Towards an Understanding of the Correlations in Jet Substructure

Report of BOOST2013, hosted by the University of Arizona, 12th-16th of August 2013.

```
D. Adams<sup>1</sup>, A. Arce<sup>2</sup>, L. Asquith<sup>3</sup>, M. Backovic<sup>4</sup>, T. Barillari<sup>5</sup>, P. Berta<sup>6</sup>, D. Bertolini<sup>7</sup>,
D. Adams<sup>1</sup>, A. Arce<sup>2</sup>, L. Asquith<sup>3</sup>, M. Backovic<sup>4</sup>, T. Barillari<sup>3</sup>, P. Berta<sup>3</sup>, D. Bertolini<sup>7</sup>, A. Buckley<sup>8</sup>, J. Butterworth<sup>9</sup>, R. C. Camacho Toro<sup>10</sup>, J. Caudron<sup>11</sup>, Y.-T. Chien<sup>12</sup>, J. Cogan<sup>13</sup>, B. Cooper<sup>9</sup>, D. Curtin<sup>14</sup>, C. Debenedetti<sup>15</sup>, J. Dolen<sup>16</sup>, M. Eklund<sup>17</sup>, S. El Hedri<sup>11</sup>, S. D. Ellis<sup>18</sup>, T. Embry<sup>17</sup>, D. Ferencek<sup>19</sup>, J. Ferrando<sup>8</sup>, S. Fleischmann<sup>20</sup>, M. Freytsis<sup>21</sup>, M. Giulini<sup>22</sup>, Z. Han<sup>23</sup>, D. Hare<sup>24</sup>, P. Harris<sup>25</sup>, A. Hinzmann<sup>26</sup>, R. Hoing<sup>27</sup>, A. Hornig<sup>12</sup>, M. Jankowiak<sup>28</sup>, K. Johns<sup>17</sup>, G. Kasieczka<sup>29</sup>, R. Kogler<sup>27</sup>, W. Lampl<sup>17</sup>, A. J. Larkoski<sup>30</sup>, C. Lee<sup>12</sup>, R. Leone<sup>17</sup>, P. Loch<sup>17</sup>, D. Lopez Mateos<sup>21</sup>, H. K. Lou<sup>31</sup>, M. Low<sup>32</sup>, P. Maksimovic<sup>33</sup>, I. Marchesini<sup>27</sup>, S. Marzani<sup>30</sup>, L. Masetti<sup>11</sup>, R. McCarthy<sup>34</sup>, S. Menke<sup>5</sup>, D. W. Millar<sup>32</sup>, K. Mishar<sup>24</sup>, P. Nasharan<sup>13</sup>, P. Nafl<sup>3</sup>, E. T. O'Carthy<sup>17</sup>, A. Ousharan<sup>35</sup>,
D. W. Miller<sup>32</sup>, K. Mishra<sup>24</sup>, B. Nachman<sup>13</sup>, P. Nef<sup>13</sup>, F. T. O'Grady<sup>17</sup>, A. Ovcharova<sup>35</sup>,
A. Picazio<sup>10</sup>, C. Pollard<sup>8</sup>, B. Potta-Landua<sup>25</sup>, C. Potter<sup>25</sup>, S. Rappoccio<sup>16</sup>, J. Rojo<sup>36</sup>, J. Rutherfoord<sup>17</sup>, G. P. Salam<sup>25,37</sup>, J. Schabinger<sup>38</sup>, A. Schwartzman<sup>13</sup>, M. D. Schwartz<sup>21</sup>
B. Shuve<sup>39</sup>, P. Sinervo<sup>40</sup>, D. Soper<sup>23</sup>, D. E. Sosa Corral<sup>22</sup>, M. Spannowsky<sup>41</sup>, E. Strauss<sup>13</sup>, M. Swiatlowski<sup>13</sup>, J. Thaler<sup>30</sup>, C. Thomas<sup>25</sup>, E. Thompson<sup>42</sup>, N. V. Tran<sup>24</sup>, J. Tseng<sup>36</sup>, E. Usai<sup>27</sup>, L. Valery<sup>43</sup>, J. Veatch<sup>17</sup>, M. Vos<sup>44</sup>, W. Waalewijn<sup>45</sup>, J. Wacker<sup>13</sup>, and C. Young<sup>25</sup>
 <sup>1</sup>Brookhaven National Laboratory, Upton, NY 11973, USA
<sup>2</sup>Duke University, Durham, NC 27708, USA
<sup>3</sup>University of Sussex, Brighton, BN1 9RH, UK
 <sup>4</sup>CP3, Universite catholique du Louvain, B-1348 Louvain-la-Neuve, Belgium
<sup>5</sup>Max-Planck-Institute fuer Physik, 80805 Muenchen, Germany
<sup>6</sup>Charles University in Prague, FMP, V Holesovickach 2, Prague, Czech Republic
<sup>7</sup>University of California, Berkeley, CA 94720, USA
 <sup>8</sup>University of Glasgow, Glasgow, G12 8QQ, UK
 <sup>9</sup>University College London, WC1E 6BT, UK
<sup>10</sup>University of Geneva, CH-1211 Geneva 4, Switzerland
<sup>11</sup>Universitaet Mainz, DE 55099, Germany
<sup>12</sup>Los Alamos National Laboratory, Los Alamos, NM 87545, USA
<sup>13</sup>SLAC National Accelerator Laboratory, Menlo Park, CA 94025, USA
<sup>14</sup>University of Maryland, College Park, MD 20742, USA
<sup>15</sup>University of California, Santa Cruz, CA 95064, USA
<sup>16</sup>University at Buffalo, Buffalo, NY 14260, USA
<sup>17</sup>University of Arizona, Tucson, AZ 85719, USA
<sup>18</sup>University of Washington, Seattle, WA 98195, USA
<sup>19</sup>Rutgers University, Piscataway, NJ 08854, USA
<sup>20</sup>Bergische Universitaet Wuppertal, Wuppertal, D-42097, Germany
<sup>21</sup>Harvard University, Cambridge, MA 02138, USA
<sup>22</sup>Universitaet Heidelberg, DE-69117, Germany
<sup>23</sup>University of Oregon, Eugene, OR 97403, USA
<sup>24</sup>Fermi National Accelerator Laboratory, Batavia, IL 60510, USA
<sup>25</sup>CERN, CH-1211 Geneva 23, Switzerland
<sup>26</sup>Universitaet Zuerich, 8006 Zuerich, Switzerland
<sup>27</sup>Universitaet Hamburg, DE-22761, Germany
<sup>28</sup>New York University, New York, NY 10003, USA
<sup>29</sup>ETH Zuerich, 8092 Zuerich, Switzerland
<sup>30</sup>Massachusetts Institute of Technology, Cambridge, MA 02139, USA
<sup>31</sup>Princeton University, Princeton, NJ 08544, USA
<sup>32</sup>University of Chicago, IL 60637, USA
<sup>33</sup> Johns Hopkins University, Baltimore, MD 21218, USA
<sup>34</sup>YITP, Stony Brook University, Stony Brook, NY 11794-3840, USA
<sup>35</sup>Berkeley National Laboratory, University of California, Berkeley, CA 94720, USA
<sup>36</sup>University of Oxford, Oxford, OX1 3NP, UK
<sup>37</sup>LPTHE, UPMC Univ. Paris 6 and CNRS UMR 7589, Paris, France
^{38} Universidad Autonoma de Madrid, 28049 Madrid, Spain
<sup>39</sup>Perimeter Institute for Theoretical Physics, Waterloo, Ontario N2L 2Y5, Canada
<sup>40</sup>University of Toronto, Toronto, Ontario M5S 1A7, Canada
<sup>41</sup>IPPP, University of Durham, Durham, DH1 3LE, UK
<sup>42</sup>Columbia University, New York, NY 10027, USA
<sup>43</sup>LPC Clermont-Ferrand, 63177 Aubiere Cedex, France
```

¹Address(es) of author(s) should be given Received: date / Accepted: date

⁴⁴Instituto de Física Corpuscular, IFIC/CSIC-UVEG, E-46071 Valencia, Spain

⁴⁵University of Amsterdam, 1012 WX Amsterdam, Netherlands

Abstract Over the past decade, a large number of jet sub-51 structure observables have been proposed in the literature, 52 and explored at the LHC experiments. Such observables at-53 tempt to utilise the internal structure of jets in order to dis-54 tinguish those initiated by quarks, gluons, or by boosted 55 heavy objects, such as Top quarks and W bosons. This re-56 port, originating from and motivated by the BOOST201357 workshop, presents original particle-level studies that aim to 58 improve our understanding of the relationships between jet 59 substructure observables, their complementarity, and their 60 10 dependence on the underlying jet properties, particularly the 61 11 jet radius R and jet p_T . This is explored in the context of 62 12 quark/gluon discrimination, boosted W-boson tagging and 63 boosted Top quark tagging. 14

Keywords boosted objects · jet substructure · beyondthe-Standard-Model physics searches · Large Hadron Collider

66

68

69

1 Introduction

15

45

47

48 49

The center-of-mass energies at the Large Hadron Collider 72 are large compared to the heaviest of known particles, even 73 20 after accounting for parton density functions. With the start 74 21 of the second phase of operation in 2015, the center-of-mass⁷⁵ 22 energy will further increase from 7 TeV in 2010-2011 and 76 23 8 TeV in 2012 to 13 TeV. Thus, even the heaviest states 77 in the Standard Model (and potentially previously unknown⁷⁸ 25 particles) will often be produced at the LHC with substan-79 tial boosts, leading to a collimation of the decay products. 80 27 For fully hadronic decays, these heavy particles will not be 81 reconstructed as several jets in the detector, but rather as 82 29 a single hadronic jet with distinctive internal substructure.83 30 This realization has led to a new era of sophistication in our 84 31 understanding of both standard Quantum Chromodynamics 85 32 (QCD) jets, as well as jets containing the decay of a heavy 86 particle, with an array of new jet observables and detec-87 34 tion techniques introduced and studied to distinguish the two88 types of jets. To allow the efficient propagation of results 89 36 from these studies of jet substructure, a series of BOOST90 Workshops have been held on an annual basis: SLAC (2009) [1], yses presented in this report are: B. Cooper, S. D. Ellis, 38 Oxford University (2010) [2], Princeton University (2011) [39, 39 IFIC Valencia (2012) [4], University of Arizona (2013) [5], 93 and, most recently, University College London (2014) [6]. Following each of these meetings, working groups have generated reports highlighting the most interesting new results,94 43 and often including original particle-level studies. Previous BOOST reports can be found at [7–9].

This report from BOOST 2013 thus views the study and 96 implementation of jet substructure techniques as a fairly ma-97 ture field, and focuses on the question of the correlations98 between the plethora of observables that have been devel-99 oped and employed, and their dependence on the underly100 ing jet parameters, especially the jet radius R and jet p_T . In new analyses developed for the report, we investigate the separation of a quark signal from a gluon background (q/g)tagging), a W signal from a gluon background (W-tagging) and a top signal from a mixed quark/gluon QCD background (top-tagging). In the case of top-tagging, we also investigate the performance of dedicated top-tagging algorithms, the HepTopTagger [10] and the Johns Hopkins Tagger [11]. We study the degree to which the discriminatory information provided by the observables and taggers overlaps by examining the extent to which the signal-background separation performance increases when two or more variables/taggers are combined in a multivariate analysis. Where possible, we provide a discussion of the physics behind the structure of the correlations and the p_T and R scaling that we observe.

We present the performance of observables in idealized simulations without pile-up and detector resolution effects; the relationship between substructure observables, their correlations, and how these depend on the jet radius R and jet p_T should not be too sensitive to such effects. Conducting studies using idealized simulations allows us to more clearly elucidate the underlying physics behind the observed performance, and also provides benchmarks for the development of techniques to mitigate pile-up and detector effects. A full study of the performance of pile-up and detector mitigation strategies is beyond the scope of the current report, and will be the focus of upcoming studies.

The report is organized as follows: in Sections 2-4, we describe the methods used in carrying out our analysis, with a description of the Monte Carlo event sample generation in Section 2, the jet algorithms, observables and taggers investigated in our report in Section 3, and an overview of the multivariate techniques used to combine multiple observables into single discriminants in Section 4. Our results follow in Sections 5-7, with q/g-tagging studies in Section 5, W-tagging studies in Section 6, and top-tagging studies in Section 7. Finally we offer some summary of the studies and general conclusions in Section 8.

The principal organizers of and contributors to the anal-M. Freytsis, A. Hornig, A. Larkoski, D. Lopez Mateos, B. Shuve, and N. V. Tran.

2 Monte Carlo Samples

Below, we describe the Monte Carlo samples used in the q/gtagging, W-tagging, and top-tagging sections of this report. Note that no pile-up (additional proton-proton interactions beyond the hard scatter) are included in any samples, and there is no attempt to emulate the degradation in angular and p_T resolution that would result when reconstructing the jets inside a real detector; such effects are deferred to future43 study.

2.1 Quark/gluon and W-tagging

1 02

1 05

107

108

1 09

110

111

112

113

115

116

118

120

1 21

123

1 24

125

127

128

129

130

132

1 33

1 34

1 35

137

1 39

140 141

142

Samples were generated at $\sqrt{s}=8$ TeV for QCD dijets, and₄₉ for W^+W^- pairs produced in the decay of a (pseudo)-scalar₁₅₀ resonance. The W bosons are decayed hadronically. The QCP₁ events were split into subsamples of gg and $q\bar{q}$ events, allowing for tests of discrimination of hadronic W bosons, quarks, and gluons.

Individual gg and $q\bar{q}$ samples were produced at leading order (LO) using MADGRAPH5 [12], while W^+W^- samples, were generated using the JHU GENERATOR [13–15]. Both, were generated using CTEQ6L1 PDFs [16]. The samples, were produced in exclusive p_T bins of width 100 GeV, with, the slicing parameter chosen to be the of any final state par, in this report were 300-400 GeV, 500-600 GeV and 1.0-1.1, TeV. The samples were then showered through PYTHIA8, (version 8.176) [17] using the default tune 4C [18]. For each of the various samples (W, q, g) and p_T bins, 500k events were simulated.

2.2 Top-tagging

Samples were generated at $\sqrt{s} = 14$ TeV. Standard Model dijet and top pair samples were produced with SHERPA 2.0.062 [19–24], with matrix elements of up to two extra partons matched to the shower. The top samples included only hadrotic decays and were generated in exclusive p_T bins of width 100 GeV, taking as slicing parameter the top quark p_T . The 66 QCD samples were generated with a lower cut on the lead 167 ing parton-level jet p_T , where parton-level jets are clustered 68 with the anti- k_T algorithm and jet radii of R = 0.4, 0.8, 1.2 The matching scale is selected to be $Q_{\rm cut} = 40, 60, 80$ GeV for the $p_{T\,\rm min} = 600, 1000$, and 1500 GeV bins, respectively. For the top samples, 100k events were generated in each bin. 170 while 200k QCD events were generated in each bin.

3 Jet Algorithms and Substructure Observables

In Sections 3.1, 3.2, 3.3 and 3.4, we describe the various jet algorithms, groomers, taggers and other substructure vari₁₇₁ ables used in these studies. Over the course of our study₁₇₂ we considered a larger set of observables, but for presenta₁₇₃ tion purposes we included only a subset in the final analysis₁₇₄ eliminating redundant observables.

3.1 Jet Clustering Algorithms

Jet clustering: Jets were clustered using sequential jet clustering algorithms [25] implemented in FASTJET 3.0.3. Final state particles i, j are assigned a mutual distance d_{ij} and a distance to the beam, d_{iB} . The particle pair with smallest d_{ij} are recombined and the algorithm repeated until the smallest distance is from a particle i to the beam, d_{iB} , in which case i is set aside and labelled as a jet. The distance metrics are defined as

$$d_{ij} = \min(p_{Ti}^{2\gamma}, p_{Tj}^{2\gamma}) \frac{\Delta R_{ij}^2}{R^2}, \tag{1}$$

$$d_{iB} = p_{Ti}^{2\gamma}, \tag{2}$$

where $\Delta R_{ij}^2 = (\Delta \eta_{ij})^2 + (\Delta \phi_{ij})^2$, with $\Delta \eta_{ij}$ being the separation in pseudorapidity of particles i and j, and $\Delta \phi_{ij}$ being the separation in azimuth. In this analysis, we use the anti- k_T algorithm ($\gamma = -1$) [26], the Cambridge/Aachen (C/A) algorithm ($\gamma = 0$) [27, 28], and the k_T algorithm ($\gamma = 1$) [29, 30], each of which has varying sensitivity to soft radiation in the definition of the jet.

Qjets: We also perform non-deterministic jet clustering [31, 32]. Instead of always clustering the particle pair with smallest distance d_{ij} , the pair selected for combination is chosen probabilistically according to a measure

$$P_{ij} \propto e^{-\alpha (d_{ij} - d_{\min})/d_{\min}},\tag{3}$$

where d_{\min} is the minimum distance for the usual jet clustering algorithm at a particular step. This leads to a different cluster sequence for the jet each time the Qjet algorithm is used, and consequently different substructure properties. The parameter α is called the rigidity and is used to control how sharply peaked the probability distribution is around the usual, deterministic value. The Qjets method uses statistical analysis of the resulting distributions to extract more information from the jet than can be found in the usual cluster sequence.

3.2 Jet Grooming Algorithms

160

Pruning: Given a jet, re-cluster the constituents using the C/A algorithm. At each step, proceed with the merger as usual unless both

$$\frac{\min(p_{Ti}, p_{Tj})}{p_{Tij}} < z_{\text{cut}} \text{ and } \Delta R_{ij} > \frac{2m_j}{p_{Tj}} R_{\text{cut}}, \tag{4}$$

in which case the merger is vetoed and the softer branch discarded. The default parameters used for pruning [33] in this report are $z_{\rm cut}=0.1$ and $R_{\rm cut}=0.5$, unless otherwise stated. One advantage of pruning is that the thresholds used to veto soft, wide-angle radiation scale with the jet kinematics, and

180

1 81

182

183

1 84

186

188

189

190

1 91

1 92

193

1 94

1 98

199

200

201

203

2 04

205

206

so the algorithm is expected to perform comparably over 2007 wide range of momenta.

Trimming: Given a jet, re-cluster the constituents into sub₂₁₀ jets of radius R_{trim} with the k_T algorithm. Discard all subjets₁₁ i with

$$p_{Ti} < f_{\text{cut}} p_{TJ}.$$
 (5)

The default parameters used for trimming [34] in this reportant are $R_{\text{trim}} = 0.2$ and $f_{\text{cut}} = 0.03$, unless otherwise stated.

Filtering: Given a jet, re-cluster the constituents into subjets of radius $R_{\rm filt}$ with the C/A algorithm. Re-define the jet to consist of only the hardest N subjets, where N is determined by the final state topology and is typically one more than the number of hard prongs in the resonance decay (to include the leading final-state gluon emission) [35]. While we do not independently use filtering, it is an important step of the HEPTopTagger to be defined later.

Soft drop: Given a jet, re-cluster all of the constituents using the C/A algorithm. Iteratively undo the last stage of the C/A²²⁸ clustering from j into subjets j_1 , j_2 . If

$$\frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} < z_{\text{cut}} \left(\frac{\Delta R_{12}}{R}\right)^{\beta}, \tag{6}_{232}^{231}$$

discard the softer subjet and repeat. Otherwise, take j to be 34 the final soft-drop jet [36]. Soft drop has two input param 235 eters, the angular exponent β and the soft-drop scale $z_{\text{cut} = 36}$. In these studies we use the default $z_{\text{cut}} = 0.1$ setting, with 37 $\beta = 2$.

239 240

3.3 Jet Tagging Algorithms

Modified Mass Drop Tagger: Given a jet, re-cluster all of the constituents using the C/A algorithm. Iteratively undo the last stage of the C/A clustering from j into subjets j_1 , j_2^{245} with $m_{j_1} > m_{j_2}$. If either

$$m_{j_1} > \mu \, m_j \text{ or } \frac{\min(p_{T1}^2, p_{T2}^2)}{m_j^2} \, \Delta R_{12}^2 < y_{\text{cut}},$$
 (7)₄₄₈

then discard the branch with the smaller transverse mass⁵⁰ $m_T = \sqrt{m_i^2 + p_{Ti}^2}$, and re-define j as the branch with the⁵¹ larger transverse mass. Otherwise, the jet is tagged. If declustering continues until only one branch remains, the jet is considered to have failed the tagging criteria [37]. In this55 study we use by default $\mu = 1.0$ (i.e. implement no mass drop criteria) and $y_{\rm cut} = 0.1$. With respect to the singulae53 parts of the splitting functions, this describes the same algo-254 rithm as running soft drop with $\beta = 0$.

