Towards an Understanding of the Correlations in Jet Substructure

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1 Introduction

The characteristic feature of collisions at the LHC is a center-43 of-mass energy, 7 TeV in 2010 and 2011, of 8 TeV in 2012,44 and near 14 TeV with the start of the second phase of op-45 eration in 2015, that is large compared to even the heaviest46 10 of the known particles. Thus these particles (and also pre-47 viously unknown ones) will often be produced at the LHC₄₈ 12 with substantial boosts. As a result, when decaying hadron-49 13 ically, these particles will not be observed as multiple jets 50 in the detector, but rather as a single hadronic jet with dis-51 tinctive internal substructure. This realization has led to a52 new era of sophistication in our understanding of both stan-53 dard QCD jets and jets containing the decay of a heavy 54 particle, with an array of new jet observables and detec-55 19 tion techniques introduced and studies. To allow the effi-56 cient sharing of results from these jet substructure studies 57 a series of BOOST Workshops have been held on a yearly basis: SLAC (2009, [?]), Oxford University (2010, [?]),58 23 Princeton University University (2011, [?]), IFIC Valencia 59 (2012 [?]), University of Arizona (2013 [?]), and, most re-60 cently, University College London (2014 [?]). After each 61 26 of these meetings Working Groups have functioned during 62 the following year to generate reports highlighting the most₆₃ 28 interesting new results, including studies of ever maturing 64 details. Previous BOOST reports can be found at [???].

This report from BOOST 2013 thus views the study and 66 implementation of jet substructure techniques as a fairly ma-67 ture field, and focuses on the question of the correlations 68 between the plethora of observables that have been developed and employed, and their dependence on the underlying jet parameters, especially the jet radius R and jet p_T . Samples of quark-, gluon-, W- and Top-initiated jets are reconstructed at the particle-level using FASTJET[REF], and the performance, in terms of separating signal from background, of various groomed jet masses and jet substructure observables investigated through Receiver Operating Characteristic (ROC) curves, which show the efficiency to "tag" the signal as a function of the efficiency (or rejection, being 1/efficiency) to "tag" the background. We investigate the separation of a quark signal from a gluon background (q/g tagging), a W signal from a gluon background (W-tagging) and a Top signal from a mixed quark/gluon QCD background (Top-tagging). In the case of Top-tagging, we also investigate the performance of dedicated Top-tagging algorithms, the HepTopTagger[REF] and John Hopkins Tagger[REF]. Using multivariate techniques, we study the degree to which the discriminatory information provided by the observables and taggers overlaps, by examining in particular the extent to which the signal-background separation performance increases when two or more variables/taggers are combined, via a Boosted Decision Tree (BDT), into a single discriminant.

The report is organized as follows. In Section 2 we describe the generation of the Monte Carlo event samples that we use in the studies that follow. In Section 3 we detail the jet algorithms, observables and taggers investigated in each section of the report, and in Section 4 the multivariate techniques used to combine the one or more of the observables into single discriminants. In Section 5 we describe the q/g-tagging studies, in Section 6 we describe the W-tagging studies, and in Section 7 we describe the Top-tagging studies. Finally we offer some summary of the studies and general conclusions in Section 8.

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2 Monte Carlo Samples

In the below sections the Monte Carlo samples used in the 16 q/g tagging, W tagging and Top tagging sections of this re₁₁₇ port are described. Note that in all cases the samples used contain no additional proton-proton interactions beyond the hard scatter (no pile-up), and there is no attempt to emulate,18 the degradation in angular and p_T resolution that would re-75 sult when reconstructing the jets inside a real detector.

2.1 Quark/gluon and W tagging

Samples were generated at $\sqrt{s} = 8$ TeV for QCD dijets, and ²³ for W^+W^- pairs produced in the decay of a (pseudo) scalar¹²⁴ resonance and decaying hadronically. The QCD events were 125 split into subsamples of gg and $q\bar{q}$ events, allowing for tests¹²⁶ of discrimination of hadronic W bosons, quarks, and gluons.

Individual gg and $q\bar{q}$ samples were produced at leading order (LO) using MADGRAPH5, while W^+W^- samples were generated using the JHU GENERATOR to allow for separation of longitudinal and transverse polarizations. Both²⁷ were generated using CTEQ6L1 PDFs[REF]. The samples28 were produced in exclusive p_T bins of width 100 GeV, with 129 the slicing parameter chosen to be the p_T of any final state³⁰ parton or W at LO. At the parton-level the p_T bins inves¹³¹ tigated were 300-400 GeV, 500-600 GeV and 1.0-1.1 TeV:32 Since no matching was performed, a cut on any parton was equivalent. The samples were then all showered through PYTH (version 8.176)[REF]using the default tune 4C[REF]. ED:

Need to report the size of the samples used

2.2 Top tagging

Samples were generated at $\sqrt{s} = 14$ TeV. Standard Model₃₄ dijet and top pair samples were produced with SHERPA 2.0. QREFilt cluster sequence for the jet each time the Qjet algorithm with matrix elements of up to two extra partons matched tq36 the shower. The top samples included only hadronic decays₃₇ and were generated in exclusive p_T bins of width 100 GeV₁₃₈ taking as slicing parameter the maximum of the top/anti-top39 p_T . The QCD samples were generated with a cut on the lead₁₄₀ ing parton-level jet p_T , where parton-level jets are clustered₄₁ with the anti- k_t algorithm and jet radii of $R = 0.4, 0.8, 1.2_{142}$ The matching scale is selected to be $Q_{\rm cut} = 40,60,80 \, \text{GeV}_{143}$ for the $p_{T \min} = 600, 1000$, and 1500 GeV bins, respectively. For the top samples, 100k events were generated in each bin, while 200k QCD events were generated in each bin.

3 Jet Algorithms and Substructure Observables 110

In this section, we define the jet algorithms and observables 111 used in our analysis. Over the course of our study, we con-112 sidered a larger set of observables, but for the final analysis, 113

we eliminated redundant observables for presentation purposes. In Sections 3.1, 3.2, 3.3 and 3.4 we first describe the various jet algorithms, groomers, taggers and other substructure variables used in these studies.

3.1 Jet Clustering Algorithms

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Jet clustering: Jets were clustered using sequential jet clustering algorithms[REF]implemented in FASTJET 3.0.3. Final state particles i, j are assigned a mutual distance d_{ij} and a distance to the beam, d_{iB} . The particle pair with smallest d_{ij} are recombined and the algorithm repeated until the smallest distance is instead the distance to the beam, d_{iB} , in which case i is set aside and labelled as a jet. The distance metrics are defined as

$$d_{ij} = \min(p_{Ti}^{2\gamma}, p_{Tj}^{2\gamma}) \frac{\Delta R_{ij}^2}{R^2}, \tag{1}$$

$$d_{i\mathrm{B}} = p_{T_i}^{2\gamma},\tag{2}$$

where $\Delta R_{ij}^2 = (\Delta \eta)^2 + (\Delta \phi)^2$. In this analysis, we use the anti- k_t algorithm ($\gamma = -1$), the Cambridge/Aachen (C/A) algorithm ($\gamma = 0$)[**REF**], and the k_t algorithm ($\gamma = 1$)[**REF**], each of which has varying sensitivity to soft radiation in defining the jet.

Qjets: We also perform non-deterministic jet clustering [**REF**]. Instead of always clustering the particle pair with smallest distance d_{ij} , the pair selected for combination is chosen probabilistically according to a measure

$$P_{ij} \propto e^{-\alpha (d_{ij} - d_{\min})/d_{\min}},\tag{3}$$

where d_{\min} is the minimum distance for the usual jet clustering algorithm at a particular step. This leads to a differis used, and consequently different substructure properties. The parameter α is called the rigidity and is used to control how sharply peaked the probability distribution is around the usual, deterministic value. The Qjets method uses statistical analysis of the resulting distributions to extract more information from the jet than can be found in the usual cluster sequence. We use $\alpha = 0.1$ and 25 trees per event for all the studies presented here.

3.2 Jet Grooming Algorithms

Pruning: Given a jet, re-cluster the constituents using the C/A algorithm. At each step, proceed with the merger as usual unless both

$$\frac{\min(p_{Ti}, p_{Tj})}{p_{Tij}} < z_{\text{cut}} \text{ and } \Delta R_{ij} > \frac{2m_j}{p_{Tj}} R_{\text{cut}}, \tag{4}$$

in which case the merger is vetoed and the softer branch₇₆ discarded. The default parameters used for pruning[**REF**]in₇₇ this study are $z_{\rm cut}=0.1$ and $R_{\rm cut}=0.5$. One advantage of pruning is that the thresholds used to veto soft, wide-angle⁷⁸ radiation scale with the jet kinematics, and so the algorithm¹⁷⁹ is expected to perform comparably over a wide range of mo¹⁸⁰ menta.

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Trimming: Given a jet, re-cluster the constituents into subjets of radius R_{trim} with the k_t algorithm. Discard all subjets i with

$$p_{Ti} < f_{\text{cut}} p_{TJ}. \tag{5}$$

The default parameters used for trimming [REF] in this study, are $R_{\text{trim}} = 0.2$ and $f_{\text{cut}} = 0.03$.

Filtering:[REF] Given a jet, re-cluster the constituents \inf_{92} subjets of radius $R_{\rm filt}$ with the C/A algorithm. Re-define the jet to consist of only the hardest N subjets, where N is deter independent only the final state topology and is typically one more than the number of hard prongs in the resonance decay (td include the leading final-state gluon emission). ED: Do we actually use filtering as described here anywhere? (BS: Yes, it is used in the HEPTopTagger.)

Soft drop: Given a jet, re-cluster all of the constituents using³⁰⁰ the C/A algorithm. Iteratively undo the last stage of the C/A³⁰¹ clustering from j into subjets j_1 , j_2 . If

$$\frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} < z_{\text{cut}} \left(\frac{\Delta R_{12}}{R}\right)^{\beta}, \tag{6}$$

discard the softer subjet and repeat. Otherwise, take j to be the final soft-drop jet[REF]. Soft drop has two input parameters, the angular exponent β and the soft-drop scale $z_{\text{cut}_{209}}$ with default value $z_{\text{cut}} = 0.1$. ED: Soft-drop actually functions as a tagger when $\beta = -1$

3.3 Jet Tagging Algorithms

Modified Mass Drop Tagger: Given a jet, re-cluster all of₁₁₅ the constituents using the C/A algorithm. Iteratively und_{Q16} the last stage of the C/A clustering from j into subjets j_1 , j_{217} with $m_{j_1} > m_{j_2}$. If either

$$m_{j_1} > \mu \, m_j \text{ or } \frac{\min(p_{T1}^2, p_{T2}^2)}{m_j^2} \, \Delta R_{12}^2 < y_{\text{cut}},$$
 (7)

then discard the branch with the smaller transverse mass $_{222}$ $m_T = \sqrt{m_i^2 + p_{Ti}^2}$, and re-define j as the branch with the larger transverse mass. Otherwise, the jet is tagged. If de224 clustering continues until only one branch remains, the jet25 is untagged. In this study we use by default $\mu = 1.0$ and 250 and 250

 $y_{\rm cut} = 0.1$.

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Johns Hopkins Tagger: Re-cluster the jet using the C/A algorithm. The jet is iteratively de-clustered, and at each step the softer prong is discarded if its p_T is less than $\delta_p p_{Tiet}$. This continues until both prongs are harder than the p_T threshold, both prongs are softer than the p_T threshold, or if they are too close $(|\Delta \eta_{ij}| + |\Delta \phi_{ij}| < \delta_R)$; the jet is rejected if either of the latter conditions apply. If both are harder than the $p_{\rm T}$ threshold, the same procedure is applied to each: this results in 2, 3, or 4 subjets. If there exist 3 or 4 subjets, then the jet is accepted: the top candidate is the sum of the subjets, and W candidate is the pair of subjets closest to the W mass. The output of the tagger is m_t , m_W , and θ_h , a helicity angle defined as the angle, measured in the rest frame of the W candidate, between the top direction and one of the W decay products. The two free input parameters of the John Hopkins tagger in this study are δ_p and δ_R , defined above.

HEPTopTagger: Re-cluster the jet using the C/A algorithm. The jet is iteratively de-clustered, and at each step the softer prong is discarded if $m_1/m_{12} > \mu$ (there is not a significant mass drop). Otherwise, both prongs are kept. This continues until a prong has a mass $m_i < m$, at which point it is added to the list of subjets. Filter the jet using $R_{\rm filt} = \min(0.3, \Delta R_{ij})$, keeping the five hardest subjets (where ΔR_{ij} is the distance between the two hardest subjets). Select the three subjets whose invariant mass is closest to m_t . The output of the tagger is m_t , m_W , and θ_h , a helicity angle defined as the angle, measured in the rest frame of the W candidate, between the top direction and one of the W decay products. The two free input parameters of the HEPTopTagger in this study are m and μ , defined above.

Top Tagging with Pruning: For comparison with the other top taggers, we add a *W* reconstruction step to the trimming algorithm described above. A *W* candidate is found as follows: if there are two subjets, the highest-mass subjet is the *W* candidate (because the *W* prongs end up clustered in the same subjet); if there are three subjets, the two subjets with the smallest invariant mass comprise the *W* candidate. In the case of only one subjet, no *W* is reconstructed.

Top Tagging with Trimming: For comparison with the other top taggers, we add a W reconstruction step to the trimming algorithm described above. A W candidate is found as follows: if there are two subjets, the highest-mass subjet is the W candidate (because the W prongs end up clustered in the same subjet); if there are three subjets, the two subjets with the smallest invariant mass comprise the W candidate. In the case of only one subjet, no W is reconstructed.

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3.4 Other Jet Substructure Observables

Qjet mass volatility: As described above, Qjet algorithms₄₅ re-cluster the same jet non-deterministically to obtain a col246 lection of interpretations of the jet. For each jet interpreta₂₄₇ tion, the pruned jet mass is computed with the default prun248 ing parameters. The mass volatility, Γ_{Oiet} , is defined as

$$\Gamma_{
m Qjet} = rac{\sqrt{\langle m_J^2 \rangle - \langle m_J
angle^2}}{\langle m_J
angle},$$
 (8)51

where averages are computed over the Qjet interpretations. 253

N-subjettiness: N-subjettiness[REF] quantifies how well the radiation in the jet is aligned along N directions. To compute $_{\mathbf{256}}$ *N*-subjettiness, $\tau_N^{(\beta)}$, one must first identify *N* axes within $\tau_{257}^{(\beta)}$

$$\tau_N = \frac{1}{d_0} \sum_i p_{Ti} \min\left(\Delta R_{1i}^{\beta}, \dots, \Delta R_{Ni}^{\beta}\right),$$
(9)50

where distances are between particles i in the jet and the $_{61}$ axes.

$$d_0 = \sum_i p_{Ti} R^{\beta} \tag{10}$$

and R is the jet clustering radius. The exponent β is a free 263 parameter. There is also some choice in how the axes used to compute N-subjettiness are determined. The optimal configuration of axes is the one that minimizes N-subjettiness; recently, it was shown that the "winner-takes-all" (WTA) axes can be easily computed and have superior performance compared to other minimization techniques [REF]. We use both the WTA and one-pass k_t optimization axes in our analyses.

