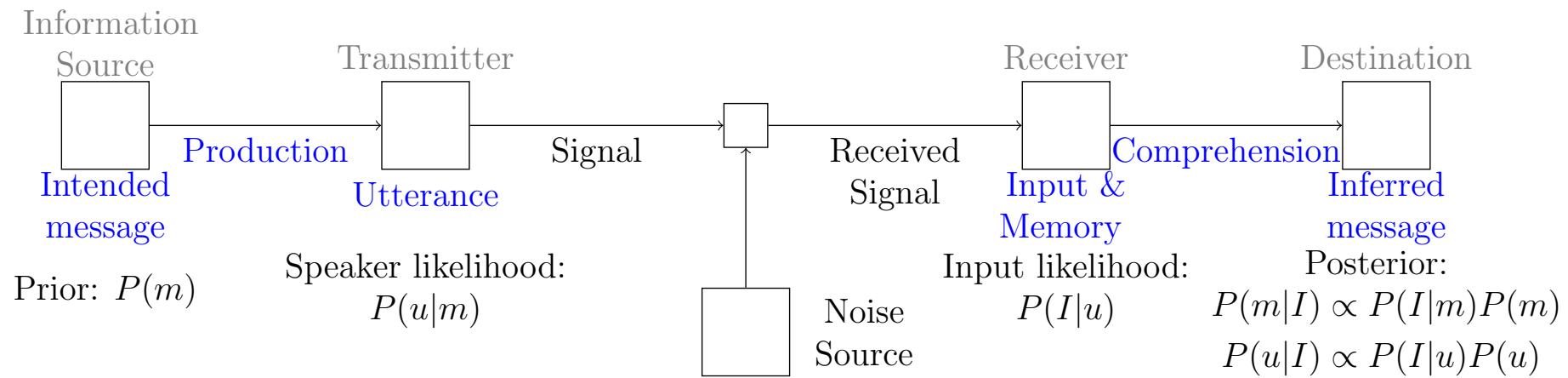


Noisy-channel sentence comprehension theory



Roger Levy

9.19: Computational Psycholinguistics

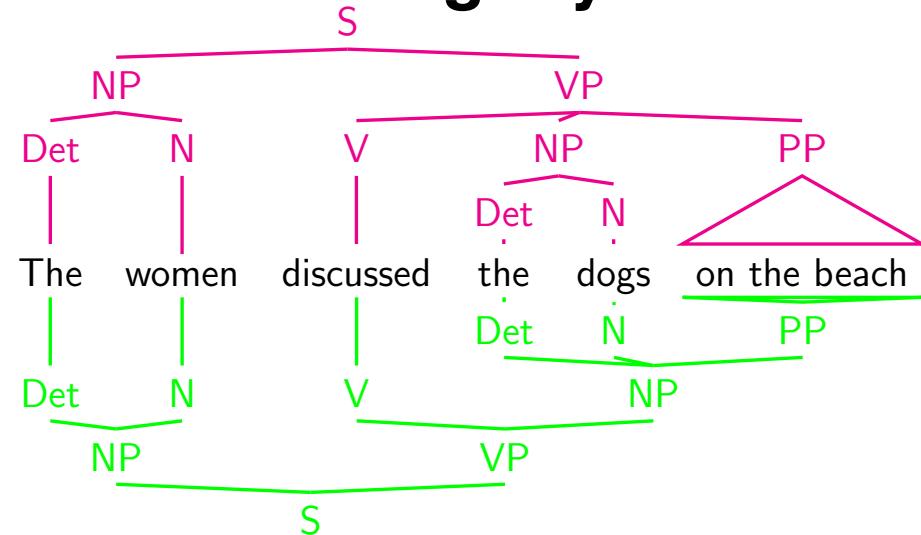
13 November 2023

Today's agenda

- Review principles of rational analysis and its application to theory of language comprehension
- Examine a phenomenon challenging for surprisal theory
- Propose a noisy-channel processing theory, using information theory and probabilistic grammars
- Develop a hypothesis within the theory for the challenging phenomenon
- Empirically test a key prediction of the theory

Challenges for efficient linguistic communication

Ambiguity



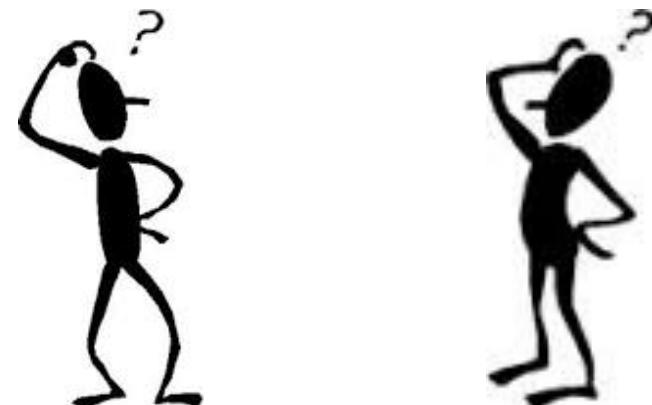
Environmental noise



Memory Limitations



Incomplete knowledge of one's interlocutors



Rational analysis

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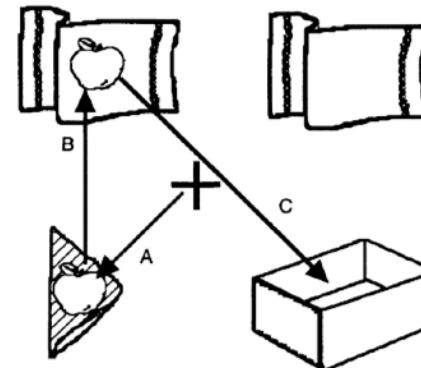
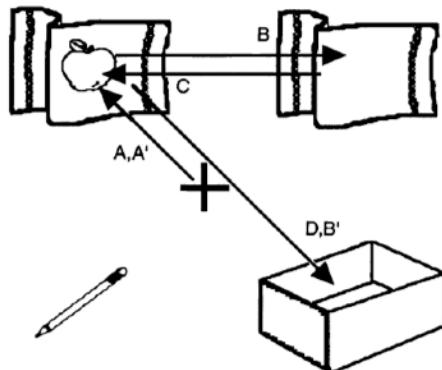
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 6. If necessary, iterate 1—5

Efficient comprehension as rational, goal-driven

- Online sentence comprehension is hard
- But lots of information sources can be usefully brought to bear to help with the task
- Therefore, it would be *rational* for people to use *all information sources available*, whenever possible
- This is what *incrementality* is
- We have lots of evidence that people do this often
- How do we reconcile these information sources?



“Put the apple on the towel in the box.” (Tanenhaus et al., 1995, Science)

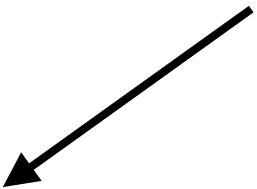
Comprehenders as reverse engineers

Discourse goals [eat tastier food]

Comprehenders as reverse engineers

Discourse goals [eat tastier food]

Planned
communicative
acts



[ask dinner partner
for spices]

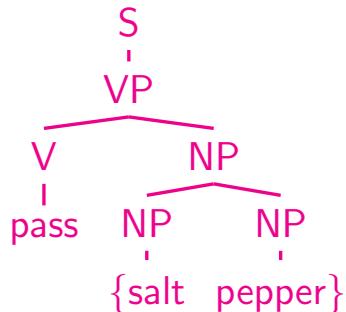
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Lexicalization
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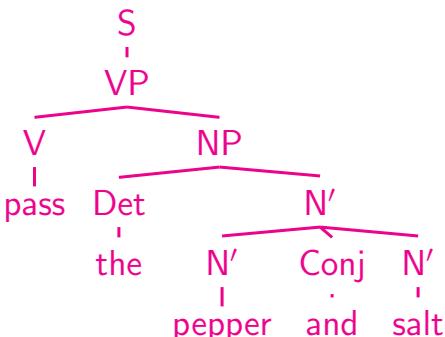
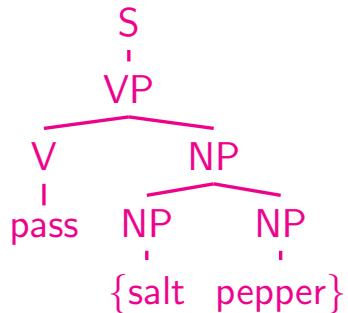
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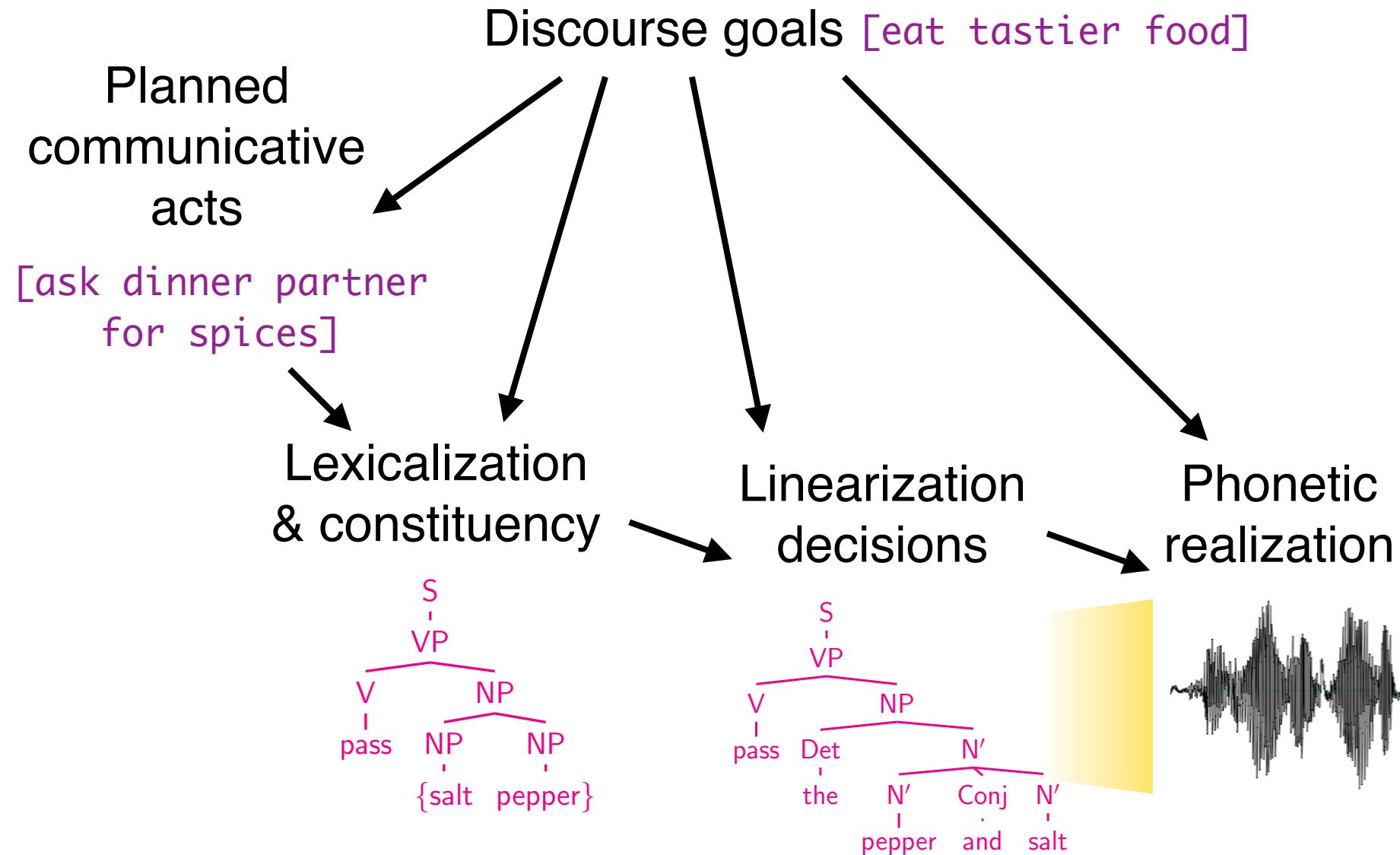
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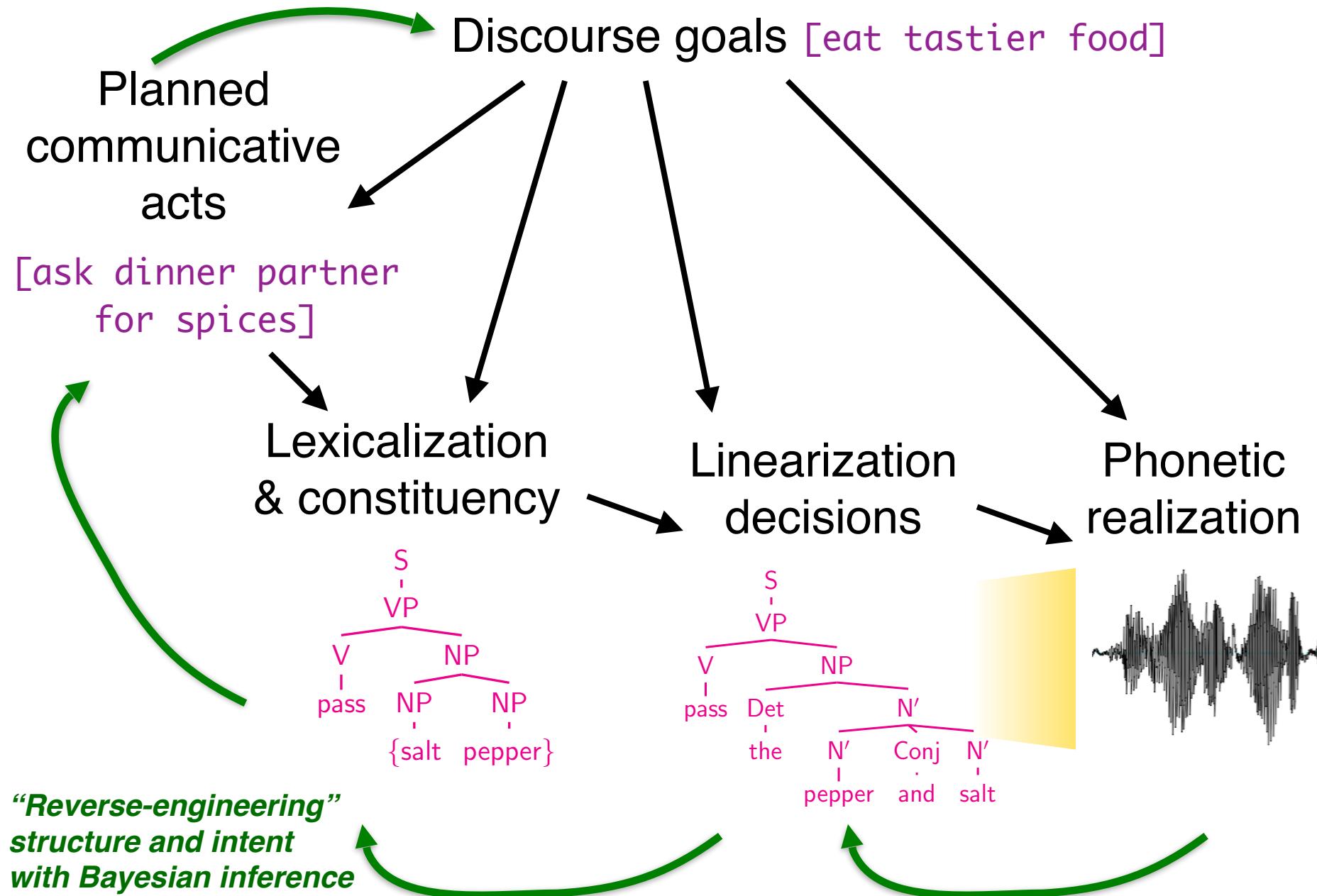
Linearization
decisions



Comprehenders as reverse engineers



Comprehenders as reverse engineers



Surprisal summary: psycholinguistic evidence

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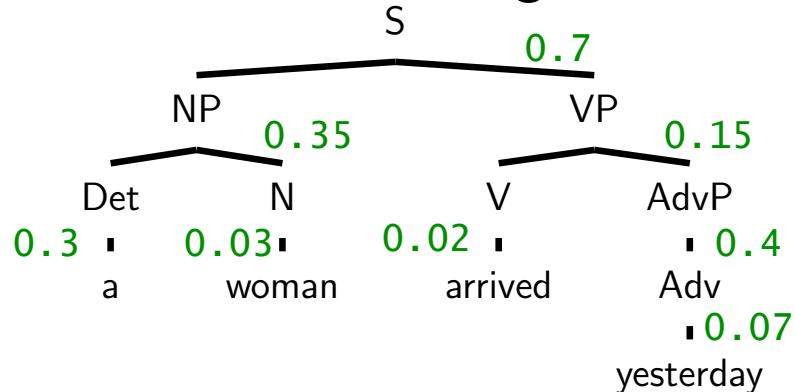
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$$\begin{aligned} P(T) &= 0.7 * 0.35 * 0.15 * 0.3 * 0.03 * 0.02 * 0.4 * 0.07 \\ &= 1.85 \cdot 10^{-7} \end{aligned}$$

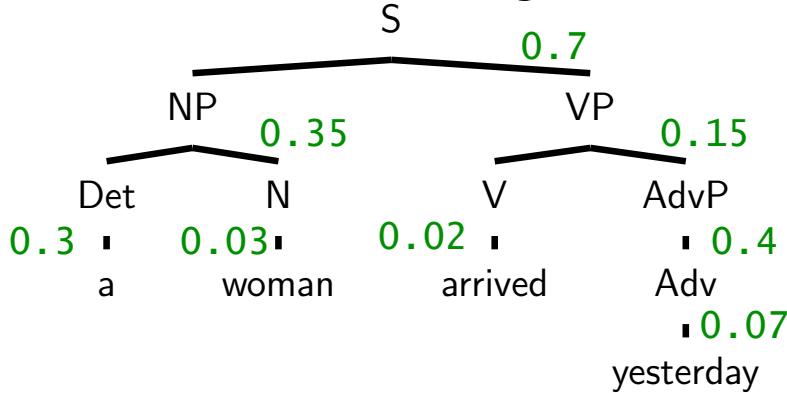
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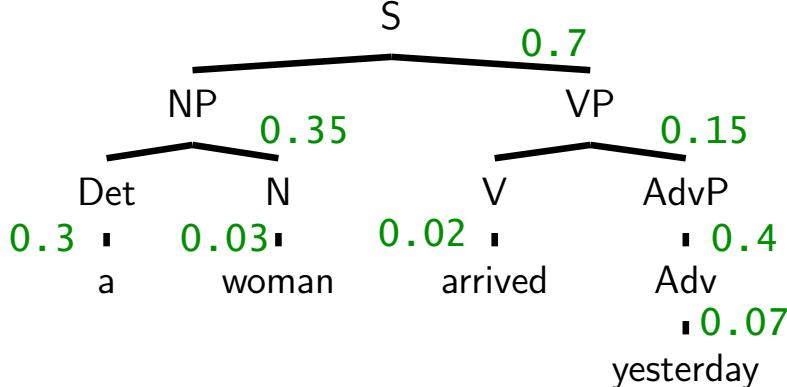
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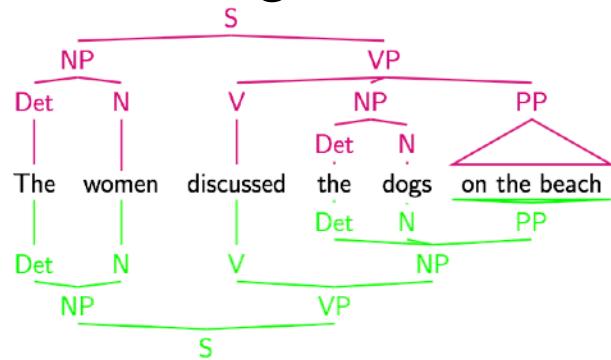
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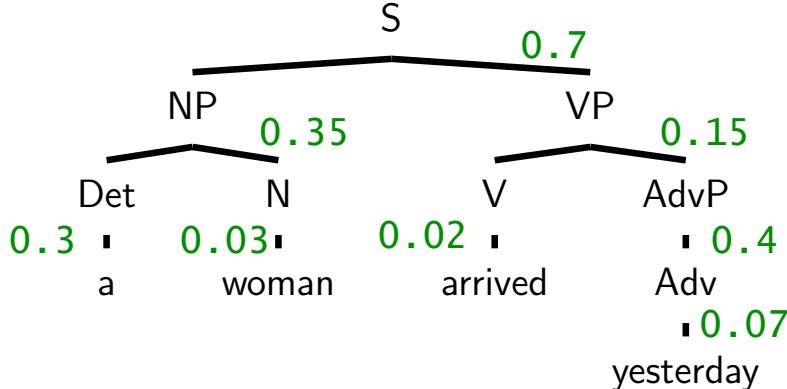
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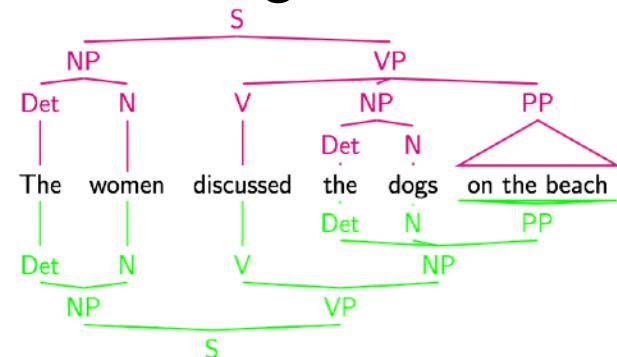
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- Garden-pathing

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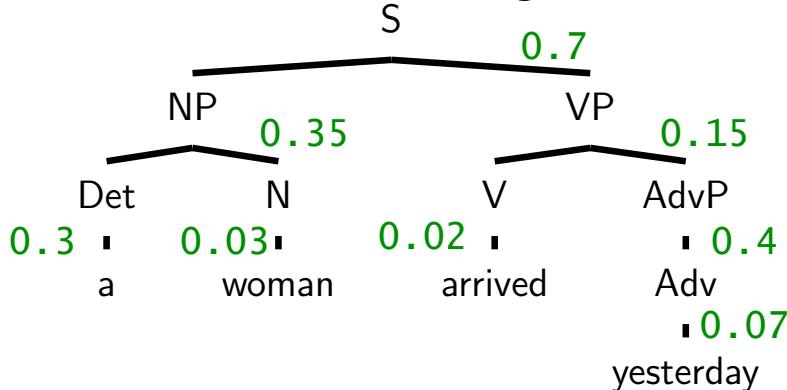
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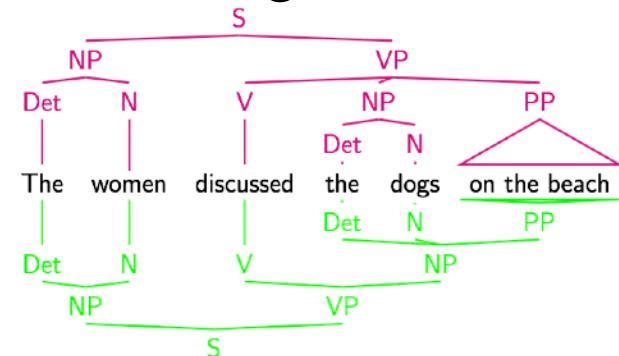
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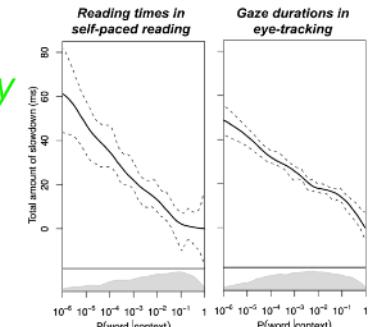


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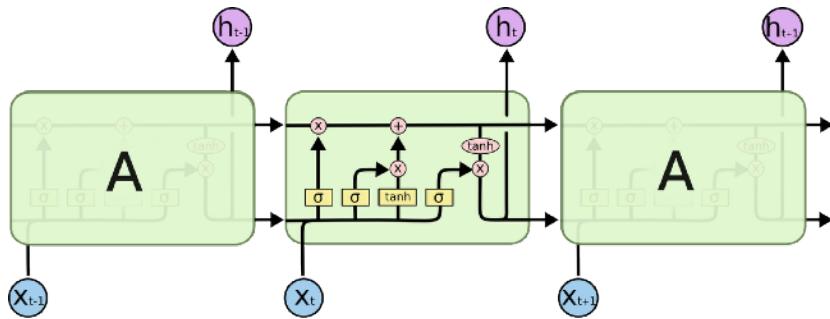
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- Prediction & reading times

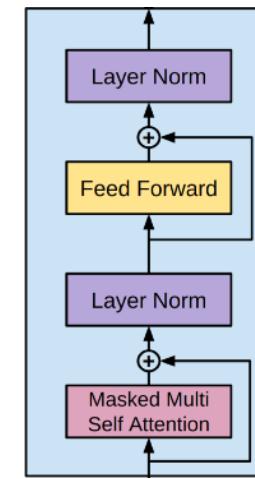
*my brother came inside to...
the children went outside to...*



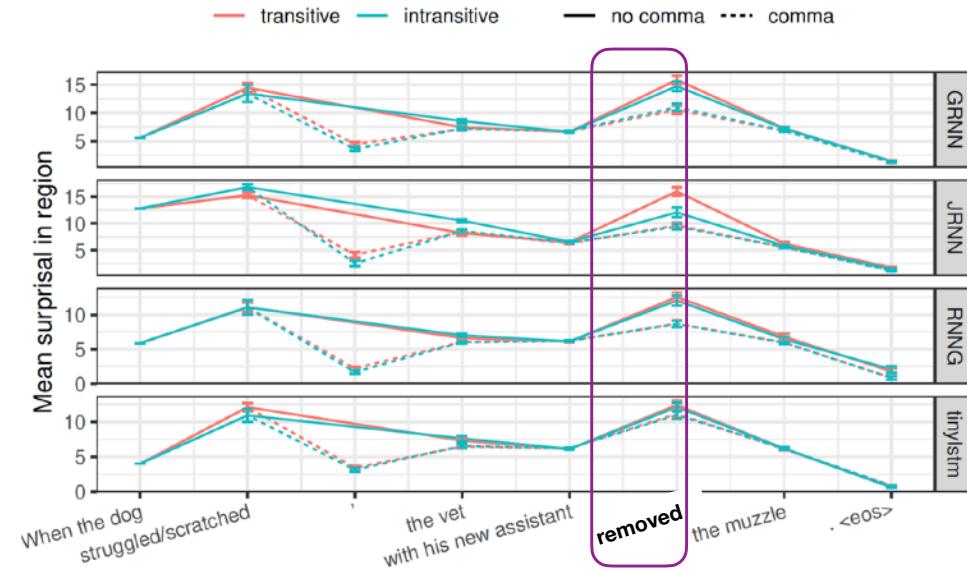
Syntax-like surprisal from deep-learning models



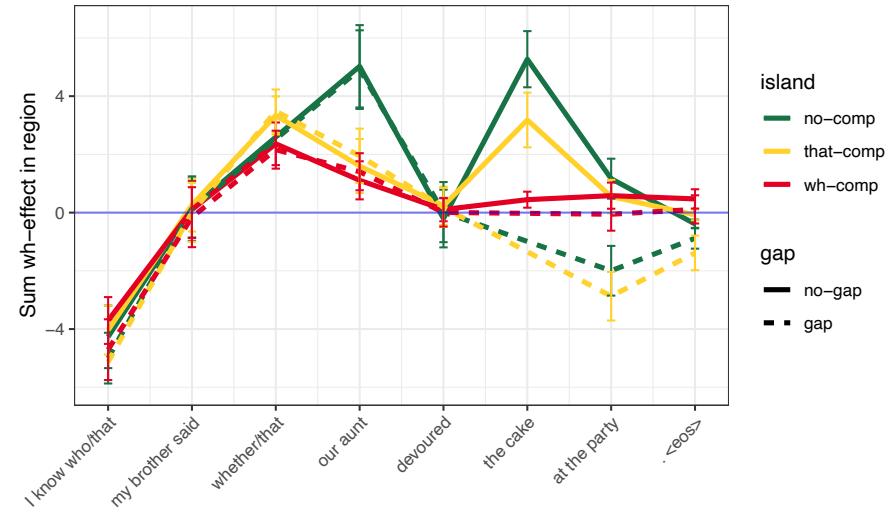
(Elman, 1990; Hochreiter & Schmidhuber, 1997)



(Vaswani et al., 2017; Radford et al., 2018, 2019)



(Futrell et al. 2019, NAACL)



(Wilcox et al., 2018, BlackBox NLP)

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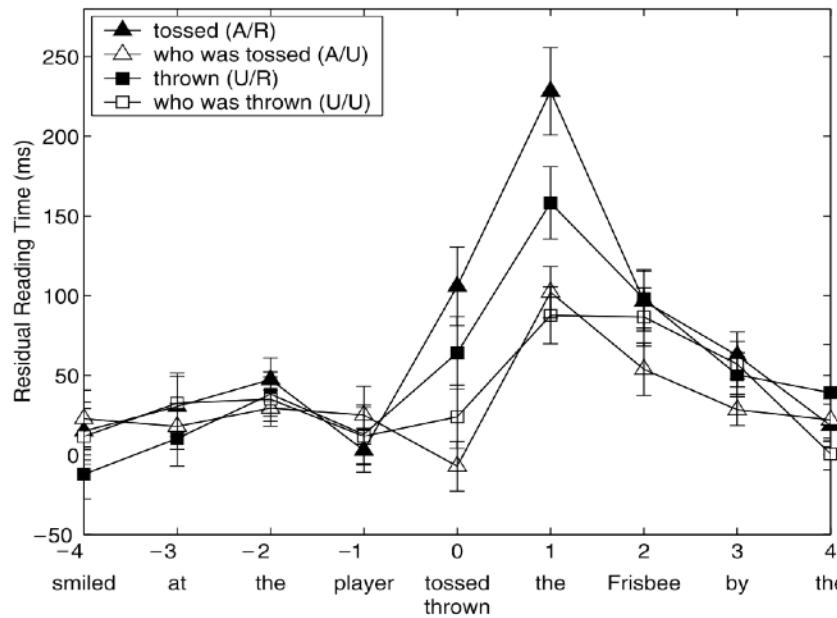
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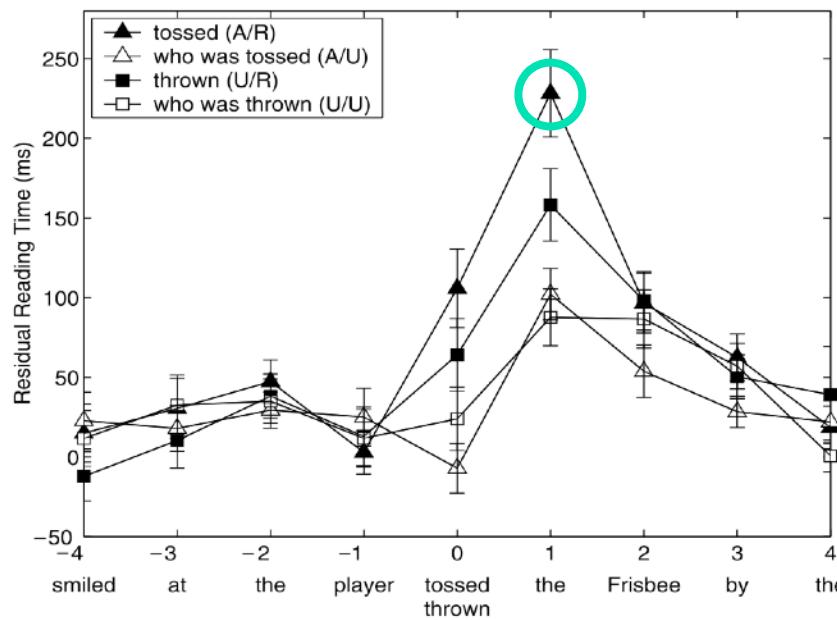


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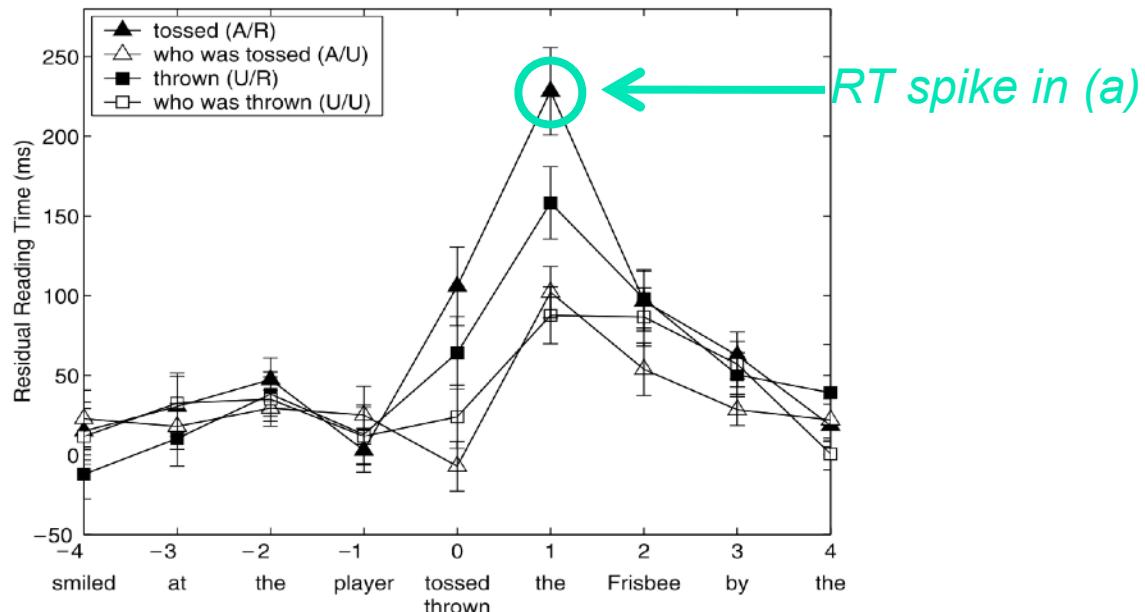


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 - *The woman brought the sandwich...tripped*

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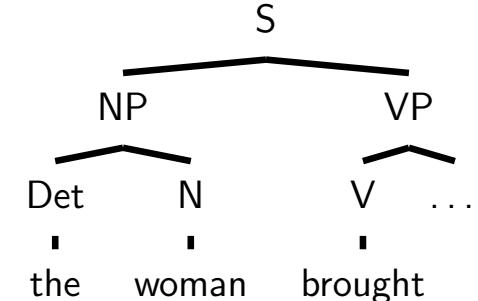
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verb?
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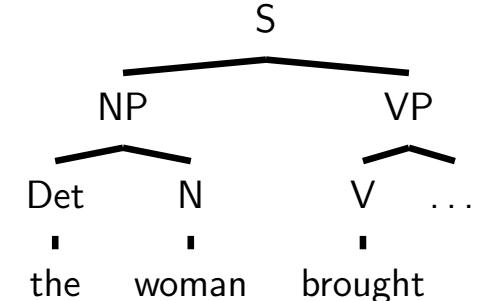


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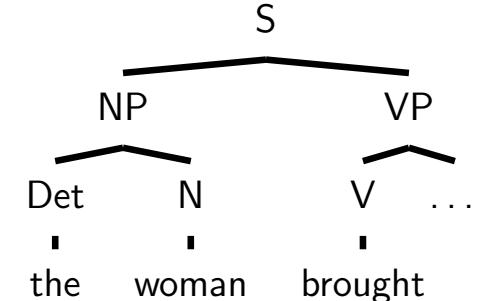
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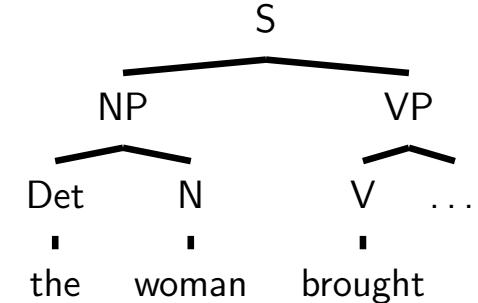
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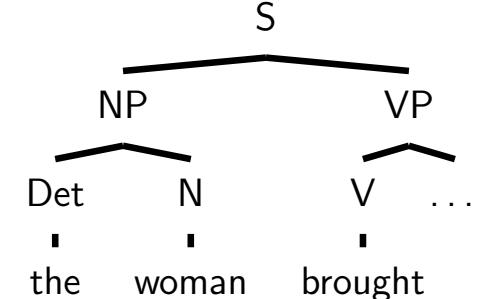
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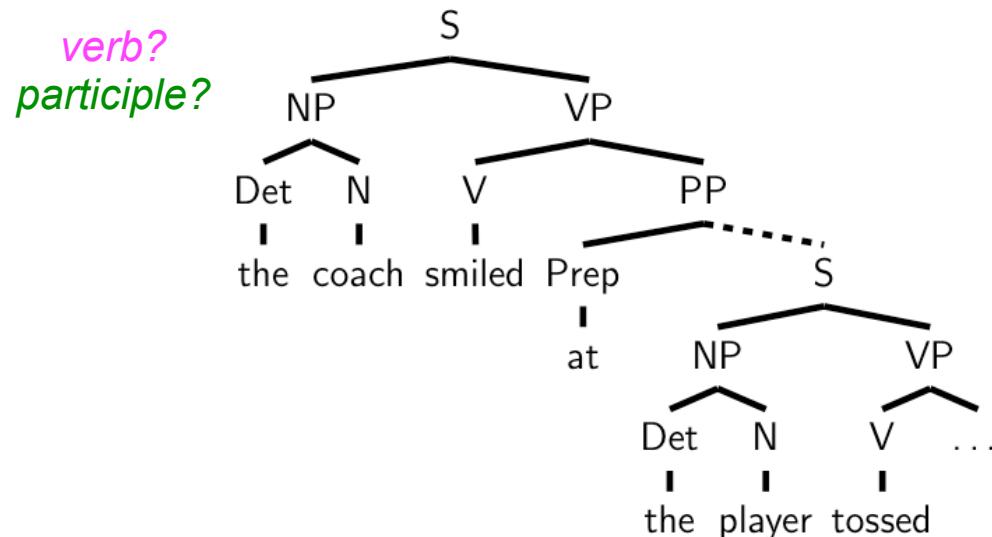
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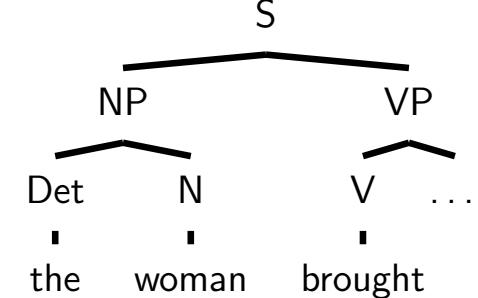


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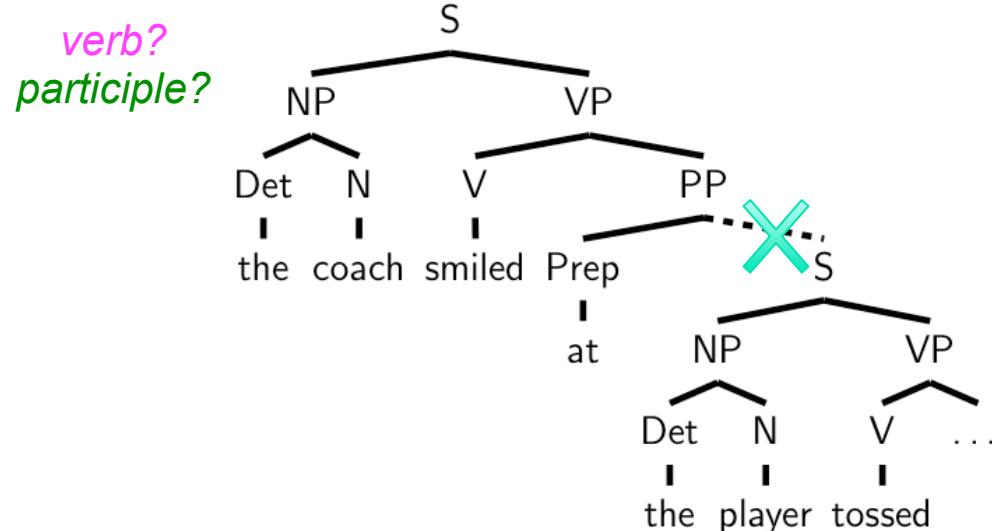
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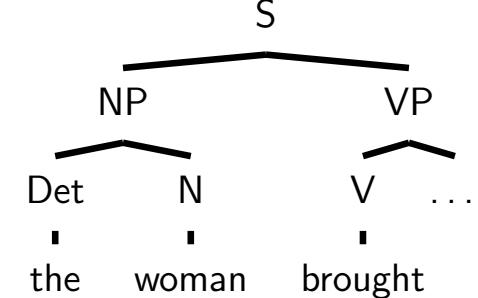


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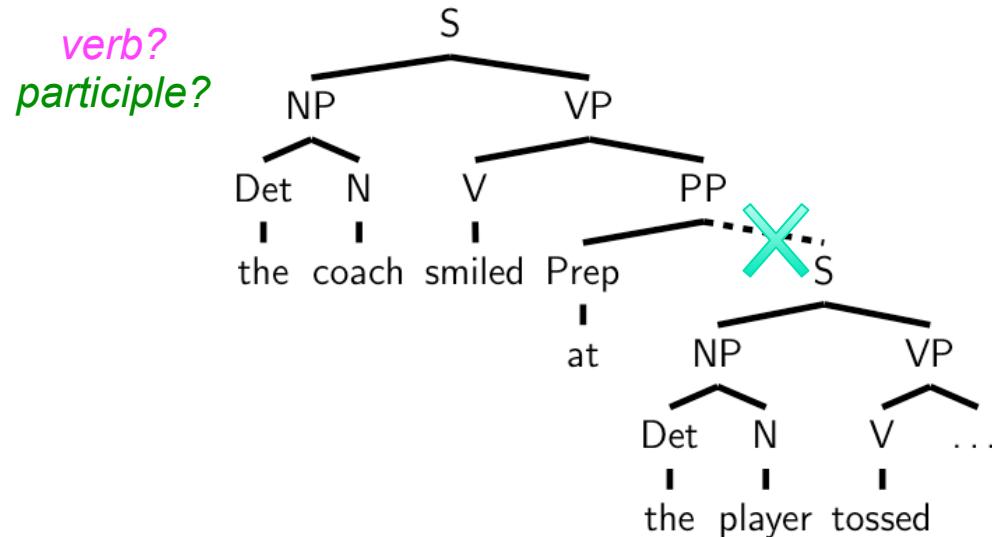
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- A challenge for rational models: **failure to condition on relevant context**

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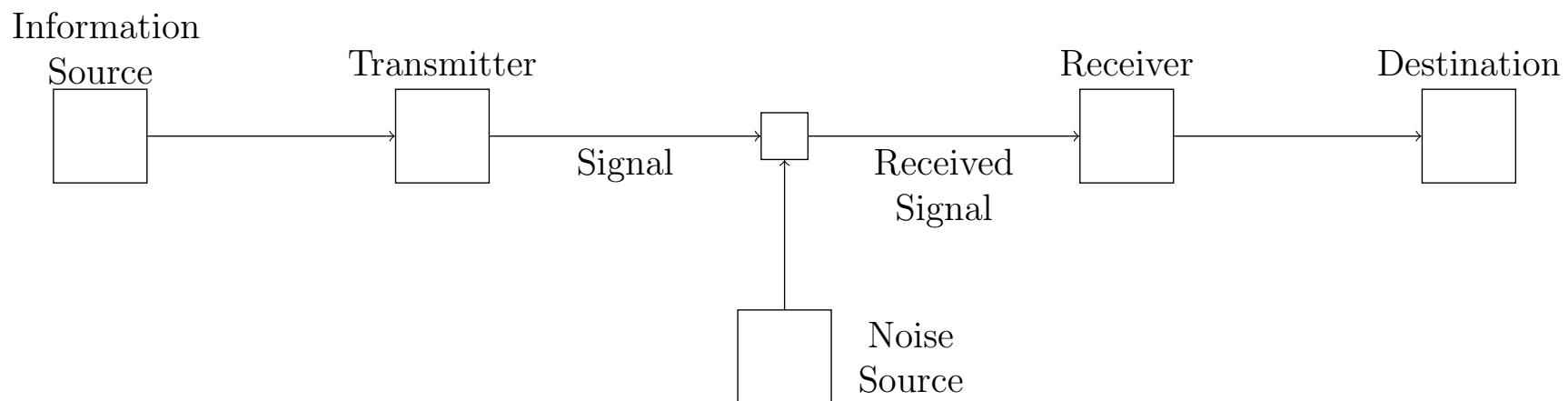
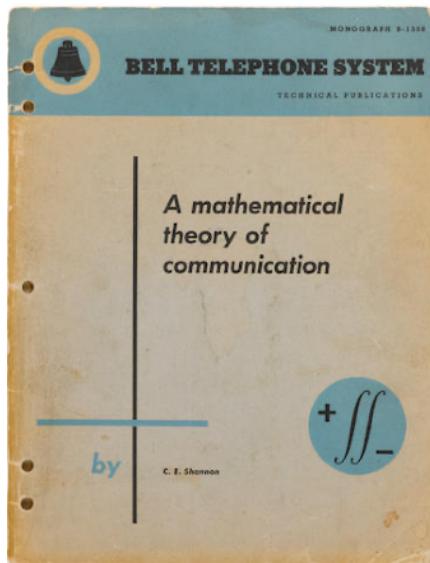
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- Leads to two questions:
 1. What might a model of sentence comprehension under uncertain input look like?
 2. What interesting consequences might such a model have?

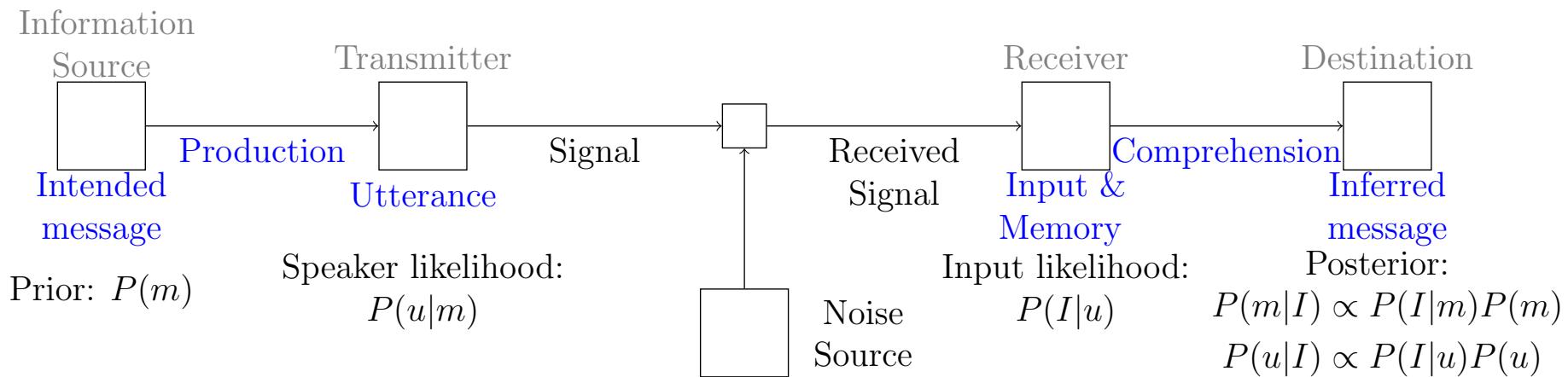
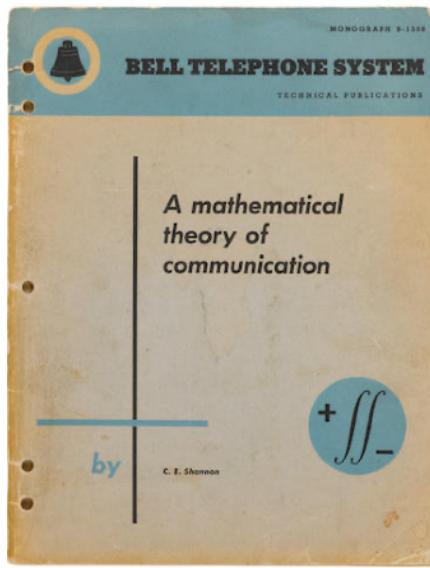
Noisy-channel theory of language processing

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*comprehender's
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$$P_G(T|I) \propto \sum_{\mathbf{w}} P(I|T, \mathbf{w})P(\mathbf{w}|T)P(T)$$

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- If we know true sentence \mathbf{w}^* but not input I : *true model*

$$P(\mathbf{w}|\mathbf{w}^*) = \int_I P_C(\mathbf{w}|I, \mathbf{w}^*) P_T(I|\mathbf{w}^*) dI$$

comprehender's model

Noisy-channel sentence processing

- Standard probabilistic sentence processing:

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comprehender's model

$$= P_C(\mathbf{w}) \int_I \frac{P_C(I|\mathbf{w})P_T(I|\mathbf{w}^*)}{P_C(I)} dI$$

$$\propto Q(\mathbf{w}, \mathbf{w}^*)$$

Levy (2008, EMNLP)

Representing noisy input

Representing noisy input

- How can we represent the type of noisy input generated by a word sequence?