Johns Hopkins Tagger: Re-cluster the jet using the C/A algorithm. The jet is iteratively de-clustered, and at each step the softer prong is discarded if its p_T is less than $\delta_p p_{Tjet}$. This continues until both prongs are harder than the p_T threshold, both prongs are softer than the p_T threshold, or if they are too close $(|\Delta \eta_{ij}| + |\Delta \phi_{ij}| < \delta_R)$; the jet is rejected if either of the latter conditions apply. If both are harder than the $p_{\rm T}$ threshold, the same procedure is applied to each: this results in 2, 3, or 4 subjets. If there exist 3 or 4 subjets, then the jet is accepted: the top candidate is the sum of the subjets, and W candidate is the pair of subjets closest to the W mass [11]. The output of the tagger is m_t , m_W , and θ_h , a helicity angle defined as the angle, measured in the rest frame of the W candidate, between the top direction and one of the W decay products. The two free input parameters of the John Hopkins tagger in this study are δ_p and δ_R , defined above, and their values are optimized for different jet kinematics and parameters in Section 7.

HEPTopTagger: Re-cluster the jet using the C/A algorithm. The jet is iteratively de-clustered, and at each step the softer prong is discarded if $m_1/m_{12} > \mu$ (there is not a significant mass drop). Otherwise, both prongs are kept. This continues until a prong has a mass $m_i < m$, at which point it is added to the list of subjets. Filter the jet using $R_{\rm filt} = \min(0.3, \Delta R_{ij})$, keeping the five hardest subjets (where ΔR_{ij} is the distance between the two hardest subjets). Select the three subjets whose invariant mass is closest to m_t [10]. The output of the tagger is m_t , m_W , and θ_h (as defined in the Johns Hopkins Tagger). The two free input parameters of the HEPTopTagger in this study are m and μ , defined above, and their values are optimized for different jet kinematics and parameters in Section 7.

Top-tagging with Pruning or Trimming: In the studies presented in Section 7 we add a *W* reconstruction step to the pruning and trimming algorithms, to enable a fairer comparison with the dedicated top tagging algorithms described above. A *W* candidate is found as follows: if there are two subjets, the highest-mass subjet is the *W* candidate (because the *W* prongs end up clustered in the same subjet); if there are three subjets, the two subjets with the smallest invariant mass comprise the *W* candidate. In the case of only one subjet, no *W* is reconstructed.

3.4 Other Jet Substructure Observables

The jet substructure observables defined in this section are calculated using jet constituents prior to any grooming. This approach has been used in several analyses in the past, for example [38, 39], whilst others have used the approach of

only considering the jet constituents that survive the grooming procedure [40]. We expect that, in the absence of pile-up, the difference between these approaches will be small.

257

258

259

260

261

262

263

265

267

268

269

270

272

274

275

276

277

278

Qjet mass volatility: As described above, Qjet algorithms re-cluster the same jet non-deterministically to obtain a collection of interpretations of the jet. For each jet interpretation, the pruned jet mass is computed with the default pruning parameters. The mass volatility, Γ_{Qjet} , is defined as [31],

$$\Gamma_{\text{Qjet}} = \frac{\sqrt{\langle m_J^2 \rangle - \langle m_J \rangle^2}}{\langle m_J \rangle},$$
(8)

where averages are computed over the Qjet interpretations₂₈₂ We use a rigidity parameter of $\alpha=0.1$ (although other studies suggest a smaller value of α may be optimal [31, 32])_{\$\rightarrow\$83} and 25 trees per event for all of the studies presented here. ²⁸⁴}

N-subjettiness: *N*-subjettiness [41] quantifies how well the radiation in the jet is aligned along *N* directions. To compute *N*-subjettiness, $\tau_N^{(\beta)}$, one must first identify *N* axes within the jet. Then,

$$\tau_N = \frac{1}{d_0} \sum_i p_{Ti} \min\left(\Delta R_{1i}^{\beta}, \dots, \Delta R_{Ni}^{\beta}\right), \tag{9)91}$$

where distances are between particles i in the jet and the axes,

$$d_0 = \sum_{i} p_{Ti} R^{\beta} \tag{10}_{296}$$

and R is the jet clustering radius. The exponent β is a free parameter. There is also some choice in how the axes used to compute N-subjettiness are determined. The optimal configuration of axes is the one that minimizes N-subjettiness; recently, it was shown that the "winner-take-all" (WTA) axes can be easily computed and have superior performance compared to other minimization techniques [42]. We use both the WTA (Section 7) and one-pass k_T optimization axes (Section 5 and 6) in our studies.

Often, a powerful discriminant is the ratio,

$$\tau_{N,N-1} \equiv \frac{\tau_N}{\tau_{N-1}}.\tag{11}_{306}^{305}$$

While this is not an infrared-collinear (IRC) safe observable $_{308}$ it is calculable [43] and can be made IRC safe with a loose $_{309}$ lower cut on τ_{N-1} .

Energy correlation functions: The transverse momentum₃₁₂ version of the energy correlation functions are defined as₃₁₃ [44]:

$$ECF(N,\beta) = \sum_{i_1 < i_2 < \dots < i_N \in j} \left(\prod_{a=1}^{N} p_{Ti_a} \right) \left(\prod_{b=1}^{N-1} \prod_{c=b+1}^{N} \Delta R_{i_b i_c} \right)^{\beta^{315}}_{,317}$$

where i is a particle inside the jet. It is preferable to work in terms of dimensionless quantities, particularly the energy correlation function double ratio:

$$C_N^{(\beta)} = \frac{\text{ECF}(N+1,\beta) \, \text{ECF}(N-1,\beta)}{\text{ECF}(N,\beta)^2}.$$
 (13)

This observable measures higher-order radiation from leading-order substructure. Note that $C_2^{(0)}$ is identical to the variable p_TD introduced by CMS in [45].

4 Multivariate Analysis Techniques

Multivariate techniques are used to combine multiple variables into a single discriminant in an optimal manner. The extent to which the discrimination power increases in a multivariable combination indicates to what extent the discriminatory information in the variables overlaps. There exist alternative strategies for studying correlations in discrimination power, such as "truth matching" [46], but these are not explored here.

In all cases, the multivariate technique used to combine variables is a Boosted Decision Tree (BDT) as implemented in the TMVA package [47]. An example of the BDT settings used in these studies, chosen to reduce the effect of overtraining, is given in [47]. The BDT implementation including gradient boost is used. Additionally, the simulated data were split into training and testing samples and comparisons of the BDT output were compared to ensure that the BDT performance was not affected by overtraining.

5 Quark-Gluon Discrimination

In this section, we examine the differences between quarkand gluon-initiated jets in terms of substructure variables. At a fundamental level, the primary difference between quarkand gluon-initiated jets is the color charge of the initiating parton, typically expressed in terms of the ratio of the corresponding Casimir factors $C_F/C_A = 4/9$. Since the quark has the smaller color charge, it radiates less than a corresponding gluon and the naive expectation is that the resulting quark jet will contain fewer constituents than the corresponding gluon jet. The differing color structure of the two types of jet will also be realized in the detailed behavior of their radiation patterns. We determine the extent to which the substructure observables capturing these differences are correlated, providing some theoretical understanding of these variables and their performance. The motivation for these studies arises not only from the desire to "tag" a jet as originating from a quark or gluon, but also to improve our understanding of the

319

320

321

322

324

326

327

328

330

331

332

333

334

335

336

337

339

340

341

342

343

344

345

346

347

348

349

350

351

352

353

354

355

356

357

358

359

360

361

362

364

365

366

quark and gluon components of the QCD backgrounds rel-367 ative to boosted resonances. While recent studies have sug-368 gested that quark/gluon tagging efficiencies depend highly669 on the Monte Carlo generator used [48, 49], we are moreinterested in understanding the scaling performance with p_{7371} and R, and the correlations between observables, which are a_{72} expected to be treated consistently within a single showeB73 scheme.

Other examples of recent analytic studies of the corre-375 lations between jet observables relevant to quark jet versus76 gluon jet discrimination can be found in [43, 46, 50, 51].

5.1 Methodology and Observable Classes

These studies use the qq and gg MC samples described in $_{82}$ Section 2. The showered events were clustered with FAST₃₈₃ JET 3.03 using the anti- k_T algorithm with jet radii of $R = _{384}$ 0.4, 0.8, 1.2. In both signal (quark) and background (gluon)₈₅ samples, an upper and lower cut on the leading jet p_T is applied after showering/clustering, to ensure similar p_T spectra for signal and background in each p_T bin. The bins in leading jet p_T that are considered are 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV, for the 300-400 GeV, 500-600 GeV, 1.0-387 1.1 TeV parton p_T slices respectively. Various jet grooming approaches are applied to the jets, as described in Sec-389 tion 3.4. Only leading and subleading jets in each sample are g_{90} used. The following observables are studied in this section: 391

- Number of constituents (n_{constits}) in the jet.
- Pruned Qjet mass volatility, Γ_{Qjet} .
- 1-point energy correlation functions, C₁^β with β = 0, 1, 2.
 1-subjettiness, τ₁^β with β = 1, 2. The *N*-subjettiness axes are computed using one-pass k_t axis optimization.
- Ungroomed jet mass, m.

For simplicity, we hereafter refer to quark-initiated jets (gluones initiated jets) as quark jets (gluon jets).

We will demonstrate that, in terms of their jet-by-jet cor₄₀₁ relations and their ability to separate quark jets from gluon, jets, the above observables fall into five Classes. The firs \mathbf{t}_{los} three observables, n_{constits} , Γ_{Qjet} and $C_1^{\beta=0}$, each constitutes α_{04} a Class of its own (Classes I to III) in the sense that they,05 each carry some independent information about a jet and 406 when combined, provide substantially better quark jet and or gluon jet separation than any one observable alone. Of theoremaining observables, $C_1^{\beta=1}$ and $\tau_1^{\beta=1}$ comprise a singleso class (Class IV) because their distributions are similar for 10 a sample of jets, their jet-by-jet values are highly correlated 411 and they exhibit very similar power to separate quark jets12 and gluon jets (with very similar dependence on the jet pa413 rameters R and p_T); this separation power is not improved₁₄ when they are combined. The fifth class (Class V) is com₄₁₅ posed of $C_1^{\beta=2}$, $\tau_1^{\beta=2}$ and the (ungroomed) jet mass. Again₁₀

the jet-by-jet correlations are strong (even though the individual observable distributions are somewhat different), the quark versus gluon separation power is very similar (including the R and p_T dependence), and little is achieved by combining more than one of the Class V observables. This class structure is not surprising given that the observables within a class exhibit very similar dependence on the kinematics of the underlying jet constituents. For example, the members of Class V are constructed from of a sum over pairs of constituents using products of the energy of each member of the pair times the angular separation squared for the pair (this is apparent for the ungroomed mass when viewed in terms of a mass-squared with small angular separations). By the same argument, the Class IV and Class V observables will be seen to be more similar than any other pair of classes, differing only in the power (β) of the dependence on the angular separations, which produces small but detectable differences. We will return to a more complete discussion of jet masses in Section 5.4.

5.2 Single Variable Discrimination

In Figure 1 are shown the quark and gluon distributions of different substructure observables in the $p_T = 500 - 600$ GeV bin for R = 0.8 jets. These distributions illustrate some of the distinctions between the Classes made above. The fundamental difference between quarks and gluons, namely their color charge and consequent amount of radiation in the jet, is clearly indicated in Figure 1(a), suggesting that simply counting constituents provides good separation between quark and gluon jets. In fact, among the observables considered, one can see by eye that n_{constits} should provide the highest separation power, i.e., the quark and gluon distributions are most distinct, as was originally noted in [49, 52]. Figure 1 further suggests that $C_1^{\beta=0}$ should provide the next best separation, followed by $C_1^{\beta=1}$, as was also found by the CMS and ATLAS Collaborations [48, 53].

To more quantitatively study the power of each observable as a discriminator for quark/gluon tagging, Receiver Operating Characteristic (ROC) curves are built by scanning each distribution and plotting the background efficiency (to select gluon jets) vs. the signal efficiency (to select quark jets). Figure 2 shows these ROC curves for all of the substructure variables shown in Figure 1 for R = 0.4, 0.8 and 1.2 jets (in the $p_T = 300\text{-}400$ GeV bin). In addition, the ROC curve for a tagger built from a BDT combination of all the variables (see Section 4) is shown. As suggested earlier, n_{constits} is the best performing variable for all R values, although $C_1^{\beta=0}$ is not far behind, particularly for R=0.8. Most other variables have similar performance, with the main exception of Γ_{Qjet} , which shows significantly worse discrimination (this may be due to our choice of rigidity $\alpha = 0.1$,

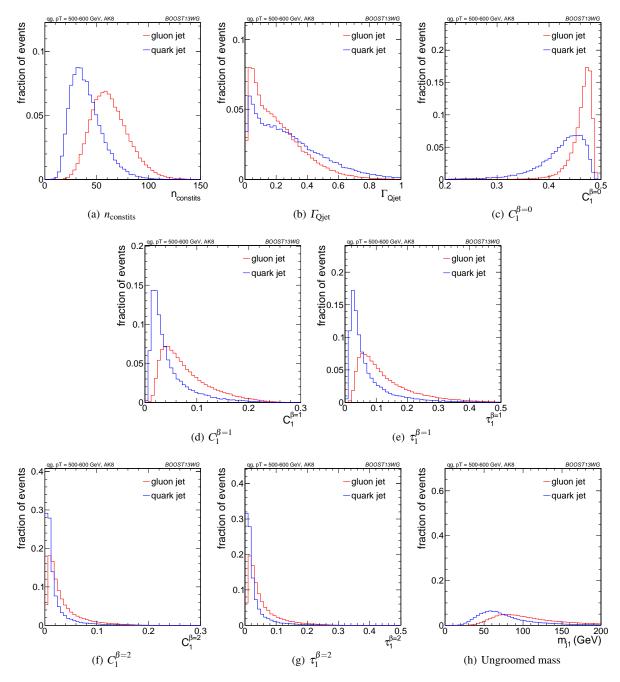


Fig. 1 Comparisons of quark and gluon distributions of different substructure variables, organized by Class, for leading jets in the $p_T = 500 - 600$ GeV bin using the anti- k_T R = 0.8 algorithm. The first three plots are Classes I-III, with Class IV in the second row, and Class V in the third row

with other studies suggesting that a smaller value, such a_{224} $\alpha=0.01$, produces better results [31, 32]). The combina₁₂₅ tion of all variables shows somewhat better discrimination₂₆ than any individual observable, and we give a more detailed₂₇ discussion in Section 5.3 of the correlations between the ob₄₂₈ servables and their impact on the combined discrimination₂₉ power.

4 21

We now examine how the performance of the substructure observables varies with p_T and R. To present the results in a "digestible" fashion we focus on the gluon jet "rejection" factor, $1/\varepsilon_{\rm bkg}$, for a quark signal efficiency, $\varepsilon_{\rm sig}$, of 50%. We can use the values of $1/\varepsilon_{\rm bkg}$ generated for the 9 kinematic points introduced above (R=0.4,0.8,1.2 and the $100~{\rm GeV}$ p_T bins with lower limits $p_T=300~{\rm GeV}$, $500~{\rm GeV}$, $1000~{\rm GeV}$) to generate surface plots. The surface plots in

4 3 3

4 34

4 36

437

4 38

4 39

440

441

442

443

444

446

447

448

449

451

453

4 54

455

456

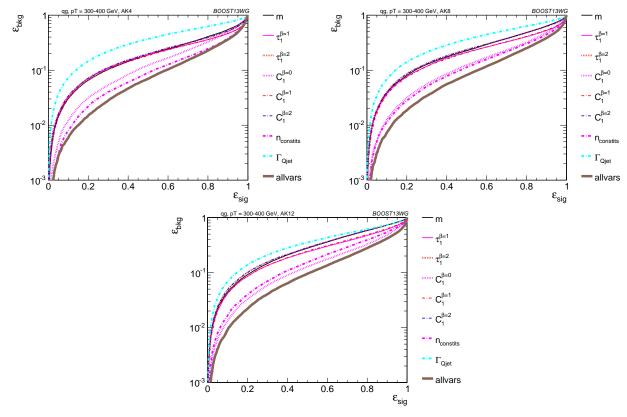


Fig. 2 The ROC curve for all single variables considered for quark-gluon discrimination in the p_T 300-400 GeV bin using the anti- k_T R = 0.4 (top-left), 0.8 (top-right) and 1.2 (bottom) algorithm.

Figure 3 indicate both the level of gluon rejection and thast variation with p_T and R for each of the studied single obts servable. The color shading in these plots is defined so that ass value of $1/\varepsilon_{\rm bkg} \simeq 1$ yields the color "violet", while $1/\varepsilon_{\rm bkg} \simeq$ 20 yields the color "red". The "rainbow" of colors in bette tween vary linearly with $\log_{10}(1/\varepsilon_{\rm bkg})$.

We organize our results by the classes introduced in the 63 previous subsection:

Class I: The sole constituent of this class is n_{constits} . We see in Figure 3(a) that, as expected, the numerically largest re⁴⁶⁵ jection rates occur for this observable, with the rejection fac⁴⁶⁷ tor ranging from 6 to 11 and varying rather dramatically with R. As R increases the jet collects more constituents from the underlying event, which are the same for quark and gluon jets, and the separation power decreases. At large R, there is me improvement with increasing p_T due to the enhanced QCD radiation, which is different for quarks vs. gluons.

Class II: The variable Γ_{Qjet} constitutes this class. Figure 3(b)⁷⁴ confirms the limited efficacy of this single observable (at east for our parameter choices) with a rejection rate only in the range 2.5 to 2.8. On the other hand, this observable roperbes a very different property of jet substructure, *i.e.*, that sensitivity to detailed changes in the grooming procedure and this difference is suggested by the distinct R and P_T de end pendence illustrated in Figure 3(b). The rejection rate in the

creases with increasing R and decreasing p_T , since the distinction between quark and gluon jets for this observable arises from the relative importance of the one "hard" gluon emission configuration. The role of this contribution is enhanced for both decreasing p_T and increasing R.

Class III: The only member of this class is $C_1^{\beta=0}$. Figure 3(c) indicates that this observable can itself provide a rejection rate in the range 7.8 to 8.6 (intermediate between the two previous observables), and again with distinct R and p_T dependence. In this case the rejection rate decreases slowly with increasing R, which follows from the fact that $\beta=0$ implies no weighting of ΔR in the definition of $C_1^{\beta=0}$, greatly reducing the angular dependence. The rejection rate peaks at intermediate p_T values, an effect visually enhanced by the limited number of p_T values included.

Class IV: Figures 3(d) and (e) confirm the very similar properties of the observables $C_1^{\beta=1}$ and $\tau_1^{\beta=1}$ (as already suggested in Figures 1(d) and (e)). They have essentially identical rejection rates (4.1 to 5.4) and identical R and p_T dependence (a slow decrease with increasing R and an even slower increase with increasing p_T).

Class V: The observables $C_1^{\beta=2}$, $\tau_1^{\beta=2}$, and m have similar rejection rates in the range 3.5 to 5.3, as well as very similar R and p_T dependence (a slow decrease with increasing R and an even slower increase with increasing p_T).

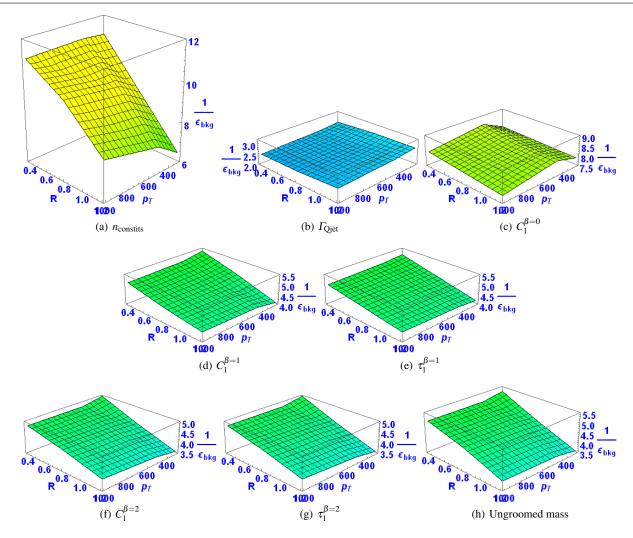


Fig. 3 Surface plots of $1/\varepsilon_{\text{bkg}}$ for all single variables considered for quark-gluon discrimination as functions of R and p_T . The first three plots are Classes I-III, with Class IV in the second row, and Class V in the third row.

