defined by NFA is The strings in I will be rejected by the NFA above To find I, we have to find the cases when the strings are rejected. The NFA rejects strings which include 'bb+' Thus, the set of all strings which include 'bbt' is I. Now, we have to construct an NFA which accepts strings including 'bb+' The NFA accepts strings including 'bbt'. Thus, the NFA accepts I.

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A language is regular if there exists DFA which accepts the language.

Since DFA is equivalent to NFA, a language is regular if there exists NFA which accepts the language.

Let language L is finite language.

If $L = \phi$ or $L = \{\lambda\}$, then there exist NFA or DFA which accept L. So, L is regular.

The state of NFA or DFA is final state, and for $L = \phi$, the state ϕ is both initial state and final state of NFA or DFA.

Assume $L = \{w_1, w_2, \dots, w_i, \dots, w_n\}$. $(\forall n \in \mathbb{N}, \text{ and } n \text{ is a finite number.})$

We can construct DFAs for each wi in L. (i=1,2,...,n). Then there are 'n' numbers of DFAs, and each DFA accepts each wi in L. (i=1,2,3,...,n).

After constructing DFAs for each string in L, construct new initial state given, and connect the given to each initial state of DFAs with x-transition.

(f(given, x) = (g:g is initial state of each DFA).

The initial state of each DFA is now non-initial state of NFA.

Then construct new final state given, and connect each final state of DFAs to given with x-transition (f(gg, x) = Egippags, gg is final state of each DFA).

The final state of each DFA is now non-final state of NFA.

Now there exists an NFA which accepts L. Thus, L is regular.

Then let's add new string with (white) to L. Similar to previous steps, construct a DFA which accepts while. Then connect initial state of NFA to the initial state of DFA for while with λ -transition, and the final state of DFA for while to the final state of NFA with λ -transition. $f(q_NFAi, \lambda) = \{q_{MAII}i\}, g_{MAII}: initial state of DFA for while it initial state of DFA$

f(qwn+1f, x) = {qNFAf}, qwn+1f: final state of DFA for Wm.

Now, initial state and final state of DFA for WAHI are non-initial state and non-final state of NFA.

There exists an NFA which accepts LUEWn+13.
Thus, LUEWn+13 is regular.

Since n can be any finite number, and there exists NFA for L, we proved that finite languages are regular by induction.

Therefore, all finite languages are regular.

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