Towards an Understanding of the Correlations in Jet Substructure

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Abstract Over the past decade, a large number of jet sub-51 structure observables have been proposed in the literature, 52 and explored at the LHC experiments. Such observables at-53 tempt to utilise the internal structure of jets in order to dis-54 tinguish those initiated by quarks, gluons, or by boosted 55 heavy objects, such as Top quarks and W bosons. This re-56 port, originating from and motivated by the BOOST201357 workshop, presents original particle-level studies that aim to 58 improve our understanding of the relationships between jet 59 substructure observables, their complementarity, and their 60 10 dependence on the underlying jet properties, particularly the 61 11 jet radius R and jet p_T . This is explored in the context of 62 12 quark/gluon discrimination, boosted W-boson tagging and 63 boosted Top quark tagging.

Keywords boosted objects · jet substructure · beyondthe-Standard-Model physics searches · Large Hadron Collider

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1 Introduction

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The center-of-mass energies at the Large Hadron Collider 72 are large compared to the heaviest of known particles, even 73 after accounting for parton density functions. With the start⁷⁴ of the second phase of operation in 2015, the center-of-mass⁷⁵ energy will further increase from 7 TeV in 2010-2011 and 76 8 TeV in 2012 to 13 TeV. Thus, even the heaviest states 77 in the Standard Model (and potentially previously unknown⁷⁸ particles) will often be produced at the LHC with substan-79 tial boosts, leading to a collimation of the decay products. 80 For fully hadronic decays, these heavy particles will not be 81 reconstructed as several jets in the detector, but rather as 82 a single hadronic jet with distinctive internal substructure.83 This realization has led to a new era of sophistication in our84 understanding of both standard Quantum Chromodynamics 85 (QCD) jets, as well as jets containing the decay of a heavy 86 particle, with an array of new jet observables and detec-87 tion techniques introduced and studied to distinguish the two88 types of jets. To allow the efficient propagation of results⁸⁹ from these studies of jet substructure, a series of BOOST90 Workshops have been held on an annual basis: SLAC (2009) [1], yses presented in this report are: B. Cooper, S. D. Ellis, Oxford University (2010) [2], Princeton University (2011) [39]; IFIC Valencia (2012) [4], University of Arizona (2013) [5], 93 and, most recently, University College London (2014) [6]. Following each of these meetings, working groups have generated reports highlighting the most interesting new results,94 and often including original particle-level studies. Previous BOOST reports can be found at [7–9].

This report from BOOST 2013 thus views the study and 96 implementation of jet substructure techniques as a fairly ma-97 ture field, and focuses on the question of the correlations98 between the plethora of observables that have been devel-99 oped and employed, and their dependence on the underly 100 ing jet parameters, especially the jet radius R and jet p_T . In new analyses developed for the report, we investigate the separation of a quark signal from a gluon background (q/g)tagging), a W signal from a gluon background (W-tagging) and a top signal from a mixed quark/gluon QCD background (top-tagging). In the case of top-tagging, we also investigate the performance of dedicated top-tagging algorithms, the HepTopTagger [10] and the Johns Hopkins Tagger [11]. We study the degree to which the discriminatory information provided by the observables and taggers overlaps by examining the extent to which the signal-background separation performance increases when two or more variables/taggers are combined in a multivariate analysis. Where possible, we provide a discussion of the physics behind the structure of the correlations and the p_T and R scaling that we observe.

We present the performance of observables in idealized simulations without pile-up and detector resolution effects; the relationship between substructure observables, their correlations, and how these depend on the jet radius R and jet p_T should not be too sensitive to such effects. Conducting studies using idealized simulations allows us to more clearly elucidate the underlying physics behind the observed performance, and also provides benchmarks for the development of techniques to mitigate pile-up and detector effects. A full study of the performance of pile-up and detector mitigation strategies is beyond the scope of the current report, and will be the focus of upcoming studies.

The report is organized as follows: in Sections 2-4, we describe the methods used in carrying out our analysis, with a description of the Monte Carlo event sample generation in Section 2, the jet algorithms, observables and taggers investigated in our report in Section 3, and an overview of the multivariate techniques used to combine multiple observables into single discriminants in Section 4. Our results follow in Sections 5-7, with q/g-tagging studies in Section 5, W-tagging studies in Section 6, and top-tagging studies in Section 7. Finally we offer some summary of the studies and general conclusions in Section 8.

The principal organizers of and contributors to the anal-M. Freytsis, A. Hornig, A. Larkoski, D. Lopez Mateos, B. Shuve, and N. V. Tran.

2 Monte Carlo Samples

Below, we describe the Monte Carlo samples used in the q/gtagging, W-tagging, and top-tagging sections of this report. Note that no pile-up (additional proton-proton interactions beyond the hard scatter) are included in any samples, and there is no attempt to emulate the degradation in angular and p_T resolution that would result when reconstructing the jets inside a real detector; such effects are deferred to future43 study.

2.1 Quark/gluon and W-tagging

Samples were generated at $\sqrt{s}=8$ TeV for QCD dijets, and₄₉ for W^+W^- pairs produced in the decay of a scalar reso₁₅₀ nance. The W bosons are decayed hadronically. The QCD₅₁ events were split into subsamples of gg and $q\bar{q}$ events, allowing for tests of discrimination of hadronic W bosons, quarks, and gluons.

Individual gg and $q\bar{q}$ samples were produced at leading order (LO) using MADGRAPH5 [12], while W^+W^- samples, were generated using the JHU GENERATOR [13–15]. Both, were generated using CTEQ6L1 PDFs [16]. The samples, were produced in exclusive p_T bins of width 100 GeV, with, the slicing parameter chosen to be the of any final state par, in this report were 300-400 GeV, 500-600 GeV and 1.0-1.1, this TeV. The samples were then showered through PYTHIAS, (version 8.176) [17] using the default tune 4C [18]. For each of the various samples (W, q, g) and p_T bins, 500k events were simulated.

2.2 Top-tagging

Samples were generated at $\sqrt{s}=14$ TeV. Standard Model⁶¹ dijet and top pair samples were produced with SHERPA 2.0.0⁶² [19–24], with matrix elements of up to two extra partons⁶³ matched to the shower. The top samples included only hadro100 decays and were generated in exclusive p_T bins of widtl⁶⁵ 100 GeV, taking as slicing parameter the top quark p_T . The⁶⁶ QCD samples were generated with a lower cut on the lead¹⁶⁷ ing parton-level jet p_T , where parton-level jets are clustered⁶⁸ with the anti- k_T algorithm and jet radii of R=0.4, 0.8, 1.2¹⁶⁹ The matching scale is selected to be $Q_{\rm cut}=40, 60, 80$ GeV for the $p_{T\,\rm min}=600, 1000,$ and 1500 GeV bins, respectively. For the top samples, 100k events were generated in each bin, while 200k QCD events were generated in each bin.

3 Jet Algorithms and Substructure Observables

In Sections 3.1, 3.2, 3.3 and 3.4, we describe the various jet algorithms, groomers, taggers and other substructure vari₁₇₁ ables used in these studies. Over the course of our study₁₇₂ we considered a larger set of observables, but for presenta₁₇₃ tion purposes we included only a subset in the final analysis₁₇₄ eliminating redundant observables.

3.1 Jet Clustering Algorithms

Jet clustering: Jets were clustered using sequential jet clustering algorithms [25] implemented in FASTJET 3.0.3. Final state particles i, j are assigned a mutual distance d_{ij} and a distance to the beam, d_{iB} . The particle pair with smallest d_{ij} are recombined and the algorithm repeated until the smallest distance is from a particle i to the beam, d_{iB} , in which case i is set aside and labelled as a jet. The distance metrics are defined as

$$d_{ij} = \min(p_{Ti}^{2\gamma}, p_{Tj}^{2\gamma}) \frac{\Delta R_{ij}^2}{R^2}, \tag{1}$$

$$d_{iB} = p_{Ti}^{2\gamma}, \tag{2}$$

where $\Delta R_{ij}^2 = (\Delta \eta_{ij})^2 + (\Delta \phi_{ij})^2$, with $\Delta \eta_{ij}$ being the separation in pseudorapidity of particles i and j, and $\Delta \phi_{ij}$ being the separation in azimuth. In this analysis, we use the anti- k_T algorithm ($\gamma = -1$) [26], the Cambridge/Aachen (C/A) algorithm ($\gamma = 0$) [27, 28], and the k_T algorithm ($\gamma = 1$) [29, 30], each of which has varying sensitivity to soft radiation in the definition of the jet.

Qjets: We also perform non-deterministic jet clustering [31, 32]. Instead of always clustering the particle pair with smallest distance d_{ij} , the pair selected for combination is chosen probabilistically according to a measure

$$P_{ij} \propto e^{-\alpha (d_{ij} - d_{\min})/d_{\min}},\tag{3}$$

where d_{\min} is the minimum distance for the usual jet clustering algorithm at a particular step. This leads to a different cluster sequence for the jet each time the Qjet algorithm is used, and consequently different substructure properties. The parameter α is called the rigidity and is used to control how sharply peaked the probability distribution is around the usual, deterministic value. The Qjets method uses statistical analysis of the resulting distributions to extract more information from the jet than can be found in the usual cluster sequence.

3.2 Jet Grooming Algorithms

Pruning: Given a jet, re-cluster the constituents using the C/A algorithm. At each step, proceed with the merger as usual unless both

$$\frac{\min(p_{Ti}, p_{Tj})}{p_{Tij}} < z_{\text{cut}} \text{ and } \Delta R_{ij} > \frac{2m_j}{p_{Tj}} R_{\text{cut}}, \tag{4}$$

in which case the merger is vetoed and the softer branch discarded. The default parameters used for pruning [33] in this report are $z_{\rm cut}=0.1$ and $R_{\rm cut}=0.5$, unless otherwise stated. One advantage of pruning is that the thresholds used to veto soft, wide-angle radiation scale with the jet kinematics, and

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so the algorithm is expected to perform comparably over 2007 wide range of momenta.

Trimming: Given a jet, re-cluster the constituents into sub₂₁₀ jets of radius R_{trim} with the k_T algorithm. Discard all subjets₁₁₁ i with

$$p_{Ti} < f_{\text{cut}} p_{TJ}.$$
 (5)

The default parameters used for trimming [34] in this reportance $R_{\text{trim}} = 0.2$ and $f_{\text{cut}} = 0.03$, unless otherwise stated.

Filtering: Given a jet, re-cluster the constituents into subjets of radius $R_{\rm filt}$ with the C/A algorithm. Re-define the jet to consist of only the hardest N subjets, where N is determined by the final state topology and is typically one more than the number of hard prongs in the resonance decay (to include the leading final-state gluon emission) [35]. While we do not independently use filtering, it is an important step of the HEPTopTagger to be defined later.

Soft drop: Given a jet, re-cluster all of the constituents using the C/A algorithm. Iteratively undo the last stage of the C/A clustering from j into subjets j_1 , j_2 . If

$$\frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} < z_{\text{cut}} \left(\frac{\Delta R_{12}}{R}\right)^{\beta}, \qquad (6)_{230}^{229}$$

discard the softer subjet and repeat. Otherwise, take j to be the final soft-drop jet [36]. Soft drop has two input parameters, the angular exponent β and the soft-drop scale $z_{\text{cut}_{234}}$. In these studies we use the default $z_{\text{cut}} = 0.1$ setting, with $\beta = 2$.

3.3 Jet Tagging Algorithms

Modified Mass Drop Tagger: Given a jet, re-cluster all of the constituents using the C/A algorithm. Iteratively undo the last stage of the C/A clustering from j into subjets j_1 , j_2 with $m_{j_1} > m_{j_2}$. If either

$$m_{j_1} > \mu \, m_j \text{ or } \frac{\min(p_{T1}^2, p_{T2}^2)}{m_j^2} \, \Delta R_{12}^2 < y_{\text{cut}},$$
 (7)

then discard the branch with the smaller transverse $\max_{246} m_T = \sqrt{m_i^2 + p_{Ti}^2}$, and re-define j as the branch with the arger transverse mass. Otherwise, the jet is tagged. If de 248 clustering continues until only one branch remains, the jet49 is considered to have failed the tagging criteria [37]. In this study we use by default $\mu = 1.0$ (i.e. implement no mass drop criteria) and $y_{\rm cut} = 0.1$. With respect to the singulars parts of the splitting functions, this describes the same algo253 rithm as running soft drop with $\beta = 0$.

Johns Hopkins Tagger: Re-cluster the jet using the C/A algorithm. The jet is iteratively de-clustered, and at each step the softer prong is discarded if its p_T is less than $\delta_p p_{Tjet}$. This continues until both prongs are harder than the p_T threshold, both prongs are softer than the p_T threshold, or if they are too close $(|\Delta \eta_{ij}| + |\Delta \phi_{ij}| < \delta_R)$; the jet is rejected if either of the latter conditions apply. If both are harder than the $p_{\rm T}$ threshold, the same procedure is applied to each: this results in 2, 3, or 4 subjets. If there exist 3 or 4 subjets, then the jet is accepted: the top candidate is the sum of the subjets, and W candidate is the pair of subjets closest to the W mass [11]. The output of the tagger is the mass of the top candidate (m_t) , the mass of the W candidate (m_W) , and θ_h , a helicity angle defined as the angle, measured in the rest frame of the W candidate, between the top direction and one of the W decay products. The two free input parameters of the John Hopkins tagger in this study are δ_p and δ_R , defined above, and their values are optimized for different jet kinematics and parameters in Section 7.

HEPTopTagger: Re-cluster the jet using the C/A algorithm. The jet is iteratively de-clustered, and at each step the softer prong is discarded if $m_1/m_{12} > \mu$ (there is not a significant mass drop). Otherwise, both prongs are kept. This continues until a prong has a mass $m_i < m$, at which point it is added to the list of subjets. Filter the jet using $R_{\rm filt} = \min(0.3, \Delta R_{ij})$, keeping the five hardest subjets (where ΔR_{ij} is the distance between the two hardest subjets). Select the three subjets whose invariant mass is closest to m_t [10]. The output of the tagger is m_t , m_W , and θ_h (as defined in the Johns Hopkins Tagger). The two free input parameters of the HEPTopTagger in this study are m and μ , defined above, and their values are optimized for different jet kinematics and parameters in Section 7.

Top-tagging with Pruning or Trimming: In the studies presented in Section 7 we add a W reconstruction step to the pruning and trimming algorithms, to enable a fairer comparison with the dedicated top tagging algorithms described above. A W candidate is found as follows: if there are two subjets, the highest-mass subjet is the W candidate (because the W prongs end up clustered in the same subjet), and the W candidate mass, m_W , the mass of this subjet; if there are three subjets, the two subjets with the smallest invariant mass comprise the W candidate, and m_W is the invariant mass of this subjet pair. In the case of only one subjet, no W is reconstructed. The top mass, m_t , is the full mass of the groomed jet.

3.4 Other Jet Substructure Observables

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The jet substructure observables defined in this section are calculated using jet constituents prior to any grooming. This approach has been used in several analyses in the past, for example [38, 39], whilst others have used the approach of only considering the jet constituents that survive the grooming procedure [40]. We expect that, in the absence of pile-up, the difference between these approaches will be small.

Qjet mass volatility: As described above, Qjet algorithms re-cluster the same jet non-deterministically to obtain a collection of interpretations of the jet. For each jet interpretation, the pruned jet mass is computed with the default pruning parameters. The mass volatility, Γ_{Ojet} , is defined as [31]

$$\Gamma_{
m Qjet} = rac{\sqrt{\langle m_J^2
angle - \langle m_J
angle^2}}{\langle m_J
angle},$$
 (8) $^{
m 283}_{
m 285}$

where averages are computed over the Qjet interpretations. We use a rigidity parameter of $\alpha=0.1$ (although other stud₂₈₆ ies suggest a smaller value of α may be optimal [31, 32]), and 25 trees per event for all of the studies presented here. ₂₈₇

N-subjettiness: *N*-subjettiness [41] quantifies how well the serial radiation in the jet is aligned along *N* directions. To compute *N*-subjettiness, $\tau_N^{(\beta)}$, one must first identify *N* axes withing the jet. Then,

$$\tau_N^{\beta} = \frac{1}{d_0} \sum_i p_{Ti} \min\left(\Delta R_{1i}^{\beta}, \dots, \Delta R_{Ni}^{\beta}\right), \tag{9}$$

where distances are between particles i in the jet and the axes,

$$d_0 = \sum_{i} p_{Ti} R^{\beta} \tag{10}^{999}$$

and R is the jet clustering radius. The exponent β is a free parameter. There is also some choice in how the axes used to compute N-subjettiness are determined. The optimal configuration of axes is the one that minimizes N-subjettiness; recently, it was shown that the "winner-take-all" (WTA) axes₀₄ can be easily computed and have superior performance compared to other minimization techniques [42]. We use bothos the WTA (Section 7) and one-pass k_T optimization axes (Secotions 5 and 6) in our studies.

Often, a powerful discriminant is the ratio,

$$\tau_{N,N-1}^{\beta} \equiv \frac{\tau_N^{\beta}}{\tau_{N-1}^{\beta}}.\tag{11}_{_{_{_{_{_{_{_{_{1}}}}}}}}}$$

While this is not an infrared-collinear (IRC) safe observable313 it is calculable [43] and can be made IRC safe with a loose14

lower cut on τ_{N-1} .