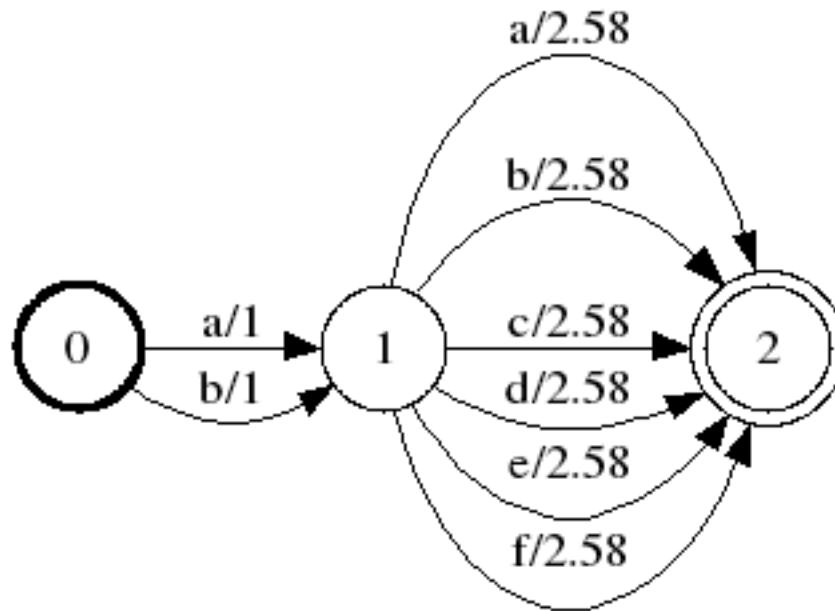
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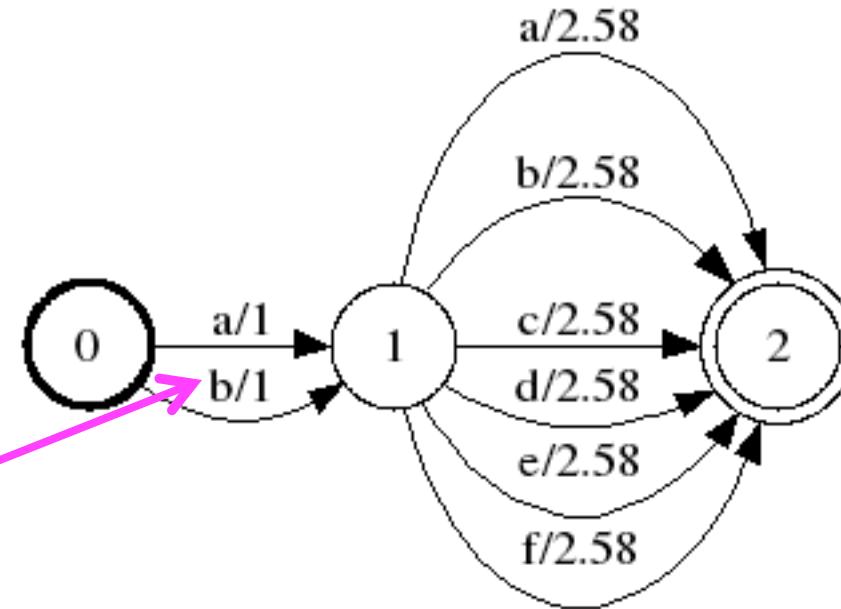


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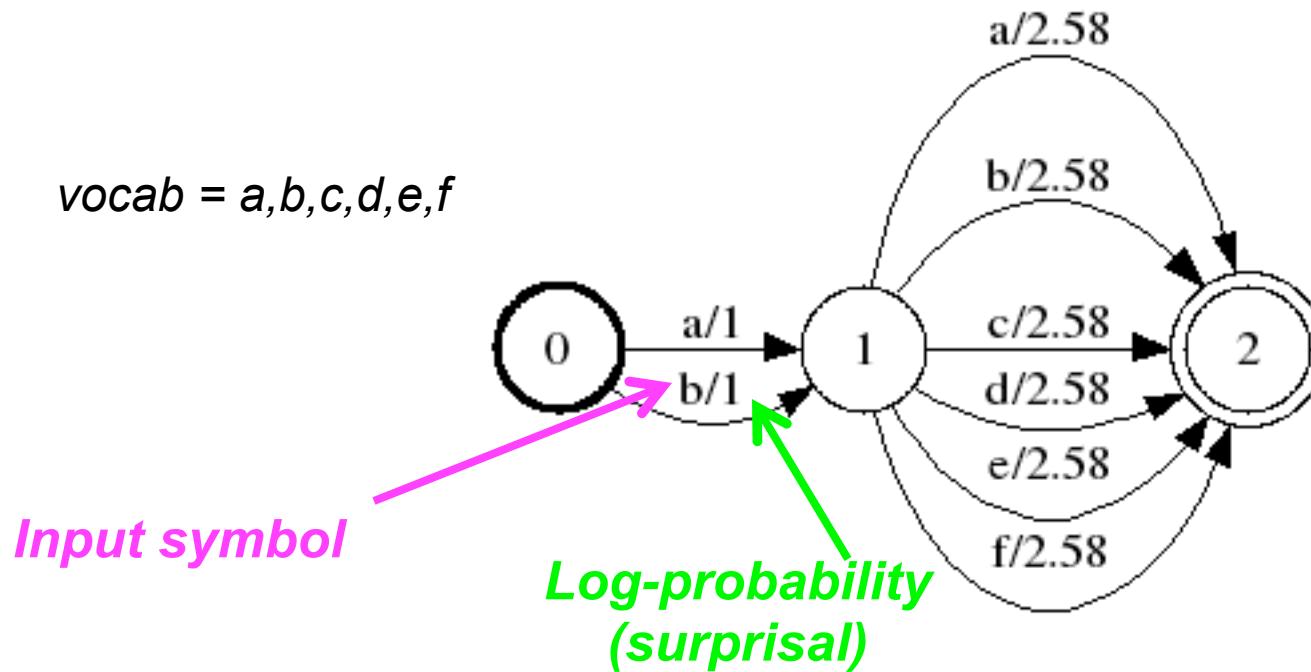
Input symbol



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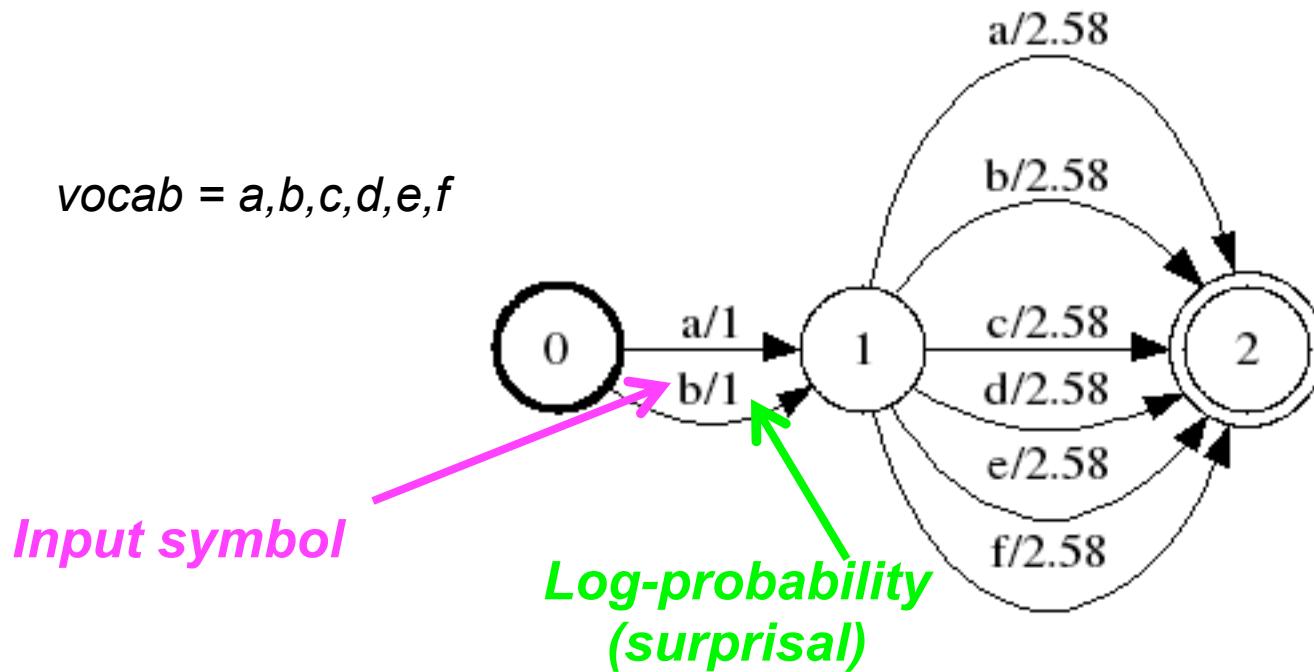
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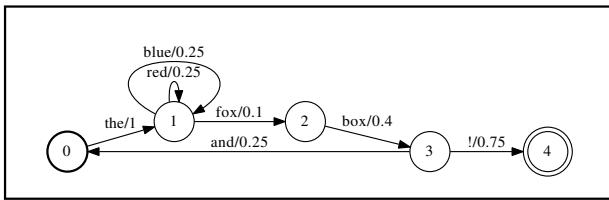
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- “Word 1 is a or b, and I have no info about Word 2”

Weighted finite-state automata



A WEIGHTED FINITE-STATE AUTOMATON (WFSA) consists of a tuple (Q, V, S, R) such that:

- ▶ Q is a finite set of STATES $q_0 q_1 \dots q_N$, with q_0 the designated START STATE;
- ▶ Σ is a finite set of terminal symbols;
- ▶ $F \subseteq Q$ is the set of FINAL STATES;
- ▶ Δ is a finite set of TRANSITIONS each of the form $q \xrightarrow{i} q'$, meaning that “if you are in state q and see symbol i you can consume it and move to state q' ”;
- ▶ λ is a function mapping transitions to real numbers (weights);
- ▶ ρ is a function mapping final states to real numbers (weights).

Weighted finite-state automata (2)

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- ▶ $w_{1\dots N} \in \Sigma^N$ is ACCEPTED or RECOGNIZED by an automaton iff there is a PATH of transitions $\xrightarrow{1\dots N}$ to a final state $q^* \in F$ such that

$$q_0 \xrightarrow[1]{w_1} \xrightarrow[2]{w_2} \dots \xrightarrow[N-1]{w_{N-1}} \xrightarrow[N]{w_N} q^*$$

- ▶ The WEIGHT of such a path $\xrightarrow{1\dots N}$ is the product of the weights of each of the transitions, together with the weight of the final state:

$$P(q_0 \xrightarrow[1]{w_1} \xrightarrow[2]{w_2} \dots \xrightarrow[N-1]{w_{N-1}} \xrightarrow[N]{w_N} q^*) = \rho(q^*) \prod_{i=1}^N \lambda(\xrightarrow{i}) \quad (1)$$

Probabilistic Linguistic Knowledge

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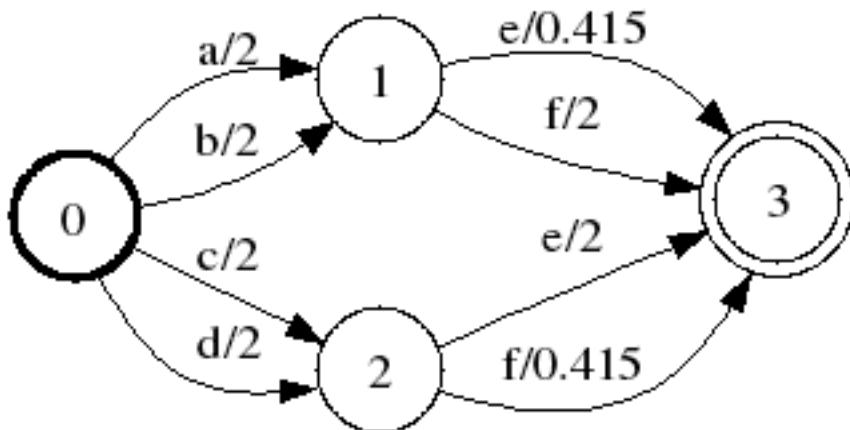
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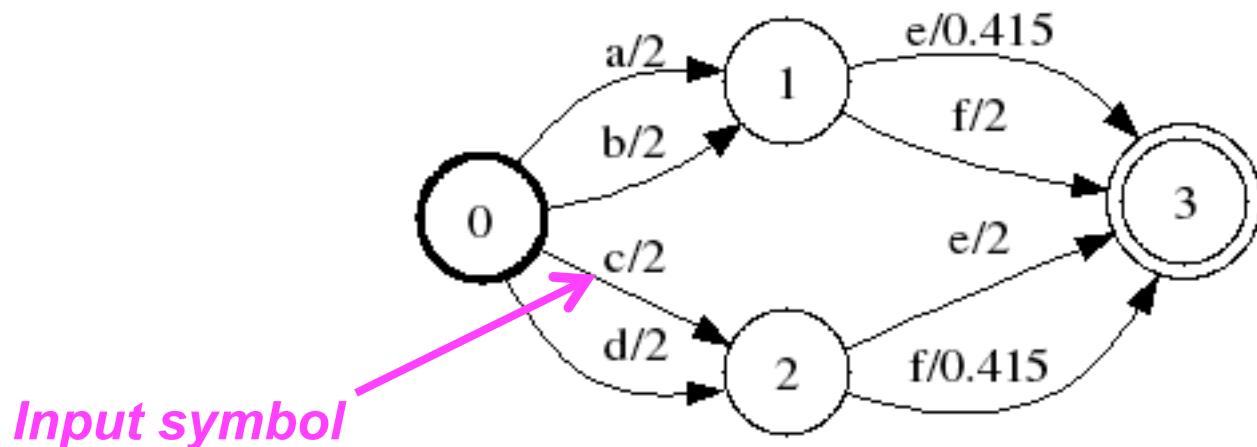
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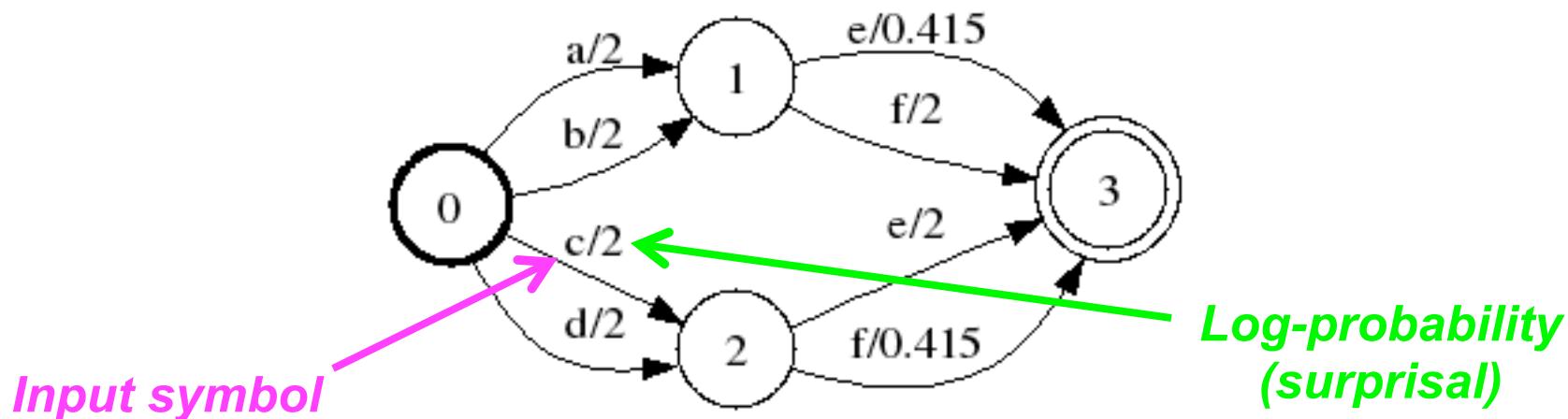
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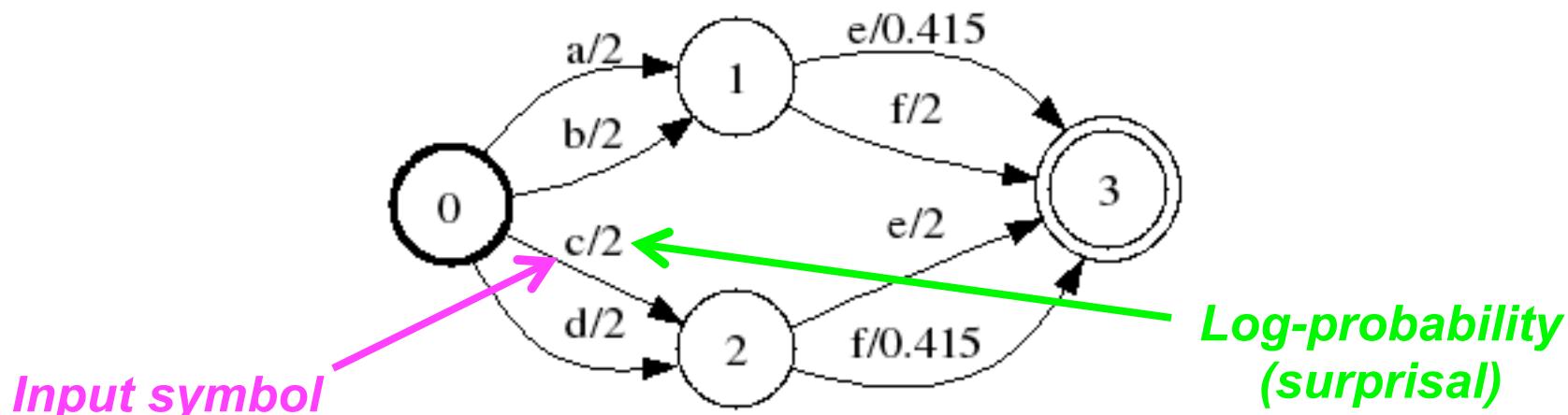
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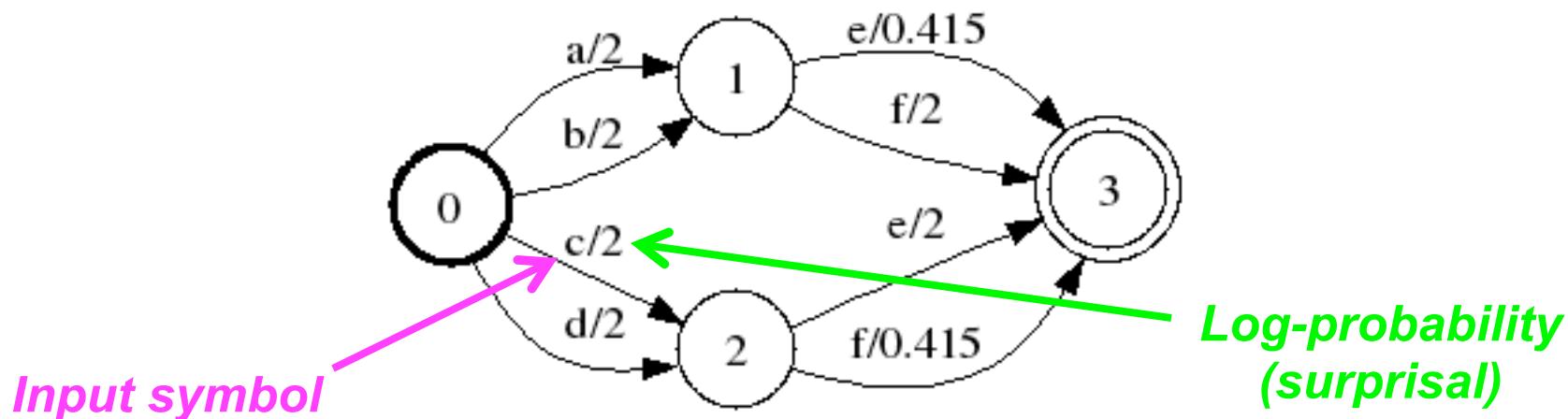
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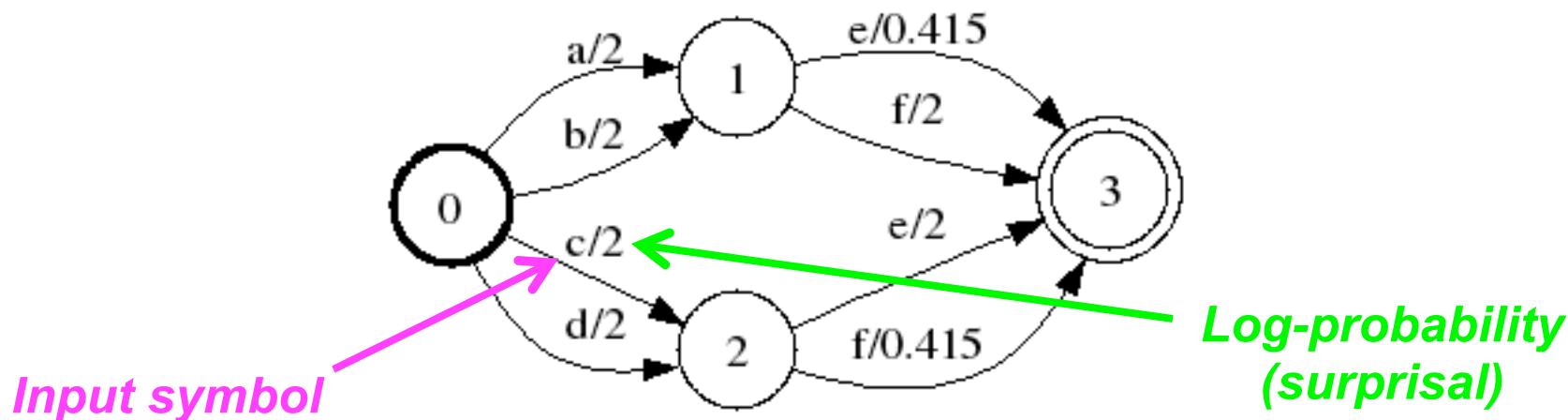
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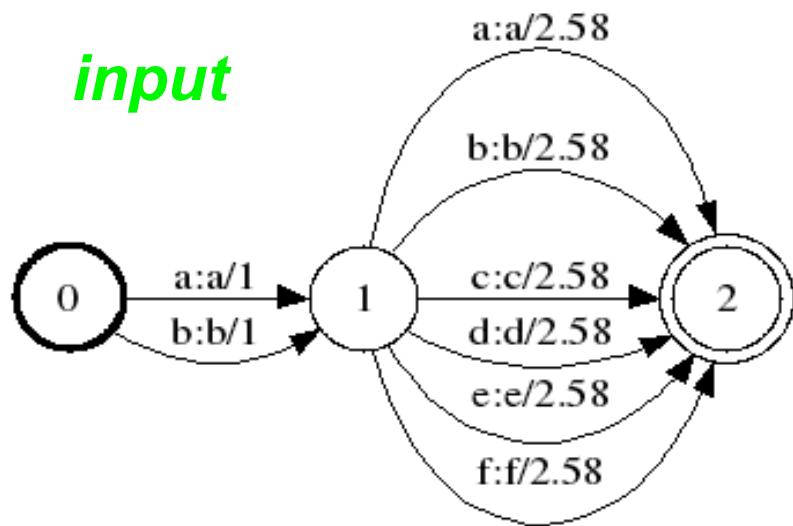
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Combining grammar & uncertain input

- Bayes' Rule says that the *evidence* and the *prior* should be combined (multiplied)
- For probabilistic grammars, this combination is the formal operation of *weighted intersection*

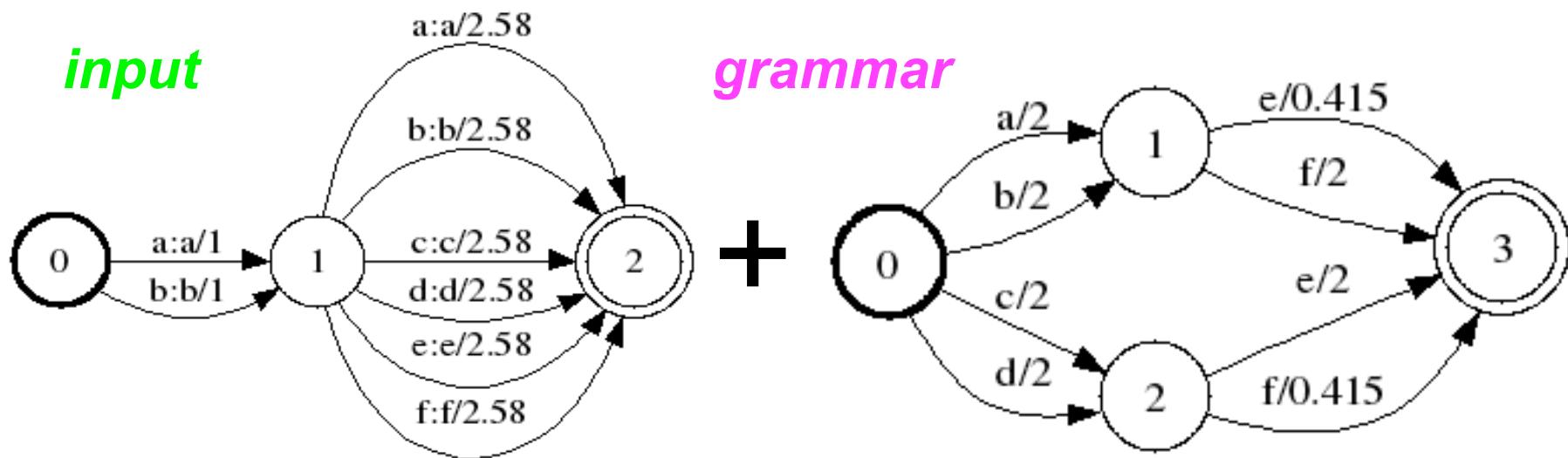
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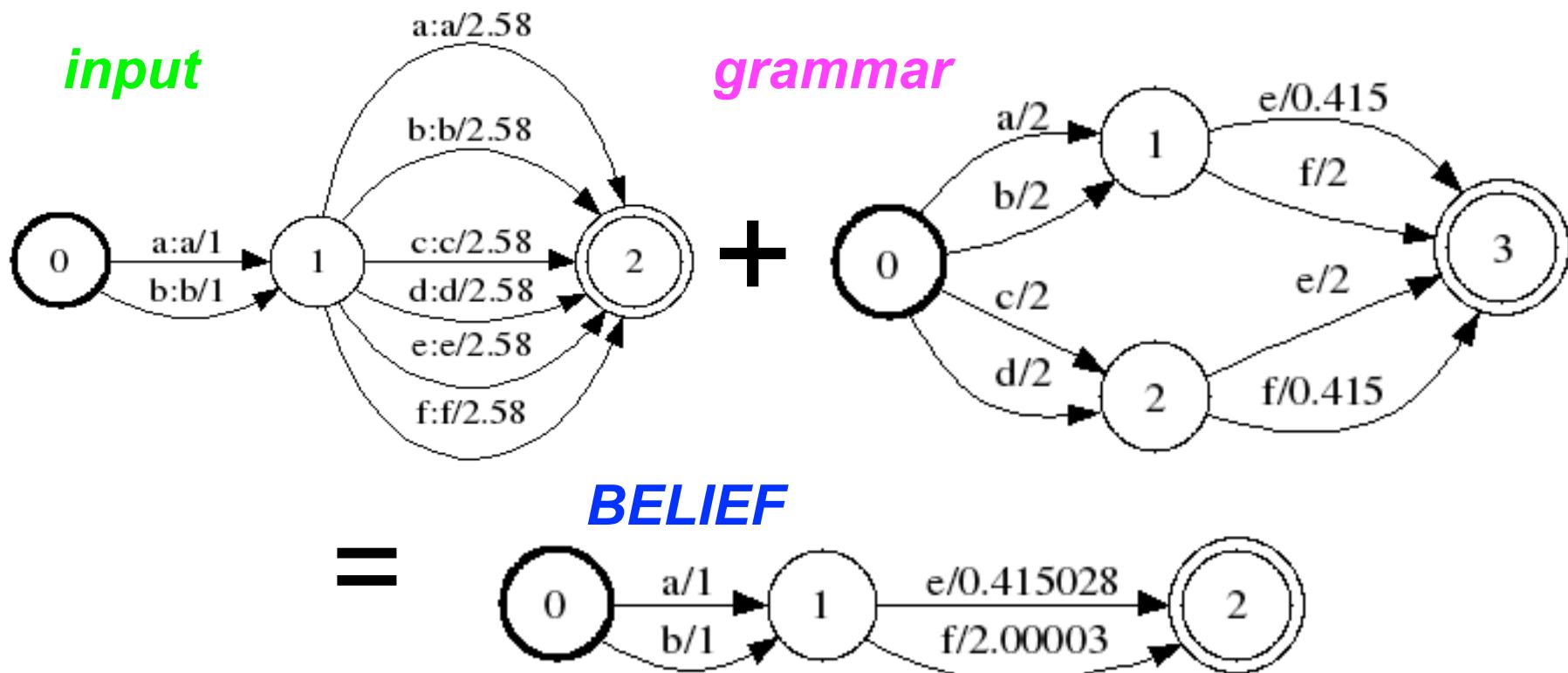
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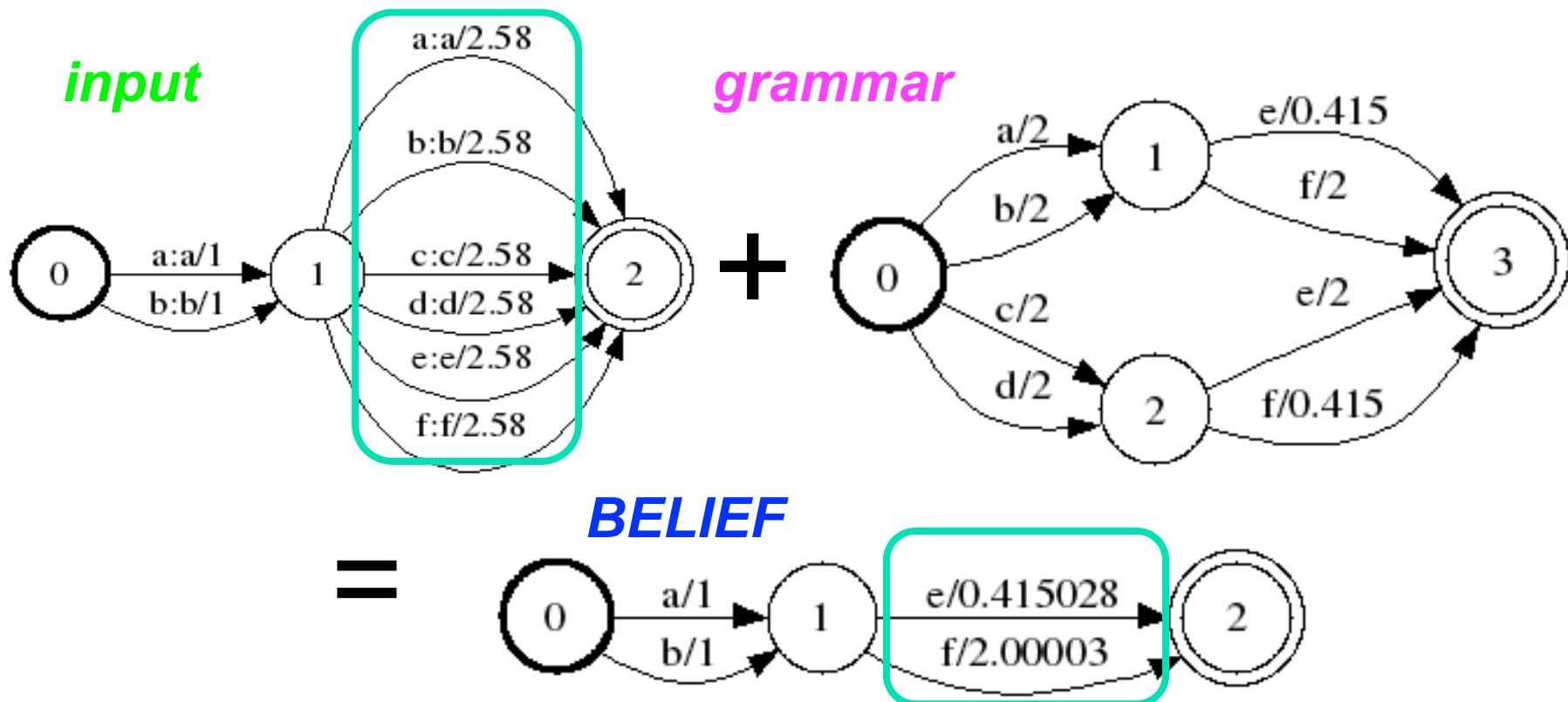
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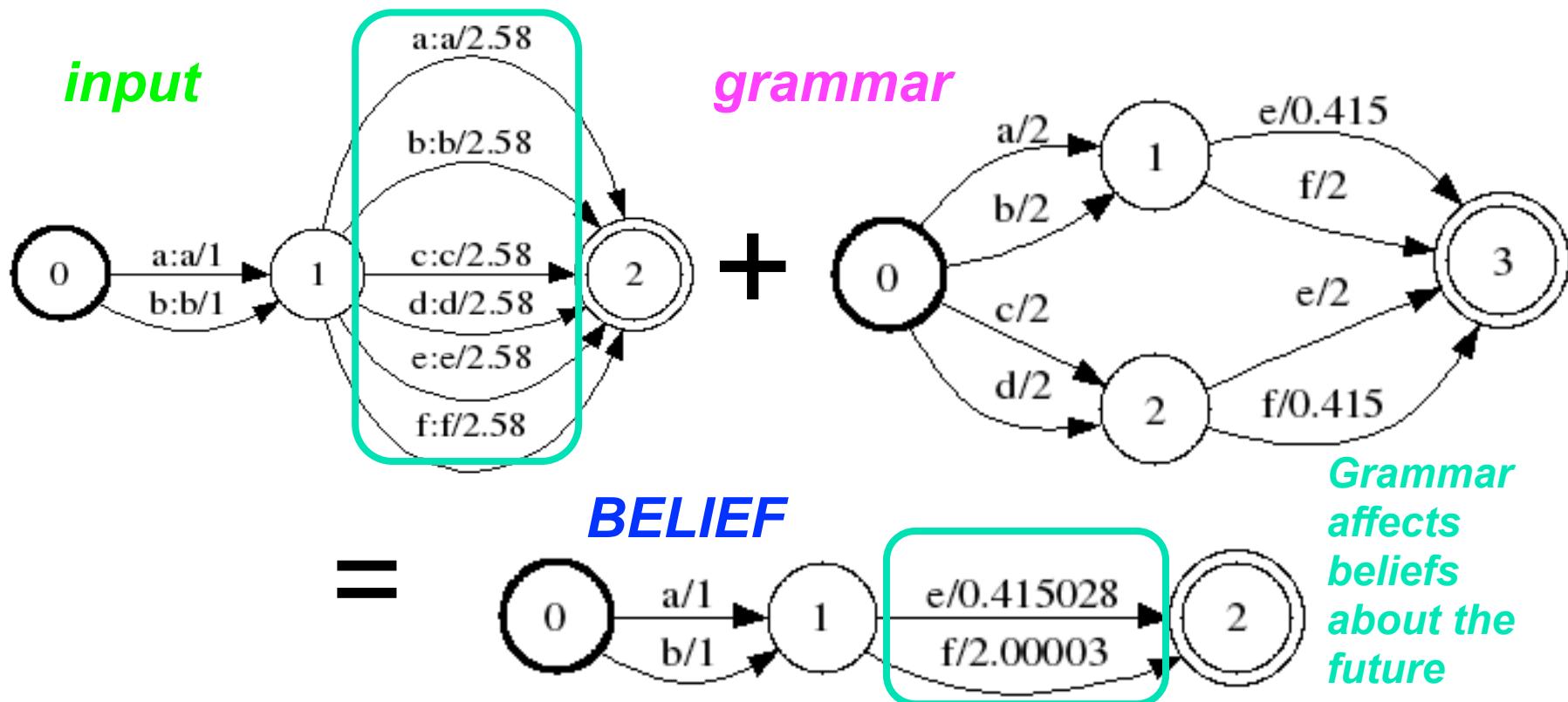
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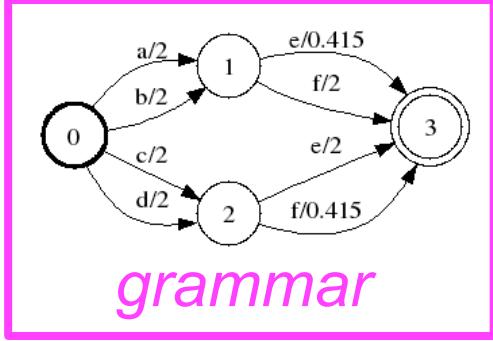
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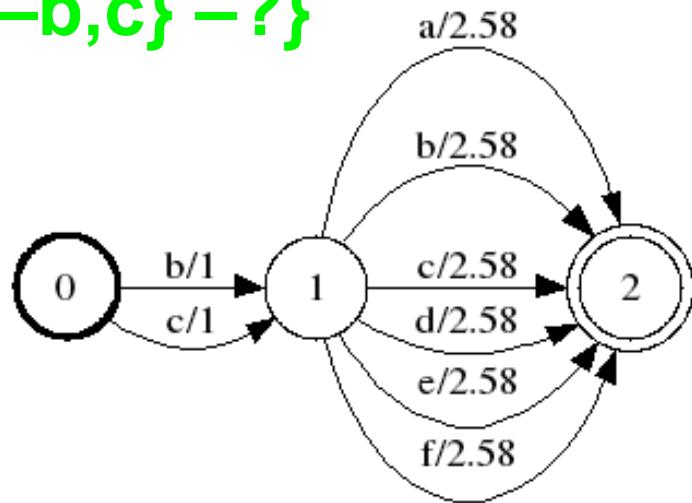
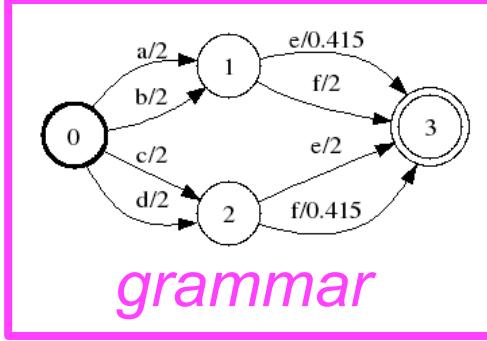
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Revising beliefs about the past

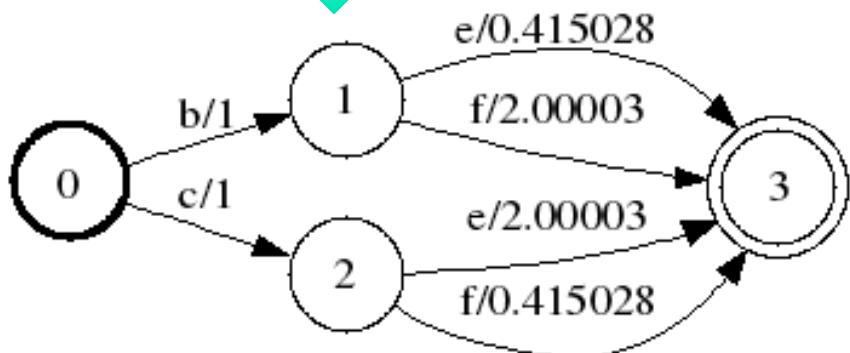
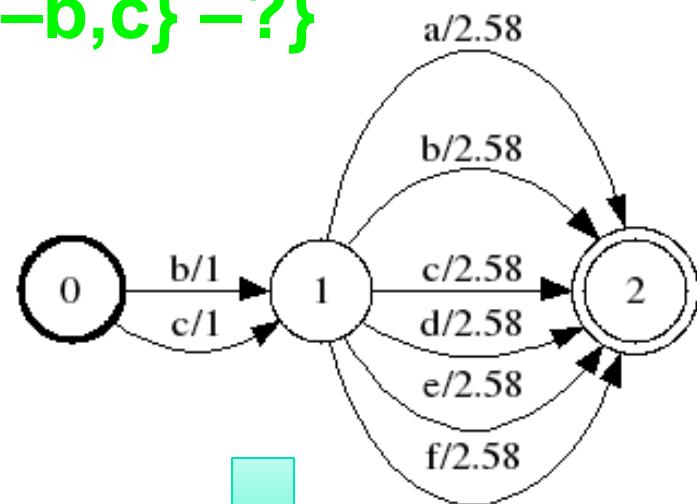
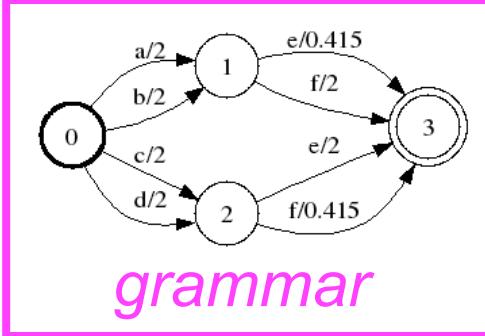
- When we're uncertain about the future, grammar + partial input can affect beliefs about what will happen
- With uncertainty of the past, grammar + future input can affect beliefs about *what has already happened*

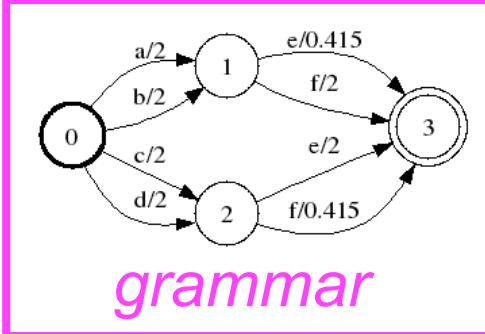




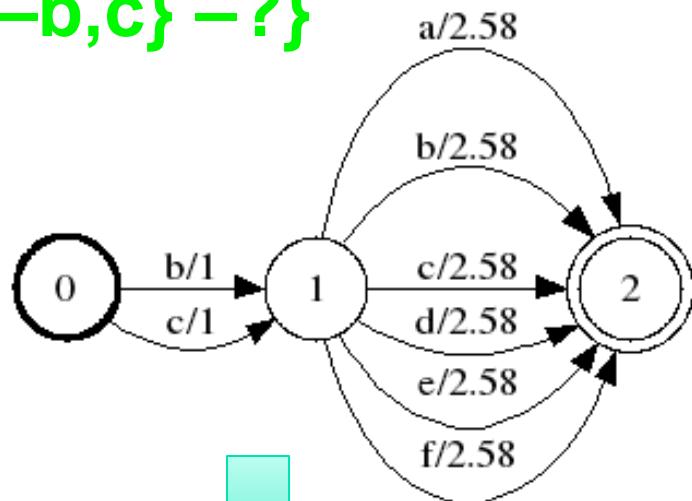
word 1

-b,c} -?}

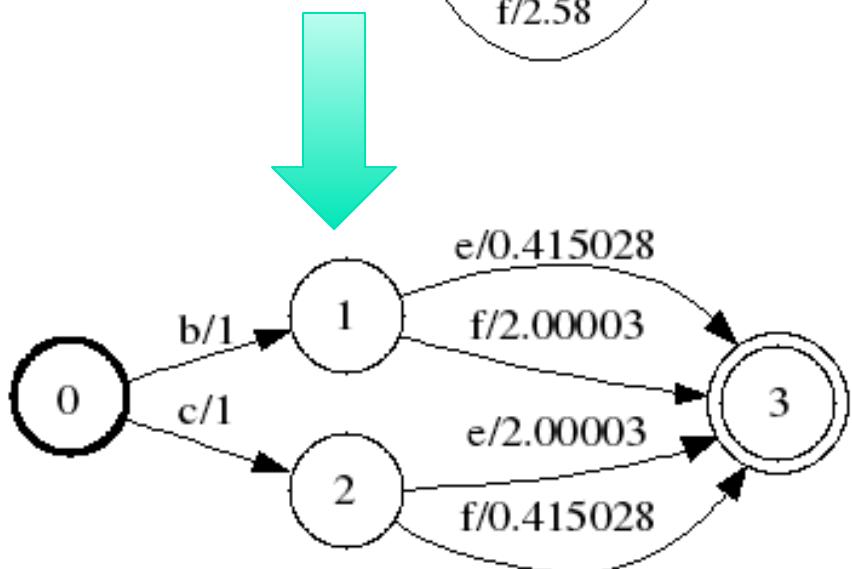
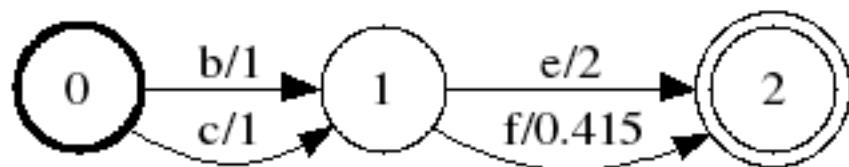


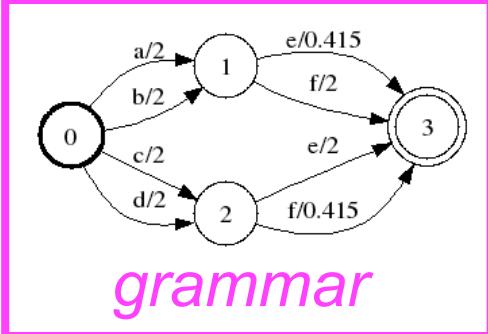


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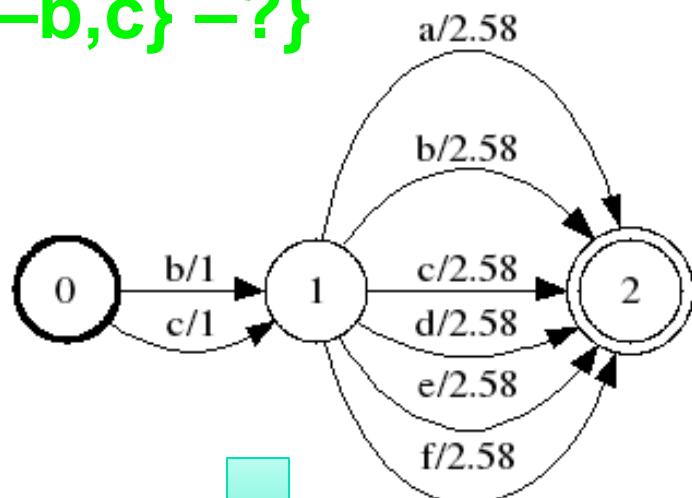


words 1 + 2
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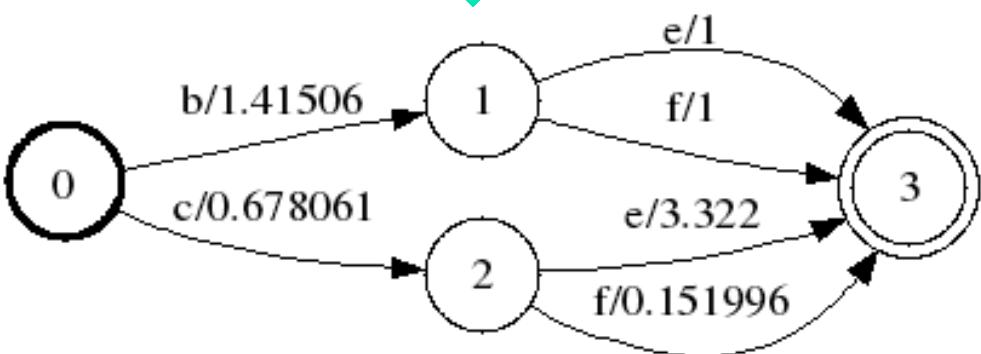
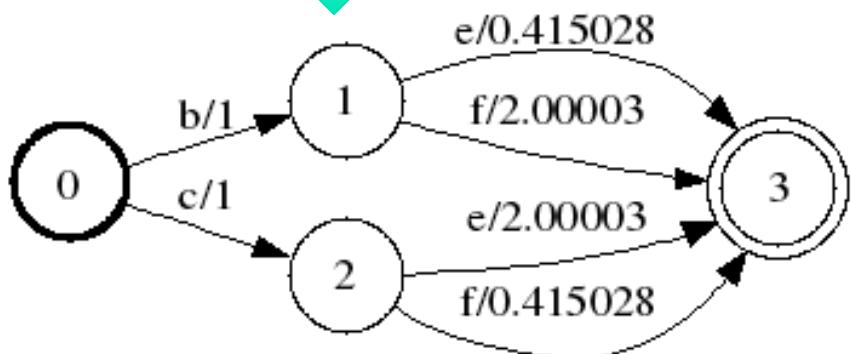
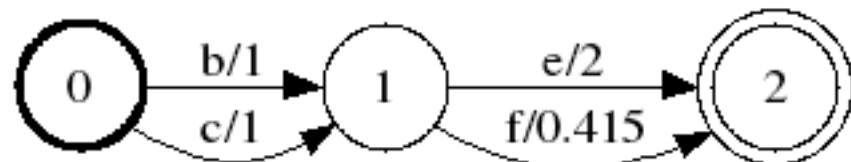


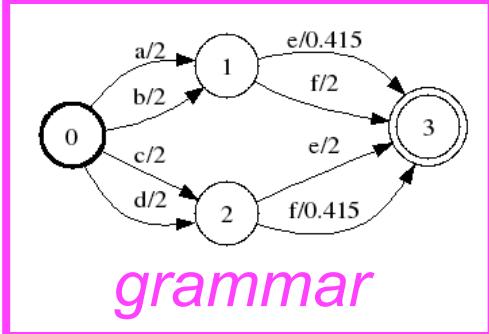


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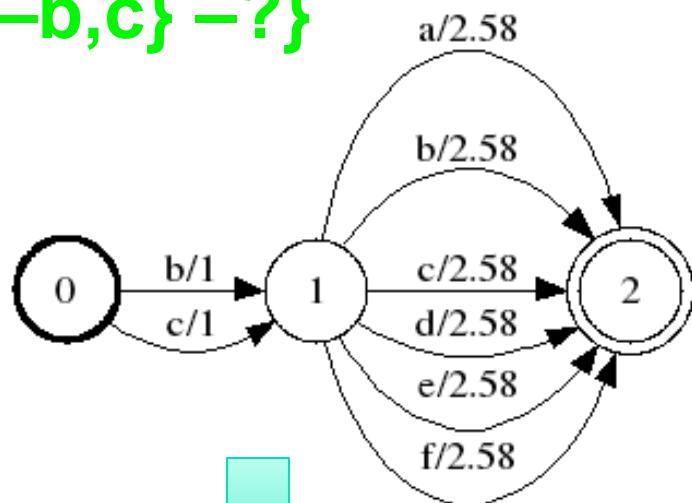


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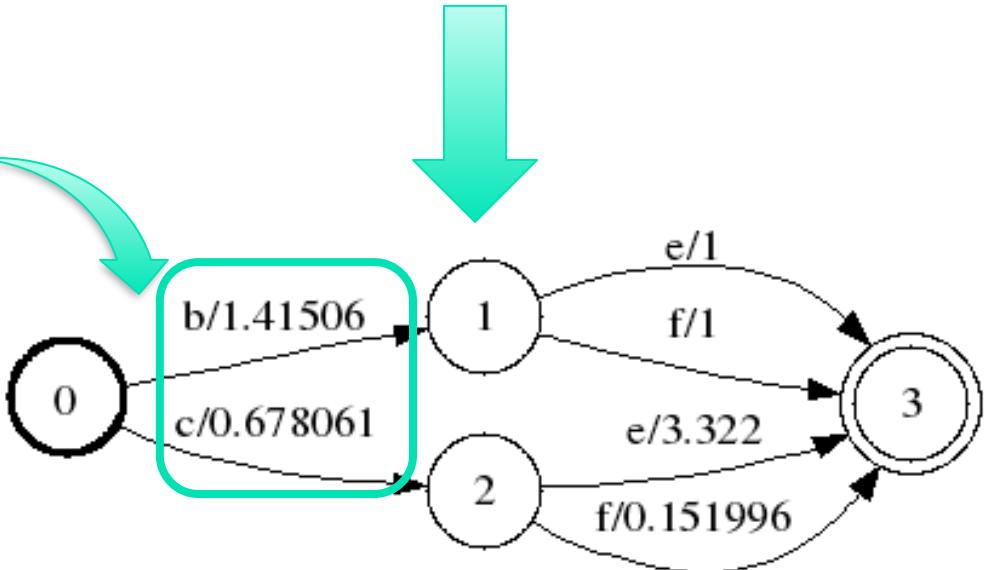
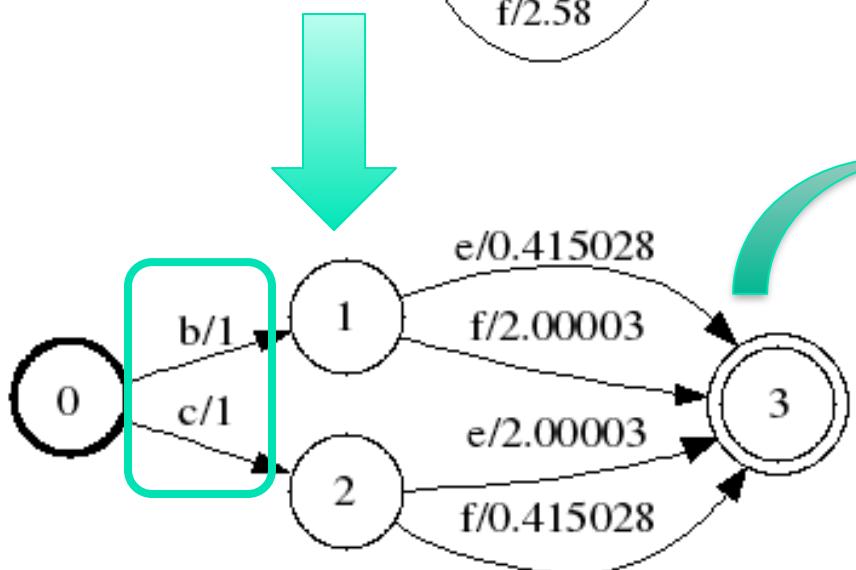
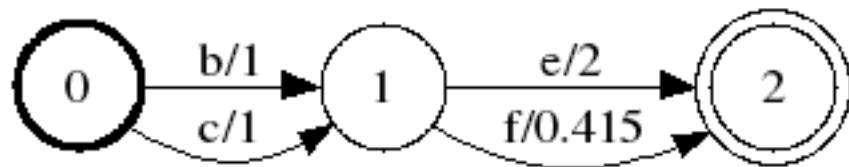




