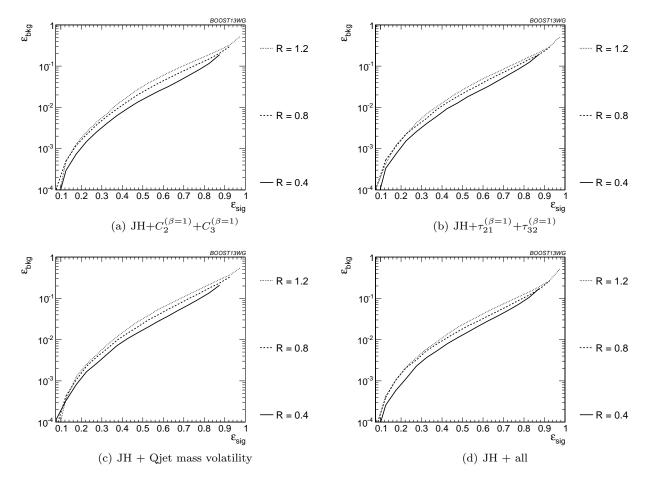


Fig. 38 Comparison of BDT combination of JH tagger + shape at different radius at  $p_T = 1.5$ -1.6 TeV.

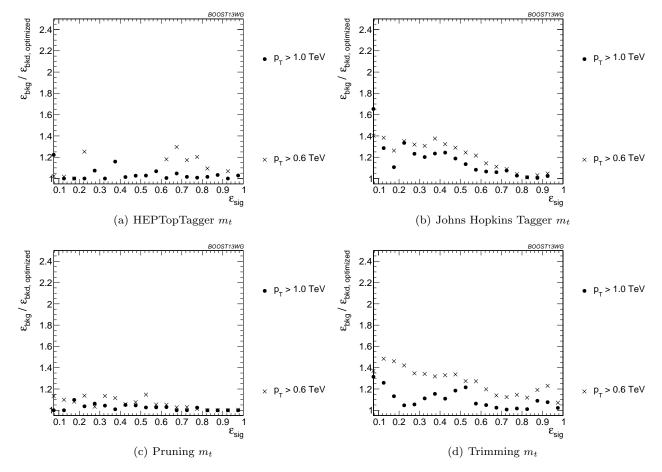


Fig. 39 Comparison of top mass performance of different taggers at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm; the tagger inputs are set to the optimum value for  $p_T = 1.5 - 1.6$  TeV.

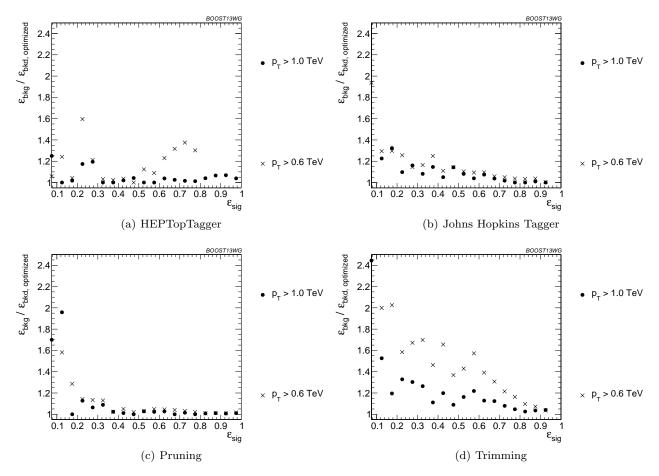


Fig. 40 Comparison of BDT combination of tagger performance at different  $p_T$  using the anti- $k_T$  R=0.8 algorithm; the tagger inputs are set to the optimum value for  $p_T = 1.5 - 1.6$  TeV.

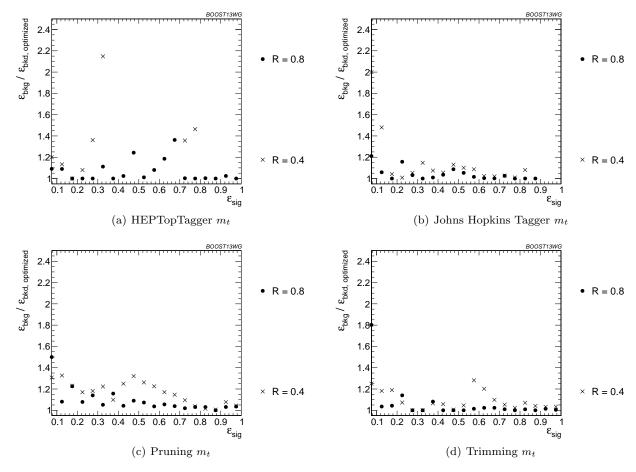


Fig. 41 Comparison of top mass performance of different taggers at different R in the  $p_T = 1500 - 1600$  GeV bin; the tagger inputs are set to the optimum value for R = 1.2.

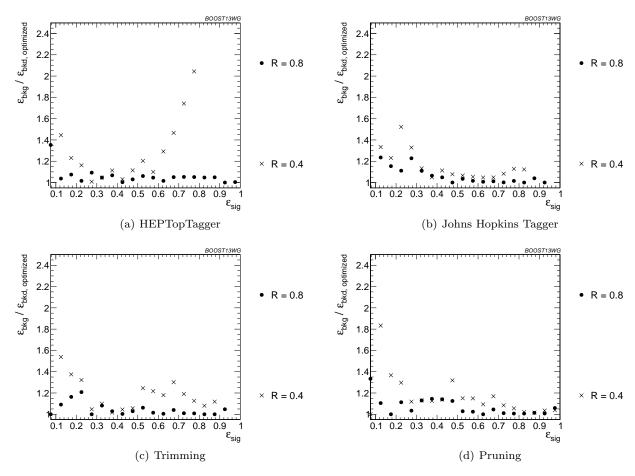


Fig. 42 Comparison of BDT combination of tagger performance at different radius at  $p_T = 1.5$ -1.6 TeV; the tagger inputs are set to the optimum value for R = 1.2.