(11)272

A more powerful discriminant is often the ratio,

$$\tau_{N,N-1} \equiv \frac{\tau_N}{\tau_{N-1}}.$$
(11)*7

While this is not an infrared-collinear (IRC) safe observable, it is calculable [REF] and can be made IRC safe with a loose, 15 lower cut on τ_{N-1} .

Energy correlation functions: The transverse momentum₇₈ version of the energy correlation functions are defined as [REF]:

$$ECF(N, \beta) = \sum_{i_1 < i_2 < \dots < i_N \in j} \left(\prod_{a=1}^{N} p_{Ti_a} \right) \left(\prod_{b=1}^{N-1} \prod_{c=b+1}^{N} \Delta R_{i_b i_c} \right)_{\substack{280 \\ 280}}^{\beta 279},$$

$$(12)^{81}$$

where i is a particle inside the jet. It is preferable to work in terms of dimensionless quantities, particularly the energy $_{\mathbf{284}}$ correlation function double ratio:

$$C_N^{(\beta)} = \frac{\text{ECF}(N+1,\beta) \, \text{ECF}(N-1,\beta)}{\text{ECF}(N,\beta)^2}.$$
 (13)⁸⁶

This observable measures higher-order radiation from leadings order substructure.

4 Multivariate Analysis Techniques

Multivariate techniques are used to combine variables into an optimal discriminant. In all cases variables are combined using a boosted decision tree (BDT) as implemented in the TMVA package [?]. We use the BDT implementation including gradient boost. An example of the BDT settings are as follows:

- NTrees=1000
- BoostType=Grad
- Shrinkage=0.1
- UseBaggedGrad=F
- nCuts=10000
- MaxDepth=3
- UseYesNoLeaf=F
- nEventsMin=200

Exact parameter values are chosen to best reduce the effect of overtraining. ED: Can we describe a bit more the tests we do to ensure that we are not suffering from overtraining?

5 Quark-Gluon Discrimination

In this section, we examine the differences between quarkand gluon-initiated jets in terms of substructure variables, and to determine to what extent these variables are correlated. Along the way, we provide some theoretical understanding of these observables and their performance. The motivation for these studies comes not only from the desire to "tag" a jet as originating from a quark or gluon, but also to improve our understanding of the quark and gluon components of the QCD backgrounds relative to boosted resonances. While recent studies have suggested that quark/gluon tagging efficiencies depend highly on the Monte Carlo generator used[REF], we are more interested in understanding the scaling performance with p_T and R, and the correlations between observables, which are expected to be treated consistently within a single shower scheme.

5.1 Methodology

These studies use the qq and gg MC samples, described previously in Section 2. The showered events were clustered with FASTJET 3.03[REF] using the anti- $k_{\rm T}$ algorithm[REF] with jet radii of R = 0.4, 0.8, 1.2. In both signal (quark) and background (gluon) samples, an upper and lower cut on the leading jet p_T is applied after showering/clustering, to ensure similar p_T spectra for signal and background in each p_T bin. The bins in leading jet p_T that are considered are 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV, for the 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV parton p_T slices respectively. Various

jet grooming approaches are applied to the jets, as described 40 in Section 3.4. Only leading and subleading jets in each sam₃₄₁ ple are used. The following observables are studied in this42 section:

- The ungroomed jet mass, m.

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- 1-subjettiness, τ_1^{β} with $\beta = 1, 2$. The *N*-subjettiness axes are computed using one-pass k_t axis optimization.
 - 1-point energy correlation functions, $C_1^{(\beta)}$ with $\beta = 1, 2_{\frac{348}{348}}$

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- The pruned Qjet mass volatility, Γ_{Qjet} .
- The number of constituents (N_{constits}).

5.2 Single Variable Discrimination

Figure 1 shows the mass of jets in the quark and gluon sam³⁵⁴ ples when using different groomers, and the ungroomed jets mass, for jets with R=0.8 and in the $p_T = 500 - 600 \,\text{GeV}_{356}$ bin. Qualitatively, the application of grooming shifts the massisdistributions towards lower values when compared to the58 ungroomed mass, as expected. No clear gain in discrimi359 nation can be seen, and for certain grooming parameters, and such as the use of soft drop with $\beta = -1$ a clear loss in dis₃₆₁ crimination power is observed; this is because the soft-drop 62 condition for $\beta = -1$ discards collinear radiation, and the condition for $\beta = -1$ differences between quarks and gluons are manifest in the 64 collinear structure (spin, splitting functions, etc.).

The quark and gluon distributions of different substruc₃₆₆ ture variables are shown in Figure 2. Among those consid₃₆₇ ered, one can see by eye that n_{constits} provides the highes separation power, followed by $C_1^{\beta=0}$ and $C_1^{\beta=1}$, as was also so found by the CMS and ATLAS Collaborations[REF].

To more quantitatively study the power of each observ₃₇₁ able as a discriminator for quark/gluon tagging, ROC curves72 are built by scanning each distribution and plotting the back₃₇₃ ground efficiency (to select gluon jets) vs. the signal ef 374 ficiency (to select quark jets). Figure 3 shows these ROG75 curves for all of the substructure variables shown in Fig₃₇₆ ure 2, along with the ungroomed mass, representing the best-77 performing mass variable, for R=0.4, 0.8 and 1.2 jets in the78 $p_T = 300 - 400$ GeV bin. In addition, the ROC curve for are tagger built from a BDT combination of all the variables (seeso Section 4) is shown. Clearly, n_{constits} is the best performing variable for all Rs, even though $C_1^{\beta=0}$ is close, particularly for R=0.8. Most other variables have similar performance, except Γ_{Ojet} , which shows significantly worse discrimination₈₈₂ (this may be due to our choice of rigidity $\alpha = 0.1$, with other studies suggesting that a smaller value, such as $\alpha = 0.01_{383}$ produces better results[REF]). The combination of all vari384 ables shows somewhat better discrimination.

We now examine how performance of masses and sub386 structure observables changes with p_T and R. For jet masses₃₈₇ few variations are observed as the radius parameter of the jesses reconstruction is increased in the two highest p_T bins; this p_T bins; this p_T bins; this p_T bins; this p_T bins p_T is because the radiation is more collimated and the dependence on R is consequently smaller. However, for the 300 – 400 GeV bin, the use of small-R jets produces a shift in the mass distributions towards lower values, so that large-R jet masses are more stable with p_T and small-R jet masses are smaller at low- p_T as expected from the spatial constraints imposed by the R parameter. These statements are explored more quantitatively later in this section. (BS: Do we have plots for this?)

The evolution of some of the substructure variable distributions with p_T and R is less trivial than for the jet masses. In particular, changing the R parameter at high p_T changes significantly the C_a^{β} for $\beta > 0$ and the n_{constits} distributions, while leaving all other distributions qualitatively unchanged. This is illustrated in Figure 4 for $\beta = 0$ and $\beta = 1$ using a = 1in both cases for jets with $p_T = 1.0 - 1.1$ TeV.

The shift towards lower values with changing R is evident for the $C_1^{\beta=1}$ distributions, while the stability of $C_1^{\beta=0}$ can also be observed. These features are present in all p_T bins studied, but are even more pronounced for lower p_T bins. The shape of the Q-jet volatility distribution shows some non-trivial shape that deserves some explanation. Two peaks are observed, one at low volatility values and one at mid-volatility. These peaks are generated by two somewhat distinct populations. The high volatility peak arises from jets that get their mass primarily from soft (and sometimes wideangle) emissions. The removal of some of the constituents when building Q-jets thus changes the mass significantly, increasing the volatility. The lower volatility peak corresponds to jets for which mass is generated by a hard emission, which makes the fraction of Q-jets that change the mass significantly to be smaller. Since the probability of a hard emission is proportional to the colour charge (squared), the volatility peak is higher for gluon jets by about the colour factor C_A/C_F .

In summary, the overall discriminating power between quarks and gluons decreases with increasing R due to the reduction in the amount of out-of-cone radiation differences and and increased contamination from the underlying event (**BS:** is this ok?). The broad performance features discussed for this p_T bin also apply to the higher p_T bins. These is further quantified in the next section.

5.3 Combined Performance and Correlations

The quark/gluon tagging performance can be further improved over cuts on single observables by combining multiple observables in a BDT; due to the challenging nature of q/g-tagging, any improvement in performance with multivariable techniques could be critical for certain analyses, and the improvement could be more substantial in data than the marginal benefit found in MC and shown in Fig. 3. Fur-

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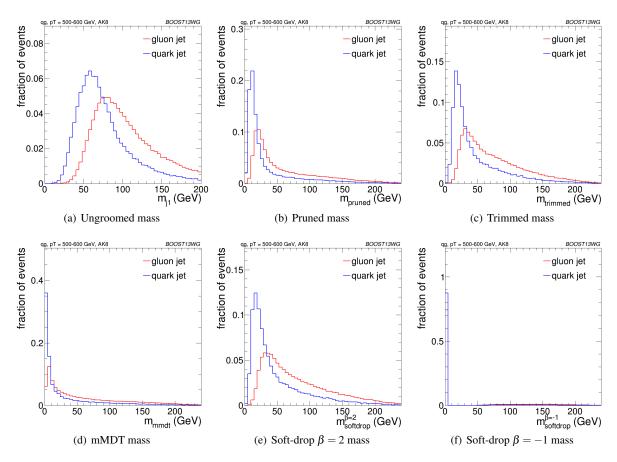


Fig. 1 Comparisons of ungroomed and groomed quark and gluon mass distributions for leading jets in the $p_T = 500 - 600$ GeV bin using the anti- k_T R=0.8 algorithm.

thermore, insight can be gained into the features allowing fob12 quark/gluon discrimination if the origin of the improvement, is understood. To quantitatively study this improvement, weq.14 build quark/gluon taggers from every pair-wise combination, of variables studied in the previous section for comparison, with the all-variable combination.

In order to quantitatively study the value of each variable $_{18}$ for quark/gluon tagging, we study the gluon rejection, de $_{219}$ fined as $1/\varepsilon_{\rm gluon}$, at a fixed quark selection efficiency of $50\%_{420}$ using jets with $p_T=1-1.1$ TeV and for different R param $_{221}$ eters. Figure 5 shows the gluon rejection for each pair-wise $_{22}$ combination. The pair-wise gluon rejection at 50% quark ef $_{423}$ ficiency can be compared to the single-variable values shown along the diagonal. The gluon rejection for the BDT all-variable combination is also shown on the bottom right of each plot. As already observed in the previous section, $n_{\rm constig}$ is the most powerful single variable and $C_1^{(\beta=0)}$ follows closely. However, the gains are largely correlated; the combined per formance of $n_{\rm constits}$ and $C_1^{(\beta=0)}$ is generally poorer than com n_{300} binations of $n_{\rm constits}$ with other jet substructure observables the end of $n_{\rm constits}$ and $n_{\rm constits}$ with other jet substructure observables n_{310} tween $n_{\rm constits}$ and n_{310} in spite of the high correlation be n_{310} tween $n_{\rm constits}$ and n_{310} in the two-variable combinations of n_{310}

 n_{constits} generally fare worse than two-variable combinations with $C_1^{(\beta=0)}$. In particular, the combinations of $\tau_1^{\beta=1}$ or $C_1^{(\beta=1)}$ with n_{constits} are capable of getting very close to the rejection achievable through the use of all variables for R=0.4 and R=0.8.

Tagger performance is generally better at small R. The overall loss in performance with increasing R can be seen in most single variables we study; this is expected, since more of the parton radiation is captured in the jet and more contamination from underlying event occurs, suppressing the differences between q/g jets. The principal exceptions are $C_1^{(\beta=0)}$ and the Q-jet mass volatility, which are both quite resilient to increasing R. For $C_1^{(\beta=0)}$, this is due to the fact that the exponent on ΔR is zero, and so soft radiation at the periphery of the jet does not substantially change the distribution; as a result, the performance is largely independent of R. Similarly, the soft radiation distant from the jet centre will be vetoed during pruning regardless of the cluster sequence, and so the R-dependence of Γ_{Oiet} is not significant. (BS: Check my logic?) Their combination, however, does perform slightly worse at larger R. (BS: I don't understand this, but it is a $\sim 10\%$ effect, so maybe not too

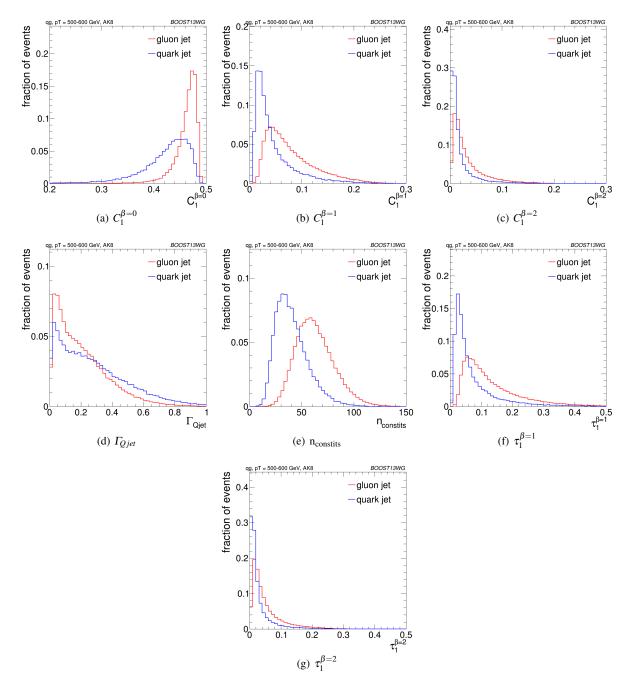


Fig. 2 Comparisons of quark and gluon distributions of different substructure variables for leading jets in the $p_T = 500 - 600$ GeV bin using the anti- k_T R=0.8 algorithm.

significant?). By contrast, $\tau_1^{(\beta=2)}$ and $C_1^{(\beta=2)}$ are particu443 larly sensitive to increasing R since, for $\beta=2$, large-angle44 emissions are given a larger weight.