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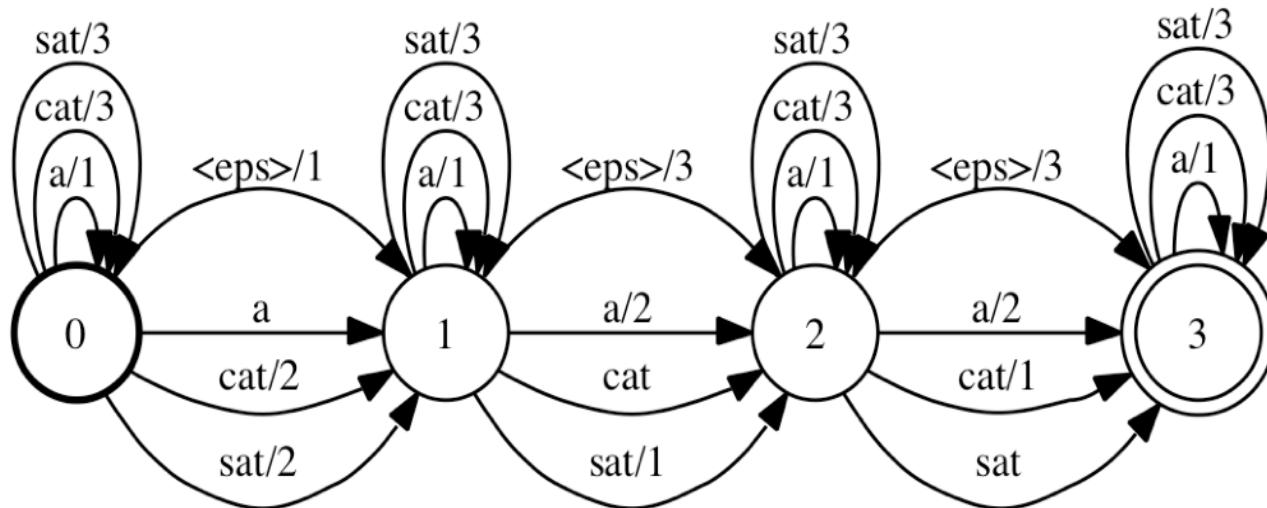
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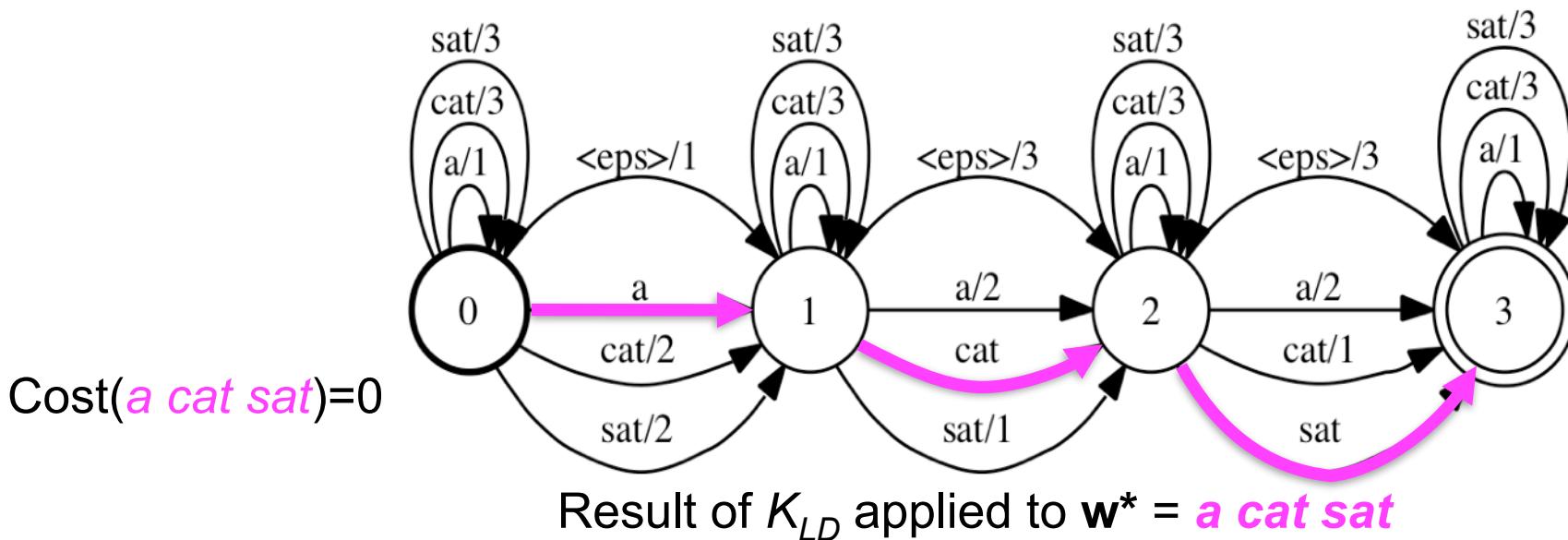
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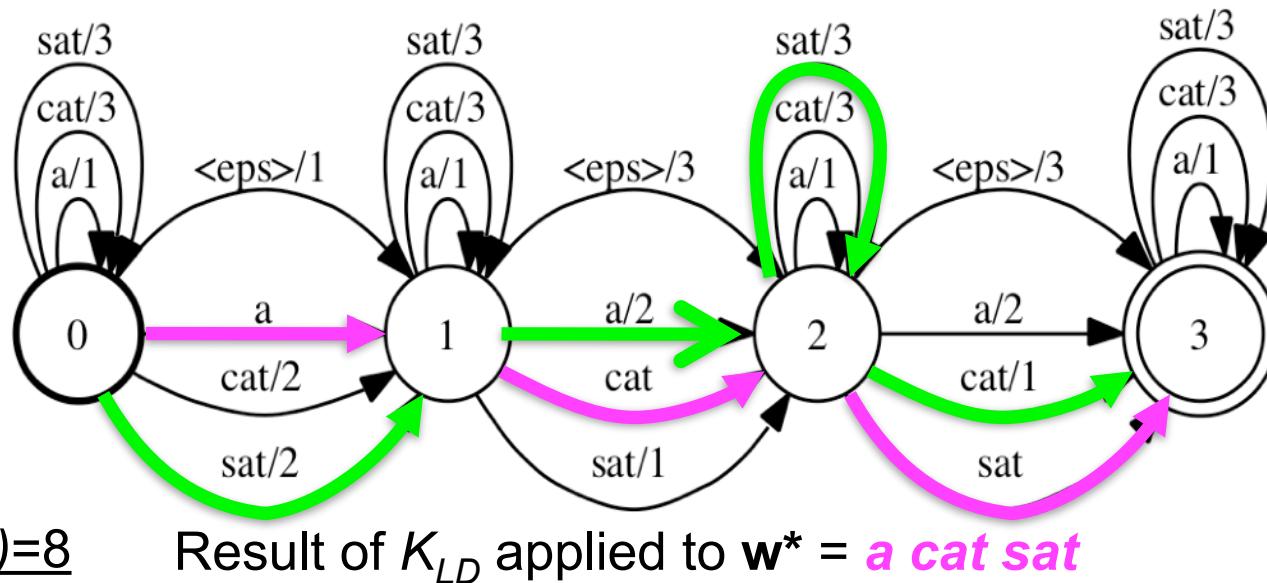
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Rational analysis

- Background assumption: cognitive agent is optimized via evolution and learning to solve everyday tasks effectively
 1. Specify precisely the goals of the cognitive system
 2. Formalize model of the environment adapted to
 3. Make minimal assumptions re: computational limitations
 4. Derive predicted optimal behavior given 1—3
 5. Compare predictions with empirical data
 6. If necessary, iterate 1—5

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*The coach smiled at the player **tossed** the frisbee*

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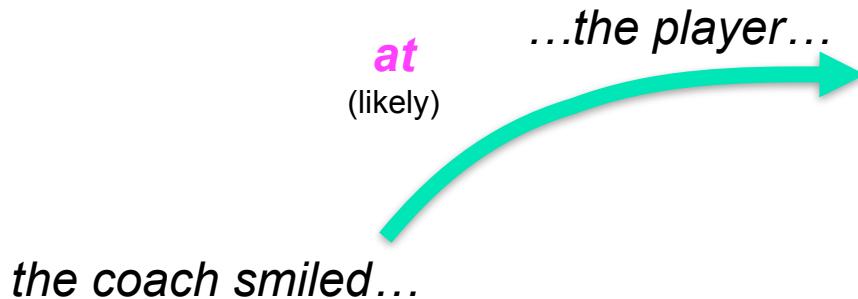
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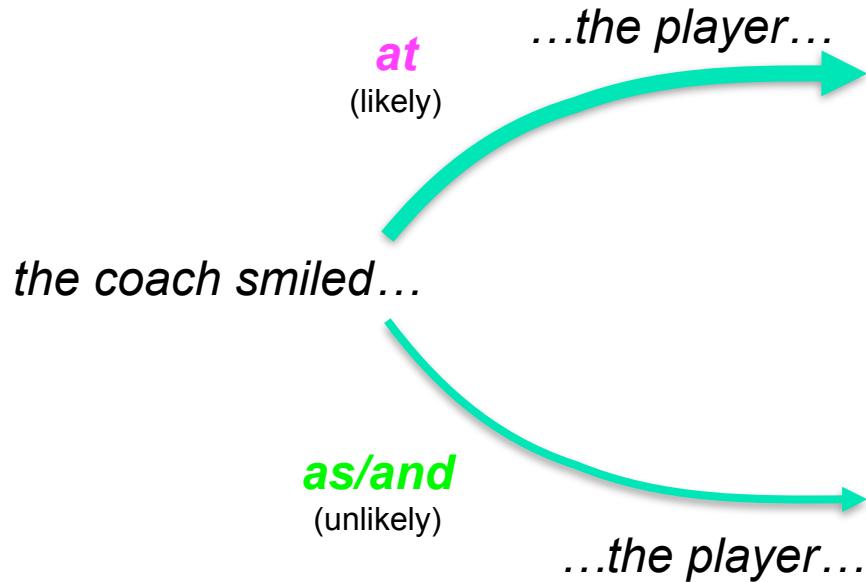
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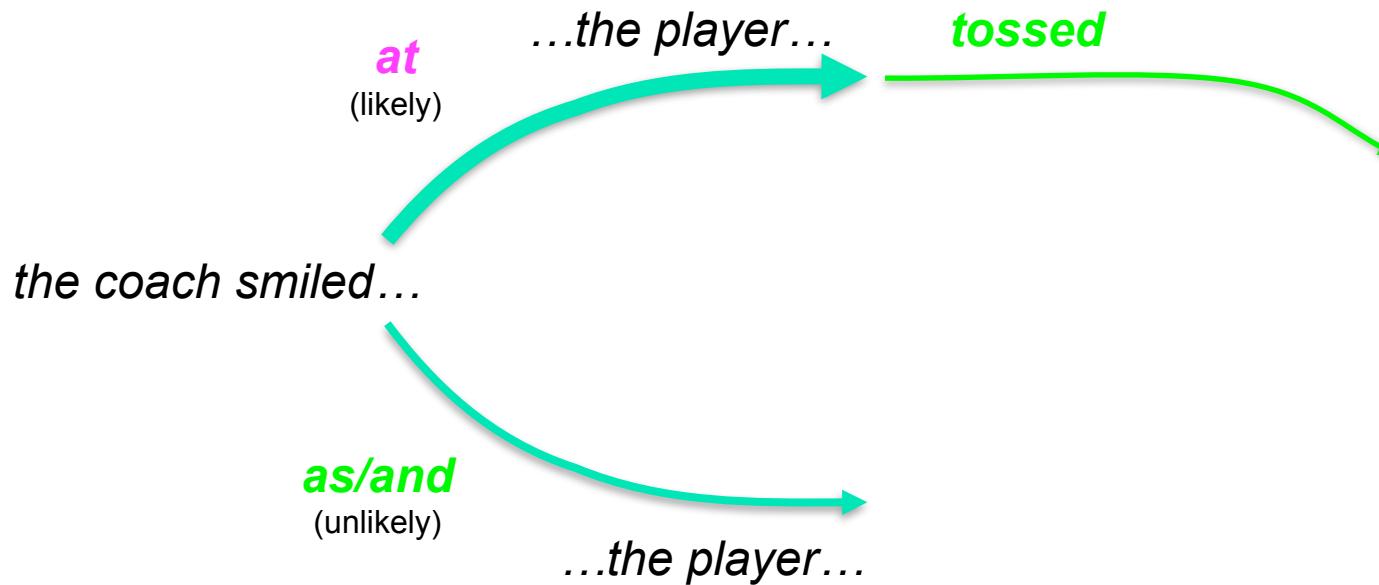
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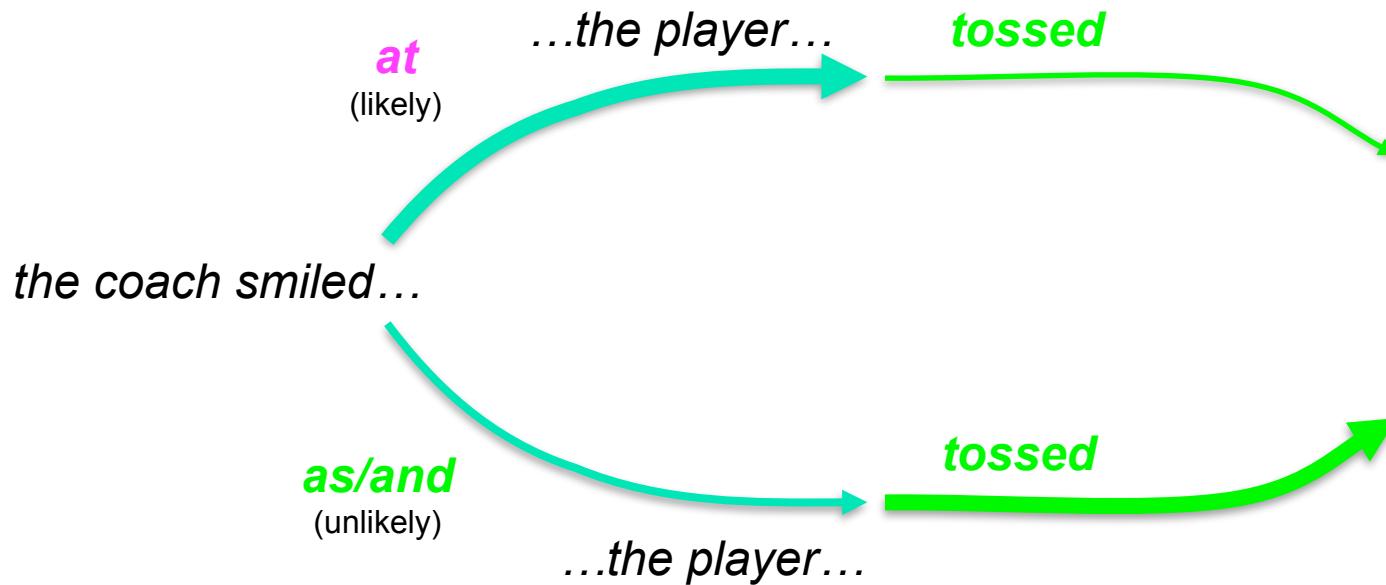
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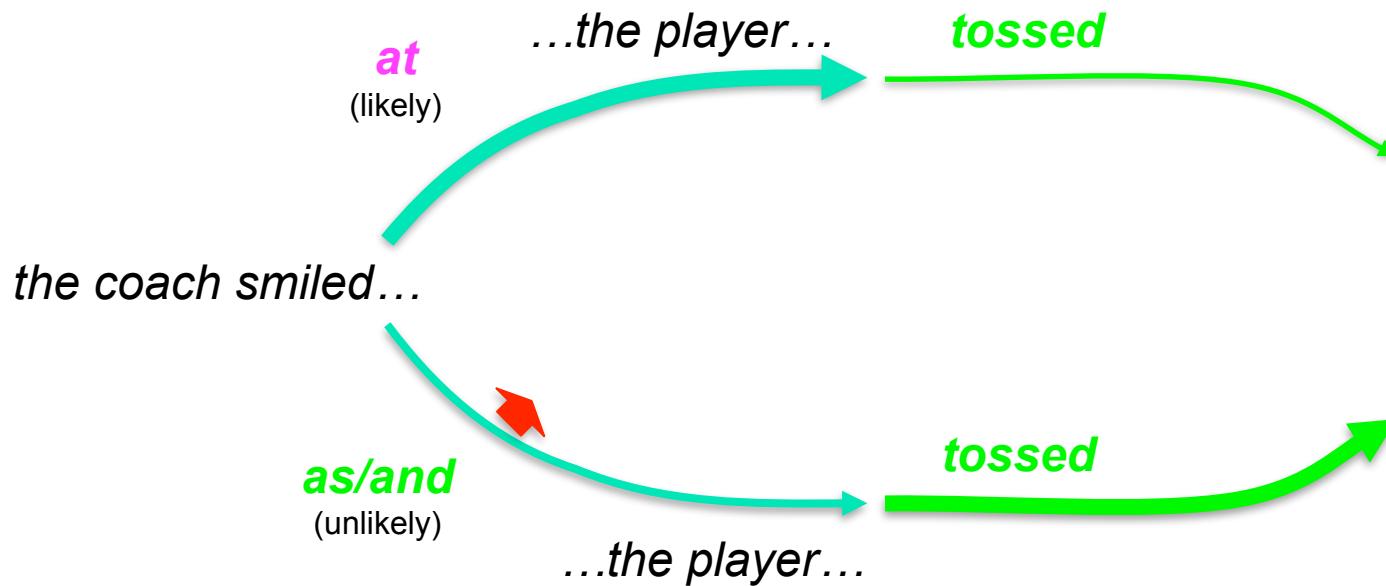
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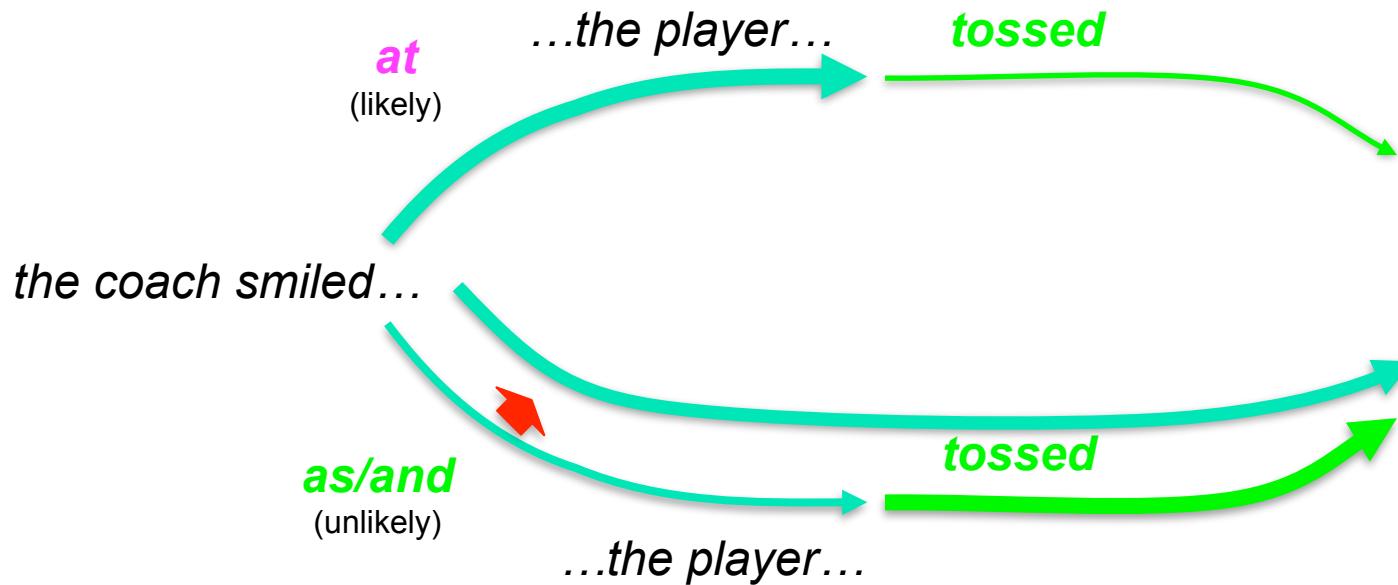
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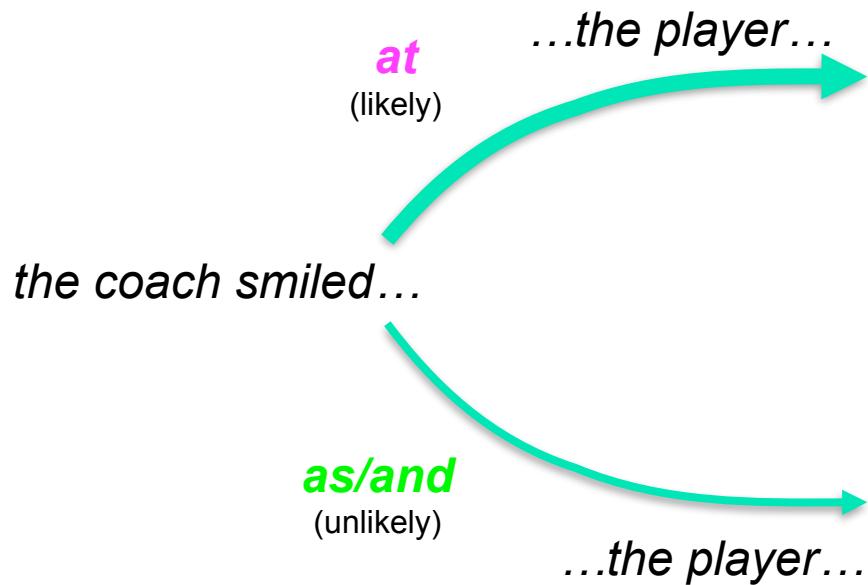
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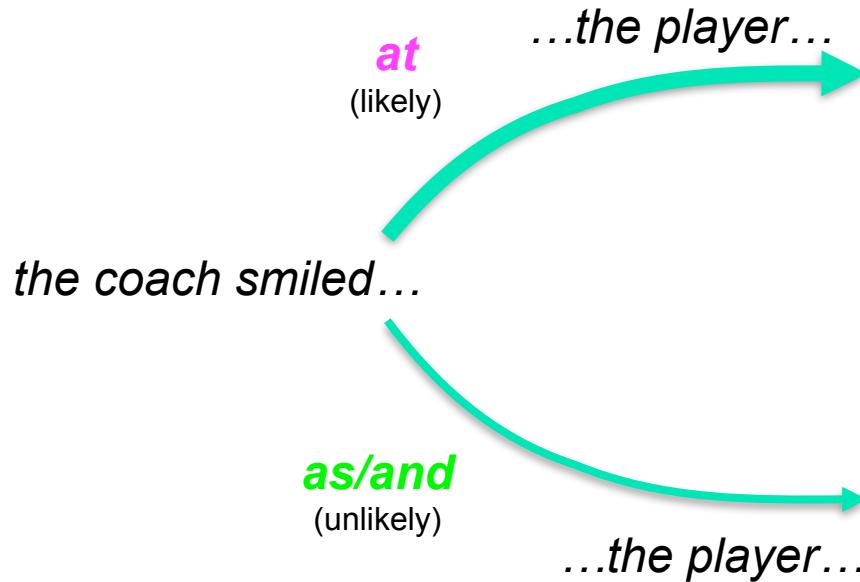
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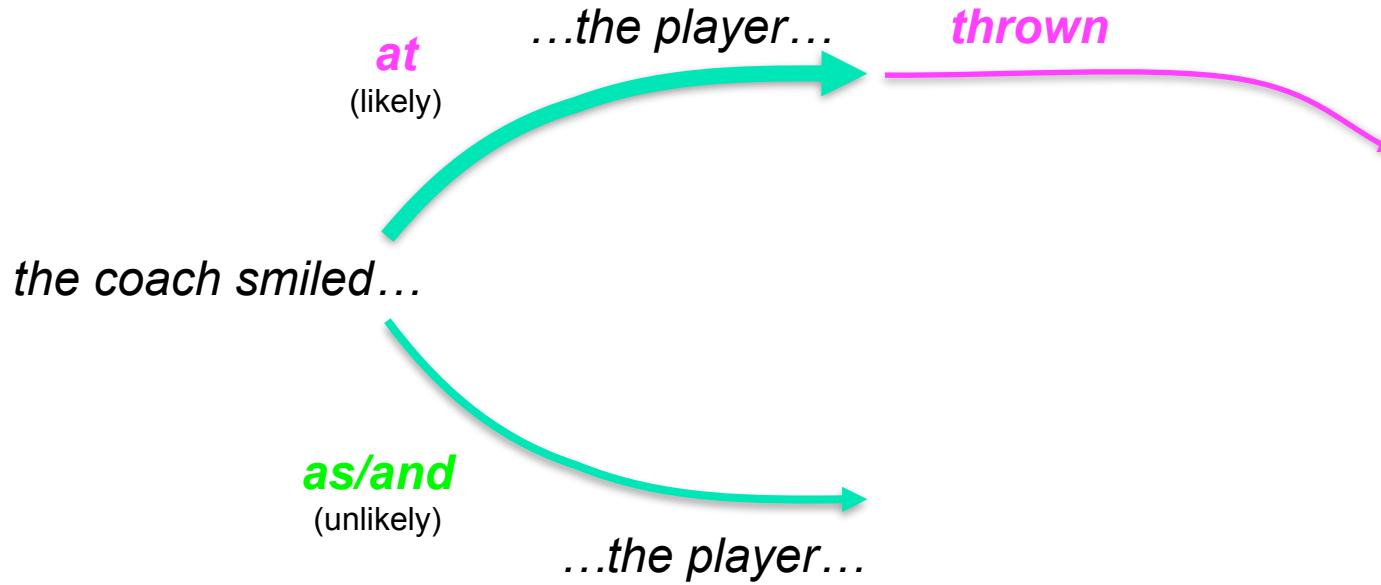
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 - This creates a large shift in belief in the *tossed* condition

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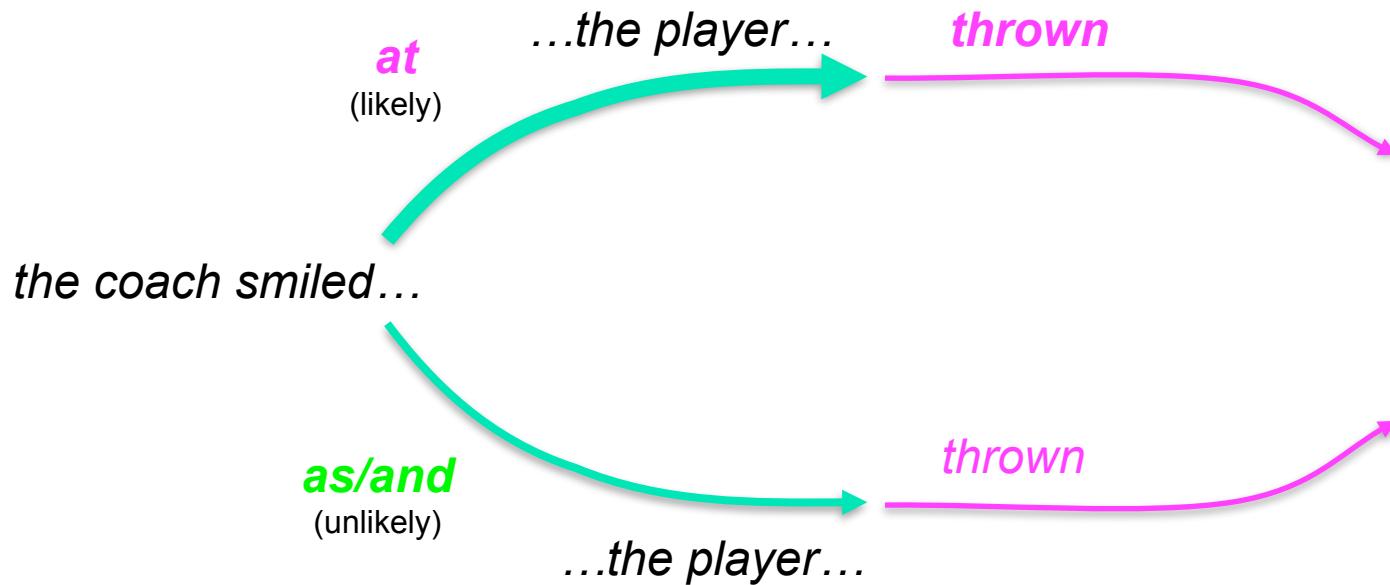
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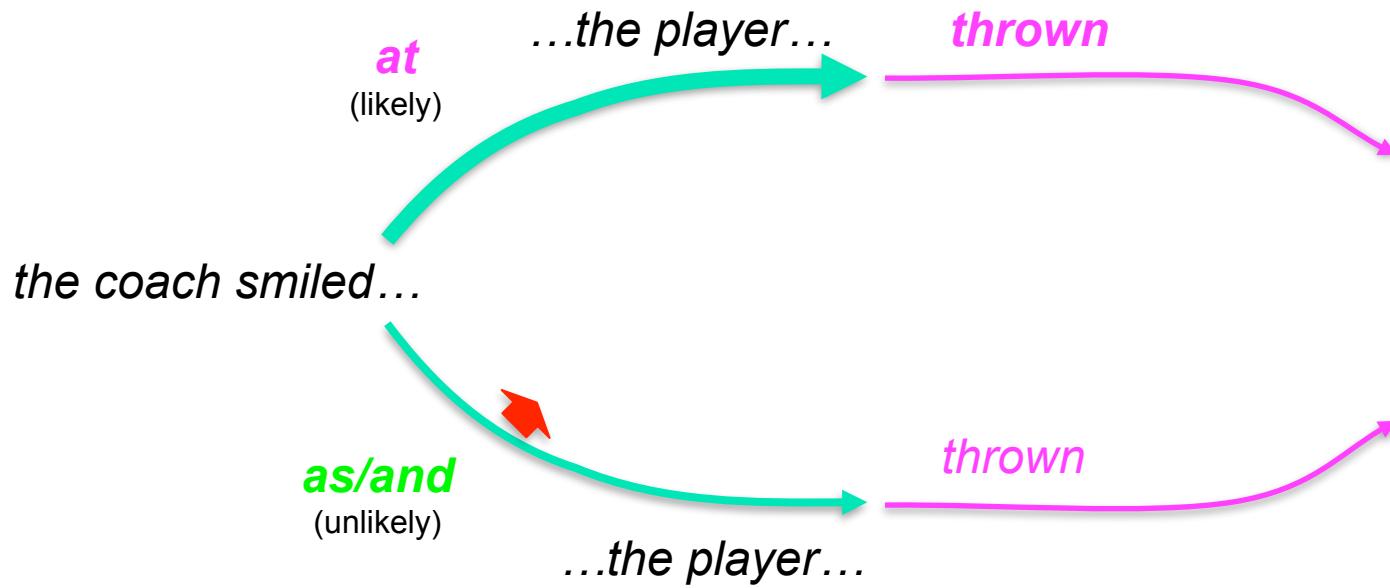
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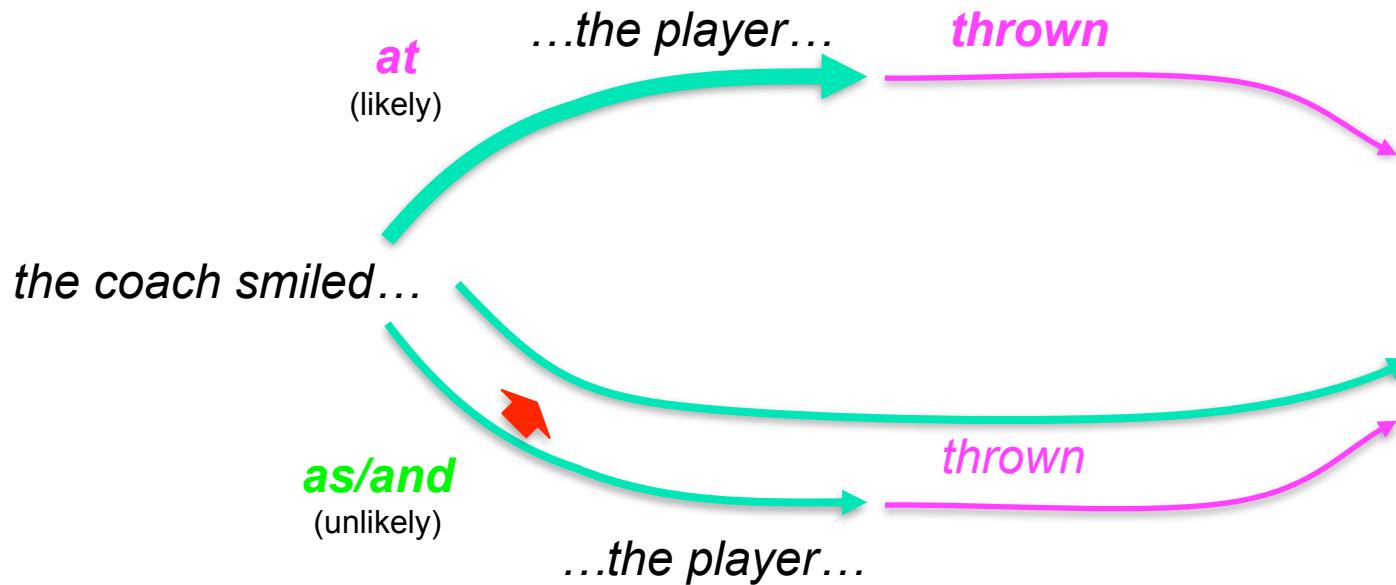
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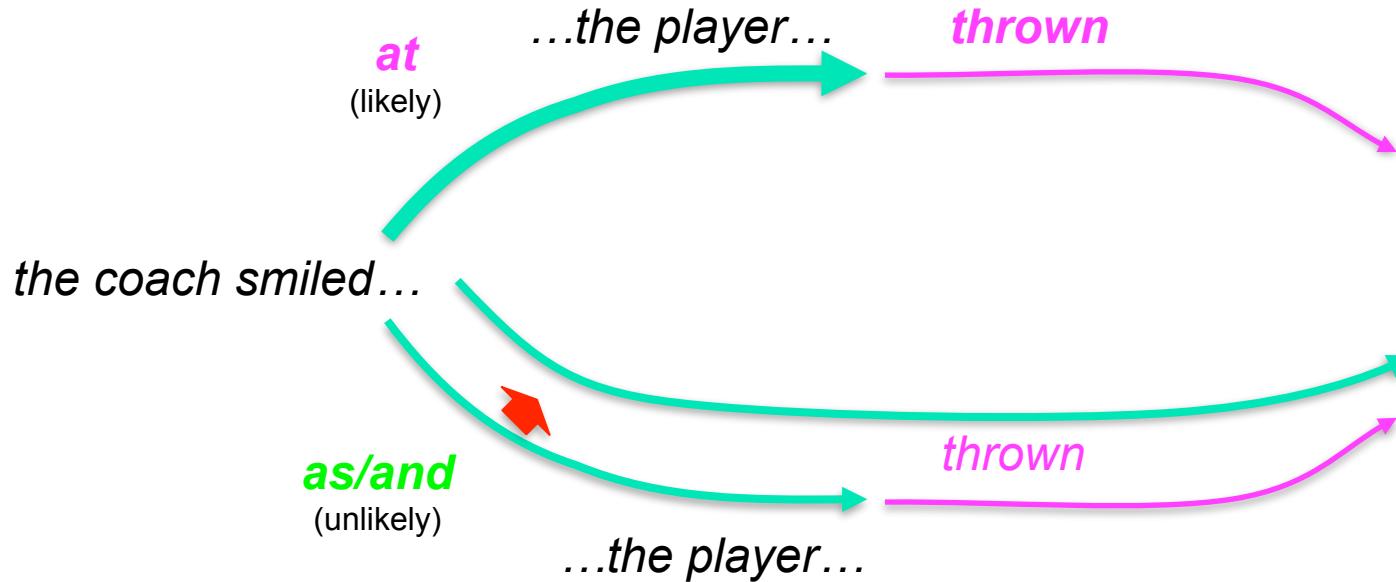
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- *tossed* is more likely to happen along the bottom path
 - This creates a large shift in belief in the *tossed* condition
- *thrown* is very unlikely to happen along the bottom path
 - As a result, there is no corresponding shift in belief

Ingredients for the model

$$P(\mathbf{w}|\mathbf{w}^*) \propto P_C(\mathbf{w}) Q(\mathbf{w}, \mathbf{w}^*)$$


Prior Expected evidence

Ingredients for the model

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Prior Expected evidence

- $Q(\mathbf{w}, \mathbf{w}^*)$ comes from K_{LD} (with minor changes)

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The equation is shown with two curly braces underneath. The first brace, under $P_C(\mathbf{w})$, is labeled "Prior" in blue. The second brace, under $Q(\mathbf{w}, \mathbf{w}^*)$, is labeled "Expected evidence" in blue.

- $Q(\mathbf{w}, \mathbf{w}^*)$ comes from K_{LD} (with minor changes)
- $P_C(\mathbf{w})$ comes from a probabilistic grammar (this time finite-state)

Ingredients for the model

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- $Q(\mathbf{w}, \mathbf{w}^*)$ comes from K_{LD} (with minor changes)
- $P_C(\mathbf{w})$ comes from a probabilistic grammar (this time finite-state)
- We need one more ingredient:
 - a **quantified signal** of the alarm induced by word w , about changes in beliefs about the past

Quantifying alarm about the past

Quantifying alarm about the past

- *Relative Entropy* (KL-divergence) is a natural metric of change in a probability distrib. (Levy, 2008; Itti & Baldi, 2005)

$$D(P || Q) = \sum_x P(x) \log \frac{P(x)}{Q(x)}$$

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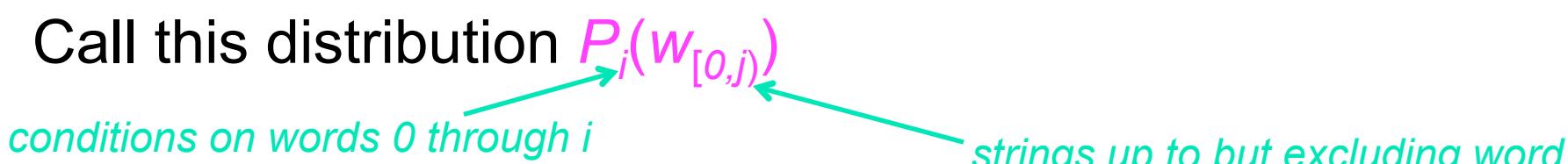
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- The change induced by w_i is the **error identification signal EIS_i**, defined as

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new distribution

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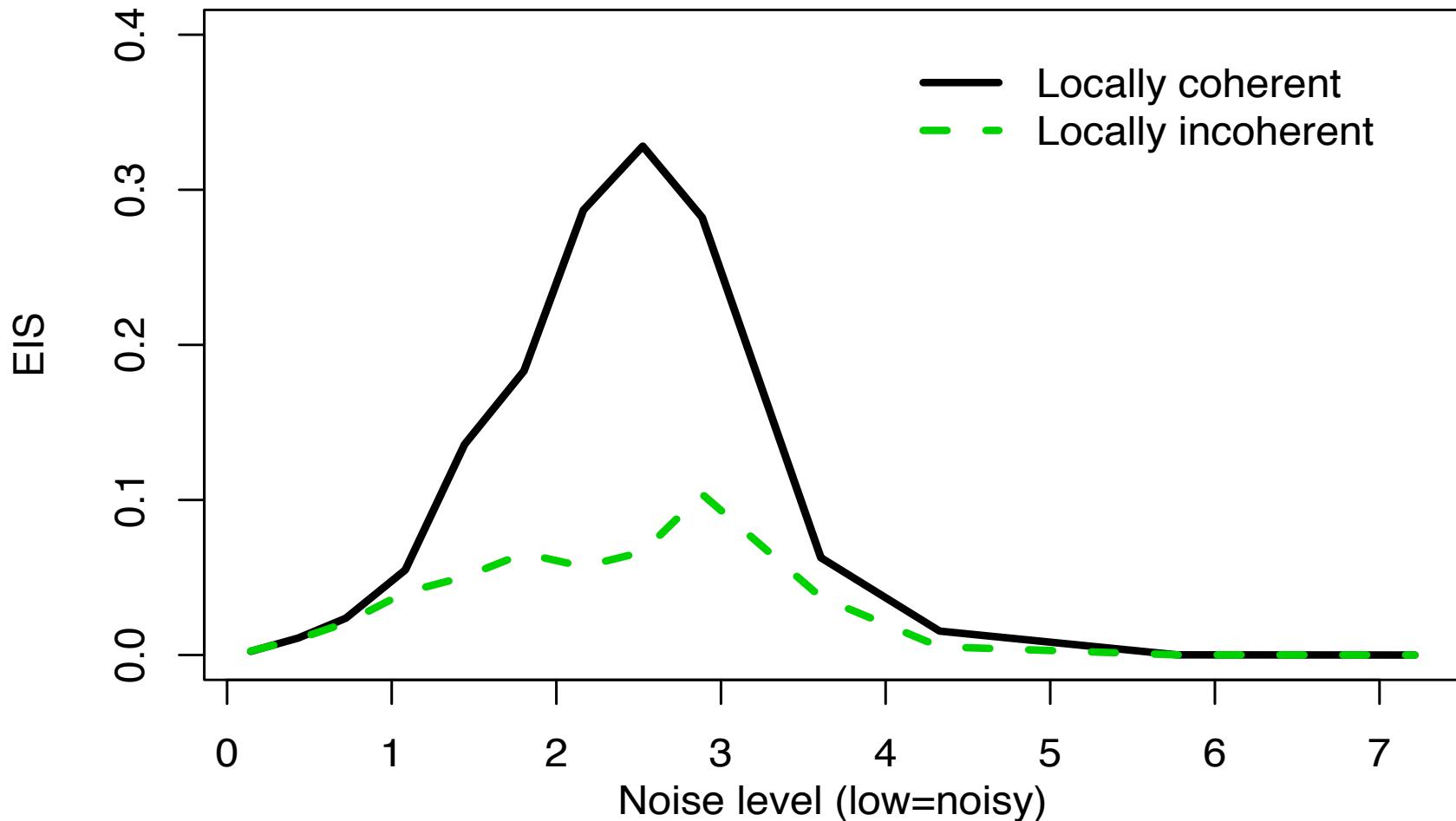
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Results on local-coherence sentences

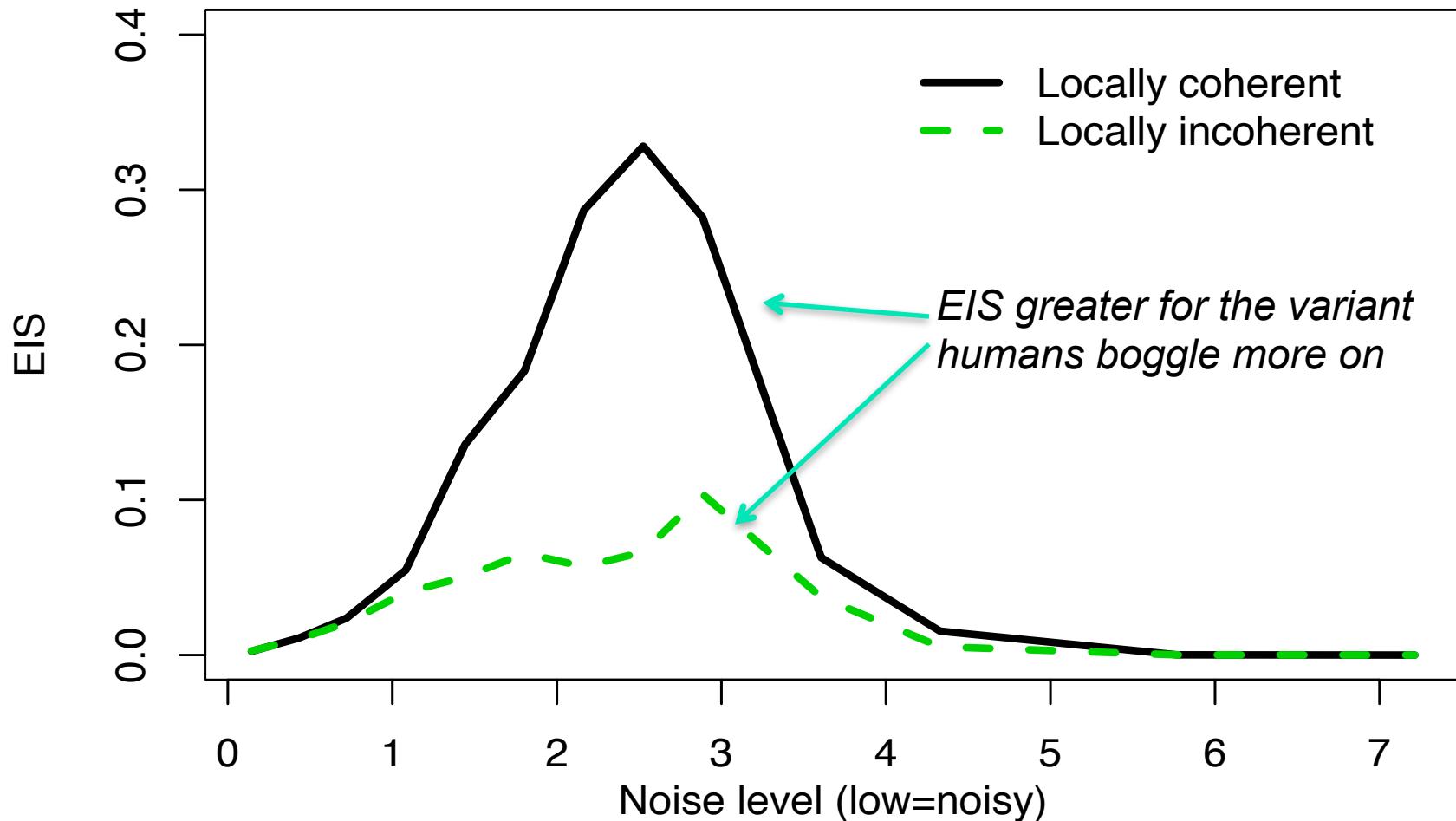
- Locally coherent: *The coach smiled at the player tossed the frisbee*
- Locally incoherent: *The coach smiled at the player thrown the frisbee*



(All sentences of Tabor et al. 2004 with lexical coverage in model)

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Today's summary

- Reviewed principles of rational analysis and its application to theory of language comprehension
- Examined a phenomenon challenging for surprisal theory
- Proposed a noisy-channel processing theory, using information theory and probabilistic grammars
- Developed a hypothesis within the theory for the challenging phenomenon
-

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Prediction 2: hallucinated garden paths

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While the clouds crackled, above the glider soared a magnificent eagle.

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While the clouds crackled, above the glider soared a magnificent eagle.

- There's a garden-path clause in this sentence...

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- Readers are ordinarily very good at using commas to guide syntactic analysis:

While the man hunted, the deer ran into the woods

While Mary was mending the sock fell off her lap

- “With a comma after *mending* there would be no syntactic garden path left to be studied.” (Fodor, 2002)

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- We'll see that the story is slightly more complicated.