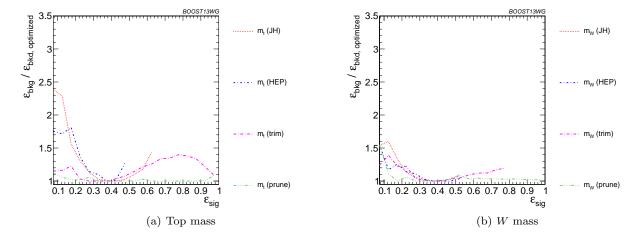


Fig. 43 Comparison of single-variable top-tagging performance in the  $p_T = 1-1.1$  GeV bin using the anti- $k_T$ , R=0.8 algorithm; the inputs for each tagger are optimized for the  $\varepsilon_{\rm sig} = 0.3-0.35$  bin.

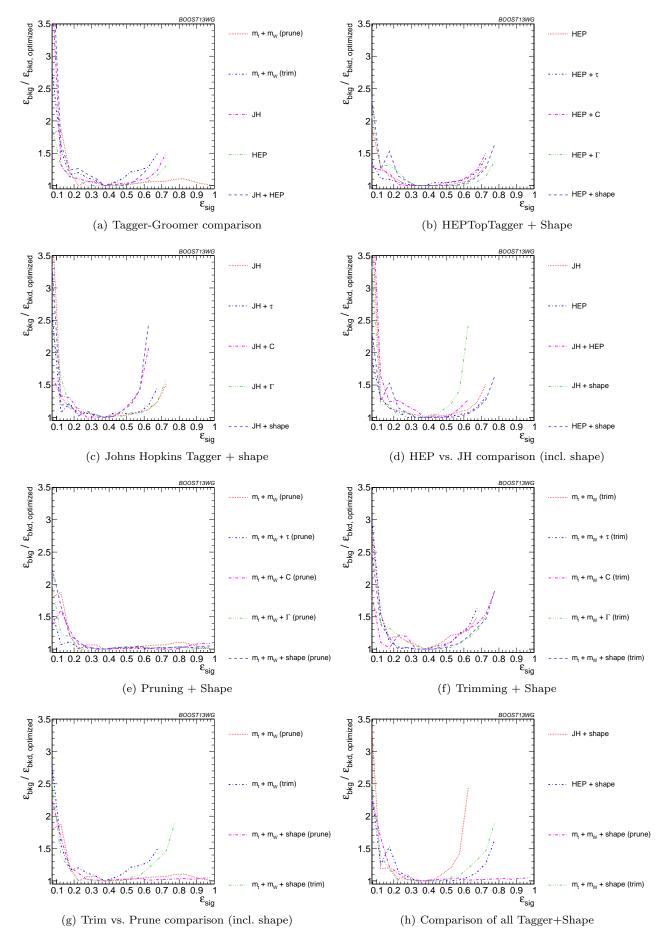


Fig. 44 The BDT combinations in the  $p_T=1-1.1$  TeV bin using the anti- $k_T$  R=0.8 algorithm. Taggers are combined with the following shape observables:  $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$ ,  $C_2^{(\beta=1)} + C_3^{(\beta=1)}$ ,  $\Gamma_{\rm Qjet}$ , and all of the above (denoted "shape"). The inputs for each tagger are optimized for the  $\varepsilon_{\rm sig}=0.3-0.35$  bin.

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## 8 Summary & Conclusions

In this report we have attempted to understand the delaster gree to which the discriminatory information in various jet substructure observables/taggers overlaps, and how this varies as a function of the parameters of the jets, such as their  $p_T$  and radius. This has been done by combining the variables into BDT discriminants, and comparing the background rejection power of this discriminant to the rejection power achieved by the in in dividual variables. The performance of "all variables" BDT discriminants has also been investigated, to une derstand the potential of the "ultimate" tagger where "all" available information (at least, all of that provided the variables considered) is used.

Ideas for general conclusions:

## Acknowledgements

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## References

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- A. Abdesselam, E. B. Kuutmann, U. Bitenc,
   G. Brooijmans, J. Butterworth, et al., Boosted objects: A Probe of beyond the Standard Model physics, Eur. Phys. J.
   C71 (2011) 1661, [arXiv:1012.5412].
- A. Altheimer, S. Arora, L. Asquith, G. Brooijmans, J. Butterworth, et al., Jet Substructure at the Tevatron and LHC: New results, new tools, new benchmarks, J.Phys. G39 (2012) 063001, [arXiv:1201.0008].
- A. Altheimer, A. Arce, L. Asquith, J. Backus Mayes, E. Bergeaas Kuutmann, et al., Boosted objects and jet substructure at the LHC, arXiv:1311.2708.
- A. Hoecker, P. Speckmayer, J. Stelzer, J. Therhaag,
   E. von Toerne, and H. Voss, TMVA: Toolkit for Multivariate Data Analysis, PoS ACAT (2007) 040,
   [physics/0703039].
- C. Anders, C. Bernaciak, G. Kasieczka, T. Plehn, and T. Schell, Benchmarking an Even Better HEPTopTagger, Phys. Rev. D89 (2014) 074047, [arXiv:1312.1504].

– It is clear from both the q/g tagging and W tagging studies that the correlation structure between the observables considered is complicated, being both  $p_T$  and R dependent.