Arguably, drawing a distinction between the Class IV₆₀₀ and Class V observables is a fine point, but the color shad₅₀₁ ing does suggest some distinction from the slightly smalle_{E02} rejection rate in Class V. Again the strong similarities between the plots within the second and third rows in Figure 3 speaks to the common properties of the observables within₆₀₃ the two classes.

483

4 84

4 85

486

488

490

4 91

493

4 95

4 97

In summary, the overall discriminating power between quark and gluon jets tends to decrease with increasing R, \exp_{506} cept for the $\Gamma_{\rm Qjet}$ observable, presumably in large part due \exp_{507} the contamination from the underlying event. Since the \exp_{508} struction of the $\Gamma_{\rm Qjet}$ observable explicitly involves pruning way the soft, large angle constituents, it is not surprising that it exhibits different R dependence. In general the \exp_{508} criminating power increases slowly and monotonically with \Pr_{T} (except for the \Pr_{T} and \Pr_{T} observables). This is \exp_{513} sumably due to the overall increase in radiation from \exp_{514} probjects, which accentuates the differences in the quark \Pr_{T}

and gluon color charges and providing some increase in discrimination. In the following section, we study the effect of combining multiple observables.

5.3 Combined Performance and Correlations

Combining multiple observables in a BDT can give further improvement over cuts on a single variable. Since the improvement from combining correlated observables is expected to be inferior to that from combining uncorrelated observables, studying the performance of multivariable combinations gives insight into the correlations between substructure variables and the physical features allowing for quark/gluon discrimination. Based on our discussion of the correlated properties of observables within a single class, we expect little improvement in the rejection rate when combining observables from the same class, and substantial improvement when combining observables from different classes. Our clas-

517

518

519

520

521

523

5 2 4

525

526

527

528

529

5 30

5 31

5 3 2

533

5 3 5

536

537

538

540

542

543

546

547

548

550

551

552

553

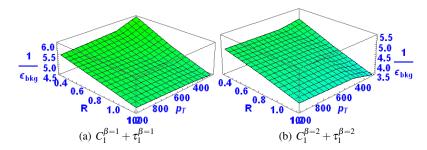


Fig. 4 Surface plots of $1/\epsilon_{\rm bkg}$ for the indicated pairs of variables from (a) Class IV and (b) Class V considered for quark-gluon discrimination as functions of R and p_T .

sification of observables for quark/gluon tagging thereforess motivates the study of particular combinations of variabless for use in experimental analyses.

557

To quantitatively study the improvement obtained from 559 multivariate analyses, we build quark/gluon taggers from every pair-wise combination of variables studied in the previous section; we also compare the pair-wise performance 561 with the all-variables combination. To illustrate the results⁵⁶² achieved in this way, we use the same 2D surface plots as 563 in Figure 3. Figure 4 shows pair-wise plots for variables in 564 (a) Class IV and (b) Class V, respectively. Comparing to⁵⁶⁵ the corresponding plots in Figure 3, we see that combin-566 ing $C_1^{\beta=1} + \tau_1^{\beta=1}$ provides a small ($\sim 10\%$) improvement in ⁵⁶⁷ the rejection rate with essentially no change in the R and p_T^{568} dependence, while combining $C_1^{\beta=2} + \tau_1^{\beta=2}$ yields a rejection rate that is essentially identical to the single observable rejection rate for all R and p_T values (with a similar conclusion if one of these observables is replaced with the ungroomed jet mass m). This confirms the expectation that the observables within a single class effectively probe the same jet properties.

Next, we consider cross-class pairs of observables in Fig577 ure 5, where, except in the one case noted below, we use78 only a single observable from each class for illustrative pur579 poses. Since n_{constits} is the best performing single variable₅₈₀ the largest rejection rates are obtained from combining an 581 other observable with n_{constits} (Figures 5(a) to (e)). In gen₅₈₂ eral, the rejection rates are larger for the pair-wise case than, for the single variable case. In particular, the pair n_{constits} + $C_1^{\beta=1}$ in Figure 5(b) yields rejection rates in the range 6.4 to 14.7 with the largest values at small R and large p_T . Asaa expected, the pair $n_{\text{constits}} + \tau_1^{\beta=1}$ in Figure 5(e) yields very similar rejection rates (6.4 to 15.0), since $C_1^{\beta=1}$ and $\tau_1^{\beta=1_{\text{bas}}}$ are both in Class IV. The other pairings with n_{constits} yield 86 smaller rejection rates and smaller dynamic ranges. The pair⁵⁸⁷ $n_{\text{constits}} + C_1^{\beta=0}$ (Figure 5(d)) exhibits the smallest range of rates (8.3 to 11.3), suggesting that the differences between these two observables serve to substantially reduce the R and p_T dependence for the pair, but this also to reduce the possible optimization. The other pairs shown exhibit similar behavior.

The R and p_T dependence of the pair-wise combinations is generally similar to the single observable with the most dependence on R and p_T . The smallest R and p_T variation always occurs when pairing with $C_1^{\beta=0}$. Changing any of the observables in these pairs with a different observable in the same class $(e.g., C_1^{\beta=2})$ for $\tau_1^{\beta=2}$ produces very similar results. Figure 5(k) shows the result of a BDT analysis including all of the current observables with rejection rates in the range 10.5 to 17.1. This is a somewhat narrower range than in Figure 5(b) but with larger maximum values.

Some features are more easily seen with an alternative presentation of the data: we fix R and p_T and simultaneously show the single- and pair-wise observables performance in a single matrix, and these matrices are shown in Figures 6 and 7. The numbers in each cell are the same rejection rate for gluons used earlier, $1/\varepsilon_{\rm bkg}$, with $\varepsilon_{\rm sig} = 50\%$ (quarks). Figure 6 shows the results for $p_T = 1 - 1.1$ TeV and R =0.4, 0.8, 1.2, while Figure 7 is for R = 0.4 and the 3 p_T bins. The single observable rejection rates appear on the diagonal, and the pairwise results are off the diagonal. The largest pair-wise rejection rate, as already suggested by Figure 5(e), appears at large p_T and small R for the pair $n_{\text{constits}} + \tau_1^{\beta=1}$ (with very similar results for $n_{\text{constits}} + C_1^{\beta=1}$). The correlations indicated by the shading should be largely understood as indicating the organization of the observables into the now-familiar classes. The all-observable (BDT) result appears as the number at the lower right in each plot.

5.4 QCD Jet Masses

To close the discussion of q/g-tagging, we provide some insight into the behavior of the masses of QCD jets initiated by both kinds of partons, with and without grooming. Recall that, in practice, an identified jet is simply a list of constituents, *i.e.*, final state particles. To the extent that

¹The connection between the value of the rejection rate and the shading color in Figures 6 and 7 is the same as that in Figures 3 to 5.



Fig. 5 Surface plots of $1/\epsilon_{\rm bkg}$ for the indicated pairs of variables from different classes considered for quark-gluon discrimination as functions of R and p_T .

5 91

5 9 2

5 9 3

5 9 5

5 9 7

598

5 9 9

600

601

602

603

605

606

608

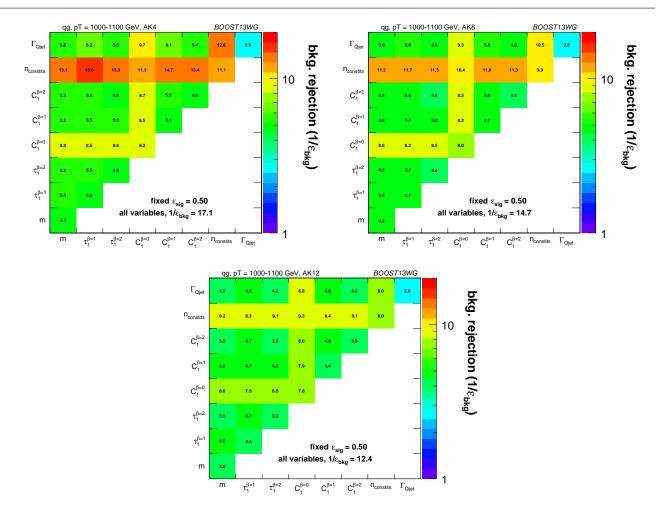


Fig. 6 Gluon rejection defined as $1/\varepsilon_{\text{gluon}}$ when using each 2-variable combination as a tagger with 50% acceptance for quark jets. Results are shown for jets with $p_T = 1 - 1.1$ TeV and for (top left) R = 0.4; (top right) R = 0.8; (bottom) R = 1.2. The rejection obtained with a tagger that uses all variables is also shown in the plots.

the masses of these individual constituents can be neglected of (due to the constituents being relativistic), each constituent has a "well-defined" 4-momentum from its energy and dis11 rection. It follows that the 4-momentum of the jet is simply the sum of the 4-momenta of the constituents and its square is the jet mass squared. Simply on dimensional grounds 14 we know that jet mass must have an overall linear scaling 15 with p_T , with the remaining p_T dependence arising predom 16 in antly from the running of the coupling, $\alpha_s(p_T)$. The R de 17 pendence is also crudely linear as the jet mass scales ap 18 proximately with the largest angular opening between any 210 constituents, which is set by R.

To demonstrate this universal behavior for jet mass, w@21 first note that if we consider the mass distributions for many622 kinematic points (various values of R and p_T), we observ@23 considerable variation in behaviour. This variation, however.624 can largely be removed by plotting versus the scaled variable $m/p_T/R$. The mass distributions for quark and gluon jets26 versus $m/p_T/R$ for all of our kinematic points are shown27

in Figure 8, where we use a logarithmic scale on the y-axis to clearly exhibit the behavior of these distributions over a large dynamic range. We observe that the distributions for the different kinematic points do approximately scale as expected, *i.e.*, the simple arguments above capture most of the variation with R and p_T . We will consider shortly an explanation of the residual non-scaling. A more rigorous quantitative understanding of jet mass distributions requires allorders calculations in QCD, which have been performed for ungroomed jet mass spectra at high logarithmic accuracy, both in the context of direct QCD resummation [54, 55] and Soft Collinear Effective Theory [56, 57].

Several features of Figure 8 can be easily understood. The distributions all cut off rapidly for $m/p_T/R > 0.5$, which is understood as the precise limit (maximum mass) for a jet composed of just 2 constituents. As expected from the soft and collinear singularities in QCD, the mass distribution peaks at small mass values. The actual peak is "pushed" away from the origin by the so-called Sudakov form fac-

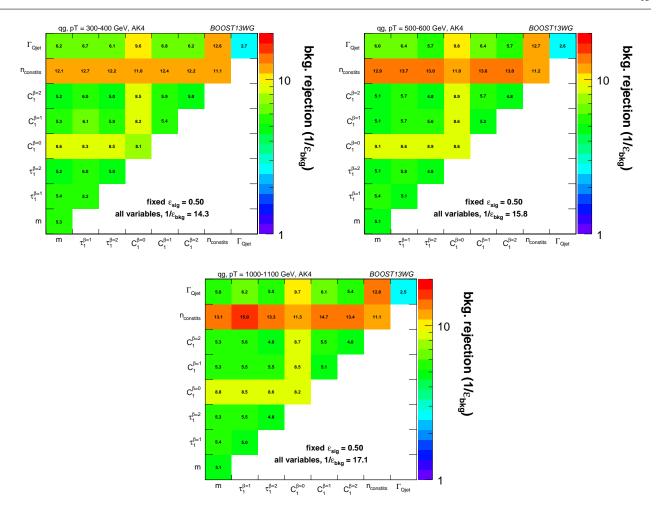


Fig. 7 Gluon rejection defined as $1/\varepsilon_{\text{gluon}}$ when using each 2-variable combination as a tagger with 50% acceptance for quark jets. Results are shown for R=0.4 jets with (top left) $p_T=300-400$ GeV, (top right) $p_T=500-600$ GeV and (bottom) $p_T=1-1.1$ TeV. The rejection obtained with a tagger that uses all variables is also shown in the plots.

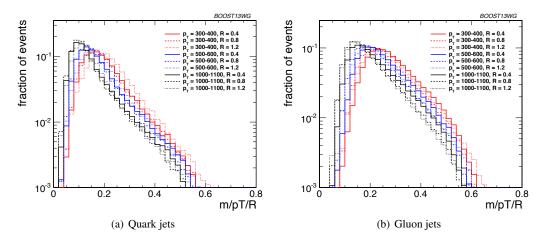


Fig. 8 Comparisons of quark and gluon ungroomed mass distributions versus the scaled variable $m/p_T/R$.

630

631

632

633

634

635

636

638

639

640

641

642

643

645

646

647

648

649

650

652

654

656

657

658

660

661

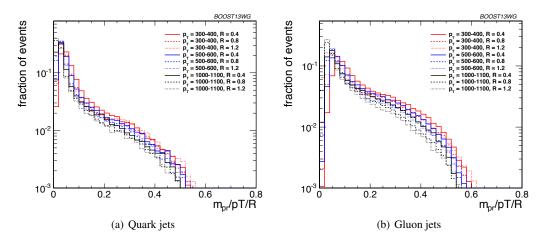


Fig. 9 Comparisons of quark and gluon pruned mass distributions versus the scaled variable $m_{\rm pr}/p_T/R$.

tor. Summing the corresponding logarithmic structure (sin-662 gular in both p_T and angle) to all orders in perturbation the 663 ory yields a distribution that is highly damped as the mass664 vanishes. In words, there is precisely zero probability that &65 color parton emits no radiation (and the resulting jet has zero mass). Above the Sudakov-suppressed part of phase space667 there are two structures in the distribution: the "shoulder"668 and the "peak". The large mass shoulder $(0.3 < m/p_T/R < 669)$ 0.5) is driven largely by the presence of a single large an₆₇₀ gle, energetic emission in the underlying QCD shower, i.e. 671 this regime is quite well described by low-order perturba₆₇₂ tion theory² In contrast, we can think of the peak region as 2, corresponding to multiple soft emissions. This simple, nec-674 essarily approximate picture provides an understanding of the bulk of the differences between the quark and gluon jet $_{76}$ mass distributions. Since the probability of the single large angle, energetic emission is proportional to the color charge the gluon distribution should be enhanced in this region by, a factor of about $C_A/C_F = 9/4$, consistent with what is ob_₆₈₀ served in Figure 8. Similarly the exponent in the Sudakov, damping factor for the gluon jet mass distribution is enhanced by the same factor, leading to a peak "pushed" fur- $_{\overline{683}}$ ther from the origin. Therefore, compared to a quark jet, the gluon jet mass distribution exhibits a larger average jet mass with a larger relative contribution arising from the perturba-686 tive shoulder region and a small mass peak that is further from the origin.

Together with the fact that the number of constituents in the jet is also larger (on average) for the gluon jet simply because a gluon will radiate more than a quark, these features explain much of what we observed earlier in terms of the effectiveness of the various observables to separate quark jets from gluons jets. They also give us insight into the difference in the distributions for the observable $\Gamma_{\rm Qjet}$.

Since the shoulder is dominated by a single large angle, hard emission, it is minimally impacted by pruning, which is designed to remove the large angle, soft constituents (as shown in more detail below). Thus, jets in the shoulder exhibit small volatility and they are a larger component in the gluon jet distribution. Hence gluon jets, on average, have smaller values of $\Gamma_{\rm Qjet}$ than quark jets as in Figure 1(b). Further, this feature of gluon jets is distinct from the fact that there are more constituents, explaining why $\Gamma_{\rm Qjet}$ and $n_{\rm constits}$ supply largely independent information for distinguishing quark and gluon jets.

To illustrate some of these points in more detail, Figure 9 exhibits the same jet mass distributions *after pruning* [33, 58]. Removing the large angle, soft constituents moves the peak in both of the distributions from $m/p_T/R \sim 0.1-0.2$ to the region around $m/p_T/R \sim 0.05$. This explains why pruning works to reduce the QCD background when looking for a signal in a specific jet mass bin. The shoulder feature at higher mass is much more apparent after pruning, as is the larger shoulder for the gluon jets. A quantitative (all-orders) understanding of groomed mass distributions is also possible. For instance, resummation of the pruned mass distribution was achieved in [37, 59]. Figure 9 serves to confirm the physical understanding of the relative behavior of $\Gamma_{\rm Qjet}$ for quark and gluon jets.

Our final topic in this section is the residual R and p_T dependence exhibited in Figures 8 and 9, which indicates a deviation from the naive linear scaling that has been removed by using the scaled variable $m/p_T/R$. A helpful, intuitively simple, if admittedly imprecise, model of a jet is to separate the constituents of the jet into "hard" (with p_T 's that are of order the jet p_T) versus "soft" (with p_T 's small and fixed compared to the jet p_T), and "large" angle (with an angular separation from the jet direction of order R) versus "small" angle (with an angular separation from the jet direction smaller than and not scaling with R) components.

²The shoulder label will become more clear when examining groomed ⁹⁶ jet mass distributions.

As described above the Sudakov damping factor excludes48 constituents that are very soft or very small angle (or both). In this simple picture perturbative large angle, hard con-749 stituents appear rarely, but, as described above, they charac-750 terize the large mass jets that appear in the "shoulder" of the 51 jet mass distribution where the mass scales approximately 52 linearly with the jet p_T and with R. The hard, small angle 53 constituents are somewhat more numerous and contribute to54 a jet mass that does not scale with R. The soft constituents 55 are much more numerous (becoming more numerous with 56 increasing jet p_T) and contribute to a jet mass that scale § 57 like $\sqrt{p_{T,jet}}$. The small angle, soft constituents contribute to 58 a jet mass that does not scale with R, while the large angle₇59 soft constituents do contribute to a jet mass that scales like R_{60} and grow in number approximately linearly in R (i.e., with, the area of the annulus at the outer edge of the jet). This, simple picture allows at least a qualitative explanation of the behavior observed in Figures 8 and 9.

699

701

702

703

704

706

707

708

709

710

711

712

713

715

716

717

718

719

720

721

722

723

725

726

727

728

729

730

732

733

735

736

737

738

739

740

742

744

745

As already suggested, the residual p_T dependence can residual p_T be understood as arising primarily from the slow decrease of the strong coupling $\alpha_s(p_T)$ as p_T increases. This leads to a corresponding decrease in the (largely perturbative) shoul-769 der regime for both distributions at higher p_T , i.e., a decrease⁷⁷⁰ in the number of hard, large angle constituents. At the same 771 time, and for the same reason, the Sudakov damping is less $^{772}\,$ strong with increasing p_T and the peak moves in towards⁷⁷³ the origin. While the number of soft constituents increases⁷⁷⁴ with increasing jet p_T , their contributions to the scaled jet⁷⁷⁵ mass distribution shift to smaller values of m/p_T (decreas-776 ing approximately like $1/\sqrt{p_T}$). Thus the overall impact of increasing p_T for both distributions is a (gradual) shift to⁷⁷⁸ smaller values of $m/p_T/R$. This is just what is observed in 779 Figures 8 and 9, although the numerical size of the effect is 780 reduced in the pruned case.

The residual R dependence is somewhat more complized cated. The perturbative large angle, hard constituent contribution largely scales in the variable $m/p_T/R$, which is whyres we see little residual R dependence in either figure at highermasses $(m/p_T/R > 0.4)$. The contribution of the small angless constituents (hard and soft) contribute at fixed m and thus shift to the left versus the scaled variable as R increases₇₈₇ This presumably explains the small shifts in this direction** at small mass observed in both figures. The large angle, softso constituents contribute to mass values that scale like R, and $_{790}$ as noted above, tend to increase in number as R increases, (i.e., as the area of the jet grows). Such contributions yield 92 a scaled jet mass distribution that shifts to the right with in 793 creasing R and presumably explain the behavior at small $p_{T^{794}}$ in Figure 8. Since pruning largely removes this contribution₇₉₅ we observe no such behavior in Figure 9.

5.5 Conclusions

In Section 5 we have seen that a variety of jet observables provide information about the jet that can be employed to effectively separate quark-initiated from gluon-initiated jets. Further, when used in combination, these observables can provide superior separation. Since the improvement depends on the correlation between observables, we use the multivariable performance to separate the observables into different classes, with each class containing highly correlated observables. We saw that the best performing single observable is simply the number of constituents in the jet, n_{constits} , while the largest further improvement comes from combining with $C_1^{\beta=1}$ (or $\tau_1^{\beta=1}$), but the smallest R and p_T dependence arises from combining with $C_1^{\beta=0}$. On the other hand, some of the commonly used observables are highly correlated and do not provide extra information and enhanced tagging when used together. In addition to demonstrating these correlations, we have provided a discussion of the physics behind the structure of the correlation. Using the jet mass as an example, we have given arguments to explicitly explain the differences between jet observables initiated by each type of parton.