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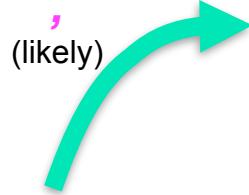
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- Inferences through ...*glider* should thus involve a tradeoff between perceptual input and prior expectations

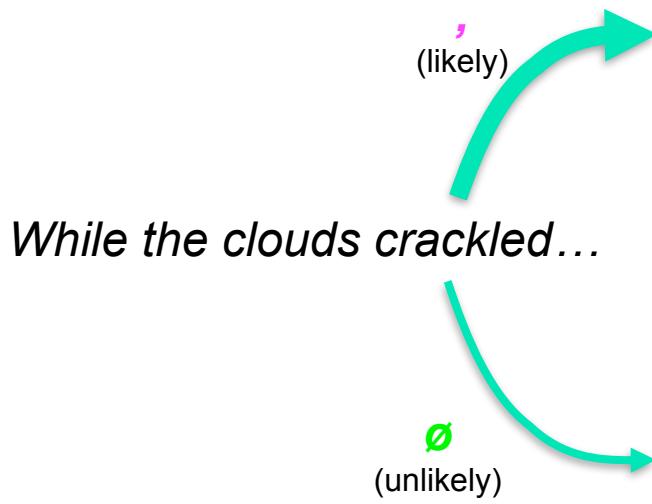
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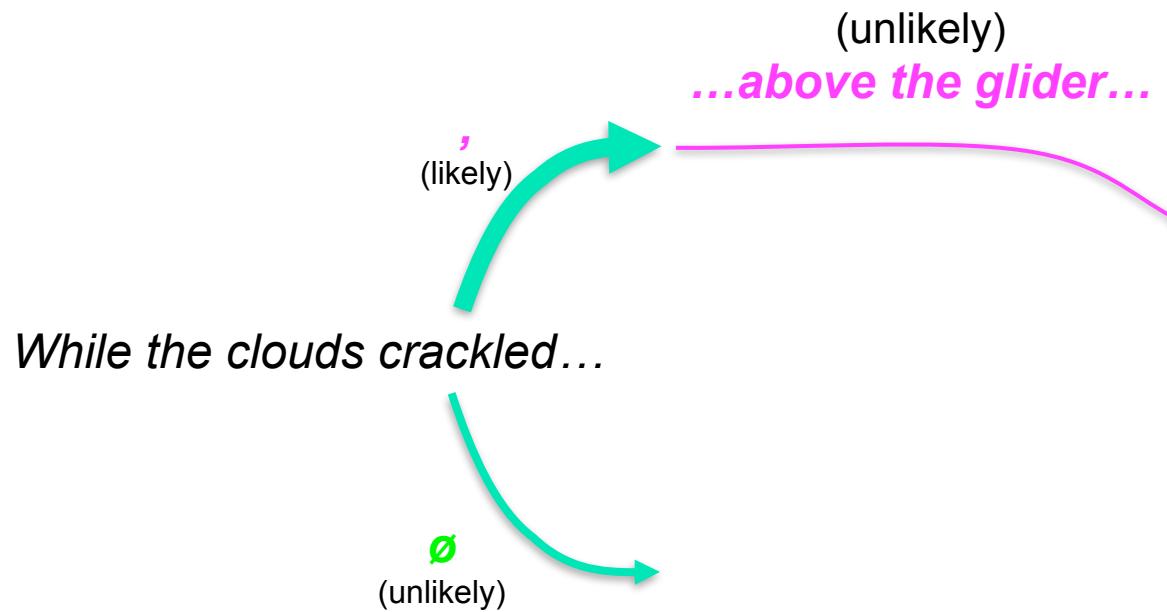


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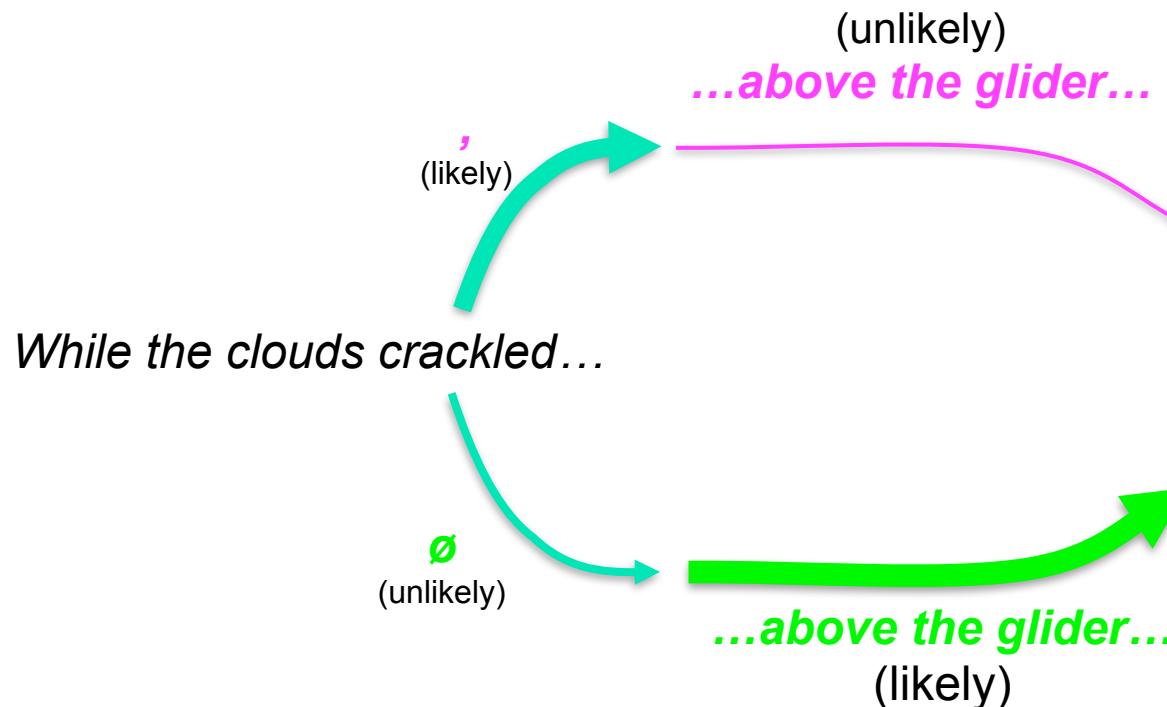
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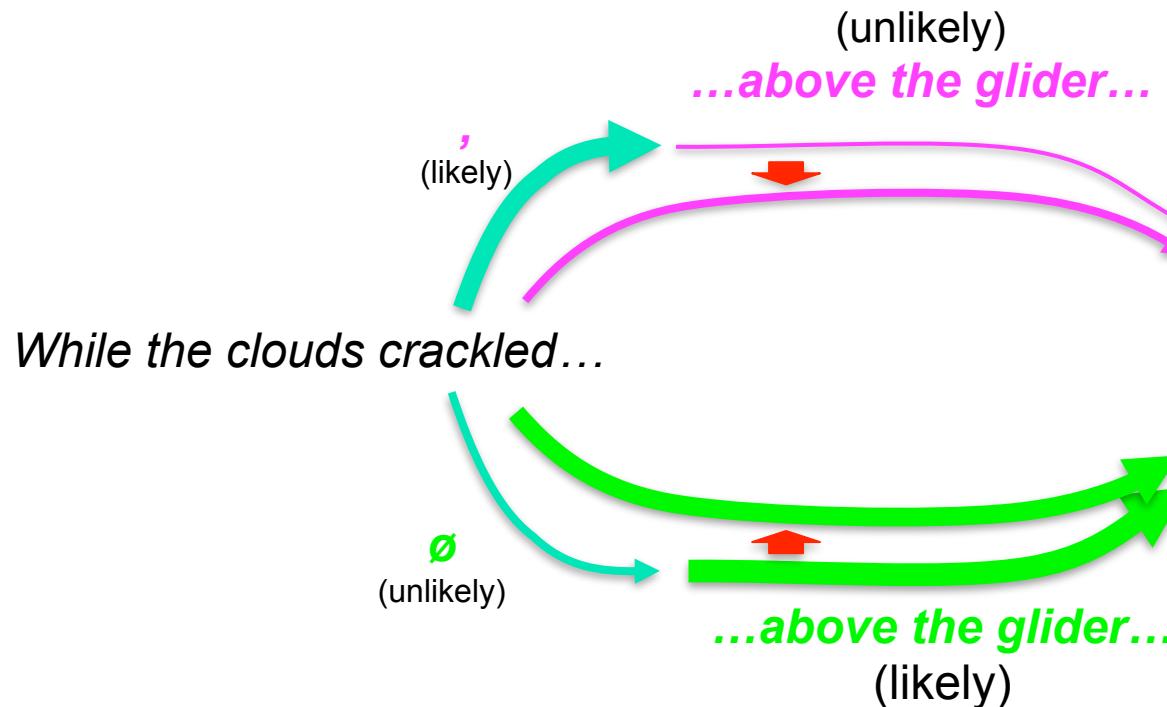
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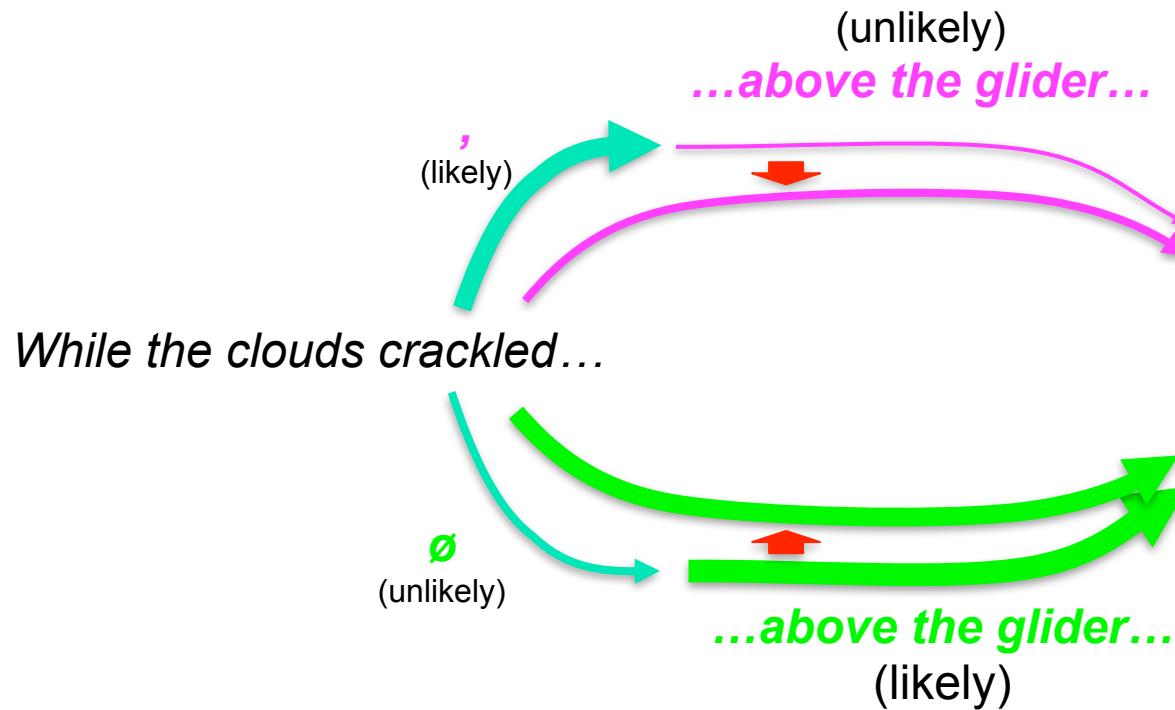
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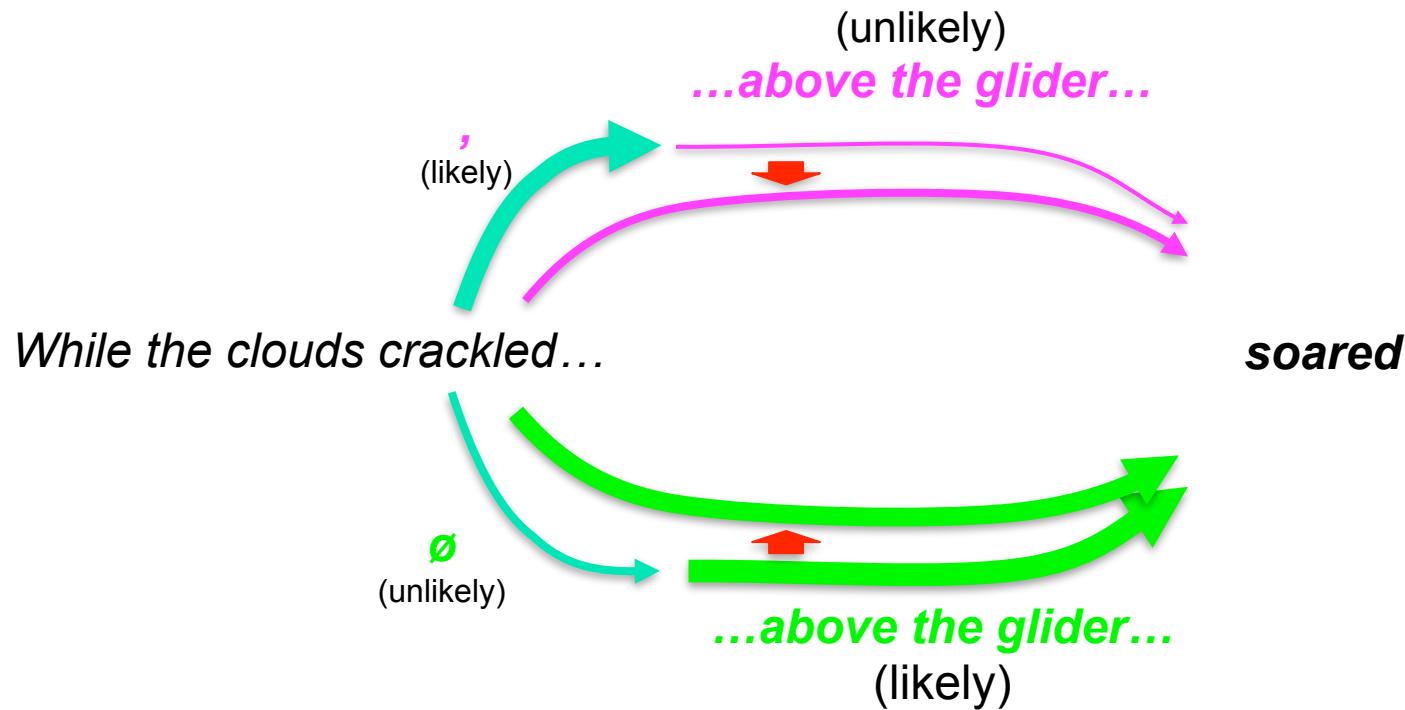
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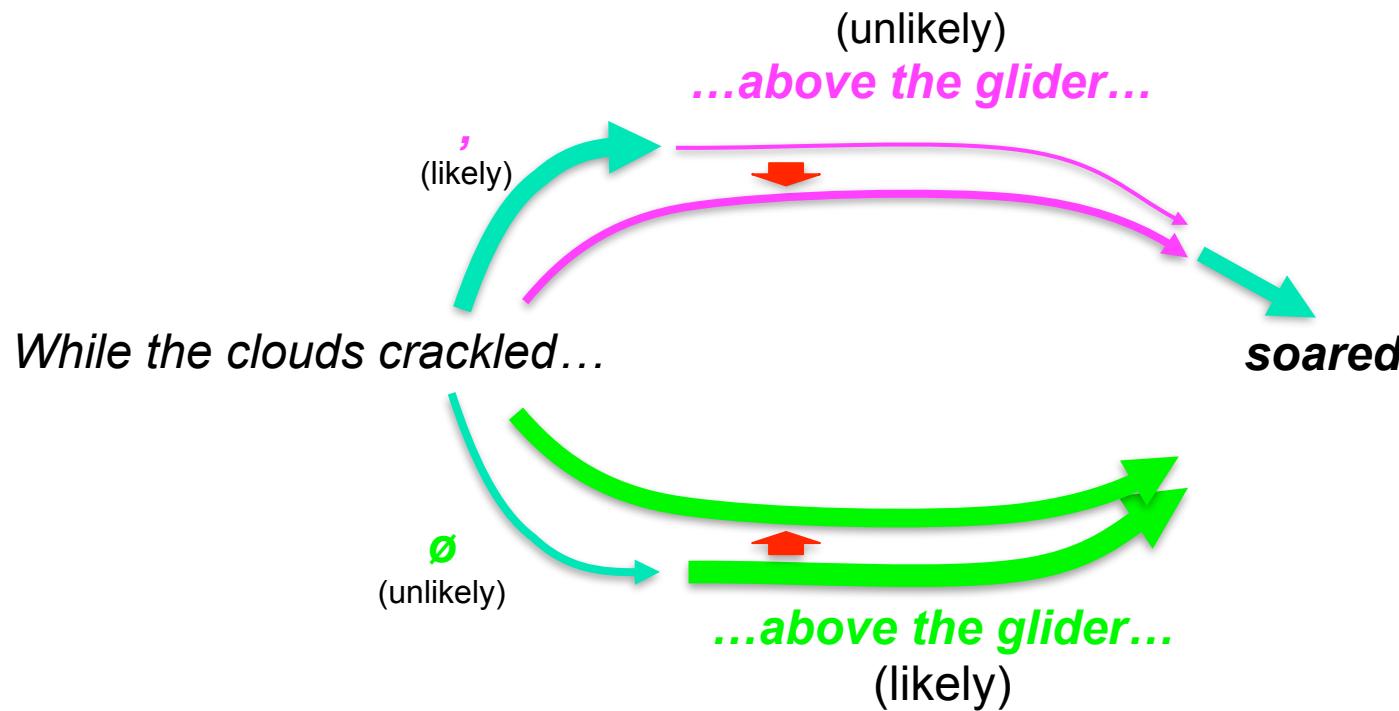
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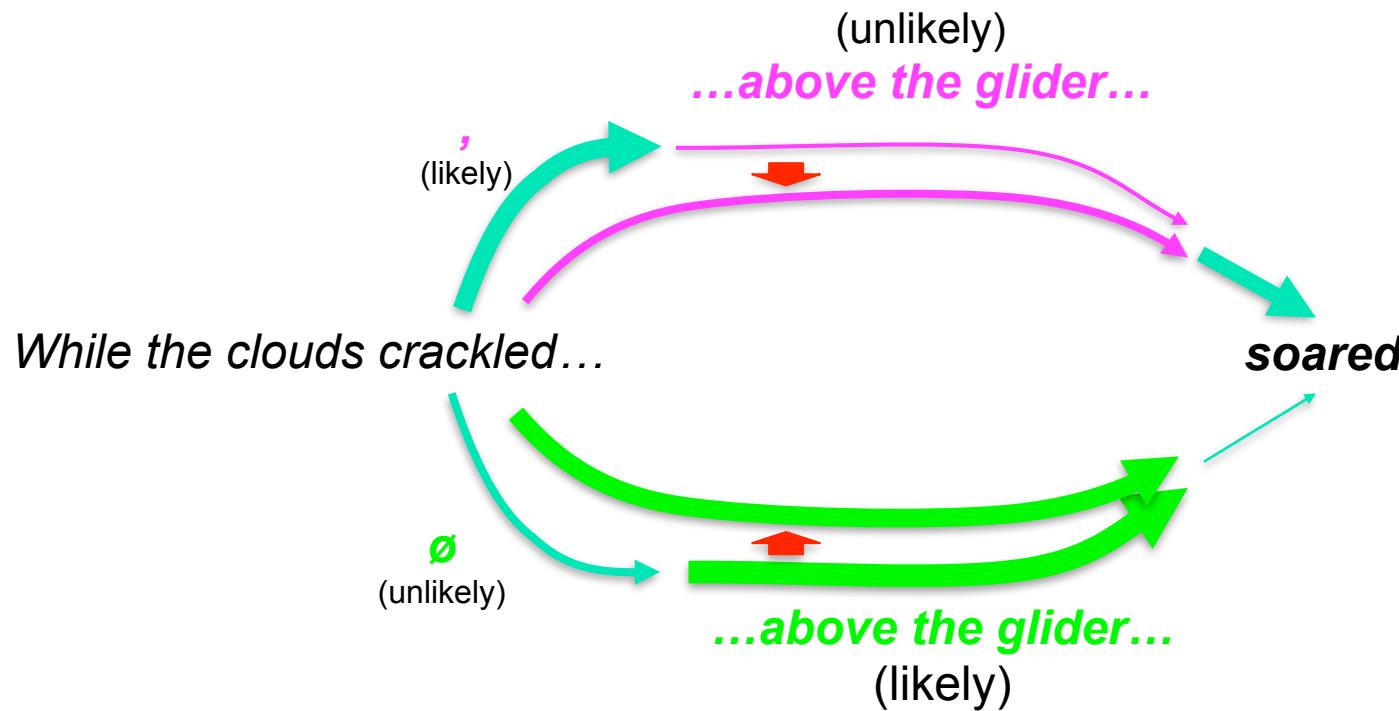
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- These inferences together make *soared* very surprising!



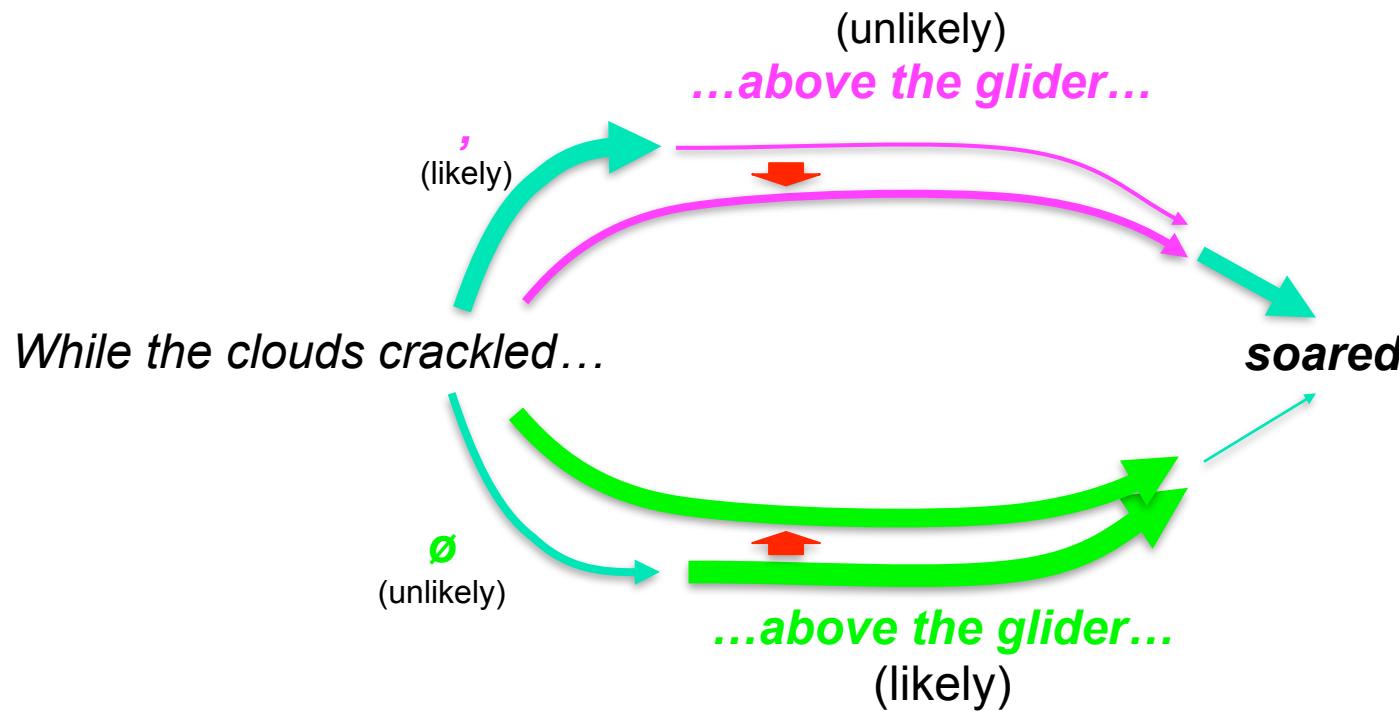
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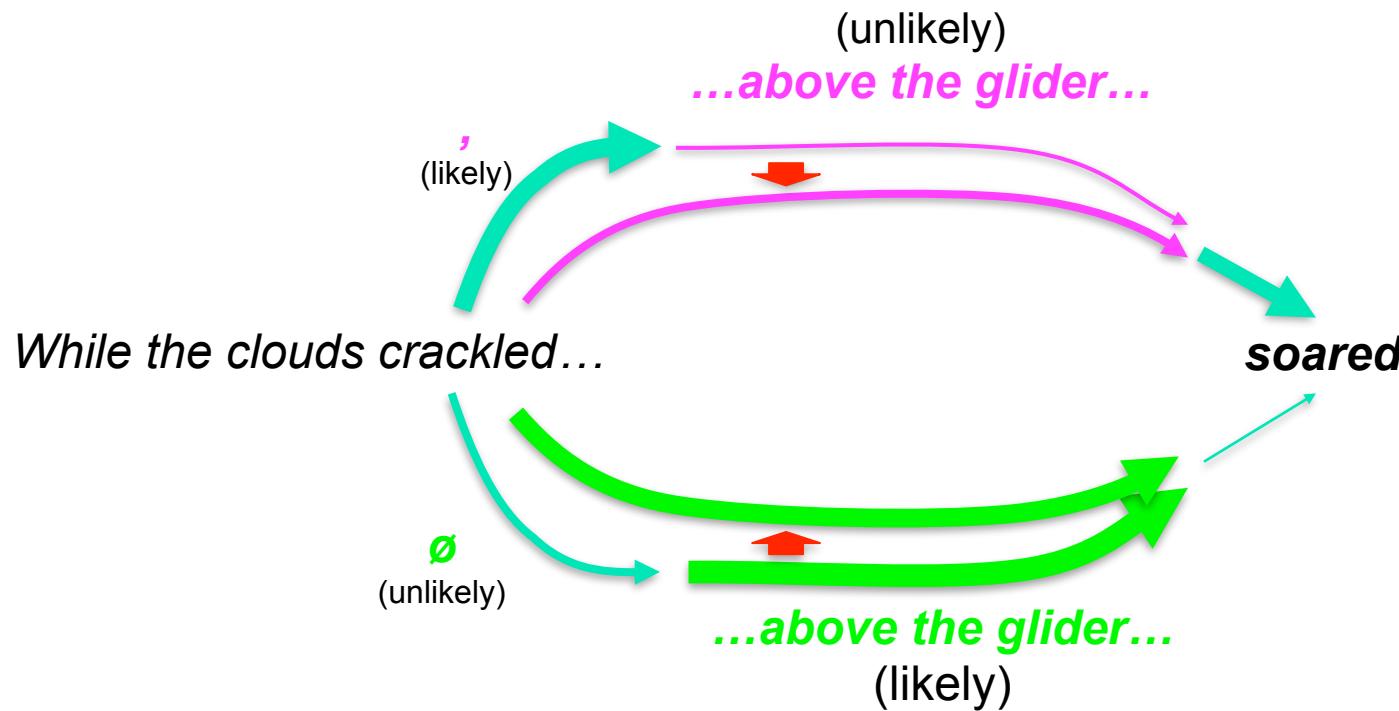


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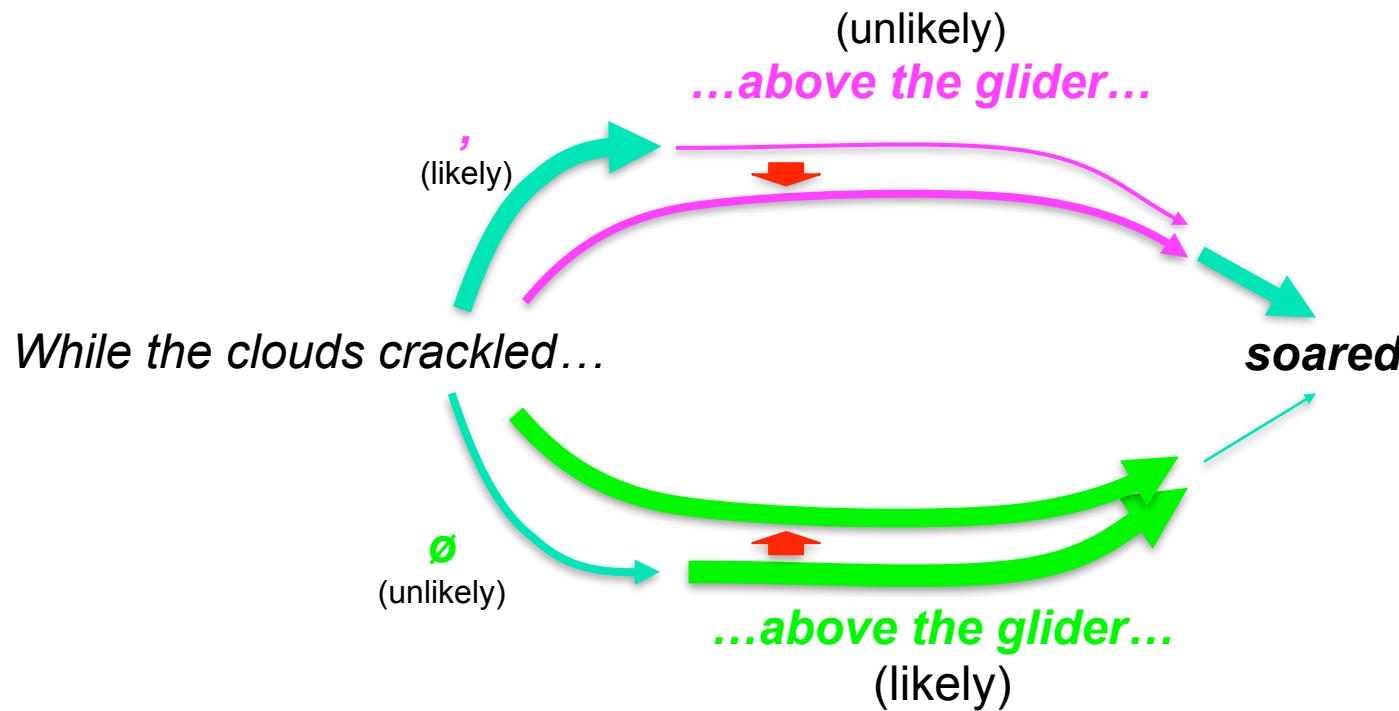
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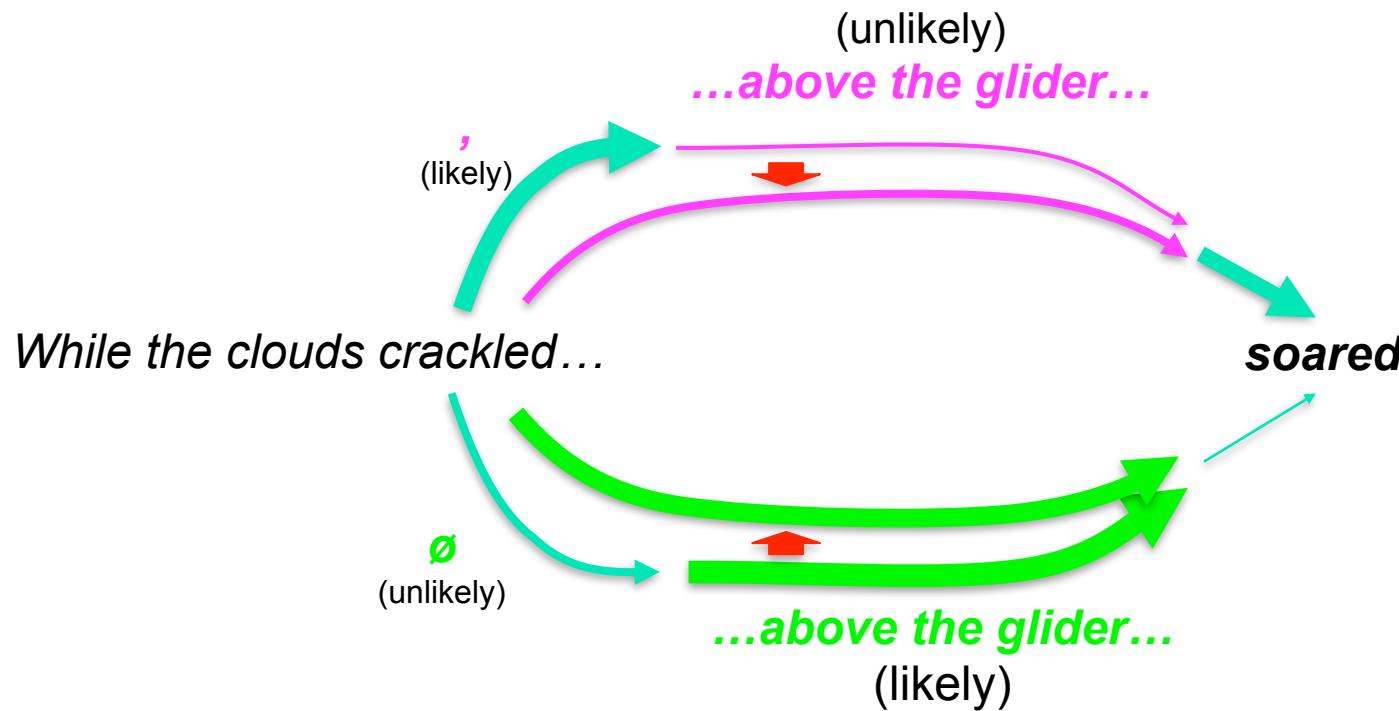
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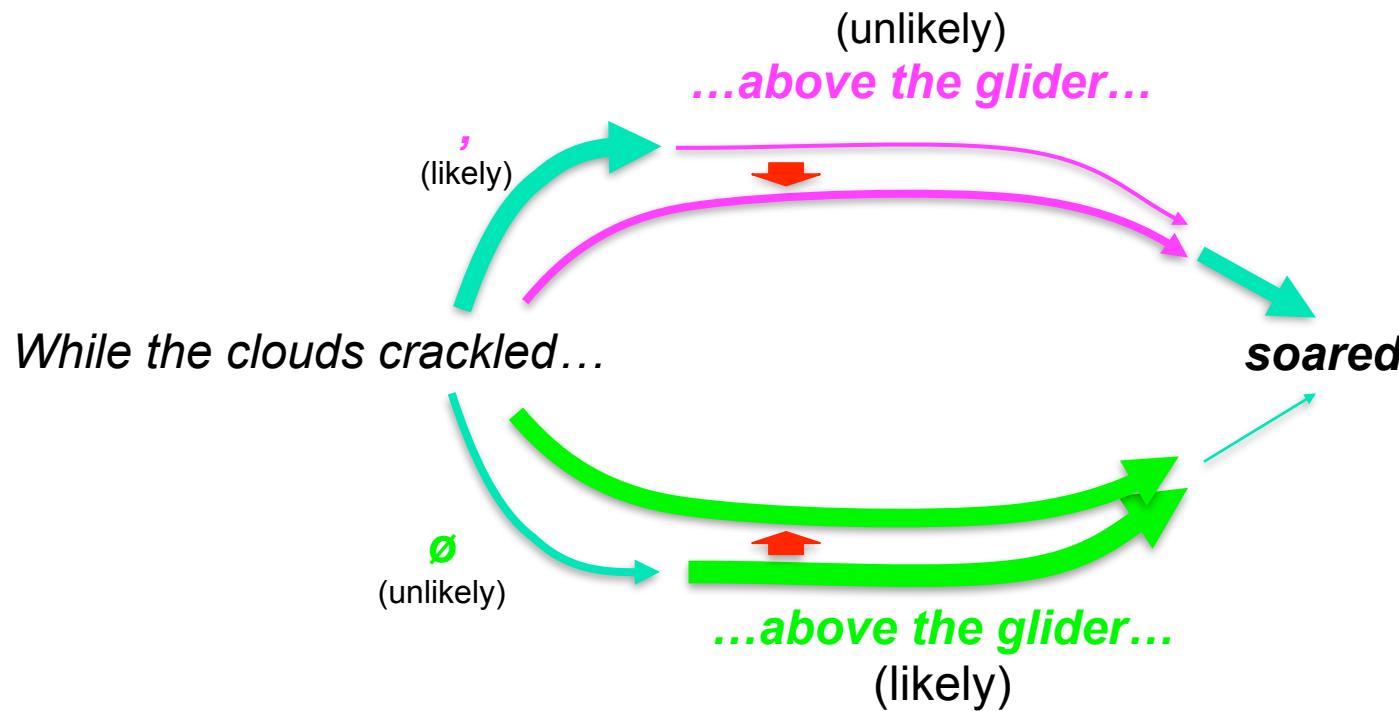
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- Two properties come together to create “hallucinated garden path”
 1. Subordinate clause into which the main-clause inverted phrase would fit well
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- The phrase *in the distance* fulfills a similar thematic role as above the glider for crackled

Prediction 2: hallucinated garden paths

- Two properties come together to create “hallucinated garden path”
 1. Subordinate clause into which the main-clause inverted phrase would fit well
 2. Main clause with locative inversion
- Experimental design: cross (1) and (2)

While the clouds crackled, above the glider soared a magnificent eagle.

While the clouds crackled, the glider soared above a magnificent eagle.

While the clouds crackled in the distance, above the glider soared a magnificent eagle.

While the clouds crackled in the distance, the glider soared above a magnificent eagle.

- The phrase *in the distance* fulfills a similar thematic role as above the glider for crackled
- Should reduce hallucinated garden-path effect

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Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading
- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading
-
- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

white-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

white-the-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

white-the-eleuds-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

white-the-elouds-erackled,-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

white-the-eleuds-erackled,-above-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

white-the-eleuds-crackled,-above-the-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

white-the-eleuds-crackled,-above-the-glider-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

white-the-eleuds-crackled,-above-the-glider-seared-----

- Readers aren't allowed to backtrack

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

white-the-~~the~~-clouds-crackled,-above-the-glider-soared-----

- Readers aren't allowed to backtrack
- So the comma is visually *gone* by the time the inverted main clause appears

Prediction 2: Hallucinated garden paths

- Methodology: word-by-word self-paced reading

white-the-~~the~~-heads-crackled,-above-the-glider-soared-----

- Readers aren't allowed to backtrack
- So the comma is visually *gone* by the time the inverted main clause appears
- Simple test of whether beliefs about previous input can be revised

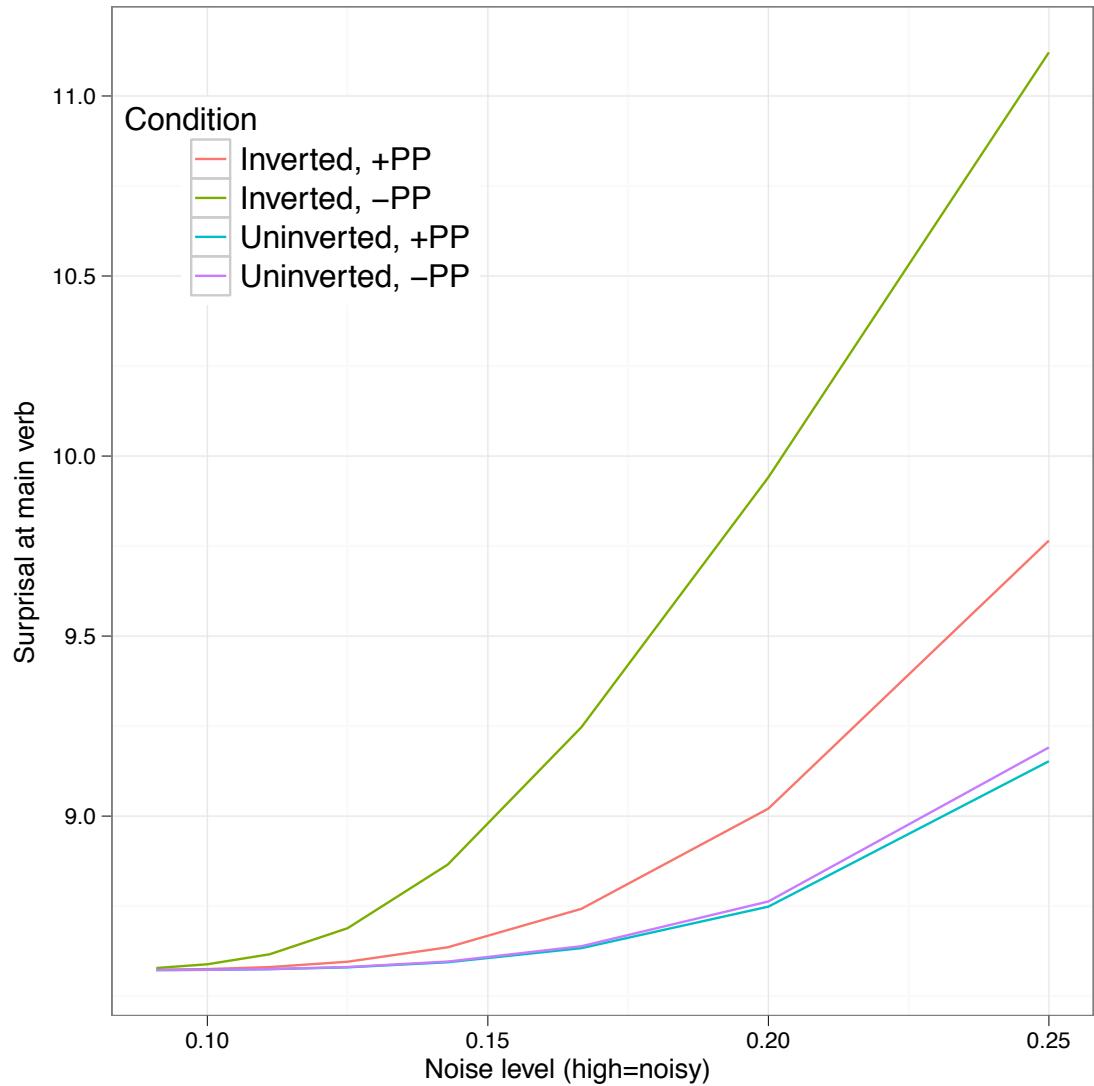
Model predictions

While the clouds
crackled, **above** the
glider soared a
magnificent eagle.

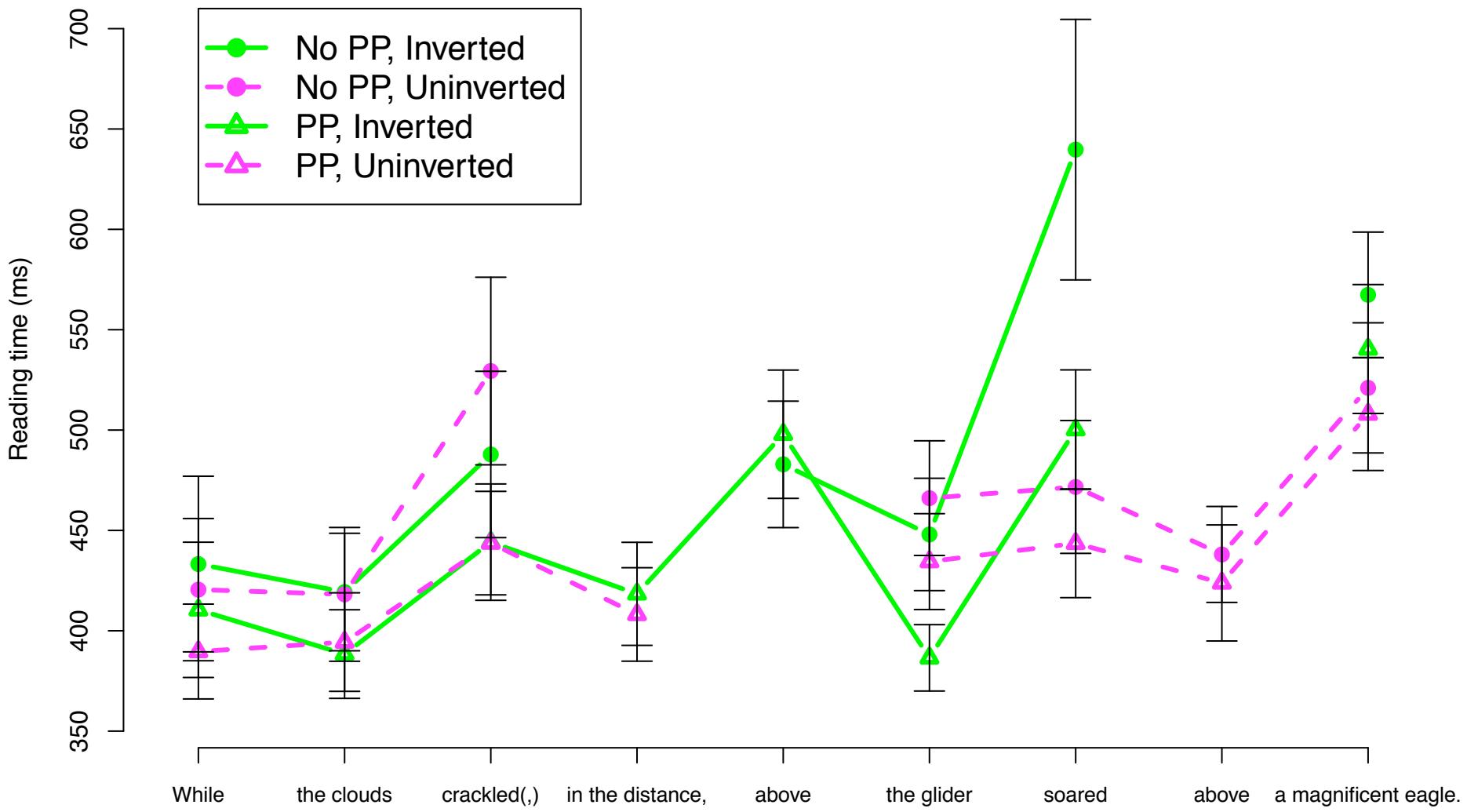
While the clouds **crackled**
in the distance, **above**
the glider soared a
magnificent eagle.

While the clouds
crackled, the glider
soared **above** a
magnificent eagle.

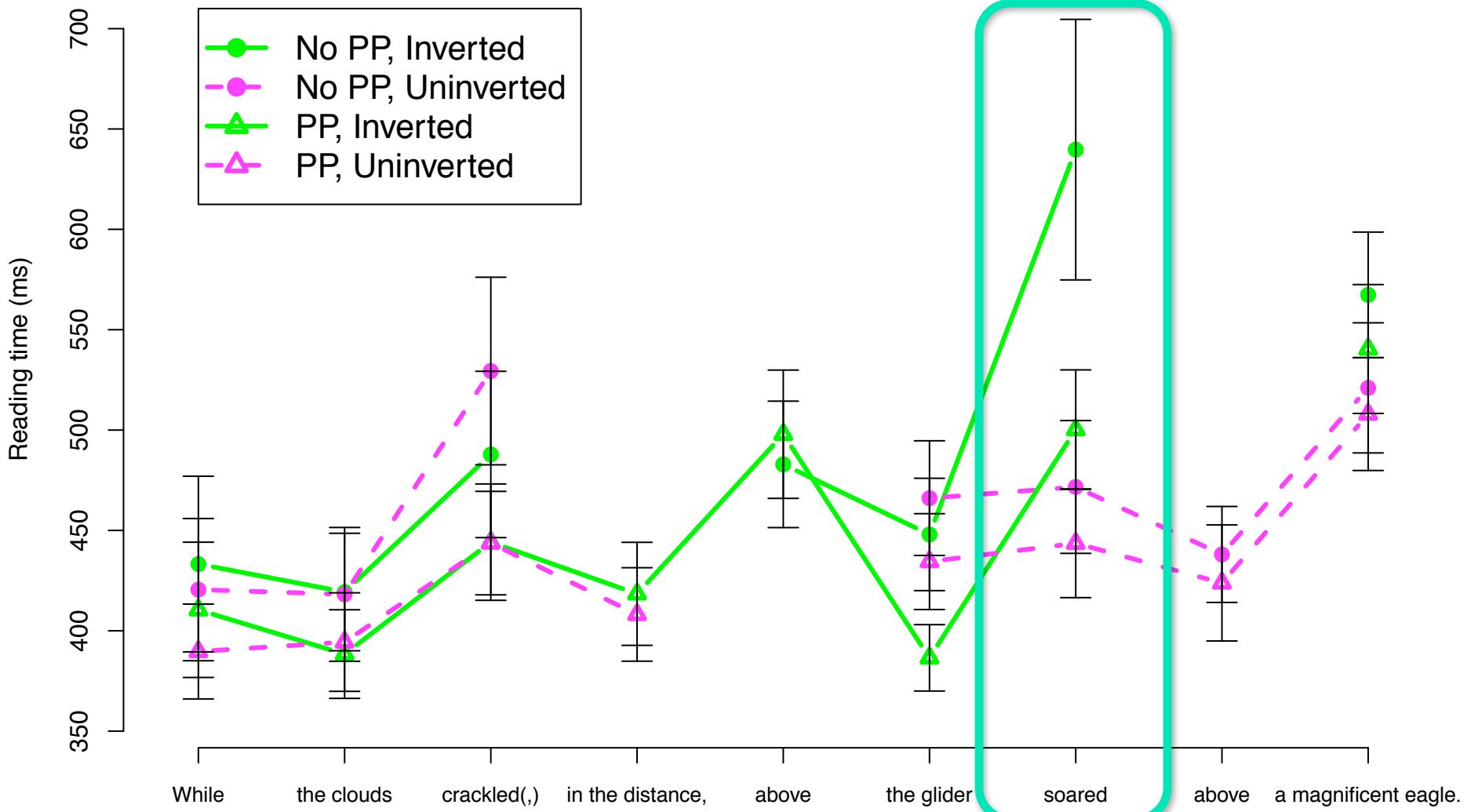
While the clouds **crackled**
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glider soared **above** a
magnificent eagle.



Results: whole sentence reading times

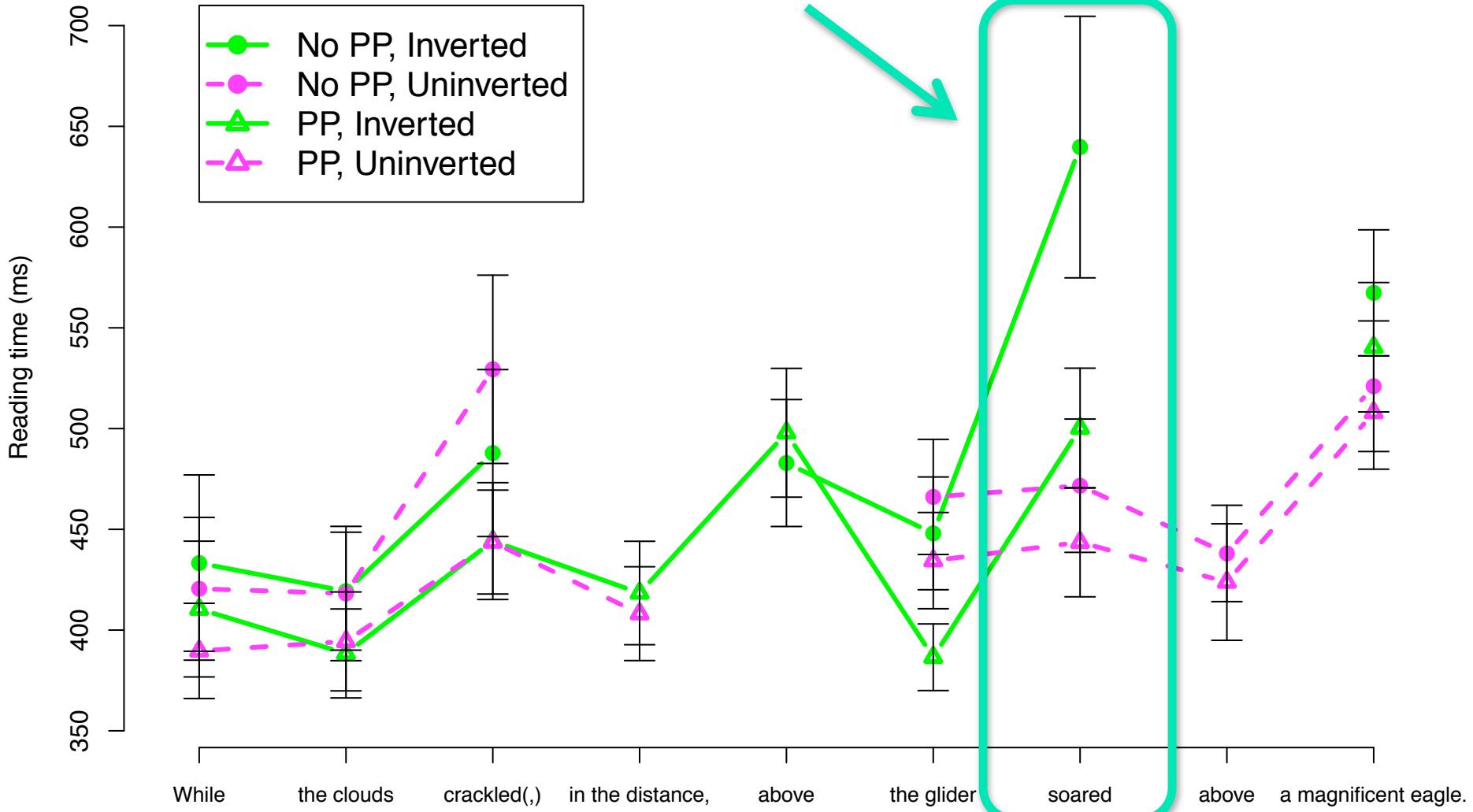


Results: whole sentence reading times



Results: whole sentence reading times

Processing boggle occurs exactly where predicted



Hallucinated garden-path summary

- The *at/toward* study showed that comprehenders *note the possibility of alternative strings and act on it*
- This study showed that comprehenders can actually *devote resources to grammatical analyses inconsistent with the surface string*

Hallucinated garden paths cont'd

- Sure, but punctuation's weird stuff
 - What about *real words*?
-
- At least sometimes, bias *against N N interpretation*

Hallucinated garden paths cont'd

- Sure, but punctuation's weird stuff
- What about *real words*?

I know that the desert trains could resupply the camp.

