# CS 584: Machine Learning

Spring 2020 Assignment 4

In 2014, Allstate provided the data on Kaggle.com for the Allstate Purchase Prediction Challenge which is open. The data contain transaction history for customers that ended up purchasing a policy. For each Customer ID, you are given their quote history and the coverage options they purchased.

The data is available on the Blackboard as Purchase Likelihood.csv.

- 1. It contains 665,249 observations on 97,009 unique Customer ID.
- 2. The nominal target variable is **insurance** which has these categories 0, 1, and 2
- 3. The nominal features are (categories are inside the parentheses):
  - a. **group\_size**. How many people will be covered under the policy (1, 2, 3 or 4)?
  - b. **homeowner**. Whether the customer owns a home or not (0 = No, 1 = Yes)?
  - c. married\_couple. Does the customer group contain a married couple (0 = No, 1 = Yes)?

### Question 1 (35 points)

You will build a multinomial logistic model with the following model specifications.

- 1. Enter the six effects to the model in this sequence:
  - a. group\_size
  - b. homeowner
  - c. married\_couple
  - d. group size \* homeowner
  - e. group\_size \* married\_couple
  - f. homeowner \* married couple
- 2. Include the Intercept term in the model
- 3. The optimization method is Newton
- 4. The maximum number of iterations is 100
- 5. The tolerance level is 1e-8.
- 6. Use the sympy.Matrix().rref() method to identify the non-aliased parameters

Please answer the following questions based on your model.

a) (5 points) List the aliased columns that you found in your model matrix.

```
group_size_4
homeowner_1
married_couple_1
group_size_4* homeowner_0
group_size_1* homeowner_1
group_size_2* homeowner_1
```

```
group_size_3* homeowner_1
group_size_4* homeowner_1
group_size_4* married_couple_0
group_size_1* married_couple_1
group_size_2* married_couple_1
group_size_3* married_couple_1
group_size_4* married_couple_1
homeowner_0* married_couple_1
homeowner_1* married_couple_0
homeowner_1* married_couple_1
```

b) (5 points) How many degrees of freedom does your model have?

Ans. Degrees of Freedom: 2

c) (20 points) After entering each model effect, calculate the Deviance test statistic, its degrees of freedom, and its significance value between the current model and the previous model. List your Deviance test results by the model effects in a table.

#### Ans.

Step	Effect Entered	# Free Parameter	Log-Likelihood	Deviance	Degrees of Freedom	Significance
0	Intercept	2	-595406.7618	Not Applicable		
1	group_size	8	-594912.9735	987.5766	6	4.3478e-210
2	homeowner	10	-591979.0828	5867.7815	2	0.0
3	married_couple	12	-591936.7938	84.5780	2	4.3064e-19
4	group_size * homeowner	18	-591809.7547	254.0781	6	5.5121e-52
5	group_size * married_couple	24	-59118.4835	1382.5423	6	1.4597e-295
6	homeowner * married_couple	26	-591105.4931	25.9808	2	2.2821e-06

d) (5 points) Calculate the Feature Importance Index as the negative base-10 logarithm of the significance value. List your indices by the model effects.

Effect Entered	Importance		
Intercept	Not Applicable		
group_size	209.04		
homeowner	inf		
married_couple	18.04		
group_size * homeowner	51.04		
group_size * married_couple	294.8357		
homeowner * married_couple	5.6417		

# Question 2 (25 points)

Please answer the following questions based on your multinomial logistic model in Question 1.

a) (10 points) For each of the sixteen possible value combinations of the three features, calculate the predicted probabilities for insurance = 0, 1, 2 based on your multinomial logistic model. List your answers in a table with proper labeling.

	group_size	homeowner	married_couple	insurance = 0	insurance = 1	insurance = 2
0	1	0	0	0.257582	0.591653	0.150765
1	1	0	1	0.328060	0.510687	0.161253
2	1	1	0	0.180464	0.686085	0.133452
3	1	1	1	0.217257	0.628228	0.154515
4	2	0	0	0.279425	0.550953	0.169623
5	2	0	1	0.203284	0.647446	0.149269
6	2	1	0	0.249383	0.597778	0.152838
7	2	1	1	0.161437	0.701504	0.137059
8	3	0	0	0.237434	0.654601	0.107965
9	3	0	1	0.240406	0.597961	0.161632
10	3	1	0	0.282651	0.603586	0.113763
11	3	1	1	0.260167	0.562521	0.177312
12	4	0	0	0.304008	0.595211	0.100781
13	4	0	1	0.193714	0.673257	0.133029
14	4	1	0	0.505939	0.406206	0.087855
15	4	1	1	0.332066	0.531139	0.136796

b) (5 points) Based on your answers in (a), what value combination of group\_size, homeowner, and married\_couple will maximize the odds value Prob(insurance = 1) / Prob(insurance = 0)? What is that maximum odd value?