Finally, we remind the reader that the numerical results were derived for a particular color configuration (qq and gg events), in a particular implementation of the parton shower and hadronization. Color connections in more complex event configurations, or different Monte Carlo programs, may well exhibit somewhat different efficiencies and rejection factors. The value of our results is that they indicate a subset of variables expected to be rich in information about the partonic origin of final-state jets. These variables can be expected to act as valuable discriminants in searches for new physics, and could also be used to define model-independent final-state measurements which would nevertheless be sensitive to the short-distance physics of quark and gluon production.

6 Boosted W-Tagging

In this section, we study the discrimination of a boosted, hadronically decaying W boson (signal) against a gluon-initiated jet background, comparing the performance of various groomed jet masses and substructure variables. A range of different distance parameters for the anti- k_T jet algorithm are explored, in a range of different leading jet p_T bins. This allows us to determine the performance of observables as a function of jet radius and jet boost, and to see where different approaches may break down. The groomed mass and substructure variables are then combined in a BDT as described in Section 4, and the performance of the resulting BDT discriminant explored through ROC curves to understand the degree to which variables are correlated, and how this changes with jet boost and jet radius.

800

801

803

805

806

807

809

810

811

812

814

815

816

817

818

819

820

821

822

823

825

826

827

828

829

830

831

833

834

835

836

837

838

839

840

842

843 844

845

6.1 Methodology

These studies use the WW samples as signal and the dijet₈₄₈ gg as background, described previously in Section 2. Whilst₈₄₉ only gluonic backgrounds are explored here, the conclusions₈₅₀ regarding the dependence of the performance and correla₈₅₁ tions on the jet boost and radius are not expected to be sub₈₅₂ stantially different for quark backgrounds; we will see that₈₅₃ the differences in the substructure properties of quark- and₈₅₄ gluon-initiated jets, explored in the last section, are signifi₈₅₅ cantly smaller than the differences between W-initiated and₈₅₆ gluon-initiated jets.

As in the q/g tagging studies, the showered events were clustered with FASTJET 3.03 using the anti- k_T algorithm₈₅₉ with jet radii of R=0.4,0.8,1.2. In both signal and back₈₆₀ ground samples, an upper and lower cut on the leading jet₈₆₁ p_T is applied after showering/clustering, to ensure similate₈₆₂ p_T spectra for signal and background in each p_T bin. The₈₆₃ bins in leading jet p_T that are considered are 300-400 GeV₈₆₄ 500-600 GeV, 1.0-1.1 TeV, for the 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV parton p_T slices respectively. The jets then₈₆₆ have various grooming algorithms applied and substructure observables reconstructed as described in Section 3.4. The₈₆₈ substructure observables studied in this section are:

- Ungroomed, trimmed (m_{trim}) , and pruned (m_{prun}) jet masses.
- Mass output from the modified mass drop tagger $(m_{\text{mmdt}})^{871}$
- Soft drop mass with $\beta = 2$ (m_{sd}).
- 2-point energy correlation function ratio $C_2^{\beta=1}$ (we also studied $\beta=2$ but do not show its results because it showed poor discrimination power).
- N-subjettiness ratio τ_2/τ_1 with $\beta = 1$ ($\tau_{21}^{\beta=1}$) and with axes computed using one-pass k_t axis optimization (we also studied $\beta = 2$ but did not show its results because if showed poor discrimination power).

882

- Pruned Qjet mass volatility, Γ_{Qjet} .

6.2 Single Variable Performance

In this section we explore the performance of the variousss groomed jet mass and substructure variables in separatingss signal from background. Since we have not attempted to opsst timise the grooming parameter settings of each groomingss algorithm, we do not place much emphasis here on the relss ative performance of the groomed masses, but instead consponentiate on how their performance changes depending on these kinematic bin and jet radius considered.

Figure 10 compares the signal and background in terms93 of the different groomed masses explored for the anti- k_T R =894 0.8 algorithm in the p_T = 500-600 GeV bin. One can clearly695 see that, in terms of separating signal and background, th696 groomed masses are significantly more performant than th697 ungroomed anti- k_T R = 0.8 mass. Using the same jet radius998

and p_T bin, Figure 11 compares signal and background for the different substructure variables studied.

Figures 12, 13 and 14 show the single variable ROC curves for various p_T bins and values of R. The single-variable performance is also compared to the ROC curve for a BDT combination of all the variables (labelled "allvars"). In all cases, the "allvars" option is significantly more performant than any of the individual single variables considered, indicating that there is considerable complementarity between the variables, and this is explored further in Section 6.3.

In Figures 15, 16 and 17 the same information is shown in a format that more readily allows for a quantitative comparison of performance for different R and p_T ; matrices are presented which give the background rejection for a signal efficiency of 70% for single variable cuts, as well as two- and three-variable BDT combinations. The results are shown separately for each p_T bin and jet radius considered. Most relevant for our immediate discussion, the diagonal entries of these plots show the background rejections for a single-variable BDT using the labelled observable, and can thus be examined to get a quantitative measure of the individual single variable performance, and to study how this changes with jet radius and momenta. The off-diagonal entries give the performance when two variables (shown on the x-axis and on the y-axis, respectively) are combined in a BDT. The final column of these plots shows the background rejection performance for three-variable BDT combinations of $m_{sd}^{\beta=2} + C_2^{\beta=1} + X$. These results will be discussed later in Section 6.3.3.

In general, the most performant single variables are the groomed masses. However, in certain kinematic bins and for certain jet radii, $C_2^{\beta=1}$ has a background rejection that is comparable to or better than the groomed masses.

We first examine the variation of performance with jet p_T . By comparing Figures 15(a), 16(a) and 17(b), we can see how the background rejection performance varies with increased momenta whilst keeping the jet radius fixed to R =0.8. Similarly, by comparing Figures 15(b), 16(b) and 17(c) we can see how performance evolves with p_T for R = 1.2. For both R = 0.8 and R = 1.2 the background rejection power of the groomed masses increases with increasing p_T , with a factor 1.5-2.5 increase in rejection in going from the 300-400 GeV to 1.0-1.1 TeV bins. In Figure 18 we show the $m_{\rm sd}$ and $m_{\rm prun}$ groomed masses for signal and background in the $p_T = 300-400$ and $p_T = 1.0-1.1$ TeV bins for R = 1.2jets. Two effects result in the improved performance of the groomed mass at high p_T . Firstly, as is evident from the figure, the resolution of the signal peak after grooming improves, because the groomer finds it easier to pick out the hard signal component of the jet against the softer components of the underlying event when the signal is boosted. Secondly, it follows from Figure 9 and the discussion in Section 5.4 that, for increasing p_T , the perturbative shoulder of

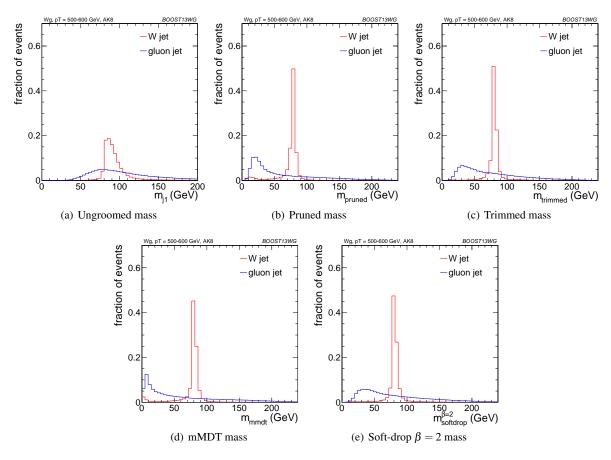


Fig. 10 Leading jet mass distributions in the gg background and WW signal samples in the $p_T = 500\text{-}600$ GeV bin using the anti- k_T R = 0.8 algorithm.

the gluon distribution decreases in size, and thus there is a_{21} slight decrease (or at least no increase) of the background₂₂ contamination in the signal mass region (m/ $p_T/R \sim 0.5$).

However, one can see from the Figures 15(b), 16(b) and $\mathfrak{h}_{24}^{-7}(c)$ that the $C_2^{\beta=1}$, $\Gamma_{\rm Qjet}$ and $\tau_{21}^{\beta=1}$ substructure variables behave somewhat differently. The background rejection power of \mathfrak{h}_{26} the $\Gamma_{\rm Qjet}$ and $\tau_{21}^{\beta=1}$ variables both decrease with increasing \mathfrak{p}_{27} to 1.0-1.1 TeV bins. Conversely the rejection power of $C_2^{\beta=1}$ dramatically increases with increasing \mathfrak{p}_T for R=0.8, but $\mathfrak{p}_T=0.8$ of $\mathfrak{p}_T=0.8$ does not improve with $\mathfrak{p}_T=0.8$ for the larger jet radius $\mathfrak{p}_T=0.8$ signal and background in the $\mathfrak{p}_T=0.8$ distributions for $\mathfrak{p}_T=0.8$ signal and background in the $\mathfrak{p}_T=0.8$ jets. For $\tau_{21}^{\beta=1}=0.8$ one can see that, in moving from lower to higher $\mathfrak{p}_T=0.8$ bins, the signal peak remains fairly unchanged, whereas the background peak shifts to smaller $\tau_{21}^{\beta=1}=0.8$ values, reducing the discriminating power of the variable. This is expected, since jet substructure methods explicitly relying on the identification of hard prongs would tended to be more separated. However, $C_2^{\beta=1}=0.8$ does not rely on the explicit identification of subjets, and one can see from Fig. 10 and 1

ure 19 that the discrimination power visibly increases with increasing p_T . This is in line with the observation in [44] that $C_2^{\beta=1}$ performs best when m/p_T is small.

We now compare the performance of different jet radius parameters in the same p_T bin by comparing the individual sub-figures of Figures 15, 16 and 17. To within $\sim 25\%$, the background rejection power of the groomed masses remains constant with respect to the jet radius. Figure 20 shows how the groomed mass changes for varying jet radius in the p_T = 1.0-1.1 TeV bin. One can see that the signal mass peak remains unaffected by the increased radius, as expected, since grooming removes the soft contamination which could otherwise increase the mass of the jet as the radius increased. The gluon background in the signal mass region also remains largely unaffected, as follows from Figure 9 and the discussion in Section 5.4, where it is shown that there is very little dependence of the groomed gluon mass distribution on R in the signal region $(m/p_T/R \sim 0.5)$.

However, we again see rather different behaviour versus R for the substructure variables. In all p_T bins considered, the most performant substructure variable, $C_2^{\beta=1}$, performs best for an anti- k_T distance parameter of R=0.8. The per-



Fig. 11 Leading jet substructure variable distributions in the gg background and WW signal samples in the $p_T = 500$ -600 GeV bin using the anti- k_T R = 0.8 algorithm.



Fig. 12 ROC curves for single variables considered for W tagging in the $p_T = 300\text{-}400$ GeV bin using the anti- k_T R = 0.8 algorithm and R = 1.2 algorithm, along with a BDT combination of all variables ("allvars").



Fig. 13 ROC curves for single variables considered for W tagging in the $p_T = 500\text{-}600$ GeV bin using the anti- k_T R = 0.8 algorithm and R = 1.2 algorithm, along with a BDT combination of all variables ("allvars")



Fig. 14 ROC curves for single variables considered for W tagging in the $p_T = 1.0$ -1.1 TeV bin using the anti- $k_T R = 0.4$ algorithm, anti- $k_T R = 0.8$ algorithm and R = 1.2 algorithm, along with a BDT combination of all variables ("allvars")

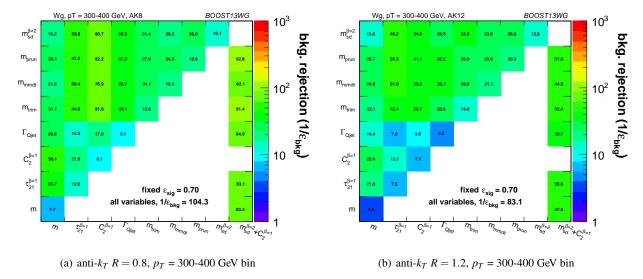


Fig. 15 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the $p_T = 300\text{-}400$ GeV bin using the anti- k_T R = 0.8 algorithm and R = 1.2 algorithm. Also shown is the background rejection for three-variable combinations involving $m_{sd}^{\beta=2} + C_2^{\beta=1}$, and for a BDT combination of all of the variables considered.

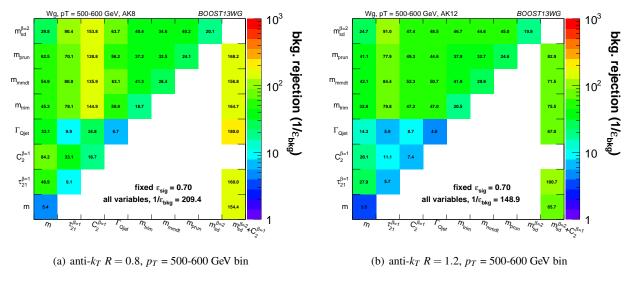


Fig. 16 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the $p_T = 500\text{-}600$ GeV bin using the anti- k_T R = 0.8 algorithm and R = 1.2 algorithm. Also shown is the background rejection for three-variable combinations involving $m_{sd}^{\beta=2} + C_2^{\beta=1}$, and for a BDT combination of all of the variables considered.

formance of this variable is dramatically worse for the largeb54 jet radius of R=1.2 (a factor seven worse background re955 jection in the $p_T=1.0$ -1.1 TeV bin), and substantially worse56 for R=0.4. For the other jet substructure variables consid957 ered, $\Gamma_{\rm Ojet}$ and $\tau_{21}^{\beta=1}$, their background rejection power also958 reduces for larger jet radius, but not to the same extent. Fig.959 ure 21 shows the $\tau_{21}^{\beta=1}$ and $C_2^{\beta=1}$ distributions for signal and background in the $p_T=1.0$ -1.1 TeV bin for R=0.8 and R=1.2 jet radii. For the larger jet radius, the $C_2^{\beta=1}$ distribution of both signal and background get wider, and conse.963 quently the discrimination power decreases. For $\tau_{21}^{\beta=1}$ there

is comparatively little change in the distributions with increasing jet radius. The increased sensitivity of C_2 to soft wide angle radiation in comparison to τ_{21} is a known feature of this variable [44], and a useful feature in discriminating coloured versus colour singlet jets. However, at very large jet radii ($R \sim 1.2$), this feature becomes disadvantageous; the jet can pick up a significant amount of initial state or other uncorrelated radiation, and C_2 is more sensitive to this than is τ_{21} . This uncorrelated radiation has no (or very little) dependence on whether the jet is W- or gluon-initiated, and

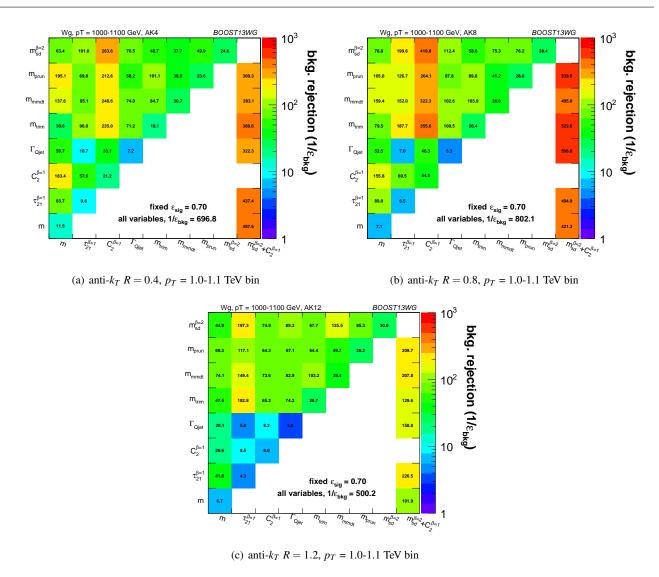


Fig. 17 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the $p_T = 1.0$ -1.1 TeV bin using the anti- $k_T R = 0.4$, R = 0.8 and R = 1.2 algorithm. Also shown is the background rejection for three-variable combinations involving $m_{sd}^{\beta=2} + C_2^{\beta=1}$, and for a BDT combination of all of the variables considered.

so sensitivity to this radiation means that the discrimination power will decrease.

6.3 Combined Performance

Studying the improvement in performance (or lack thereof)⁹⁸² when combining single variables into a multivariate analy⁹⁸³ sis gives insight into the correlations among jet observables.⁹⁸⁴ The off-diagonal entries in Figures 15, 16 and 17 can be used₈₅ to compare the performance of different BDT two-variable₈₆ combinations, and see how this varies as a function of p_{T987} and R. By comparing the background rejection achieved fo₈₆₈ the two-variable combinations to the background rejection₈₆₉ of the "all variables" BDT, one can also understand how dis₉₉₀

crimination can be improved by adding further variables to the two-variable BDTs.

In general the most powerful two-variable combinations involve a groomed mass and a non-mass substructure variable $(C_2^{\beta=1}, \Gamma_{\rm Qjet} \text{ or } \tau_{21}^{\beta=1})$. Two-variable combinations of the substructure variables are not as powerful in comparison. Which particular mass + substructure variable combination is the most powerful depends strongly on the p_T and R of the jet, as discussed in the sections to follow.

There is also modest improvement in the background rejection when different groomed masses are combined, indicating that there is complementary information between the different groomed masses. In addition, there is an improvement in the background rejection when the groomed masses are combined with the ungroomed mass, indicating

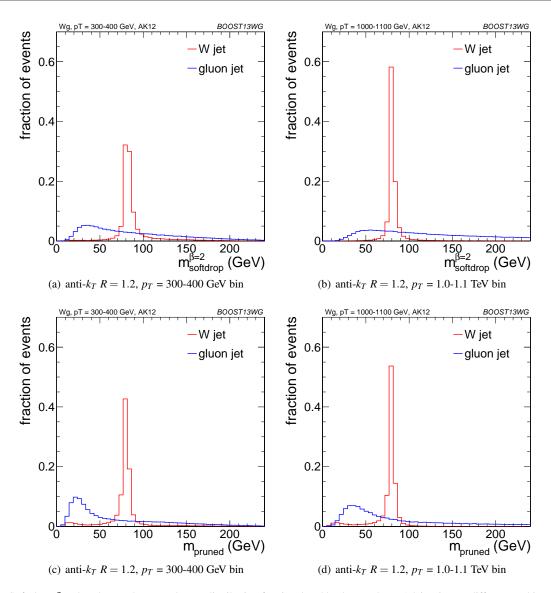


Fig. 18 The Soft-drop $\beta = 2$ and pruned groomed mass distribution for signal and background R = 1.2 jets in two different p_T bins.

that grooming removes some useful discriminatory informa₀₀₅ tion from the jet. These observations are explored further inoc the section below.

Generally, the R=0.8 jets offer the best two-variableous combined performance in all p_T bins explored here. This isometes despite the fact that in the highest $p_T=1.0\text{-}1.1$ TeV bin theoret average separation of the quarks from the W decay is muchous smaller than 0.8, and well within 0.4. This conclusion could of course be susceptible to pile-up, which is not considered in this study.

As already noted, the largest background rejection at 70% signal efficiency are in general achieved using those two variable BDT combinations which involve a groomed masses

and a non-mass substructure variable. We now investigate the p_T and R dependence of the performance of these combinations.

For both R = 0.8 and R = 1.2 jets, the rejection power of these two-variable combinations increases substantially with increasing p_T , at least within the p_T range considered here.