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Energy correlation functions: The transverse momentum version of the energy correlation functions are defined as [44]:

$$ECF(N,\beta) = \sum_{i_1 < i_2 < \dots < i_N \in j} \left(\prod_{a=1}^N p_{Ti_a} \right) \left(\prod_{b=1}^{N-1} \prod_{c=b+1}^N \Delta R_{i_b i_c} \right)^{\beta},$$
(12)

where *i* is a particle inside the jet. It is preferable to work in terms of dimensionless quantities, particularly the energy correlation function double ratio:

$$C_N^{\beta} = \frac{\text{ECF}(N+1,\beta) \, \text{ECF}(N-1,\beta)}{\text{ECF}(N,\beta)^2}.$$
 (13)

This observable measures higher-order radiation from leading-order substructure. Note that $C_2^{\beta=0}$ is identical to the variable p_TD introduced by CMS in [45].

4 Multivariate Analysis Techniques

Multivariate techniques are used to combine multiple variables into a single discriminant in an optimal manner. The extent to which the discrimination power increases in a multivariable combination indicates to what extent the discriminatory information in the variables overlaps. There exist alternative strategies for studying correlations in discrimination power, such as "truth matching" [46], but these are not explored here.

In all cases, the multivariate technique used to combine variables is a Boosted Decision Tree (BDT) as implemented in the TMVA package [47]. An example of the BDT settings used in these studies, chosen to reduce the effect of overtraining, is given in [47]. The BDT implementation including gradient boost is used. Additionally, the simulated data were split into training and testing samples and comparisons of the BDT output were compared to ensure that the BDT performance was not affected by overtraining.

5 Quark-Gluon Discrimination

In this section, we examine the differences between quarkand gluon-initiated jets in terms of substructure variables. At a fundamental level, the primary difference between quarkand gluon-initiated jets is the color charge of the initiating parton, typically expressed in terms of the ratio of the corresponding Casimir factors $C_F/C_A = 4/9$. Since the quark has the smaller color charge, it radiates less than a corresponding gluon and the naive expectation is that the resulting quark jet will contain fewer constituents than the corresponding gluon jet. The differing color structure of the two types of jet will

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also be realized in the detailed behavior of their radiations64 patterns. We determine the extent to which the substructure 65 observables capturing these differences are correlated, pros66 viding some theoretical understanding of these variables and 67 their performance. The motivation for these studies arises 68 not only from the desire to "tag" a jet as originating from a69 quark or gluon, but also to improve our understanding of the quark and gluon components of the QCD backgrounds rel371 ative to boosted resonances. While recent studies have sug₃₇₂ gested that quark/gluon tagging efficiencies depend highly, on the Monte Carlo generator used [48, 49], we are more₇₄ interested in understanding the scaling performance with $p_{T_{375}}$ and R, and the correlations between observables, which are $_{76}$ expected to be treated consistently within a single shower, scheme.

Other examples of recent analytic studies of the corre₃₇₉ lations between jet observables relevant to quark jet versuş₈₀ gluon jet discrimination can be found in [43, 46, 50, 51].

5.1 Methodology and Observable Classes

These studies use the qq and gg MC samples described in Section 2. The showered events were clustered with FAST₃₈₇ JET 3.03 using the anti- k_T algorithm with jet radii of $R = _{388}$ 0.4, 0.8, 1.2. In both signal (quark) and background (gluon) gag samples, an upper and lower cut on the leading jet p_T is applied after showering/clustering, to ensure similar p_T spectra for signal and background in each p_T bin. The bins in leading jet p_T that are considered are 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV, for the 300-400 GeV, 500-600 GeV, 1.0-301 1.1 TeV parton p_T slices respectively. Various jet grooming approaches are applied to the jets, as described in Sec-393 tion 3.4. Only leading and subleading jets in each sample are used. The following observables are studied in this section:

- Number of constituents (n_{constits}) in the jet.
- Pruned Qjet mass volatility, Γ_{Qjet} .
- 1-point energy correlation functions, C₁^β with β = 0, 1, 2.
 1-subjettiness, τ₁^β with β = 1, 2. The *N*-subjettiness axes are computed using one-pass k_t axis optimization.
- Ungroomed jet mass, m.

For simplicity, we hereafter refer to quark-initiated jets (gluons initiated jets) as quark jets (gluon jets).

We will demonstrate that, in terms of their jet-by-jet cor₄₀₅ relations and their ability to separate quark jets from gluon₁₀₆ jets, the above observables fall into five Classes. The first three observables, n_{constits} , Γ_{Qjet} and $C_1^{\beta=0}$, each constitutes and a Class of its own (Classes I to III) in the sense that theyoo each carry some independent information about a jet and410 when combined, provide substantially better quark jet and gluon jet separation than any one observable alone. Of the remaining observables, $C_1^{\beta=1}$ and $\tau_1^{\beta=1}$ comprise a single is single in the sum of t class (Class IV) because their distributions are similar for a sample of jets, their jet-by-jet values are highly correlated, and they exhibit very similar power to separate quark jets and gluon jets (with very similar dependence on the jet parameters R and p_T); this separation power is not improved when they are combined. The fifth class (Class V) is composed of $C_1^{\beta=2}$, $au_1^{\beta=2}$ and the (ungroomed) jet mass. Again the jet-by-jet correlations are strong (even though the individual observable distributions are somewhat different), the quark versus gluon separation power is very similar (including the R and p_T dependence), and little is achieved by combining more than one of the Class V observables. This class structure is not surprising given that the observables within a class exhibit very similar dependence on the kinematics of the underlying jet constituents. For example, the members of Class V are constructed from of a sum over pairs of constituents using products of the energy of each member of the pair times the angular separation squared for the pair (this is apparent for the ungroomed mass when viewed in terms of a mass-squared with small angular separations). By the same argument, the Class IV and Class V observables will be seen to be more similar than any other pair of classes, differing only in the power (β) of the dependence on the angular separations, which produces small but detectable differences. We will return to a more complete discussion of jet masses in Section 5.4.

5.2 Single Variable Discrimination

In Figure 1 are shown the quark and gluon distributions of different substructure observables in the $p_T = 500 - 600$ GeV bin for R = 0.8 jets. These distributions illustrate some of the distinctions between the Classes made above. The fundamental difference between quarks and gluons, namely their color charge and consequent amount of radiation in the jet, is clearly indicated in Figure 1(a), suggesting that simply counting constituents provides good separation between quark and gluon jets. In fact, among the observables considered, one can see by eye that n_{constits} should provide the highest separation power, i.e., the quark and gluon distributions are most distinct, as was originally noted in [49, 52]. Figure 1 further suggests that $C_1^{\beta=0}$ should provide the next best separation, followed by $C_1^{\beta=1}$, as was also found by the CMS and ATLAS Collaborations [48, 53].

To more quantitatively study the power of each observable as a discriminator for quark/gluon tagging, Receiver Operating Characteristic (ROC) curves are built by scanning each distribution and plotting the background efficiency (to select gluon jets) vs. the signal efficiency (to select quark jets). Figure 2 shows these ROC curves for all of the substructure variables shown in Figure 1 for R = 0.4, 0.8 and 1.2 jets (in the $p_T = 300\text{-}400$ GeV bin). In addition, the ROC



Fig. 1 Comparisons of quark and gluon distributions of different substructure variables, organized by Class, for leading jets in the $p_T = 500 - 600$ GeV bin using the anti- k_T R = 0.8 algorithm. The first three plots are Classes I-III, with Class IV in the second row, and Class V in the third row

curve for a tagger built from a BDT combination of all tha22 variables (see Section 4) is shown. As suggested earlier, $n_{\text{con}9488}$ is the best performing variable for all R values, although24 $C_1^{\beta=0}$ is not far behind, particularly for R=0.8. Most other25 variables have similar performance, with the main excep426 tion of Γ_{Qjet} , which shows significantly worse discrimina427 tion (this may be due to our choice of rigidity $\alpha=0.1$, with other studies suggesting that a smaller value, such a928

 $\alpha=0.01$, produces better results [31, 32]). The combination of all variables shows somewhat better discrimination than any individual observable, and we give a more detailed discussion in Section 5.3 of the correlations between the observables and their impact on the combined discrimination power.

We now examine how the performance of the substructure observables varies with p_T and R. To present the results

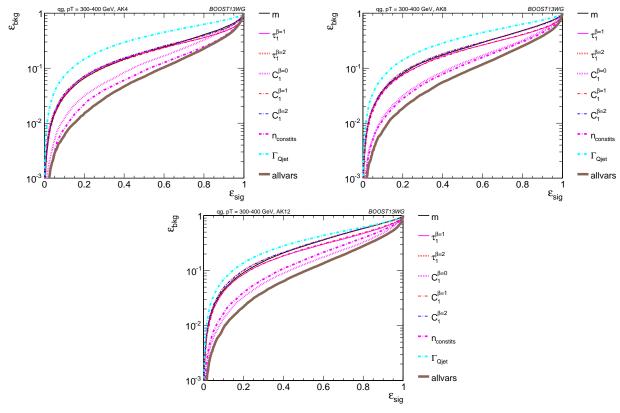


Fig. 2 The ROC curve for all single variables considered for quark-gluon discrimination in the p_T 300-400 GeV bin using the anti- k_T R = 0.4 (top-left), 0.8 (top-right) and 1.2 (bottom) algorithm.

in a "digestible" fashion we focus on the gluon jet "rejec455 tion" factor, $1/\epsilon_{\rm bkg}$, for a quark signal efficiency, $\epsilon_{\rm sig}$, of 50%. We can use the values of $1/\epsilon_{\rm bkg}$ generated for the 957 kinematic points introduced above (R=0.4,0.8,1.2 and thas 100 GeV p_T bins with lower limits $p_T=300\,{\rm GeV}$, 500 GeV 4559 1000 GeV) to generate surface plots. The surface plots in Figure 3 indicate both the level of gluon rejection and thas variation with p_T and R for each of the studied single ob462 servable. The color shading in these plots is defined so that a63 value of $1/\epsilon_{\rm bkg} \simeq 1$ yields the color "violet", while $1/\epsilon_{\rm bkg} \simeq$ 464 20 yields the color "red". The "rainbow" of colors in be465 tween vary linearly with $\log_{10}(1/\epsilon_{\rm bkg})$.

We organize our results by the classes introduced in the previous subsection: 468

Class I: The sole constituent of this class is $n_{\rm constits}$. We see in Figure 3(a) that, as expected, the numerically largest re⁴⁷⁰ jection rates occur for this observable, with the rejection fac⁴⁷¹ tor ranging from 6 to 11 and varying rather dramatically with 72 R. As R increases the jet collects more constituents from the 73 underlying event, which are the same for quark and gluon 74 jets, and the separation power decreases. At large R, there is 975 some improvement with increasing p_T due to the enhanced 76 QCD radiation, which is different for quarks vs. gluons.

Class II: The variable $\Gamma_{\rm Qjet}$ constitutes this class. Figure 3(b)78 confirms the limited efficacy of this single observable (at 70)

least for our parameter choices) with a rejection rate only in the range 2.5 to 2.8. On the other hand, this observable probes a very different property of jet substructure, *i.e.*, the sensitivity to detailed changes in the grooming procedure, and this difference is suggested by the distinct R and p_T dependence illustrated in Figure 3(b). The rejection rate increases with increasing R and decreasing p_T , since the distinction between quark and gluon jets for this observable arises from the relative importance of the one "hard" gluon emission configuration. The role of this contribution is enhanced for both decreasing p_T and increasing R.

Class III: The only member of this class is $C_1^{\beta=0}$. Figure 3(c) indicates that this observable can itself provide a rejection rate in the range 7.8 to 8.6 (intermediate between the two previous observables), and again with distinct R and p_T dependence. In this case the rejection rate decreases slowly with increasing R, which follows from the fact that $\beta=0$ implies no weighting of ΔR in the definition of $C_1^{\beta=0}$, greatly reducing the angular dependence. The rejection rate peaks at intermediate p_T values, an effect visually enhanced by the limited number of p_T values included.

Class IV: Figures 3(d) and (e) confirm the very similar properties of the observables $C_1^{\beta=1}$ and $\tau_1^{\beta=1}$ (as already suggested in Figures 1(d) and (e)). They have essentially identical rejection rates (4.1 to 5.4) and identical R and p_T dependent

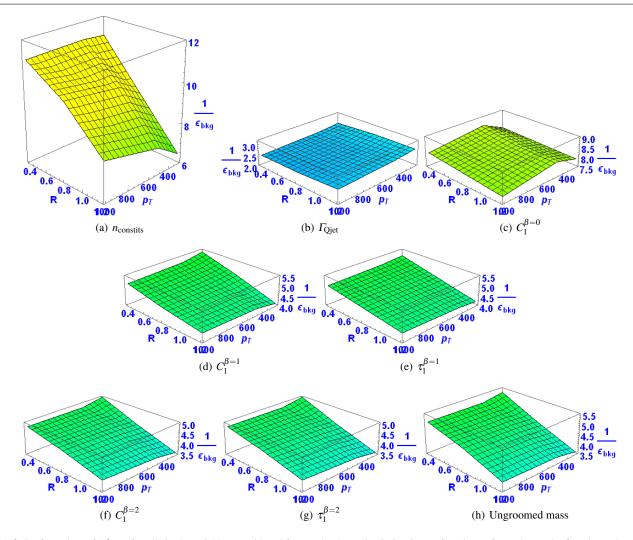


Fig. 3 Surface plots of $1/\varepsilon_{\text{bkg}}$ for all single variables considered for quark-gluon discrimination as functions of R and p_T . The first three plots are Classes I-III, with Class IV in the second row, and Class V in the third row.

dence (a slow decrease with increasing R and an even slower increase with increasing p_T).

Class V: The observables $C_1^{\beta=2}$, $\tau_1^{\beta=2}$, and m have similarejection rates in the range 3.5 to 5.3, as well as very similareform R and p_T dependence (a slow decrease with increasing R^{502} and an even slower increase with increasing p_T).

Arguably, drawing a distinction between the Class IV and Class V observables is a fine point, but the color shading does suggest some distinction from the slightly smaller rejection rate in Class V. Again the strong similarities between the plots within the second and third rows in Figure 3 speaks to the common properties of the observables within the two classes.

In summary, the overall discriminating power between quark and gluon jets tends to decrease with increasing R, exsice cept for the $\Gamma_{\rm Qjet}$ observable, presumably in large part due to the contamination from the underlying event. Since the consize struction of the $\Gamma_{\rm Qjet}$ observable explicitly involves pruning 13

away the soft, large angle constituents, it is not surprising that it exhibits different R dependence. In general the discriminating power increases slowly and monotonically with p_T (except for the $\Gamma_{\rm Qjet}$ and $C_1^{\beta=0}$ observables). This is presumably due to the overall increase in radiation from high p_T objects, which accentuates the differences in the quark and gluon color charges and providing some increase in discrimination. In the following section, we study the effect of combining multiple observables.

5.3 Combined Performance and Correlations

Combining multiple observables in a BDT can give further improvement over cuts on a single variable. Since the improvement from combining correlated observables is expected to be inferior to that from combining uncorrelated observables, studying the performance of multivariable combinations gives insight into the correlations between substructure

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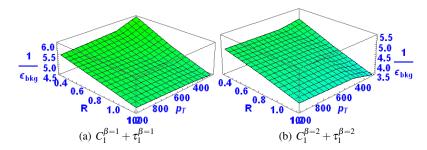


Fig. 4 Surface plots of $1/\epsilon_{\rm bkg}$ for the indicated pairs of variables from (a) Class IV and (b) Class V considered for quark-gluon discrimination as functions of R and p_T .

variables and the physical features allowing for quark/gluonьsa discrimination. Based on our discussion of the correlated properties of observables within a single class, we expect little improvement in the rejection rate when combining ob servables from the same class, and substantial improvement when combining observables from different classes. Our class sification of observables for quark/gluon tagging therefore motivates the study of particular combinations of variables for use in experimental analyses.

To quantitatively study the improvement obtained from 562 multivariate analyses, we build quark/gluon taggers from ev-563 ery pair-wise combination of variables studied in the pre564 vious section; we also compare the pair-wise performance 565 with the all-variables combination. To illustrate the results66 achieved in this way, we use the same 2D surface plots as 657 in Figure 3. Figure 4 shows pair-wise plots for variables in F68 (a) Class IV and (b) Class V, respectively. Comparing to 569 the corresponding plots in Figure 3, we see that combin⁵⁷⁰ ing $C_1^{\beta=1}+\tau_1^{\beta=1}$ provides a small (\sim 10%) improvement in the rejection rate with essentially no change in the R and $p_{T_{\bf 572}}$ dependence, while combining $C_1^{\beta=2}+\tau_1^{\beta=2}$ yields a rejection tion rate that is essentially identical to the single observable rejection rate for all R and p_T values (with a similar conclusion if one of these observables is replaced with the ungroomed jet mass m). This confirms the expectation that the observables within a single class effectively probe the same, jet properties.

Next, we consider cross-class pairs of observables in Fig₅₈₀ ure 5, where, except in the one case noted below, we use₆₈₁ only a single observable from each class for illustrative pur₅₈₂ poses. Since n_{constits} is the best performing single variable, the largest rejection rates are obtained from combining another observable with n_{constits} (Figures 5(a) to (e)). In general, the rejection rates are larger for the pair-wise case than for the single variable case. In particular, the pair $n_{\text{constits}} + \frac{580}{587}$ in Figure 5(b) yields rejection rates in the range 6.4 to 14.7 with the largest values at small R and large p_T . As expected, the pair $n_{\text{constits}} + \tau_1^{\beta=1}$ in Figure 5(e) yields very similar rejection rates (6.4 to 15.0), since $C_1^{\beta=1}$ and $\tau_1^{\beta=1}$ are both in Class IV. The other pairings with n_{constits} yield

smaller rejection rates and smaller dynamic ranges. The pair $n_{\text{constits}} + C_1^{\beta=0}$ (Figure 5(d)) exhibits the smallest range of rates (8.3 to 11.3), suggesting that the differences between these two observables serve to substantially reduce the R and p_T dependence for the pair, but this also serves to reduce the possible optimization of the observables required. The other pairs shown exhibit similar behavior.

