

Heuristic Functions



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Contents

- 3.6.1 Heuristics for 8-puzzle
- 3.6.2 Search Cost

Heuristics for 8-puzzle 8数码难题的启发式

- To find shortest solutions by using A*, need a heuristic function that are two commonly used candidates.

要用A*算法找到最短距离的解，需要一个启发式函数，通常有两个候选。

$$h_1 = \text{number of misplaced tiles} = 8.$$

错位棋子的个数

$$h_2 = \text{total Manhattan distance (tiles from desired locations)} = 3+1+2+2+2+3+3+2 = 18$$

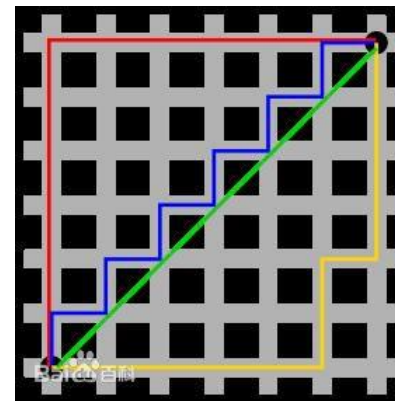
曼哈顿距离之和（每个棋子到目标位置）

7	2	4
5		6
8	3	1

Start state

	1	2
3	4	5
6	7	8

Goal state



Manhattan distance

Search Cost 搜索代价

Search Cost (nodes generated)

d (depth)	Iterative Deepening Search	$A^*(h_1)$	$A^*(h_2)$
2	10	6	6
4	112	13	12
6	680	20	18
8	6384	39	25
10	47127	93	39
12	3644035	227	73
14	-	539	113
16	-	1301	211
18	-	3056	363
20	-	7276	676
22	-	18094	1219
24	-	39135	1641

□ If $h_2(n) \geq h_1(n)$ for all n , then h_2 dominates h_1 and is better for search.

若对于所有的 n , $h_2(n) \geq h_1(n)$, 则 h_2 优于 h_1 , 因而 h_2 更适合搜索。

Thank you for your attention!