For a jet radius of R=0.8, across the full p_T range considered, the groomed mass + substructure variable combinations with the largest background rejection are those which involve $C_2^{\beta=1}$. For example, in combination with $m_{\rm sd}$, this produces a five-, eight- and fifteen-fold increase in background rejection compared to using the groomed mass alone. In Figure 22, the low degree of correlation between $m_{\rm sd}$ versus $C_2^{\beta=1}$ that leads to these large improvements in background rejection can be seen. What little correlation exists is rather

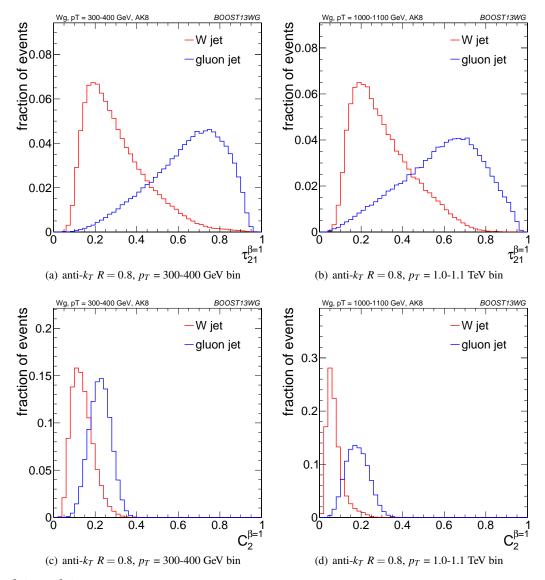


Fig. 19 The $\tau_{21}^{\beta=1}$ and $C_2^{\beta=1}$ distributions for signal and background R=0.8 jets in two different p_T bins.

non-linear in nature, changing from a negative to a positive correlation as a function of the groomed mass, something which helps to improve the background rejection in the region of the W mass peak.

However, when we switch to a jet radius of R=1.2 the picture for $C_2^{\beta=1}$ combinations changes dramatically. These picture for $C_2^{\beta=1}$ combinations changes dramatically. These variable in groomed mass combinations becomes $\tau_{21}^{\beta=1}$ for all jet p_T considered. Figure 23 shows the correlation because $m_{sd}^{\beta=2}$ and $C_2^{\beta=1}$ in the $p_T=1.0$ - 1.2 TeV bin for the various jet radii considered. Figure 24 is the equivalent set $q_{sd}^{\beta=4}$ distributions for $m_{sd}^{\beta=2}$ and $\tau_{21}^{\beta=1}$. One can see from Figure 23 that, due to the sensitivity of the observable to to soft, wide $q_{sd}^{\beta=1}$ angle radiation, as the jet radius increases $C_2^{\beta=1}$ increases and becomes more and more smeared out for both signal and $q_{sd}^{\beta=1}$

background, leading to worse discrimination power. This does not happen to the same extent for $\tau_{21}^{\beta=1}$. We can see from Figure 24 that the negative correlation between $m_{sd}^{\beta=2}$ and $\tau_{21}^{\beta=1}$ that is clearly visible for R=0.4 decreases for larger jet radius, such that the groomed mass and substructure variable are far less correlated and $\tau_{21}^{\beta=1}$ offers improved discrimination within a $m_{sd}^{\beta=2}$ mass window.

6.3.2 Mass + Mass Performance

The different groomed masses and the ungroomed mass are of course not fully correlated, and thus one can always see some kind of improvement in the background rejection when two different mass variables are combined in the BDT. However, in some cases the improvement can be dramatic, partic-

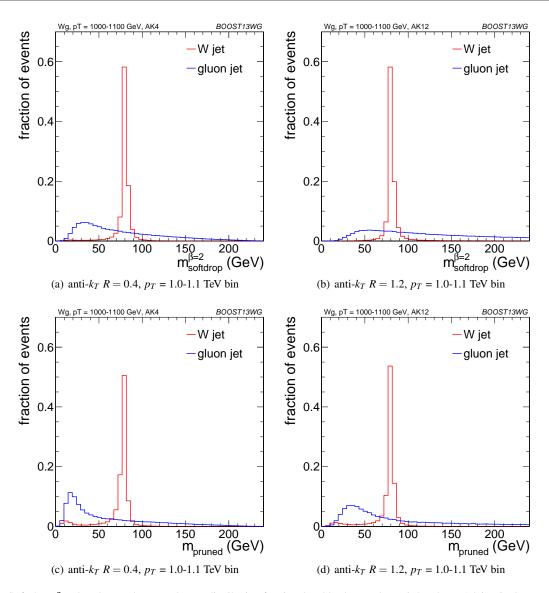


Fig. 20 The Soft-drop $\beta = 2$ and pruned groomed mass distribution for signal and background R = 0.4 and R = 1.2 jets in the $p_T = 1.0$ -1.1 TeV bin.

ularly at higher p_T , and particularly for combinations without the ungroomed mass. For example, in Figure 17 we can secons that in the p_T =1.0-1.1 TeV bin, the combination of prunedommass with ungroomed mass produces a greater than eightost fold improvement in the background rejection for R = 0.4668 jets, a greater than five-fold improvement for R = 0.8 jets, a greater than five-fold improvement for R = 0.8 jets. A similative behaviour can be seen for mMDT mass. In Figures 25, 26071 and 27, we show the 2-D correlation plots of the prunedot mass versus the ungroomed mass separately for the WW673 signal and gg background samples in the $p_T = 1.0$ -1.1 TeV674 bin, for the various jet radii considered. For comparison, theoretical combination of the trimmed mass with the ungroomed mass gr a combination that does not improve on the single mass gr dramatically, is shown. In all cases one can see that therefore

is a much smaller degree of correlation between the pruned mass and the ungroomed mass in the backgrounds sample than for the trimmed mass and the ungroomed mass. This is most obvious in Figure 25, where the high degree of correlation between the trimmed and ungroomed mass is expected, since with the parameters used (in particular $R_{\rm trim}=0.2$) we cannot expect trimming to have a significant impact on an R=0.4 jet. The reduced correlation with ungroomed mass for pruning in the background means that, once we have required that the pruned mass is consistent with a W (i.e. ~ 80 GeV), a relatively large difference between signal and background in the ungroomed mass still remains, and can be exploited to improve the background rejection further. In other words, many of the background events which pass the pruned mass requirement do so because they are shifted

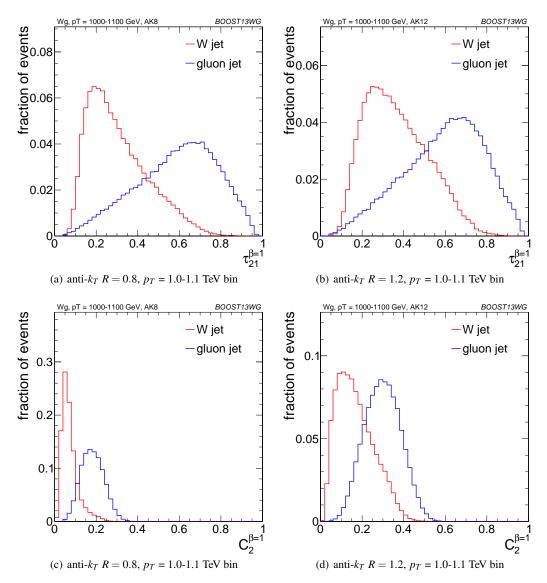


Fig. 21 The $\tau_{21}^{\beta=1}$ and $C_2^{\beta=1}$ distributions for signal and background R=0.8 and R=1.2 jets in the $p_T=1.0$ -1.1 TeV bin.

to lower mass (to be within a signal mass window) by theos grooming, but these events still have the property that they look very much like background events before the groomosting. A requirement on the groomed mass alone does not exploit this property. Of course, the impact of pile-up, not considered in this study, could limit the degree to which theos ungroomed mass could be used to improve discrimination in this way.

Figures 15, 16 and 17 report the background rejection achieved by a combination of all the variables considered into a single of BDT discriminant. In all cases, the rejection power of this of "all variables" BDT is significantly larger than the best two 107 variable combination. This indicates that, beyond the best of

two-variable combination, there is still significant complementary information available in the remaining observables to improve the discrimination of signal and background. How much complementary information is available appears to be p_T dependent. In the lower $p_T = 300\text{-}400$ and 500-600 GeV bins, the background rejection of the "all variables" combination is a factor ~ 1.5 greater than the best two-variable combination, but in the highest p_T bin it is a factor ~ 2.5 greater.

The final column in Figures 15, 16 and 17 allows us to further explore the all variables performance relative to the pair-wise performance. It shows the background rejection for three-variable BDT combinations of $m_{\rm sd}^{\beta=2}+C_2^{\beta=1}+X$, where X is the variable on the y-axis. For jets with R=0.4 and R=0.8, the combination $m_{\rm sd}^{\beta=2}+C_2^{\beta=1}$ is (at least close to) the best performant two-variable combination in every



Fig. 22 2-D histograms of $m_{sd}^{\beta=2}$ versus $C_2^{\beta=1}$ distributions for R=0.8 jets in the various p_T bins considered, shown separately for signal and background.



Fig. 23 2-D histograms of $m_{sd}^{\beta=2}$ versus $C_2^{\beta=1}$ for R=0.4,0.8 and 1.2 jets in the $p_T=1.0$ -1.1 TeV bin, shown separately for signal and background.



Fig. 24 2-D histograms of $m_{sd}^{\beta=2}$ versus $\tau_{21}^{\beta=1}$ for R=0.4,0.8 and 1.2 jets in the $p_T=1.0$ -1.1 TeV bin, shown separately for signal and background.

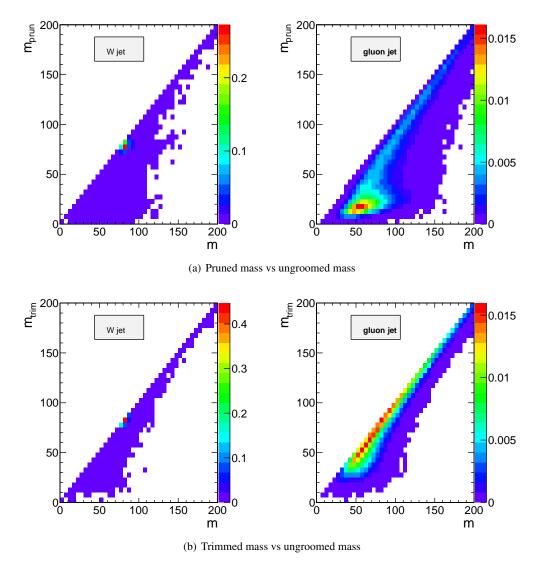


Fig. 25 2-D histograms of groomed mass versus ungroomed mass in the $p_T = 1.0$ -1.1 TeV bin using the anti- $k_T R = 0.4$ algorithm, shown separately for signal and background.

 p_T bin considered. For R=1.2 this is not the case, as $C_2^{\beta=1\atop 1125}$ is superseded by $\tau_{21}^{\beta=1}$ in performance, as discussed earliet thus, in considering the three-variable combination results this simplest to focus on the R=0.4 and R=0.8 cases. Here we see that, for the lower $p_T=300$ -400 and 500-600 GeV bins, adding the third variable to the best two-variable continuous bination brings us to within $\sim 15\%$ of the "all variables $p_T=1.0$ -1.1 TeV bin, whilst adding the third variable does improve the performance considerably, we are still $\sim 40\%$ from the observed "all variables" background rejection, and clearly adding a fourth or maybe even fifth variable would bring considerable gains. In terms of which variable offers the best improvement when added to the $m_{\rm sd}^{\beta=2} + C_2^{\beta=1}$ combination, it is hard to see an obvious pattern; the best third variable changes depending on the p_T and R considered.

It appears that there is a rich and complex structure in terms of the degree to which the discriminatory information provided by the set of variables considered overlaps, with the degree of overlap apparently decreasing at higher p_T . This suggests that in all p_T ranges, but especially at higher p_T , there are substantial performance gains to be made by designing a more complex multivariate W tagger.

6.4 Conclusions

We have studied the performance, in terms of the separation of a hadronically decaying *W* boson from a gluon-initiated jet background, of a number of groomed jet masses, substructure variables, and BDT combinations of the above. We have used this to gain insight into how the discriminatory information contained in the variables overlaps, and how this

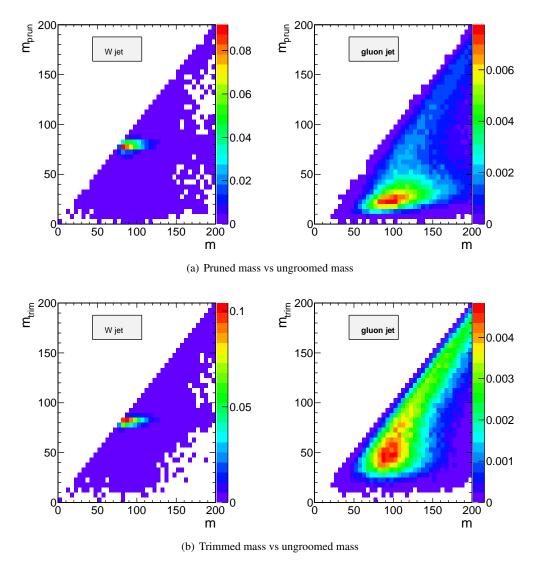


Fig. 26 2-D histograms of groomed mass versus ungroomed mass in the $p_T = 1.0$ -1.1 TeV bin using the anti- $k_T R = 0.8$ algorithm, shown separately for signal and background.

complementarity between the variables changes with jet p_{T_154} and anti- k_T distance parameter R.

In terms of the performance of individual variables, with find that, in agreement with other studies [40], the groomed masses generally perform best, with a background rejection power that increases with larger p_T , but which is more consistent with respect to changes in R. We have explained the dependence of the groomed mass performance on p_T and 62 R using the understanding of the QCD mass distribution developed in Section 5.4. Conversely, the performance of 64 other substructure variables, such as $C_2^{\beta=1}$ and $\tau_{21}^{\beta=1}$, is more susceptible to changes in radius, with background rejection power decreasing with increasing R. This is due to the in-167 herent sensitivity of these observables to soft, wide anglass radiation.

The best two-variable performance is obtained by combining a groomed mass with a substructure variable. Which particular substructure variable works best in combination strongly depends on p_T and R. $C_2^{\beta=1}$ offers significant complementarity to groomed mass at smaller R, owing to the small degree of correlation between the variables. However, the sensitivity of $C_2^{\beta=1}$ to soft, wide-angle radiation leads to worse discrimination power at large R, where $\tau_{21}^{\beta=1}$ performs better in combination. Our studies also demonstrate the potential for enhancing discrimination by combining groomed and ungroomed mass information, although the use of ungroomed mass in this may be limited in practice by the presence of pile-up that is not considered in these studies.

By examining the performance of a BDT combination of all variables considered, it is clear that there are potentially substantial performance gains to be made by designing

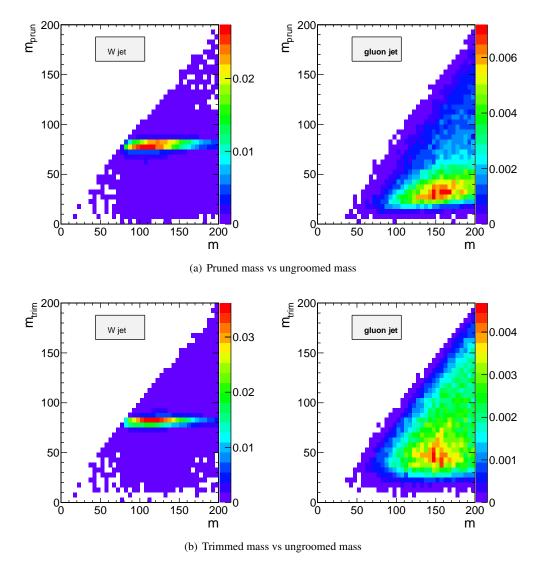


Fig. 27 2-D histograms of groomed mass versus ungroomed mass in the $p_T = 1.0$ -1.1 TeV bin using the anti- $k_T R = 1.2$ algorithm, shown separately for signal and background.

a more complex multivariate W tagger, especially at higher 84 1171 p_T .

7 Top Tagging

In this section, we investigate the identification of boosted top quarks using jet substructure. Boosted top quarks resultso in large-radius jets with complex substructure, containing as b-subjet and a boosted W. The additional kinematic handlesso coming from the reconstruction of the W mass and b-taggings allow a very high degree of discrimination of top quark jetsso from QCD backgrounds relative to W tagging. As a consesso quence of the many kinematic differences between top and QCD jets, top taggers are typically complex, with a couplasso finput parameters necessary for any given algorithm. Was study the variation in performance of top tagging techniquesso

with respect to jet p_T and R, re-optimizing the tagger inputs for each different kinematic range and jet radius considered. We also investigate the effects of combining dedicated top tagging algorithms with other jet substructure observables, giving insight into the correlations among top-tagging observables.

We use the top quark MC samples for each bin described in Section 2.2. The analysis relies on FASTJET 3.0.3 for jet clustering and calculation of jet substructure observables. Jets are clustered using the anti- k_T algorithm, and only the leading jet is used in each analysis. An upper and lower p_T cut are applied after jet clustering to each sample to ensure similar p_T spectra in each bin. The bins in leading jet p_T for top tagging are 600-700 GeV, 1-1.1 TeV, and 1.5-1.6 TeV. Jets are clustered with radii R = 0.4, 0.8, and 1.2; R = 0.4 jets are only studied in the 1.5-1.6 TeV bin because the top

1201

1202

1203

1204

1205

1206

1207

1208

1209

1210

1211

1213

1214

1215

1216

1217

1218

1219

1220

1222

1223

1224

1225

1226

1227

1228

1229

1230

1231

1233

1234

1235

1236

1238

1239

1240

1241

1242

1244

1245

1246 1247

1248

decay products are all contained within an R = 0.4 jet for for formula R = 0.4 jet for formula R = 0.4 jet for Rtop quarks with this boost.

7.1 Methodology

We study a number of top-tagging strategies, which can b_e^{1253} divided into two distinct categories. In the first category are dedicated top-tagging algorithms, which aim to directly re-255 construct the top and W candidates in the top decay. In particular, we study: 1258

- 1. HEPTopTagger
- 2. Johns Hopkins Tagger (JH)
- 3. Trimming with W-identification
- 4. Pruning with W-identification

as described in Section 3.3. The top mass, m_t , is the mass₆₃ of the groomed jet. All of the above taggers and groomers, incorporate a step to remove contributions from the under 265 lying event and other soft radiation.

In the second category are individual jet substructure ob $_{267}$ servables that are sensitive to the radiation pattern within the jet, which we refer to as "jet-shape observables". While the most sensitive top-tagging observables are typically sensized tive to three-pronged radiation, we also consider observables, 71 sensitive to two-pronged radiation in the limit where the W_{272} is very boosted and its subjets overlap. The observables weconsider are:

- The ungroomed jet mass.
- N-subjettiness ratios $\tau_{21} \equiv \tau_2/\tau_1$ and $\tau_{32} \equiv \tau_3/\tau_2$ with τ_{76} $\beta = 1$ and the "winner-takes-all" axes.
- 2-point energy correlation function ratios $C_2^{\beta=1}$ and $C_3^{\beta=\frac{1}{2}78}$.
- The pruned Qjet mass volatility, Γ_{Oiet} .

Several of these observables were also considered earlier for^{280} q/g-tagging and W-tagging.

To study the correlation among the above top-tagging 1282 methods with the shape observables. For multivariate analy-1284 ses, we combine the relevant tagger output observables and/or jet shapes into a BDT. Additionally, because each tagger has 1286 two input parameters (as described in Section 3.3), we scan 287 over reasonable values of the input parameters to determine 1288 the optimal value that gives the largest background rejection 1286 for each top tagging signal efficiency. This allows a direct²⁹⁰ comparison of the optimized version of each tagger. The in 1291 put values scanned for the various algorithms are:

- 1293 **– HEPTopTagger:** $m \in [30, 100]$ GeV, $\mu \in [0.5, 1]$ **JH Tagger:** $\delta_p \in [0.02, 0.15], \delta_R \in [0.07, 0.2]$ 1295 **Trimming:** $f_{\text{cut}} \in [0.02, 0.14], R_{\text{trim}} \in [0.1, 0.5]$ **– Pruning:** $z_{\text{cut}} \in [0.02, 0.14], R_{\text{cut}} \in [0.1, 0.6]$
- We also investigate the degradation in performance of the 98 top-tagging observables when moving away from the opti299 mal parameter choice.

7.2 Single-Observable Performance

1251

1252

1259

1260

1261

We begin by investigating the behaviour of individual jet substructure observables. Because of the rich, three-pronged structure of the top decay, it is expected that combinations of masses and jet shapes will far outperform single observables in identifying boosted tops. However, a study of the toptagging performance of single variables facilitates a direct comparison with the W tagging results in Section 6, and also allows a straightforward examination of the performance of each observable for different p_T and jet radius.

