1. A turing machine M can either change the tape symbol or move the read/write head, but not both on each move.

 $M = (Q, \Sigma, \Gamma, \mathcal{E}, \mathcal{G}_0, D, F3.$  $\mathcal{E}: Q \times \Gamma \longrightarrow \{Q \times \Gamma\} \cup \{Q \times \{L, R33\}$ 

We can simulate M by using a standard Turing machine M.

 $\hat{M} = (\hat{Q}, \Sigma, \Gamma, \hat{\mathcal{F}}, \hat{\mathcal{G}}_0, D, \hat{\mathcal{F}}).$ 

First in case of changing the tape symbol, we can stop  $\hat{M}$  after changing the tape symbol.  $f(g_i, a) = f(g_j, b)$ 

 $\hat{f}(\hat{g}_i, a) = \hat{f}(\hat{g}_j, b, R)$  and  $\hat{f}(\hat{g}_j, c) = \hat{f}(\hat{g}_j, c, L)$ 

In case of moving the read/write head, we can just move M without changing the tape symbol.

 $f(g_R, d) = f(g_R, Lor R)$  $f(\hat{g}_R, d) = f(\hat{g}_R, d, Lor R)$ 

Thus, M is simulated by a standard Turing Machine.

2. Let two independent stacks of two-stack upda

NTM NTM are 31 and 31.

Nondetermini Assume two stacks are starting at 2, and the tope is empty. - Stic Turing A move depends on the tops of SL and SR, and Machine results in new values being pushed on SL and SR We will write the top of St to the left of the head and the top of SR to the right of the head of nondeterminatic luring i) Initiation  $f(g_0, \square) = (g_{05}, \#, R), f(g_0, \#) = g(g_1, S(L_1, L),$  $f(g_{os}, \Omega) = (g_o, \Omega, L) \qquad (g_2, SR_1, R)$ Shi is top of Sh (i=1,2,3,...) ii) for pushing new values. E(qi, D) = (qi 51k+1, L) for 5L f(q1, D) = (qm 5km+1, R). f(gm D) = (gn, D, L) for SR iii) for a movement, depending on the tops f(ga, 5Li) = (gas, 5Li, L) f (gas, Di) = (Za, D, R) (for 5L) f (gd, 5 Rk) = (gds, 4 k, R) (for SR) δ(qds, □) = (qd, □, L)

iv) For poping tops of Sr and SR.

TM: Turing  $f(g_i, SL_j) = (g_{i+1}, D, L)$ Machine  $f(g_{i}) = (g_{i+1}, D, R)$  for SL

 $f(g_k, SRe) = (g_{k+1}, D, R)$  $f(g_{k+1}, D) = (g_{k+1}, D, L)$  for SR

Since every automation in nondeterministic TM is in an automation of two-stack npda, two-stack npda is equivalent to nondeterministic Turing machine.

By Theorem 10.2 in the textbook, nondeterministic Turing machine is equivalent to standard Turing machine.

Therefore, two-stack npdas are equivalent to standard Turing machines.

3. S. and S. are countable sets.

Countable sets can be written by enumeration procedure.

Turing machine can implement the enumeration procedure used in countable sets.

Thus, Countable sets are accepted by Turing machines.

S. USz can be accepted by two - tape Turing machines.

machine or a standard Turing machine with four tracks.

5. x52 can be accepted by two-dimensional Turing machine,

By Theorem 10.3 in the textbook, Turing machinees which accept 5.USz or 5.XSz (but not both) are countable.

Therefore, 5, US, and 5, xS2 are countable.

MOCKEUK