These observations are qualitatively similar across all ranges of p_T . Quantitatively, however, there is a loss of rejection power for the taggers made of a combination of variables as the p_T decreases. This can be observed in Fig. 6 for anti- k_T R=0.4 jets of different p_T s. Clearly, most single variables retain their gluon rejection potential at lower

 p_T . However, when combined with other variables, the highest performing pairwise combinations lose ground with respect to other pairwise combinations. This is also reflected in the rejection of the tagger that uses a combination of all variables, which is lower at lower p_T s. [do we understand this?] (BS: This is a bit of a guess, but could it be that there is typically less radiation for low p_T , and so you're more sensitive to fluctuations; since you have less access

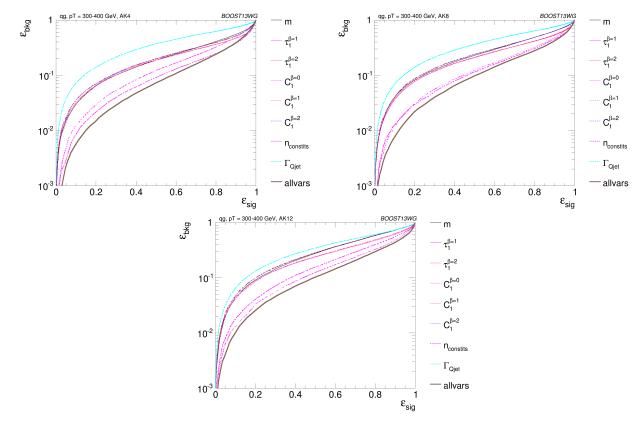


Fig. 3 The ROC curve for all single variables considered for quark-gluon discrimination in the p_T 300-400 GeV bin using the anti- k_T R=0.4, 0.8 and 1.2 algorithm.**ED: Hard to tell the lines on the plots apart**

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to information, combinations of observables perform less₇₂ well than at high p_T .)

6 Boosted W-Tagging

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In this section, we study the discrimination of a boosted hadronically decaying W signal against a gluon background comparing the performance of various groomed jet masses substructure variables, and BDT combinations of groomed mass and substructure. We produce ROC curves that elucidate the performance of the various groomed mass and substructure variables. A range of different distance parameters R for the anti- $k_{\rm T}$ jet algorithm are explored, as well as a variety of kinematic regimes (lead jet p_T 300-400 GeV_{le7} 500-600 GeV, 1.0-1.1 TeV). This allows us to determine $_{\tiny{\mbox{\scriptsize 488}}}$ the performance of observables as a function of jet radius and jet boost, and to see where different approaches may break down. The groomed mass and substructure variables are then combined in a BDT as described in Section 4, and 91 the performance of the resulting BDT discriminant explored 92 through ROC curves to understand the degree to which vari493 ables are correlated, and how this changes with jet boost and 94 jet radius.

6.1 Methodology

These studies use the WW samples as signal and the dijet gg as background, described previously in Section 2. Whilst only gluonic backgrounds are explored here, the conclusions as to the dependence of the performance and correlations on the jet boost and radius have been verified to hold also for qq backgrounds. **ED: To be checked!**

As in the q/g tagging studies, the showered events were clustered with FASTJET 3.03 using the anti- k_T algorithm with jet radii of $R=0.4,\,0.8,\,1.2$. In both signal and background samples, an upper and lower cut on the leading jet p_T is applied after showering/clustering, to ensure similar p_T spectra for signal and background in each p_T bin. The bins in leading jet p_T that are considered are 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV, for the 300-400 GeV, 500-600 GeV, 1.0-1.1 TeV parton p_T slices respectively. The jets then have various grooming approaches applied and substructure observables reconstructed as described in Section 3.4. The substructure observables studied in this section are:

- The ungroomed, trimmed (m_{trim}) , and pruned (m_{prun}) jet
- The mass output from the modified mass drop tagger (m_{mmdt}) .
- The soft drop mass with $\beta = -1, 2$ (m_{sd}).

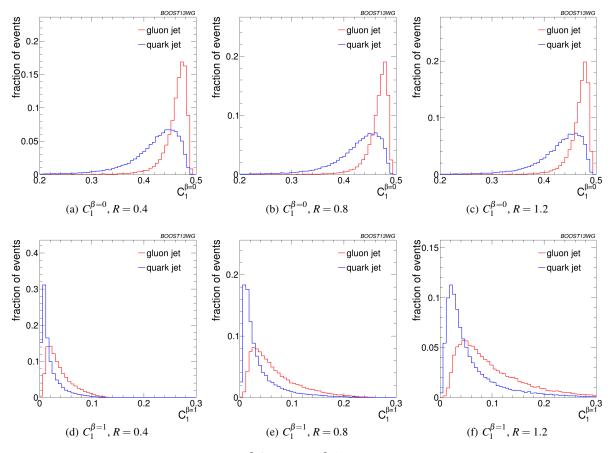


Fig. 4 Comparisons of quark and gluon distributions of $C_1^{\beta=0}$ (top) and $C_1^{\beta=1}$ (bottom) for leading jets in the $p_T=1-1.1$ TeV bin using the anti- k_T algorithm with R=0.4, 0.8 and 1.2.

- 2-point energy correlation function ratio $C_2^{\beta=1}$ (we also studied $\beta=2$ but do not show its results because it showed poor discrimination power).
- *N*-subjettiness ratio τ_2/τ_1 with $\beta = 1$ ($\tau_{21}^{\beta=1}$) and with axes computed using one-pass k_t axis optimization (we also studied $\beta = 2$ but did not show its results because it showed poor discrimination power).
- The pruned Qjet mass volatility, Γ_{Qjet} .

6.2 Single Variable Performance

In this section we will explore the performance of the vars22 ious groomed jet mass and substructure variables in terms22 of discriminating signal and background, and how this pers22 formance changes depending on the kinematic bin and jets30 radius considered.

Figure 7 the compares the signal and background in terms 2 of the different groomed masses explored for the anti- $k_{\rm T}$ 833 R=0.8 algorithm in the p_T 500-600 bin. One can clearly 34 see that in terms of separating signal and background the 35 groomed masses will be significantly more performant than 36 the ungroomed anti- $k_{\rm T}$ R=0.8 mass. Figure 8 compares sig 537

nal and background in the different substructure variables explored for the same jet radius and kinematic bin.

Figures 9, 10 and 11 show the single variable ROC curves compared to the ROC curve for a BDT combination of all the variables (labelled "allvars"), for each of the anti- $k_{\rm T}$ distance parameters considered in each of the kinematic bins. One can see that, in all cases, the "allvars" option is considerably better performant than any of the individual single variables considered, indicating that there is considerable complementarity between the variables, and this will be explored further in the next section.

Although the ROC curves give all the relevant information, it is hard to compare performance quantitatively. In Figures 12, 13 and 14 are shown matrices which give the background rejection for a signal efficiency of 70% when two variables (that on the x-axis and that on the y-axis) are combined in a BDT. These are shown separately for each p_T bin and jet radius considered. In the final column of these plots are shown the background rejection performance for three-variable BDT combinations of $m_{sd}^{\beta=2} + C_2^{\beta=1} + X$. These results will be discussed later in Section 6.3.3. The diagonal of these plots correspond to the background rejec-

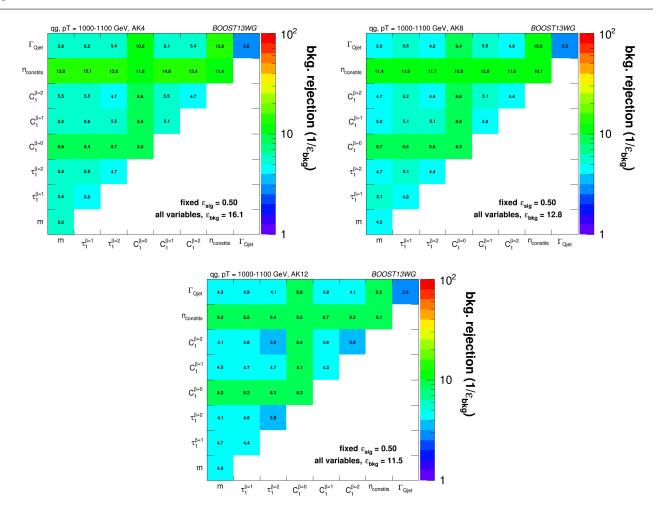


Fig. 5 Gluon rejection defined as $1/\varepsilon_{\text{gluon}}$ when using each 2-variable combination as a tagger with 50% acceptance for quark jets. Results are shown for jets with $p_T = 1 - 1.1$ TeV and for (left) R = 0.4; (centre) R = 0.8; (right) R = 1.2. The rejection obtained with a tagger that uses all variables is also shown in the plots.

tions for a single variable BDT, and can thus be examined tost get a quantitative measure of the individual single variables performance, and to study how this changes with jet radius and momenta.

One can see that in general the most performant $single_{61}$ variables are the groomed masses. However, in certain $kine_{562}$ matic bins and for certain jet radii, $C_2^{\beta=1}$ has a background rejection that is comparable to or better than the groomed masses.

By comparing Figures 12(a), 13(a) and 14(b), we can segoon how the background rejection performance evolves as we in 507 crease momenta whilst keeping the jet radius fixed to R=0.8568 Similarly, by comparing Figures 12(b), 13(b) and 14(c) we 509 can see how performance evolves with p_T for R=1.2. Fo 570 both R=0.8 and R=1.2 the background rejection power of the 571 groomed masses increases with increasing p_T , with a facto 572 1.5-2.5 increase in rejection in going from the 300-400 GeV 573 to 1.0-1.1 TeV bins. **ED: Add some of the 1-D plots com** 574 **paring signal and bkgd in the different masses and pT** 575

bins here? However, the $C_2^{\beta=1}$, Γ_{Qjet} and $\tau_{21}^{\beta=1}$ substructure variables behave somewhat differently. The background rejection power of the Γ_{Qjet} and $\tau_{21}^{\beta=1}$ variables both decrease with increasing p_T , by up to a factor two in going from the 300-400 GeV to 1.0-1.1 TeV bins. Conversely the rejection power of $C_2^{\beta=1}$ dramatically increases with increasing p_T for R=0.8, but does not improve with p_T for the larger jet radius R=1.2. ED: Can we explain this? Again, should we add some of the 1-D plots?

By comparing the individual sub-figures of Figures 12, 13 and 14 we can see how the background rejection performance depends on jet radius within the same p_T bin. To within $\sim 25\%$, the background rejection power of the groomed masses remains constant with respect to the jet radius. However, we again see rather different behaviour for the substructure variables. In all p_T bins considered the most performant substructure variable, $C_2^{\beta=1}$, performs best for an anti- k_T distance parameter of R=0.8. The performance of this variable is dramatically worse for the larger jet radius

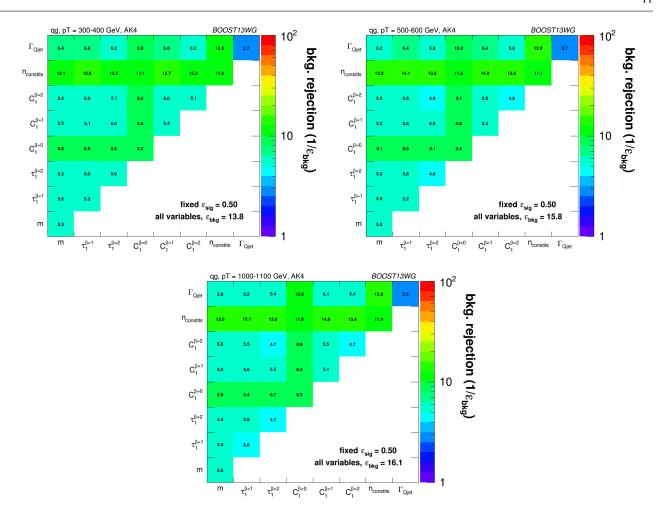


Fig. 6 Gluon rejection defined as $1/\varepsilon_{\text{gluon}}$ when using each 2-variable combination as a tagger with 50% acceptance for quark jets. Results are shown for R=0.4 jets with $p_T = 300 - 400$ GeV, $p_T = 500 - 600$ GeV and $p_T = 1 - 1.1$ TeV. The rejection obtained with a tagger that uses all variables is also shown in the plots.

of R=1.2 (a factor seven worse background rejection in the $_{92}$ 1.0-1.1 TeV bin), and substantially worse for R=0.4. For the $_{93}$ other jet substructure variables considered, Γ_{Qjet} and $\tau_{21}^{\beta=1}$ so their background rejection power also reduces for larger jet $_{95}$ radius, but not to the same extent. ED: Insert some nice discussion/explanation of why jet substructure power gen $_{597}$ erally gets worse as we go to large jet radius, but groomed $_{98}$ mass performance does not. Probably need the 1-D fig $_{599}$ ures for this.

6.3 Combined Performance

The off-diagonal entries in Figures 12, 13 and 14 can be used to compare the performance of different BDT two-variable combinations, and see how this varies as a function of p_{T007} and R. By comparing the background rejection achieved for the two-variable combinations to the background rejection of the "all variables" BDT, one can understand how much 10 to compare the same performance of the "all variables" BDT, one can understand how much 10 to compare the same performance of the "all variables" BDT, one can understand how much 10 to compare the performance of different BDT two-variables are the same performance of the same performance of different BDT two-variables are the same performance of the same performa

more discrimination is possible by adding further variables to the two-variable BDTs.

One can see that in general the most powerful two-variable combinations involve a groomed mass and a non-mass substructure variable $(C_2^{\beta=1}, \Gamma_{Qjet} \text{ or } \tau_{21}^{\beta=1})$. Two-variable combinations of the substructure variables are not powerful in comparison. Which particular mass + substructure variable combination is the most powerful depends strongly on the p_T and R of the jet, as discussed in the sections that follow.

There is also modest improvement in the background rejection when different groomed masses are combined, compared to the single variable groomed mass performance, indicating that there is complementary information between the different groomed masses. In addition, there is an improvement in the background rejection when the groomed masses are combined with the ungroomed mass, indicating that grooming removes some useful discriminatory information from the jet. These observations are explored further in the section below.

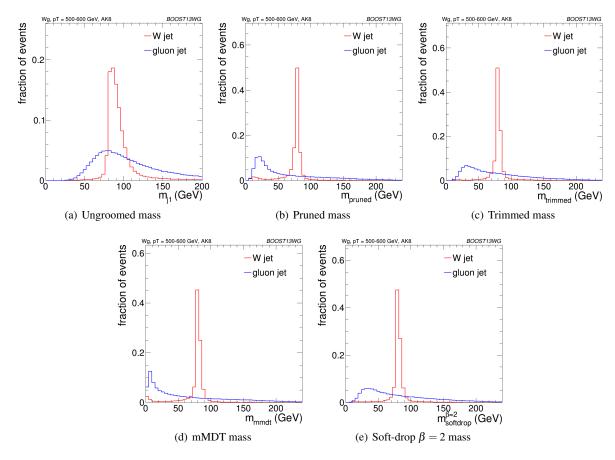


Fig. 7 Comparisons of the QCD background to the WW signal in the p_T 500-600 GeV bin using the anti- k_T R=0.8 algorithm: leading jet mass distributions.