Top-tagging observable performance is quantified using ROC curves. Fig. 28 shows the ROC curves for each of the top-tagging observables, with the bare (ungroomed) jet mass also plotted for comparison. The jet-shape observables all perform substantially worse than jet mass; this is in contrast with W tagging, for which several observables are competitive with or perform better than jet mass (see, for example, Fig. 10). To understand why this is the case, consider N-subjettiness: the W is two-pronged and the top is three-pronged, and so we expect τ_{21} and τ_{32} to be the bestperformant N-subjettiness ratio, respectively. However, a cut for small values of τ_{21} necessarily also selects for events with large τ_1 , which is strongly correlated with jet mass, up to Sudakov-suppressed contributions. Therefore, τ_{21} combines both mass and shape information to some extent. By contrast, and as is clear in Fig.28(a), the best shape for top tagging is τ_{32} , which contains no information on the jet mass. It is therefore unsurprising that the shapes most useful for top tagging are less sensitive to the jet mass, and underperform relative to the corresponding observables for W tagging.

Of the two top-tagging algorithms, it is apparent from Figure 28 that the Johns Hopkins (JH) tagger out-performs the HEPTopTagger in terms of its background rejection at observables, we consider combinations of the mass-reconstruction fixed signal efficiency for both the top and W candidate masses; this is expected, as the HEPTopTagger was designed to reconstruct moderate- p_T top jets in ttH events (for a proposal for a high- p_T variant of the HEPTopTagger, see [60]). In Figure 29, we show the histograms for the top mass output from the JH and HEPTopTagger for different R in the p_T = 1.5-1.6 TeV bin, and in Figure 30 for different p_T at at R =0.8, optimized at a signal efficiency of 30%. One can see from these figures that the likely reason for the better performance of the JH tagger is that, in the HEPTopTagger algorithm, the jet is filtered to select the five hardest subjets, and then three subjets are chosen which most closely reconstruct the top mass. This requirement tends to shape a peak in the QCD background around m_t for the HEPTop-Tagger, while the JH tagger has no such requirement. It has been suggested [61] that performance in the HEPTopTagger may be improved by selecting the three subjets reconstructing the top only among those that pass the W mass con-

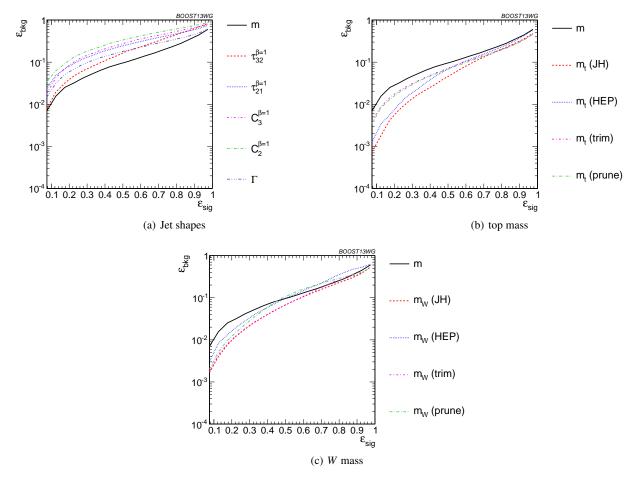


Fig. 28 Comparison of single-variable top-tagging performance in the $p_T = 1 - 1.1$ GeV bin using the anti- k_T , R=0.8 algorithm.

straints, which somewhat reduces the shaping of the back₅₂₂ ground. The discrepancy between the JH and HEPTopTag₅₂₃ gers is more pronounced at higher p_T and larger jet radius₂₄ (see Figs. 32 and 35).

1302

1303

1304

1305

1307

1309

1310

1311

1312

1314

1316

1318

1319

1320

1321

We also see in Figure 28(b) that the top mass from the²⁷ JH tagger and the HEPTopTagger has superior performance 228 relative to either of the grooming algorithms; this is because³²⁹ the pruning and trimming algorithms do not have inherente30 W-identification steps and are not optimized for this purssi pose. Indeed, because of the lack of a W-identification step332 grooming algorithms are forced to strike a balance between 333 under-grooming the jet, which broadens the signal peak due34 to underlying event contamination and features a larger back335 ground rate, and over-grooming the jet, which occasionally 36 throws out the b-jet and preserves only the W components³⁷ inside the jet. We demonstrate this effect in Figures 29 ant 38 30, showing that with 30% signal efficiency, the optimal per-339 formance of the tagger over-grooms a substantial fraction of the jets ($\sim 20-30\%$), leading to a spurious second peak⁴¹ at m_W . This effect is more pronounced at large R and $p_{T,342}$ since more aggressive grooming is required in these limits43 to combat the increased contamination from UE and QCD radiation.

In Figures 31 and 32 we directly compare ROC curves for jet-shape observable performance and top-mass performance, respectively, in three different p_T bins whilst keeping the jet radius fixed at R = 0.8. The input parameters of the taggers, groomers and shape variables are separately optimized in each p_T bin. One can see from Figure 31 that the tagging performance of jet shapes do not change substantially with p_T . The observables $\tau_{32}^{(\beta=1)}$ and Qjet volatility Γ have the most variation and tend to degrade with higher p_T , as can be seen in Figure 33. This makes sense, as higher- p_T QCD jets have more, harder emissions within the jet, giving rise to substructure that fakes the signal. By contrast, from Figure 32 we can see that most of the top-mass observables have superior performance at higher p_T due to the radiation from the top quark becoming more collimated. The notable exception is the HEPTopTagger, which degrades at higher p_T , likely in part due to the background-shaping effects studied above.

In Figures 34 and 35 we directly compare ROC curves for jet-shape observable performance and top-mass perfor-

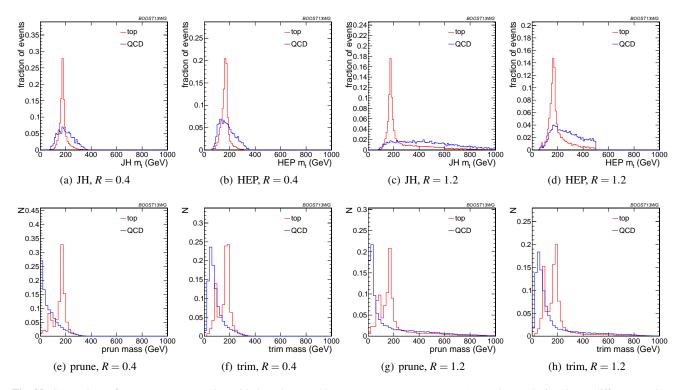


Fig. 29 Comparison of top mass reconstruction with the Johns Hopkins (JH), HEPTopTaggers (HEP), pruning, and trimming at different R using the anti- k_T algorithm, $p_T = 1.5$ -1.6 TeV. Each histogram is shown for the working point optimized for best performance with m_t in the 0.3-0.35 signal efficiency bin, and is normalized to the fraction of events passing the tagger. In this and subsequent plots, the HEPTopTagger distribution cuts off at 500 GeV because the tagger fails to tag jets with a larger mass.

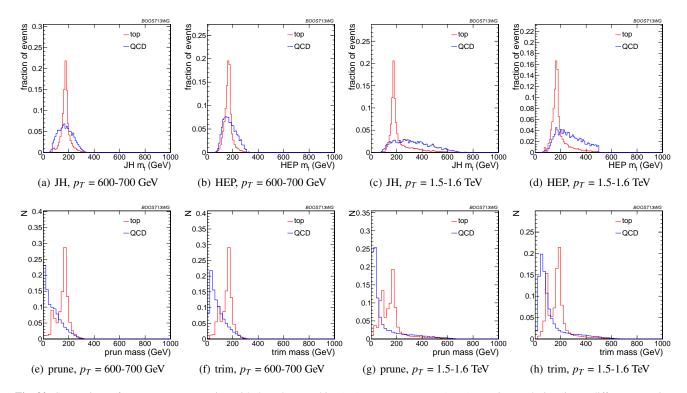


Fig. 30 Comparison of top mass reconstruction with the Johns Hopkins (JH), HEPTopTaggers (HEP), pruning, and trimming at different p_T using the anti- k_T algorithm, R = 0.8. Each histogram is shown for the working point optimized for best performance with m_t in the 0.3-0.35 signal efficiency bin, and is normalized to the fraction of events passing the tagger.

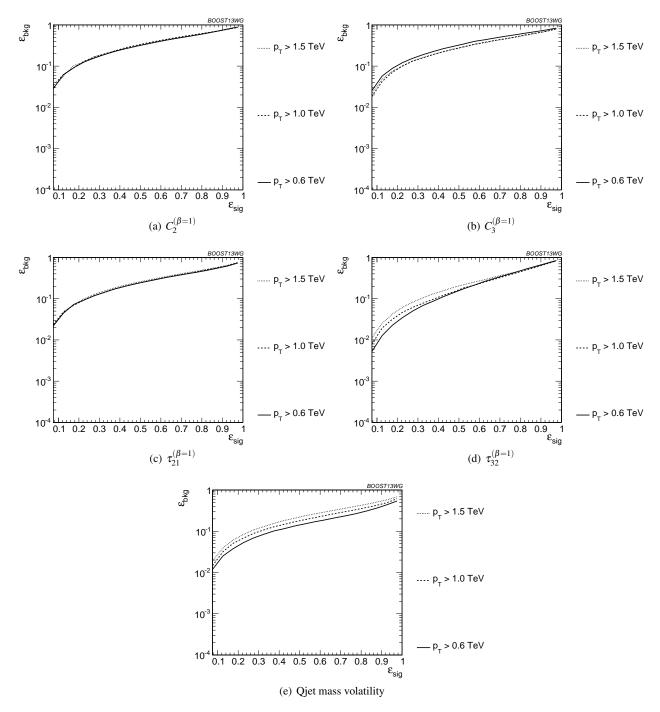


Fig. 31 Comparison of individual jet shape performance at different p_T using the anti- k_T R=0.8 algorithm.

mance, respectively, for three different jet radii within the $p_T = 1.5$ -1.6 TeV bin. Again, the input parameters of the tag 953 gers, groomers and shape variables are separately optimized for each jet radius. We can see from these figures that mos 555 of the top-tagging variables, both shape and reconstructed top mass, perform best for smaller radius. This is likely be 957 cause, at such high p_T , most of the radiation from the top 958 quark is confined within R = 0.4, and having a larger jet 559

radius makes the observable more susceptible to contamination from the underlying event and other uncorrelated radiation. In Figure 36, we compare the individual top signal and QCD background distributions for each shape variable considered in the $p_T=1.5-1.6$ TeV bin for the various jet radii. The distributions for both signal and background broaden with increasing R, degrading the discriminating power. For $C_2^{(\beta=1)}$ and $C_3^{(\beta=1)}$, the background distributions are shifted

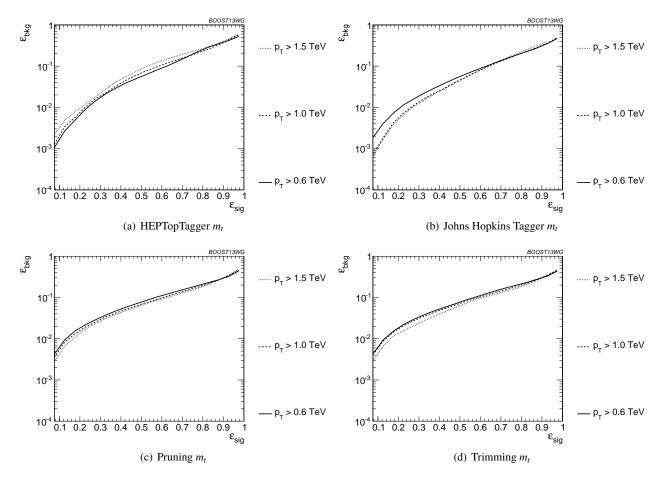


Fig. 32 Comparison of top mass performance of different taggers at different p_T using the anti- k_T R=0.8 algorithm.

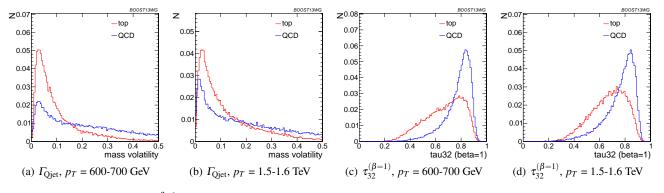


Fig. 33 Comparison of Γ_{Qjet} and $\tau_{32}^{\beta=1}$ at R=0.8 and different values of the p_T . These shape observables are the most sensitive to varying p_T .

1373

upward as well. Therefore, the discriminating power generates ally gets worse with increasing R. The main exception is for $C_3^{(\beta=1)}$, which performs optimally at R=0.8; in this case and the signal and background coincidentally happen to have the same distribution around R=0.4, and so R=0.8 gives between ter discrimination.

1363

1365

7.3 Performance of Multivariable Combinations

We now consider various BDT combinations of the observables from Section 7.2, using the techniques described in Section 4. In particular, we consider the performance of individual taggers such as the JH tagger and HEPTopTagger, which output information about the top and W candidate masses and the helicity angle; groomers, such as trimming and pruning, which remove soft, uncorrelated radiation from

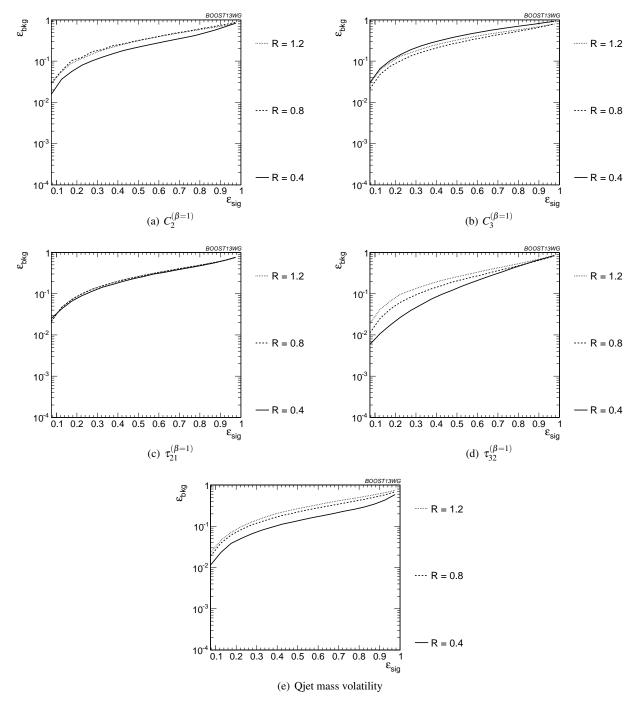


Fig. 34 Comparison of individual jet shape performance at different R in the $p_T = 1.5$ -1.6 TeV bin.

the top candidate to improve mass reconstruction, and tost which we have added a *W* reconstruction step; and the com-982 bination of the outputs of the above taggers/groomers, boths with each other, and with the shape variables. For all observe-984 ables with tuneable input parameters, we scan and optimizes over realistic values of such parameters, as described in Seq-986 tion 7.1.

In Figure 37, we directly compare the performance of the HEPTopTagger, the JH tagger, trimming, and pruning, in the $p_T = 1 - 1.1$ TeV bin with R = 0.8, where both m_t and m_W are used in the groomers. Generally, we find that pruning, which does not naturally incorporate subjets into the algorithm, does not perform as well as the others. Interestingly, trimming, which does include a subjet-identification step, performs comparably to the HEPTopTagger over much

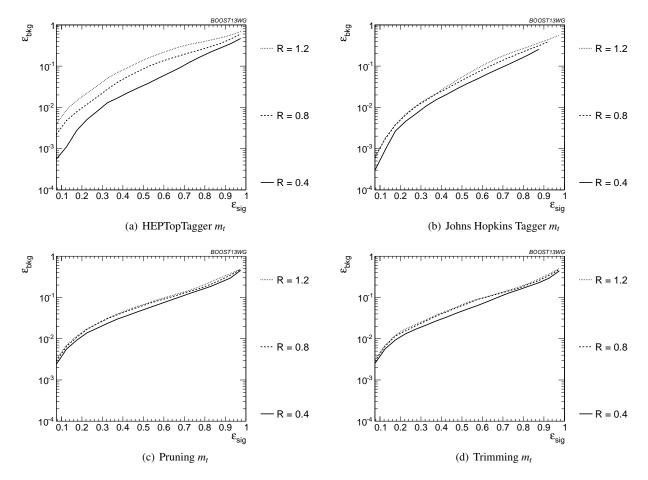


Fig. 35 Comparison of top mass performance of different taggers at different R in the $p_T = 1.5 \cdot 1.6$ TeV bin.

of the range, possibly due to the background-shaping oba11 served in Section 7.2. By contrast, the JH tagger outperforms12 the other algorithms. To determine whether there is compla113 mentary information in the mass outputs from different top114 taggers, we also consider in Figure 37 a multivariable com115 bination of all of the JH and HEPTopTagger outputs. Tha16 maximum efficiency of the combined JH and HEPTopTag417 gers is limited, as some fraction of signal events inevitabls118 fails either one or other of the taggers. We do see a 20-50%119 improvement in performance when combining all outputs420 which suggests that the different algorithms used to identifs121 the top and W for different taggers contains complementars122 information.

In Figure 38 we present the results for multivariable combinations of the top tagger outputs with and without shapsa25 variables. We see that, for both the HEPTopTagger and thsa26 JH tagger, the shape observables contain additional inforsa27 mation uncorrelated with the masses and helicity angle, and 28 give on average a factor 2-3 improvement in signal discrimisa29 nation. We see that, when combined with the tagger outputs630 both the energy correlation functions $C_2 + C_3$ and the N_{431} subjettiness ratios $\tau_{21} + \tau_{32}$ give comparable performance632

while the Qjet mass volatility is slightly worse; this is unsurprising, as Qjets accesses shape information in a more indirect way from other shape observables. Combining all shape observables with a single top tagger provides even greater enhancement in discrimination power. We directly compare the performance of the JH and HEPTopTaggers in Figure 38(c). Combining the taggers with shape information nearly erases the difference between the tagging methods observed in Figure 37; this indicates that combining the shape information with the HEPTopTagger identifies the differences between signal and background missed by the tagger alone. This also suggests that further improvement to discriminating power may be minimal, as various multivariable combinations converge to within a factor of 20% or so.

In Figure 39 we present the results for multivariable combinations of groomer outputs with and without shape variables. As with the tagging algorithms, combinations of groomers with shape observables improves their discriminating power; combinations with $\tau_{32} + \tau_{21}$ perform comparably to those with $C_3 + C_2$, and both of these are superior to combinations with the mass volatility, Γ . Substantial improvement is further possible by combining the groomers with all shape

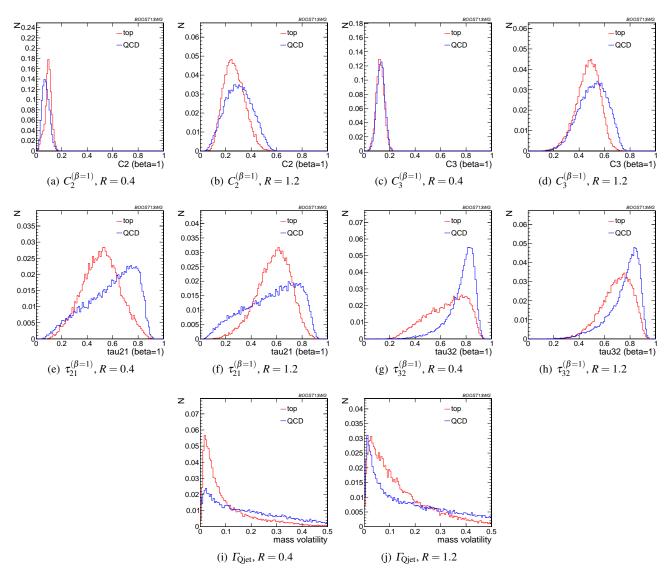


Fig. 36 Comparison of various shape observables in the $p_T = 1.5-1.6$ TeV bin and different values of the anti- k_T radius R.

observables. Not surprisingly, the taggers that lag behind48 in performance enjoy the largest gain in signal-background49 discrimination with the addition of shape observables. Oncaso again, in Figure 39(c), we find that the differences between51 pruning and trimming are erased when combined with shapa52 information.

Finally, in Figure 40, we compare the performance of $_{1456}^{4}$ each of the tagger/groomers when their outputs are com_{1457}^{4} bined with all of the shape observables considered. One can_{158}^{4} see that the discrepancies between the performance of the different taggers/groomers all but vanishes, suggesting per_{1460}^{4} haps that we are here utilising all available signal-background discrimination information, and that this is the optimal ton_{162}^{4} tagging performance that could be achieved in these conditions.