The R and p_T dependence of the pair-wise combinations is generally similar to the single observable with the most dependence on R and p_T . The smallest R and p_T variation always occurs when pairing with $C_1^{\beta=0}$. Changing any of the observables in these pairs with a different observable in the same class $(e.g., C_1^{\beta=2} \text{ for } \tau_1^{\beta=2})$ produces very similar results. Figure 5(k) shows the result of a BDT analysis including all of the current observables with rejection rates in the range 10.5 to 17.1. This is a somewhat narrower range than in Figure 5(b) but with larger maximum values.

Some features are more easily seen with an alternative presentation of the data: we fix R and p_T and simultaneously show the single- and pair-wise observables performance in a single matrix, and these matrices are shown in Figures 6 and 7. The numbers in each cell are the same rejection rate for gluons used earlier, $1/\epsilon_{bkg}$, with $\epsilon_{sig} = 50\%$ (quarks). Figure 6 shows the results for $p_T = 1 - 1.1$ TeV and R =0.4, 0.8, 1.2, while Figure 7 is for R = 0.4 and the 3 p_T bins. The single observable rejection rates appear on the diagonal, and the pairwise results are off the diagonal. The largest pair-wise rejection rate, as already suggested by Figure 5(e), appears at large p_T and small R for the pair $n_{\text{constits}} + \tau_1^{\beta=1}$ (with very similar results for $n_{\text{constits}} + C_1^{\beta=1}$). The correlations indicated by the shading 1 should be largely understood as indicating the organization of the observables into the now-familiar classes. The all-observable (BDT) result appears as the number at the lower right in each plot.

¹The connection between the value of the rejection rate and the shading color in Figures 6 and 7 is the same as that in Figures 3 to 5.



Fig. 5 Surface plots of $1/\epsilon_{\rm bkg}$ for the indicated pairs of variables from different classes considered for quark-gluon discrimination as functions of R and p_T .

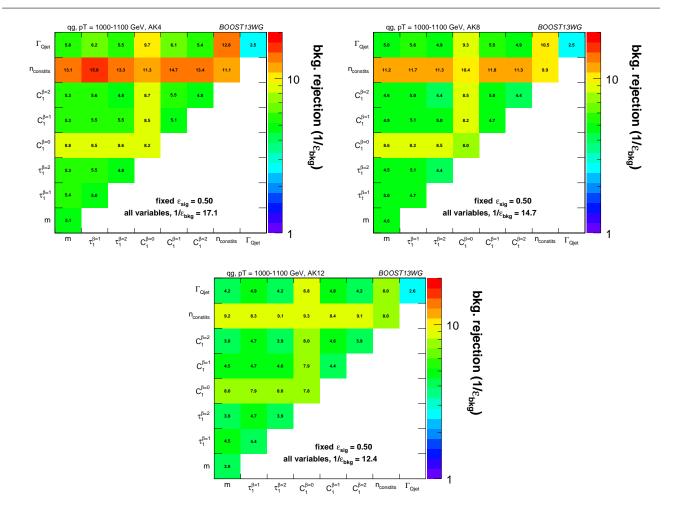


Fig. 6 Gluon rejection defined as $1/\varepsilon_{\text{gluon}}$ when using each 2-variable combination as a tagger with 50% acceptance for quark jets. Results are shown for jets with $p_T = 1 - 1.1$ TeV and for (top left) R = 0.4; (top right) R = 0.8; (bottom) R = 1.2. The rejection obtained with a tagger that uses all variables is also shown in the plots.

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5.4 QCD Jet Masses

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To close the discussion of q/g-tagging, we provide some insight into the behavior of the masses of QCD jets initiated by both kinds of partons, with and without grooming. Recall that, in practice, an identified jet is simply a list of constituents, *i.e.*, final state particles. To the extent that the masses of these individual constituents can be neglected (due to the constituents being relativistic), each constituent has a "well- defined" 4-momentum from its energy and direction. It follows that the 4-momentum of the jet is simply the sum of the 4-momenta of the constituents and its square is the jet mass squared. Simply on dimensional grounds, we know that jet mass must have an overall linear scaling with p_T , with the remaining p_T dependence arising predominantly from the running of the coupling, $\alpha_s(p_T)$. The R dependence is also crudely linear as the jet mass scales approximately with the largest angular opening between any 2 constituents, which is set by R.

To demonstrate this universal behavior for jet mass, we first note that if we consider the mass distributions for many kinematic points (various values of R and p_T), we observe considerable variation in behaviour. This variation, however, can largely be removed by plotting versus the scaled variable $m/p_T/R$. The mass distributions for quark and gluon jets versus $m/p_T/R$ for all of our kinematic points are shown in Figure 8, where we use a logarithmic scale on the y-axis to clearly exhibit the behavior of these distributions over a large dynamic range. We observe that the distributions for the different kinematic points do approximately scale as expected, i.e., the simple arguments above capture most of the variation with R and p_T . We will consider shortly an explanation of the residual non-scaling. A more rigorous quantitative understanding of jet mass distributions requires allorders calculations in QCD, which have been performed for ungroomed jet mass spectra at high logarithmic accuracy, both in the context of direct QCD resummation [54, 55] and Soft Collinear Effective Theory [56, 57].

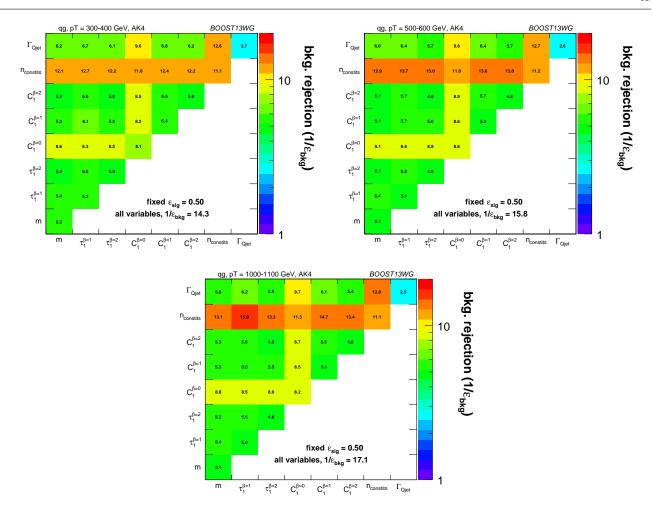


Fig. 7 Gluon rejection defined as $1/\varepsilon_{\text{gluon}}$ when using each 2-variable combination as a tagger with 50% acceptance for quark jets. Results are shown for R=0.4 jets with (top left) $p_T=300-400$ GeV, (top right) $p_T=500-600$ GeV and (bottom) $p_T=1-1.1$ TeV. The rejection obtained with a tagger that uses all variables is also shown in the plots.

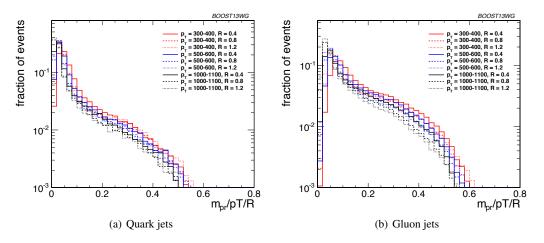


Fig. 8 Comparisons of quark and gluon ungroomed mass distributions versus the scaled variable $m/p_T/R$.

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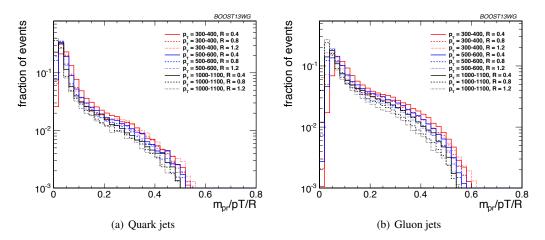


Fig. 9 Comparisons of quark and gluon pruned mass distributions versus the scaled variable $m_{\rm pr}/p_T/R$.

Several features of Figure 8 can be easily understood₆₅₉ The distributions all cut off rapidly for $m/p_T/R > 0.5$, which is understood as the precise limit (maximum mass) for a661 jet composed of just 2 constituents. As expected from the 62 soft and collinear singularities in QCD, the mass distribute63 tion peaks at small mass values. The actual peak is "pushed" 664 away from the origin by the so-called Sudakov form face665 tor. Summing the corresponding logarithmic structure (sin 666 gular in both p_T and angle) to all orders in perturbation the 667 ory yields a distribution that is highly damped as the massis vanishes. In words, there is precisely zero probability that about color parton emits no radiation (and the resulting jet has zero-70 mass). Above the Sudakov-suppressed part of phase space 671 there are two structures in the distribution: the "shoulder"672 and the "peak". The large mass shoulder $(0.3 < m/p_T/R <_{673}$ 0.5) is driven largely by the presence of a single large anera gle, energetic emission in the underlying QCD shower, i.e. 675 this regime is quite well described by low-order perturba₆₇₆ tion theory² In contrast, we can think of the peak region as corresponding to multiple soft emissions. This simple, $\operatorname{nec}_{\overline{678}}$ essarily approximate picture provides an understanding of the bulk of the differences between the quark and gluon jetso mass distributions. Since the probability of the single large angle, energetic emission is proportional to the color charge $_{\bf \delta 82}$ the gluon distribution should be enhanced in this region by, a factor of about $C_A/C_F = 9/4$, consistent with what is ob₆₈₄ served in Figure 8. Similarly the exponent in the Sudakovess damping factor for the gluon jet mass distribution is enhanced by the same factor, leading to a peak "pushed" further from the origin. Therefore, compared to a quark jet, the gluon jet mass distribution exhibits a larger average jet mass with a larger relative contribution arising from the perturbative shoulder region and a small mass peak that is further from the origin.

Together with the fact that the number of constituents in the jet is also larger (on average) for the gluon jet simply because a gluon will radiate more than a quark, these features explain much of what we observed earlier in terms of the effectiveness of the various observables to separate quark jets from gluons jets. They also give us insight into the difference in the distributions for the observable Γ_{Oiet} . Since the shoulder is dominated by a single large angle, hard emission, it is minimally impacted by pruning, which is designed to remove the large angle, soft constituents (as shown in more detail below). Thus, jets in the shoulder exhibit small volatility and they are a larger component in the gluon jet distribution. Hence gluon jets, on average, have smaller values of Γ_{Qjet} than quark jets as in Figure 1(b). Further, this feature of gluon jets is distinct from the fact that there are more constituents, explaining why Γ_{Qjet} and n_{constits} supply largely independent information for distinguishing quark and gluon jets.

To illustrate some of these points in more detail, Figure 9 exhibits the same jet mass distributions *after pruning* [33, 58]. Removing the large angle, soft constituents moves the peak in both of the distributions from $m/p_T/R \sim 0.1-0.2$ to the region around $m/p_T/R \sim 0.05$. This explains why pruning works to reduce the QCD background when looking for a signal in a specific jet mass bin. The shoulder feature at higher mass is much more apparent after pruning, as is the larger shoulder for the gluon jets. A quantitative (all-orders) understanding of groomed mass distributions is also possible. For instance, resummation of the pruned mass distribution was achieved in [37, 59]. Figure 9 serves to confirm the physical understanding of the relative behavior of $\Gamma_{\rm Qjet}$ for quark and gluon jets.

Our final topic in this section is the residual R and p_T dependence exhibited in Figures 8 and 9, which indicates a deviation from the naive linear scaling that has been removed by using the scaled variable $m/p_T/R$. A helpful, in-

²The shoulder label will become more clear when examining groome⁶⁹³ jet mass distributions.

tuitively simple, if admittedly imprecise, model of a jet is48 to separate the constituents of the jet into "hard" (with p_T '\$49 that are of order the jet p_T) versus "soft" (with p_T 's small so and fixed compared to the jet p_T), and "large" angle (with $_{51}$ an angular separation from the jet direction of order R) versus "small" angle (with an angular separation from the jet direction smaller than and not scaling with R) components.⁷⁵² As described above the Sudakov damping factor excludes constituents that are very soft or very small angle (or both).753 In this simple picture perturbative large angle, hard con-754 stituents appear rarely, but, as described above, they charac⁷⁵⁵ terize the large mass jets that appear in the "shoulder" of the 756 jet mass distribution where the mass scales approximately 757 linearly with the jet p_T and with R. The hard, small angle 7^{58} constituents are somewhat more numerous and contribute to⁷⁵⁹ a jet mass that does not scale with R. The soft constituents⁷⁶⁰ are much more numerous (becoming more numerous with⁷⁶¹ increasing jet p_T) and contribute to a jet mass that scales⁷⁶² like $\sqrt{p_{T,jet}}$. The small angle, soft constituents contribute to⁶³ a jet mass that does not scale with R, while the large angle,764 soft constituents do contribute to a jet mass that scales like R⁶⁵ and grow in number approximately linearly in R (i.e., with 766 the area of the annulus at the outer edge of the jet). This 67 simple picture allows at least a qualitative explanation of the 688 behavior observed in Figures 8 and 9.

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As already suggested, the residual p_T dependence car⁷⁷⁰ be understood as arising primarily from the slow decrease⁷¹ of the strong coupling $\alpha_s(p_T)$ as p_T increases. This leads t_0^{72} a corresponding decrease in the (largely perturbative) shoul⁷⁷³ der regime for both distributions at higher p_T , i.e., a decreas e^{74} in the number of hard, large angle constituents. At the same⁷⁵ time, and for the same reason, the Sudakov damping is less⁷⁶ strong with increasing p_T and the peak moves in towards⁷⁷⁷ the origin. While the number of soft constituents increases⁷⁷⁸ with increasing jet p_T , their contributions to the scaled jet⁷⁹ mass distribution shift to smaller values of m/p_T (decreas-780 ing approximately like $1/\sqrt{p_T}$). Thus the overall impact of 81 increasing p_T for both distributions is a (gradual) shift td^{82} smaller values of $m/p_T/R$. This is just what is observed in ⁸³ Figures 8 and 9, although the numerical size of the effect is⁷⁸⁴ reduced in the pruned case.

The residual R dependence is somewhat more complicated. The perturbative large angle, hard constituent contri₇₈₆ bution largely scales in the variable $m/p_T/R$, which is why we see little residual R dependence in either figure at higherst masses $(m/p_T/R > 0.4)$. The contribution of the small angless constituents (hard and soft) contribute at fixed m and thus shift to the left versus the scaled variable as R increases 790 This presumably explains the small shifts in this direction at small mass observed in both figures. The large angle, soft 200 constituents contribute to mass values that scale like R, and 391 as noted above, tend to increase in number as R increases 992 (i.e., as the area of the jet grows). Such contributions yield 395

a scaled jet mass distribution that shifts to the right with increasing R and presumably explain the behavior at small p_T in Figure 8. Since pruning largely removes this contribution, we observe no such behavior in Figure 9.

5.5 Conclusions

In Section 5 we have seen that a variety of jet observables provide information about the jet that can be employed to effectively separate quark-initiated from gluon-initiated jets. Further, when used in combination, these observables can provide superior separation. Since the improvement depends on the correlation between observables, we use the multivariable performance to separate the observables into different classes, with each class containing highly correlated observables. We saw that the best performing single observable is simply the number of constituents in the jet, n_{constits} , while the largest further improvement comes from combining with $C_1^{\beta=1}$ (or $\tau_1^{\beta=1}$), but the smallest *R* and p_T dependence arises from combining with $C_1^{\beta=0}$. On the other hand, some of the commonly used observables are highly correlated and do not provide extra information and enhanced tagging when used together. In addition to demonstrating these correlations, we have provided a discussion of the physics behind the structure of the correlation. Using the jet mass as an example, we have given arguments to explicitly explain the differences between jet observables initiated by each type of parton.

Finally, we remind the reader that the numerical results were derived for a particular color configuration (qq and gg events), in a particular implementation of the parton shower and hadronization. Color connections in more complex event configurations, or different Monte Carlo programs, may well exhibit somewhat different efficiencies and rejection factors. The value of our results is that they indicate a subset of variables expected to be rich in information about the partonic origin of final-state jets. These variables can be expected to act as valuable discriminants in searches for new physics, and could also be used to define model-independent final-state measurements which would nevertheless be sensitive to the short-distance physics of quark and gluon production.

6 Boosted W-Tagging

In this section, we study the discrimination of a boosted, hadronically decaying W boson (signal) against a gluoninitiated jet background, comparing the performance of various groomed jet masses and substructure variables. A range of different distance parameters for the anti- k_T jet algorithm are explored, in a range of different leading jet p_T bins. This allows us to determine the performance of observables as a function of jet radius and jet boost, and to see where different approaches may break down. The groomed mass and

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substructure variables are then combined in a BDT as de⁸⁴⁴ scribed in Section 4, and the performance of the resulting⁴⁵ BDT discriminant explored through ROC curves to under⁸⁴⁶ stand the degree to which variables are correlated, and how⁸⁴⁷ this changes with jet boost and jet radius.

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6.1 Methodology

These studies use the *WW* samples as signal and the dije⁸⁵² gg as background, described previously in Section 2. Whils⁶⁵³ only gluonic backgrounds are explored here, the conclusions⁸⁵⁴ regarding the dependence of the performance and correla⁸⁵⁵ tions on the jet boost and radius are not expected to be sub⁸⁵⁶ stantially different for quark backgrounds; we will see tha⁸⁵⁷ the differences in the substructure properties of quark- and⁸⁵⁸ gluon-initiated jets, explored in the last section, are signifi⁸⁵⁹ cantly smaller than the differences between *W*-initiated and⁶⁶⁰ gluon-initiated jets.

