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- ☐ 10.1. Classification
- ☐ 10.2. Regression
- ☐ 10.3. Clustering
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Ranking



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What is Ranking 什么是排名

□ A longer description 较长描述

A ranking is a relationship between a set of items such that, for any two items, the first is either 'ranked higher than', 'ranked lower than' or 'ranked equal to' the second.

排名是一组项之间的关系，即对于任意两个项，满足第一个“排名高于”、“排名低于”或“排名等于”第二个。

□ A shorter description 较短描述

The data transformation in which numerical or ordinal values are replaced by their rank.

排名是一种数据转换，其中数值或者顺序值由其排名来代替。

□ A very short description 极简描述

To order items according to some criterion.

依据某种准则整理数据项。

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- ☐ 10.4.1. How Ranking Works
- ☐ 10.4.2. Major Approaches of Ranking
- ☐ 10.4.3. Applications and Algorithms

A Formal Description of Ranking 一种排名的形式化描述

Let \mathcal{X} denote input space, D an unknown distribution over $\mathcal{X} \times \mathcal{X}$.

设 \mathcal{X} 表示输入空间, D 是 $\mathcal{X} \times \mathcal{X}$ 上的未知分布。

□ Target ranking function: 目标排名函数:

$$f: \mathcal{X} \times \mathcal{X} \rightarrow \mathcal{Y} = \{-1, 0, +1\}$$

where

其中

- $f(x, x') = +1$, if x is ranked higher than x' , 若 x 排名高于 x' ,
- $f(x, x') = -1$, if x is ranked lower than x' , 若 x 排名低于 x' ,
- $f(x, x') = 0$, if both x and x' has same ranking. 若 x 与 x' 二者排名相同。

□ Training data: 训练数据

$$\mathcal{S} = \{(x^{(i)}, x'^{(i)}, y^{(j)}) \mid y^{(j)} = f(x^{(i)}, x'^{(i)}) \in \mathcal{Y}, i \in [1, m], j \in [1, 3]\}$$

A Formal Description of Ranking 一种排名的形式化描述

□ Ranking problem: 排名问题

Given a hypothesis set H of functions mapping $\mathcal{X} \times \mathcal{X}$ to $\mathcal{Y} = \{-1, 0, +1\}$, to select a hypothesis $h \in H$ with the target function f :

给定一个将 $\mathcal{X} \times \mathcal{X}$ 映射到 $\mathcal{Y} = \{-1, 0, +1\}$ 的假设函数集 H ，选择一个具有目标函数 f 的假设 $h \in H$ ：

■ small expected generalization error: 最小预期泛化错误:

$$R(h) = \Pr_{(x, x')} [f(x, x') \neq 0 \wedge (f(x, x')(h(x') - h(x)) \leq 0)]$$

■ empirical pairwise misranking error: 经验性成对误排名错误：

$$\hat{R}(h) = \frac{1}{m} \sum_{i=1}^m 1 ((y^{(i)} \neq 0) \wedge (y^{(i)} (h(x'^{(i)}) - h(x^{(i)})) \leq 0))$$

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Typical Approaches of Ranking 典型的排名方法

□ 1) Score-based approach 基于分值方法

- The predictor is a real-valued function, called *scoring function*.
该预测器是一个实数函数，称为分值函数。
- The scores assigned to input points by this function determine their ranking.
由该函数分派给输入数据点的分值决定其排名。
- This approach is the most widely explored one.
这种方法是研究得最多的一种。

□ 2) Preference-based approach 基于偏好方法

- The predictor is a *preference function*.
该预测器是一个偏好函数。

Contents:

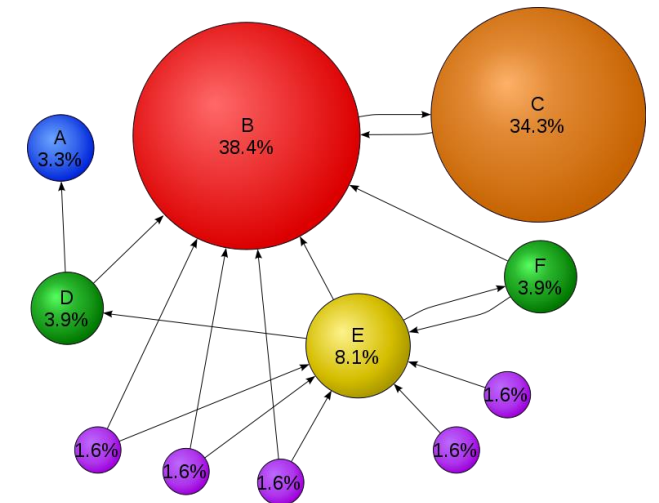
- ☐ 10.4.1. How Ranking Works
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Typical Applications of Ranking 排名的典型应用

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|-----------------------------|--------|
| □ In information retrieval | 信息检索领域 |
| ■ Search engine | 搜索引擎 |
| ■ Document retrieval | 文档检索 |
| ■ Collaborative filtering | 协同式过滤 |
| ■ Sentiment analysis | 情感分析 |
| ■ Computational advertising | 计算广告学 |
| □ In other areas | 其它领域 |
| ■ Machine translation | 机器翻译 |
| ■ Recommender systems | 推荐系统 |
| ■ Computational biology | 计算生物学 |
| ■ Proteomics | 蛋白质组学 |

Case Study: PageRank

- ❑ An algorithm used by Google to rank websites in their search engine, named after Larry Page, one of Google founders.
谷歌用于在其搜索引擎中对网站进行排名的一种算法，以谷歌创始人之一拉里·佩奇的名字命名。
- ❑ PageRank works by counting the number and quality of links to a page to determine how important the website is.
PageRank通过计算网页的链接数量和质量来决定该网站的重要性。
- ❑ The underlying assumption is that more important websites are likely to receive more links from other websites.
其基本假设是：越重要的网站，就会被越多其它网站所链接。



Thank you for your attention!

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