Generally one can see that the R=0.8 jets offer the best₅₂ two-variable combined performance in all p_T bins explored₆₃₃ here. This is despite the fact that in the highest 1.0-1.1 GeV₆₃₄ p_T bin the average separation of the quarks from the W₆₃₅ decay is much smaller than 0.8, and well within 0.4. This conclusion could of course be susceptible to pile-up, which is not considered in this study.

6.3.1 Mass + Substructure Performance

As already noted, the largest background rejection at $70\%_{642}^{642}$ signal efficiency are in general achieved using those two variable BDT combinations which involve a groomed mass and a non-mass substructure variable. For both R=0.8 and R=1.2 jets, the rejection power of these two variable combinations increases substantially with increasing p_T , at least within the p_T range considered here.

For a jet radius of R=0.8, across the full p_T range considered, the groomed mass + substructure variable combinations with the largest background rejection are those which involve $C_2^{\beta=1}$. For example, in combination with $m_{sd}^{\beta=2}$, this produces a five-, eight- and fifteen-fold increase in back ground rejection compared to using the groomed mass alone m_{sd}^{652}

In Figure 15 the low degree of correlation between $m_{sd}^{\beta=2}$ versus $C_2^{\beta=1}$ that leads to these large improvements in background rejection can be seen. One can also see that what little correlation exists is rather non-linear in nature, changing from a negative to a positive correlation as a function of the groomed mass, something which helps to improve the background rejection in the region of the W mass peak.

However, when we switch to a jet radius of R=1.2 the picture for $C_2^{\beta=1}$ combinations changes dramatically. These become significantly less powerful, and the most powerful variable in groomed mass combinations becomes $\tau_{21}^{\beta=1}$ for all jet p_T considered. Figure 16 shows the correlation between $m_{sd}^{\beta=2}$ and $C_2^{\beta=1}$ in the p_T 1.0 - 1.2 TeV bin for the various jet radii considered. Figure 17 is the equivalent set of distributions for $m_{sd}^{\beta=2}$ and $\tau_{21}^{\beta=1}$. One can see from Figure 16 that, due to the sensitivity of the observable to to soft, wideangle radiation, as the jet radius increases $C_2^{\beta=1}$ increases and becomes more and more smeared out for both signal and background, leading to worse discrimination power. This does not happen to the same extent for $\tau_{21}^{\beta=1}$. We can see from Figure 17 that the negative correlation between $m_{sd}^{\beta=2}$ and $\tau_{21}^{\beta=1}$ that is clearly visible for R=0.4 decreases for larger



Fig. 8 Comparisons of the QCD background to the WW signal in the p_T 500-600 GeV bin using the anti- k_T R=0.8 algorithm: substructure variables.

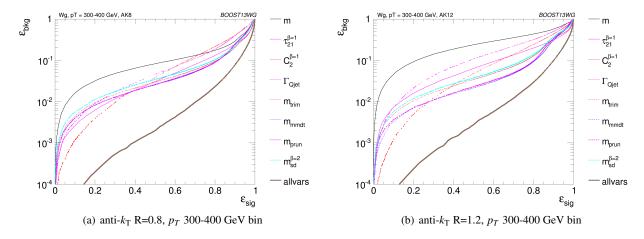


Fig. 9 The ROC curve for all single variables considered for W tagging in the p_T 300-400 GeV bin using the anti- k_T R=0.8 algorithm and R=1.2 algorithm.

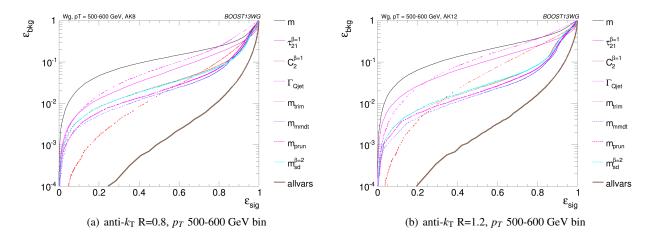


Fig. 10 The ROC curve for all single variables considered for W tagging in the p_T 500-600 GeV bin using the anti- k_T R=0.8 algorithm and R=1.2 algorithm.

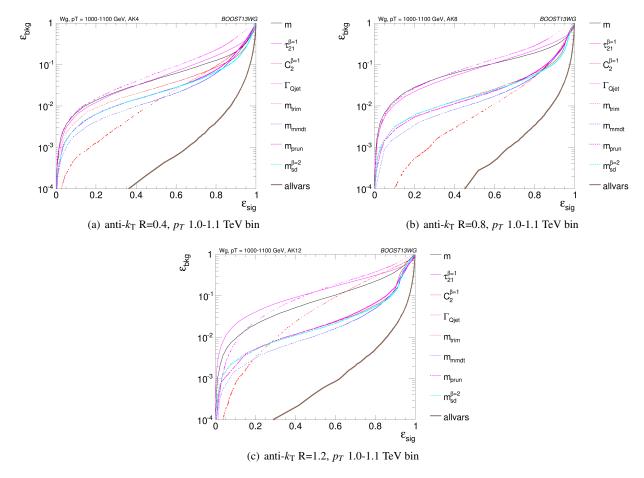


Fig. 11 The ROC curve for all single variables considered for W tagging in the p_T 1.0-1.1 TeV bin using the anti- k_T R=0.4 algorithm, anti- k_T R=0.8 algorithm and R=1.2 algorithm.

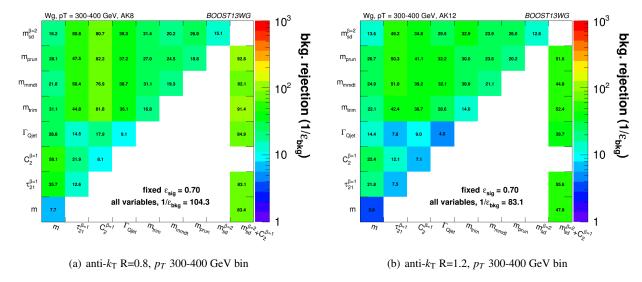


Fig. 12 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the p_T 300-400 GeV bin using the anti- k_T R=0.8 algorithm and R=1.2 algorithm. Also shown is the background rejection for a BDT combination of all of the variables considered.

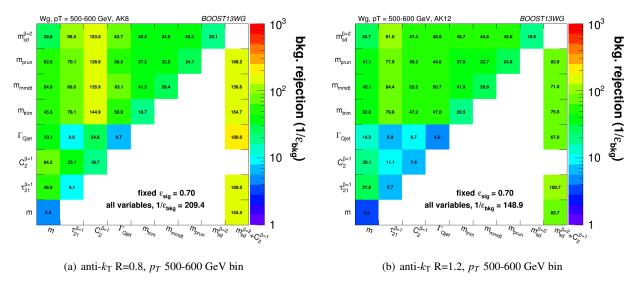


Fig. 13 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the p_T 500-600 GeV bin using the anti- k_T R=0.8 algorithm and R=1.2 algorithm. Also shown is the background rejection for a BDT combination of all of the variables considered.

jet radius, such that the groomed mass and substructure varised able are far less correlated and $\tau_{21}^{\beta=1}$ offers improved disection crimination within a $m_{sd}^{\beta=2}$ mass window.

6.3.2 Mass + Mass Performance

The different groomed masses and the ungroomed mass are of course not fully correlated, and thus one can always see some kind of improvement in the background rejection (relative to the single mass performance) when two different mass variables are combined in the BDT. However, in some cases the improvement can be dramatic, particularly at higher

 p_T , and particularly for combinations with the ungroomed mass. For example, in Figure 14 we can see that in the p_T 1.0-1.1 TeV bin the combination of pruned mass with ungroomed mass produces a greater than eight-fold improvement in the background rejection for R=0.4 jets, a greater than five-fold improvement for R=0.8 jets, and a factor \sim two improvement for R=1.2 jets. A similar behaviour can be seen for mMDT mass. In Figures 18, 19 and 20 is shown the 2-D correlation plots of the pruned mass versus the ungroomed mass separately for the WW signal and gg background samples in the p_T 1.0-1.1 TeV bin, for the various jet radii considered. For comparison, the correlation of the trimmed

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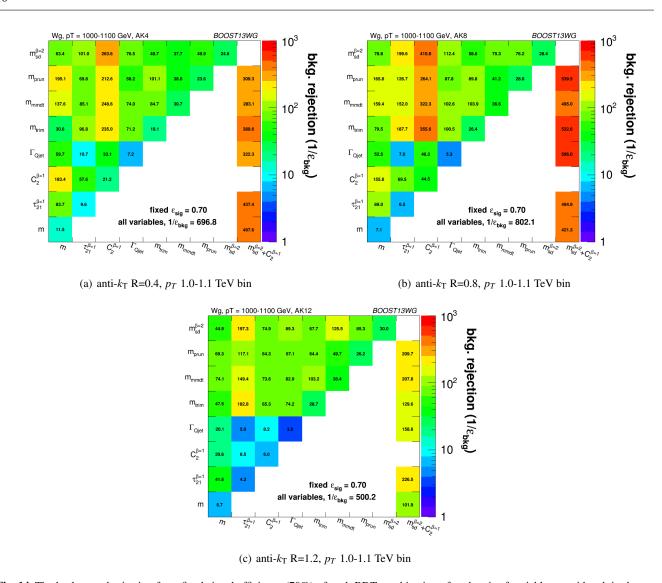


Fig. 14 The background rejection for a fixed signal efficiency (70%) of each BDT combination of each pair of variables considered, in the p_T 1.0-1.1 TeV bin using the anti- k_T R=0.4, R=0.8 and R=1.2 algorithm. Also shown is the background rejection for a BDT combination of all of the variables considered.

mass with the ungroomed mass, a combination that does notes improve on the single mass as dramatically, is shown. In albos cases one can see that there is a much smaller degree of cor694 relation between the pruned mass and the ungroomed masses in the backgrounds sample than for the trimmed mass and the ungroomed mass. This is most obvious in Figure 18697 where the high degree of correlation between the trimmedos and ungroomed mass is expected, since with the parameters99 used (in particular $R_{trim} = 0.2$) we cannot expect trimming₀₀ to have a significant impact on an R=0.4 jet. The reduced correlation with ungroomed mass for pruning in the background means that, once we have made the requirement that the pruned mass is consistent with a W (i.e. ~80 GeV), a₇₀₂ relatively large difference between signal and backgroundon in the ungroomed mass still remains, and can be exploited ou to improve the background rejection further. In other words₇₀₅ many of the background events which pass the pruned mass requirement do so because they are shifted to lower mass (to be within a signal mass window) by the grooming, but these events still have the property that they look very much like background events before the grooming. A single requirement on the groomed mass only does not exploit this. Of course, the impact of pile-up, not considered in this study, could significantly limit the degree to which the ungroomed mass could be used to improve discrimination in this way.

6.3.3 "All Variables" Performance

As well as the background rejection at a fixed 70% signal efficiency for two-variable combinations, Figures 12, 13 and 14 also report the background rejection achieved by a combination of all the variables considered into a single

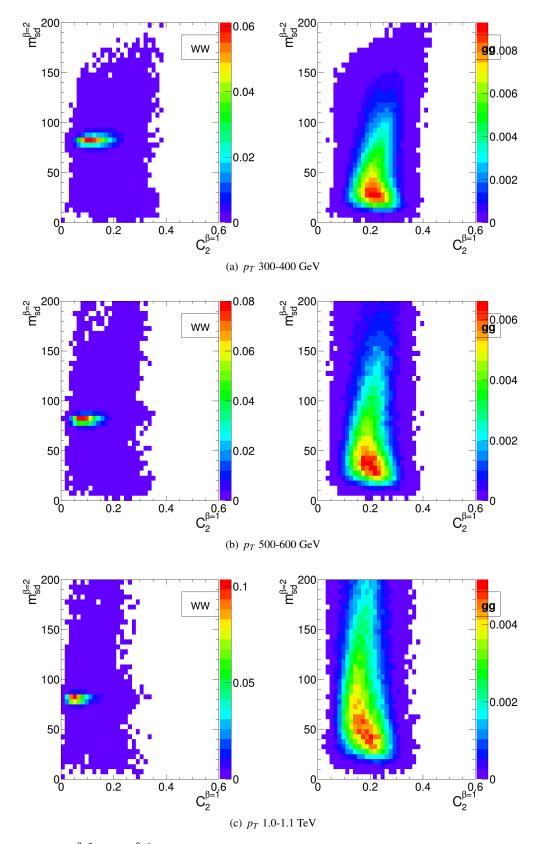


Fig. 15 2-D plots showing $m_{sd}^{\beta=2}$ versus $C_2^{\beta=1}$ for R=0.8 jets in the various p_T bins considered.



Fig. 16 2-D plots showing $m_{sd}^{\beta=2}$ versus $C_2^{\beta=1}$ for R=0.4, 0.8 and 1.2 jets in the p_T 1.0-1.1 TeV bin.

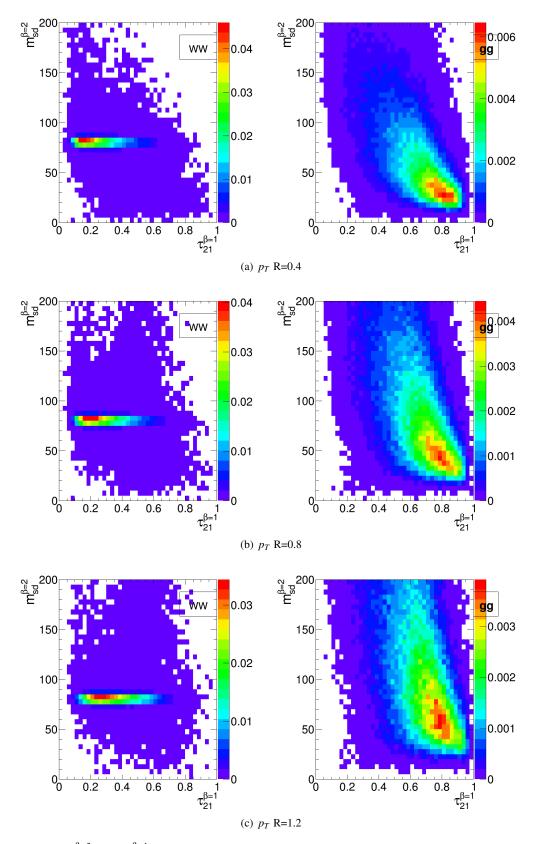


Fig. 17 2-D plots showing $m_{sd}^{\beta=2}$ versus $\tau_{21}^{\beta=1}$ for R=0.4, 0.8 and 1.2 jets in the p_T 1.0-1.1 TeV bin.

