

# Local Search for CSPs



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# Contents

- ☐ 6.4.1 Local Search for CSPs
- ☐ 6.4.2 Min-conflicts Heuristic
- ☐ 6.4.3 Algorithm Solving CSPs by Local Search
- ☐ 6.4.4 Constraint Weighting

### Local Search for CSPs CSPs的局部搜索

- Local search algorithms are also effective in solving many CSPs, using **complete-state formulation**:

局部搜索算法在求解许多CSPs问题中也很有效，采用完整状态形式化：

- Initial state: assign a value for each variable  
初始状态：为每个变量赋值
- Search: change the value of one variable at a time  
搜索：一次改变一个变量的值

### *Example*: 8-queens problem

- Initial state is a random configuration of 8 queens in 8 columns, and each step moves a single queen to a new position in its column.  
初始状态是在8列上随机地摆放8个皇后，然后每一步将一个皇后移动到该列上的新位置。
- Typically, the initial guess violates several constraints, point is to eliminate the violated constraints.  
通常，初始状态会违反若干约束。要点是消除这些违反的约束。

## Min-conflicts Heuristic 最小冲突启发式

- A most obvious heuristic is to select a new value for a variable.

一个最明显的启发式是对一个变量选择一个新的值。

- Features 特点

- Variable selection: randomly select any conflicted variable

变量选择：随机选择任意一个冲突变量

- Value selection: select new value that results in a **minimum number of conflicts** with others

值的选择：选择导致与其它变量呈现最少冲突的新值

- Surprisingly effective for many CSPs 对许多CSPs出奇的有效

- on ***n-queens*** problem, the run time of min-conflicts is roughly *independent of problem size*.

在 $n$ 皇后问题上，最小冲突的运行时间与问题大小基本上无关。

- even on ***million-queens*** problem, it solves in an average of 50 steps, after the initial assignment!

甚至对于百万皇后问题，在初始赋值后，平均50步左右就能得到解！

## Algorithm Solving CSPs by Local Search 局部搜索求解CSPs算法

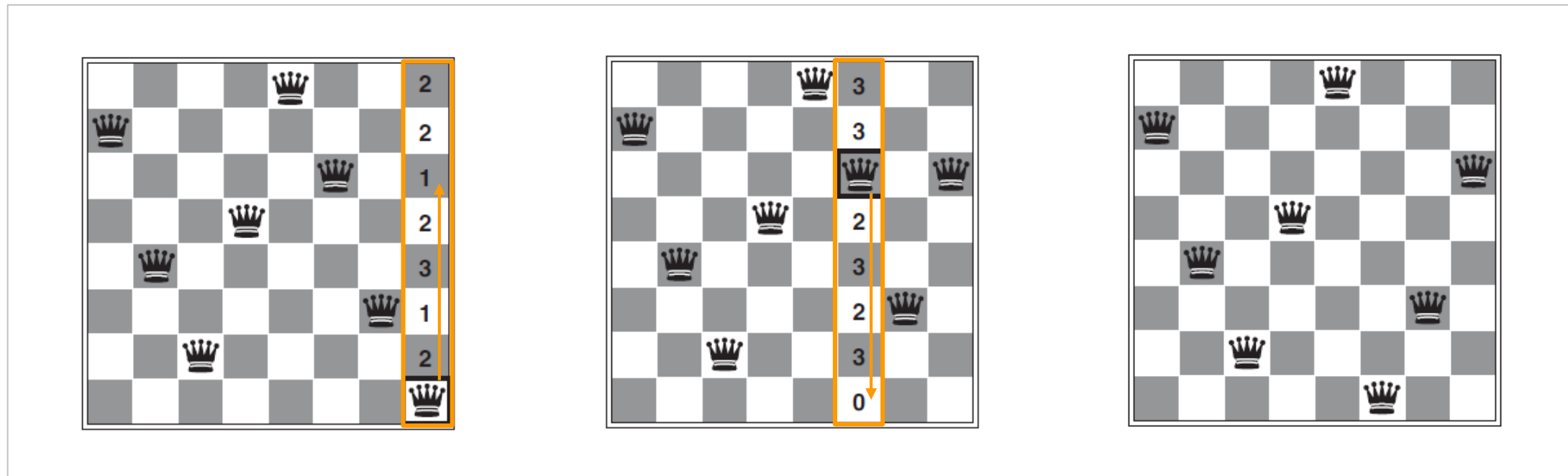
```
function MIN-CONFLICTS(csp, max_steps) returns a solution or failure
  inputs: csp, a constraint satisfaction problem
           max_steps, the number of steps allowed before giving up
  current  $\leftarrow$  an initial complete assignment for csp
  for i = 1 to max_steps do
    if current is a solution for csp then return current
    var  $\leftarrow$  a randomly chosen conflicted variable from csp.VARIABLES
    value  $\leftarrow$  the value v for var that minimizes CONFLICTS(var, v, current, csp)
    set var = value in current
  return failure
```

The initial state may be chosen randomly that chooses a min-conflict value for each variable in turn.

The CONFLICTS function counts the number of constraints violated by a particular value, given the rest of the current assignment.

初始状态可以随机选择，依次为每个变量选择一个最小冲突值。  
给定当前赋值的其余部分，CONFLICTS函数计算特定值违反约束的个数。

## Example: Min-conflicts for an 8-Queens Problem 8皇后问题的最小冲突法



### A two-step solution using min-conflicts 用最小冲突法的两部解决方案

At each stage, a queen is chosen for reassignment in its column. The number of attacking queens is shown in each square. The algorithm moves the queen to the min-conflicts square, breaking ties randomly.

每一阶段，选择一个皇后在该列上重新分配。每个方格显示皇后攻击的数量。  
算法将皇后移到最小冲突的方格内，随机地切断束缚。

## Constraint Weighting 约束加权

### □ Can focus on the important constraints 能聚焦于重要的约束

- Give each constraint a numeric weight,  $W_i$ , initially all 1.  
给定每个约束一个数值权重,  $W_i$ , 初始值都为1。
- At each step, choose a variable/value pair to change, that will result in lowest total weight of all violated constraints.  
每一步, 选择一个变量/值对加以改变, 这将导致所有违反约束的总权重为最低。
- Then, weights are adjusted by incrementing the weight of each constraint that is violated by current assignment.  
然后, 通过增加当前分配所违反的每个约束的权重来调整权重。

### □ Two benefits 两个益处

- Add topography to plateau, making sure that it is possible to improve from the current state  
对高原增加了地势, 确保能够改善当前的状态。
- Also add weight to the constraints that are proving difficult to solve.  
对证明难以求解的约束也增加权重。

Thank you for your attention!