As in the q/g tagging studies, the showered events were clustered with FASTJET 3.03 using the anti- k_T algorithm with jet radii of R=0.4,0.8,1.2. In both signal and back ground samples, an upper and lower cut on the leading jet p_T is applied after showering/clustering, to ensure similate by properties in leading jet p_T that are considered are 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV, for the 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV parton p_T slices respectively. The jets then have various grooming algorithms applied and substructure observables reconstructed as described in Section 3.4. The substructure observables studied in this section are:

- Ungroomed, trimmed (m_{trim}) , and pruned (m_{prun}) jet masses.
- Mass output from the modified mass drop tagger $(m_{\text{mmdt}})_{\text{a.6}}$
- Soft drop mass with $\beta = 2$ (m_{sd}).
- 2-point energy correlation function ratio $C_2^{\beta=1}$ (we also studied $\beta=2$ but do not show its results because it showed poor discrimination power).
- N-subjettiness ratio τ_2/τ_1 with $\beta=1$ ($\tau_{21}^{\beta=1}$) and with axes computed using one-pass k_t axis optimization (we also studied $\beta=2$ but did not show its results because it showed poor discrimination power).
- Pruned Qjet mass volatility, Γ_{Qjet} .

6.2 Single Variable Performance

In this section we explore the performance of the various groomed jet mass and substructure variables in separating signal from background. Since we have not attempted to op 100 timise the grooming parameter settings of each grooming 100 algorithm, we do not place much emphasis here on the rel 100 ative performance of the groomed masses, but instead con 100 centrate on how their performance changes depending on the 100 kinematic bin and jet radius considered.

Figure 10 compares the signal and background in terms of the different groomed masses explored for the anti- k_T R = 0.8 algorithm in the $p_T = 500\text{-}600$ GeV bin. One can clearly see that, in terms of separating signal and background, the groomed masses are significantly more performant than the ungroomed anti- k_T R = 0.8 mass. Using the same jet radius and p_T bin, Figure 11 compares signal and background for the different substructure variables studied.

Figures 12, 13 and 14 show the single variable ROC curves for various p_T bins and values of R. The single-variable performance is also compared to the ROC curve for a BDT combination of all the variables (labelled "allvars"). In all cases, the "allvars" option is significantly more performant than any of the individual single variables considered, indicating that there is considerable complementarity between the variables, and this is explored further in Section 6.3.

In Figures 15, 16 and 17 the same information is shown in a format that more readily allows for a quantitative comparison of performance for different R and p_T ; matrices are presented which give the background rejection for a signal efficiency of 70% for single variable cuts, as well as two- and three-variable BDT combinations. The results are shown separately for each p_T bin and jet radius considered. Most relevant for our immediate discussion, the diagonal entries of these plots show the background rejections for a single-variable BDT using the labelled observable, and can thus be examined to get a quantitative measure of the individual single variable performance, and to study how this changes with jet radius and momenta. The off-diagonal entries give the performance when two variables (shown on the x-axis and on the y-axis, respectively) are combined in a BDT. The final column of these plots shows the background rejection performance for three-variable BDT combinations of $m_{sd}^{\beta=2} + C_2^{\beta=1} + X$. These results will be discussed later in Section 6.3.3.

In general, the most performant single variables are the groomed masses. However, in certain kinematic bins and for certain jet radii, $C_2^{\beta=1}$ has a background rejection that is comparable to or better than the groomed masses.

We first examine the variation of performance with jet p_T . By comparing Figures 15(a), 16(a) and 17(b), we can see how the background rejection performance varies with increased momenta whilst keeping the jet radius fixed to R = 0.8. Similarly, by comparing Figures 15(b), 16(b) and 17(c) we can see how performance evolves with p_T for R = 1.2. For both R = 0.8 and R = 1.2 the background rejection power of the groomed masses increases with increasing p_T , with a factor 1.5-2.5 increase in rejection in going from the 300-400 GeV to 1.0-1.1 TeV bins. In Figure 18 we show the $m_{\rm sd}$ and $m_{\rm prun}$ groomed masses for signal and background in the $p_T = 300$ -400 and $p_T = 1.0$ -1.1 TeV bins for R = 1.2 jets. Two effects result in the improved performance of the groomed mass at high p_T . Firstly, as is evident from the

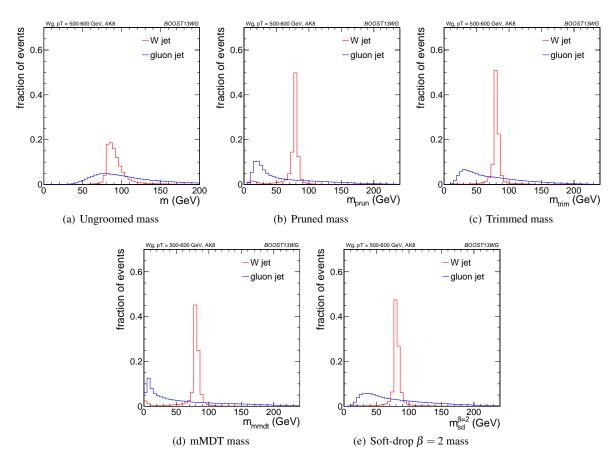


Fig. 10 Leading jet mass distributions in the gg background and WW signal samples in the $p_T = 500\text{-}600$ GeV bin using the anti- k_T R = 0.8 algorithm.

figure, the resolution of the signal peak after grooming im₉₁₀ proves, because the groomer finds it easier to pick out th₆₂₀ hard signal component of the jet against the softer compo₉₂₁ nents of the underlying event when the signal is boosted₉₂₂ Secondly, it follows from Figure 9 and the discussion in Sec₉₂₃ tion 5.4 that, for increasing p_T , the perturbative shoulder of₅₂₄ the gluon distribution decreases in size, and thus there is a_{25} slight decrease (or at least no increase) of the background₂₆ contamination in the signal mass region (m/ p_T /R \sim 0.5).

However, one can see from the Figures 15(b), 16(b) and 17(c) that the $C_2^{\beta=1}$, $\Gamma_{\rm Ojet}$ and $\tau_{21}^{\beta=1}$ substructure variables behave somewhat differently. The background rejection power of the $\Gamma_{\rm Ojet}$ and $\tau_{21}^{\beta=1}$ variables both decrease with increasing ρ_T , by up to a factor two in going from the 300-400 GeV to 1.0-1.1 TeV bins. Conversely the rejection power of $C_2^{\beta=1}$ and dramatically increases with increasing ρ_T for ρ_T for the larger jet radius ρ_T for larger jet radius ρ_T for the larger jet radius ρ_T for ρ_T in Figure 19 we show the ρ_T for the larger jet radius ρ_T for ρ_T in Figure 19 we show the ρ_T for the larger jet radius ρ_T for ρ_T for ρ_T does not improve with ρ_T for the larger jet radius ρ_T for ρ_T for ρ_T for ρ_T does not improve with ρ_T for the larger jet radius ρ_T for ρ_T for ρ_T does not improve with ρ_T for the larger jet radius ρ_T for ρ_T for ρ_T for ρ_T does not improve with ρ_T for the larger jet radius ρ_T for ρ_T for

to smaller $au_{21}^{\beta=1}$ values, reducing the discriminating power of the variable. This is expected, since jet substructure methods explicitly relying on the identification of hard prongs would expect to work best at low p_T , where the prongs would tend to be more separated. However, $C_2^{\beta=1}$ does not rely on the explicit identification of subjets, and one can see from Figure 19 that the discrimination power visibly increases with increasing p_T . This is in line with the observation in [44] that $C_2^{\beta=1}$ performs best when m/p_T is small.

We now compare the performance of different jet radius parameters in the same p_T bin by comparing the individual sub-figures of Figures 15, 16 and 17. To within $\sim 25\%$, the background rejection power of the groomed masses remains constant with respect to the jet radius. Figure 20 shows how the groomed mass changes for varying jet radius in the p_T = 1.0-1.1 TeV bin. One can see that the signal mass peak remains unaffected by the increased radius, as expected, since grooming removes the soft contamination which could otherwise increase the mass of the jet as the radius increased. The gluon background in the signal mass region also remains largely unaffected, as follows from Figure 9 and the discussion in Section 5.4, where it is shown that there is very



Fig. 11 Leading jet substructure variable distributions in the gg background and WW signal samples in the $p_T = 500$ -600 GeV bin using the anti- k_T R = 0.8 algorithm.



Fig. 12 ROC curves for single variables considered for W tagging in the $p_T = 300\text{-}400$ GeV bin using the anti- k_T R = 0.8 algorithm and R = 1.2 algorithm, along with a BDT combination of all variables ("allvars").



Fig. 13 ROC curves for single variables considered for W tagging in the $p_T = 500\text{-}600$ GeV bin using the anti- k_T R = 0.8 algorithm and R = 1.2 algorithm, along with a BDT combination of all variables ("allvars")



Fig. 14 ROC curves for single variables considered for W tagging in the $p_T = 1.0$ -1.1 TeV bin using the anti- $k_T R = 0.4$ algorithm, anti- $k_T R = 0.8$ algorithm and R = 1.2 algorithm, along with a BDT combination of all variables ("allvars")

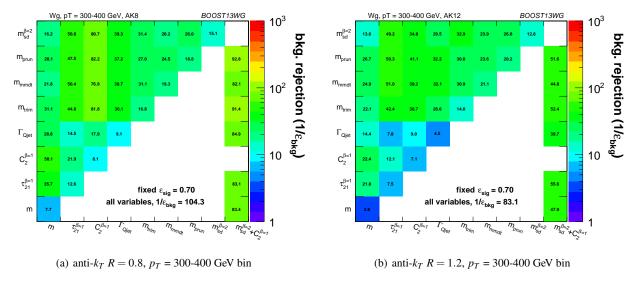


Fig. 15 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the $p_T = 300\text{-}400$ GeV bin using the anti- k_T R = 0.8 algorithm and R = 1.2 algorithm. Also shown is the background rejection for three-variable combinations involving $m_{sd}^{\beta=2} + C_2^{\beta=1}$, and for a BDT combination of all of the variables considered.

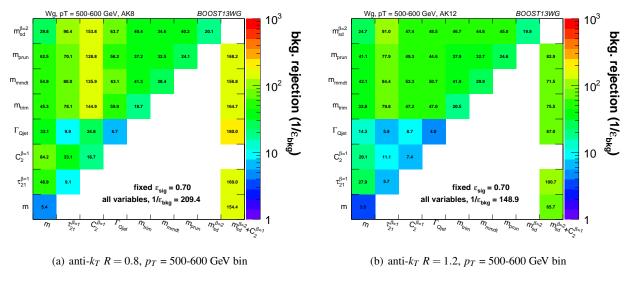


Fig. 16 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the $p_T = 500\text{-}600$ GeV bin using the anti- k_T R = 0.8 algorithm and R = 1.2 algorithm. Also shown is the background rejection for three-variable combinations involving $m_{sd}^{\beta=2} + C_2^{\beta=1}$, and for a BDT combination of all of the variables considered.

little dependence of the groomed gluon mass distribution on $_{52}$ R in the signal region $(m/p_T/R \sim 0.5)$.

However, we again see rather different behaviour versus R for the substructure variables. In all p_T bins considered, the most performant substructure variable, $C_2^{\beta=1}$, performs best for an anti- k_T distance parameter of R=0.8. The performance of this variable is dramatically worse for the larger jet radius of R=1.2 (a factor seven worse background rejection in the $p_T=1.0$ -1.1 TeV bin), and substantially worse for R=0.4. For the other jet substructure variables considered, Γ_{Ojet} and $\tau_{21}^{\beta=1}$, their background rejection power also

reduces for larger jet radius, but not to the same extent. Figure 21 shows the $\tau_{21}^{\beta=1}$ and $C_2^{\beta=1}$ distributions for signal and background in the $p_T=1.0$ -1.1 TeV bin for R=0.8 and R=1.2 jet radii. For the larger jet radius, the $C_2^{\beta=1}$ distribution of both signal and background get wider, and consequently the discrimination power decreases. For $\tau_{21}^{\beta=1}$ there is comparatively little change in the distributions with increasing jet radius. The increased sensitivity of C_2 to soft wide angle radiation in comparison to τ_{21} is a known feature of this variable [44], and a useful feature in discriminating coloured versus colour singlet jets. However, at very large

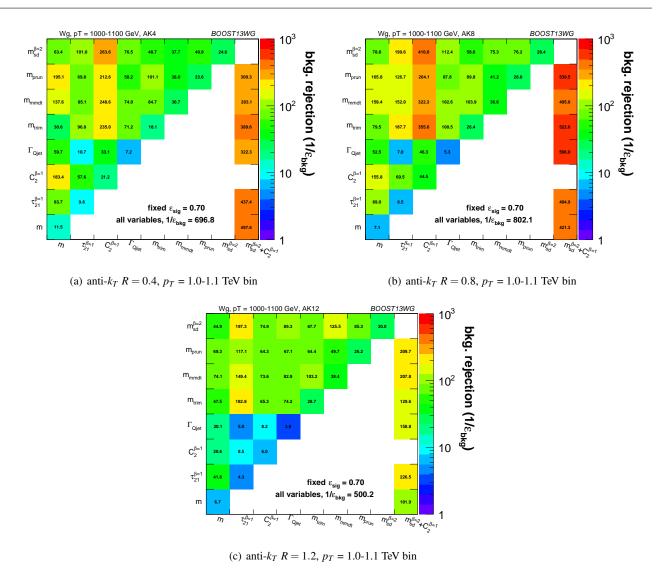


Fig. 17 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the p_T = 1.0-1.1 TeV bin using the anti- k_T R = 0.4, R = 0.8 and R = 1.2 algorithm. Also shown is the background rejection for three-variable combinations involving $m_{sd}^{\beta=2} + C_2^{\beta=1}$, and for a BDT combination of all of the variables considered.

jet radii ($R \sim 1.2$), this feature becomes disadvantageous₉₇₆ the jet can pick up a significant amount of initial state ob77 other uncorrelated radiation, and C_2 is more sensitive to this₇₈ than is τ_{21} . This uncorrelated radiation has no (or very little)₇₉ dependence on whether the jet is W- or gluon-initiated, and so sensitivity to this radiation means that the discrimination₉₁ power will decrease.

6.3 Combined Performance

Studying the improvement in performance (or lack thereof)⁹⁸⁶ when combining single variables into a multivariate analy⁹⁸⁷ sis gives insight into the correlations among jet observables.⁹⁸⁸ The off-diagonal entries in Figures 15, 16 and 17 can be used⁹⁸⁹ to compare the performance of different BDT two-variable⁹⁹⁰

combinations, and see how this varies as a function of p_T and R. By comparing the background rejection achieved for the two-variable combinations to the background rejection of the "all variables" BDT, one can also understand how discrimination can be improved by adding further variables to the two-variable BDTs.

In general the most powerful two-variable combinations involve a groomed mass and a non-mass substructure variable ($C_2^{\beta=1}$, $\Gamma_{\rm Qjet}$ or $\tau_{21}^{\beta=1}$). Two-variable combinations of the substructure variables are not as powerful in comparison. Which particular mass + substructure variable combination is the most powerful depends strongly on the p_T and R of the jet, as discussed in the sections to follow.

There is also modest improvement in the background rejection when different groomed masses are combined, in-

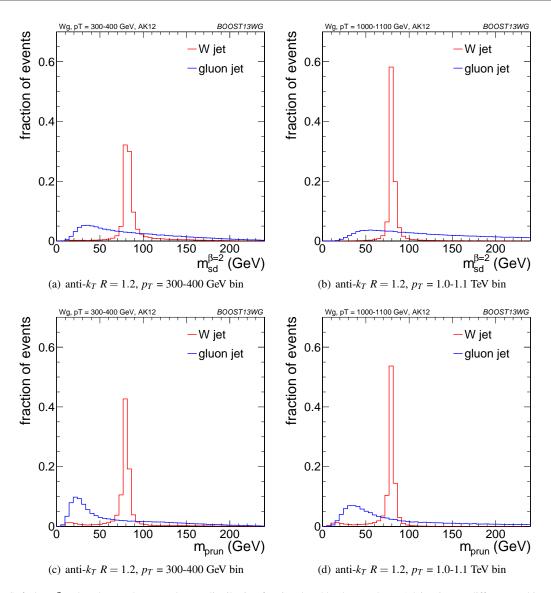


Fig. 18 The Soft-drop $\beta = 2$ and pruned groomed mass distribution for signal and background R = 1.2 jets in two different p_T bins.

dicating that there is complementary information betweenos the different groomed masses. In addition, there is an improvement in the background rejection when the groomedoo masses are combined with the ungroomed mass, indicatingor that grooming removes some useful discriminatory informacos tion from the jet. These observations are explored further into the section below.

Generally, the R=0.8 jets offer the best two-variable combined performance in all p_T bins explored here. This is despite the fact that in the highest $p_T=1.0$ -1.1 TeV bin the average separation of the quarks from the W decay is much smaller than 0.8, and well within 0.4. This conclusion could of course be susceptible to pile-up, which is not considered in this study.

6.3.1 Mass + Substructure Performance

As already noted, the largest background rejection at 70% signal efficiency are in general achieved using those two-variable BDT combinations which involve a groomed mass and a non-mass substructure variable. We now investigate the p_T and R dependence of the performance of these combinations.

