INDIAN INSTITUTE OF TECHNOLOGY GUWAHATI
DEPARTMENT OF MECHANICAL ENGINEERING
Guwahati – 781 039, Assam, India

ME 543 Computational Fluid Dynamics
Computer Assignment – 3A
Due Date for Submission: 27.09.15 (Sunday), No Late Submission

Solve the following partial differential equation using the finite difference method with the specified boundary conditions for the geometry with **100×100** grid size as shown in the figure.

$$\frac{\partial^2\psi}{\partial x^2}+\frac{\partial^2\psi}{\partial y^2}=-\omega$$

$$u\frac{\partial\omega}{\partial x}+v\frac{\partial\omega}{\partial y}=\frac{1}{\mathrm{Re}}\left(\frac{\partial^2\omega}{\partial x^2}+\frac{\partial^2\omega}{\partial y^2}\right)$$

$$u=\frac{\partial\psi}{\partial y}\,,\quad v=-\frac{\partial\psi}{\partial x}$$

Convergence Criteria: Find the maximum error of stream function and vorticity and reduce that maximum error to 10^{-6}. Apply the finite difference discretization to replace all derivatives with the corresponding central difference expressions with uniform grid $M \times N$ and *write the discretized equations of the governing equations and boundary conditions of stream function & vorticity in the* ***report***. Write the code in such a way so that you can input the values of Re, M, N. Submit the results and discussion for **Re=100** in terms of streamlines, velocity vectors, u velocity along vertical centerline and v velocity along horizontal centerline. **Email** only the soft copy of the code.

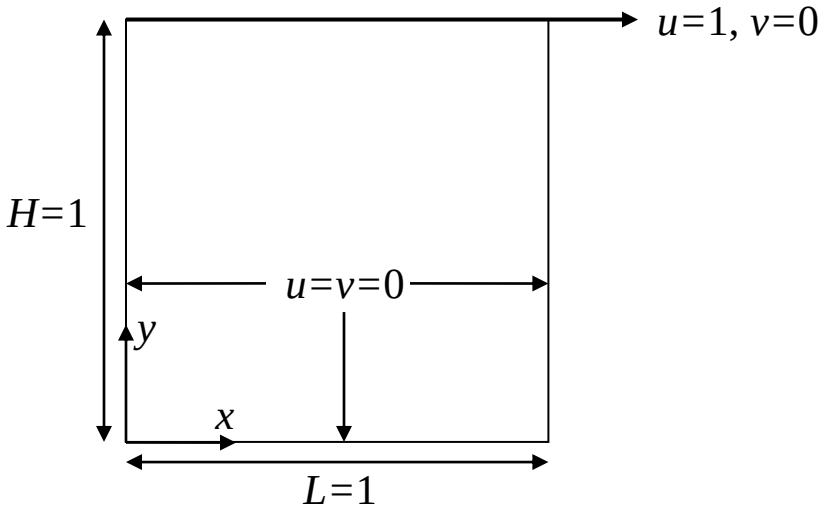

Figure: Flow inside a lid-driven cavity

Reference: U. Ghia, K.N. Ghia, and C. T. Shin, "High-Resolutions for Incompressible Flow Using the Navier-Stokes Equations", Journal of Computational Physics, vol. 48, pp. 387-411, 1982.