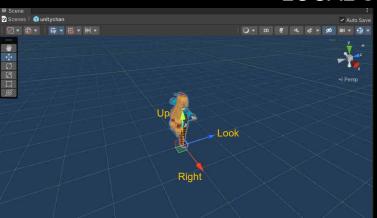
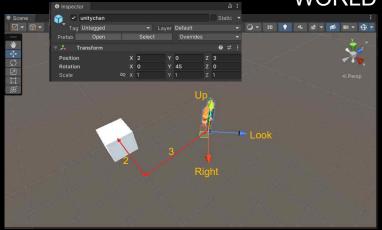
# PROJECTION 변환 행렬

### LOCAL SPACE

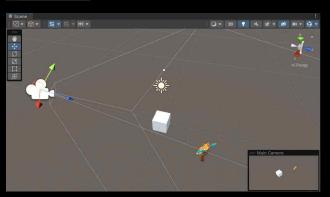


### **WORLD SPACE**

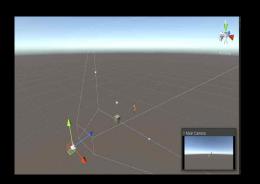


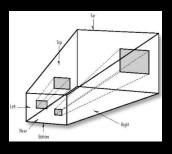


## VIEW (CAMERA, EYE) SPACE

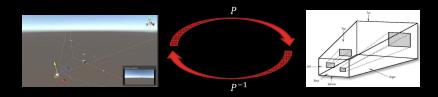


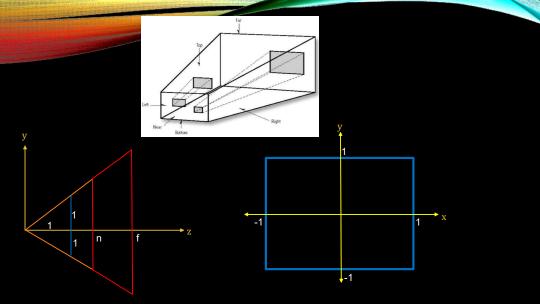
# PROJECTION SPACE (HOMOGENOUS CLIP SPACE)

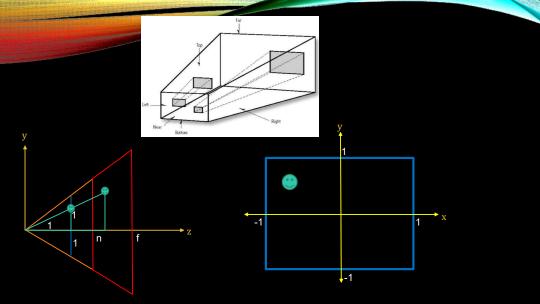


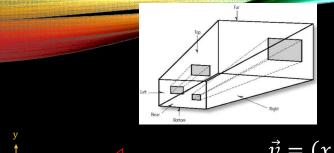


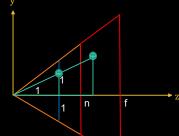
### **PROJECTION MATRIX**







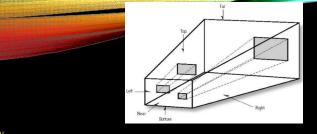


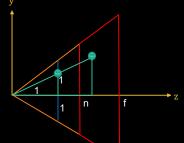


$$\vec{v} = (x, y, z)$$

$$X = \frac{x}{z}$$

$$'=$$



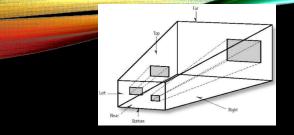


$$\vec{v} = (x, y, z)$$

$$X = \frac{x}{r_z}$$

$$Y = \frac{y}{r_z}$$

$$r = \frac{800}{600} = 1$$

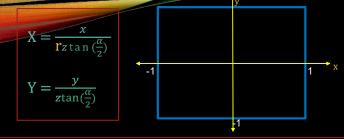


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$$\vec{v} = (x, y, z)$$

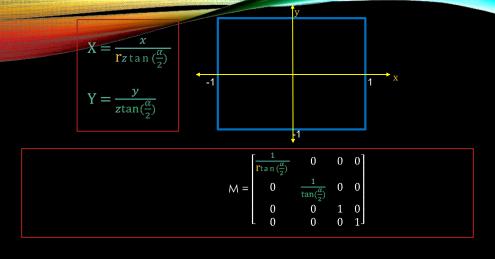
$$X = \frac{x}{r_{z \tan \left(\frac{\alpha}{2}\right)}}$$

$$\frac{800}{600} = 1.$$

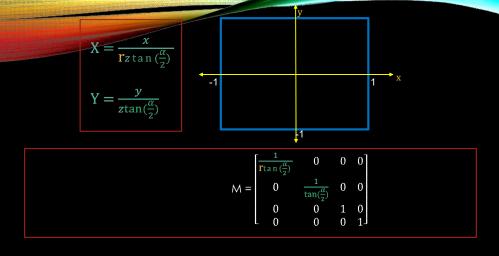


$$\mathsf{M} = \begin{bmatrix} m_{11} & m_{12} & m_{13} & m_{14} \\ m_{21} & m_{22} & m_{23} & m_{24} \\ m_{31} & m_{32} & m_{33} & m_{34} \\ m_{41} & m_{42} & m_{43} & m_{44} \end{bmatrix}$$

