

1.  $L = \{a^x b^y c^z : z = x + y\}$

$$S \rightarrow A$$

$$A \rightarrow aAc \mid B \mid \lambda$$

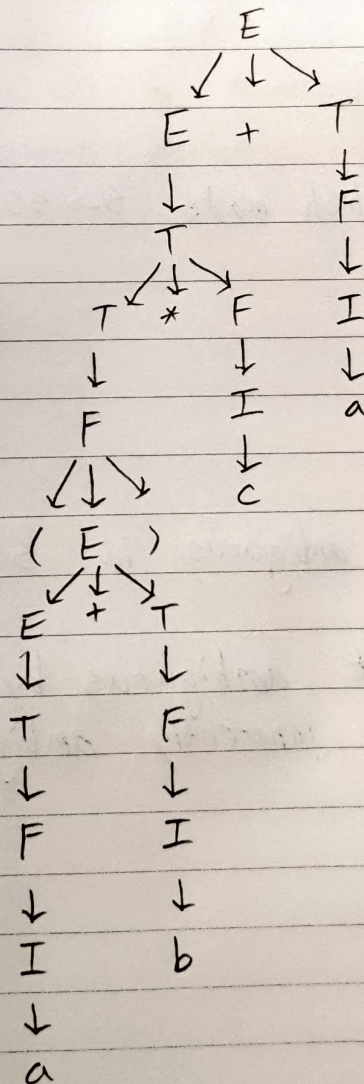
$$B \rightarrow bBc \mid \lambda$$

2.  $L = \{a^n b^n : n \text{ is not multiple of } 3\}$

$$S \rightarrow aS_1b \mid aaS_1bb$$

$$S_1 \rightarrow aaaS_1bbb \mid \lambda$$

3.





4. To prove the language is not inherently ambiguous, we have to find the grammar which is not ambiguous.

$S \rightarrow SS | aSb | \lambda$  is ambiguous

$S \Rightarrow SS \Rightarrow aSbS \Rightarrow aaSbbS \Rightarrow aabb$

$S \Rightarrow aSb \Rightarrow aaSbb \Rightarrow aabb$ .

Let's find equivalent grammar which is not ambiguous.

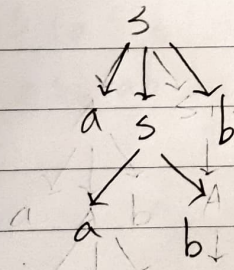
Let  $S \rightarrow SS | aSb | Aab$

$S_0 \rightarrow \lambda$

Let  $A \rightarrow aAb | B$   $S_1 \rightarrow aSb$

Let  $B \rightarrow \lambda$   $aabb$ .

In case of 'aabb' which made  $S \rightarrow SS | aSb | \lambda$  ambiguous,



So, 'aabb' is not ambiguous in  $S \rightarrow SS | aSb | \lambda$ .

As the language is not ambiguous by  $S \rightarrow SS | aSb | \lambda$ , the language is not inherently ambiguous.



5. Since  $G$  is a context-free grammar where every variable occurs on the left side of at most one production, the grammar  $G$  will generate one leftmost derivation in the derivation tree when it terminals.

As ambiguity implies the existence of two or more leftmost or rightmost derivations according to definition 5.5 in the textbook,  $G$  has only one leftmost derivation so that  $G$  is unambiguous.

Thus,  $G$  is unambiguous because it has only one leftmost derivation in derivation tree of  $G$ .