- At least sometimes, bias *against N N interpretation*

Hallucinated garden paths cont'd

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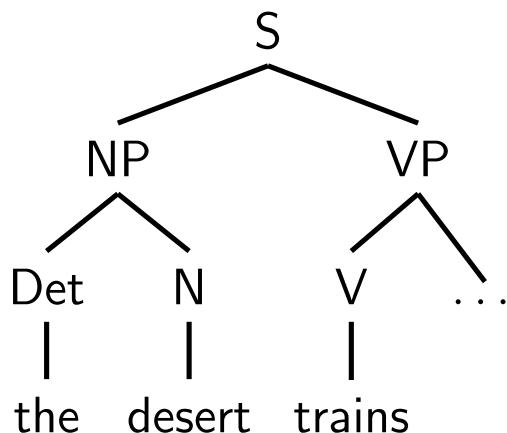
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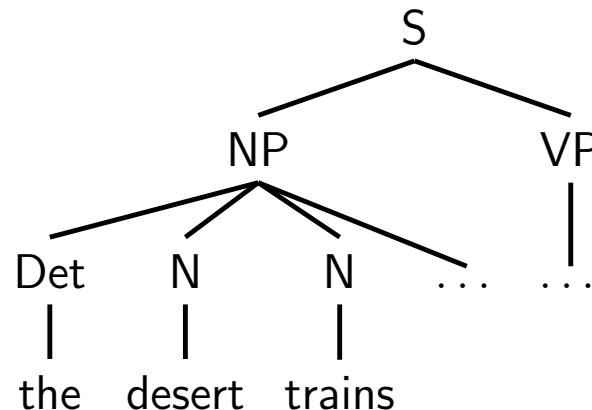
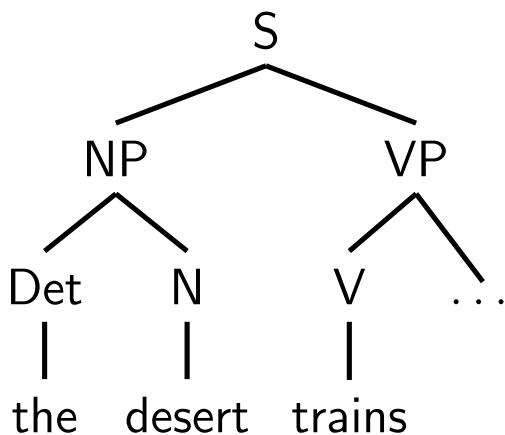


- At least sometimes, bias *against* N N interpretation

Hallucinated garden paths cont'd

- Sure, but punctuation's weird stuff
- What about *real words*?

I know that the desert trains could resupply the camp.



- At least sometimes, bias against N N interpretation

Hallucinated GPs with words

Could be “intern chauffeured”

Could NOT be “inexperienced chauffeured”

Hallucinated GPs with words

- We use a contextual bias against NN and toward NV to test for GP hallucinations involving wordform change

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Hallucinated GPs with words

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Could be “intern chauffeured”

The intern chauffeur for the governor hoped for more interesting work.
[NN, “dense” neighborhood]

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[NV, “dense” neighborhood]

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The inexperienced chauffeur for the governor hoped for more interesting work.
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[NN, “dense” neighborhood]

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[NV, “dense” neighborhood]

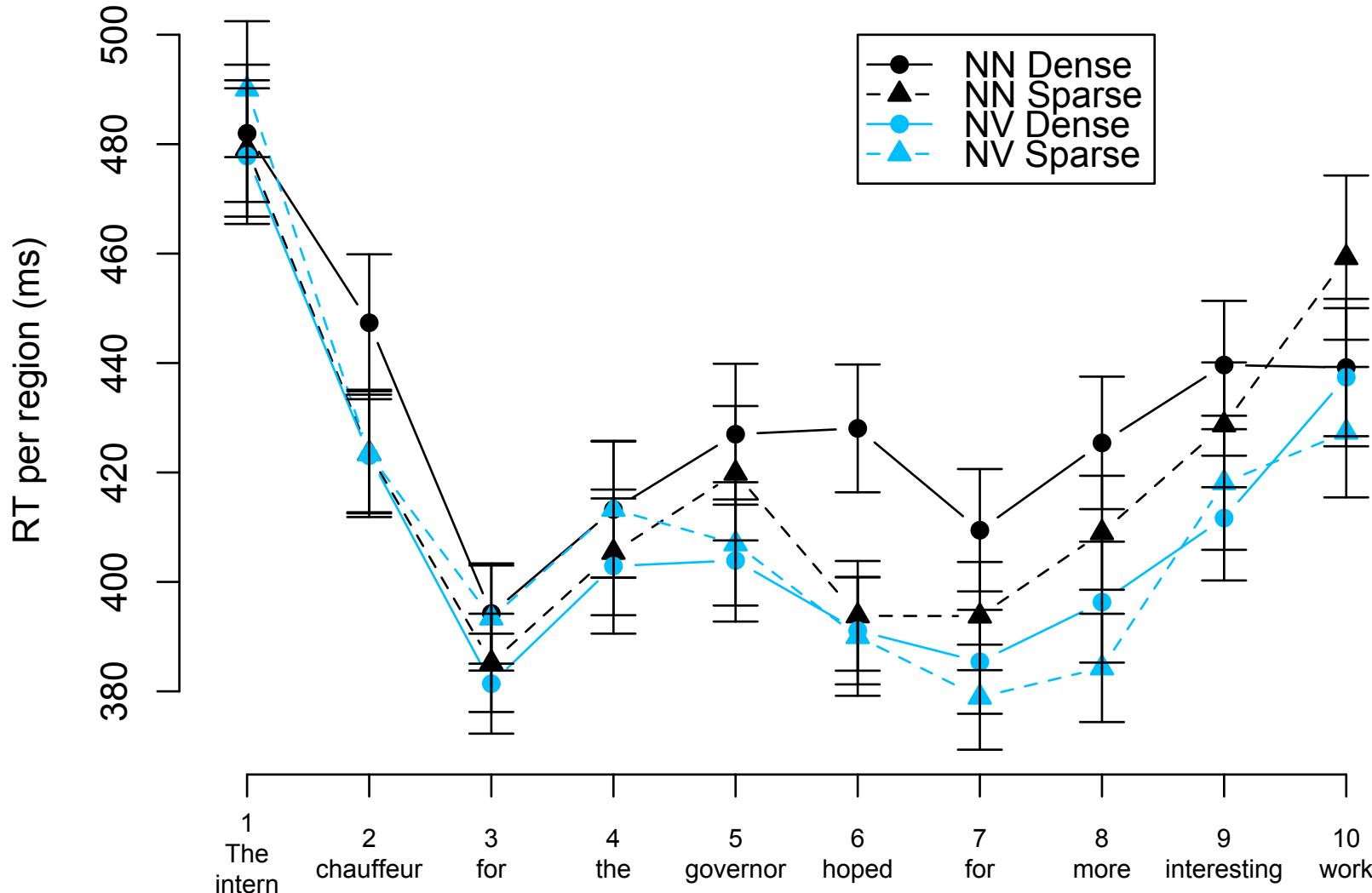
Could NOT be “inexperienced chauffeured”

The inexperienced chauffeur for the governor hoped for more interesting work.
[NN, “sparse” neighborhood]

Some interns chauffeured for the governor but hoped for more interesting work.
[NV, “sparse” neighborhood]

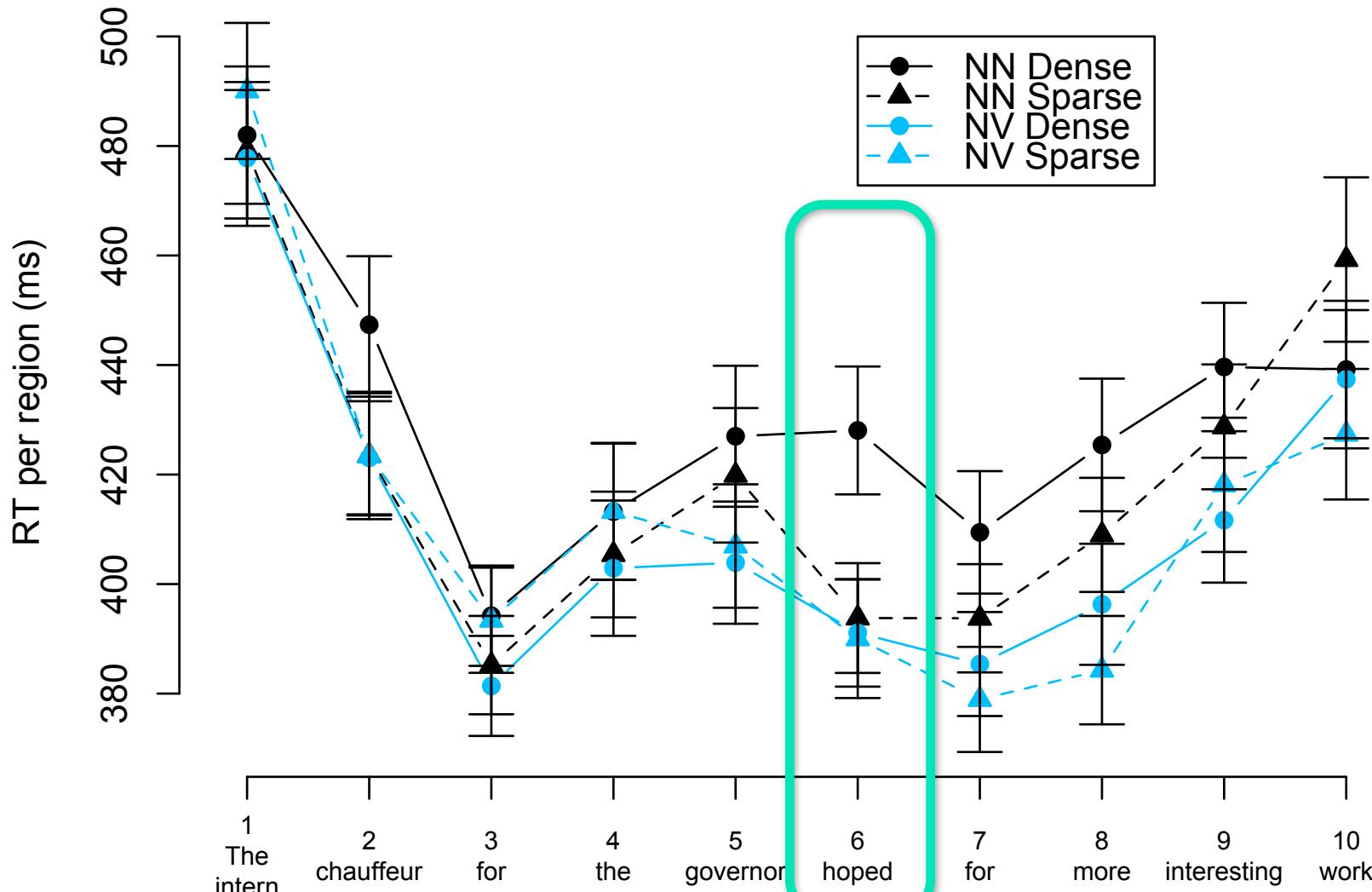
Results

- RT spike at disambiguating region for NN Dense

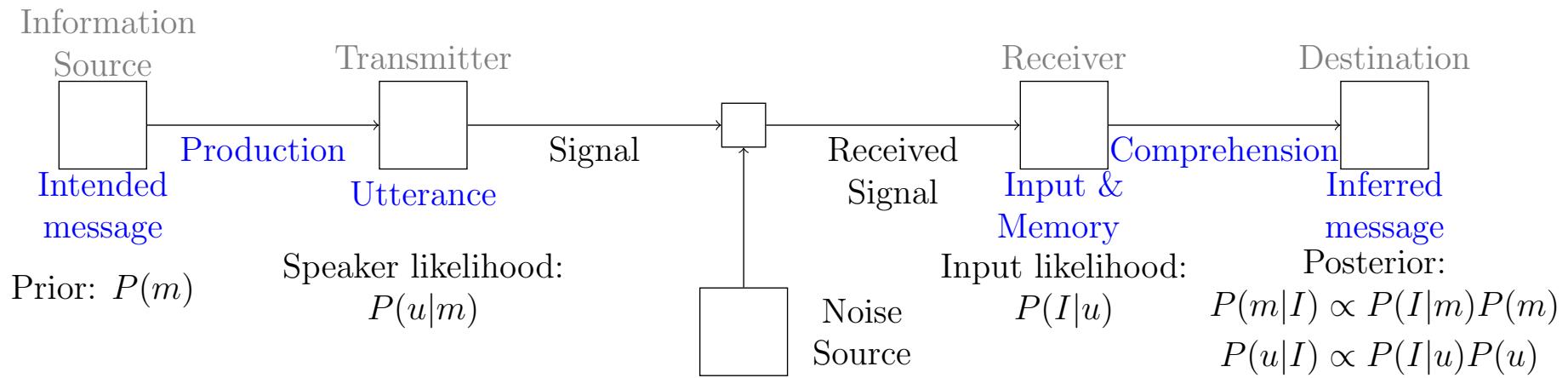


Results

- RT spike at disambiguating region for NN Dense



Noisy-channel theory of language processing



Simple question-answering

Simple question-answering

The woman lost the diamond.

Did the woman lose something?

Simple question-answering

The woman lost the diamond.

Did the woman lose something?

Yes

Simple question-answering

The woman lost the diamond.

Did the woman lose something?

Yes

The ball kicked the girl.

Did the girl kick something?

Simple question-answering

The woman lost the diamond.

Did the woman lose something?

Yes

The ball kicked the girl.

Did the girl kick something?

No

Simple question-answering

The woman lost the diamond.

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Did the girl kick something?

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The businessman benefited from the tax law.

Did the tax law benefit from anything?

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The cook baked a cake Lucy.

Was something baked for Lucy?

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Did the woman lose something?

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Did the tax law benefit from anything?

No

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Was something baked for Lucy?

No (Yes?)

Simple question-answering

The woman lost the diamond.

Did the woman lose something?

Yes

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Did the girl kick something?

No

The businessman benefited from the tax law.

Did the tax law benefit from anything?

No

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Was something baked for Lucy?

No

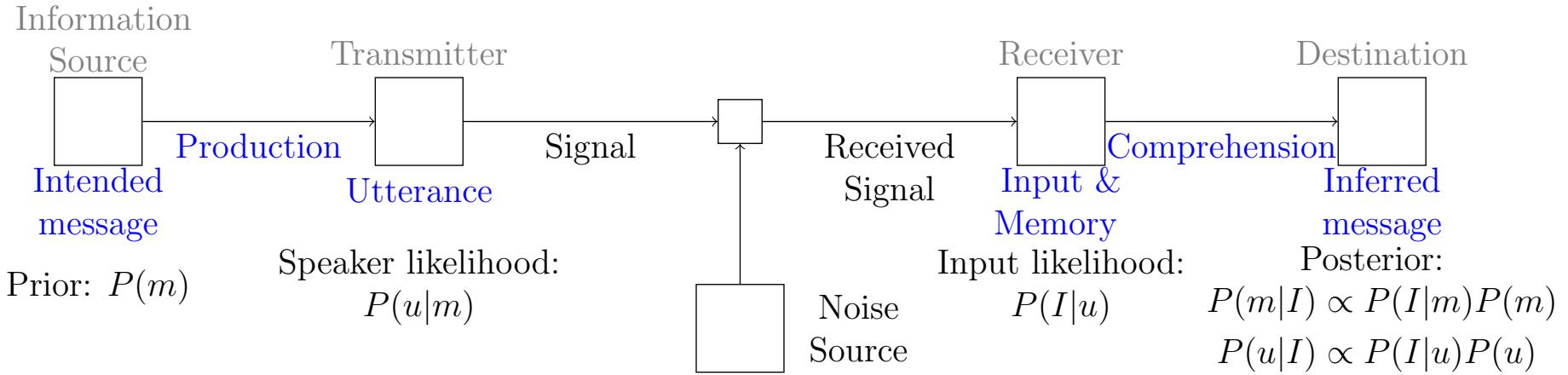
(Yes?)

Over 2/3 of answers!

Noisy-channel semantic interpretation?

The cook baked a cake Lucy.

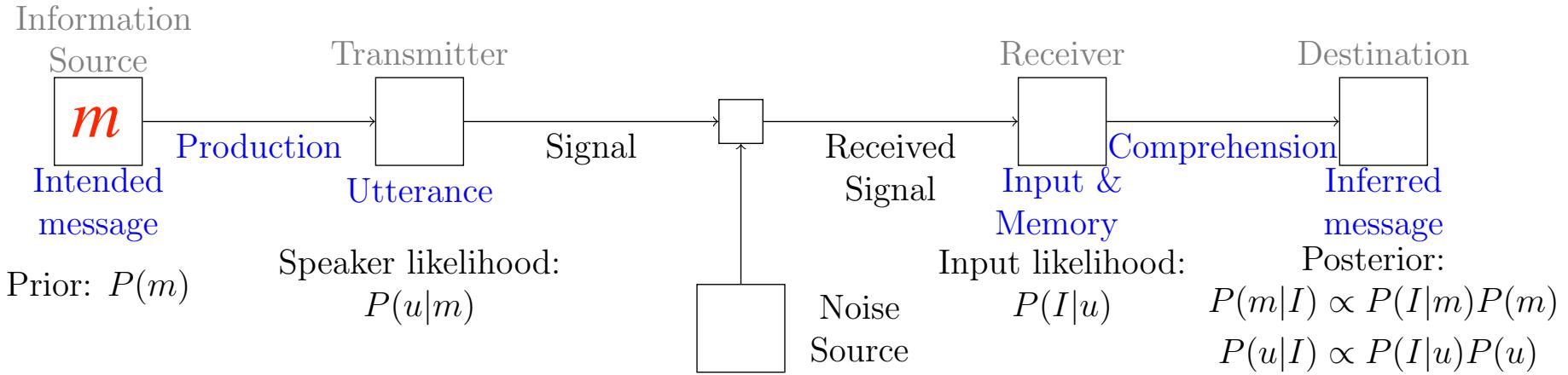
Was something baked for Lucy?



Noisy-channel semantic interpretation?

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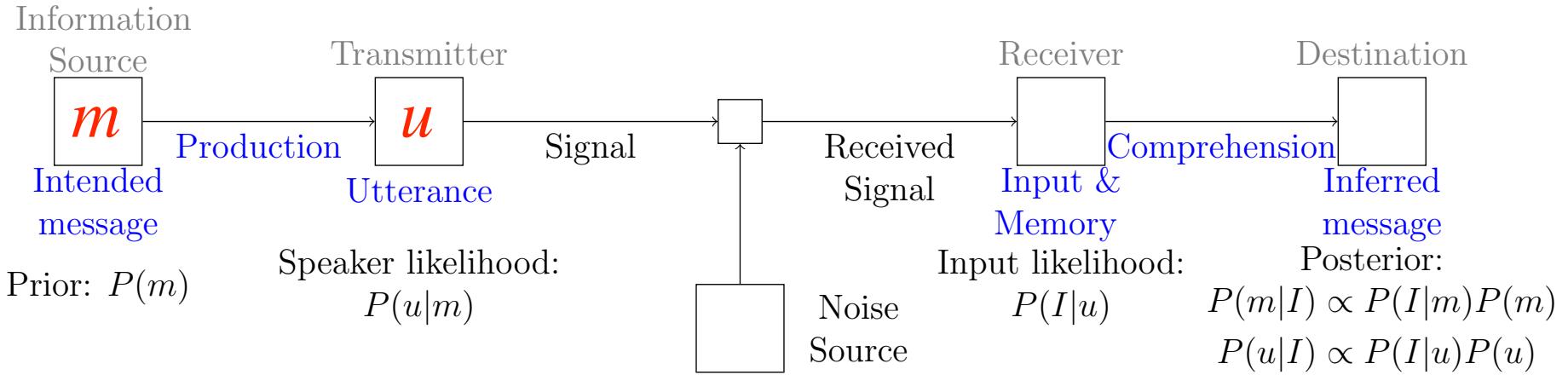
Was something baked for Lucy?



Noisy-channel semantic interpretation?

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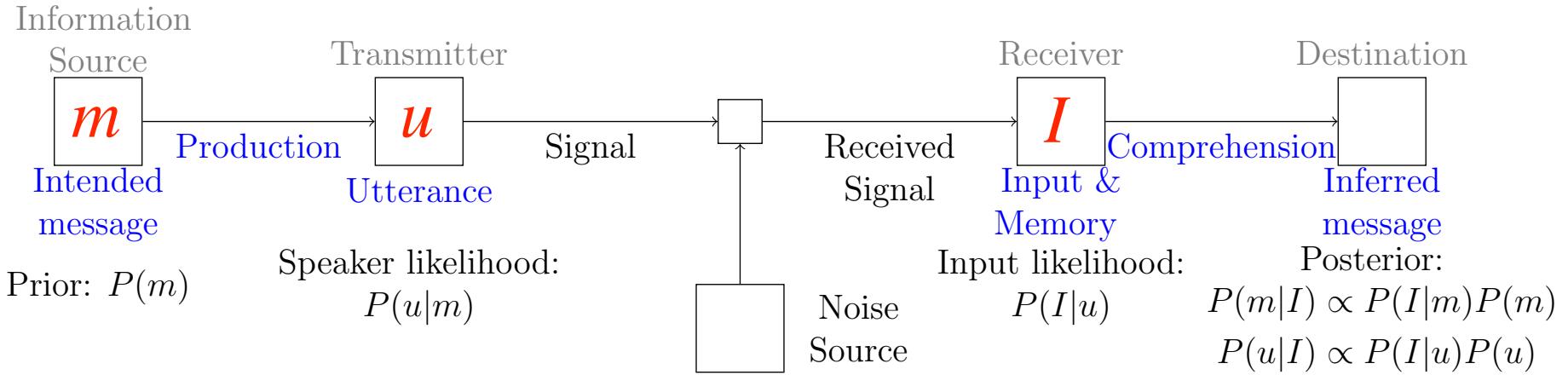
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Noisy-channel semantic interpretation?

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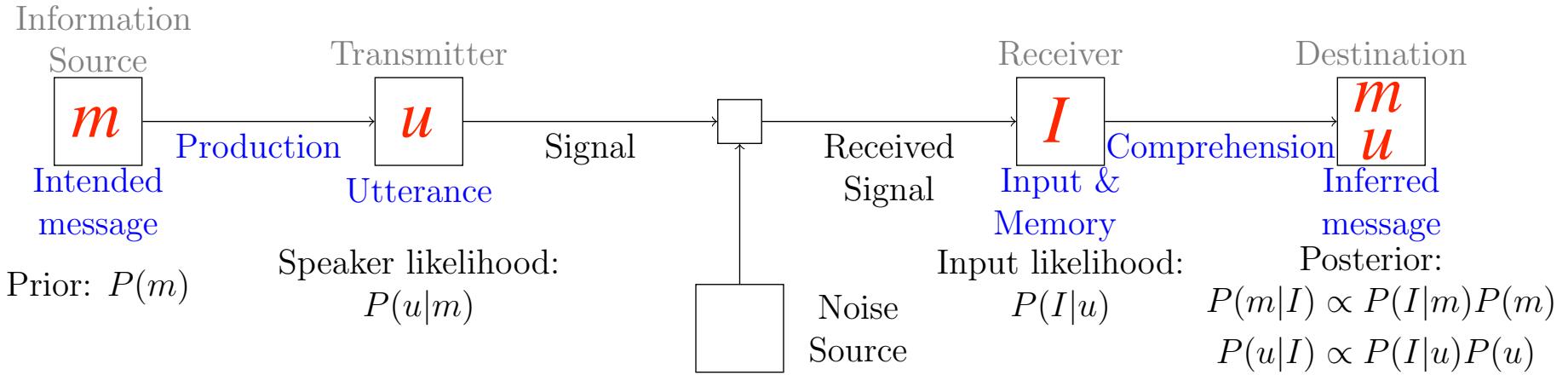
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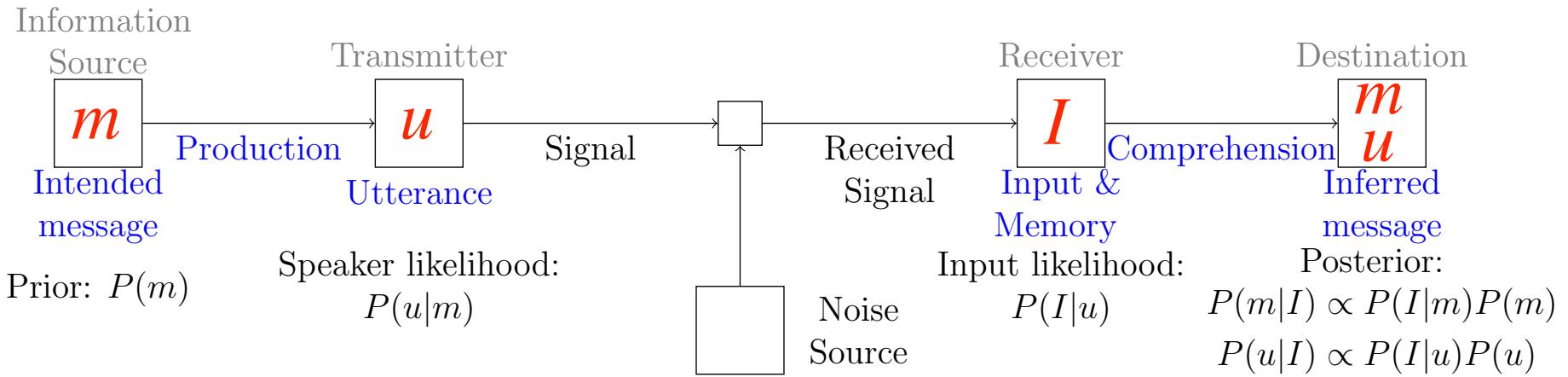
Was something baked for Lucy?



Noisy-channel semantic interpretation?

I ← The cook baked a cake Lucy.

Was something baked for Lucy?

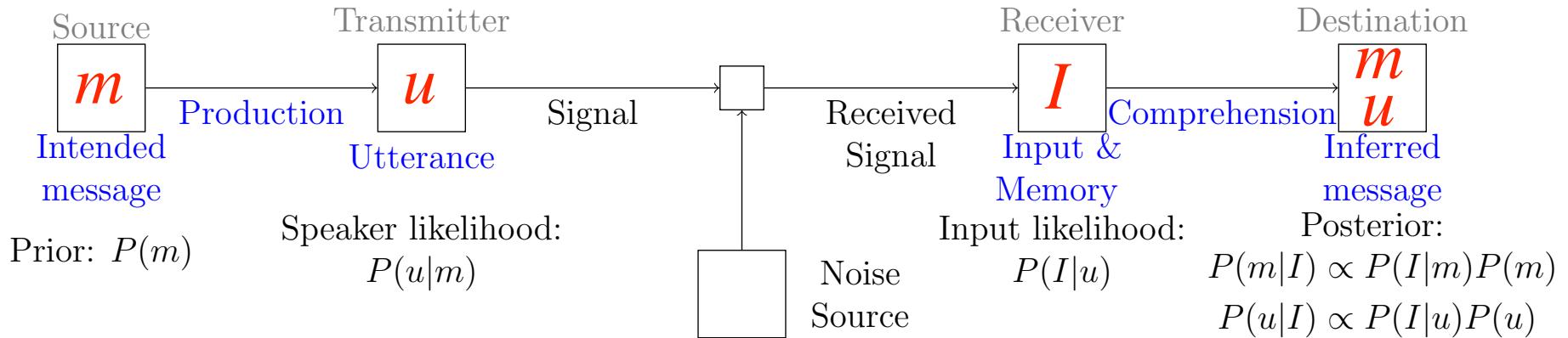


Noisy-channel semantic interpretation?

I ← The cook baked a cake Lucy.

m? Was something baked for Lucy?

Information

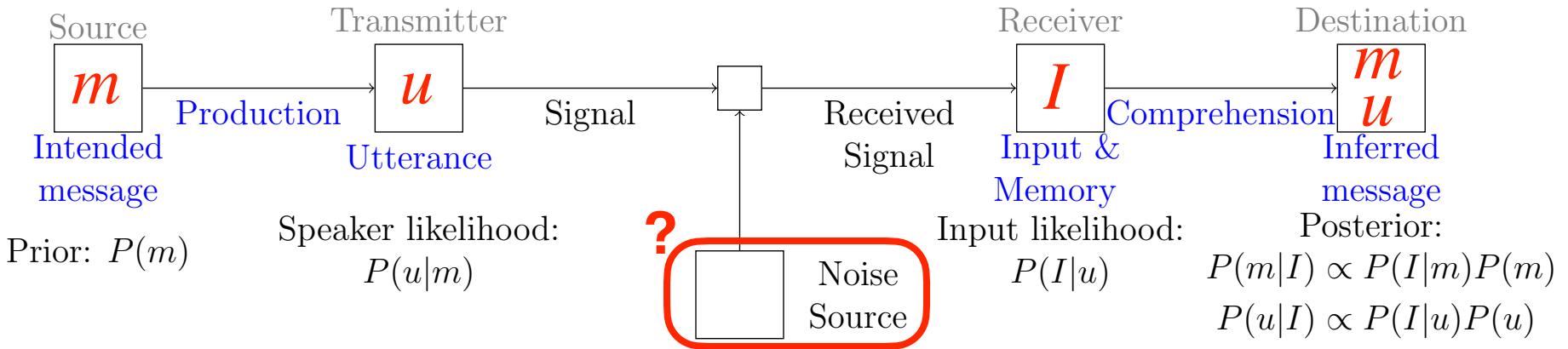


Noisy-channel semantic interpretation?

I←The cook baked a cake Lucy.

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Information

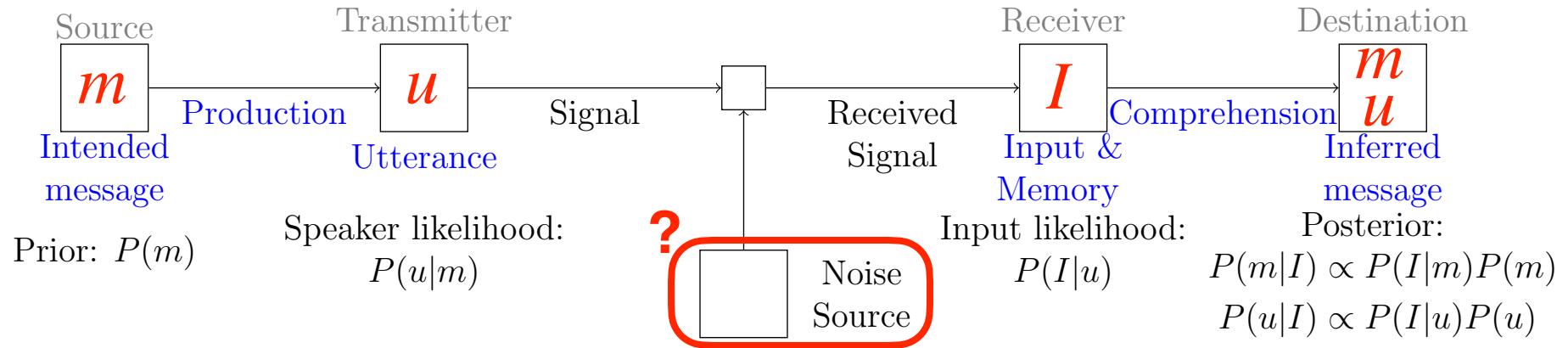


Noisy-channel semantic interpretation?

I←The cook baked a cake Lucy.

m? Was something baked for Lucy?

Information



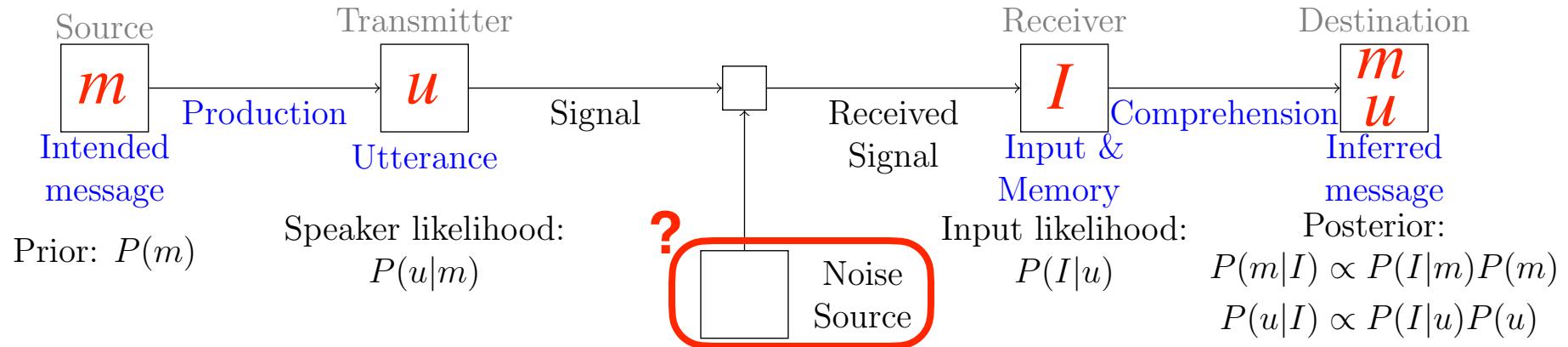
In two semantically plausible "neighbor" sentences, the answer is "yes":

Noisy-channel semantic interpretation?

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m? Was something baked for Lucy?

Information



In two semantically plausible "neighbor" sentences, the answer is "yes":

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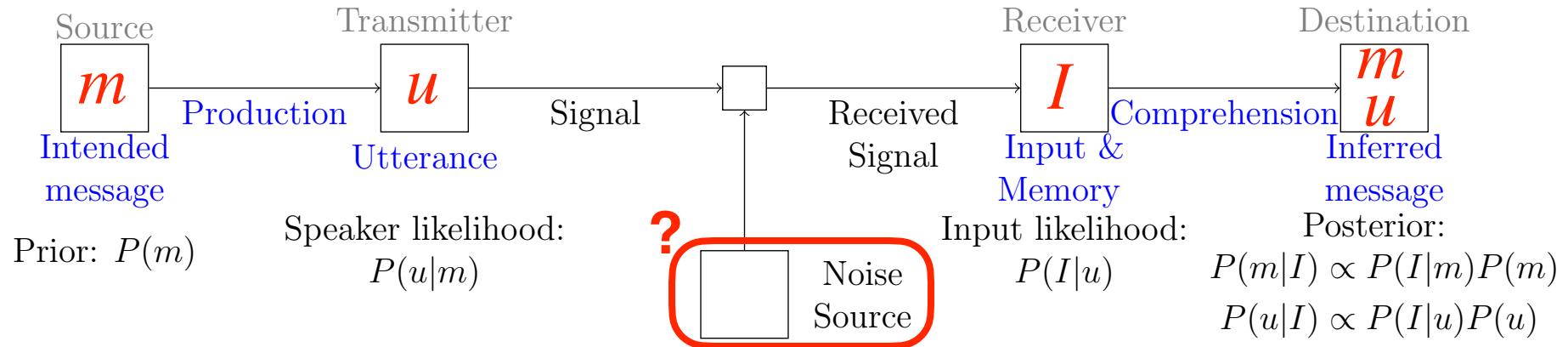
for

Noisy-channel semantic interpretation?

I ← The cook baked a cake Lucy.

m? Was something baked for Lucy?

Information



In two semantically plausible "neighbor" sentences, the answer is "yes":

The cook baked a cake Lucy.

Hypothesized noise operation: deletion

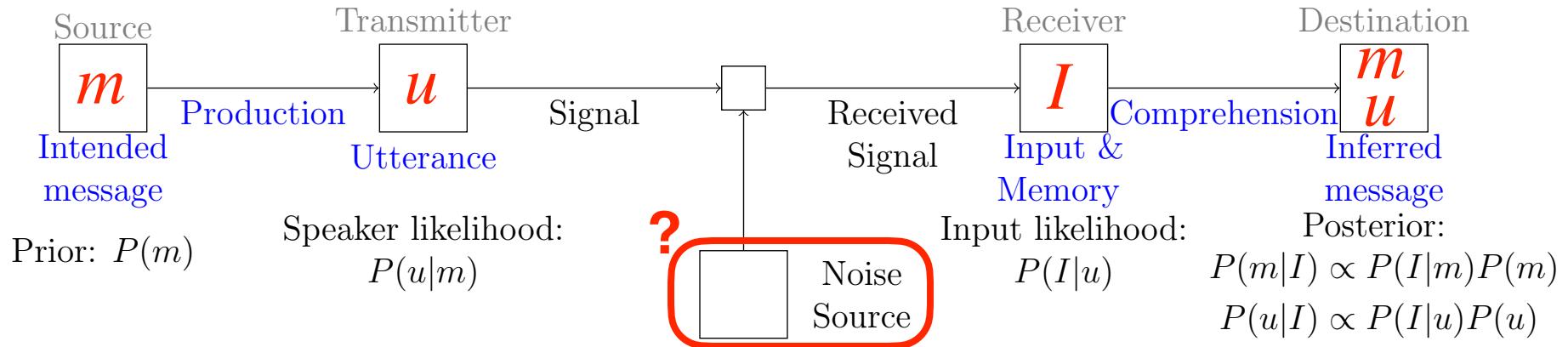
for

Noisy-channel semantic interpretation?

I←The cook baked a cake Lucy.

m? Was something baked for Lucy?

Information



In two semantically plausible "neighbor" sentences, the answer is "yes":

The cook baked a cake Lucy.

Hypothesized noise operation: deletion

for

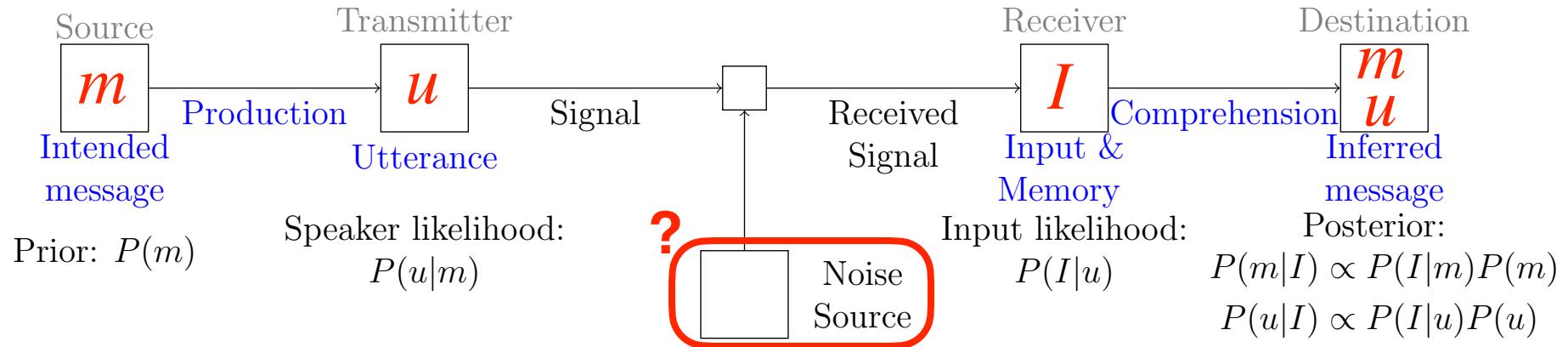
The cook baked a cake Lucy.
Lucy a cake

Noisy-channel semantic interpretation?

I←The cook baked a cake Lucy.

m? Was something baked for Lucy?

Information



In two semantically plausible "neighbor" sentences, the answer is "yes":

The cook baked a cake Lucy.

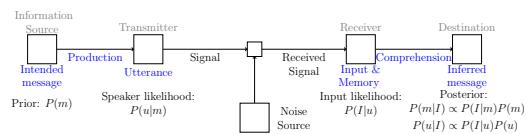
Hypothesized noise operation: deletion

for

The cook baked a cake Lucy.

Hypothesized noise operation: exchange Lucy a cake

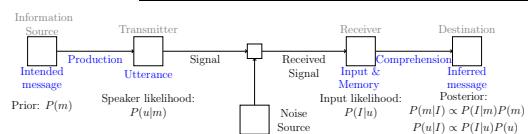
Predictions for implausible sentences



$$P(m | I) \propto P(I | m)P(m)$$

Noise operation Plausibility

Predictions for implausible sentences



$$P(m | I) \propto P(I | m)P(m)$$

Noise operation Plausibility

Non-literal interpretation?

Double Object/Benefactive-for alternation

*Deletion/
insertion Exchange*

The cook baked a cake Lucy.

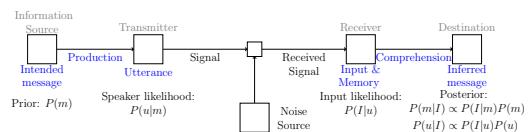
Yes Yes

The cook baked Lucy for a cake.

Yes Yes

Implausible

Predictions for implausible sentences



$$P(m | I) \propto P(I | m)P(m)$$

Noise operation Plausibility

Non-literal interpretation?

Double Object/Benefactive-for alternation

*Deletion/
insertion Exchange*

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Yes Yes

The cook baked Lucy for a cake.

Yes Yes

The cook baked Lucy a cake.

No No

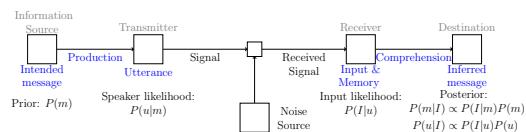
The cook baked a cake for Lucy.

No No

Implausible

Plausible

Predictions for implausible sentences



$$P(m | I) \propto P(I | m)P(m)$$

Noise operation Plausibility

Non-literal interpretation?

Implausible

Double Object/Benefactive-for alternation

The cook baked a cake Lucy.

Yes Yes

The cook baked Lucy for a cake.

Yes Yes

Plausible

The cook baked Lucy a cake.

No No

The cook baked a cake for Lucy.

No No

*Deletion/
insertion Exchange*

Implausible

Active/Passive alternation

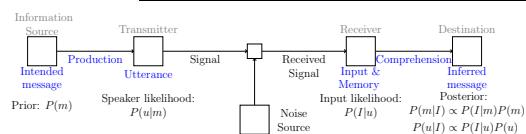
The ball kicked the girl.

No Yes

The girl was kicked by the ball.

No Yes

Predictions for implausible sentences



$$P(m | I) \propto P(I | m)P(m)$$

Noise operation Plausibility

Non-literal interpretation?

Implausible

Double Object/Benefactive-for alternation

The cook baked a cake Lucy.

Yes Yes

The cook baked Lucy for a cake.

Yes Yes

Plausible

The cook baked Lucy a cake.

No No

The cook baked a cake for Lucy.

No No

*Deletion/
insertion Exchange*

Implausible

Active/Passive alternation

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No Yes

The girl was kicked by the ball.

No Yes

Plausible

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No Yes

The ball was kicked by the girl.

No Yes

Literal vs. non-literal interpretation rates

Non-literal interpretations for implausible sentences?

Insertion/Deletion

Yes

Exchange

Yes

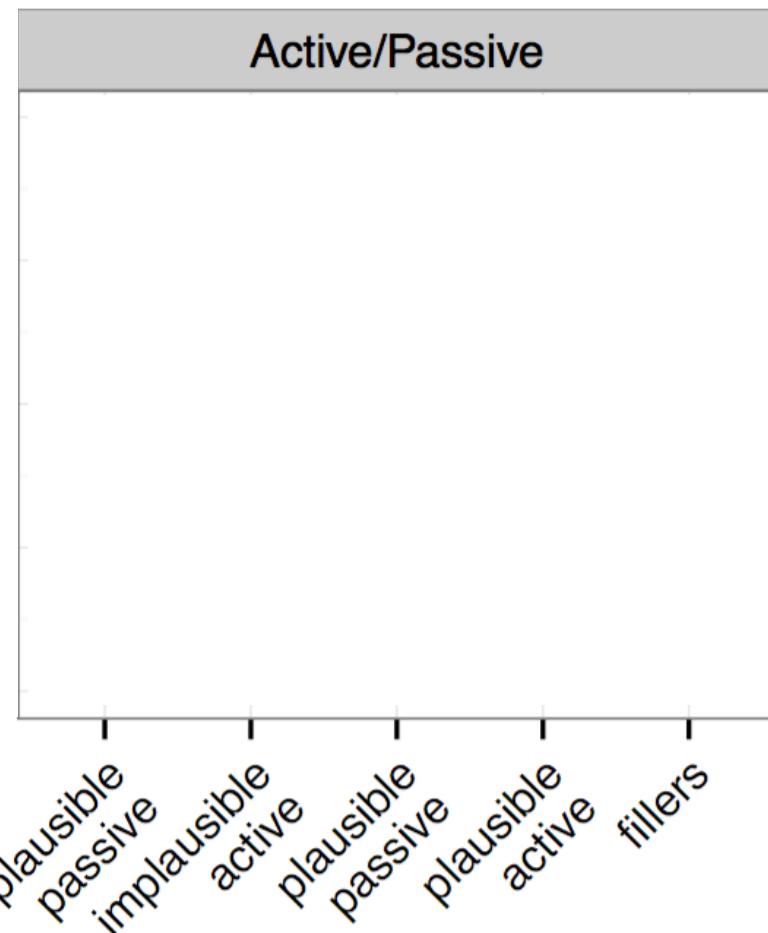
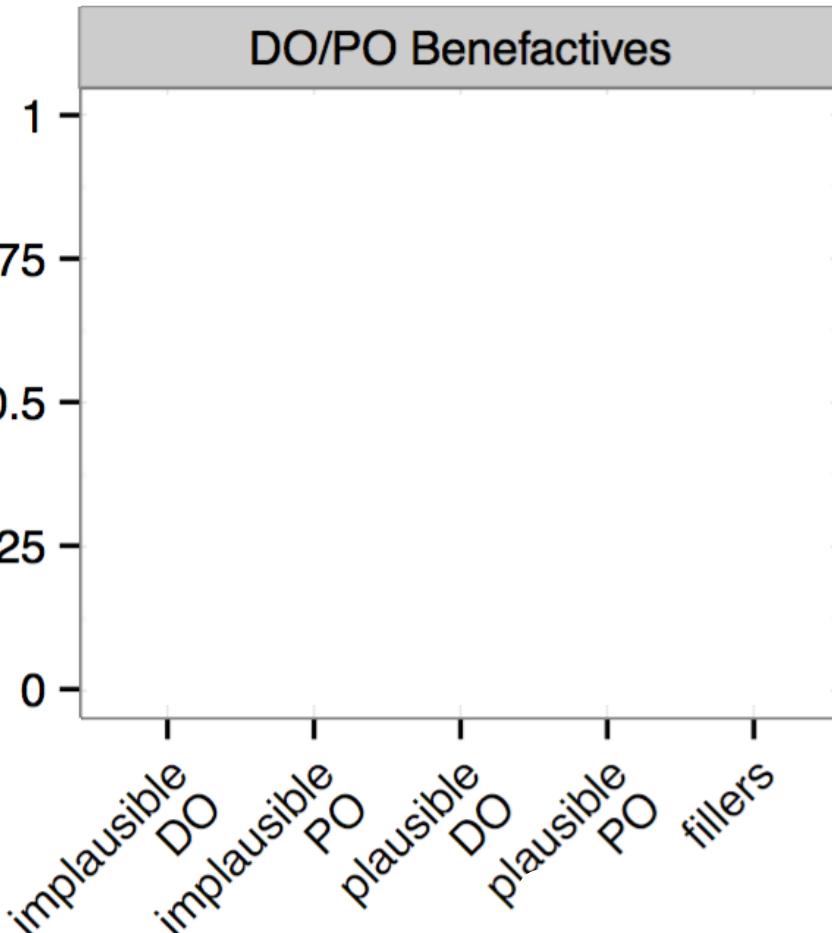
Insertion/Deletion

No

Exchange

Yes

Proportion of literal responses



Literal vs. non-literal interpretation rates

Non-literal interpretations for implausible sentences?

Insertion/Deletion

Yes

Exchange

Yes

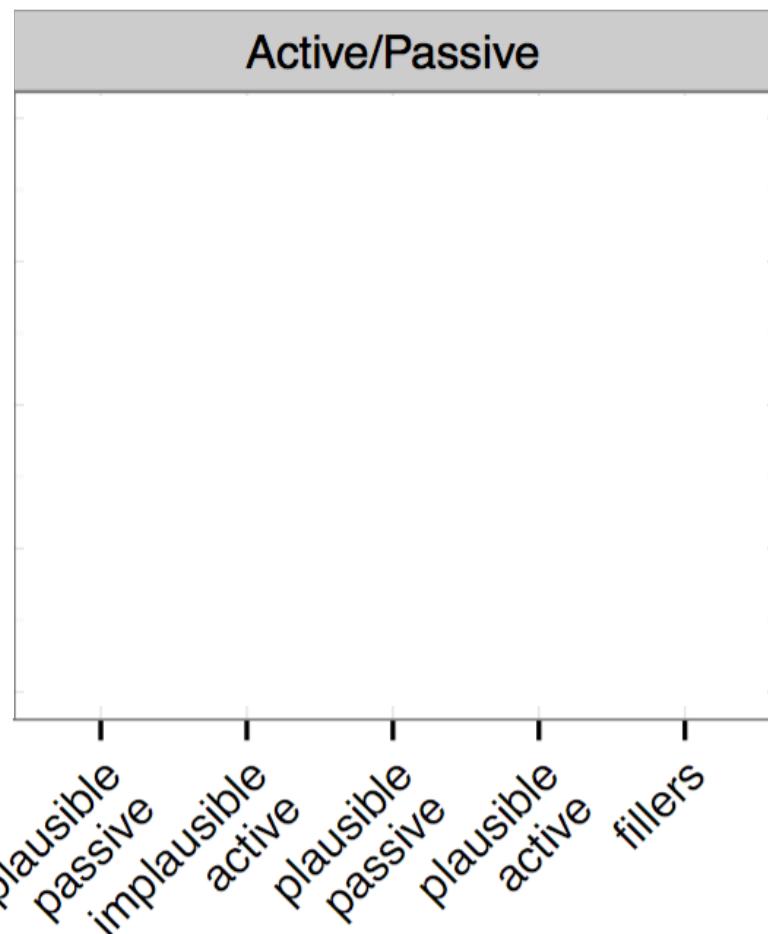
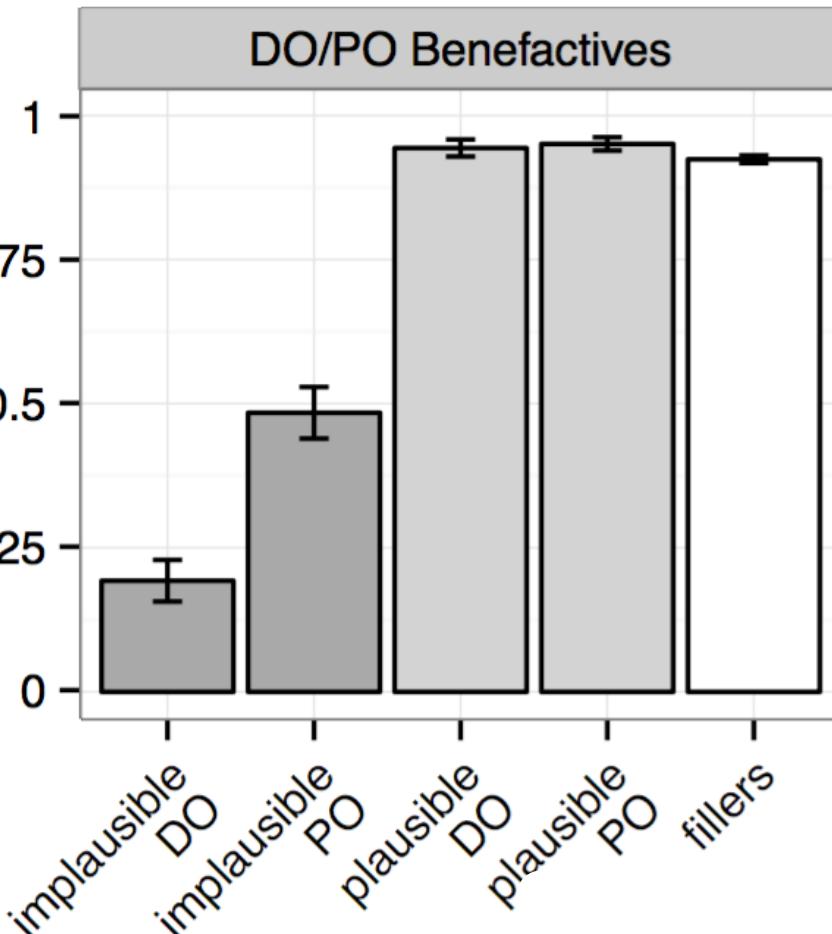
Insertion/Deletion

No

Exchange

Yes

Proportion of literal responses



Literal vs. non-literal interpretation rates

Non-literal interpretations for implausible sentences?