Up to this point, we have considered only the combined multivariable performance in the $p_T = 1.0$ -1.1 TeV bin with jet radius R = 0.8. We now compare the BDT combinations of tagger outputs, with and without shape variables, at different p_T . The taggers are optimized over all input parameters for each choice of p_T and signal efficiency. As with the single-variable study, we consider anti- k_T jets clustered with R = 0.8 and compare the outcomes in the $p_T = 500$ -600 GeV, $p_T = 1$ -1.1 TeV, and $p_T = 1.5$ -1.6 TeV bins. The comparison of the taggers/groomers is shown in Figure 41. The behaviour with p_T is qualitatively similar to the behaviour of the m_t observable for each tagger/groomer shown in Figure 32; this suggests that the p_T behaviour of the taggers is dominated by the top-mass reconstruction. As before, the HEPTopTagger performance degrades slightly with in-

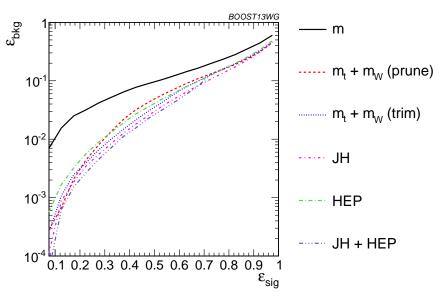


Fig. 37 The performance of the various taggers in the $p_T = 1 - 1.1$ TeV bin using the anti- k_T R=0.8 algorithm. For the groomers a BDT combination of the reconstructed m_t and m_W are used. Also shown is a multivariable combination of all of the JH and HEPTopTagger outputs. The ungroomed mass performance is shown for comparison.

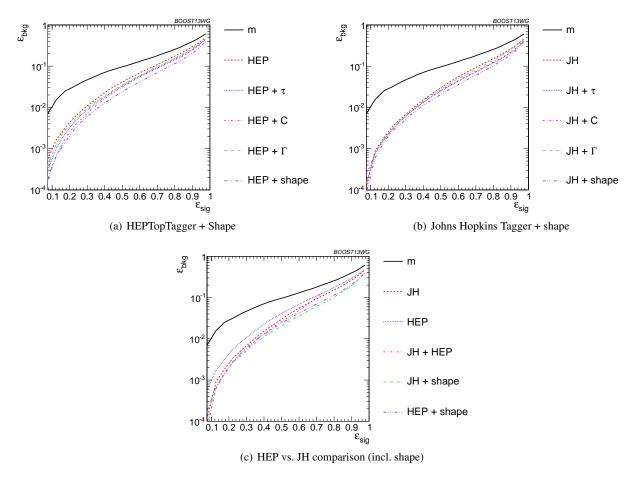


Fig. 38 The performance of BDT combinations of the JH and HepTopTagger outputs with various shape observables in the $p_T = 1 - 1.1$ TeV bin using the anti- k_T R = 0.8 algorithm. Taggers are combined with the following shape observables: $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$, $C_2^{(\beta=1)} + C_3^{(\beta=1)}$, Γ_{Qjet} , and all of the above (denoted "shape").

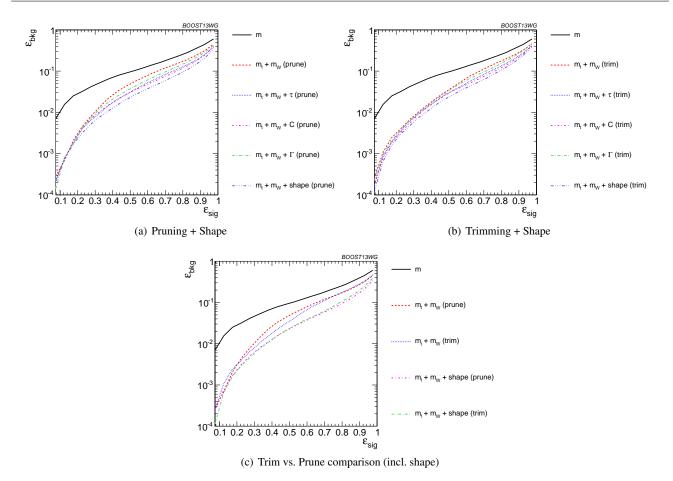


Fig. 39 The performance of the BDT combinations of the trimming and pruning outputs with various shape observables in the $p_T = 1 - 1.1$ TeV bin using the anti- k_T R = 0.8 algorithm. Groomer mass outputs are combined with the following shape observables: $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)} + C_3^{(\beta=1)} + C_3^{(\beta=1)}$, Γ_{Qjet} , and all of the above (denoted "shape").

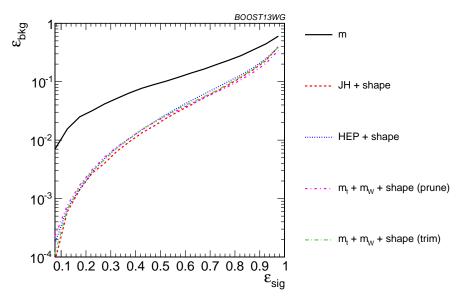


Fig. 40 Comparison of the performance of the BDT combinations of all the groomer/tagger outputs with all the available shape observables in the $p_T=1-1.1$ TeV bin using the anti- k_T R=0.8 algorithm. Tagger/groomer outputs are combined with all of the following shape observables: $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$, $C_2^{(\beta=1)} + C_3^{(\beta=1)}$, Γ_{Qjet} .

1464

1465

1466

1467

1468

1470

1471

1472

1473

1474

1475

1476

1478

1479

1480

1481

1482

1483

1484

1486

1487

1488

1490

1491

1492

1493

1495

1496

1497

1499

1500

1501

1502

1504

1505

1506

1508

1509

1510

1511

creased p_T due to the background shaping effect, while the 12 JH tagger and groomers modestly improve in performance 1513

In Figure 42, we show the p_T -dependence of BDT com⁵¹⁴ binations of the JH tagger output combined with shape ob515 servables. We find that the curves look nearly identical: the 16 p_T dependence is again dominated by the top-mass recon⁵¹⁷ struction, and combining the tagger outputs with different18 shape observables does not substantially change this behav-519 ior. The same holds true for trimming and pruning. By con⁵²⁰ trast, HEPTopTagger ROC curves, shown in Figure 43, do²¹ change somewhat when combined with different shape ob522 servables; due to the suboptimal performance of the HEP523 TopTagger at high p_T , we find that combining the HER524 TopTagger with $C_3^{(\hat{\beta}=1)}$, which in Figure 31(b) is seen tb⁵²⁵ have some modest improvement at high p_T , can improve its 26 performance. Combining the HEPTopTagger with multiple²⁷ shape observables gives the maximum improvement in pet528 formance at high p_T relative to at low p_T .

In Figure 44 we compare the BDT combinations of tag-1531 ger outputs, with and without shape variables, at different sales jet radius R in the $p_T = 1.5 - 1.6$ TeV bin. The taggers are optimized over all input parameters for each choice of R and 34 signal efficiency. We find that, for all taggers and groomers,535 the performance is always best at small R; the choice of R^{36} is sufficiently large to admit the full top quark decay at such 37 high p_T , but is small enough to suppress contamination from f^{38} additional radiation. This is not altered when the taggers are 39 combined with shape observables. For example, in Figure 45540 is shown the dependence on R of the JH tagger when com⁵⁴¹ bined with shape observables, where one can see that the 542 R-dependence is identical for all combinations. The same 43 holds true for the HEPTopTagger, trimming, and pruning. 1544

7.4 Performance at Sub-Optimal Working Points

Up until now, we have re-optimized our tagger and groome #550 parameters for each p_T , R, and signal efficiency working⁵¹ point. In reality, experiments will choose a finite set of work 552 ing points to use. When this is taken into account, how will 53 the top-tagging performance compare to the optimal results54 already shown? To address this concern, we replicate 04,555 analyses, but optimize the top taggers only for a single $p_T/R/\epsilon f$ same holds true for the BDT combinations of the and subsequently apply the same parameters to other sca557 narios. This allows us to determine the extent to which rassa optimization is necessary to maintain the high signal-to-backeround the optimized performance, and the HEPTopTagger perdiscrimination power seen in the top-tagging algorithms was studied. In this section, we focus on the taggers and groomers₆₁ and their combination with shape observables, as the shape 62 observables alone typically do not have any input paramesos ters to optimize.

Optimizing at a single p_T: We show in Figure 46 the performance of the reconstructed top mass for the $p_T = 0.6$ -0.7 TeV and $p_T = 1.0-1.1$ TeV bins, with all input parameters optimized to the $p_T = 1.5$ -1.6 TeV bin (and R = 0.8throughout). This is normalized to the performance using the optimized tagger inputs at each p_T . While the performance degrades by about 50% when the high- p_T optimized inputs are used at other momenta, this is only an order-one adjustment of the tagger performance, with trimming and the Johns Hopkins tagger degrading the most. The jagged behaviour of the points is due to the finite resolution of the scan. We also observe a particular effect associated with using suboptimal taggers: since taggers sometimes fail to return a top candidate, parameters optimized for a particular signal efficiency ε_{sig} at $p_T = 1.5\text{-}1.6$ TeV may not return enough signal candidates to reach the same efficiency at a different p_T . Consequently, no point appears for that p_T value. This is not often a practical concern, as the largest gains in signal discrimination and significance are for smaller values of $\varepsilon_{\rm sig}$, but it may be an important effect to consider when selecting benchmark tagger parameters and signal efficiencies.

The degradation in performance is more pronounced for the BDT combinations of the full tagger outputs, shown in Figure 47). This is true particularly at very low signal efficiency, where the optimization of inputs picks out a cut on the tail of some distribution that depends precisely on the p_T/R of the jet. Once again, trimming and the Johns Hopkins tagger degrade more markedly. Similar behavior holds for the BDT combinations of tagger outputs plus all shape observables.

Optimizing at a single R: In Figure 48, we show the performance of the reconstructed top mass for R = 0.4 and 0.8, with all input parameters optimized to R = 1.2 TeV bin (and $p_T = 1.5 - 1.6$ TeV throughout). This is normalized to the performance using the optimized tagger inputs at each R. While the performance of each observable degrades at small $\varepsilon_{\rm sig}$ compared to the optimized search, the HEPTopTagger fares the worst as the observed is quite sensitive to the selected value of R. It is not surprising that a tagger whose top mass reconstruction is susceptible to background-shaping at large R and p_T would require a more careful optimization of parameters to obtain the best performance.

1547

full tagger outputs, shown in Figure 49). The performance for the sub-optimal taggers is still within an O(1) factor forms better with the combination of all of its outputs relative to the performance with just m_t . The same behaviour holds for the BDT combinations of tagger outputs and shape observables.

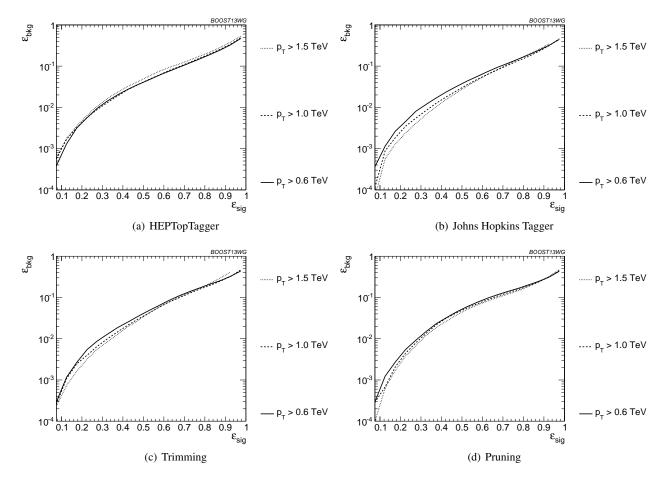


Fig. 41 Comparison of BDT combination of tagger performance at different p_T using the anti- k_T R = 0.8 algorithm.

Optimizing at a single efficiency: The strongest assumpsst tion we have made so far is that the taggers can be re-optimized for each signal efficiency point. This is useful for making asso direct comparison of the power of different top-tagging algorithms, but is not particularly practical for LHC analyses. We now consider the scenario in which the tagger inputs are optimized once, in the $\varepsilon_{\rm sig}=0.3$ -0.35 bin, and then used for all signal efficiencies. We do this in the $p_T=1.0$ -1.1 TeV bit 191 and with R=0.8.

1565

1566

1569

1571

1572

1573

1574

1575

1576

1577

1579

1581

1583

1584

1585

1586

The performance of each tagger, normalized to its person formance optimized in each signal efficiency bin, is showned in Figure 50 for cuts on the top mass and W mass, and in Figson ure 51 for BDT combinations of tagger outputs and shaped variables. In both plots, it is apparent that optimizing theod taggers in the $\varepsilon_{\rm sig} = 0.3$ -0.35 efficiency bin gives comparationable performance over efficiencies ranging from 0.2-0.5, also though performance degrades at substantially different signon nal efficiencies. Pruning appears to give especially robusto signal-background discrimination without re-optimization most likely due to the fact that there are no absolute discontance or p_T scales that appear in the algorithm. Figures 500 and 51 suggest that, while optimization at all signal efficiencos

cies is a useful tool for comparing different algorithms, it is not crucial to achieve good top-tagging performance in experiments.

7.5 Conclusions

We have studied the performance of various jet substructure observables, groomed masses, and top taggers to study the performance of top tagging with different p_T and jet radius parameters. At each p_T , R, and signal efficiency working point, we optimize the parameters for those observables with tuneable inputs. Overall, we have found that these techniques, individually and in combination, continue to perform well at high p_T , which is important for future LHC running. In general, the John Hopkins tagger performs best, while jet grooming algorithms under-perform relative to the best top taggers due to the lack of an optimized W-identification step; as expected from its design, the HEPTopTagger performance degrades at high p_T . Tagger performance can be improved by a further factor of 2-4 through combination with jet substructure observables such as τ_{32} , C_3 , and Γ_{Oiet} ; when combined with jet substructure observables, the per-

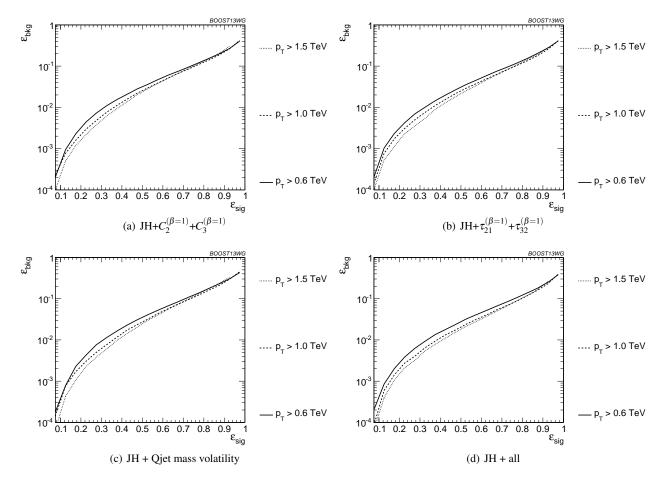


Fig. 42 Comparison of BDT combination of JH tagger + shape at different p_T using the anti- k_T R = 0.8 algorithm.

formance of various groomers and taggers becomes very628 comparable, suggesting that, taken together, the observables29 studied are sensitive to nearly all of the physical differences300 between top and QCD jets at particle-level. A small im 631 provement is also found by combining the Johns Hopkins32 and HEPTopTaggers, indicating that different taggers are no 633 fully correlated. The degree to which these findings continue to hold under more realistic pile-up and detector configura 635 tions is, however, not addressed in this analysis and left to 636 future study.

Comparing results at different p_T and R, top-tagging per₁₆₄₀ formance is generally better at smaller R due to less contam₁₆₄₁ ination from uncorrelated radiation. Similarly, most observ₁₆₄₂ ables perform better at larger p_T due to the higher degree of collimation of radiation. Some observables fare worse at higher p_T , such as the N-subjettiness ratio τ_{32} and th₁₆₄₃ Qjet mass volatility $\Gamma_{\rm Qjet}$, as higher- p_T QCD jets have more, harder emissions that fake the top-jet substructure. The HER₆₄₄ TopTagger is also worse at large p_T due to the tendency of the tagger to shape backgrounds around the top mass. Th₁₆₄₆ p_T - and R-dependence of the multivariable combinations is r_{1647}

dominated by the p_T - and R-dependence of the top mass reconstruction component of the tagger/groomer.

Finally, we consider the performance of various observable combinations under the more realistic assumption that the input parameters are only optimized at a single p_T , R, or signal efficiency, and then the same inputs are used at other working points. Remarkably, the performance of all observables is typically within a factor of 2 of the fully optimized inputs, suggesting that while optimization can lead to substantial gains in performance, the general behavior found in the fully optimized analyses extends to more general applications of each variable. In particular, the performance of pruning typically varies the least when comparing suboptimal working points to the fully optimized tagger due to the scale-invariant nature of the pruning algorithm.

8 Summary & Conclusions

Furthering our understanding of jet substructure is crucial to improving our understanding of QCD and enhancing the prospects for the discovery of new physical processes at Run II of the LHC. In this report we have studied the perfor-

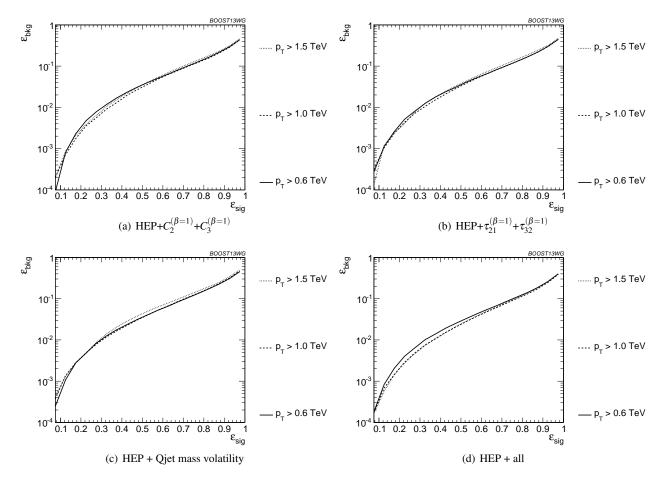


Fig. 43 Comparison of BDT combination of HEP tagger + shape at different p_T using the anti- k_T R = 0.8 algorithm.

mance of jet substructure techniques over a wide range of rokinematic regimes that will be encountered in Run II of the LHC. The performance of observables and their correlations, have been studied by combining the variables into Boosted, and Decision Tree (BDT) discriminants, and comparing the backery ground rejection power of this discriminant to the rejection power achieved by the individual variables. The performance of "all variables" BDT discriminants has also been investing gated, to understand the potential of the "ultimate" taggeters where "all" available particle-level information (at least, all of that provided by the variables considered) is used.

1649

1651

1652

1653

1656

1657

1658

1659

1660

1661

1662

1664

1666

1667

1668

1669

We focused on the discrimination of quark jets from gluon jets, and the discrimination of boosted W bosons and top quarks from the QCD backgrounds. For each, we have identified the best-performing jet substructure observables, both individually and in combination with other observables. In doing so, we have also provided a physical picture of why certain sets of observables are (un)correlated. Additionally, we have investigated how the performance of jet substructions that are particularly robust against or susceptible to these changes. In the case of q/g tagging, it seems that the

ideal performance can be nearly achieved by combining the most powerful discriminant, the number of constituents of a jet, with just one other variable, $C_1^{\beta=1}$ (or $\tau_1^{\beta=1}$). Many of the other variables considered are highly correlated and provide little additional discrimination. For both top and W tagging, the groomed mass is a very important discriminating variable, but one that can be substantially improved in combination with other variables. There is clearly a rich and complex relationship between the variables considered for W and top tagging, and the performance and correlations between these variables can change considerably with changing jet p_T and R. In the case of W tagging, even after combining groomed mass with two other substructure observables, we are still some way short of the ultimate tagger performance, indicating the complexity of the information available, and the complementarity between the observables considered. In the case of top tagging, we have shown that the performance of both the John Hopkins and HEPTopTagger can be improved when their outputs are combined with substructure observables such as τ_{32} and C_3 , and that the performance of a discriminant built from groomed mass information plus substructure observables is very comparable to the performance

1693

1696

1698

1700

1701

1703

1705

1706

1707

1710

1711

1712

1713

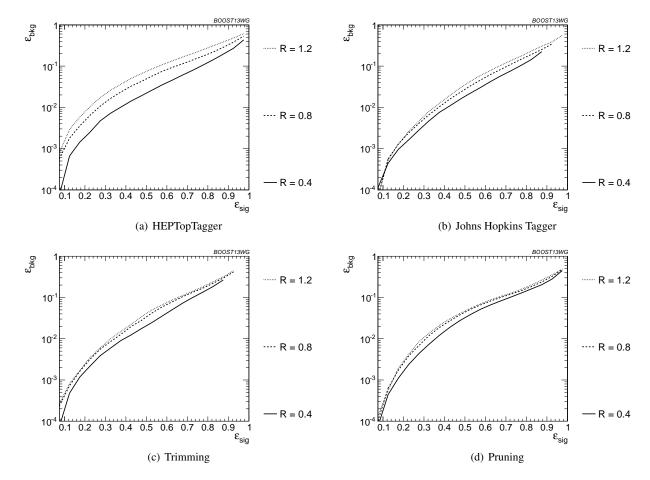


Fig. 44 Comparison of tagger and jet shape performance at different radius at $p_T = 1.5-1.6$ TeV.

of the taggers. We have optimized the top taggers for partia₇₁₄ ular values of p_T , R, and signal efficiency, and studied their₁₅ performance at other working points. We have found that₁₆ the performance of observables remains within a factor of₁₇ two of the optimized value, suggesting that the performance₁₈ of jet substructure observables is not significantly degraded when tagger parameters are only optimized for a few select benchmark points.