For both R = 0.8 and R = 1.2 jets, the rejection power of these two-variable combinations increases substantially with increasing p_T , at least within the p_T range considered here.

For a jet radius of R = 0.8, across the full p_T range considered, the groomed mass + substructure variable combinations with the largest background rejection are those which involve $C_2^{\beta=1}$. For example, in combination with $m_{\rm sd}$, this

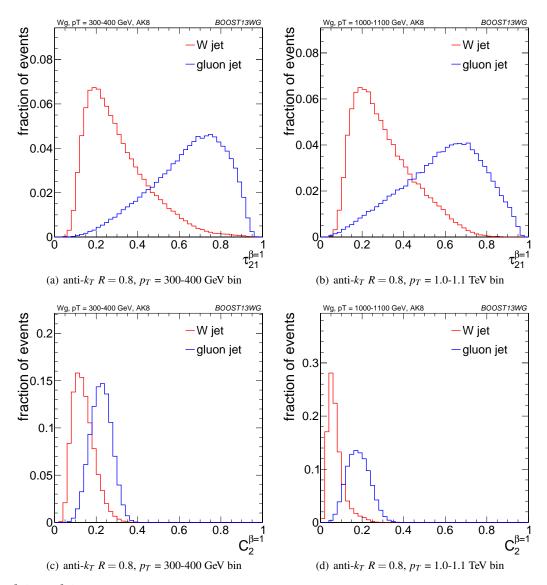


Fig. 19 The $\tau_{21}^{\beta=1}$ and $C_2^{\beta=1}$ distributions for signal and background R=0.8 jets in two different p_T bins.

produces a five-, eight- and fifteen-fold increase in backeds ground rejection compared to using the groomed mass alongous In Figure 22, the low degree of correlation between $m_{\rm sd}$ versub $T_2^{\beta=1}$ that leads to these large improvements in background rejection can be seen. What little correlation exists is ratheoson non-linear in nature, changing from a negative to a positive correlation as a function of the groomed mass, something which helps to improve the background rejection in the region of the W mass peak.

 However, when we switch to a jet radius of R=1.2 the picture for $C_2^{\beta=1}$ combinations changes dramatically. These become significantly less powerful, and the most powerful variable in groomed mass combinations becomes $\tau_{21}^{\beta=1}$ for all jet p_T considered. Figure 23 shows the correlation between $m_{sd}^{\beta=2}$ and $C_2^{\beta=1}$ in the $p_T=1.0$ - 1.2 TeV bin for the

various jet radii considered. Figure 24 is the equivalent set of distributions for $m_{sd}^{\beta=2}$ and $\tau_{21}^{\beta=1}$. One can see from Figure 23 that, due to the sensitivity of the observable to to soft, wideangle radiation, as the jet radius increases $C_2^{\beta=1}$ increases and becomes more and more smeared out for both signal and background, leading to worse discrimination power. This does not happen to the same extent for $\tau_{21}^{\beta=1}$. We can see from Figure 24 that the negative correlation between $m_{sd}^{\beta=2}$ and $\tau_{21}^{\beta=1}$ that is clearly visible for R=0.4 decreases for larger jet radius, such that the groomed mass and substructure variable are far less correlated and $\tau_{21}^{\beta=1}$ offers improved discrimination within a $m_{sd}^{\beta=2}$ mass window.

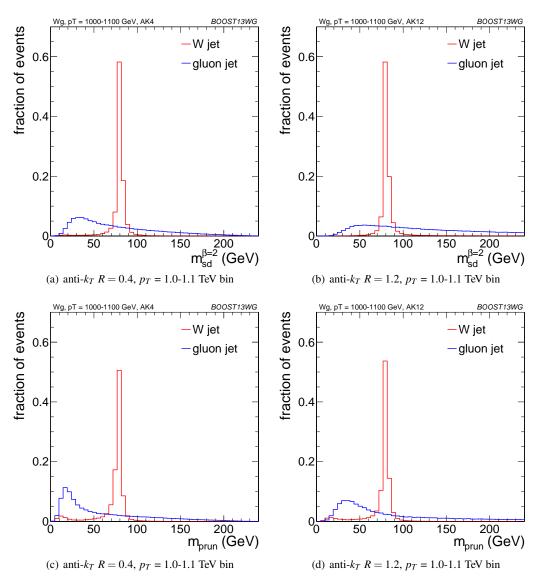


Fig. 20 The Soft-drop $\beta = 2$ and pruned groomed mass distribution for signal and background R = 0.4 and R = 1.2 jets in the $p_T = 1.0$ -1.1 TeV bin.

6.3.2 Mass + Mass Performance

The different groomed masses and the ungroomed mass are 1064 of course not fully correlated, and thus one can always see some kind of improvement in the background rejection when two different mass variables are combined in the BDT. However, in some cases the improvement can be dramatic, particularly at higher p_T , and particularly for combinations with the ungroomed mass. For example, in Figure 17 we can see that in the p_T =1.0-1.1 TeV bin, the combination of pruned mass with ungroomed mass produces a greater than eightold improvement in the background rejection for R = 0.4 jets, a greater than five-fold improvement for R = 0.8 jets and a factor ~ 2 improvement for R = 1.2 jets. A similar tors behaviour can be seen for mMDT mass. In Figures 25, 26

and 27, we show the 2-D correlation plots of the pruned mass versus the ungroomed mass separately for the WW signal and gg background samples in the p_T = 1.0-1.1 TeV bin, for the various jet radii considered. For comparison, the correlation of the trimmed mass with the ungroomed mass, a combination that does not improve on the single mass as dramatically, is shown. In all cases one can see that there is a much smaller degree of correlation between the pruned mass and the ungroomed mass in the backgrounds sample than for the trimmed mass and the ungroomed mass. This is most obvious in Figure 25, where the high degree of correlation between the trimmed and ungroomed mass is expected, since with the parameters used (in particular R_{trim} = 0.2) we cannot expect trimming to have a significant impact on an R = 0.4 jet. The reduced correlation with ungroomed mass

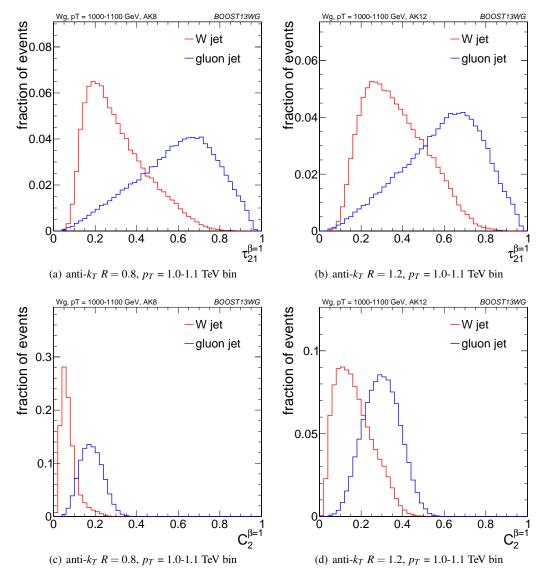


Fig. 21 The $\tau_{21}^{\beta=1}$ and $C_2^{\beta=1}$ distributions for signal and background R=0.8 and R=1.2 jets in the $p_T=1.0$ -1.1 TeV bin.

for pruning in the background means that, once we have required that the pruned mass is consistent with a W (i.e. ~ 80 GeV), a relatively large difference between signal and background in the ungroomed mass still remains, and can be exploited to improve the background rejection further In other words, many of the background events which pass the pruned mass requirement do so because they are shifted to lower mass (to be within a signal mass window) by the grooming, but these events still have the property that the groom ing. A requirement on the groomed mass alone does not considered in this study, could limit the degree to which the ungroomed mass could be used to improve discrimination in this way.

6.3.3 "All Variables" Performance

Figures 15, 16 and 17 report the background rejection achieved by a combination of all the variables considered into a single BDT discriminant. In all cases, the rejection power of this "all variables" BDT is significantly larger than the best two-variable combination. This indicates that, beyond the best two-variable combination, there is still significant complementary information available in the remaining observables to improve the discrimination of signal and background. How much complementary information is available appears to be p_T dependent. In the lower $p_T = 300\text{-}400$ and 500-600 GeV bins, the background rejection of the "all variables" combination is a factor ~ 1.5 greater than the best two-variable combination, but in the highest p_T bin it is a factor ~ 2.5 greater.



Fig. 22 2-D histograms of $m_{sd}^{\beta=2}$ versus $C_2^{\beta=1}$ distributions for R=0.8 jets in the various p_T bins considered, shown separately for signal and background.



Fig. 23 2-D histograms of $m_{sd}^{\beta=2}$ versus $C_2^{\beta=1}$ for R=0.4,0.8 and 1.2 jets in the $p_T=1.0$ -1.1 TeV bin, shown separately for signal and background.



Fig. 24 2-D histograms of $m_{sd}^{\beta=2}$ versus $\tau_{21}^{\beta=1}$ for R=0.4,0.8 and 1.2 jets in the $p_T=1.0$ -1.1 TeV bin, shown separately for signal and background.

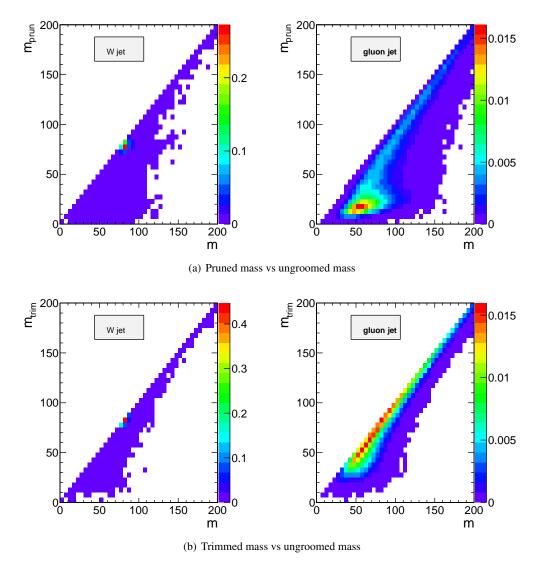


Fig. 25 2-D histograms of groomed mass versus ungroomed mass in the $p_T = 1.0$ -1.1 TeV bin using the anti- $k_T R = 0.4$ algorithm, shown separately for signal and background.

The final column in Figures 15, 16 and 17 allows us ta_{22} further explore the all variables performance relative to tha_{23} pair-wise performance. It shows the background rejection ta_{24} for three-variable BDT combinations of $ta_{24}^{\beta=2} + ta_{25}^{\beta=1} + ta_{25}^{\beta=1}$ where $ta_{25}^{\beta=1} + ta_{25}^{\beta=1}$ where $ta_{25}^{\beta=1} + ta_{25}^{\beta=1}$ is (at least close $ta_{27}^{\beta=1} + ta_{25}^{\beta=1}$ is (at least close $ta_{27}^{\beta=1} + ta_{25}^{\beta=1}$ is superseded by $ta_{21}^{\beta=1} + ta_{25}^{\beta=1}$ in performance, as discussed earlier. Thus, in considering the three-variable combination results $ta_{25}^{\beta=1} + ta_{25}^{\beta=1} + ta_{25}^{\beta=1}$ is simplest to focus on the $ta_{25}^{\beta=1} + ta_{25}^{\beta=1} + ta_{25}^{\beta=1}$ we see that, for the lower $ta_{25}^{\beta=1} + ta_{25}^{\beta=1} + ta_$

the performance considerably, we are still $\sim 40\%$ from the observed "all variables" background rejection, and clearly adding a fourth or maybe even fifth variable would bring considerable gains. In terms of which variable offers the best improvement when added to the $m_{\rm sd}^{\beta=2}+C_2^{\beta=1}$ combination, it is hard to see an obvious pattern; the best third variable changes depending on the p_T and R considered.

It appears that there is a rich and complex structure in terms of the degree to which the discriminatory information provided by the set of variables considered overlaps, with the degree of overlap apparently decreasing at higher p_T . This suggests that in all p_T ranges, but especially at higher p_T , there are substantial performance gains to be made by designing a more complex multivariate W tagger.

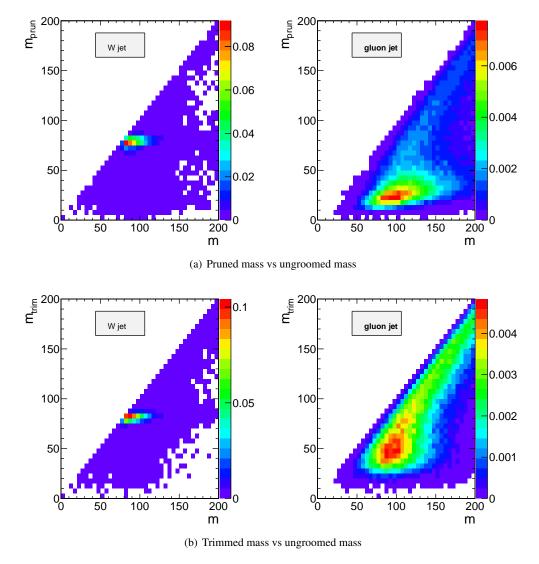


Fig. 26 2-D histograms of groomed mass versus ungroomed mass in the $p_T = 1.0$ -1.1 TeV bin using the anti- $k_T R = 0.8$ algorithm, shown separately for signal and background.

6.4 Conclusions

We have studied the performance, in terms of the separatioh of a hadronically decaying W boson from a gluon-initiated jet background, of a number of groomed jet masses, subjustification to the above. We have used this to gain insight into how the discriminatory in formation contained in the variables overlaps, and how the complementarity between the variables changes with jet $p_{\frac{1159}{1150}}$ and anti- k_T distance parameter R.

In terms of the performance of individual variables, wtil find that, in agreement with other studies [40], the groomettom masses generally perform best, with a background rejectiottom power that increases with larger p_T , but which is more contistent with respect to changes in R. We have explained that dependence of the groomed mass performance on p_T and p_T

R using the understanding of the QCD mass distribution developed in Section 5.4. Conversely, the performance of other substructure variables, such as $C_2^{\beta=1}$ and $\tau_{21}^{\beta=1}$, is more susceptible to changes in radius, with background rejection power decreasing with increasing R. This is due to the inherent sensitivity of these observables to soft, wide angle radiation.

The best two-variable performance is obtained by combining a groomed mass with a substructure variable. Which particular substructure variable works best in combination strongly depends on $p_{\rm T}$ and R. $C_2^{\beta=1}$ offers significant complementarity to groomed mass at smaller R, owing to the small degree of correlation between the variables. However, the sensitivity of $C_2^{\beta=1}$ to soft, wide-angle radiation leads to worse discrimination power at large R, where $\tau_{21}^{\beta=1}$ performs better in combination. Our studies also demonstrate the po-

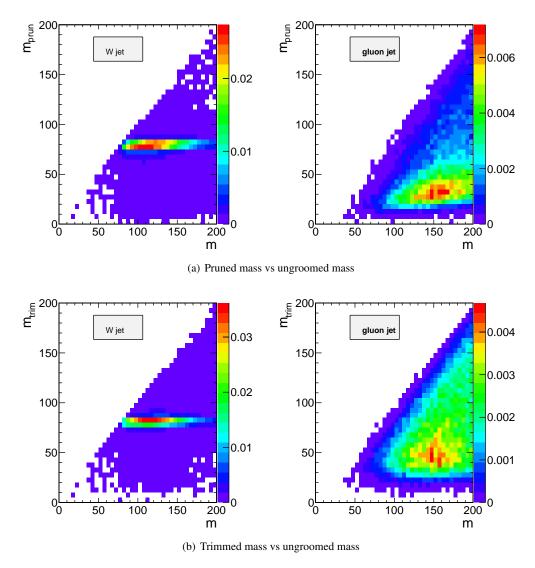


Fig. 27 2-D histograms of groomed mass versus ungroomed mass in the $p_T = 1.0$ -1.1 TeV bin using the anti- $k_T R = 1.2$ algorithm, shown separately for signal and background.

tential for enhancing discrimination by combining groomed₈₁ and ungroomed mass information, although the use of un₁₈₂ groomed mass in this may be limited in practice by the pres₁₈₃ ence of pile-up that is not considered in these studies.

By examining the performance of a BDT combinations of all variables considered, it is clear that there are poten-186 tially substantial performance gains to be made by designing a more complex multivariate W tagger, especially at higheriss p_T .

7 Top Tagging

In this section, we investigate the identification of boosted top quarks using jet substructure. Boosted top quarks result in large-radius jets with complex substructure, containing a *b*-subjet and a boosted *W*. The additional kinematic handles

coming from the reconstruction of the W mass and b-tagging allow a very high degree of discrimination of top quark jets from QCD backgrounds relative to W tagging. As a consequence of the many kinematic differences between top and QCD jets, top taggers are typically complex, with a couple of input parameters necessary for any given algorithm. We study the variation in performance of top tagging techniques with respect to jet p_T and R, re-optimizing the tagger inputs for each kinematic range and jet radius considered. We also investigate the effects of combining dedicated top tagging algorithms with other jet substructure observables, giving insight into the correlations among top-tagging observables.

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7.1 Methodology

We use the top quark MC samples for each bin described in Section 2.2. The analysis relies on FASTJET 3.0.3 for jet clustering and calculation of jet substructure observables Jets are clustered using the anti- k_T algorithm, and only the leading jet is used in each analysis. To ensure similar $p_T^{\frac{1248}{1248}}$ spectra in each bin an upper and lower p_T cut are applied 49 to each sample after jet clustering. The bins in leading jet50 p_T for top tagging are 600-700 GeV, 1-1.1 TeV, and 1.5251 1.6 TeV. Jets are clustered with radii R = 0.4, 0.8, and 1.2; R = 0.4 jets are only studied in the 1.5-1.6 TeV bin because the top decay products are all contained within an $R = 0.4^{252}$ jet for top quarks with this boost.