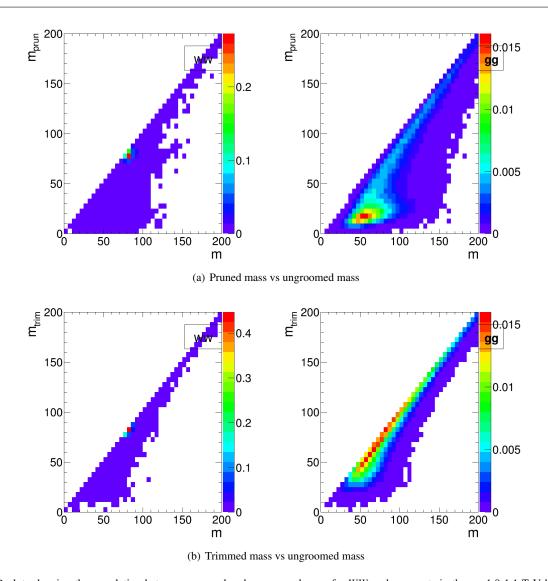


Fig. 18 2-D plots showing the correlation between groomed and ungroomed mass for WW and gg events in the p_T 1.0-1.1 TeV bin using the anti- k_T R=0.4 algorithm.

BDT discriminant. One can see that, in all cases, the re₇₂₂ jection power of this "all variables" BDT is significantly₂₃ larger than the best two-variable combination. This indicates₂₄ that beyond the best two-variable combination there is still₂₅ significant complementary information available in the remaining variables in order to improve the discrimination of signal and background. How much complementary information is available appears to be p_T dependent. In the lower p_{729} 300-400 and 500-600 GeV bins the background rejection of the "all variables" combination is a factor ~ 1.5 greater than the best two-variable combination, but in the highest p_T bin it is a factor ~ 2.5 greater.

The final column in Figures 12, 13 and 14 allows us^{34} to explore the all variables performance a little further. It shows the background rejection for three variable BDT com binations of $m_{sd}^{\beta=2} + C_2^{\beta=1} + X$, where X is the variable of m_{sd}^{37}

the y-axis. For jets with R=0.4 and R=0.8, the combination $m_{sd}^{\beta=2}+C_2^{\beta=1}$ is the best performant (or very close to the best performant) two-variable combination in every p_T bin considered. For R=1.2 this is not the case, as $C_2^{\beta=1}$ is superceded by $\tau_{21}^{\beta=1}$ in performance, as discussed earlier. Thus, in considering the three-variable combination results it is best to focus on the R=0.4 and R=0.8 cases. Here we see that, for the lower p_T 300-400 and 500-600 GeV bins, adding the third variable to the best two-variable combination brings us to within $\sim 15\%$ of the "all variables" background rejection. However, in the highest p_T 1.0-1.1 TeV bin, whilst adding the third variable does improve the performance considerably, we are still $\sim 40\%$ from the observed "all variables" background rejection, and clearly adding a fourth or maybe even fifth variable would bring considerable gains. In terms of which variable offers the best improvement when added

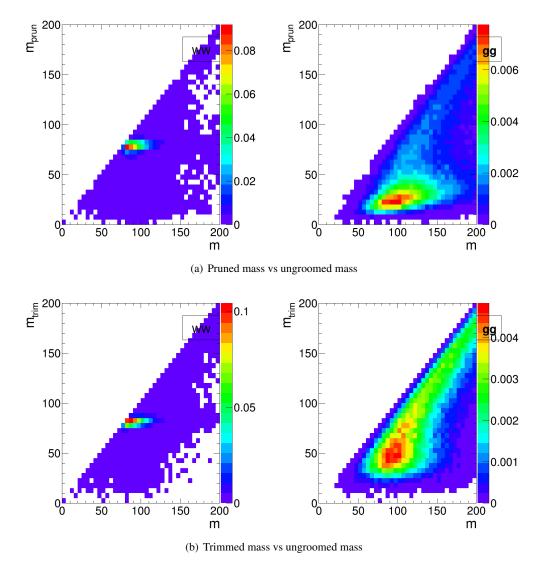


Fig. 19 2-D plots showing the correlation between groomed and ungroomed mass for WW and gg events in the p_T 1.0-1.1 TeV bin using the anti- k_T R=0.8 algorithm.

to the $m_{sd}^{\beta=2}+C_2^{\beta=1}$ combination, it is hard to see an obvious pattern; the best third variable changes depending on the $p_{T^{53}}$ and R considered.

In conclusion, it appears that there is a rich and com₇₅₅ plex structure in terms of the degree to which the discrimina₇₅₆ tory information provided by the set of variables considered₅₇ overlaps, with the degree of overlap apparently decreasing at higher p_T . This suggests that in all p_T ranges, but especially, at higher p_T , there are substantial performance gains to be made by designing a more complex multivariate W tagger.

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We have studied the performance, in terms of the degree to which a hadronically decaying W boson can be separated from a gluonic background, of a number of groomed jetsor

masses, substructure variables, and BDT combinations of the above. We have used this to build a picture of how the discriminatory information contained in the variables overlaps, and how this complementarity between the variables changes with p_T and anti- k_T distance parameter R.

In terms of the performance of individual variables, we find that, in agreement with other studies [**REF**], in general the groomed masses perform best, with a background rejection power that increases with increasing p_T , but which is more constant with respect to changes in R. Conversely, the performance of other substructure variables, such as $C_2^{\beta=1}$ and $\tau_{21}^{\beta=1}$ is more susceptible to changes in radius, with background rejection power decreasing with increasing R.

The best two-variable performance is obtained by combining a groomed mass with a substructure variable. Which particular substructure variable works best in combination

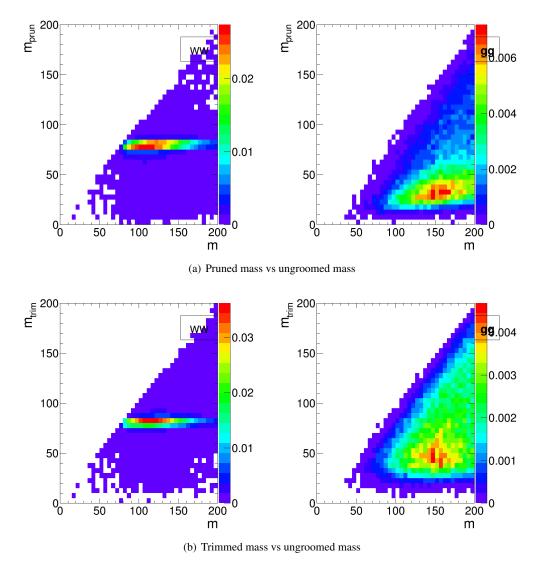


Fig. 20 2-D plots showing the correlation between groomed and ungroomed mass for WW and gg events in the p_T 1.0-1.1 TeV bin using the anti- k_T R=1.2 algorithm.

is strongly dependent on p_T and R. $C_2^{\beta=1}$ offers significantes complimentarity to groomed mass at smaller R, owing to the small degree of correlation between the variables. However, the sensitivity of $C_2^{\beta=1}$ to soft, wide-angle radiation leads to, worse discrimination power at large R, where $\tau_{21}^{\beta=1}$ performs better in combination. Our studies also demonstrate the potential for enhanced discrimination by combining groomeds and ungroomed mass information, although the use of ungroomed mass in this may in practice be limited by the prestore ence of pile-up that is not considered in these studies.

By examining the performance of a BDT combination of $_{93}$ all the variables considered, it is clear that there are poten $_{794}$ tially substantial performance gains to be made by designing a more complex multivariate W tagger, especially at higher $_{97}$.

7 Top Tagging

In this section, we study the identification of boosted top quarks at Run II of the LHC. Boosted top quarks result in large-radius jets with complex substructure, containing a *b*-subjet and a boosted *W*. The additional kinematic handles coming from the reconstruction of the *W* mass and *b*-tagging allow a very high degree of discrimination of top quark jets from QCD backgrounds.

We consider top quarks with moderate boost (600-1000 GeV), and perhaps most interestingly, at high boost ($\gtrsim 1500$ GeV). Top tagging faces several challenges in the high- p_T regime. For such high- p_T jets, the b-tagging efficiencies are no longer reliably known. Also, the top jet can also accompanied by additional radiation with $p_T \sim m_t$, leading to combinatoric ambiguities of reconstructing the top and W, and

the possibility that existing taggers or observables shape the background by looking for subjet combinations that reconstant m_t/m_W . To study this, we examine the performance of both mass-reconstruction variables, as well as shape observables that probe the three-pronged nature of the top jet and the accompanying radiation pattern.

We use the top quark MC samples for each bin described in Section 2.2. The analysis relies on FASTJET 3.0.3 for jet clustering and calculation of jet substructure observables. Sets are clustered using the anti- k_t algorithm. An upper and lower p_T cut are applied after jet clustering to each sample to ensure similar p_T spectra in each bin. The bins in leading jet p_T that are investigated for top tagging are 600-700 GeV, 1-1.1 TeV, and 1.5-1.6 TeV. Jets are clustered with radii R = 0.4, 0.8, and 1.2; R = 0.4 jets are only studied in the 1.5-858 decay products are all contained within an R = 0.4 jet.

7.1 Methodology

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We study a number of top-tagging strategies, in particular: 864

- HEPTopTagger
- 2. Johns Hopkins Tagger (JH)
- 3. Trimming
- 4. Pruning

The top taggers have criteria for reconstructing a top and W candidate, and a corresponding top and W mass, as de⁸⁷¹ scribed in Section 3.3, while the grooming algorithms (trim⁸⁷² ming and pruning) do not incorporate a W-identification step⁹⁷³ For a level playing field, where grooming is used we con⁸⁷⁴ struct a W candidate mass, m_W , from the three leading sub⁸⁷⁵ jets by taking the mass of the pair of subjets with the smalles⁸⁷⁶ invariant mass; in the case that only two subjets are recon⁸⁷⁷ structed, we take the mass of the leading subjet. The top⁹⁷⁸ mass, m_t , is the mass of the groomed jet. All of the above⁹⁷⁹ taggers and groomers incorporate a step to remove pile-up⁸⁸⁰ and other soft radiation.

We also consider the performance of the following je882 shape observables:

- The ungroomed jet mass.
- *N*-subjettiness ratios τ_2/τ_1 and τ_3/τ_2 with $\beta = 1$ and the "winner-takes-all" axes.
- 2-point energy correlation function ratios $C_2^{\beta=1}$ and $C_3^{\beta=\frac{\pi}{888}}$
- The pruned Qjet mass volatility, Γ_{Qjet} .

In addition to the jet shape performance, we combine the jet shapes with the mass-reconstruction methods described above to determine the optimal combined performance.

For determining the performance of multiple variables, we combine the relevant tagger output observables and/or jebo4 shapes into a boosted decision tree (BDT), which determines, the optimal cut. Additionally, because each tagger has two

input parameters, as described in Section 3.3, we scan over reasonable values of the parameters to determine the optimal value that gives the largest background rejection for each top tagging signal efficiency. This allows a direct comparison of the optimized version of each tagger. The input values scanned for the various algorithms are:

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- HEPTopTagger: m \in [30, 100] GeV, \mu \in [0.5, 1]
- JH Tagger: \delta_p \in [0.02, 0.15], \delta_R \in [0.07, 0.2]
- Trimming: f_{\text{cut}} \in [0.02, 0.14], R_{\text{trim}} \in [0.1, 0.5]
- Pruning: z_{\text{cut}} \in [0.02, 0.14], R_{\text{cut}} \in [0.1, 0.6]
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7.2 Single-observable performance

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We start by investigating the behaviour of individual jet substructure observables. Because of the rich, three-pronged structure of the top decay, it is expected that combinations of masses and jet shapes will far outperform single observables in identifying boosted tops. However, a study of the top-tagging performance of single variables facilitates a direct comparison with the W tagging results in Section 6, and also allows a straightforward examination of the performance of each observable for different p_T and jet radius.

Fig. 21 shows the ROC curves for each of the top-tagging observables, with the bare (ungroomed) jet mass also plotted for comparison. The jet shape observables all perform substantially worse than jet mass, unlike W tagging for which several observables are competitive with or perform better than jet mass (see, for example, Fig. 7). To understand why this is the case, consider N-subjettiness. The W is two-pronged and the top is three-pronged; therefore, we expect τ_{21} and τ_{32} to be the best-performant N-subjettiness ratio, respectively. However, τ_{21} also contains an implicit cut on the denominator, τ_1 , which is strongly correlated with jet mass. Therefore, τ_{21} combines both mass and shape information to some extent. By contrast, and as is clear in Fig.21(a), the best shape for top tagging is τ_{32} , which contains no information on the mass. Therefore, it is unsurprising that the shapes most useful for top tagging are less sensitive to the jet mass, and under-perform relative to the corresponding observables for W tagging.

Of the two top tagging algorithms, we can see from Figure 21 that the Johns Hopkins (JH) tagger out-performs the HEPTopTagger in terms of its signal-to-background separation power in both the top and W candidate masses. In Figure 22 we show the histograms for the top mass output from the JH and HEPTopTagger for different R in the p_T 1.5-1.6 TeV bin, and in Figure 23 for different p_T at at R =0.8, optimized at a signal efficiency of 30%. One can see from these figures that the likely reason for the better performance of the JH tagger is that, in the HEPTopTagger algorithm, the jet is filtered to select the five hardest subjets, and then three subjets are chosen which reconstruct the top mass. This re-

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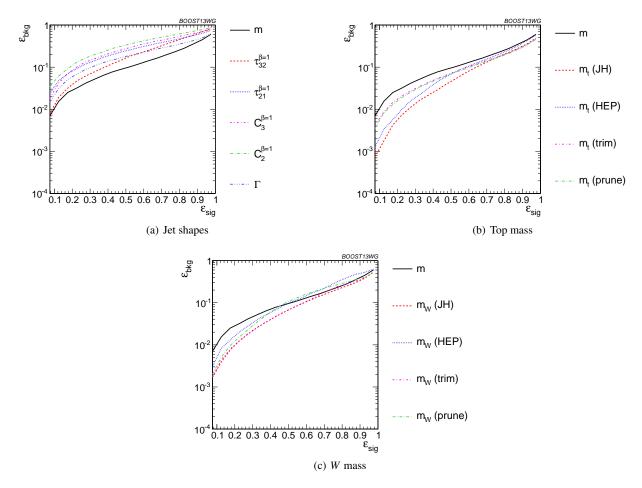


Fig. 21 Comparison of single-variable top-tagging performance in the $p_T = 1 - 1.1$ GeV bin using the anti- k_T , R=0.8 algorithm.

quirement tends to shape a peak in the QCD background₁₀ around m_t for the HEPTopTagger, while the JH tagger has₂₀ no such requirement. It has been suggested by Anders eb_{21} al. [?] that performance in the HEPTopTagger may be im₉₂₂ proved by selecting the three subjets reconstructing the top₂₃ only among those that pass the W mass constraints, which₂₄ somewhat reduces the shaping of the background. The dis₅₂₅ crepancy between the JH and HEPTopTaggers is more pro₉₂₆ nounced at higher p_T and larger jet radius (see Figs. 26 and₂₇ 29).