Insertion/Deletion

Yes

Exchange

Yes

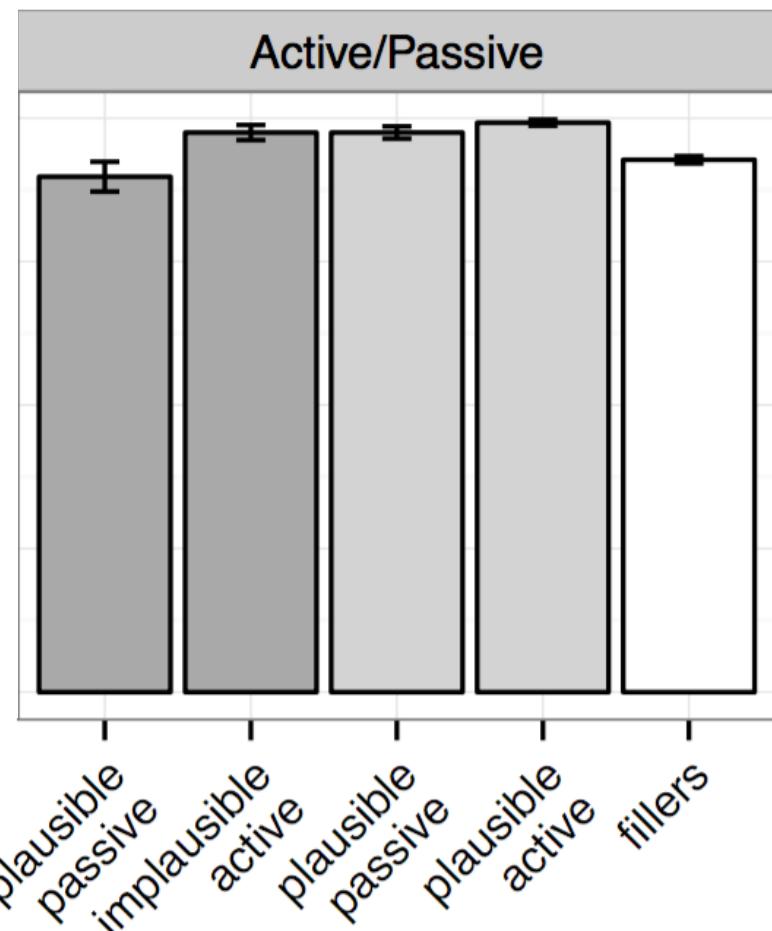
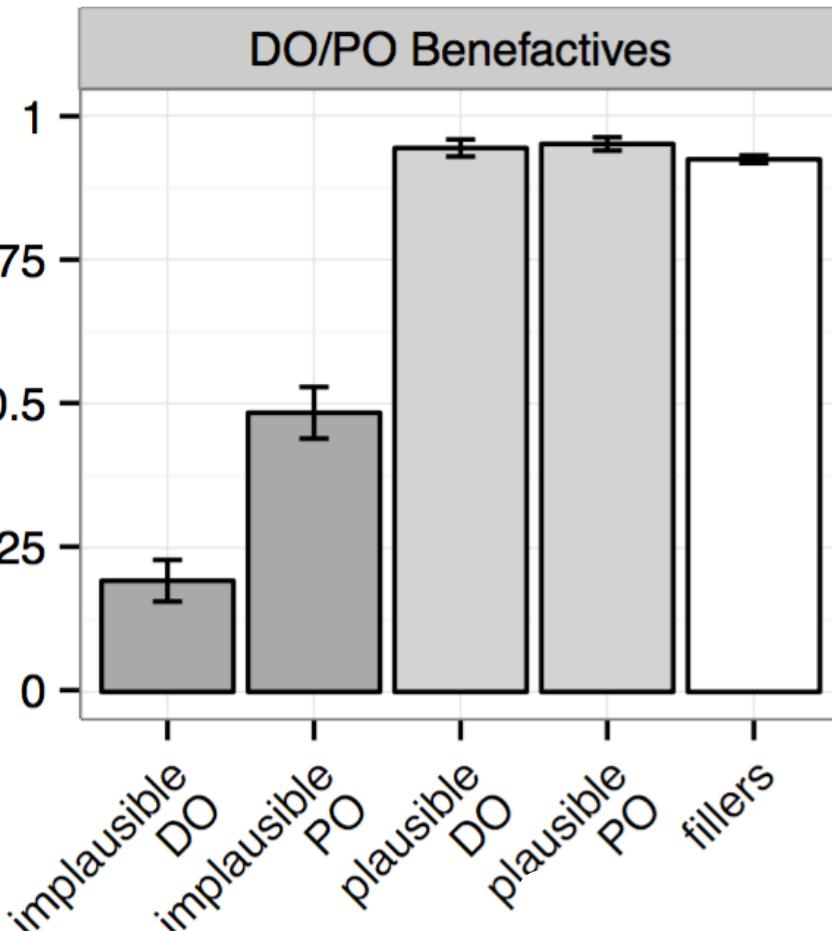
Insertion/Deletion

No

Exchange

Yes

Proportion of literal responses



Five alternations in an insertion/deletion model

English constructions	Change	Implausible version
1. Active/passive	Two insertions Two deletions	c. The girl <u>was</u> kicked <u>by</u> the ball. (passive) d. The ball kicked the girl. (active)
2. Subject-locative/ object-locative	One deletion, one insertion One insertion, one deletion	c. The table jumped <u>onto</u> a cat. (object-locative) d. <u>Onto</u> the cat jumped a table. (subject-locative)
3. Transitive/intransitive	One insertion One deletion	c. The tax law benefited <u>from</u> the businessman. (intransitive) d. The businessman benefited the tax law. (transitive)
4. DO/PO goal	One insertion One deletion	c. The mother gave the daughter <u>to</u> the candle. (PO-goal) d. The mother gave the candle the daughter. (DO-goal)
5. DO/PO benefactive	One insertion One deletion	c. The cook baked Lucy <u>for</u> a cake. (PO-benef) d. The cook baked a cake Lucy. (DO-benef)

c=inferred insertion d=inferred deletion

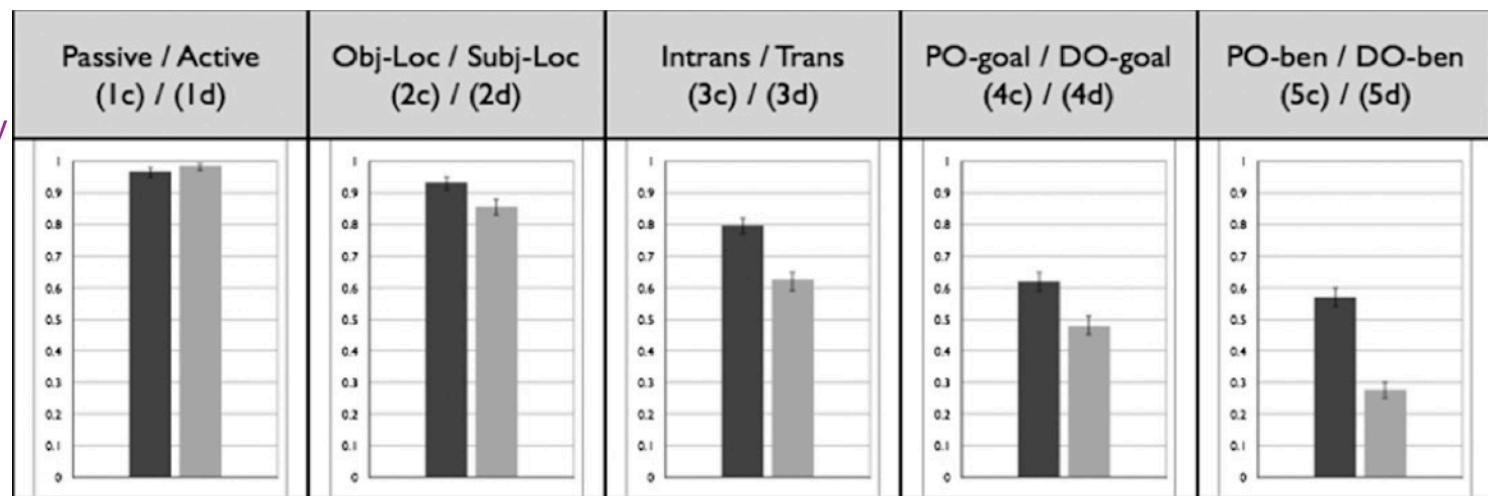
Five alternations in an insertion/deletion model

$$P(m|I) \propto P(I|m)P(m)$$

Noise operation Plausibility

Base experiment

20 experimental items,
60 plausible &
grammatically normal
fillers \rightarrow 10/80
implausible trials



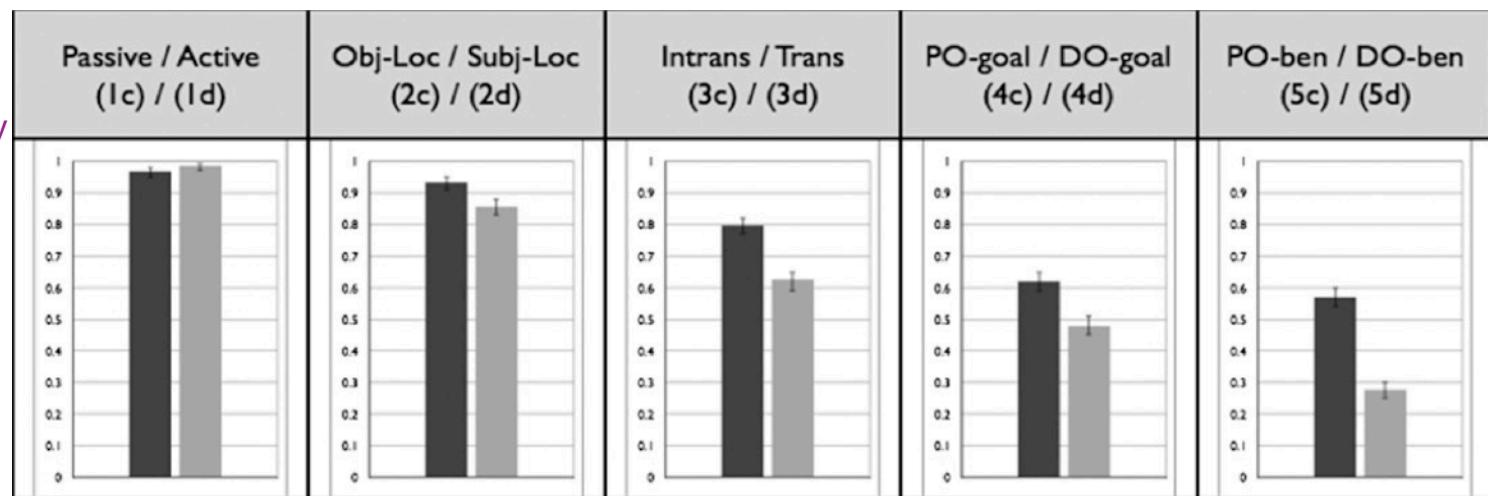
Five alternations in an insertion/deletion model

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Noise operation Plausibility

Base experiment

20 experimental items,
60 plausible &
grammatically normal
fillers → 10/80
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Fillers with syntactic errors

"A legislator lied to the
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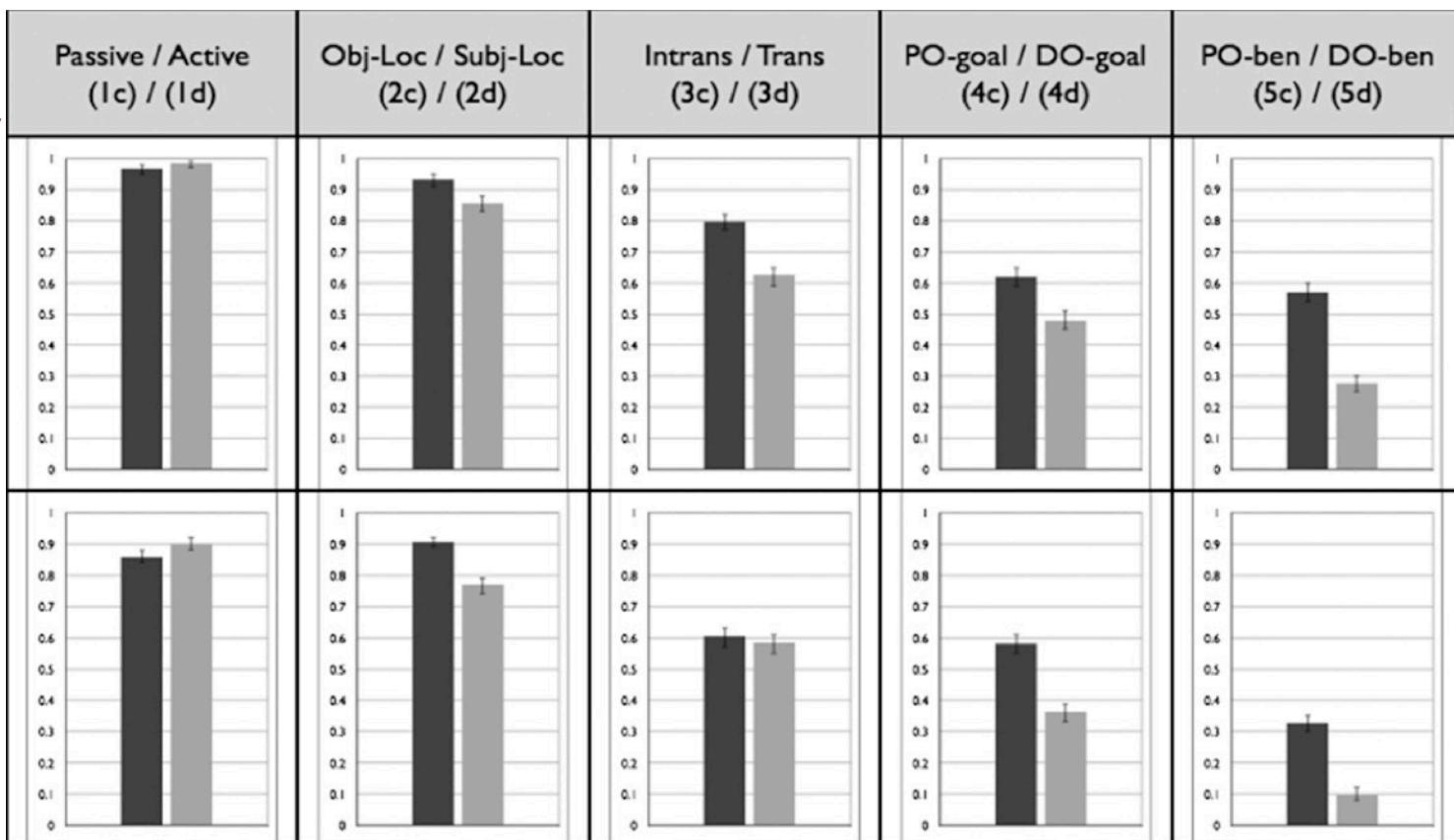
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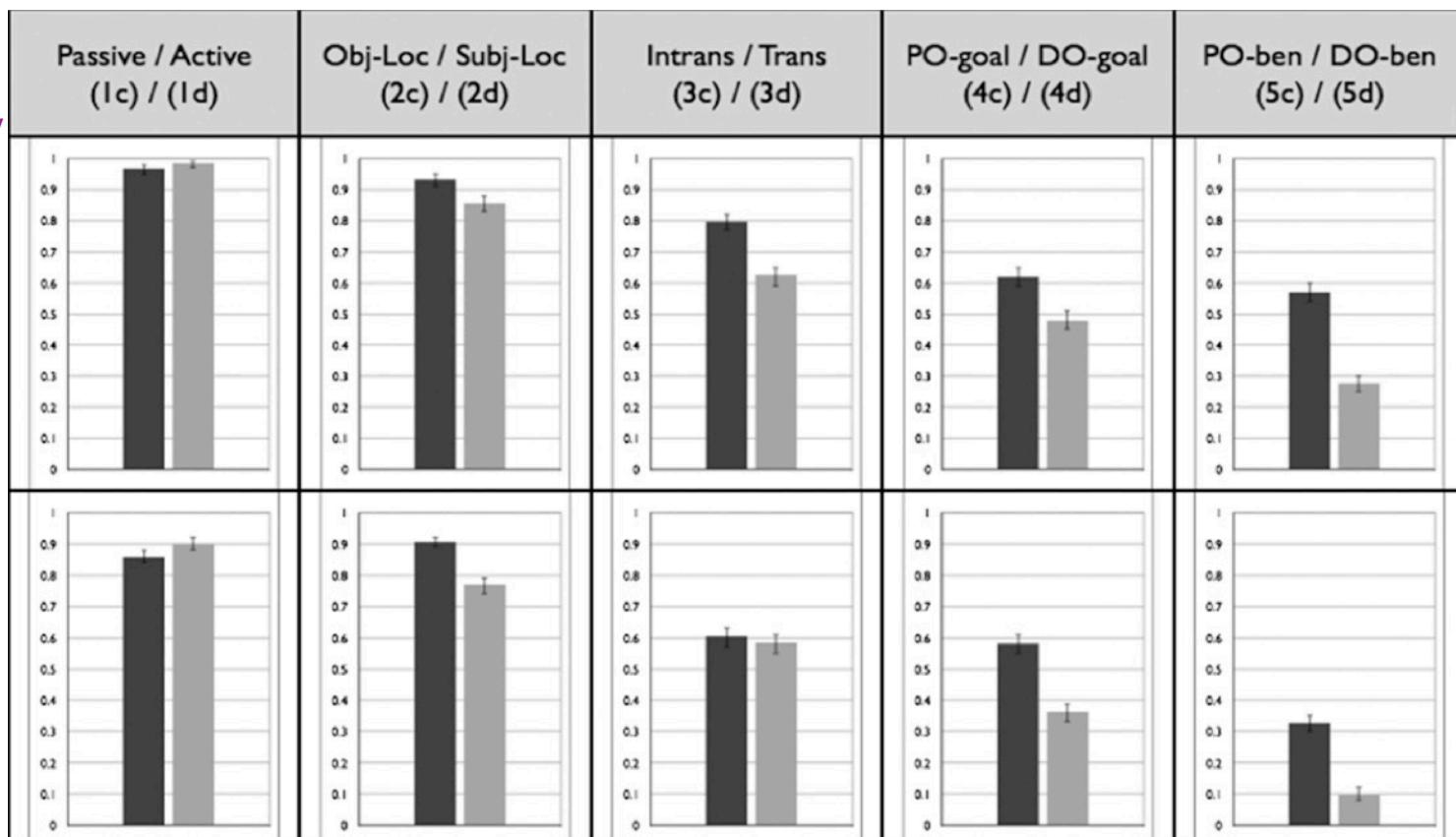
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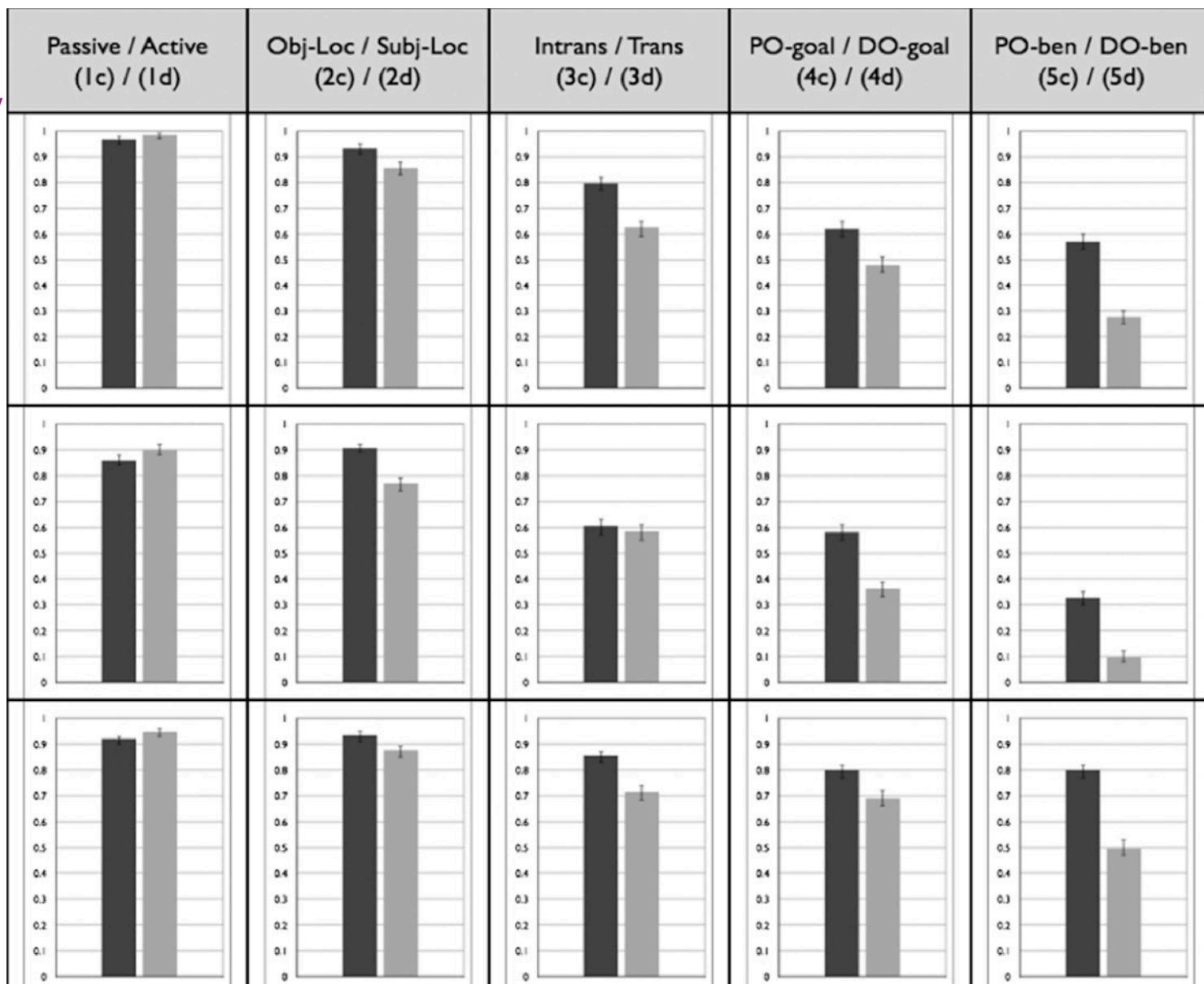
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Inferring deletions versus insertions

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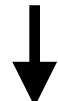
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The cook baked a cake Lucy.

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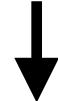


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Insert

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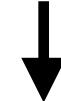


Insert



Choose insertion location

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Noisy-channel prediction: inferring deletions should be intrinsically easier than inferring insertions!

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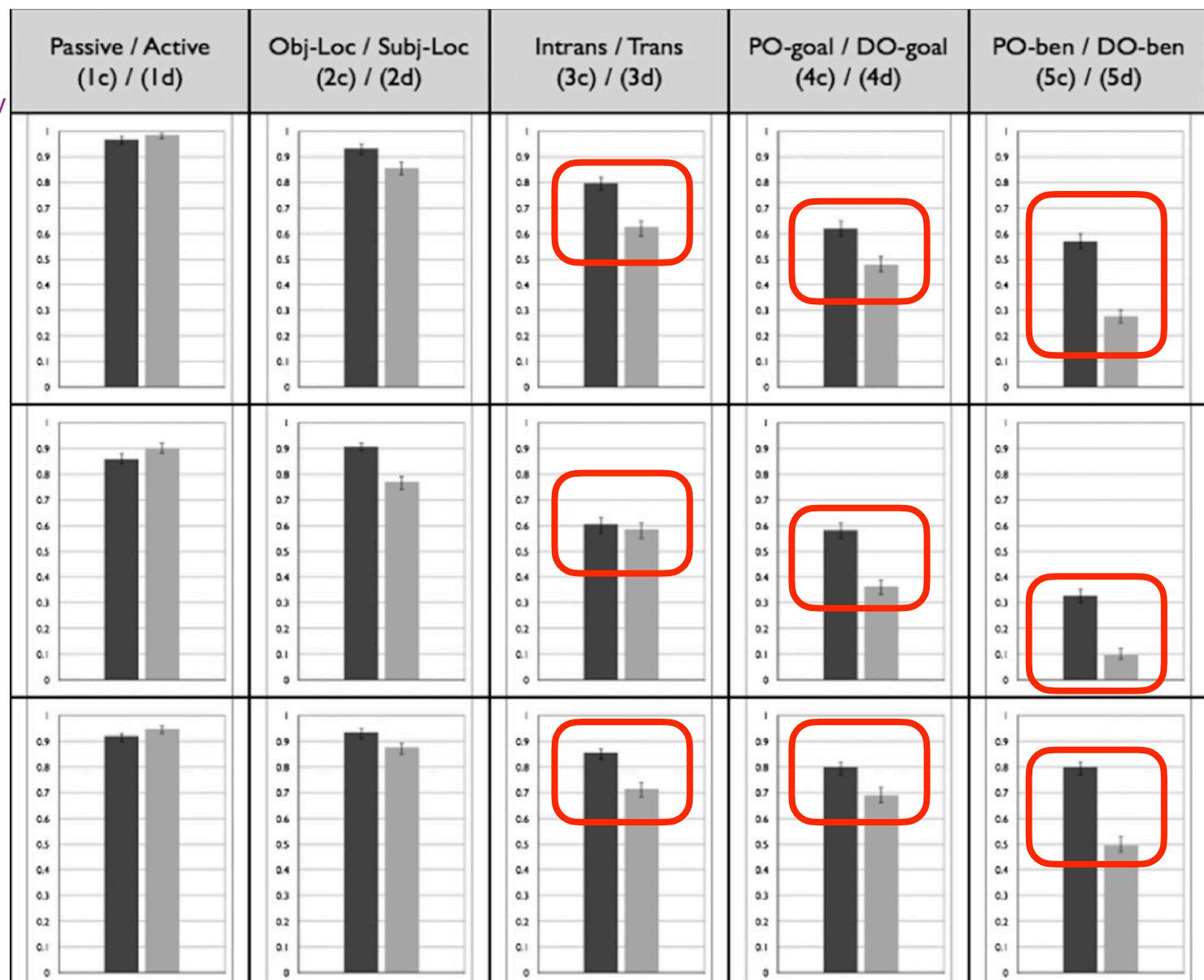
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In the real world (2008)



I'm not going to solely
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on changes in climate.

Sarah Palin (images credit Gage Skidmore)



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Sarah Palin (images credit Gage Skidmore)

CC BY-SA



I'm not one to attribute every activity
of man to climate change.

Corpora of speech errors

Anticipations

John dropped his cuff of coffee

reek long race

Perseverations

John gave the goy (=gave the boy)

Spanish speaping people

teep a cape (=keep a tape)

Exchanges

the nipper is zarrow

Fancy getting your model renosed (=nose remodeled)

Revisiting the possibility of exchanges

This is a problem that I need to talk about Joe with.

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The package fell from the table to the floor. [plausible; canonical]

The package fell to the floor from the table. [plausible; non-canonical]

The package fell from the floor to the table. [implausible; canonical]

The package fell to the table from the floor. [implausible; non-canonical]

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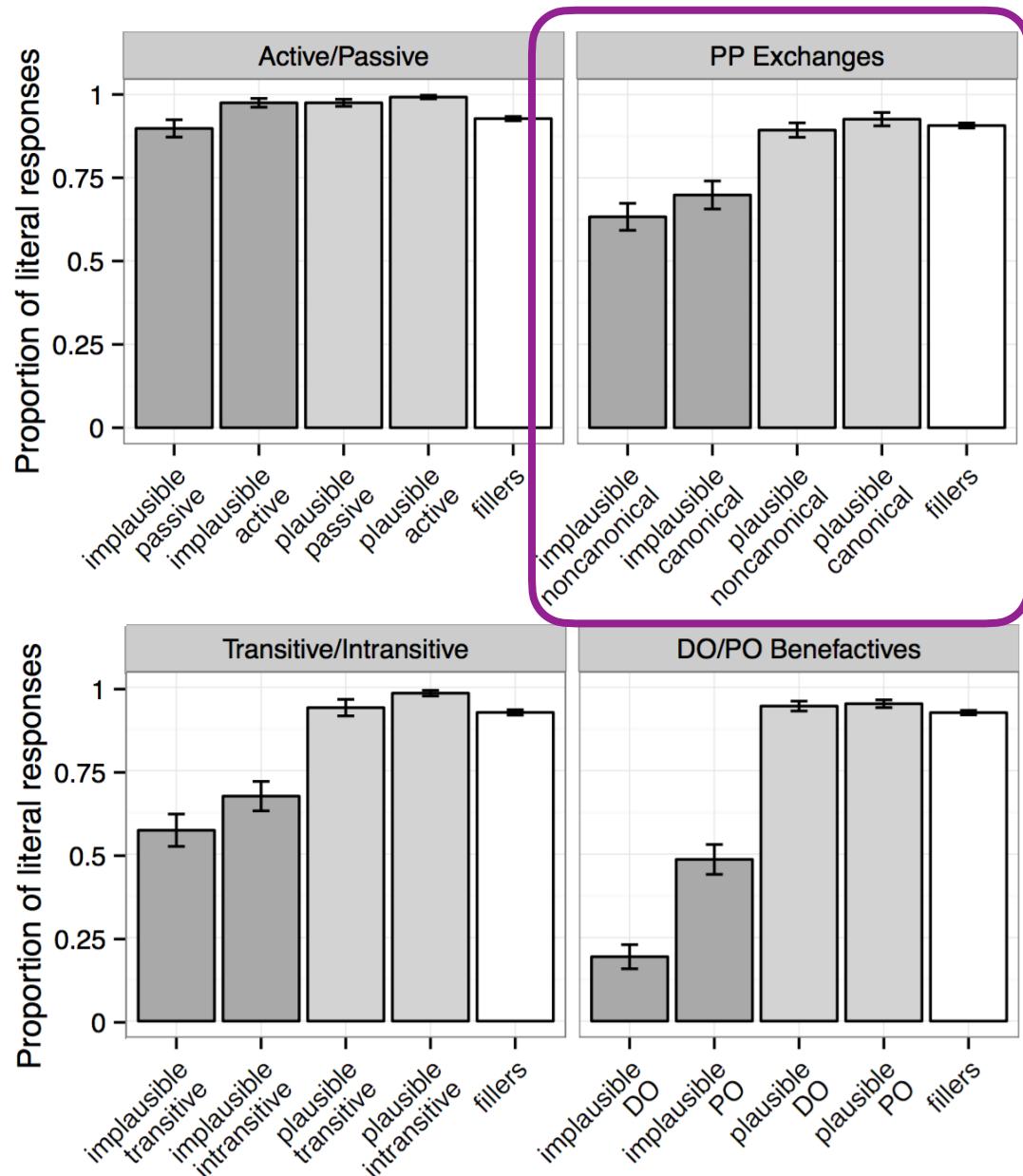
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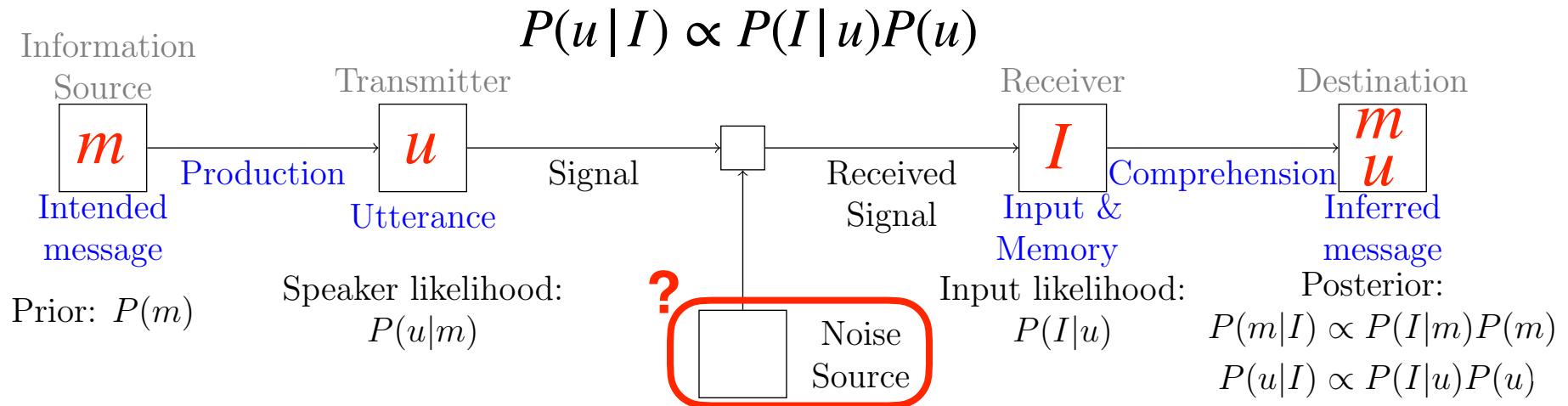
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Did something fall to the floor?

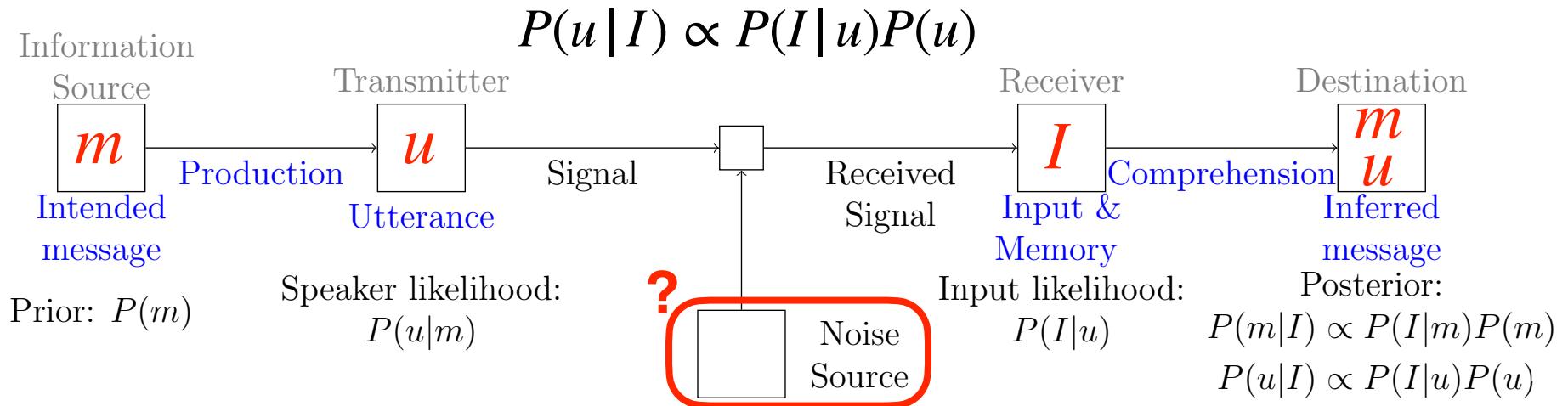
Exchanges in the noise model



Probing inferred intended utterances

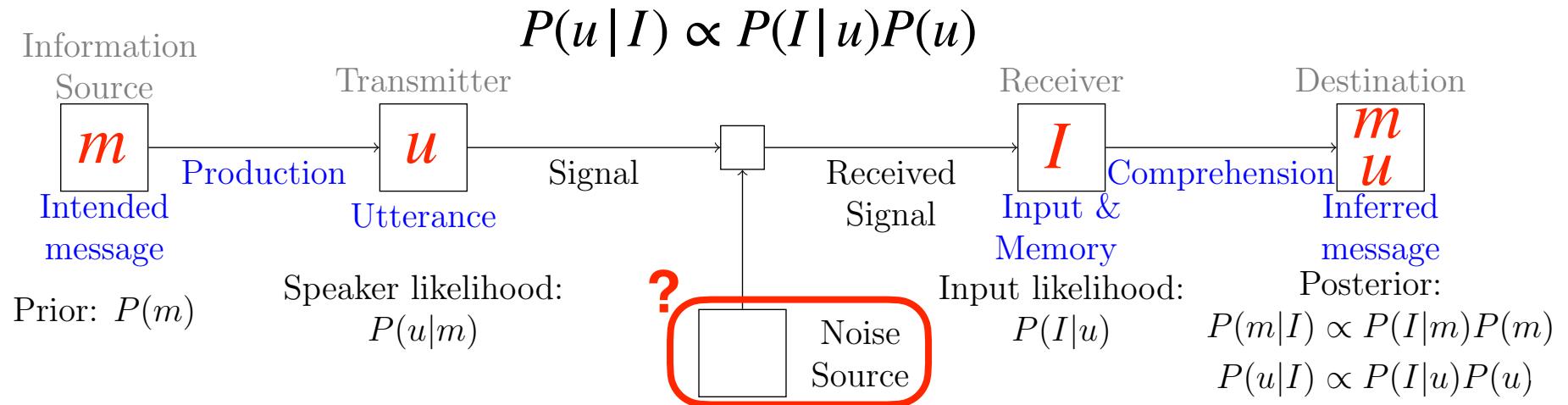


Probing inferred intended utterances



Experiment "cover story": read transcriptions of speech that might have errors, retype with edits if they think the speaker might have meant something else

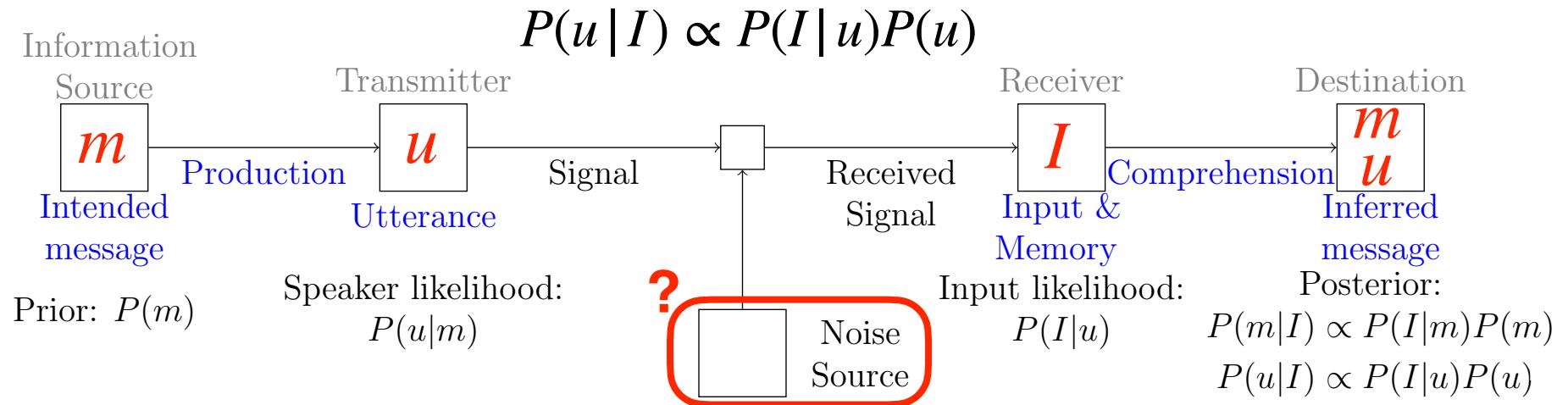
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Probing inferred intended utterances



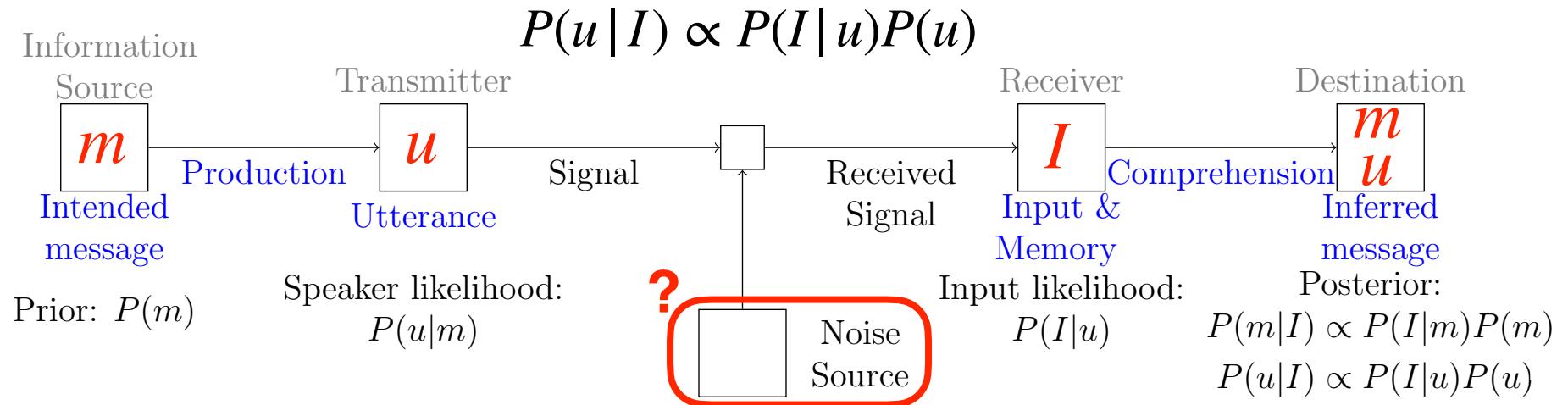
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No error

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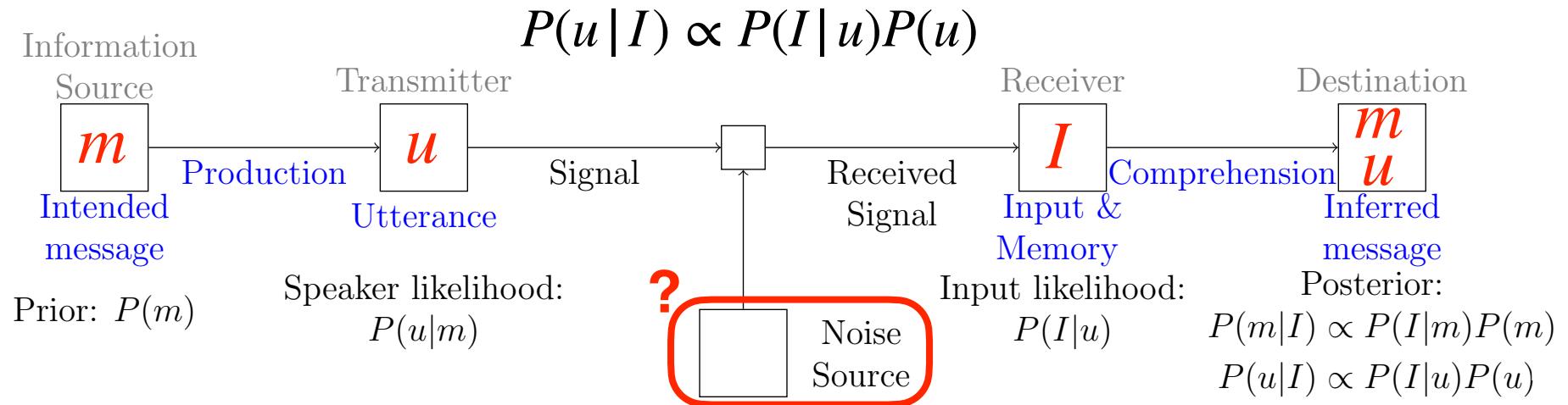
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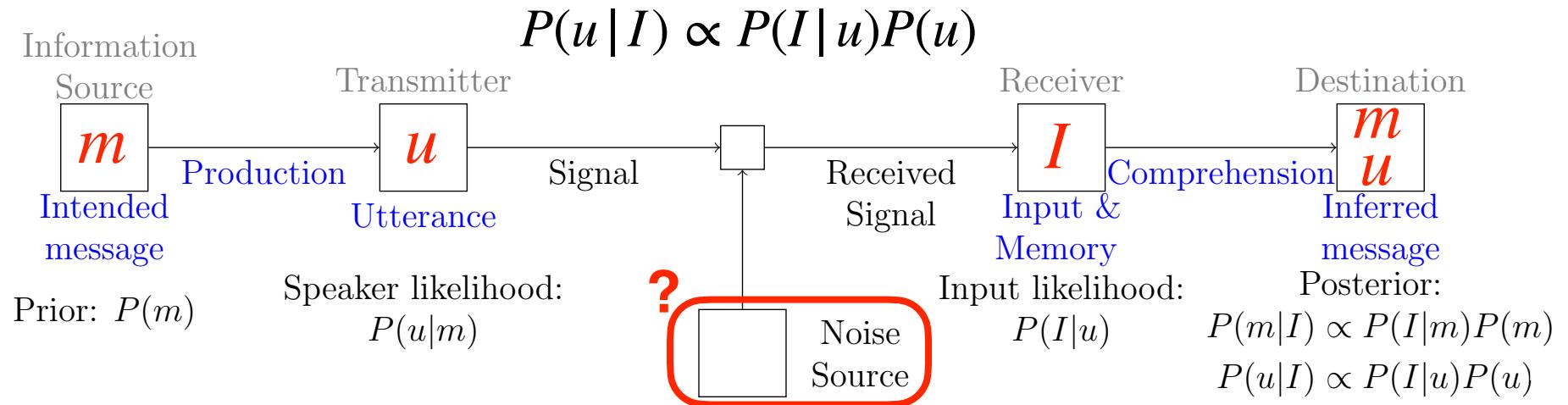
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The ball kicked the girl. The judge gave the athlete to the prize.

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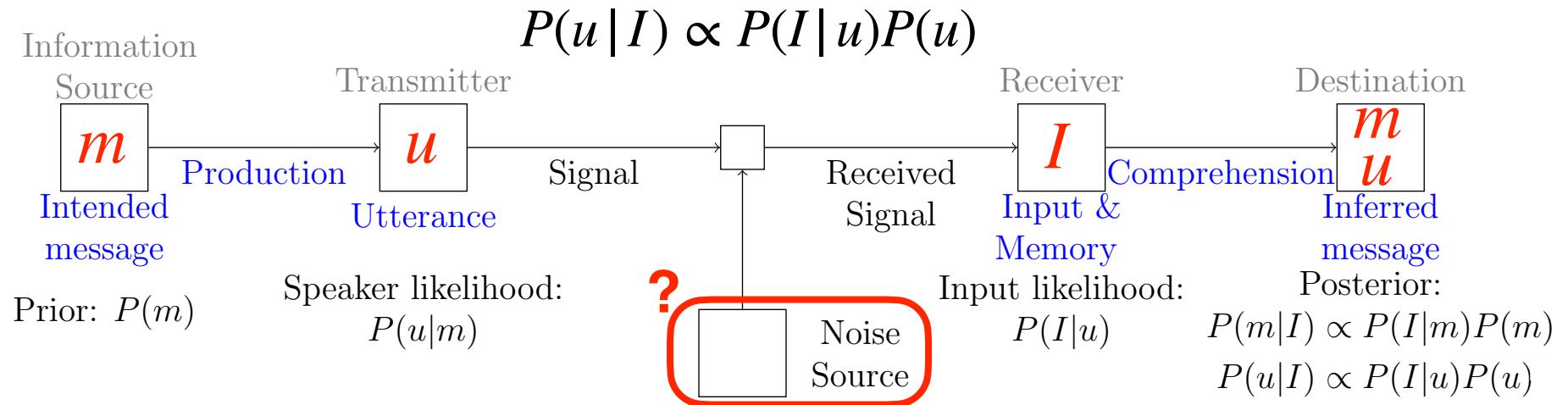
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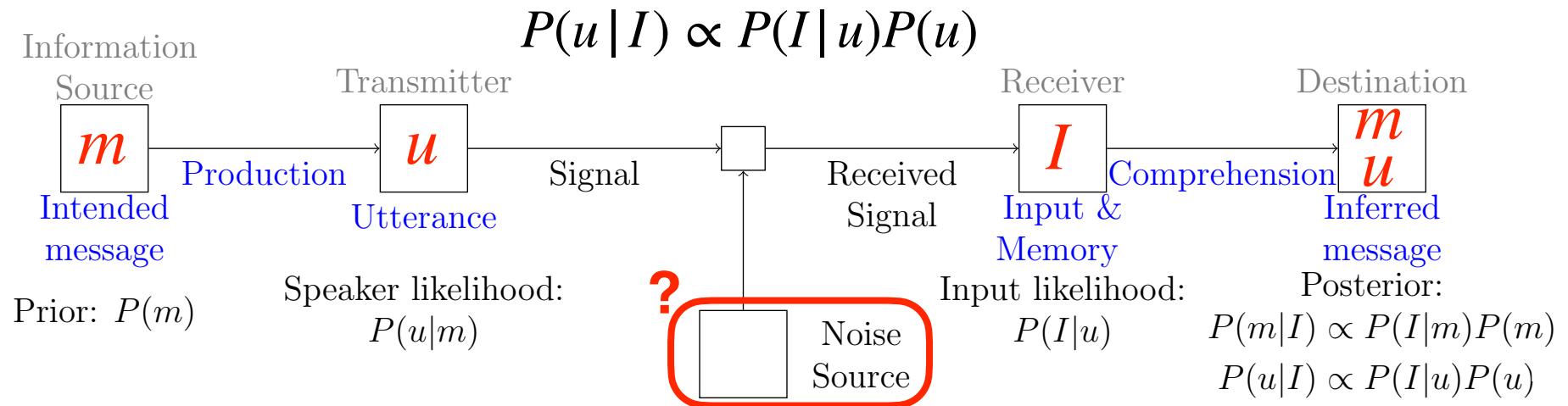
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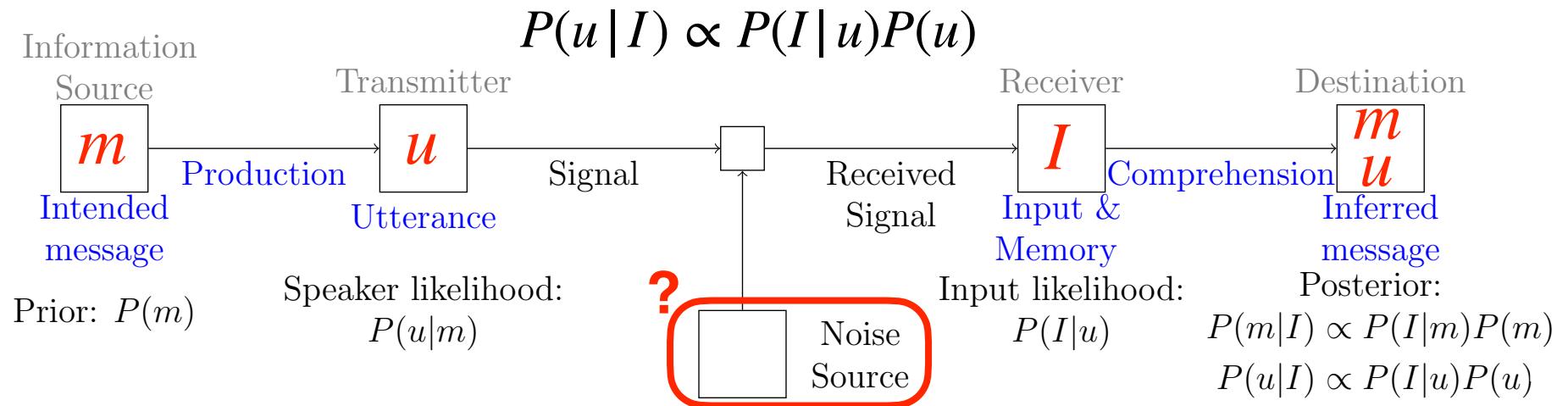
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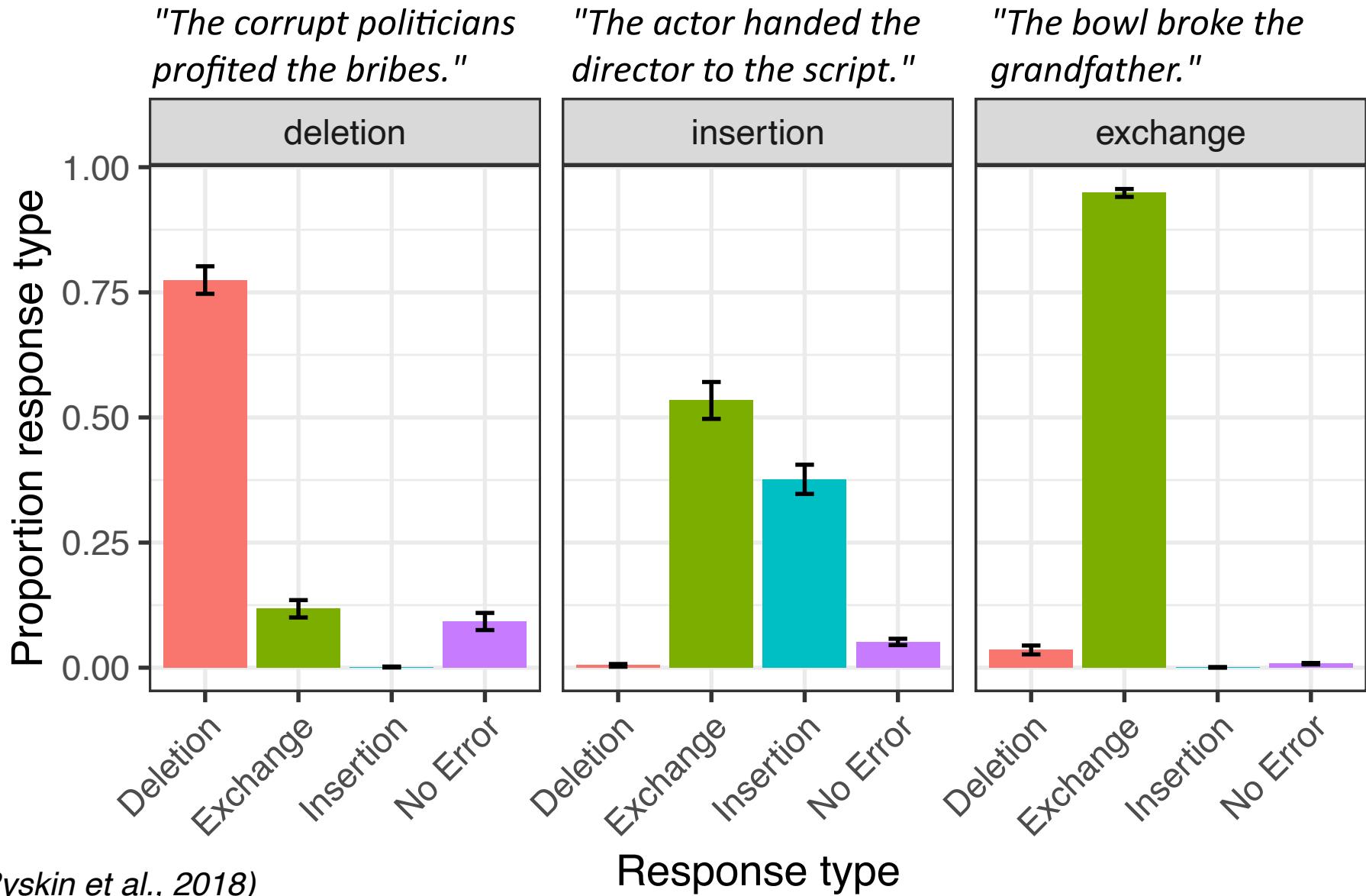
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- *However*, status of exchange errors in the noise model remains a mystery

Structural Forgetting and the Noisy Channel

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1. The apartment that the maid who the cleaning service sent over was well-decorated.