Our analyses were performed with ideal detector and pile-up conditions in order to most clearly elucidate the underlying physical scaling with p_T and R. At higher boosts, detector resolution effects will become more important, and with the higher pile-up expected at Run II of the LHC, pile-up mitigation will be crucial for future jet substructure studies. Future studies will be needed to determine which of the observables we have studied are most robust against pile-up and detector effects, and our analyses suggest particularly useful combinations of observables to consider in such studies.

At the new energy frontier of Run II of the LHC, boosted jet substructure techniques will be more central to our searches for new physics than ever before. By achieving a deeper un-733

derstanding of the underlying structure of quark, gluon, W and top-initiated jets, as well as the relations between observables sensitive to their respective structures, it is hoped that more sophisticated taggers can be commissioned that will maximally extend the reach for new physics.

References

- Boost2009, SLAC National Accelerator Laboratory, 9-10 July, 2009,
- [http://www-conf.slac.stanford.edu/Boost2009].

 2. Boost2010, University of Oxford, 22-25 June 2010,
- 2. Boost2010, University of Oxford, 22-25 June 2010, [http://www.physics.ox.ac.uk/boost2010].
- Boost2011, Princeton University, 22-26 May 2011, [https://indico.cern.ch/event/138809/].
- 4. Boost2012, IFIC Valencia, 23-27 July 2012, [http://ific.uv.es/boost2012].
- 5. Boost2013, University of Arizona, 12-16 August 2013, [https://indico.cern.ch/event/215704/].
- 6. *Boost2014*, University College London, 18-22 August 2014,

[http://http://www.hep.ucl.ac.uk/boost2014/].

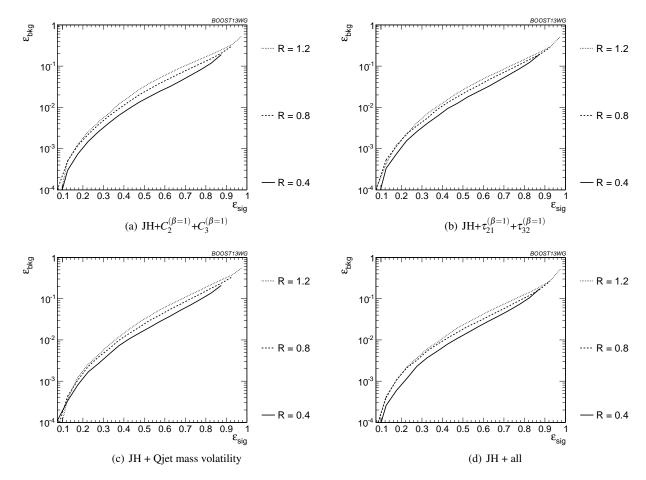


Fig. 45 Comparison of BDT combination of JH tagger + shape at different radius at $p_T = 1.5-1.6$ TeV.

7. A. Abdesselam, E. B. Kuutmann, U. Bitenc, 1756
G. Brooijmans, J. Butterworth, et al., Boosted objects:1757
A Probe of beyond the Standard Model physics, 1758
Eur.Phys.J. C71 (2011) 1661, [arXiv:1012.5412]. 1759

1735

1737

1739

1742

1743

1744

1746

1747

1748

1749

1751

1753

1754

1755

- 8. A. Altheimer, S. Arora, L. Asquith, G. Brooijmans,
 J. Butterworth, et al., *Jet Substructure at the Tevatron* 1761

 and LHC: New results, new tools, new benchmarks,
 J.Phys. G39 (2012) 063001, [arXiv:1201.0008].
- 9. A. Altheimer, A. Arce, L. Asquith, J. Backus Mayes, 1764 E. Bergeaas Kuutmann, et al., *Boosted objects and jet* 1765 substructure at the LHC, arXiv:1311.2708.
- 10. T. Plehn, M. Spannowsky, M. Takeuchi, and D. Zerwas, *Stop Reconstruction with Tagged Tops*, *JHEP* **1010** (2010) 078, [arXiv:1006.2833].
- JHEP 1010 (2010) 078, [arXiv:1006.2833].
 11. D. E. Kaplan, K. Rehermann, M. D. Schwartz, and
 B. Tweedie, Top Tagging: A Method for Identifying
 Boosted Hadronically Decaying Top Quarks,
 Phys.Rev.Lett. 101 (2008) 142001,
 [arXiv:0806.0848].
- 12. J. Alwall, M. Herquet, F. Maltoni, O. Mattelaer, and T. Stelzer, *MadGraph 5 : Going Beyond*, *JHEP* **1106** 1776 (2011) 128, [arXiv:1106.0522].

- Y. Gao, A. V. Gritsan, Z. Guo, K. Melnikov,
 M. Schulze, et al., Spin determination of single-produced resonances at hadron colliders, Phys. Rev. D81 (2010) 075022, [arXiv:1001.3396].
- S. Bolognesi, Y. Gao, A. V. Gritsan, K. Melnikov, M. Schulze, et al., On the spin and parity of a single-produced resonance at the LHC, Phys.Rev. D86 (2012) 095031, [arXiv:1208.4018].
- 15. I. Anderson, S. Bolognesi, F. Caola, Y. Gao, A. V. Gritsan, et al., *Constraining anomalous HVV interactions at proton and lepton colliders*, *Phys.Rev.* **D89** (2014) 035007, [arXiv:1309.4819].
- J. Pumplin, D. Stump, J. Huston, H. Lai, P. M. Nadolsky, et al., New generation of parton distributions with uncertainties from global QCD analysis, JHEP 0207 (2002) 012, [hep-ph/0201195].
- 17. T. Sjostrand, S. Mrenna, and P. Z. Skands, A Brief Introduction to PYTHIA 8.1, Comput. Phys. Commun. 178 (2008) 852–867, [arXiv:0710.3820].
- 18. A. Buckley, J. Butterworth, S. Gieseke, D. Grellscheid, S. Hoche, et al., *General-purpose event generators for LHC physics*, *Phys.Rept.* **504** (2011) 145–233,

1779

1780

1781

1783

1784

1785

1787

1788

1789

1790

1792

1793

1794

1797

1799

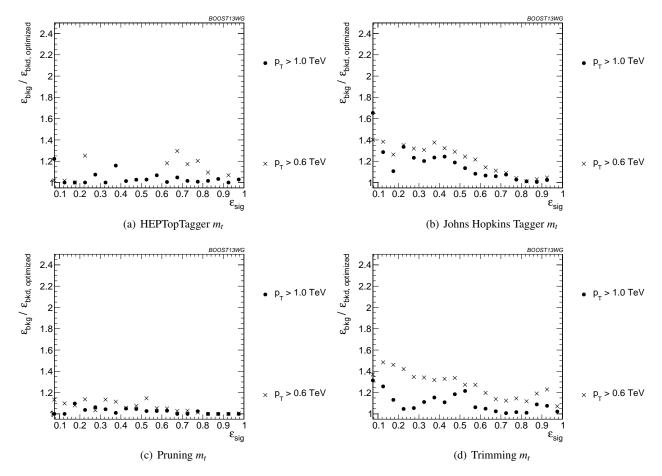


Fig. 46 Comparison of top mass performance of different taggers at different p_T using the anti- k_T R = 0.8 algorithm; the tagger inputs are set to the optimum value for $p_T = 1.5-1.6$ TeV.

1806

1807

1811

1812

[arXiv:1101.2599]. 1800 19. T. Gleisberg, S. Hoeche, F. Krauss, M. Schonherr, 1 801 S. Schumann, et al., Event generation with SHERPA 1.1, JHEP **0902** (2009) 007, [arXiv:0811.4622]. 1803 20. S. Schumann and F. Krauss, A Parton shower 1 804 algorithm based on Catani-Seymour dipole 1805 factorisation, JHEP 0803 (2008) 038,

[arXiv:0709.1027].

- 21. F. Krauss, R. Kuhn, and G. Soff, AMEGIC++ 1.0: A 1808 Matrix element generator in C++, JHEP **0202** (2002)₁₈₀₉ 044, [hep-ph/0109036].1810
- 22. T. Gleisberg and S. Hoeche, Comix, a new matrix element generator, JHEP 0812 (2008) 039, [arXiv:0808.3674].
- 23. S. Hoeche, F. Krauss, S. Schumann, and F. Siegert, 1814 QCD matrix elements and truncated showers, JHEP 1815 **0905** (2009) 053, [arXiv:0903.1219]. 1816
- 24. M. Schonherr and F. Krauss, Soft Photon Radiation in 1817 Particle Decays in SHERPA, JHEP 0812 (2008) 018, 1818 [arXiv:0810.5071].
- 25. JADE Collaboration Collaboration, S. Bethke et al., 1820 Experimental Investigation of the Energy Dependence 1821

- of the Strong Coupling Strength, Phys.Lett. B213 (1988) 235.
- 26. M. Cacciari, G. P. Salam, and G. Soyez, *The Anti-k(t)* jet clustering algorithm, JHEP 0804 (2008) 063, [arXiv:0802.1189].
- 27. Y. L. Dokshitzer, G. Leder, S. Moretti, and B. Webber, Better jet clustering algorithms, JHEP 9708 (1997) 001, [hep-ph/9707323].
- 28. M. Wobisch and T. Wengler, Hadronization corrections to jet cross-sections in deep inelastic scattering, hep-ph/9907280.
- 29. S. Catani, Y. L. Dokshitzer, M. Seymour, and B. Webber, Longitudinally invariant K_t clustering algorithms for hadron hadron collisions, Nucl. Phys. **B406** (1993) 187-224.
- 30. S. D. Ellis and D. E. Soper, Successive combination jet algorithm for hadron collisions, Phys.Rev. **D48** (1993) 3160-3166, [hep-ph/9305266].
- 31. S. D. Ellis, A. Hornig, T. S. Roy, D. Krohn, and M. D. Schwartz, Qjets: A Non-Deterministic Approach to Tree-Based Jet Substructure, Phys.Rev.Lett. 108 (2012) 182003, [arXiv:1201.1914].

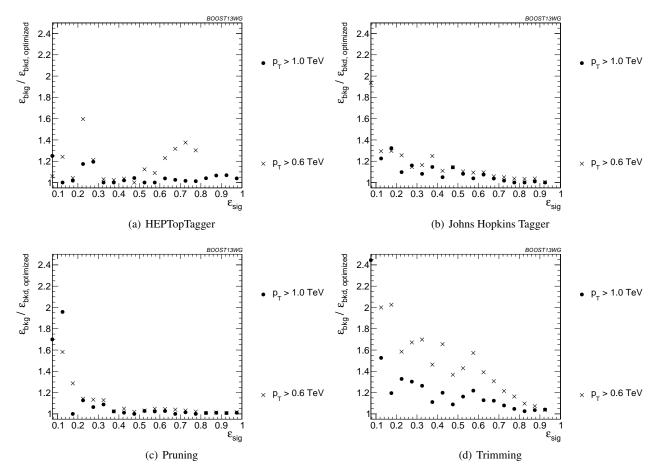


Fig. 47 Comparison of BDT combination of tagger performance at different p_T using the anti- k_T R = 0.8 algorithm; the tagger inputs are set to the optimum value for $p_T = 1.5 \cdot 1.6$ TeV.

32. S. D. Ellis, A. Hornig, D. Krohn, and T. S. Roy, *On*Statistical Aspects of Qjets, JHEP **1501** (2015) 022,

[arXiv:1409.6785].

1825

1826

1827

1828

1829

1831

1832

1833

1836

1837

1838

1840

- 33. S. D. Ellis, C. K. Vermilion, and J. R. Walsh,

 Recombination Algorithms and Jet Substructure:

 Pruning as a Tool for Heavy Particle Searches,

 Phys.Rev. **D81** (2010) 094023, [arXiv:0912.0033]. 1850
- 34. D. Krohn, J. Thaler, and L.-T. Wang, *Jet Trimming*, 1851 *JHEP* **1002** (2010) 084, [arXiv:0912.1342]. 1852
- 35. J. M. Butterworth, A. R. Davison, M. Rubin, and G. P1853 Salam, Jet substructure as a new Higgs search channel at the LHC, Phys.Rev.Lett. 100 (2008) 242001, [arXiv:0802.2470]. 1856
- 36. A. J. Larkoski, S. Marzani, G. Soyez, and J. Thaler, Soft Drop, JHEP **1405** (2014) 146, [arXiv:1402.2657].
- 37. M. Dasgupta, A. Fregoso, S. Marzani, and G. P. Salam₈₆₀

 Towards an understanding of jet substructure, JHEP 1861

 1309 (2013) 029, [arXiv:1307.0007]. 1862
- 1841 38. CMS Collaboration, V. Khachatryan et al., Search for 1863 massive resonances in dijet systems containing jets 1864 tagged as W or Z boson decays in pp collisions at \sqrt{s} 7865

- $8\ TeV, JHEP\ 1408\ (2014)\ 173, [arXiv:1405.1994].$
- 39. **ATLAS** Collaboration, G. Aad et al., *Measurement of the cross-section of high transverse momentum vector bosons reconstructed as single jets and studies of jet substructure in pp collisions at \sqrt{s} = 7 TeV with the ATLAS detector, New J.Phys. 16 (2014), no. 11 113013, [arXiv:1407.0800].*
- Performance of Boosted W Boson Identification with the ATLAS Detector, Tech. Rep. ATL-PHYS-PUB-2014-004, CERN, Geneva, Mar, 2014.
- 41. J. Thaler and K. Van Tilburg, *Identifying Boosted Objects with N-subjettiness*, *JHEP* **1103** (2011) 015, [arXiv:1011.2268].
- 42. A. J. Larkoski, D. Neill, and J. Thaler, *Jet Shapes with the Broadening Axis*, *JHEP* **1404** (2014) 017, [arXiv:1401.2158].
- 43. A. J. Larkoski and J. Thaler, *Unsafe but Calculable:* Ratios of Angularities in Perturbative QCD, JHEP **1309** (2013) 137, [arXiv:1307.1699].
- 44. A. J. Larkoski, G. P. Salam, and J. Thaler, *Energy Correlation Functions for Jet Substructure*, *JHEP* **1306**

1867

1868

1870

1871

1872

1873

1875

1876

1877

1878

1880

1881

1882

1884

1885

1887

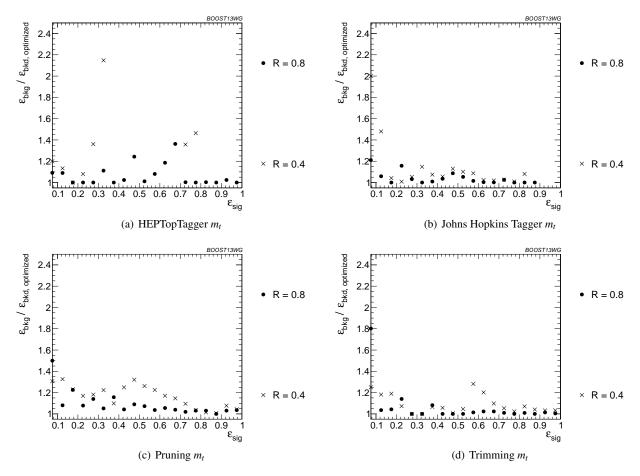


Fig. 48 Comparison of top mass performance of different taggers at different R in the $p_T = 1.5$ -1.6 TeV bin; the tagger inputs are set to the optimum value for R = 1.2.

- (2013) 108, [arXiv:1305.0007]. 1888
 45. **CMS Collaboration** Collaboration, S. Chatrchyan et al., Search for a Higgs boson in the decay channel Higgs to ZZ(*) to q qbar $\ell^ \ell^ \ell^-$ 1891
 TeV, JHEP **1204** (2012) 036, [arXiv:1202.1416]. 1892
- 46. A. J. Larkoski, J. Thaler, and W. J. Waalewijn, Gainings (Mutual) Information about Quark/Gluon
 Discrimination, JHEP 1411 (2014) 129,
 [arXiv: 1408.3122].
- 47. A. Hoecker, P. Speckmayer, J. Stelzer, J. Therhaag,
 E. von Toerne, and H. Voss, *TMVA: Toolkit for*Multivariate Data Analysis, PoS ACAT (2007) 040,
 [physics/0703039]. An example of the BDT settings900
 used in these studies are as follows: NTrees=1000;
 BoostType=Grad; Shrinkage=0.1; UseBaggedGrad=Fi902
 nCuts=10000; MaxDepth=3; UseYesNoLeaf=F;
 1903
 nEventsMin=200.
- 48. **ATLAS Collaboration** Collaboration, G. Aad et al., 1905 Light-quark and gluon jet discrimination in pp collisions at $\sqrt{s} = 7$ TeV with the ATLAS detector, Eur.Phys.J. **C74** (2014), no. 8 3023, 1908 [arXiv: 1405.6583].

- 49. J. Gallicchio and M. D. Schwartz, *Quark and Gluon Jet Substructure*, *JHEP* **1304** (2013) 090, [arXiv:1211.7038].
- 50. A. J. Larkoski, I. Moult, and D. Neill, *Toward Multi-Differential Cross Sections: Measuring Two Angularities on a Single Jet, JHEP* **1409** (2014) 046, [arXiv:1401.4458].
- 51. M. Procura, W. J. Waalewijn, and L. Zeune, Resummation of Double-Differential Cross Sections and Fully-Unintegrated Parton Distribution Functions, JHEP 1502 (2015) 117, [arXiv:1410.6483].
- 52. J. Gallicchio and M. D. Schwartz, *Quark and Gluon Tagging at the LHC*, *Phys.Rev.Lett.* **107** (2011) 172001, [arXiv:1106.3076].
- 53. **CMS Collaboration** Collaboration, C. Collaboration, *Performance of quark/gluon discrimination in 8 TeV pp data*, .
- 54. H.-n. Li, Z. Li, and C.-P. Yuan, *QCD resummation for light-particle jets*, *Phys.Rev.* **D87** (2013) 074025, [arXiv:1206.1344].
- 55. M. Dasgupta, K. Khelifa-Kerfa, S. Marzani, and M. Spannowsky, *On jet mass distributions in Z+jet and*



Fig. 49 Comparison of BDT combination of tagger performance at different radius at $p_T = 1.5$ -1.6 TeV; the tagger inputs are set to the optimum value for R = 1.2.

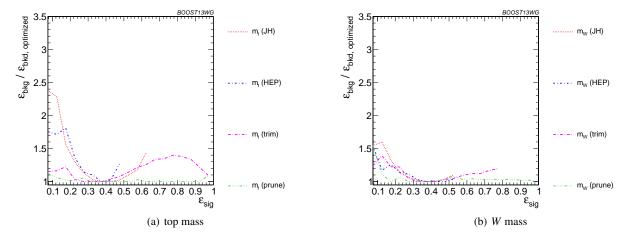


Fig. 50 Comparison of single-variable top-tagging performance in the $p_T = 1 - 1.1$ GeV bin using the anti- k_T , R = 0.8 algorithm; the inputs for each tagger are optimized for the $\varepsilon_{\text{sig}} = 0.3 - 0.35$ bin.



Fig. 51 The BDT combinations in the $p_T=1-1.1$ TeV bin using the anti- k_T R=0.8 algorithm. Taggers are combined with the following shape observables: $\tau_{21}^{(\beta=1)}+\tau_{32}^{(\beta=1)}$, $C_2^{(\beta=1)}+C_3^{(\beta=1)}$, Γ_{Qjet} , and all of the above (denoted "shape"). The inputs for each tagger are optimized for the $\varepsilon_{sig}=0.3-0.35$ bin.