We also see in Figure 21(b) that the top mass from the JH tagger and the HEPTopTagger has superior performance relative to either of the grooming algorithms; this is because 1 the pruning and trimming algorithms do not have inherent W-identification steps and are not optimized for this pure pose. Indeed, because of the lack of a W-identification step 1 grooming algorithms are forced to strike a balance between 1 under-grooming the jet, which broadens the signal peak due 1 to UE contamination and features a larger background rate 1 and over-grooming the jet, which occasionally throws out 1 the b-jet and preserves only the W components inside the 1 jet. We demonstrate this effect in Figures 22 and 23, show 1

ing that with $\varepsilon_{\rm sig} = 0.3 - 0.35$, the optimal performance of the tagger over-grooms a substantial fraction of the jets ($\sim 20 - 30\%$), leading to a spurious second peak at the W mass. This effect is more pronounced at large R and p_T , since more aggressive grooming is required in these limits to combat the increased contamination from UE and QCD radiation.

In Figures 24 and 26 we directly compare ROC curves for jet shape observable performance and top mass performance respectively in the three different p_T bins considered whilst keeping the jet radius fixed at R=0.8. The input parameters of the taggers, groomers and shape variables are separately optimized in each p_T bin. One can see from Figure 24 that the tagging performance of jet shapes do not change substantially with p_T . The observables $\tau_{32}^{(\beta=1)}$ and Qiet volatility Γ have the most variation and tend to degrade with higher p_T , as can be seen in Figure 25. This makes sense, as higher- p_T QCD jets have more, harder emissions within the jet, giving rise to substructure that fakes the signal. By contrast, from Figure 26 we can see that most of the top mass observables have superior performance at higher p_T due to the radiation from the top quark becoming more collimated. The notable exception is the HEPTopTagger, which

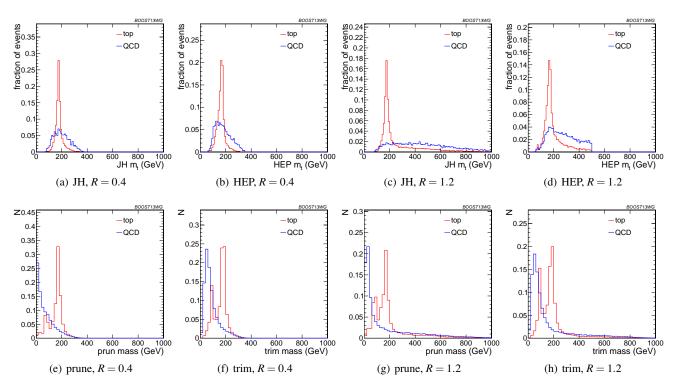


Fig. 22 Comparison of top mass reconstruction with the Johns Hopkins (JH), HEPTopTaggers (HEP), pruning, and trimming at different R using the anti- k_T algorithm, $p_T = 1.5 - 1.6$ TeV. Each histogram is shown for the working point optimized for best performance with m_t in the 0.3 - 0.35 signal efficiency bin, and is normalized to the fraction of events passing the tagger. In this and subsequent plots, the HEPTopTagger distribution cuts off at 500 GeV because the tagger fails to tag jets with a larger mass.

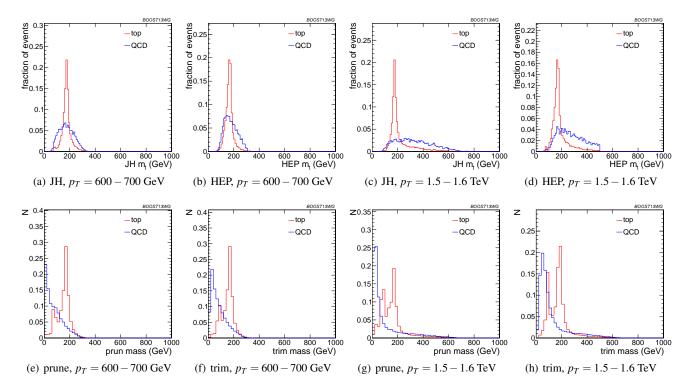


Fig. 23 Comparison of top mass reconstruction with the Johns Hopkins (JH), HEPTopTaggers (HEP), pruning, and trimming at different p_T using the anti- k_T algorithm, R = 0.8. Each histogram is shown for the working point optimized for best performance with m_t in the 0.3 - 0.35 signal efficiency bin, and is normalized to the fraction of events passing the tagger.

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degrades at higher p_T , likely in part due to the background shaping effects discussed earlier.

In Figures 27 and 29 we directly compare ROC curves os for jet shape observable performance and top mass perfor994 mance respectively for the three different jet radii considered 95 within the p_T 1.5-1.6 TeV bin. Again, the input parameter \$996 of the taggers, groomers and shape variables are separately or optimized for each jet radius. We can see from these figures 998 that most of the top tagging variables, both shape and recon 999 structed top mass, perform best for smaller radius. This isoo likely because, at such high p_T , most of the radiation from or the top quark is confined within R = 0.4, and having a larger a larger jet radius makes the observable more susceptible to contam 503 ination from the underlying event and other uncorrelated rame diation. In Figure 28, we compare the individual top signal_{los} and QCD background distributions for each shape variable on considered in the p_T 1.5-1.6 TeV bin for the various jet radi $\frac{1}{1007}$ One can see that the distributions for both signal and back toos ground broaden with increasing R, degrading the discriminates nating power. For $C_2^{(\beta=1)}$ and $C_3^{(\beta=1)}$, the background distribution butions are shifted upward as well. Therefore, the discriment inating power generally gets worse with increasing R. Theorem main exception is for $C_3^{(\beta=1)}$, which performs optimally at $(\beta=1)$ R = 0.8; in this case, the signal and background coincidental tally happen to have the same distribution around R = 0.4915and so R = 0.8 gives better discrimination.

7.3 Performance of multivariable combinations

We now consider various BDT combinations of the observ⁹²¹ ables from Section 7.2, using the techniques described itt⁹²³ Section 4. In particular, we consider the performance of irt⁹²³ dividual taggers such as the JH tagger and HEPTopTagget⁹²⁴ which output information about the top and *W* candidatt⁹²⁵ masses and the helicity angle; groomers, such as trimmint⁹²⁶ and pruning, which remove soft, uncorrelated radiation from the top candidate to improve mass reconstruction, and to which we have added a *W* reconstruction step; and the comtop bination of the outputs of the above taggers/groomers, botth with each other, and with shape variables such as *N*-subjettimess ratios and energy correlation ratios. For all observables with 22 tuneable input parameters, we scan and optimize over realto 33 istic values of such parameters, as described in Section 7.14034

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In Figure 30, we directly compare the performance $\mathfrak{G}^{\mathfrak{p}35}$ the HEPTopTagger, the JH tagger, trimming, and pruning, $\mathfrak{i}\mathfrak{p}^{36}$ the $p_T=1-1.1$ TeV bin using jet radius R=0.8, where bot \mathfrak{p}^{37} m_t and m_W are used in the groomers. Generally, we find tha \mathfrak{p}^{38} pruning, which does not naturally incorporate subjets integrate the algorithm, does not perform as well as the others. Integrate estingly, trimming, which does include a subjet-identification step, performs comparably to the HEPTopTagger over much of the range, possibly due to the background-shaping obods

served in Section 7.2. By contrast, the JH tagger outperforms the other algorithms. To determine whether there is complementary information in the mass outputs from different top taggers, we also consider in Figure 30 a multivariable combination of all of the JH and HEPTopTagger outputs. The maximum efficiency of the combined JH and HEPTopTaggers is limited, as some fraction of signal events inevitably fails either one or other of the taggers. We do see a 20-50% improvement in performance when combining all outputs, which suggests that the different algorithms used to identify the top and W for different taggers contains complementary information.

In Figure 31 we present the results for multivariable combinations of the top tagger outputs with and without shape variables. We see that, for both the HEPTopTagger and the JH tagger, the shape observables contain additional information uncorrelated with the masses and helicity angle, and give on average a factor 2-3 improvement in signal discrimination. We see that, when combined with the tagger outputs, both the energy correlation functions $C_2 + C_3$ and the Nsubjettiness ratios $\tau_{21} + \tau_{32}$ give comparable performance, while the Qjet mass volatility is slightly worse; this is unsurprising, as Qjets accesses shape information in a more indirect way from other shape observables. Combining all shape observables with a single top tagger provides even greater enhancement in discrimination power. We directly compare the performance of the JH and HEPTopTaggers in Figure 31(c). Combining the taggers with shape information nearly erases the difference between the tagging methods observed in Figure 30; this indicates that combining the shape information with the HEPTopTagger identifies the differences between signal and background missed by the tagger alone. This also suggests that further improvement to discriminating power may be minimal, as various multivariable combinations are converging to within a factor of 20% or so.

In Figure 32 we present the results for multivariable combinations of groomer outputs with and without shape variables. As with the tagging algorithms, combinations of groomers with shape observables improves their discriminating power; combinations with $\tau_{32} + \tau_{21}$ perform comparably to those with $C_3 + C_2$, and both of these are superior to combinations with the mass volatility, Γ . Substantial improvement is further possible by combining the groomers with all shape observables. Not surprisingly, the taggers that lag behind in performance enjoy the largest gain in signal-background discrimination with the addition of shape observables. Once again, in Figure 32(c), we find that the differences between pruning and trimming are erased when combined with shape information.

Finally, in Figure 33, we compare the performance of each of the tagger/groomers when their outputs are combined with all of the shape observables considered. One can

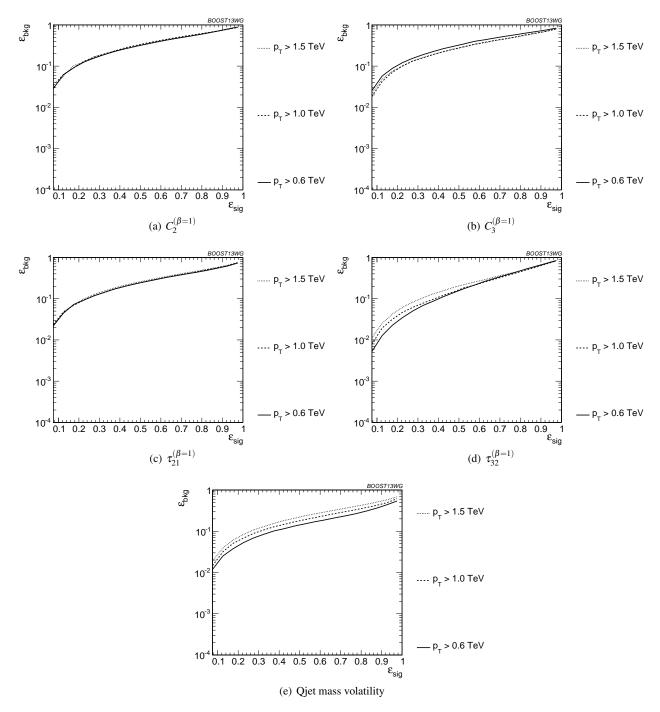


Fig. 24 Comparison of individual jet shape performance at different p_T using the anti- k_T R=0.8 algorithm.

see that the discrepancies between the performance of that different taggers/groomers all but vanishes, suggesting petiosal haps that we are here utilising all available signal-background discrimination information, and that this is the optimal tops tagging performance that could be achieved in these conditions.

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Up to this point we have just considered the combined multivariable performance in the p_T 1.0-1.1 TeV bin with

jet radius R=0.8. We now compare the BDT combinations of tagger outputs, with and without shape variables, at different p_T . The taggers are optimized over all input parameters for each choice of p_T and signal efficiency. As with the single-variable study, we consider anti- k_T jets clustered with R=0.8 and compare the outcomes in the $p_T=500-600$ GeV, $p_T=1-1.1$ TeV, and $p_T=1.5-1.6$ TeV bins. The comparison of the taggers/groomers is shown in Figure 34.

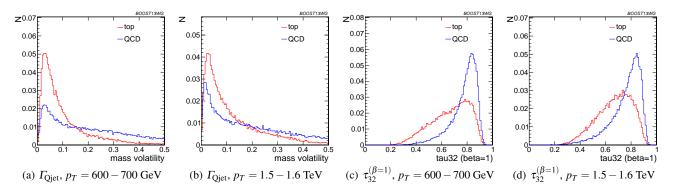


Fig. 25 Comparison of Γ_{Qjet} and $\tau_{32}^{\beta=1}$ at R=0.8 and different values of the p_T . These shape observables are the most sensitive to varying p_T .

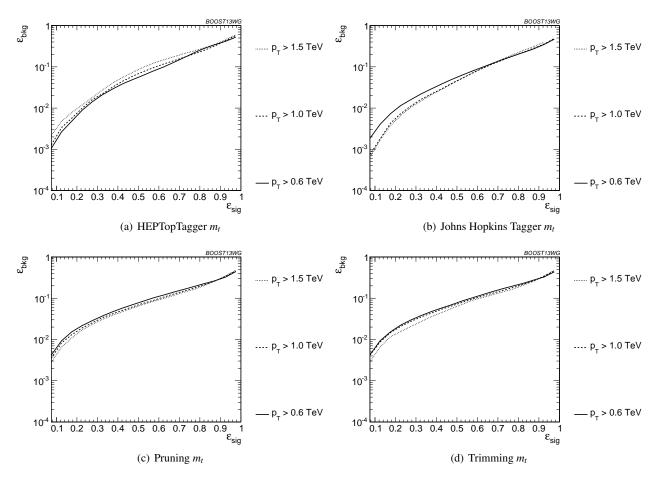


Fig. 26 Comparison of top mass performance of different taggers at different p_T using the anti- k_T R=0.8 algorithm.