#### Ans.

- Maximum odd value Prob(insurance=1)/Prob(insurance=0) is 4.3453
- Value combination of the features with maximum odds value

p group size: 2
p homeowner: 1
p married couple: 1

c) (5 points) Based on your model, what is the odds ratio for group\_size = 3 versus group\_size = 1, and insurance = 2 versus insurance = 0?
 (Hint: The odds ratio is this odds (Prob(insurance = 2) / Prob(insurance = 0) | group\_size = 3) divided by this odds ((Prob(insurance = 2) / Prob(insurance = 0) | group\_size = 1).)

#### Ans.

- The odds ratio for group\_size = 3 versus group\_size = 1, and insuran ce = 2 versus insurance = 0 is 1.0249543364157785
- d) (5 points) Based on your model, what is the odds ratio for homeowner = 1 versus homeowner = 0, and insurance = 0 versus insurance = 1?

#### Ans.

• The odds ratio for homeowner = 1 versus homeowner = 0, and insurance = 0 versus insurance = 1 is 0.6232245044401726

# Question 3 (40 points)

You will build a Naïve Bayes model without any smoothing. In other words, the Laplace/Lidstone alpha is zero. Please answer the following questions based on your model.

a) (5 points) Show in a table the frequency counts and the Class Probabilities of the target variable.

insurance	0	1	2
Frequency Count	143691	426067	95491
Class Probability	0.215996	0.640462	0.143542

b) (5 points) Show the crosstabulation table of the target variable by the feature group\_size. The table contains the frequency counts.

Ans.

group size	insurance				
group_size	0	1	2		
1	115460	329552	74293		
2	25728	91065	19600		
3 2282		5069	1505		
4	221	381	93		

c) (5 points) Show the crosstabulation table of the target variable by the feature homeowner. The table contains the frequency counts.

Ans.

homoownon	insurance			
homeowner	0	1	2	
0	78659	183130	46734	
1	65032	242937	48757	

d) (5 points) Show the crosstabulation table of the target variable by the feature married\_couple. The table contains the frequency counts.

Ans.

married sounds	insurance			
married_couple	0	1	2	
0	117110	333272	75310	
1	26581	92795	20181	

e) (5 points) Calculate the Cramer's V statistics for the above three crosstabulations tables. Based on these Cramer's V statistics, which feature has the largest association with the target insurance?

Ans.

• Cramer's V:

group size: 0.027102014055820786
 homeowner: 0.09708641964781962
 married couple: 0.03242164583520746

Based on the Cramer's V value,  $\underline{\text{homeowner}}$  has highest cramer's V value so homeowner has largest association with the target.

f) (10 points) For each of the sixteen possible value combinations of the three features, calculate the predicted probabilities for insurance = 0, 1, 2 based on the Naïve Bayes model. List your answers in a table with proper labeling.

Ans.

	group_size	homeowner	married_couple	ins_0	ins_1	ins_2
0	1	0	0	0.227037	0.627593	0.145370
1	1	0	1	0.214391	0.637467	0.148142
2	1	1	0	0.205588	0.654128	0.140284
3	1	1	1	0.193842	0.663414	0.142744
4	2	0	0	0.238441	0.614462	0.147097
5	2	0	1	0.225342	0.624635	0.150024
6	2	1	0	0.216281	0.641528	0.142192
7	2	1	1	0.204079	0.651128	0.144794
8	3	0	0	0.250201	0.601084	0.148715
9	3	0	1	0.236653	0.611546	0.151801
10	3	1	0	0.227342	0.628652	0.144006
11	3	1	1	0.214684	0.638559	0.146756
12	4	0	0	0.262308	0.587475	0.150218
13	4	0	1	0.248318	0.598215	0.153467
14	4	1	0	0.238767	0.615513	0.145720
15	4	1	1	0.225656	0.625720	0.148624

g) (5 points) Based on your model, what value combination of group\_size, homeowner, and married\_couple will maximize the odds value Prob(insurance = 1) / Prob(insurance = 0)? What is that maximum odd value?

#### Ans.

- Maximum odd value Prob(insurance=1)/Prob(insurance=0) is 3.4224
- Value combination of the features with maximum odds value

p group size: 1
p homeowner: 1

married\_couple: 1