Structural Forgetting and the Noisy Channel

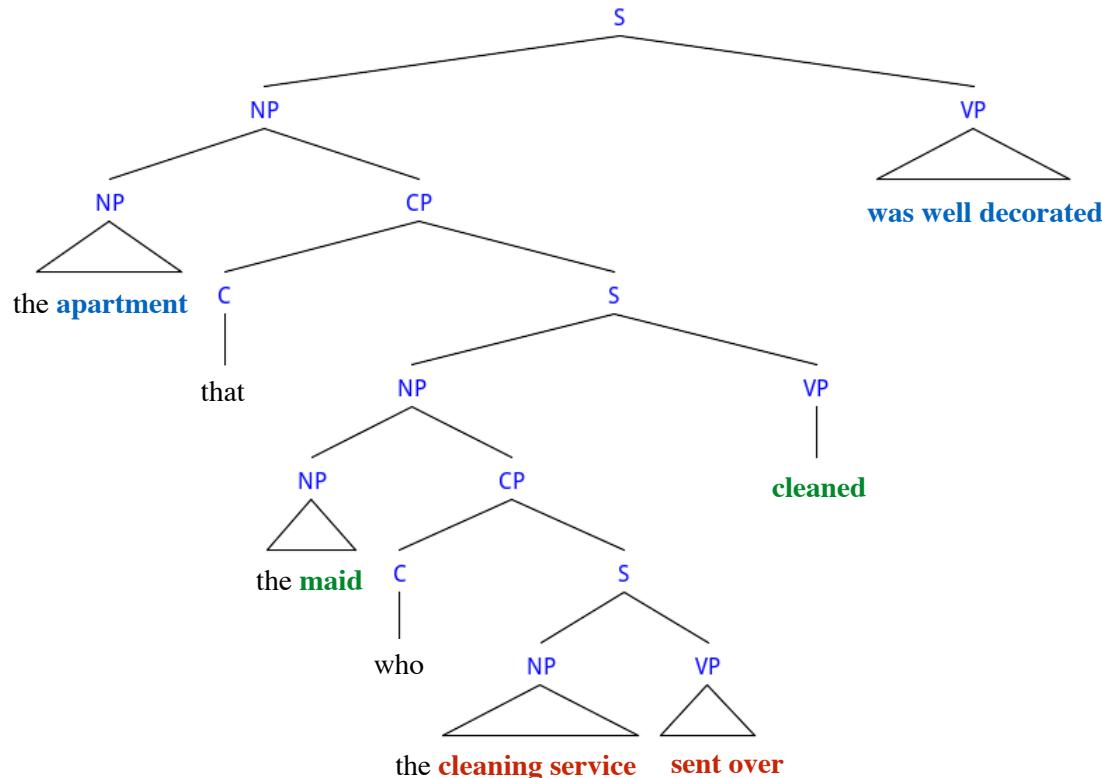
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Structural Forgetting

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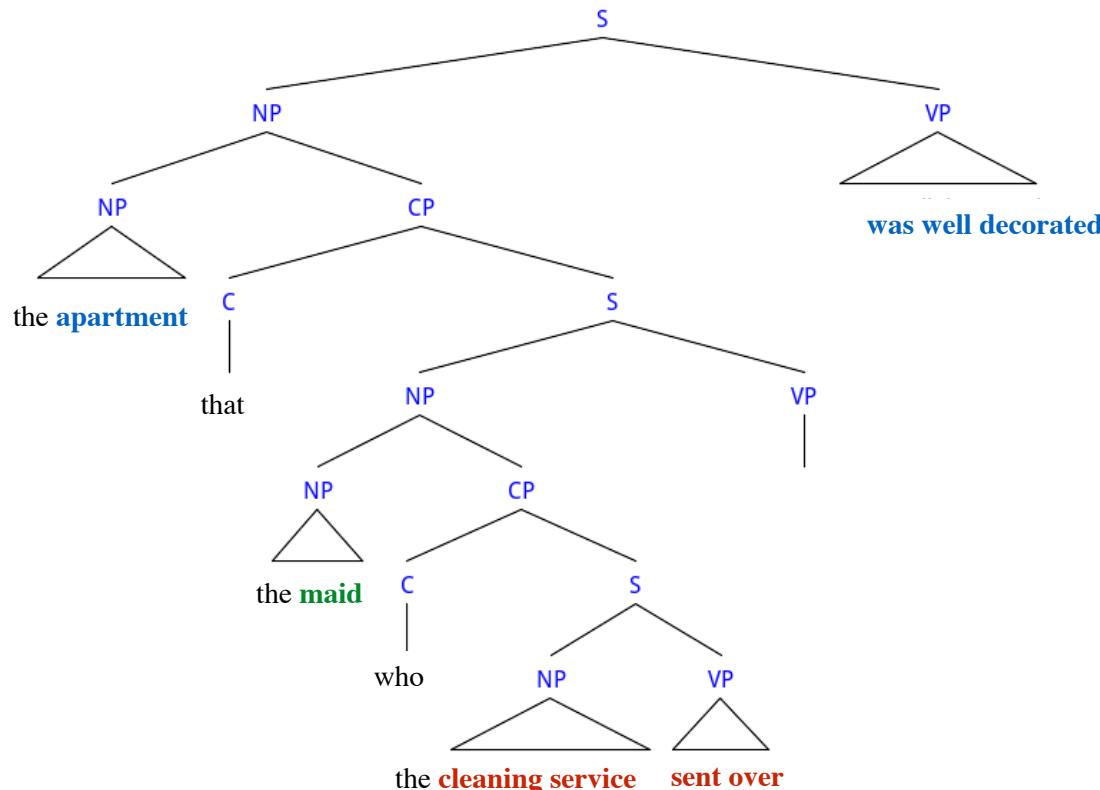
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(Slide courtesy Richard Futrell)

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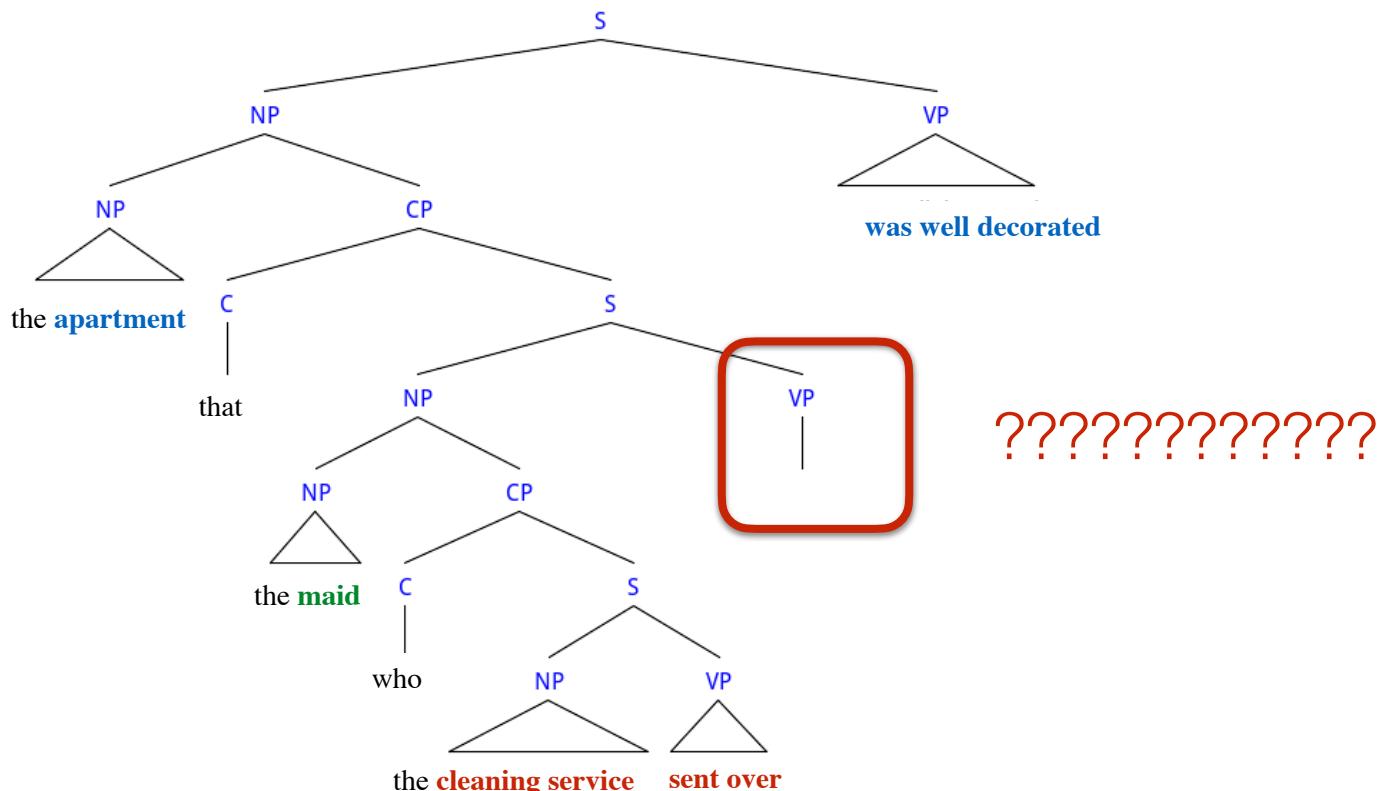
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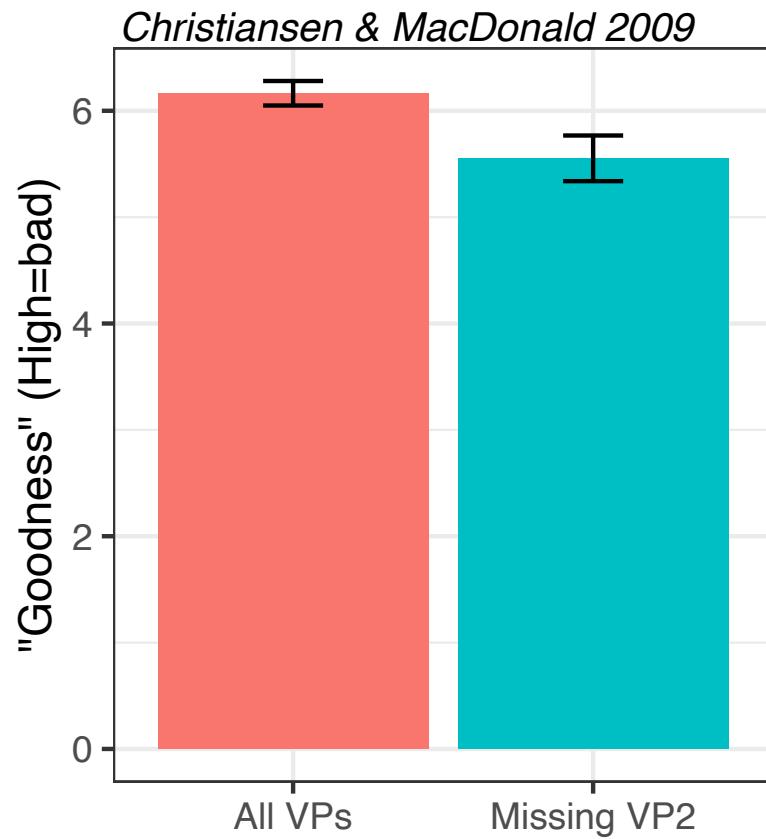
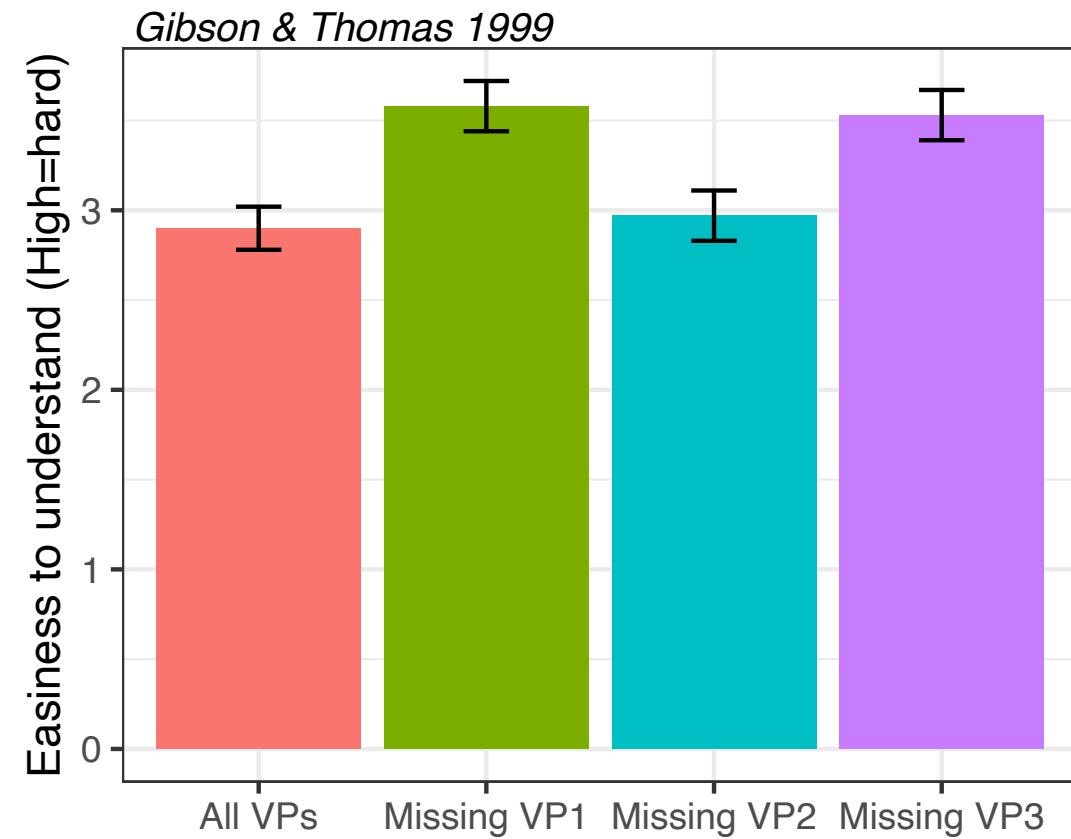
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- **Structural forgetting effect:** part of the sentence is forgotten by the time you get to the end (Gibson & Thomas, 1999; Frazier, 1985; Fodor, p.c.)
 - The ungrammatical sentence seems better than the grammatical one.
 - A "**grammaticality illusion**": how could we define grammaticality in this case?

Gibson & Thomas 1999: whole-sentence reading

The ancient manuscript that the graduate student who the new card catalog had confused a great deal was studying in the library was missing a page.

Christiansen & MacDonald 2009: word-by-word self-paced reading, follows by rating

The chef who the waiter who the busboy offended appreciated admired the musicians.



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context

key word

NOUN THAT NOUN THAT VERB VERB

VERB
#

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S -> NP VERB	1
NP -> NOUN	$1-m$
NP -> NOUN RC	mr
NP -> NOUN PP	$m(1-r)$
PP -> PREP NP	1
RC -> THAT VERB NP	s
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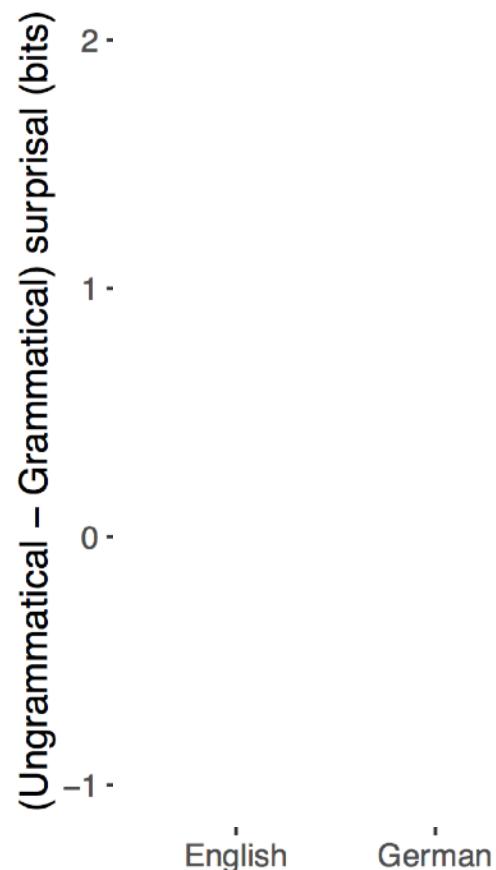
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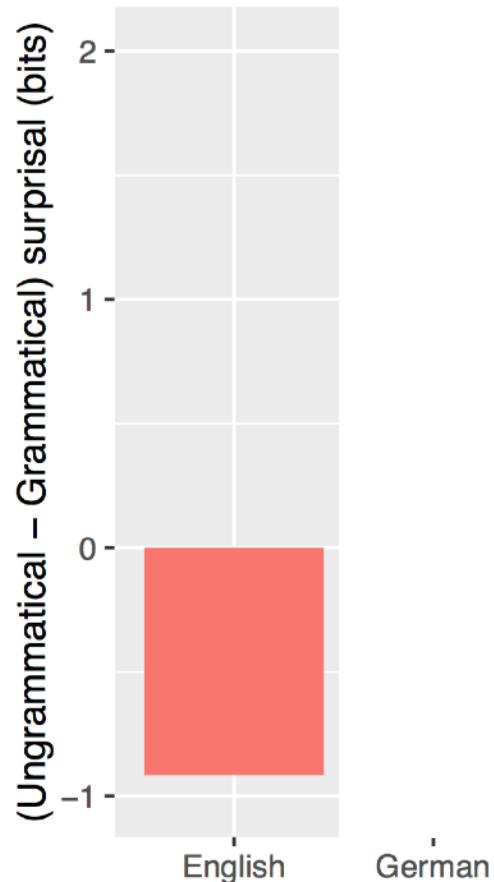
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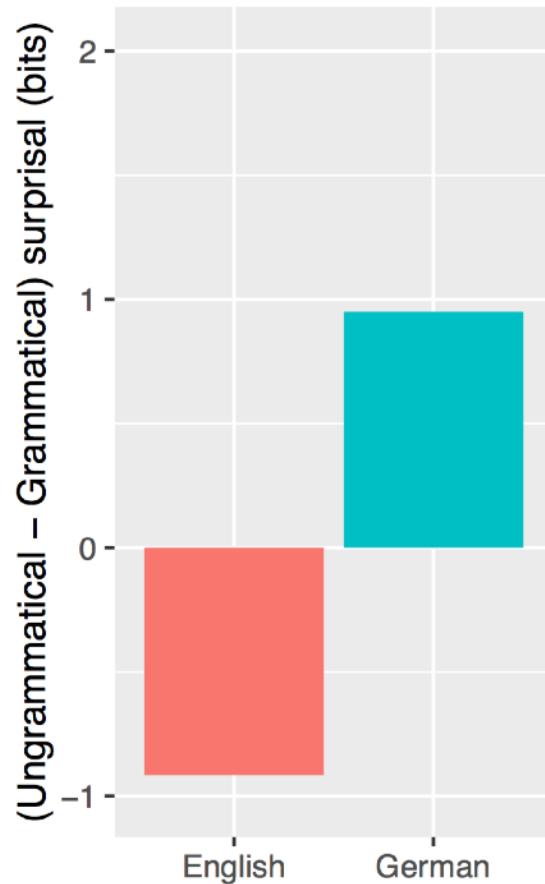
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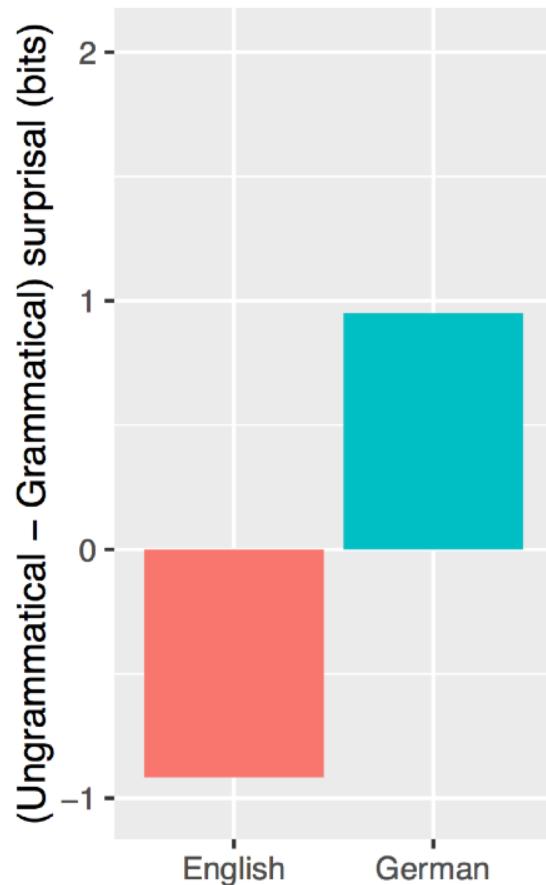


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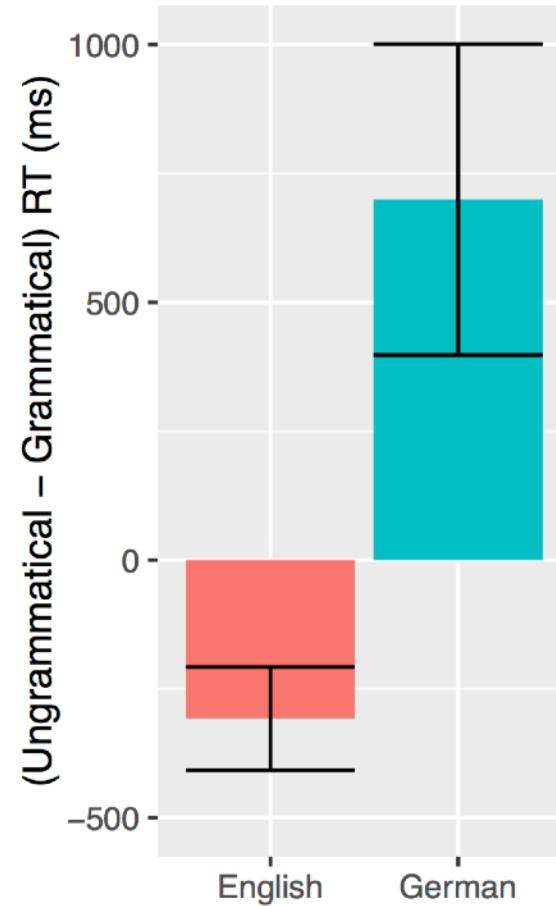
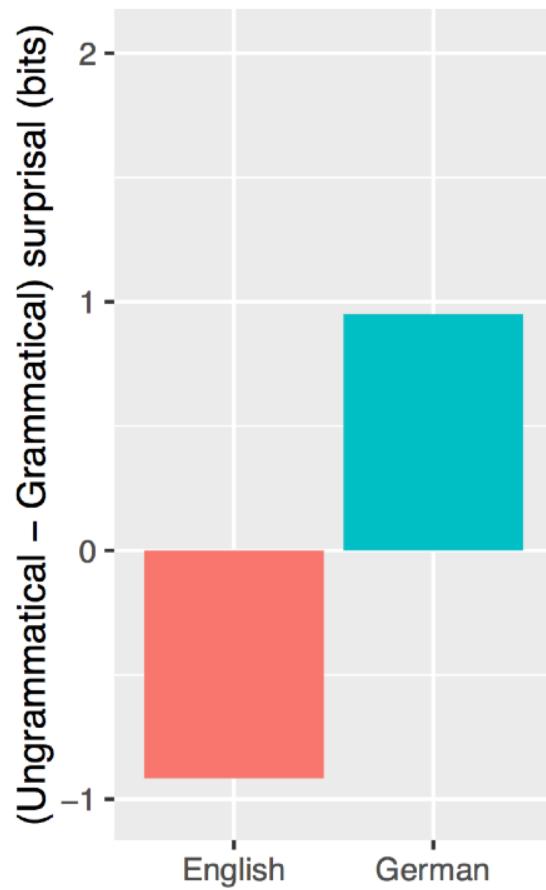
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Vasishth et al. (2010)

Robustness to choice of model parameters

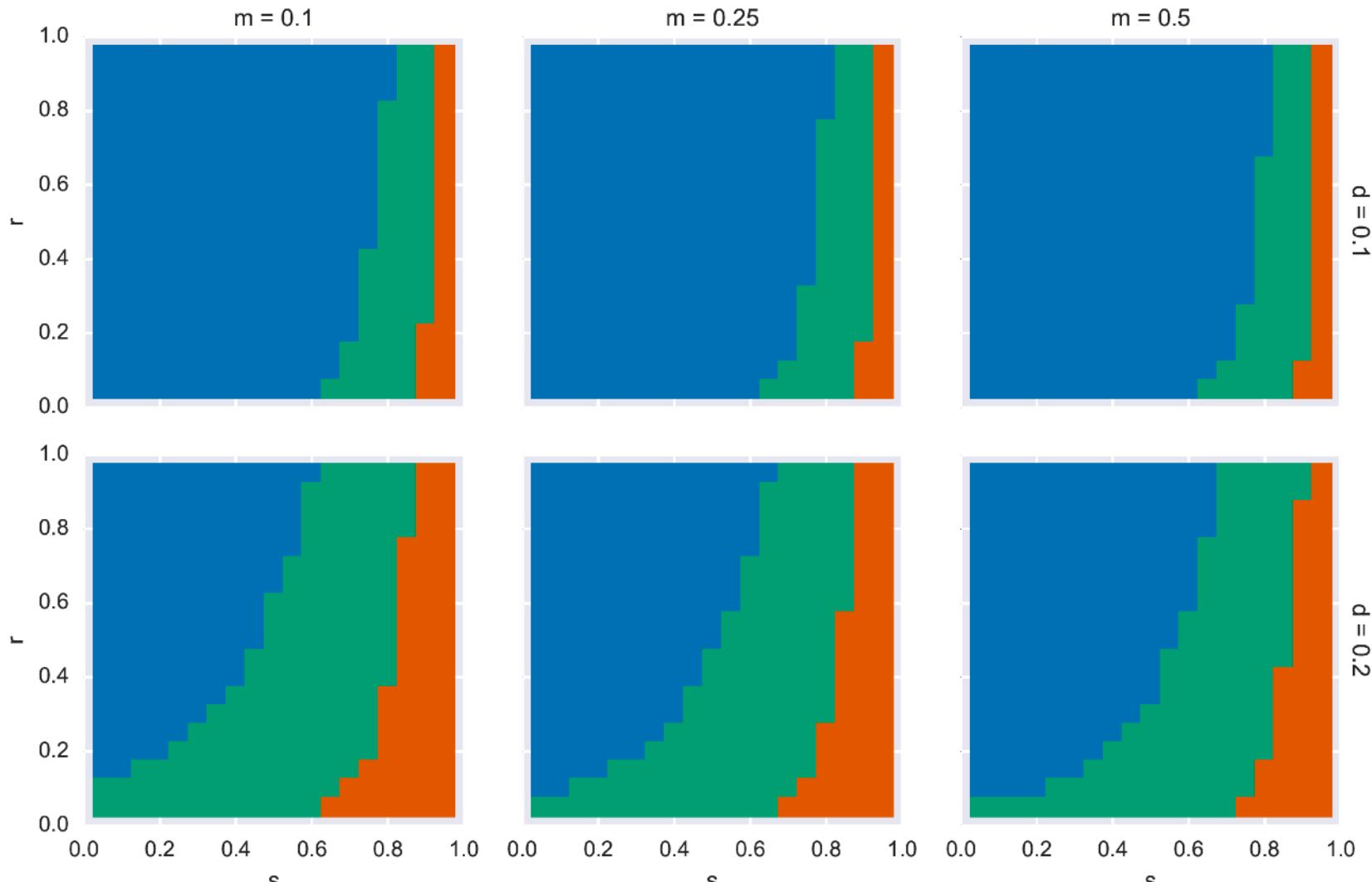
m Modifier probability

s Probability of English RC being verb-final

d Probability of context token deletion



= English+German-like pattern



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Structural Forgetting and the Noisy Channel



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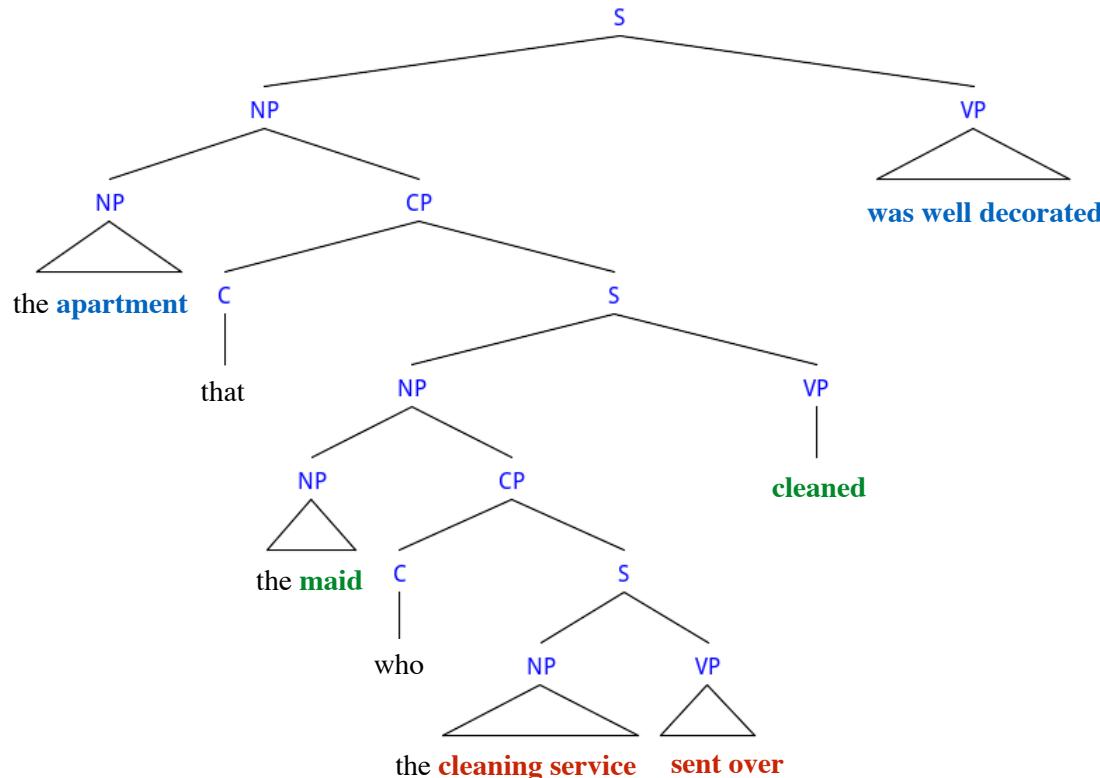


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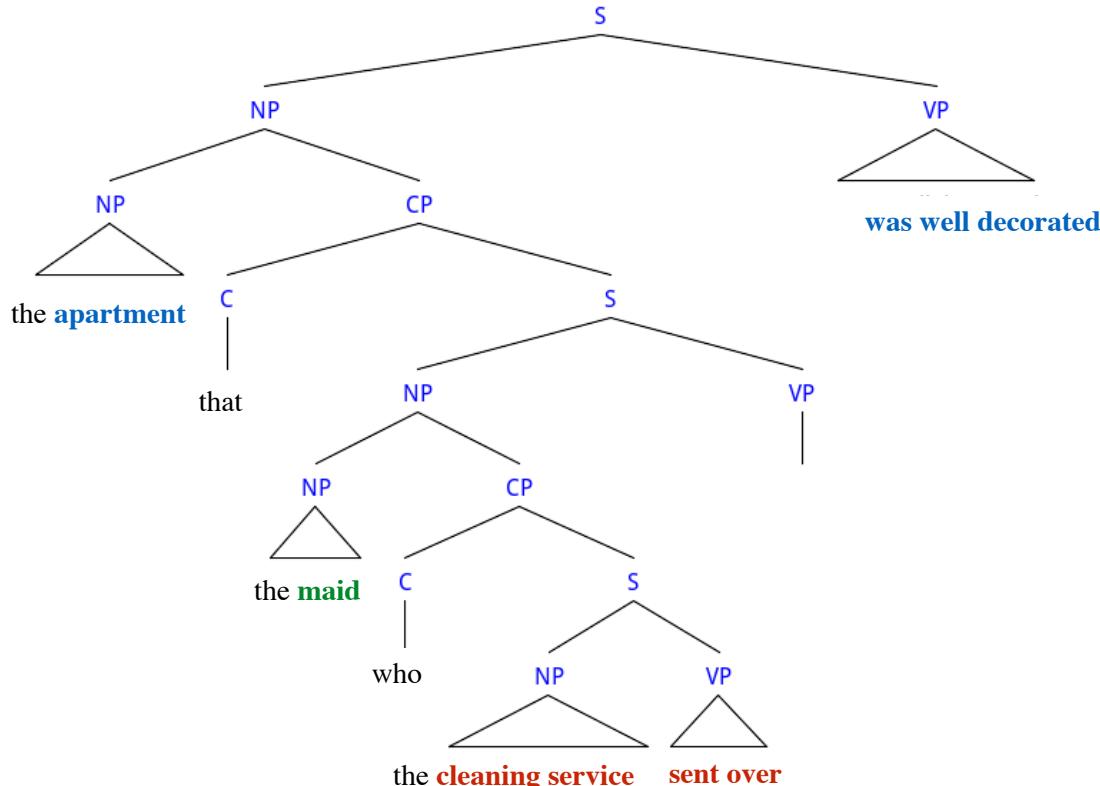
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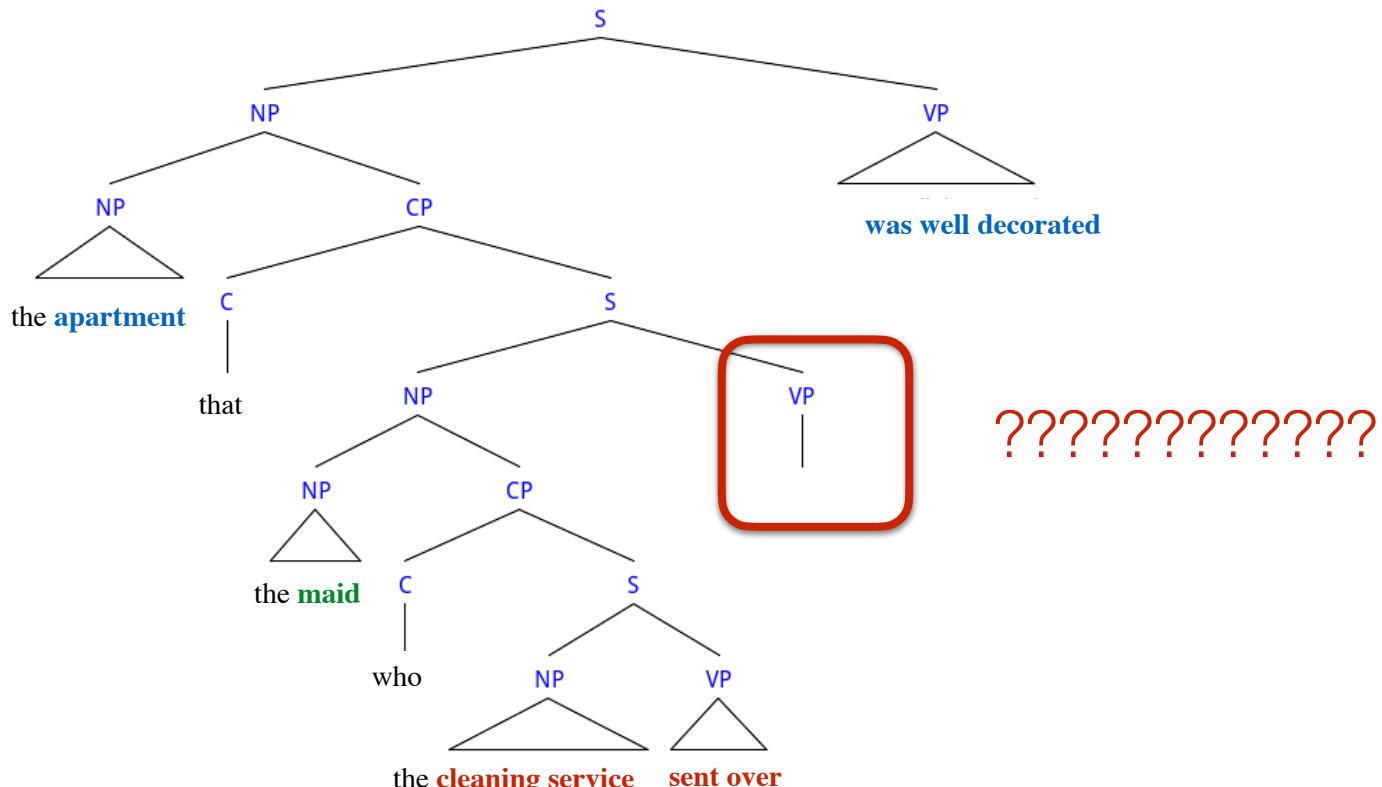
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- The ungrammatical sentence seems better than the grammatical one.
 - A "**grammaticality illusion**": how could we define grammaticality in this case?

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context

key word

NOUN THAT NOUN THAT VERB VERB

VERB
#

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NP -> n _{oun} RC	mr
NP -> n _{oun} PP	$m(1-r)$
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RC -> t _{HAT} v _{erb} NP	s
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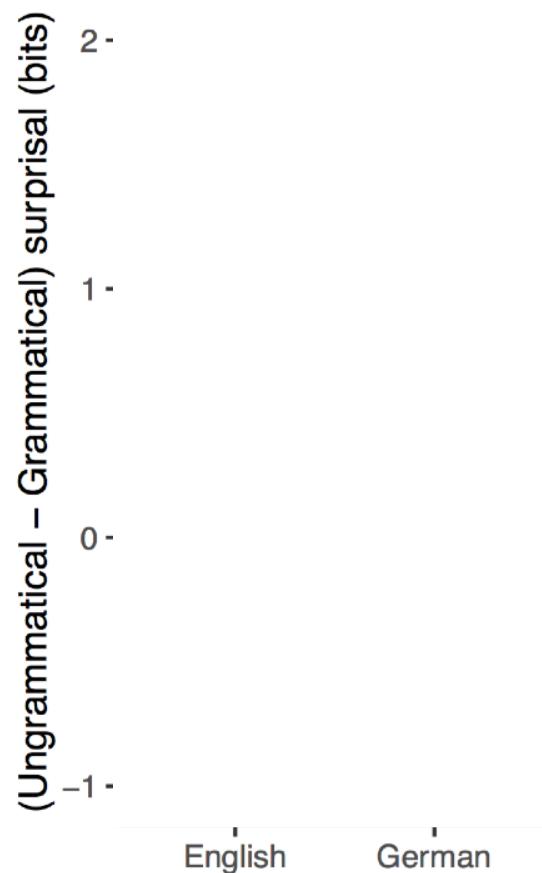
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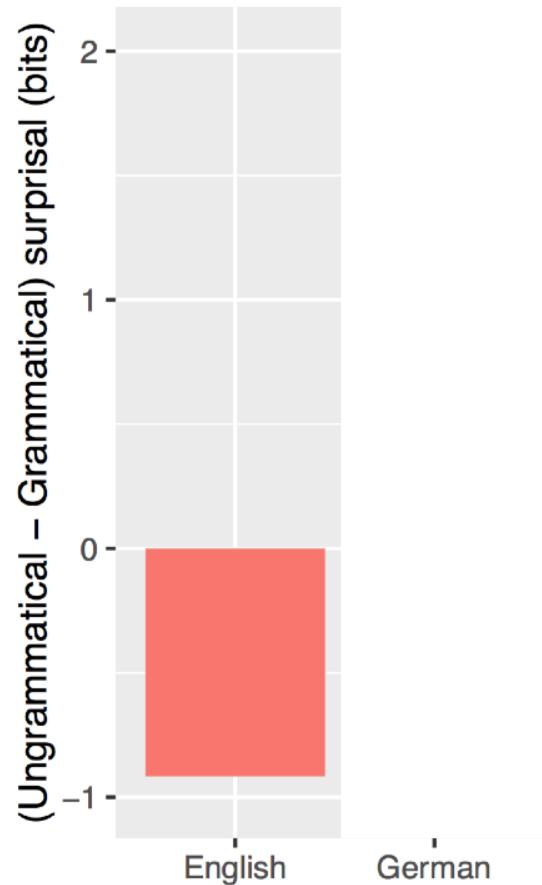
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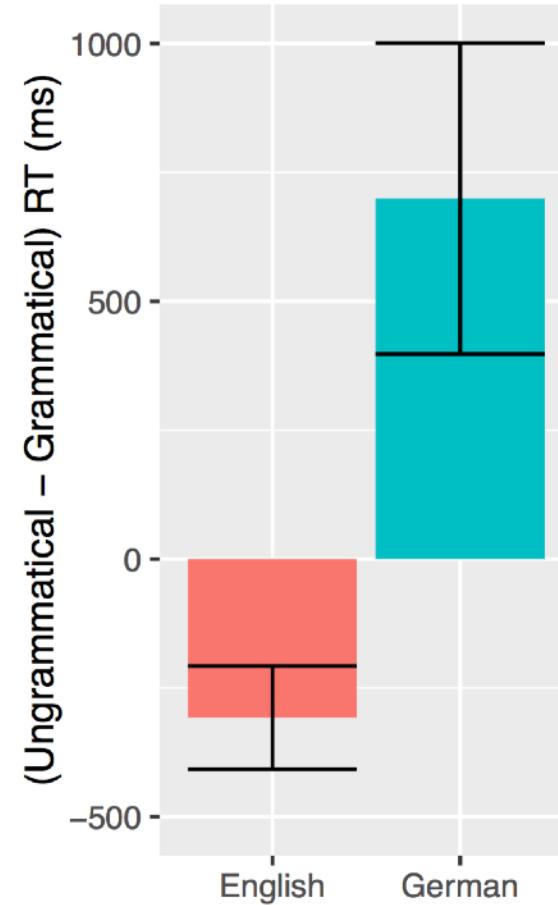
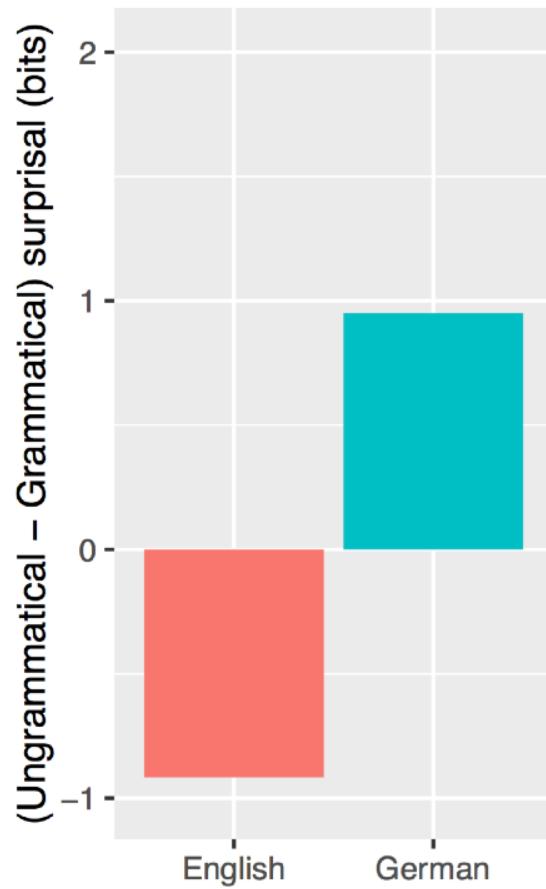
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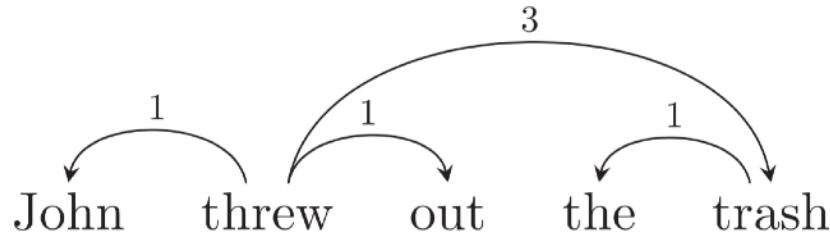
Dependency length and noisy-channel surprisal

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- Syntactic dependencies vary in linear distance

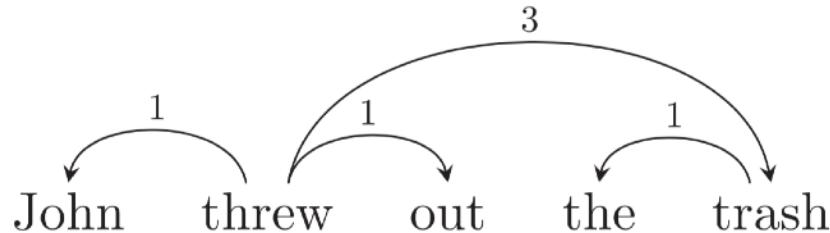
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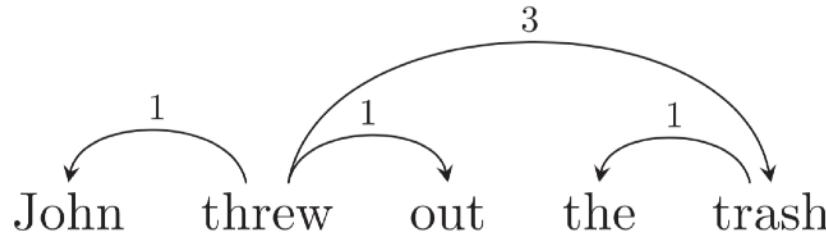
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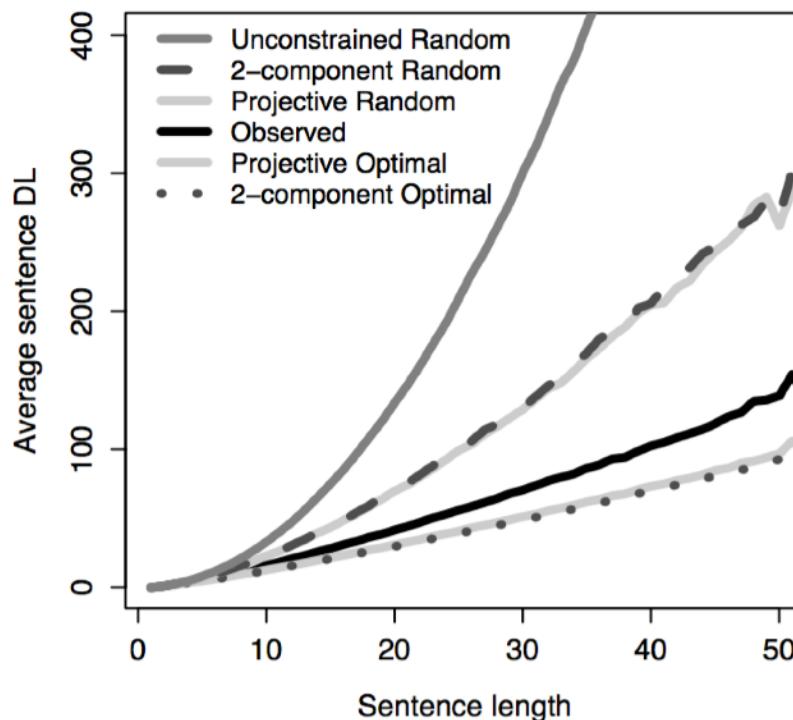
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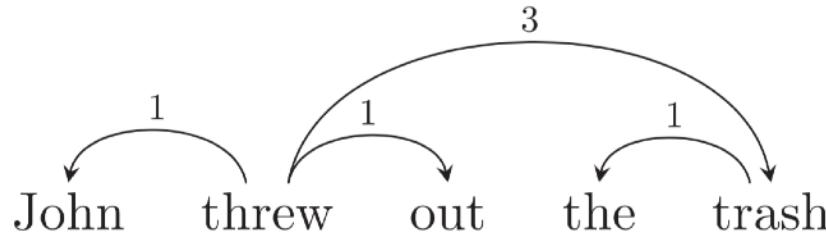