The behaviour with p_T is qualitatively similar to the beaose haviour of the m_t observable for each tagger/groomer shows in Figure 26; this suggests that the p_T behaviour of the tagger gers is dominated by the top mass reconstruction. As before the HEPTopTagger performance degrades slightly with interactions creased p_T due to the background shaping effect, while the JH tagger and groomers modestly improve in performance 1075

In Figure 35, we show the p_T dependence of BDT conf⁰⁷⁶ binations of the JH tagger output combined with shape ob⁰⁷⁷

servables. We find that the curves look nearly identical: the p_T dependence is dominated by the top mass reconstruction, and combining the tagger outputs with different shape observables does not substantially change this behaviour. The same holds true for trimming and pruning. By contrast, HEPTopTagger ROC curves, shown in Figure 36, do change somewhat when combined with different shape observables; due to the suboptimal performance of the HEPTopTagger at high p_T , we find that combining the HEPTopTagger with

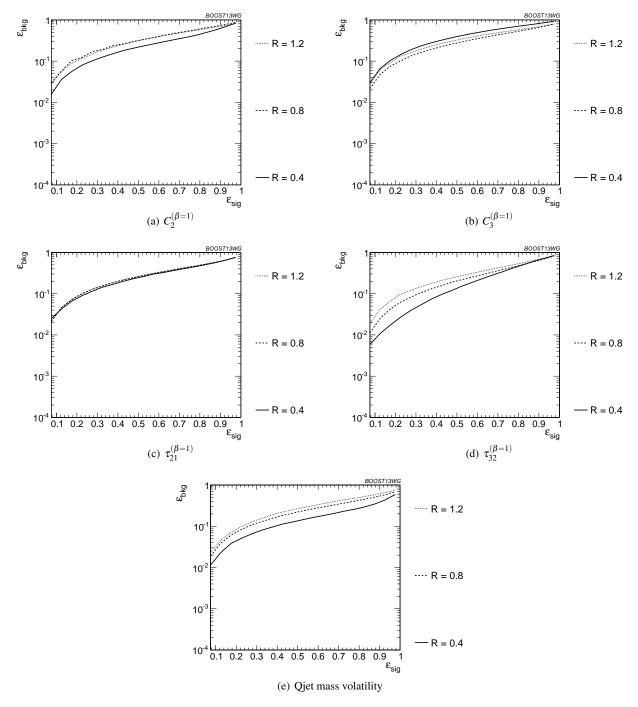


Fig. 27 Comparison of individual jet shape performance at different R in the $p_T = 1.5 - 1.6$ TeV bin.

 $C_3^{(\beta=1)}$, which in Figure 24(b) is seen to have some modese est improvement at high p_T , can improve its performance cost Combining the HEPTopTagger with multiple shape observes ables gives the maximum improvement in performance absorbigh p_T relative to at low p_T .

In Figure 37 we compare the BDT combinations of $tag_{\bar{0}93}$ ger outputs, with and without shape variables, at different jet

radius R in the $p_T=1.5-1.6$ TeV bin. The taggers are optimized over all input parameters for each choice of R and signal efficiency. We find that, for all taggers and groomers, the performance is always best at small R; the choice of R is sufficiently large to admit the full top quark decay at such high p_T , but is small enough to suppress contamination from additional radiation. This is not altered when the taggers are combined with shape observable. For example, in Figure 38

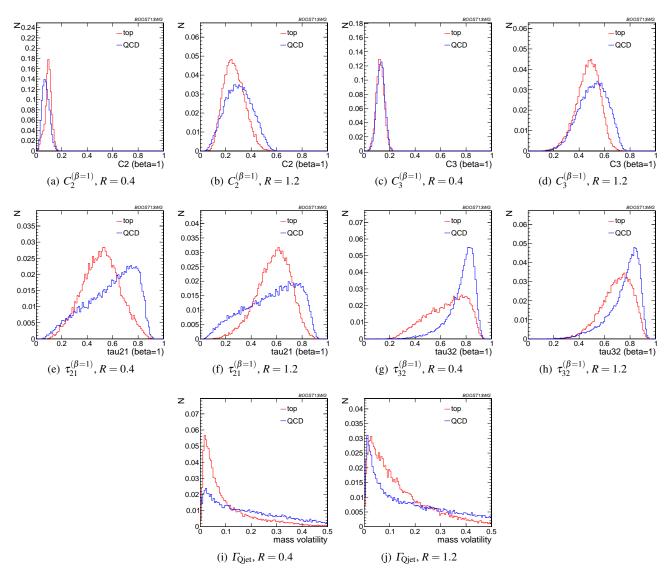


Fig. 28 Comparison of various shape observables in the $p_T = 1.5 - 1.6$ TeV bin and different values of the anti- k_T radius R.

is shown the depedence on R of the JH tagger when com₁₀₈ bined with shape observables, where one can see that thao R-dependence is identical for all combinations. The sama₁₀ holds true for the HEPTopTagger, trimming, and pruning. 1111

7.4 Performance at Sub-Optimal Working Points

Up until now, we have re-optimized our tagger and groomening parameters for each p_T , R, and signal efficiency working point. In reality, experiments will choose a finite set of working points to use. How do our results hold up when this is taken into account? To address this concern, we replique cate our analyses, but only optimize the top taggers for a_{20} particular p_T/R /efficiency and apply the same parameters to other scenarios. This allows us to determine the extentize to which re-optimization is necessary to maintain the high a_{20}

signal-background discrimination power seen in the top tagging algorithms we study. The shape observables typically do not have any input parameters to optimize. Therefore, we focus on the taggers and groomers, and their combination with shape observables, in this section.

Optimizing at a single p_T : We show in Figure 39 the performance of the top taggers, using just the reconstructed top mass as the discriminating variable, with all input parameters optimized to the $p_T = 1.5 - 1.6$ TeV bin, relative to the performance optimized at each p_T . We see that while the performance degrades by about 50% when the high- p_T optimized points are used at other momenta, this is only an order-one adjustment of the tagger performance, with trimming and the Johns Hopkins tagger degrading the most. The jagged behaviour of the points is due to the finite resolution of the scan. We also observe a particular effect asso-

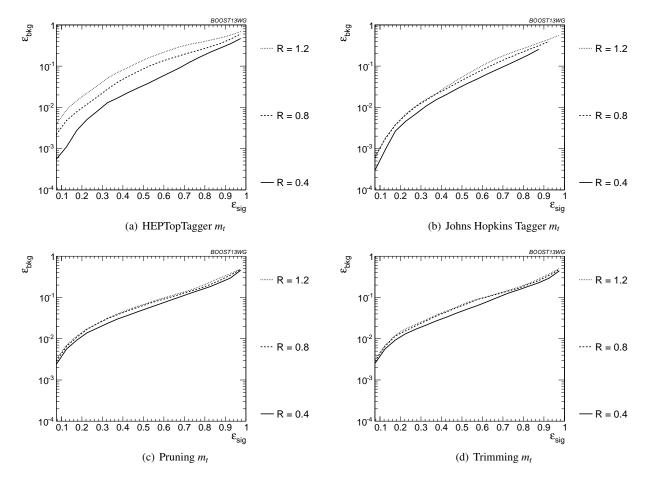


Fig. 29 Comparison of top mass performance of different taggers at different R in the $p_T = 1.5 - 1.6$ TeV bin.

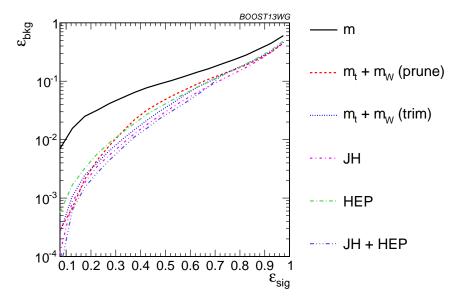


Fig. 30 The performance of the various taggers in the $p_T = 1 - 1.1$ TeV bin using the anti- k_T R=0.8 algorithm. For the groomers a BDT combination of the reconstructed m_t and m_W are used. Also shown is a multivariable combination of all of the JH and HEPTopTagger outputs. The ungroomed mass performance is shown for comparison.

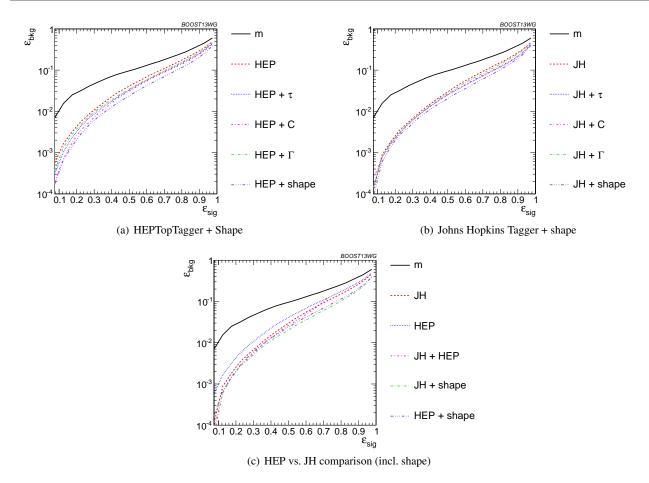


Fig. 31 The performance of BDT combinations of the JH and HepTopTagger outputs with various shape observables in the $p_T = 1 - 1.1$ TeV bin using the anti- k_T R=0.8 algorithm. Taggers are combined with the following shape observables: $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$, $C_2^{(\beta=1)} + C_3^{(\beta=1)}$, T_{Qjet} , and all of the above (denoted "shape").

ciated with using suboptimal taggers: since taggers some 145 times fail to return a top candidate, parameters optimized 46 for a particular efficiency ε_S at $p_T=1.5-1.6$ TeV may 147 not return enough signal candidates to reach the same efi148 ficiency at a different p_T . Consequently, no point appears 49 for that p_T value. This is not often a practical concern, account the largest gains in signal discrimination and significance are for smaller values of ε_S , but it is something that must be considered when selecting benchmark tagger parameters and signal efficiencies.

The degradation in performance is more pronounced for the BDT combinations of the full tagger outputs, shown in 56 Figure 40), particularly at very low signal efficiency where 57 the optimization picks out a cut on the tail of some distribution that depends precisely on the p_T/R of the jet. Onca 58 again, trimming and the Johns Hopkins tagger degrade more 59 markedly. Similar behaviour holds for the BDT combina 100 tions of tagger outputs plus all shape observables.

Optimizing at a single *R***:** We perform a similar analysis₁₆₃ optimizing tagger parameters for each signal efficiency at₆₄

R=1.2, and then use the same parameters for smaller R, in the p_T 1.5-1.6 TeV bin. In Figure 41 we show the ratio of the performance of the top taggers, using just the reconstructed top mass as the discriminating variable, with all input parameters optimized to the R=1.2 values compared to input parameters optimized separately at each radius. While the performance of each observable degrades at small $\varepsilon_{\rm sig}$ compared to the optimized search, the HEPTopTagger fares the worst as the observed is quite sensitive to the selected value of R. It is not surprising that a tagger whose top mass reconstruction is susceptible to background-shaping at large R and p_T would require a more careful optimization of parameters to obtain the best performance.

The same holds true for the BDT combinations of the full tagger outputs, shown in Figure 42). The performance for the sub-optimal taggers is still within an O(1) factor of the optimized performance, and the HEPTopTagger performs better with the combination of all of its outputs relative to the performance with just m_t . The same behaviour holds for the BDT combinations of tagger outputs and shape

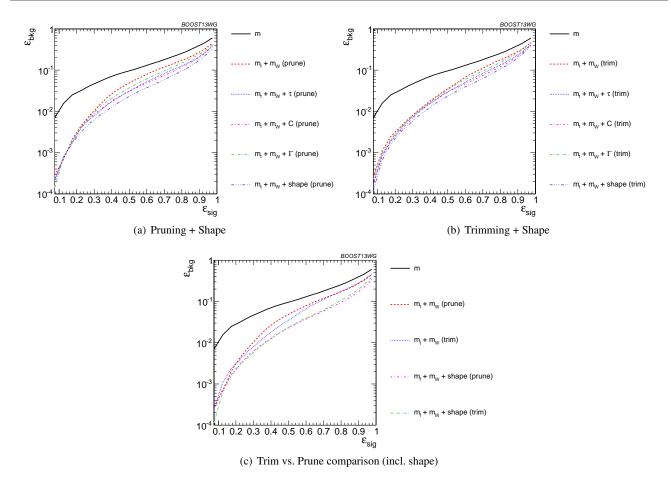


Fig. 32 The performance of the BDT combinations of the trimming and pruning outputs with various shape observables in the $p_T = 1 - 1.1$ TeV bin using the anti- k_T R=0.8 algorithm. Groomer mass outputs are combined with the following shape observables: $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$, $C_2^{(\beta=1)} + C_3^{(\beta=1)}$, Γ_{Qjet} , and all of the above (denoted "shape").

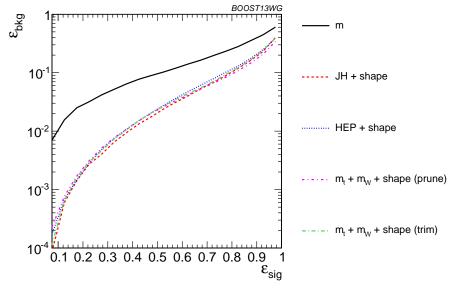


Fig. 33 Comparison of the performance of the BDT combinations of all the groomer/tagger outputs with all the available shape observables in the $p_T=1-1.1$ TeV bin using the anti- k_T R=0.8 algorithm. Tagger/groomer outputs are combined with all of the following shape observables: $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$, $C_2^{(\beta=1)} + C_3^{(\beta=1)}$, Γ_{Qjet} .

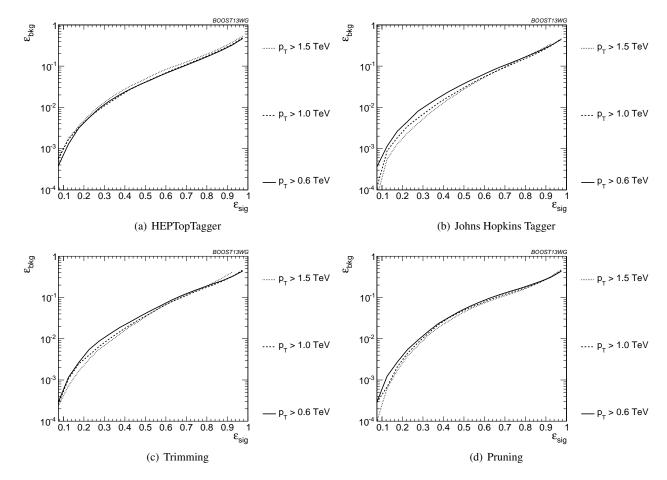


Fig. 34 Comparison of BDT combination of tagger performance at different p_T using the anti- k_T R=0.8 algorithm.

observables.

Optimizing at a single efficiency: The strongest assump¹⁻⁸⁹ tion we have made so far is that the taggers can be reop¹⁻⁹⁰ timized for each signal efficiency point. This is useful for making a direct comparison of the power of different top tagging algorithms, but is not particularly practical for the LHC analyses. We now consider the effects when the tagger inputs are optimized once, in the $\varepsilon_S = 0.3 - 0.35$ bin, and then used to determine the full ROC curve. We do this in the $p_T 1 - 1.1$ TeV bin and with R = 0.8.