We study a number of top-tagging strategies, which can be divided into two distinct categories. In the first category are dedicated top-tagging algorithms, which aim to directly reconstruct the top and W candidates in the top decay. In particular, we study: 1258

- 1. HEPTopTagger
- 2. Johns Hopkins Tagger (JH)
- Trimming with W-identification
- 4. Pruning with W-identification

as described in Section 3.3. The top mass, m_t , is the mass of the groomed jet. All of the above taggers and groomers incorporate a step to remove contributions from the underlying event and other soft radiation.

In the second category are individual jet substructure observables that are sensitive to the radiation pattern within the jet, which we refer to as "jet-shape observables". While the most sensitive top-tagging observables are typically sensitive to three-pronged radiation, we also consider observables sensitive to two-pronged radiation in the limit where the W_{1273} is very boosted and its subjets overlap. The observables we consider are:

- The ungroomed jet mass.

 N-subjettiness ratios $\tau_{21}^{\beta=1}$ and $\tau_{32}^{\beta=1}$, using the "winner takes-all" axes definition.
- takes-all" axes definition.

 2-point energy correlation function ratios $C_2^{\beta=1}$ and $C_3^{\beta=\frac{1}{2}79}$
- The pruned Qjet mass volatility, Γ_{Ojet} .

Several of these observables were also considered earlier fores2 q/g-tagging and W-tagging.

To study the correlation among the above top-taggings4 observables, we consider combinations of the mass-reconstruction at fixed methods with the shape observables. For multivariate analy 286 ses, we combine the relevant tagger output observables and/\(\alpha\) is jet shapes into a BDT, as described in Section 4. Addition288 ally, because each tagger has two input parameters, we scares over reasonable values of the input parameters to determine. the optimal value that gives the largest background rejection for each top tagging signal efficiency. This allows a directed

comparison of the optimized version of each tagger. The input parameter values scanned for the various algorithms are:

- **HEPTopTagger:** m ∈ [30, 100] GeV, μ ∈ [0.5, 1]
- JH Tagger: $\delta_p \in [0.02, 0.15], \delta_R \in [0.07, 0.2]$
- **Trimming:** $f_{\text{cut}} \in [0.02, 0.14], R_{\text{trim}} \in [0.1, 0.5]$
- **Pruning:** $z_{\text{cut}} \in [0.02, 0.14], R_{\text{cut}} \in [0.1, 0.6]$

We also investigate the degradation in performance of the top-tagging observables when moving away from the optimal parameter choice.

7.2 Single-Observable Performance

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We begin by investigating the behaviour of individual jet substructure observables. Because of the rich, three-pronged structure of the top decay, it is expected that combinations of masses and jet shapes will far outperform single observables in identifying boosted tops. However, a study of the toptagging performance of single variables facilitates a direct comparison with the W tagging results in Section 6, and also allows a straightforward examination of the performance of each observable for different p_T and jet radius.

Top-tagging observable performance is quantified using ROC curves. Figure 28 shows the ROC curves for each of the top-tagging observables, with the bare (ungroomed) jet mass also plotted for comparison. The jet-shape observables all perform substantially worse than jet mass; this is in contrast with W tagging, for which several observables are competitive with or perform better than jet mass (see, for example, Figures 16(a), 17(a) and 17(b)). To understand why this is the case, consider N-subjettiness: the W is two-pronged and the top is three-pronged, and so we expect τ_{21} and τ_{32} to be the best-performant N-subjettiness ratio, respectively. However, a cut for small values of τ_{21} necessarily also selects for events with large τ_1 , which is strongly correlated with jet mass, up to Sudakov-suppressed contributions. There fore, τ_{21} combines both mass and shape information to some extent. By contrast, and as is clear in Figure 28(a), the best shape for top tagging is τ_{32} , which contains no information on the jet mass. It is therefore unsurprising that the shapes most useful for top tagging are less sensitive to the jet mass, and under-perform relative to the corresponding observables for W tagging.

Of the two top-tagging algorithms, it is apparent from Figure 28 that the Johns Hopkins tagger out-performs the signal efficiency for both the top and W candidate masses; this is expected, as the HEPTopTagger was designed to reconstruct moderate- p_T top jets in ttH events (for a proposed high- p_T variant of the HEPTopTagger, see [60]). In Figure 29, we show the histograms for the top mass output from the JH and HEPTopTagger for different R in the $p_T = 1.5$ -1.6 TeV bin, and in Figure 30 for different p_T at R = 0.8,

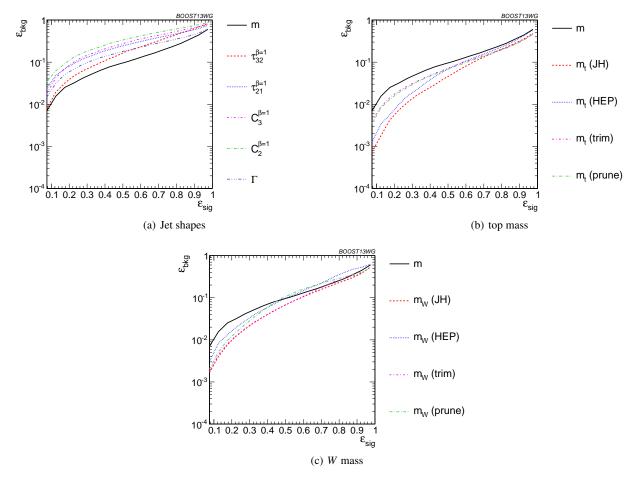


Fig. 28 Comparison of single-variable top-tagging performance in the $p_T = 1 - 1.1$ GeV bin using the anti- k_T , R=0.8 algorithm.

optimized at a signal efficiency of 30%. A particular feature of the HepTopTagger algorithm is that, after the jet is files tered to select the five hardest subjets, the three subjets are thosen which most closely reconstruct the top mass. This requirement tends to shape a peak in the QCD background around m_t for the HEPTopTagger, as can be seen from Fig. ures 29(d) and 30(d); this is the likely reason for the betten performance of the JH tagger, which has no such require ment. It has been suggested [61] that performance in the HEPTopTagger may be improved by selecting the three subset jets reconstructing the top only among those that pass the W_{225} mass constraints, which somewhat reduces the shaping of the background. The discrepancy between the JH and HEP $_{1327}$ TopTaggers is more pronounced at higher p_T and larger jets radius (see Figures 32 and 35).

We also see in Figure 28(b) that the top mass from the JH tagger and the HEPTopTagger has superior performance relative to either of the grooming algorithms; this is because the pruning and trimming algorithms do not have inherent W-identification steps and are not optimized for this put by pose. Indeed, because of the lack of a W-identification steps grooming algorithms are forced to strike a balance between 36

under-grooming the jet, which broadens the signal peak due to underlying event contamination and features a larger background rate, and over-grooming the jet, which occasionally throws out the b-jet and preserves only the W components inside the jet. We demonstrate this effect in Figures 29 and 30, showing that with 30% signal efficiency, the optimal performance of the tagger over-grooms a substantial fraction of the jets ($\sim 20-30\%$), leading to a spurious second peak at m_W . This effect is more pronounced at large R and p_T , since more aggressive grooming is required in these limits to combat the increased contamination from UE and QCD radiation.

In Figures 31 and 32 we directly compare ROC curves for jet-shape observable performance and top-mass performance, respectively, in three different p_T bins whilst keeping the jet radius fixed at R=0.8. The input parameters of the taggers, groomers and shape variables are separately optimized in each p_T bin. One can see from Figure 31 that the tagging performance of jet shapes do not change substantially with p_T . The observables $\tau_{32}^{\beta=1}$ and $\Gamma_{\rm Qjet}$ have the most variation and tend to degrade with higher p_T , as can be seen in Figure 33. This was also observed in the W-tagging

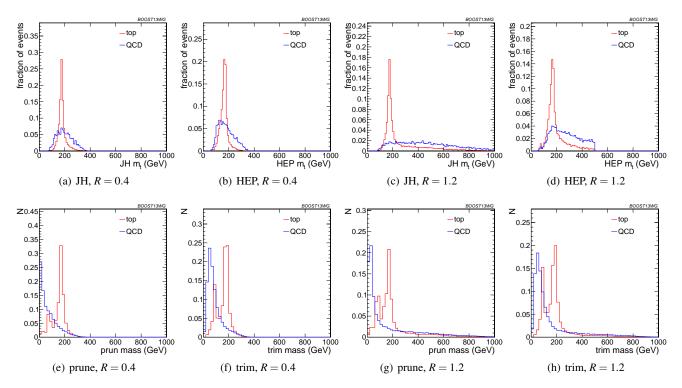


Fig. 29 Comparison of top mass reconstruction with the Johns Hopkins (JH), HEPTopTaggers (HEP), pruning, and trimming at different R using the anti- k_T algorithm in the $p_T = 1.5$ -1.6 TeV bin. Each histogram is shown for the working point optimized for best performance with m_t in the 0.3-0.35 signal efficiency bin, and is normalized to the fraction of events passing the tagger. In this and subsequent plots, the HEPTopTagger distribution cuts off at 500 GeV because the tagger fails to tag jets with a larger mass.

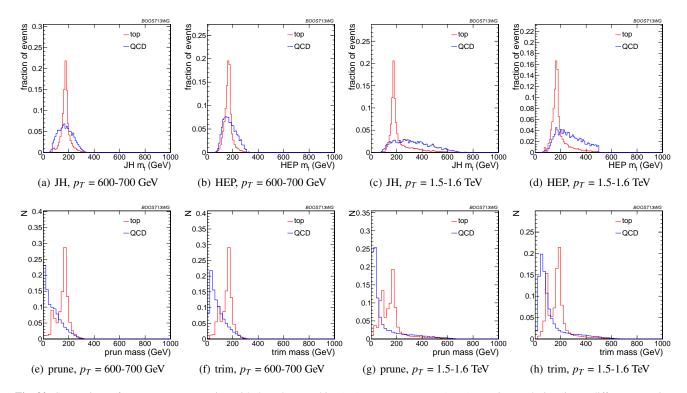


Fig. 30 Comparison of top mass reconstruction with the Johns Hopkins (JH), HEPTopTaggers (HEP), pruning, and trimming at different p_T using the anti- k_T algorithm, R = 0.8. Each histogram is shown for the working point optimized for best performance with m_t in the 0.3-0.35 signal efficiency bin, and is normalized to the fraction of events passing the tagger.

studies in Section 6, and makes sense, as higher- p_T QCD₃₆ jets have more, harder emissions within the jet, giving risc₃₇ to substructure that fakes the signal. By contrast, from Fig₃₈₈ ure 32 we can see that most of the top-mass observables have₃₈₉ superior performance at higher p_T , due to the radiation from₃₀₀ the top quark becoming more collimated. The notable ex₃₉₁ ception is the HEPTopTagger, which degrades at higher p_T ₁₃₉₂ likely in part due to the background-shaping effects studied₃₉₃ above.

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In Figures 34 and 35 we directly compare ROC curves 95 for jet-shape observable performance and top-mass performance mance, respectively, for three different jet radii within the 97 $p_T = 1.5-1.6$ TeV bin. Again, the input parameters of the tag³⁹⁸ gers, groomers and shape variables are separately optimizethous for each jet radius. We can see from these figures that most on of the top-tagging variables, both shape and reconstructed or top mass, perform best for smaller radius, as was generally 02 observed in the case of W-tagging in Section 6. This is likely 403 because, at such high p_T , most of the radiation from the to p_T quark is confined within R=0.4, and having a larger jetos radius makes the observable more susceptible to contamina406 tion from the underlying event and other uncorrelated radia₂₀₇ QCD background distributions for each shape variable con₂₀₉ sidered in the $p_T = 1.5 - 1.6$ TeV bin for the various jet radii₄₁₀ The distributions for both signal and background broaden 11 with increasing R, degrading the discriminating power. Fq. 12 $C_2^{\beta=1}$ and $C_3^{\beta=1}$, the background distributions are shifted upa13 ward as well. Therefore, the discriminating power generate ally gets worse with increasing R. The main exception is 15 for $C_3^{\beta=1}$, which performs optimally at R=0.8; in this case 416 the signal and background coincidentally happen to have the same distribution around R = 0.4, and so R = 0.8 gives beta18 ter discrimination.

7.3 Performance of Multivariable Combinations

We now consider various BDT combinations of the single variables considered in the last section, using the technique section described in Section 4. In particular, we consider the pereservation formance of individual taggers such as the JH tagger and HEPTopTagger, which output information about the top and we candidate masses and the helicity angle; groomers, such as trimming and pruning, which remove soft, uncorrelated at radiation from the top candidate to improve mass reconast struction, and to which we have added a W reconstruction step; and the combination of the outputs of the above tagas gers/groomers, both with each other, and with the shape varias ables. For all observables with tuneable input parameters space we scan and optimize over realistic values of such parameters, as described in Section 7.1.

In Figure 37, we directly compare the performance of the HEPTopTagger, the JH tagger, trimming, and pruning, in the $p_T = 1 - 1.1$ TeV bin with R = 0.8, where both m_t and m_W are used in the groomers. Generally, we find that pruning, which does not naturally incorporate subjets into the algorithm, does not perform as well as the others. Interestingly, trimming, which does include a subjet-identification step, performs comparably to the HEPTopTagger over much of the range, possibly due to the background-shaping observed in Section 7.2. By contrast, the JH tagger outperforms the other algorithms. To determine whether there is complementary information in the mass outputs from different top taggers, we also consider in Figure 37 a multivariable combination of all of the JH and HEPTopTagger outputs. The maximum efficiency of the combined JH and HEPTopTaggers is limited, as some fraction of signal events inevitably fails either one or other of the taggers. We do see a 20-50% improvement in performance when combining all outputs, which suggests that the different algorithms used to identify the top and W for different taggers contains complementary information.

In Figure 38 we present the results for multivariable combinations of the top tagger outputs with and without shape variables. We see that, for both the HEPTopTagger and the JH tagger, the shape observables contain additional information uncorrelated with the masses and helicity angle, and give on average a factor 2-3 improvement in signal discrimination. We see that, when combined with the tagger outputs, both the energy correlation functions $C_2 + C_3$ and the Nsubjettiness ratios $\tau_{21} + \tau_{32}$ give comparable performance, while Γ_{Qjet} is slightly worse; this is unsurprising, as Qjets accesses shape information in a more indirect way from other shape observables. Combining all shape observables with a single top tagger provides even greater enhancement in discrimination power. We directly compare the performance of the JH and HEPTopTaggers in Figure 38(c). Combining the taggers with shape information nearly erases the difference between the tagging methods observed in Figure 37; this indicates that combining the shape information with the HEPTopTagger identifies the differences between signal and background missed by the tagger alone. This also suggests that further improvement to discriminating power may be minimal, as various multivariable combinations converge to within a factor of 20% or so.

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In Figure 39 we present the results for multivariable combinations of groomer outputs with and without shape variables. As with the tagging algorithms, combinations of groomers with shape observables improves their discriminating power; combinations with $\tau_{32} + \tau_{21}$ perform comparably to those with $C_3 + C_2$, and both of these are superior to combinations with the mass volatility, $\Gamma_{\rm Qjet}$. Substantial further improvement is possible by combining the groomers with all shape observables. Not surprisingly, the taggers that lag behind

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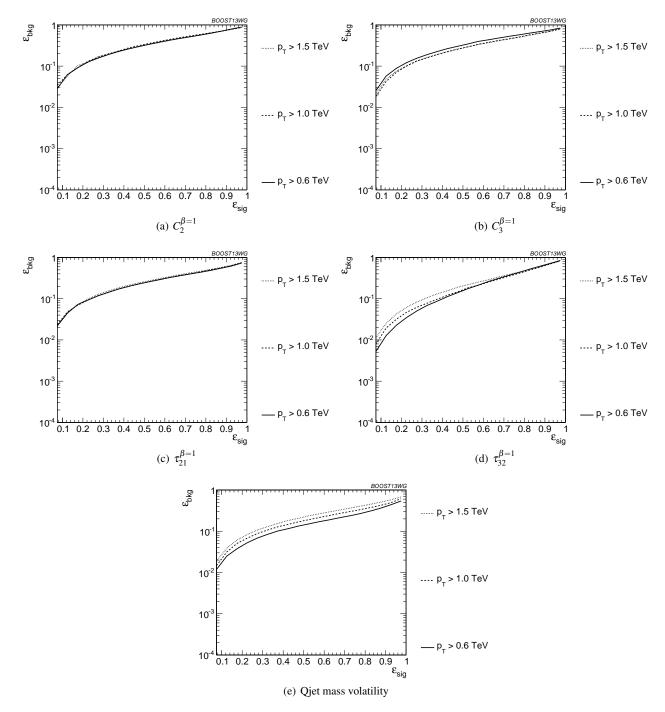


Fig. 31 Comparison of individual jet shape performance at different p_T using the anti- $k_T R = 0.8$ algorithm.

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in performance enjoy the largest gain in signal-background discrimination with the addition of shape observables. Oncada again, in Figure 39(c), we find that the differences between pruning and trimming are erased when combined with shapaso information.

Finally, in Figure 40, we compare the performance of each of the tagger/groomers when their outputs are com453 bined with all of the shape observables considered. One caths4

see that the discrepancies between the performance of the different taggers/groomers all but vanishes, suggesting perhaps that we are here utilising all available signal-background discrmination information, and that this is the optimal top tagging performance that could be achieved in these conditions.