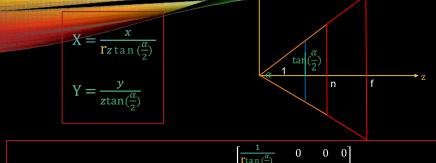
$$X = xm_{11} + ym_{21} + zm_{31} + m_{41}$$
  
$$Y = xm_{12} + ym_{22} + zm_{32} + m_{42}$$



$$\vec{V} = (\frac{x}{\operatorname{rtan}(\frac{\alpha}{2})}, \frac{y}{\operatorname{tan}(\frac{\alpha}{2})}, z, 1)$$

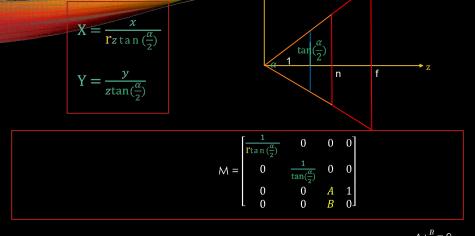


$$\vec{V} = (\frac{x}{\operatorname{\mathsf{rtan}}(\frac{\alpha}{2})}, \frac{y}{\operatorname{\mathsf{tan}}(\frac{\alpha}{2})}, \mathbf{z}, \mathbf{z})$$



$$M = \begin{bmatrix} \frac{1}{\operatorname{rtan}(\frac{\alpha}{2})} & 0 & 0 & 0\\ 0 & \frac{1}{\tan(\frac{\alpha}{2})} & 0 & 0\\ 0 & 0 & A & 1\\ 0 & 0 & B & 0 \end{bmatrix}$$

$$\vec{V} = (\frac{x}{\operatorname{rtan}(\frac{\alpha}{2})}, \frac{y}{\tan(\frac{\alpha}{2})}, \operatorname{Az+B}, z) \qquad \qquad \vec{V'} = (\frac{x}{\operatorname{rZtan}(\frac{\alpha}{2})}, \frac{y}{\operatorname{Ztan}(\frac{\alpha}{2})}, \operatorname{A+\frac{B}{z'}}, 1)$$



$$\vec{V} = (\frac{x}{\operatorname{rtan}(\frac{\alpha}{2})}, \frac{y}{\operatorname{tan}(\frac{\alpha}{2})}, \operatorname{Az} + B, z) \qquad \qquad \vec{V'} = (\frac{x}{\operatorname{rztan}(\frac{\alpha}{2})}, \frac{y}{\operatorname{ztan}(\frac{\alpha}{2})}, \operatorname{A} + \frac{B}{z}, 1) \qquad \qquad \operatorname{A} + \frac{B}{h} = 0$$

$$\operatorname{A} + \frac{B}{h} = 0$$

$$\operatorname{A} + \frac{B}{h} = 1$$

$$\vec{V} = \left(\frac{x}{\operatorname{rtan}\left(\frac{\alpha}{2}\right)}, \frac{y}{\tan\left(\frac{\alpha}{2}\right)}, \operatorname{Az} + B, z\right) \qquad \qquad \vec{V'} = \left(\frac{x}{\operatorname{rZtan}\left(\frac{\alpha}{2}\right)}, \frac{y}{\operatorname{Ztan}\left(\frac{\alpha}{2}\right)}, \operatorname{A} + \frac{B}{z'}, 1\right)$$

$$A + \frac{B}{n} = 0$$

$$A = \frac{f}{f - n}$$

$$B = \frac{-nf}{f - n}$$

$$A + \frac{B}{f} = 1$$

$$\vec{v} = \begin{bmatrix} x & y & z & 1 \end{bmatrix} \qquad M = \begin{bmatrix} \frac{1}{\operatorname{rtan}(\frac{\alpha}{2})} & 0 & 0 & 0 \\ 0 & \frac{1}{\operatorname{tan}(\frac{\alpha}{2})} & 0 & 0 \\ 0 & 0 & \frac{f}{f-n} & 1 \\ 0 & 0 & \frac{-nf}{f-n} & 0 \end{bmatrix}$$