The performance of each tagger, normalized to its period formance optimized in each bin, is shown in Figure 43 forfor cuts on the top mass and W mass, and in Figure 44 for BDTros combinations of tagger outputs and shape variables. In bothoo plots, it is apparent that optimizing the taggers in the 0.3_{200} 0.35 efficiency bin gives comparable performance over eficin ficiencies ranging from 0.2-0.5, although performance decogrades at small and large signal efficiencies. Pruning appears to give especially robust signal-background discrimination without re-optimization, possibly due to the fact that there are no absolute distance or p_T scales that appear in the algo-206

rithm. Figures 43 and 44 suggest that, while optimization at all signal efficiencies is a useful tool for comparing different algorithms, it is not crucial to achieve good top-tagging performance in experiments.

7.5 Conclusions

We have studied the performance of various jet substructure observables, groomed masses, and top taggers to study the performance of top tagging at different p_T and jet radius parameter. At each p_T , R, and signal efficiency working point, we optimize the parameters for those observables with tuneable inputs. Overall, we have found that these techniques, individually and in combination, continue to perform well at high p_T , which is important for future LHC running. In general, the John Hopkins tagger performs best, while jet grooming algorithms under-perform relative to the best top taggers due to the lack of an optimized W-identification step. Tagger performance can be improved by a further factor of 2-4 through combination with jet substructure observables such as τ_{32} , C_3 , and Qjet mass volatility; when combined with jet substructure observables, the performance of vari-

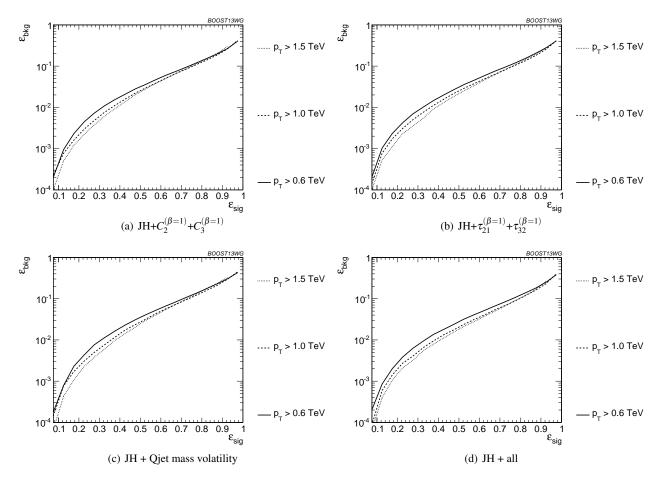


Fig. 35 Comparison of BDT combination of JH tagger + shape at different p_T using the anti- k_T R=0.8 algorithm.

ous groomers and taggers becomes very comparable, sug2220 gesting that, taken together, the observables studied are sen230 sitive to nearly all of the physical differences between top231 and QCD jets. A small improvement is also found by com232 bining the Johns Hopkins and HEPTopTaggers, indicating33 that different taggers are not fully correlated.

Comparing results at different p_T and R, top tagging performance is generally better at smaller R due to less contantion ination from uncorrelated radiation. Similarly, most observables perform better at larger p_T due to the higher degreer of collimation of radiation. Some observables fare worse at higher p_T , such as the N-subjettiness ratio τ_{32} and the Qiet mass volatility Γ , as higher- p_T QCD jets have more, harder emissions that fake the top jet substructure. The HEPTopalager is also worse at large p_T due to the tendency of the tagger to shape backgrounds around the top mass. The p_T - and R-dependence of the multivariable combinations is dominated by the p_T - and R-dependence of the top mass reconstruction component of the tagger/groomer.

Finally, we consider the performance of various observa-246 able combinations under the more realistic assumption that the input parameters are only optimized at a single p_T , R, QE48

signal efficiency, and then the same inputs are used at other working points. Remarkably, the performance of all observables is typically within a factor of 2 of the fully optimized inputs, suggesting that while optimization can lead to substantial gains in performance, the general behaviour found in the fully optimized analyses extends to more general applications of each variable. In particular, the performance of pruning typically varies the least when comparing suboptimal working points to the fully optimized tagger due to the scale-invariant nature of the pruning algorithm.

8 Summary & Conclusions

In this report we have attempted to understand the degree to which the discriminatory information in various jet substructure observables/taggers overlaps, and how this varies as a function of the parameters of the jets, such as their p_T and radius. This has been done by combining the variables into BDT discriminants, and comparing the background rejection power of this discriminant to the rejection power achieved by the individual variables. The performance of "all variables" BDT discriminants has also been investigated,

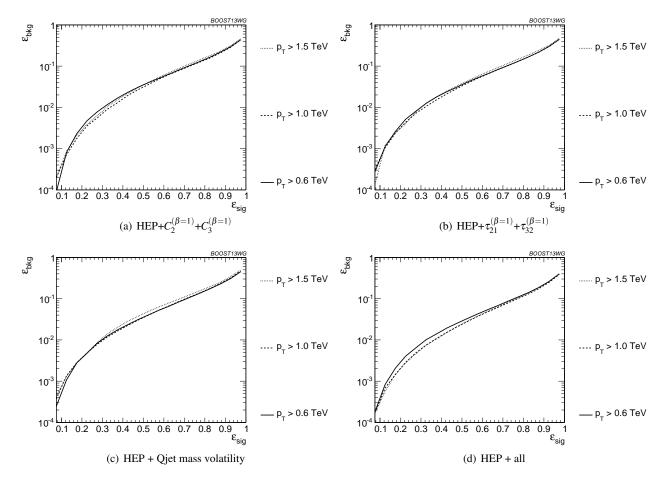


Fig. 36 Comparison of BDT combination of HEP tagger + shape at different p_T using the anti- k_T R=0.8 algorithm.

to understand the potential of the "ultimate" tagger where "all" available information (at least, all of that provided by the variables considered) is used.

Ideas for general conclusions:

- It is clear from both the q/g tagging and W tagging stud²⁷³ ies that the correlation structure between the observable³⁷⁴ considered is complicated, being both p_T and R dependent.
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Fig. 37 Comparison of tagger and jet shape performance at different radius at $p_T = 1.5$ -1.6 TeV.

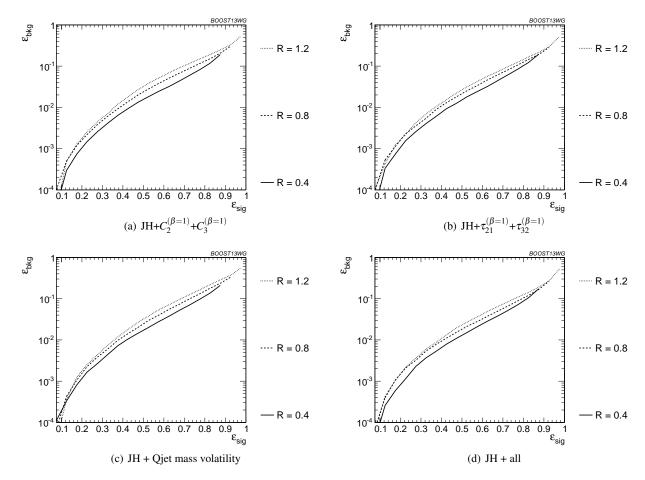


Fig. 38 Comparison of BDT combination of JH tagger + shape at different radius at $p_T = 1.5$ -1.6 TeV.

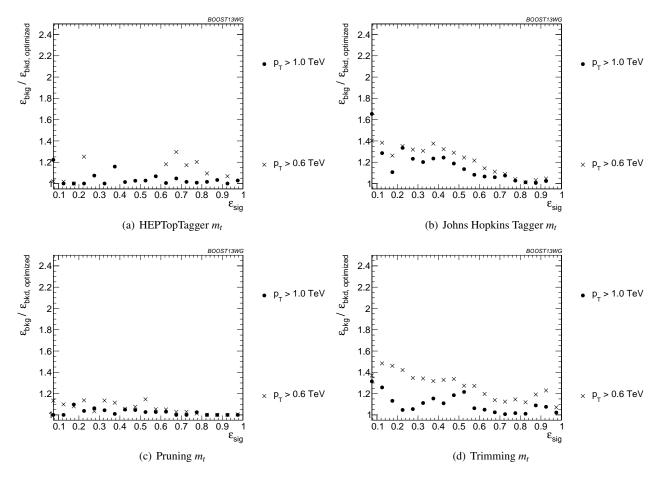


Fig. 39 Comparison of top mass performance of different taggers at different p_T using the anti- k_T R=0.8 algorithm; the tagger inputs are set to the optimum value for $p_T = 1.5 - 1.6$ TeV.

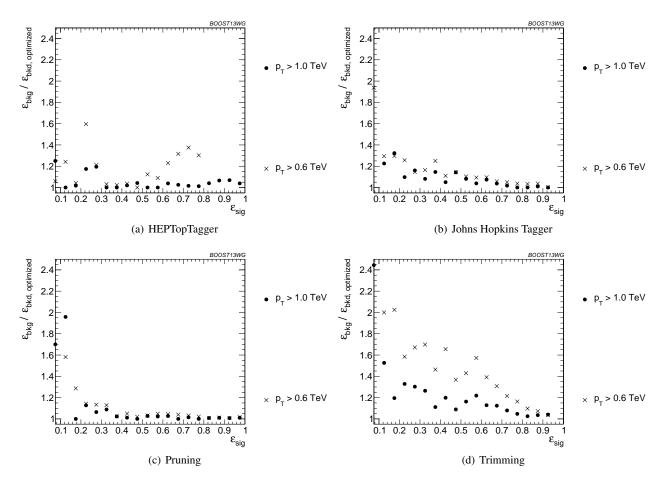


Fig. 40 Comparison of BDT combination of tagger performance at different p_T using the anti- k_T R=0.8 algorithm; the tagger inputs are set to the optimum value for $p_T = 1.5 - 1.6$ TeV.

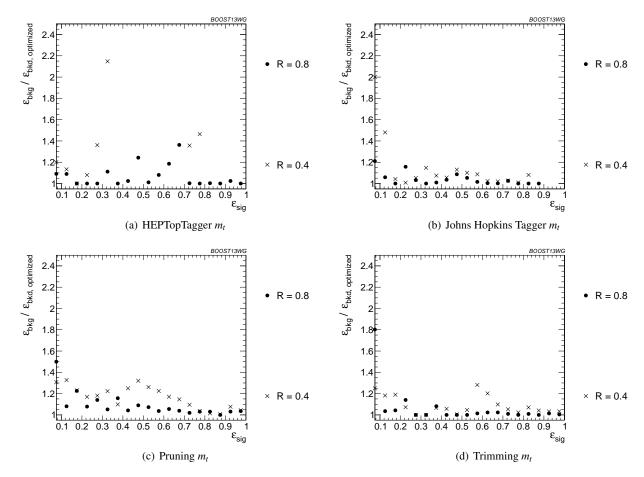


Fig. 41 Comparison of top mass performance of different taggers at different R in the $p_T = 1500 - 1600$ GeV bin; the tagger inputs are set to the optimum value for R = 1.2.

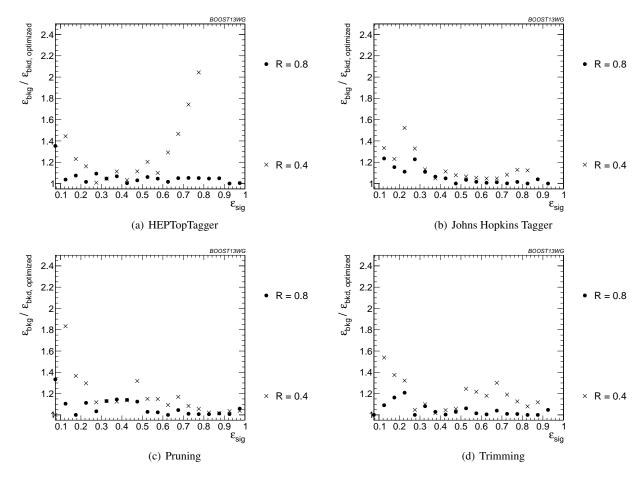


Fig. 42 Comparison of BDT combination of tagger performance at different radius at $p_T = 1.5$ -1.6 TeV; the tagger inputs are set to the optimum value for R = 1.2.



Fig. 43 Comparison of single-variable top-tagging performance in the $p_T = 1 - 1.1$ GeV bin using the anti- k_T , R=0.8 algorithm; the inputs for each tagger are optimized for the $\varepsilon_{\rm sig} = 0.3 - 0.35$ bin.

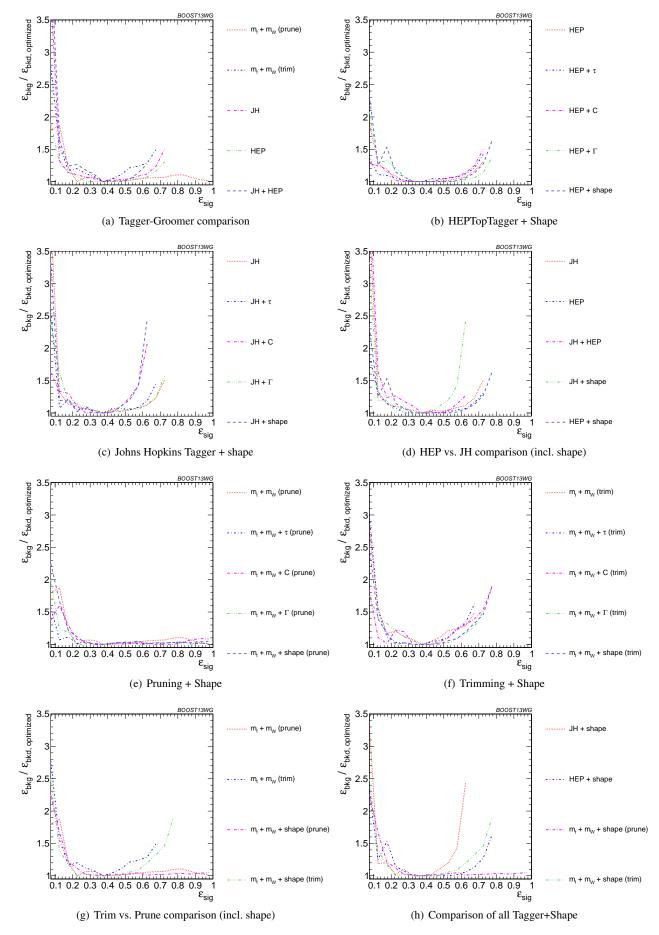


Fig. 44 The BDT combinations in the $p_T=1-1.1$ TeV bin using the anti- k_T R=0.8 algorithm. Taggers are combined with the following shape observables: $\tau_{21}^{(\beta=1)} + \tau_{32}^{(\beta=1)}$, $C_2^{(\beta=1)} + C_3^{(\beta=1)}$, Γ_{Qjet} , and all of the above (denoted "shape"). The inputs for each tagger are optimized for the $\varepsilon_{sig}=0.3-0.35$ bin.