Up to this point, we have considered only the combined multivariable performance in the $p_T = 1.0\text{-}1.1$ TeV bin with

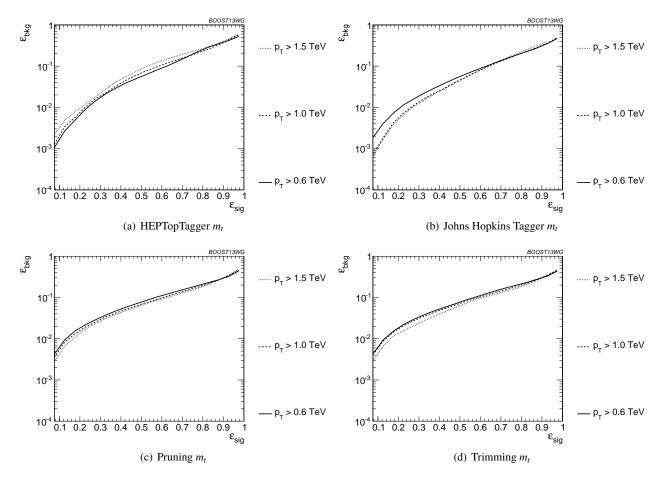


Fig. 32 Comparison of top mass performance of different taggers at different p_T using the anti- k_T R=0.8 algorithm.

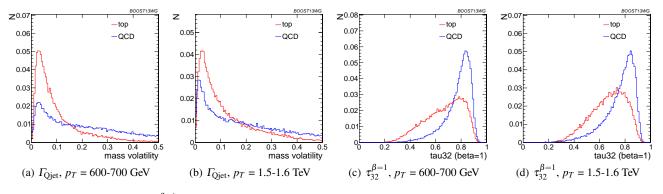


Fig. 33 Comparison of Γ_{Qjet} and $\tau_{32}^{\beta=1}$ at R=0.8 and different values of the p_T . These shape observables are the most sensitive to varying p_T .

jet radius R=0.8. We now compare the BDT combinations of tagger outputs, with and without shape variables, at different p_T . The taggers are optimized over all input paramates eters for each choice of p_T and signal efficiency. As without the single-variable study, we consider anti- k_T jets clustered with R=0.8 and compare the outcomes in the $p_T=500$ and $p_T=1.5-1.6$ TeV bins. The comparison of the taggers/groomers is shown in Figure 4 $p_T=1.5$ the behaviour with p_T is qualitatively similar to the be-in-

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haviour of the m_t observable for each tagger/groomer shown in Figure 32; this suggests that the p_T behaviour of the taggers is dominated by the top-mass reconstruction. As before, the HEPTopTagger performance degrades slightly with increased p_T due to the background shaping effect, while the JH tagger and groomers modestly improve in performance.

In Figure 42, we show the p_T -dependence of BDT combinations of the JH tagger output combined with shape observables. We find that the curves look nearly identical: the

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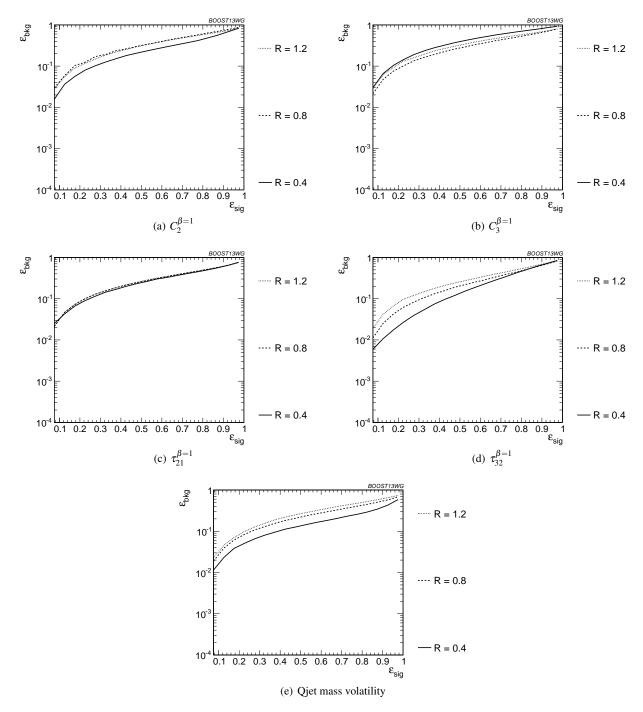


Fig. 34 Comparison of individual jet shape performance at different R in the $p_T = 1.5$ -1.6 TeV bin.

 p_T dependence is again dominated by the top-mass recon₃₈₁ struction, and combining the tagger outputs with different₈₂ shape observables does not substantially change this behav₃₂₈₃ ior. The same holds true for trimming and pruning. By con₃₈₄ trast, HEPTopTagger ROC curves, shown in Figure 43, d Ω_{85} change somewhat when combined with different shape ob₃₈₆ servables; due to the suboptimal performance of the HEP-TopTagger at high p_T , we find that combining the HEPTop⁴⁸⁷

Tagger with $C_3^{\beta=1}$, which in Figure 31(b) is seen to have some modest improvement at high p_T , can improve its performance. Combining the HEPTopTagger with multiple shape observables gives the maximum improvement in performance at high p_T relative to at low p_T .

In Figure 44 we compare the BDT combinations of tagger outputs, with and without shape variables, at different

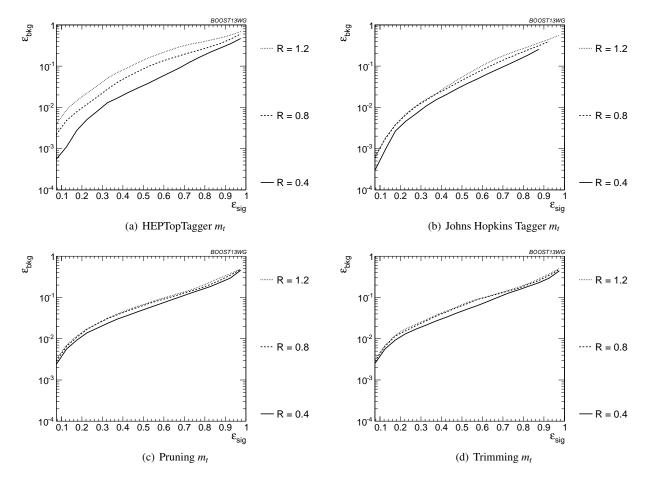


Fig. 35 Comparison of top mass performance of different taggers at different R in the $p_T = 1.5 \cdot 1.6$ TeV bin.

jet radius R in the $p_T = 1.5$ -1.6 TeV bin. The taggers are opsoot timized over all input parameters for each choice of R and signal efficiency. We find that, for all taggers and groomerssin the performance is always best at small R; the choice of R_{12} is sufficiently large to admit the full top quark decay at such high p_T , but is small enough to suppress contamination from additional radiation. This is not altered when the taggers are combined with shape observables. For example, in Figure $4\tilde{s}_{16}$ is shown the dependence on R of the JH tagger when comsin bined with shape observables, where one can see that the R-dependence is identical for all combinations. The same holds true for the HEPTopTagger, trimming, and pruning.

7.4 Performance at Sub-Optimal Working Points

Up until now, we have re-optimized our tagger and groomegab parameters for each p_T , R, and signal efficiency workingspoint. In reality, experiments will choose a finite set of workspoint points to use. When this is taken into account, how wilker the top-tagging performance compare to the optimal resultspan already shown? To address this concern, we replicate ourspan analyses, but optimize the top taggers only for a single p_{3530}

bin, single jet radius *R*, or single signal efficiency, and subsequently apply the same parameters to other scenarios. This allows us to determine the extent to which re-optimization is necessary to maintain the high signal-to-background discrimination power seen in the top-tagging algorithms we studied. In this section, we focus on the taggers and groomers and their combination with shape observables, as the shape observables alone typically do not have any input parameters to optimize.

Optimizing at a single p_T : We show in Figure 46 the performance of the reconstructed top mass for the $p_T = 0.6$ -0.7 TeV and $p_T = 1.0$ -1.1 TeV bins, with all input parameters optimized to the $p_T = 1.5$ -1.6 TeV bin (and R = 0.8 throughout). This is normalized to the performance using the optimized tagger inputs at each p_T . The performance degrades by about 50% when the high- p_T optimized inputs are used at other momenta, with trimming and the Johns Hopkins tagger degrading the most. The jagged behaviour of the points is due to the finite resolution of the scan. We also observe a particular effect associated with using suboptimal taggers: since taggers sometimes fail to return a top candidate, parameters optimized for a particular signal efficiency

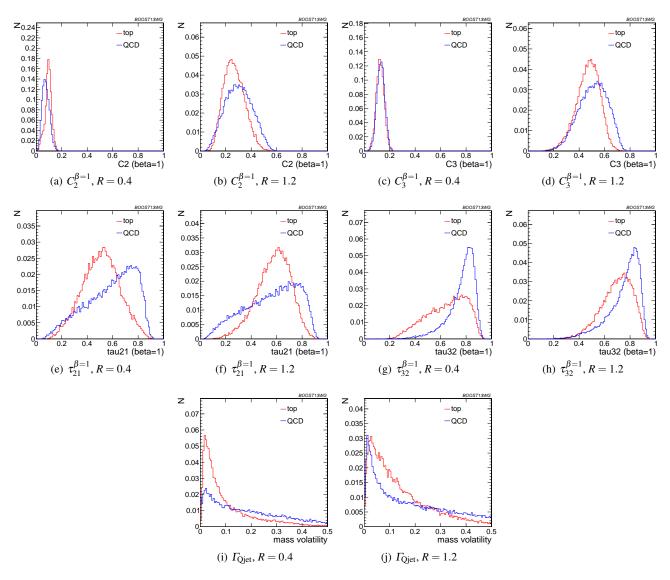


Fig. 36 Comparison of various shape observables in the $p_T = 1.5 - 1.6$ TeV bin and different values of the anti- k_T radius R.

 $\varepsilon_{\rm sig}$ at $p_T=1.5$ -1.6 TeV may not return enough signal cansa6 didates to reach the same efficiency at a different p_T . Consa7 sequently, no point appears for that p_T value. This is not often a practical concern, as the largest gains in signal discrimination and significance are for smaller values of $\varepsilon_{\rm sig}_{150}$ but it may be an important effect to consider when selecting benchmark tagger parameters and signal efficiencies.

The degradation in performance is more pronounced folists the BDT combinations of the full tagger outputs, shown in Figure 47. This is true particularly at very low signal efficiency, where the optimization of inputs picks out a cut of the tail of some distribution that depends precisely on the p_T/R of the jet. Once again, trimming and the Johns Hop-skins tagger degrade more markedly. Similar behavior holds for the BDT combinations of tagger outputs plus all shapes

observables.

Optimizing at a single R: In Figure 48, we show the performance of the reconstructed top mass for R = 0.4 and 0.8, with all input parameters optimized to R = 1.2 TeV bin (and $p_T = 1.5$ -1.6 TeV throughout). This is normalized to the performance using the optimized tagger inputs at each R. While the performance of each observable degrades at small $\varepsilon_{\rm sig}$ compared to the optimized search, the HEPTopTagger fares the worst as the observed is quite sensitive to the selected value of R. It is not surprising that a tagger whose top mass reconstruction is susceptible to background-shaping at large R and p_T would require a more careful optimization of parameters to obtain the best performance.

The same holds true for the BDT combinations of the full tagger outputs, shown in Figure 49. The performance for

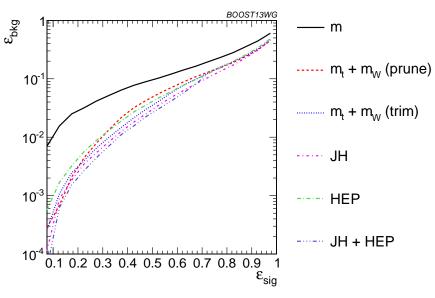


Fig. 37 The performance of the various taggers in the $p_T = 1 - 1.1$ TeV bin using the anti- k_T R=0.8 algorithm. For the groomers a BDT combination of the reconstructed m_t and m_W are used. Also shown is a multivariable combination of all of the JH and HEPTopTagger outputs. The ungroomed mass performance is shown for comparison.

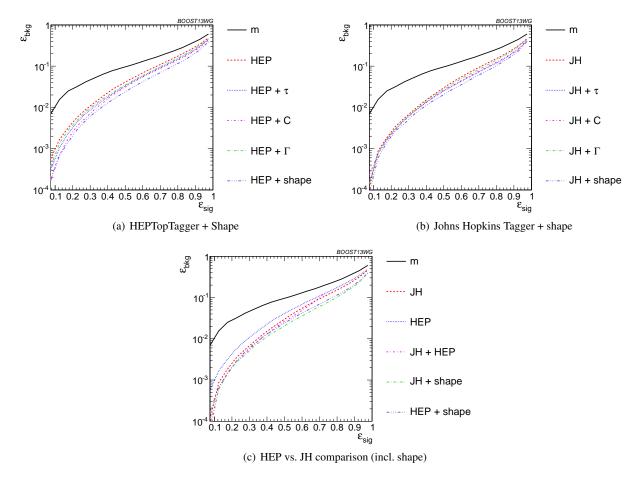


Fig. 38 The performance of BDT combinations of the JH and HepTopTagger outputs with various shape observables in the $p_T = 1 - 1.1$ TeV bin using the anti- k_T R = 0.8 algorithm. Taggers are combined with the following shape observables: $\tau_{21}^{\beta=1} + \tau_{32}^{\beta=1}$, $C_2^{\beta=1} + C_3^{\beta=1}$, Γ_{Qjet} , and all of the above (denoted "shape").

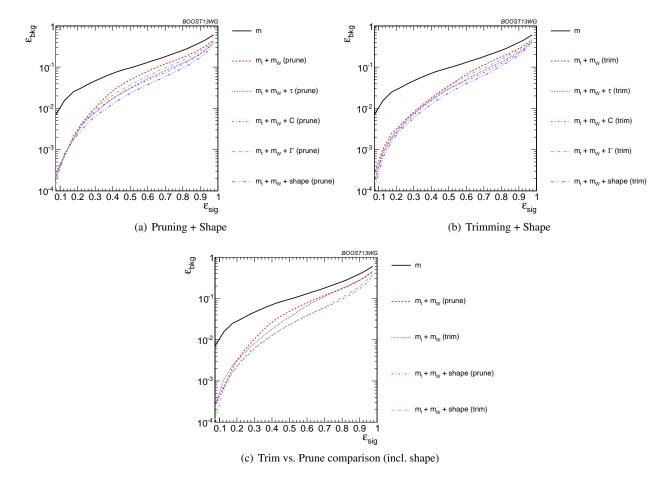


Fig. 39 The performance of the BDT combinations of the trimming and pruning outputs with various shape observables in the $p_T = 1 - 1.1$ TeV bin using the anti- k_T R = 0.8 algorithm. Groomer mass outputs are combined with the following shape observables: $\tau_{21}^{\beta=1} + \tau_{32}^{\beta=1}$, $C_2^{\beta=1} + C_3^{\beta=1}$, Γ_{Qjet} , and all of the above (denoted "shape").

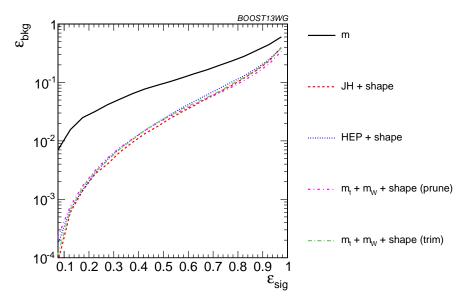


Fig. 40 Comparison of the performance of the BDT combinations of all the groomer/tagger outputs with all the available shape observables in the $p_T = 1 - 1.1$ TeV bin using the anti- k_T R=0.8 algorithm. Tagger/groomer outputs are combined with all of the following shape observables: $\tau_{21}^{\beta=1} + \tau_{32}^{\beta=1}$, $C_2^{\beta=1} + C_3^{\beta=1}$, T_{Qjet} .

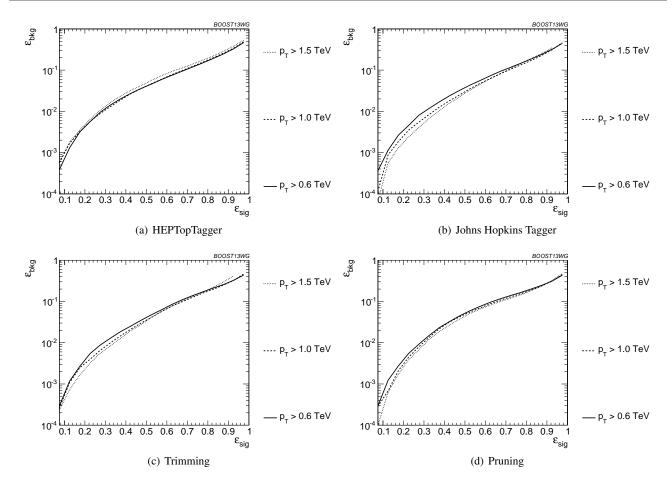


Fig. 41 Comparison of BDT combination of tagger performance at different p_T using the anti- k_T R = 0.8 algorithm.

the sub-optimal taggers is still within an O(1) factor of the optimized performance, and the HEPTopTagger performs better with the combination of all of its outputs relative to the performance with just m_t . The same behaviour holds for the BDT combinations of tagger outputs and shape observates ables.

Optimizing at a single efficiency: The strongest assumption we have made so far is that the taggers can be re-optimized for each signal efficiency point. This is useful for making a direct comparison of the power of different top-tagging algorithms, but is not particularly practical for LHC analyses. We now consider the scenario in which the tagger inputs are optimized once, in the $\varepsilon_{\text{sig}} = 0.3\text{-}0.35$ bin, and then used for all signal efficiencies. We do this in the $p_T = 1.0\text{-}1.1$ TeV bin and with R = 0.8.

The performance of each tagger, normalized to its person formance optimized in each signal efficiency bin, is shown in Figure 50 for cuts on the top mass and W mass, and in Figure 51 for BDT combinations of tagger outputs and shaped variables. In both plots, it is apparent that optimizing theo taggers in the $\varepsilon_{\rm sig}=0.3$ -0.35 efficiency bin gives comparated

ble performance over efficiencies ranging from 0.2-0.5, although performance degrades at substantially different signal efficiencies. Pruning appears to give especially robust signal-background discrimination without re-optimization, most likely due to the fact that there are no absolute distance or p_T scales that appear in the algorithm. Figures 50 and 51 suggest that, while optimization at all signal efficiencies is a useful tool for comparing different algorithms, it is not crucial to achieve good top-tagging performance in experiments.

7.5 Conclusions

We have studied the performance of various jet substructure observables, groomed masses, and top taggers to study the performance of top tagging with different p_T and jet radius parameters. At each p_T , R, and signal efficiency working point, we optimize the parameters for those observables with tuneable inputs. Overall, we have found that these techniques, individually and in combination, continue to perform well at high p_T , at least at the particle-level, which is important for future LHC running. In general, the John Hop-

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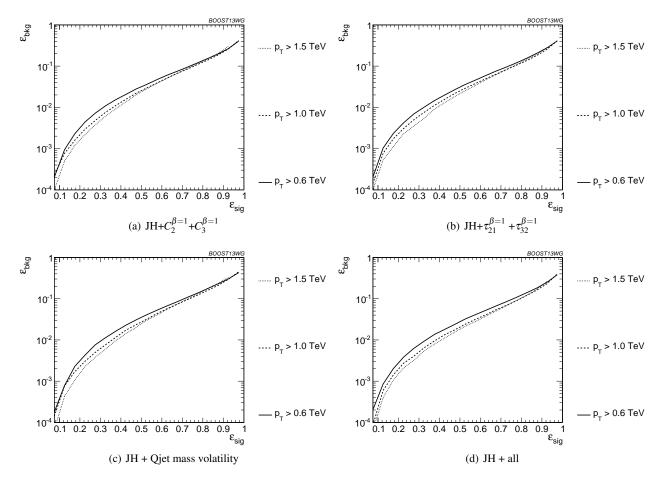


Fig. 42 Comparison of BDT combination of JH tagger + shape at different p_T using the anti- k_T R = 0.8 algorithm.

kins tagger performs best, while jet grooming algorithms26 under-perform relative to the best top taggers due to the lacker of an optimized W-identification step. Tagger performance 228 can be improved by a further factor of 2-4 through combises nation with jet substructure observables such as τ_{32} , C_3 , and ϵ_{30} Γ_{Qjet} . When combined with jet substructure observables, the 31 performance of various groomers and taggers becomes ver13632 comparable, suggesting that, taken together, the observables33 studied are sensitive to nearly all of the physical differences 34 between top and QCD jets at particle-level. A small improvement is also found by combining the Johns Hopkin 1835 and HEPTopTaggers, indicating that different taggers are notes fully correlated. The degree to which these findings continue³⁷ to hold under more realistic pile-up and detector configurates tions is, however, not addressed in this analysis and left the total times and left the same and left future study.

Comparing results at different p_T and R, top-tagging period2 formance is generally better at smaller R due to less contamod3 ination from uncorrelated radiation. Similarly, most observiod4 ables perform better at larger p_T due to the higher degree of collimation of radiation. Some observables fare worse46 at higher p_T , such as the N-subjettiness ratio τ_{32} and the τ_{32} and the τ_{32} and the τ_{32} and the τ_{32} and τ_{33} and τ_{34} and τ_{34}

Qjet mass volatility $\Gamma_{\rm Qjet}$, as higher- p_T QCD jets have more and harder emissions that fake the top-jet substructure. The HEPTopTagger is also worse at high p_T due to the tendency of the tagger to shape backgrounds around the top mass. This is unsurprising, given that the HepTopTagger was specifically designed for a lower p_T range than that considered here. The p_T - and R-dependence of the multivariable combinations is dominated by the p_T - and R-dependence of the top mass reconstruction component of the tagger/groomer.

Finally, we consider the performance of various observable combinations under the more realistic assumption that the input parameters are only optimized at a single p_T , R, or signal efficiency, and then the same inputs are used at other working points. Remarkably, the performance of all observables is typically within a factor of 2 of the fully optimized inputs, suggesting that while optimization can lead to substantial gains in performance, the general behavior found in the fully optimized analyses extends to more general applications of each variable. In particular, the performance of pruning typically varies the least when comparing suboptimal working points to the fully optimized tagger due to the scale-invariant nature of the pruning algorithm.

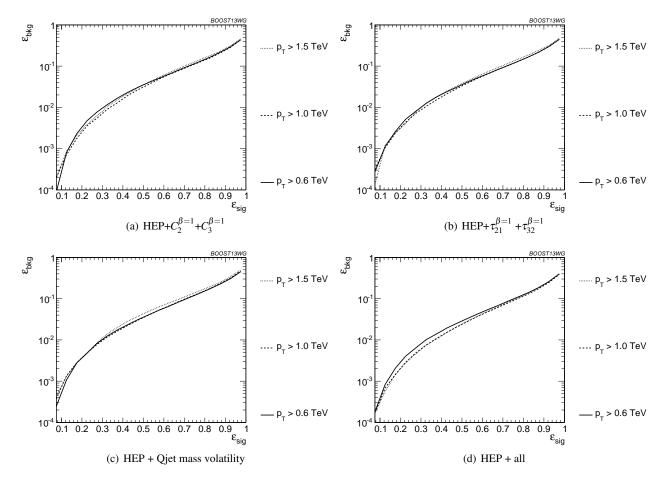


Fig. 43 Comparison of BDT combination of HEP tagger + shape at different p_T using the anti- k_T R = 0.8 algorithm.

8 Summary & Conclusions

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Furthering our understanding of jet substructure is crucidf⁷¹ to enhancing the prospects for the discovery of new physl⁶⁷² cal processes at Run II of the LHC. In this report we have⁶⁷³ studied the performance of jet substructure techniques ovelf⁷⁴ a wide range of kinematic regimes that will be encounterelf⁷⁵ in Run II of the LHC. The performance of observables and f⁷⁶ their correlations have been studied by combining the varlier ables into Boosted Decision Tree (BDT) discriminants, and f⁷⁸ comparing the background rejection power of this discrimler nant to the rejection power achieved by the individual varlies ables. The performance of "all variables" BDT discrimler nants has also been investigated, to understand the potential of the "ultimate" tagger where "all" available particle-level f⁸³ information (at least, all of that provided by the variables considered) is used.

We focused on the discrimination of quark jets from gluon jets, and the discrimination of boosted W bosons and top quarks from the QCD backgrounds. For each, we have identified the best-performing jet substructure observables, both individually and in combination with other observables. In

doing so, we have also provided a physical picture of why certain sets of observables are (un)correlated. Additionally, we have investigated how the performance of jet substructure observables varies with R and p_T , identifying observables that are particularly robust against or susceptible to these changes. In the case of q/g tagging, it seems that the ideal performance can be nearly achieved by combining the most powerful discriminant, the number of constituents of a jet, with just one other variable, $C_1^{\beta=1}$ (or $\tau_1^{\beta=1}$). Many of the other variables considered are highly correlated and provide little additional discrimination. For both top and W tagging, the groomed mass is a very important discriminating variable, but one that can be substantially improved in combination with other variables. There is clearly a rich and complex relationship between the variables considered for W and top tagging, and the performance and correlations between these variables can change considerably with changing jet p_T and R. In the case of W tagging, even after combining groomed mass with two other substructure observables, we are still some way short of the ultimate tagger performance, indicating the complexity of the information available, and the complementarity between the observables considered. In the

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Fig. 44 Comparison of tagger and jet shape performance at different radius at $p_T = 1.5-1.6$ TeV.

case of top tagging, we have shown that the performance αf_{13} both the John Hopkins and HEPTopTagger can be improved when their outputs are combined with substructure observations ables such as τ_{32} and C_3 , and that the performance of a distriction ground mass information plus subtructure observables is very comparable to the performance of the taggers. We have optimized the top taggers for partiqual reformance at other working points. We have found that the performance of observables remains within a factor αf_{22} two of the optimized value, suggesting that the performance of jet substructure observables is not significantly degraded when tagger parameters are only optimized for a few select benchmark points.

Our analyses were performed with ideal detector and pile-up conditions in order to most clearly elucidate the un₇₂₅ derlying physical scaling with p_T and R. At higher boosts₇₂₆ detector resolution effects will become more important, and₂₇ with the higher pile-up expected at Run II of the LHC, pile₇₂₈ up mitigation will be crucial for future jet substructure stud₇₂₉ ies. Future studies will be needed to determine which of the₃₀ observables we have studied are most robust against pile-up₃₁

and detector effects, and our analyses suggest particularly useful combinations of observables to consider in such studies.

At the new energy frontier of Run II of the LHC, boosted jet substructure techniques will be more central to our searches for new physics than ever before. By achieving a deeper understanding of the underlying structure of quark, gluon, W and top-initiated jets, as well as the relations between observables sensitive to their respective structures, it is hoped that more sophisticated taggers can be commissioned that will maximally extend the reach for new physics.

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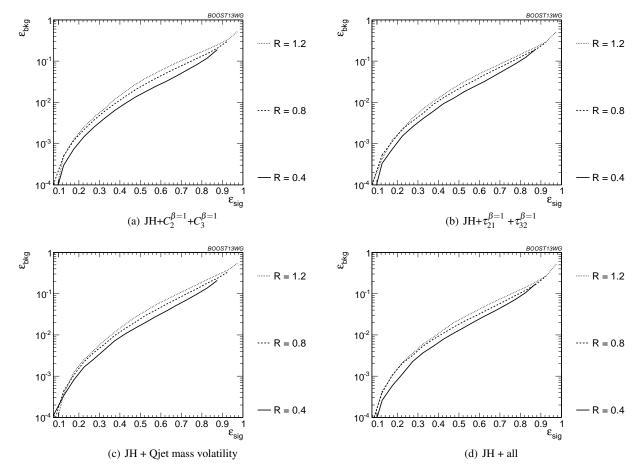


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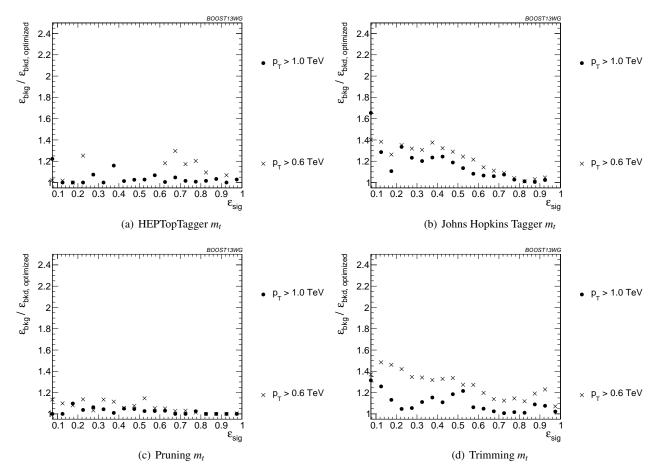


Fig. 46 Comparison of top mass performance of different taggers at different p_T using the anti- k_T R = 0.8 algorithm; the tagger inputs are set to the optimum value for $p_T = 1.5 - 1.6$ TeV.

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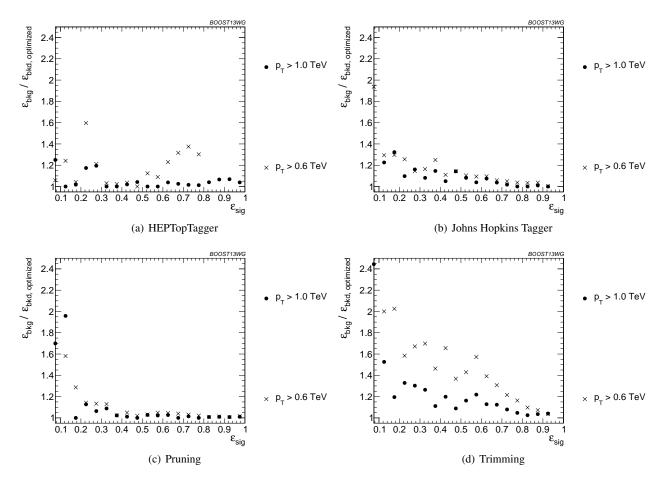


Fig. 47 Comparison of BDT combination of tagger performance at different p_T using the anti- k_T R = 0.8 algorithm; the tagger inputs are set to the optimum value for $p_T = 1.5 - 1.6$ TeV.

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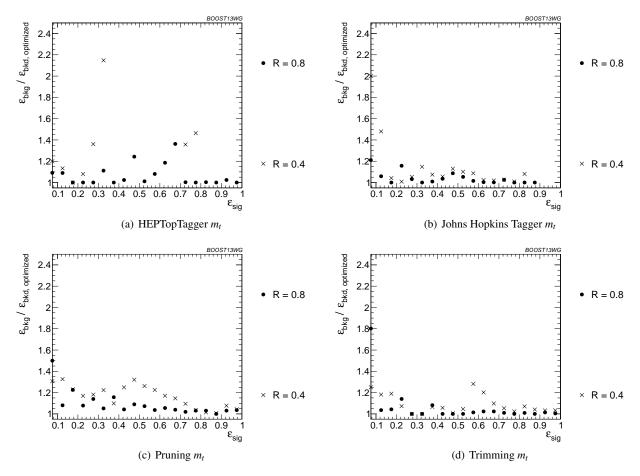


Fig. 48 Comparison of top mass performance of different taggers at different R in the $p_T = 1.5$ -1.6 TeV bin; the tagger inputs are set to the optimum value for R = 1.2.

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Fig. 49 Comparison of BDT combination of tagger performance at different radius at $p_T = 1.5$ -1.6 TeV; the tagger inputs are set to the optimum value for R = 1.2.

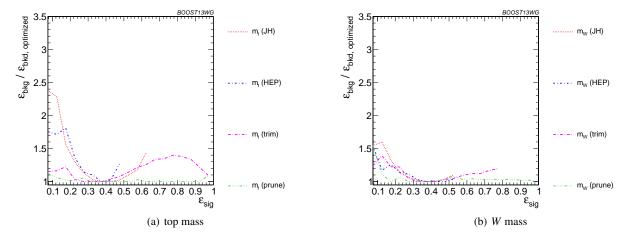


Fig. 50 Comparison of single-variable top-tagging performance in the $p_T = 1 - 1.1$ GeV bin using the anti- k_T , R = 0.8 algorithm; the inputs for each tagger are optimized for the $\varepsilon_{\text{sig}} = 0.3 - 0.35$ bin.

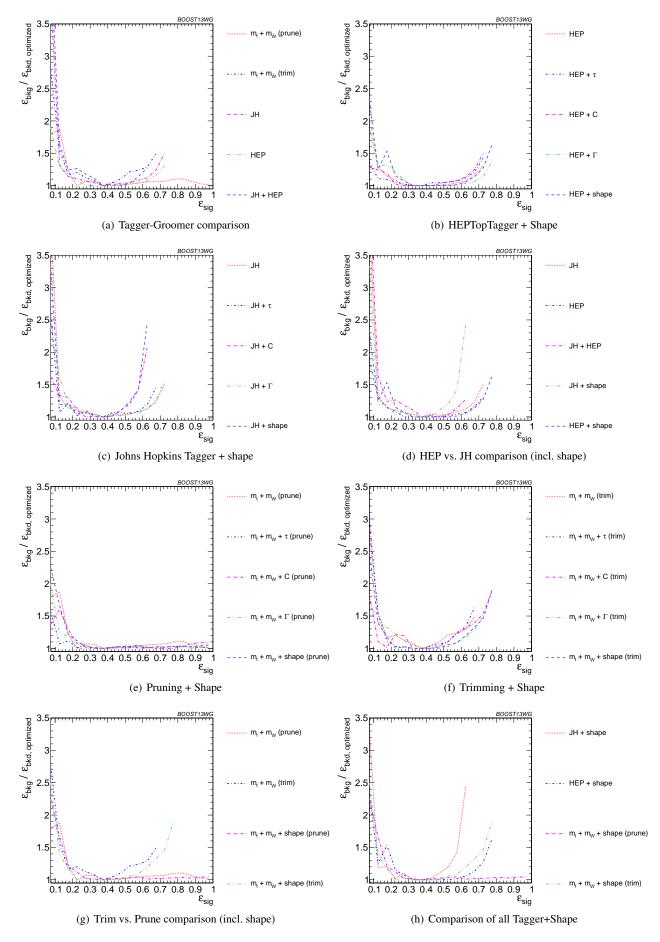


Fig. 51 The BDT combinations in the $p_T=1-1.1$ TeV bin using the anti- k_T R=0.8 algorithm. Taggers are combined with the following shape observables: $\tau_{21}^{\beta=1}+\tau_{32}^{\beta=1}$, $C_2^{\beta=1}+C_3^{\beta=1}$, $\Gamma_{\rm Qjet}$, and all of the above (denoted "shape"). The inputs for each tagger are optimized for the $\varepsilon_{\rm sig}=0.3-0.35$ bin.

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