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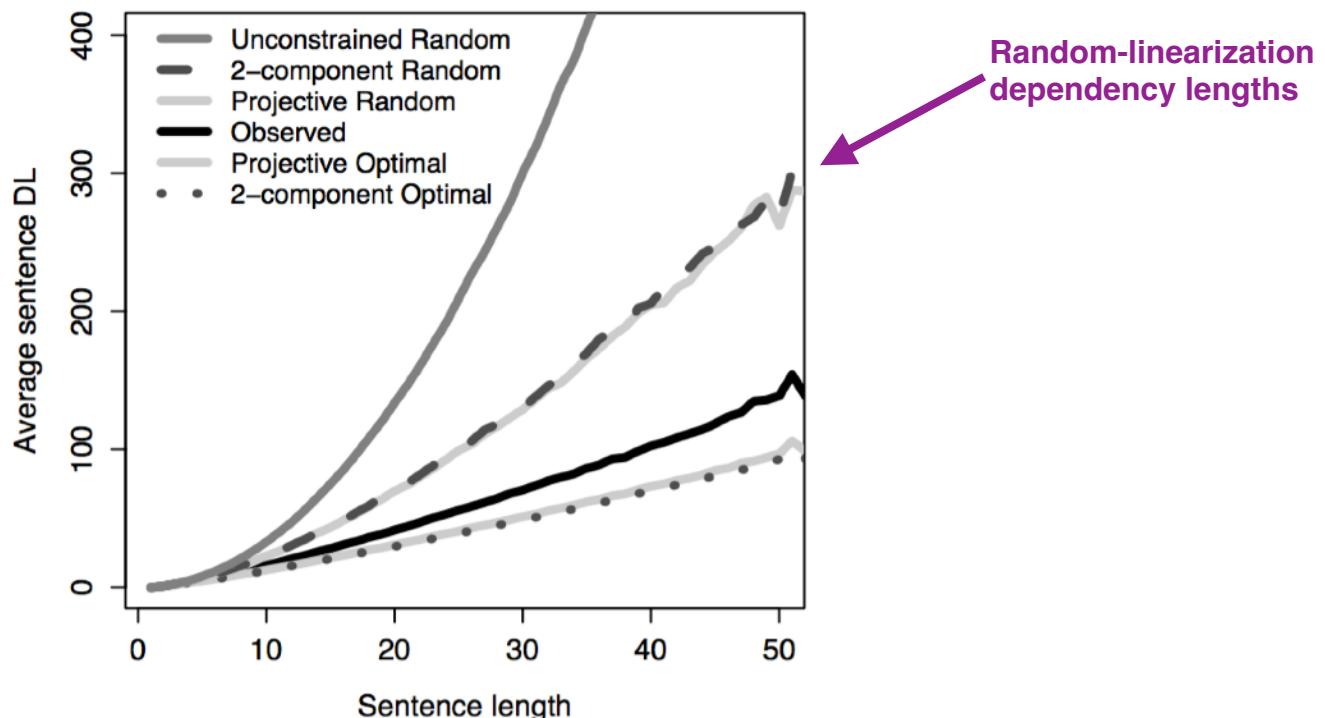


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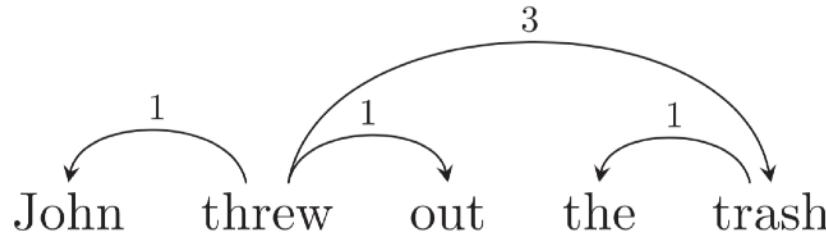


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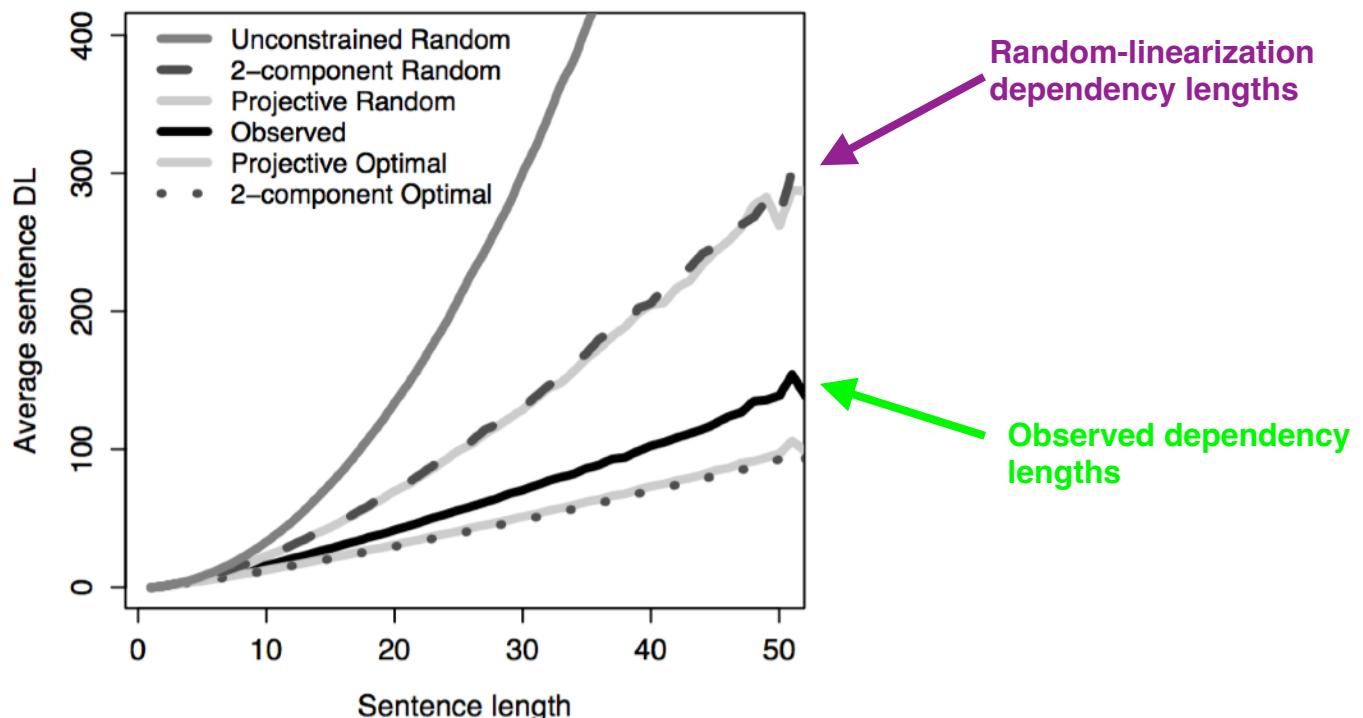


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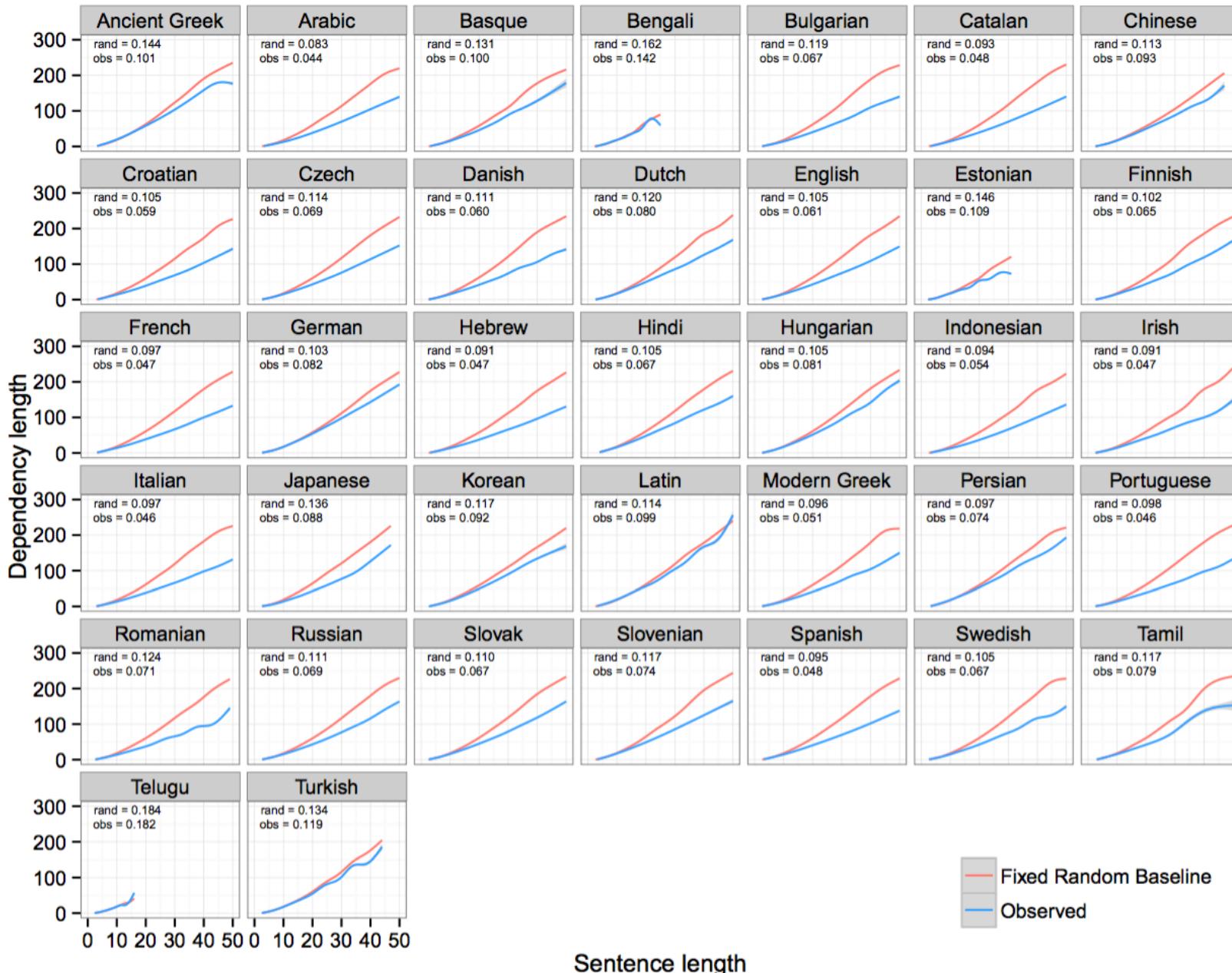
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Dependency lengths are short across languages!



Dependency lengths and the noisy channel

- Here: dependency length minimization can be derived from a combination of surprisal & noisy-channel theory



Richard Futrell

From noisy-channel & surprisal to dependency length minimization

context

John threw the old trash sitting in the kitchen

out

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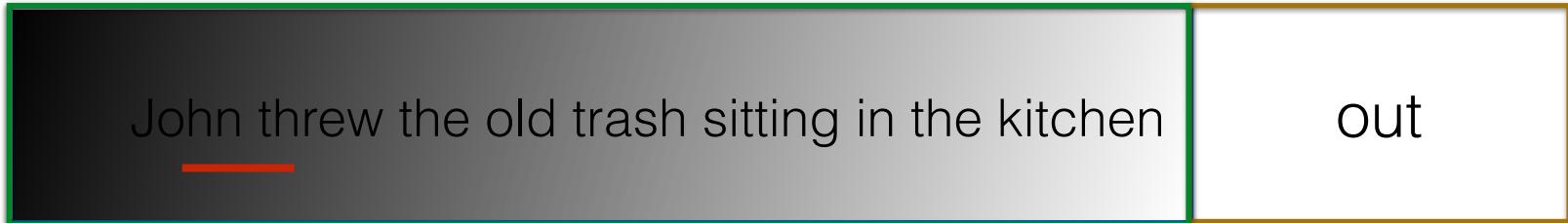
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out

- Suppose we have an **increasing noise rate** the longer a word has been in memory.

From noisy-channel & surprisal to dependency length minimization

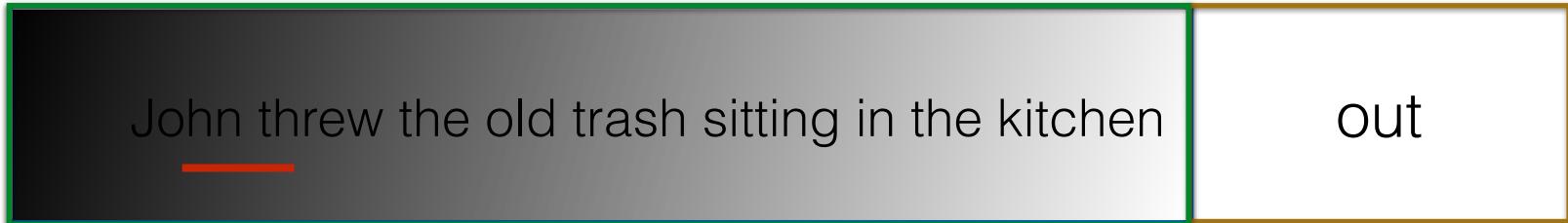
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- We call this **information locality** (following Gildea & Jaeger, 2015).

Derivation of Information Locality

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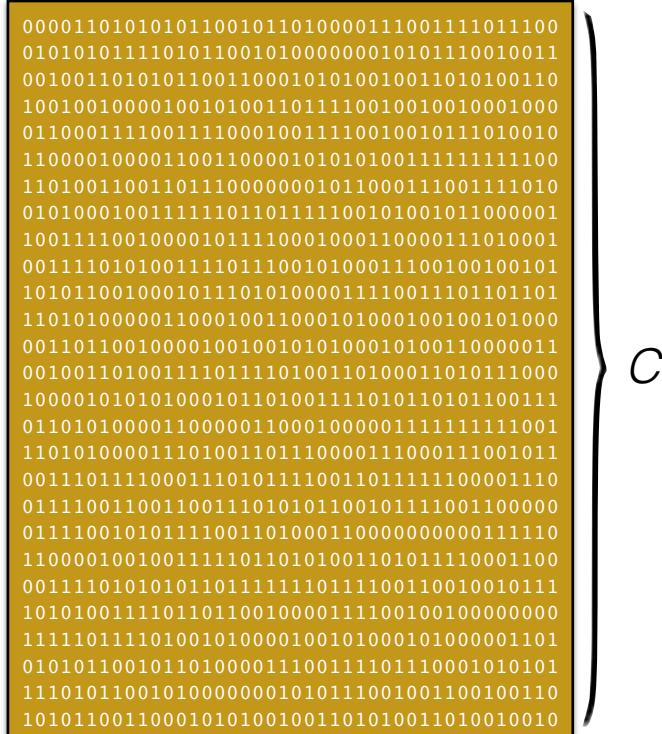
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$h(\text{out})$



000011010101100101101000011100111011100
01010101110101100101000000101011100100111
001001101010110011000101010010011010100110
10010010000100101001101110010010010001000
01100011110011110001001111001001011010010
11000010000110011000010101010011111111100
110100110011011100000001011000111001111010
01010001001111110110111100101001011000001
100111100100001011110001000110000111010001
001111010100111101110010100011100100100101
10101100100010111010100001110011101101101
11010100001100010011000101000100100101000
0011011001000010010010100010100110000011
001001101001111011101001101110010011011100
100001010101000101101001111010110101100111
011010100001100000110001000001111111111001
110101000011101001101110000111000111001011
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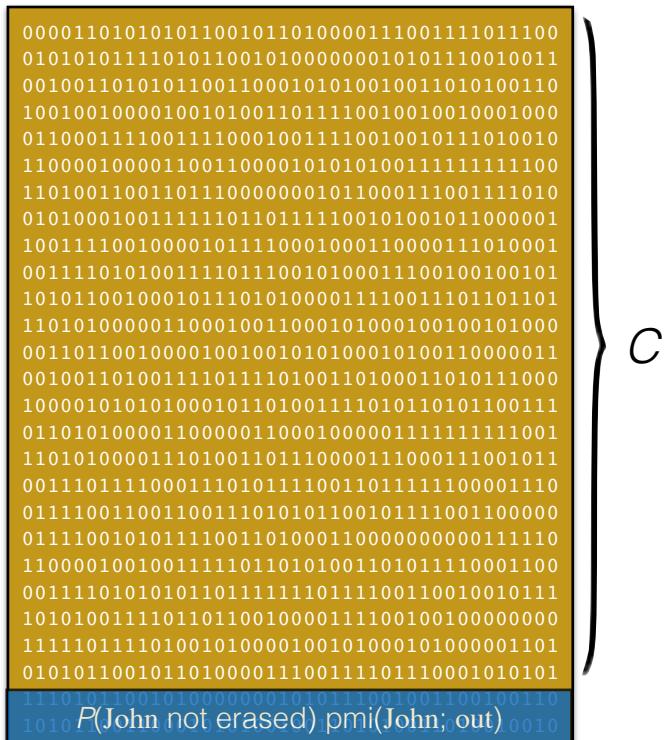
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$h(\text{out}) - P(\text{John not erased}) \text{pmi}(\text{John}; \text{out})$



```

000011010101100101101000011100111011100
01010101110101100101000000101011100100111
001001101010110011000101010010011010100110
100100100001001010011011110010010010001000
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110100110011011100000001011000111001111010
01010001001111110110111100101001011000001
100111100100001011110001000110000111010001
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0111100110011001110101011001011110011000000
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00111101010101101111110111100110010010111
101010011110110110010000111100100100000000
111110111101001010000100101000101000001101
010101100101101000011100111101110001010101
111011110010100000010101110010011001001100
1010 P(John not erased) pmi(John; out) 0010

```

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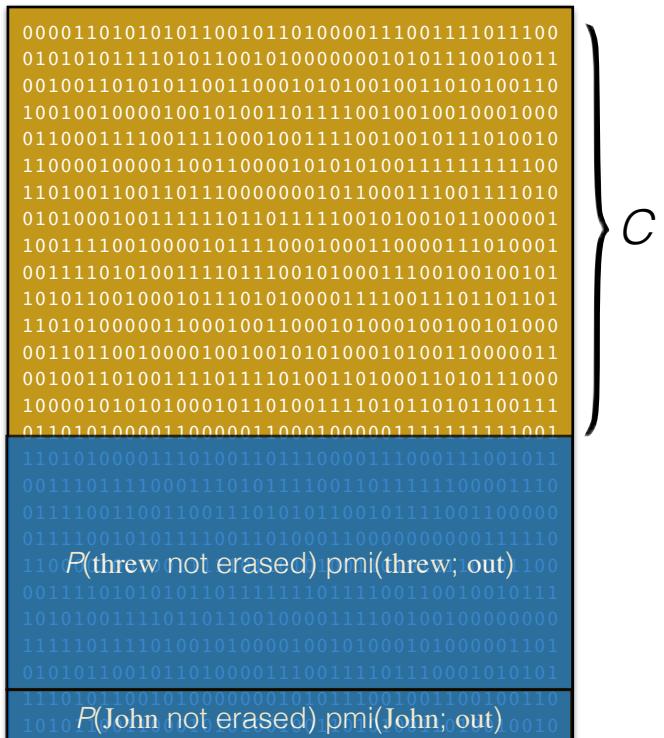
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000011010101100101101000011100111011100
 01010101110101100101000000101011100100111
 001001101010110011000101010010011010100110
 10010010000100101001101110010010010001000
 01100011110011110001001111001001011010010
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 0101000100111110110111100101001011000001
 100111100100001011110001000110000111010001
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 01101010000110000011000100001111111111001
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 00111011110001110101110011011111000011100
 011110010011001110101011001011100110000000
 011110010101111001101000110000000000111100
 110 P(threw not erased) pmi(threw; out) 100
 001111010101011111011110011001001011100101
 101010011110110110010000111100100100000000
 111110111101001010000100101000101000001101
 010101100101101000011100111100101100010101
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$$\quad - P(\text{threw} \text{ not erased}) \text{pmi}(\text{threw}; \text{out})$$

$$\quad - P(\text{the} \text{ not erased}) \text{pmi}(\text{the}; \text{out})$$

000011010101100101101000011100111011100
 01010101110101100101000000101011100100111
 001001101010110011000101010010011010100110
 10010010001001010011011110010010010001000
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 100111100100001011110001000110000111010001
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 101011001000101110101000011110011101101101
 11010100001100010011000101000100100101000
 001101100100001001001010100010100110000011
 001001101001111011110100110110010001101100
 1000011010101111011110100110110010001101110
 P(the not erased) pmi(the; out) 100111
 011010100001110100110110000111000111001011
 001110111100011101011110011011111000011100
 0111100100110011101010110010111001100000000
 0111100101011110011010000110000000000111110
 110 P(threw not erased) pmi(threw; out) 100
 00111101010101111101111001100100101111001011
 1010100111101101100100001111001001000000000
 111110111101001010000100101000101000001101
 01010110010110100001110011110011110001010101
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C

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000011010101100101101000011100111011100
 01010101110101100101000000101011100100111
 001001101010110011000101010010011010100110
 1001001000100101001101110010010010001000
 01100011110011110001001111001001011010010
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 100111100100001011110001000110000111010001
 001111010100111101110010100011100100100101
 101011001000101110101000011110011101101101
 110101000011000100110000101000100100100101000
 0011010000110001001100001010001001001001000
 P(trash not erased) pmi(trash; out) 0011
 00100101011101110110101010101010101000000000
 100001010000111010011011111000011100
 P(the not erased) pmi(the; out) 100111
 0110101000011101001101100001110001110010111
 001110111100011101011110011011111000011100
 0111100100110011010101100101110011000000000
 0111100101011110011010001100000000000111100
 P(threw not erased) pmi(threw; out) 100
 00111101010101111101111001100100100100000000
 1010100111101101100100001111001001000000000
 111110111101001010000100101000101000001101
 0101011001011010000111001111001011000010101
 1110101100101000000010101110010011001001100
 P(John not erased) pmi(John; out) 0010

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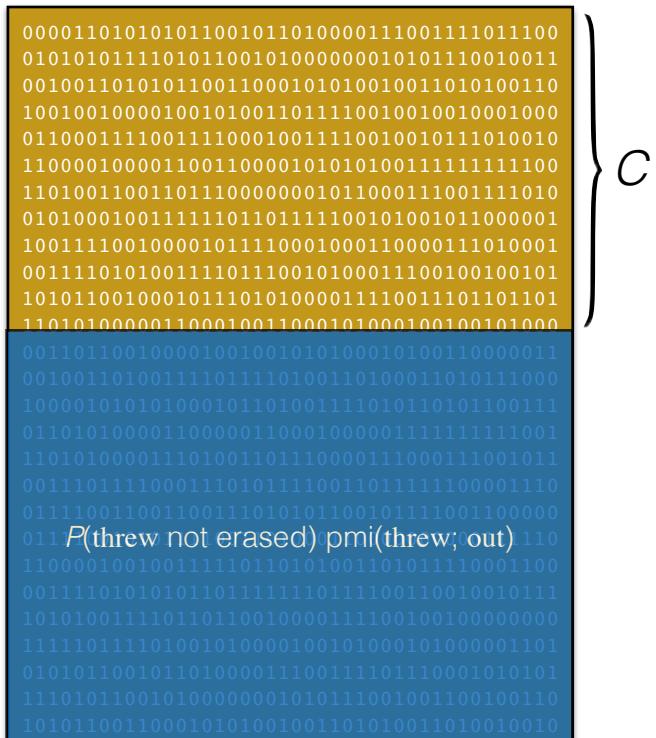
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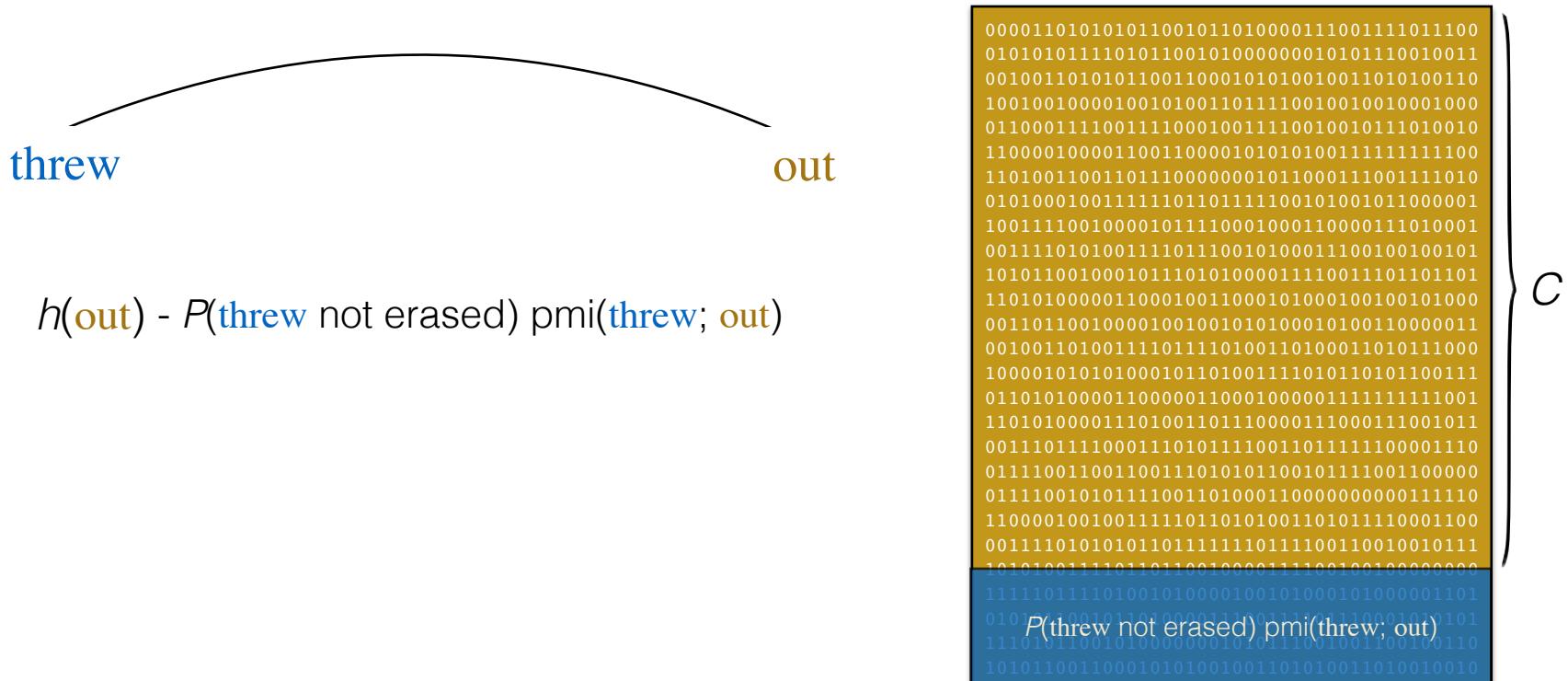
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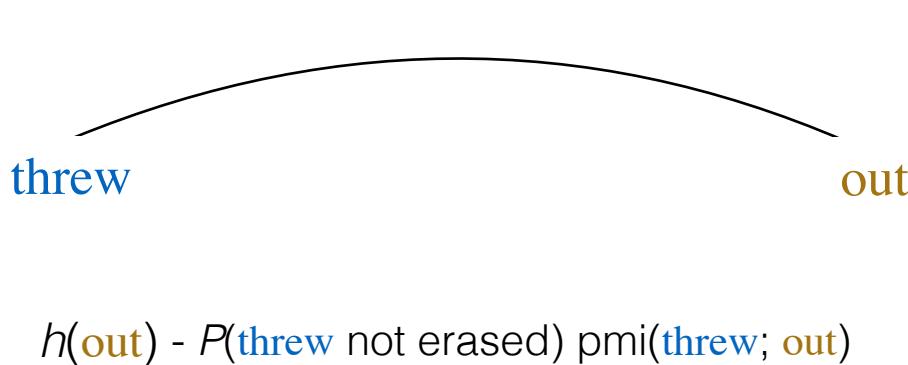
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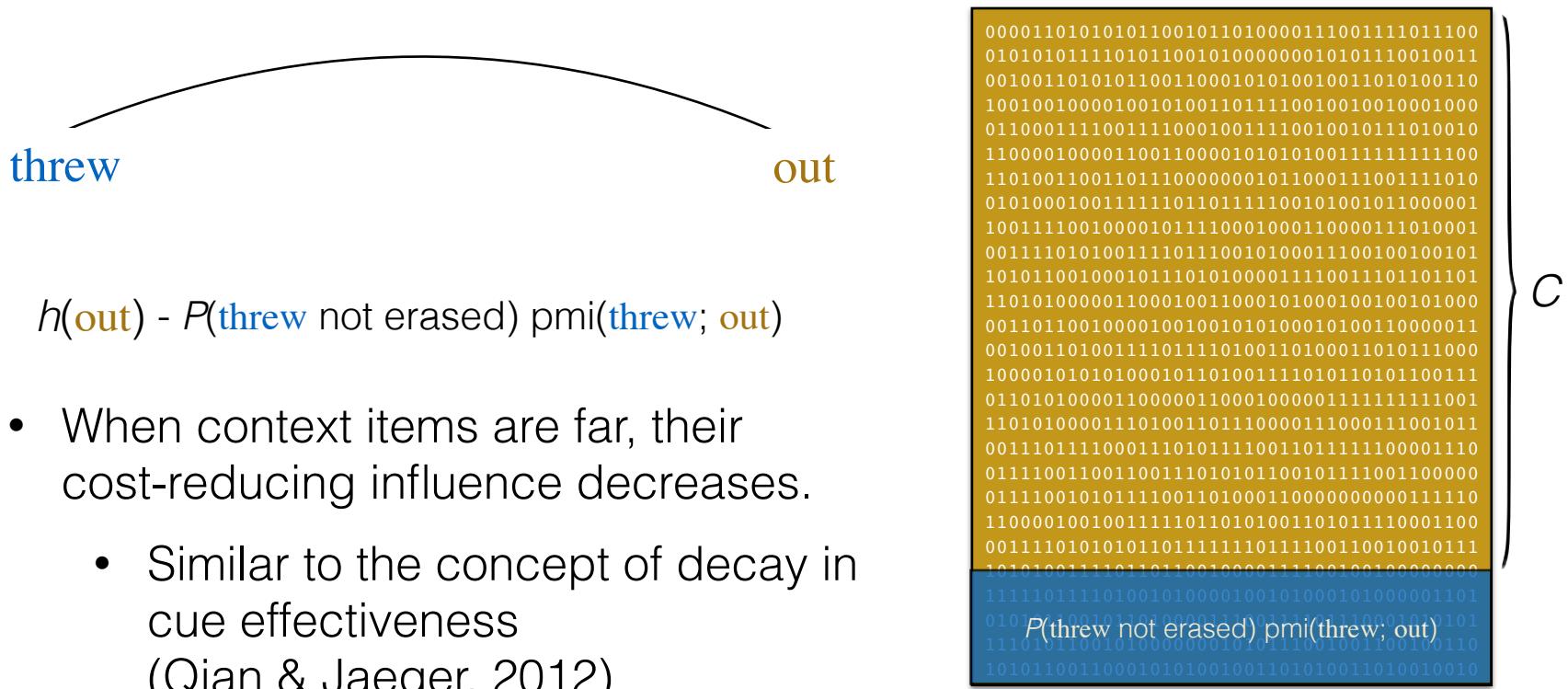
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100111100100001011110001000110000111010001
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01010100010010101010101010101010101010101
111011011001010000101010111001001100100110
1010110011000101010010011010101001100100101

$P(\text{threw not erased}) \text{pmi}(\text{threw}; \text{out})$

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- When context items are far, their cost-reducing influence decreases.
 - Similar to the concept of decay in cue effectiveness
(Qian & Jaeger, 2012)

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- We will show that the hypothesis is true in dependency corpora.

Do Dependencies Have High Mutual Information?

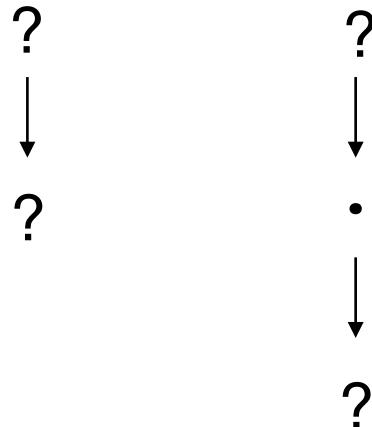
Do Dependencies Have High Mutual Information?

?

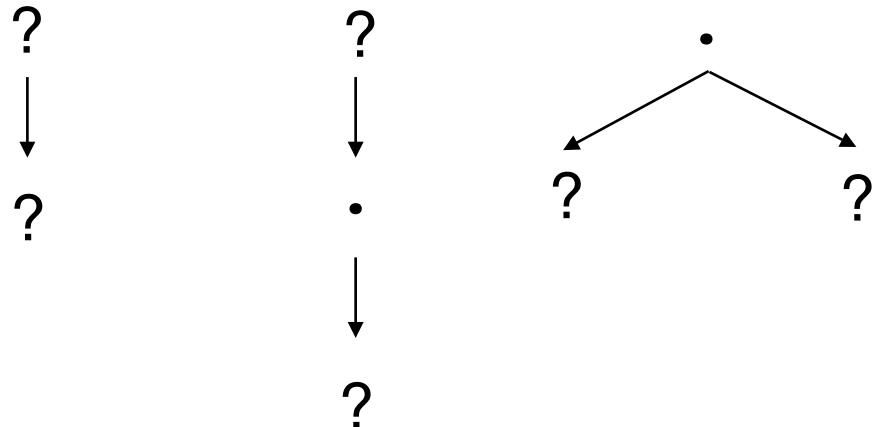


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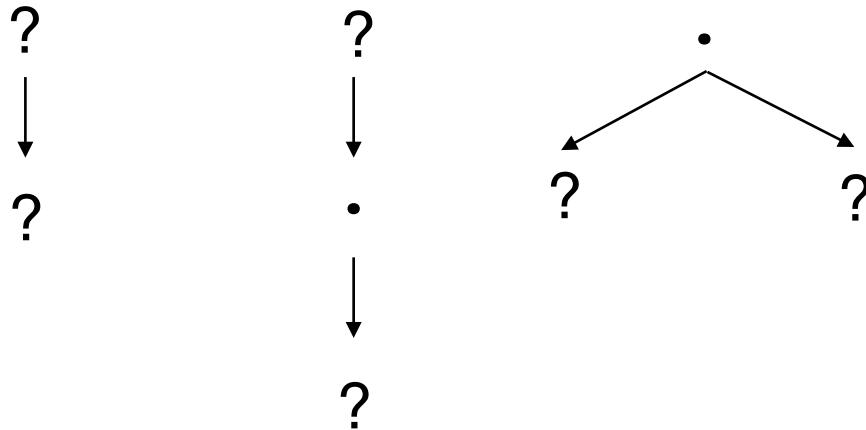
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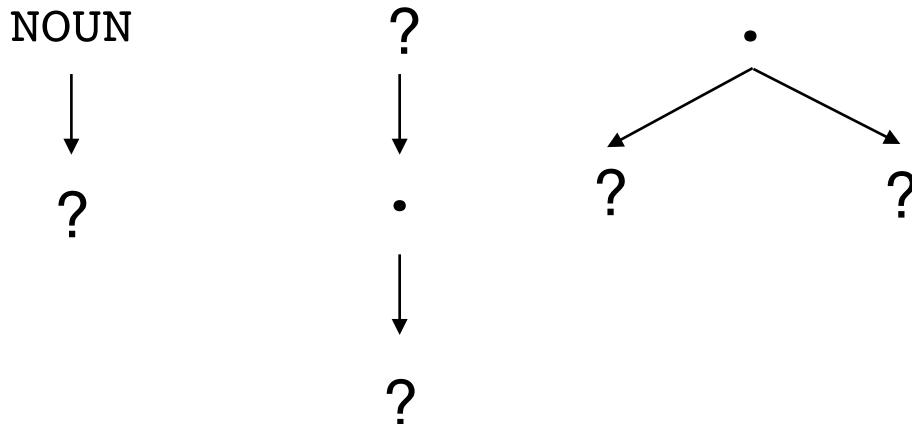


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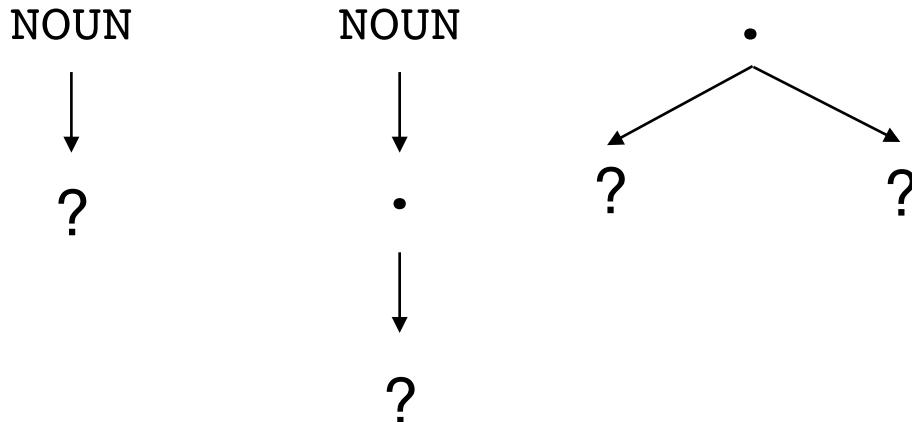
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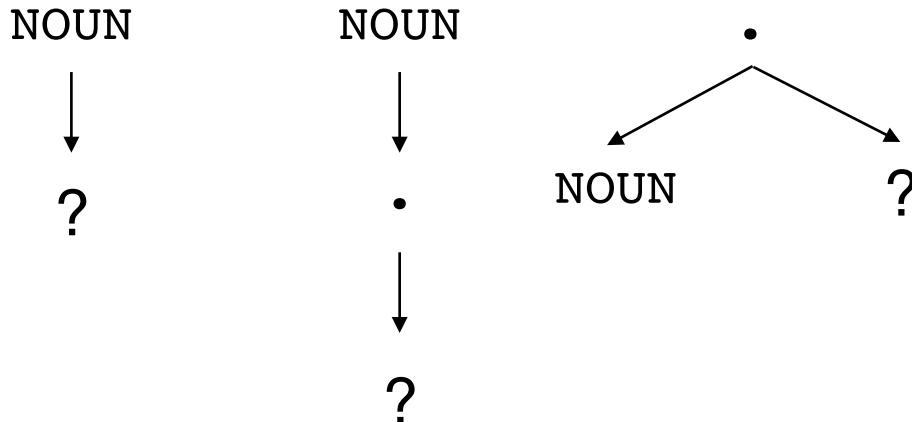
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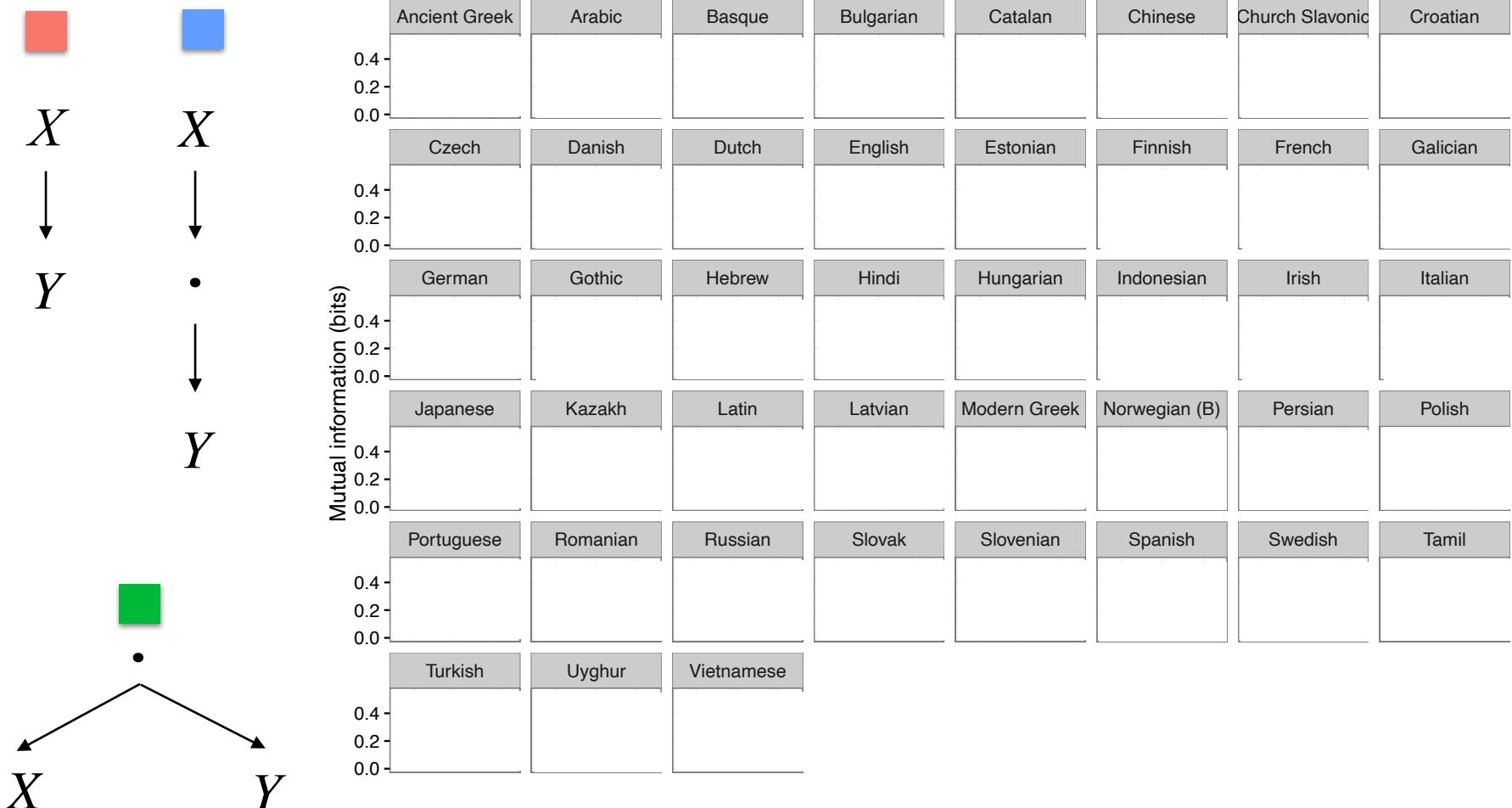


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Comprehension as exploration of input

- Broader ongoing goal: develop eye-movement control model integrating the insights discussed thus far:
 - Probabilistic linguistic knowledge
 - Uncertain input representations
 - Principles of adaptive, rational action
- *Reinforcement learning* is an attractive tool for this

A rational reader

- Very simple framework:
 - Start w/ prior expectations for text (linguistic knowledge)
 - Move eyes to get perceptual input
 - Update beliefs about text as visual arrives (Bayes' Rule)
- Add to that:
 - Set of *actions* the reader can take in discrete time
 - A *behavior policy*: how the model decides between actions

A first-cut behavior policy

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- Actions: *keep fixating*; *move the eyes*; or *stop reading*
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- Define *confidence* in a character position as the probability of the most likely character

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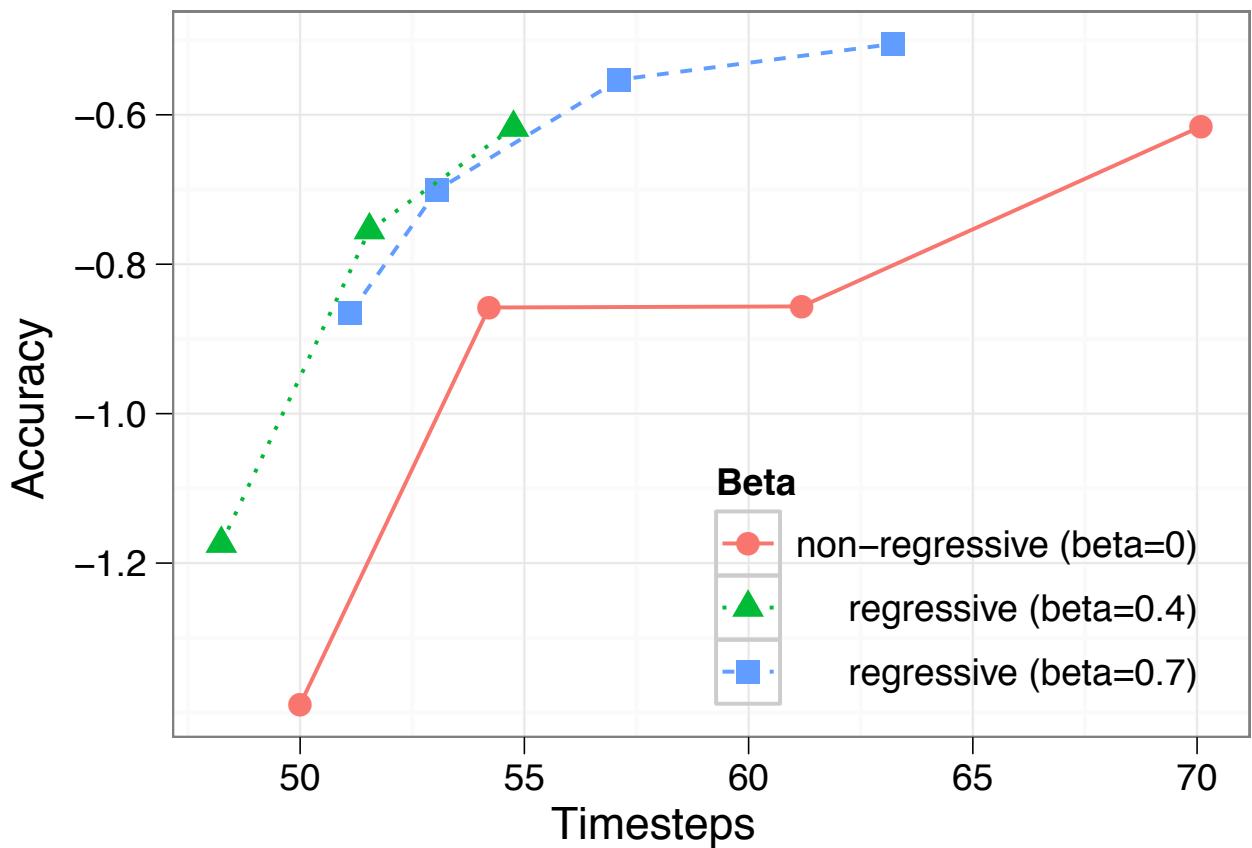
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...

- Move left to right, bringing up confidence in each character position until it reaches α
- If confidence in a previous character position drops below β , regress to it
- Finish reading when you're confident in everything

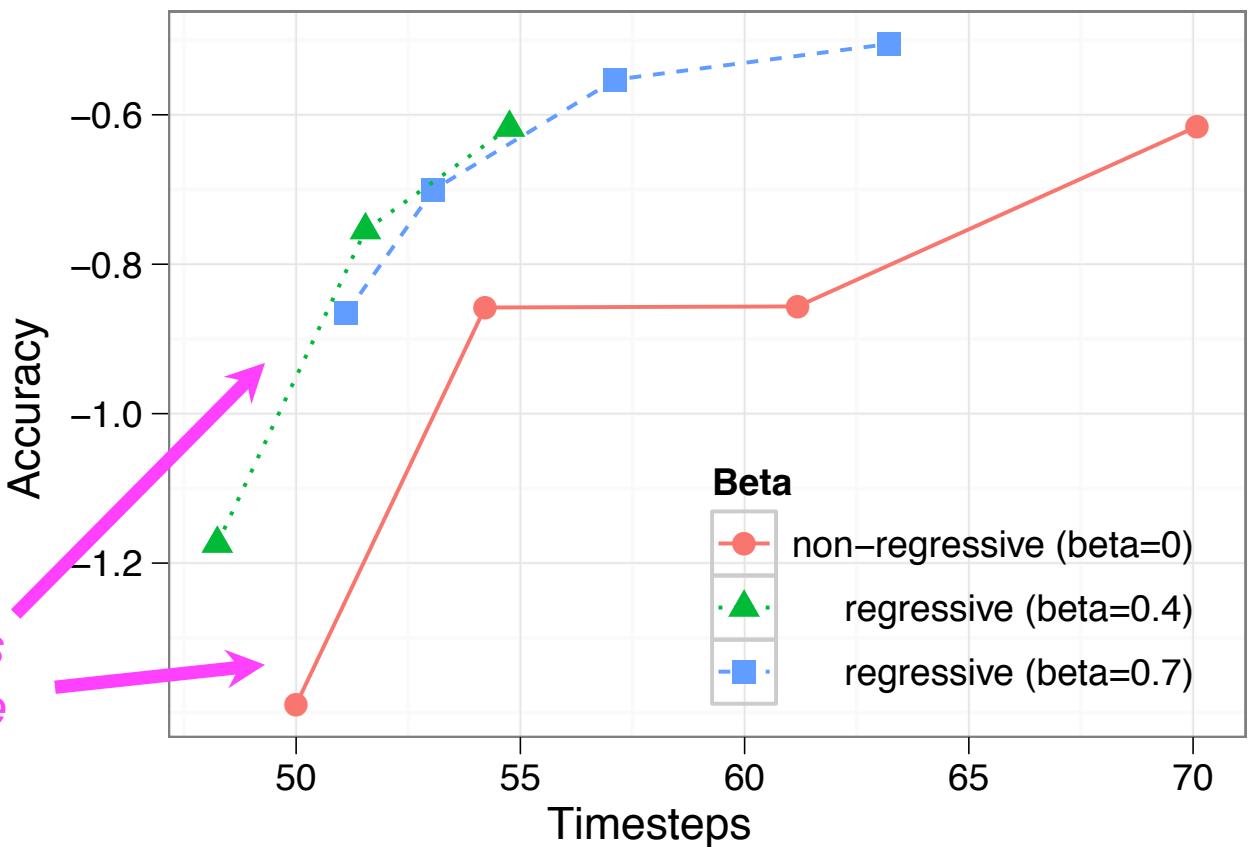
(Non)-regressive policies

- Non-regressive policies have $\beta=0$
- Hypothesis: non-regressive policies strictly dominated
- Test: estimate speed and accuracy of various policies on reading the the Schilling et al. (1998) corpus



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Goal-based adaptation

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- Open frontier: modeling the adaptation of eye movements to specific reader goals
- We set a *reward function*: relative value γ of speed (finish reading in T timesteps) versus accuracy (guess correct sentence with probability L)
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γ	α	β
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0.1		
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0.1	0.36	0.80	25.8	P(correct)=0.41
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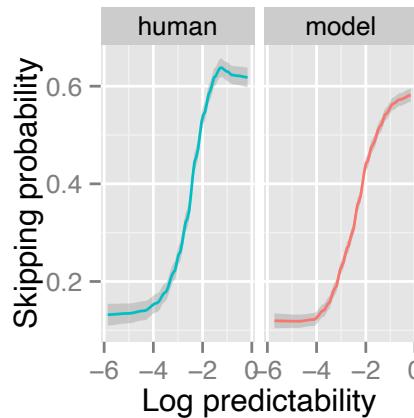
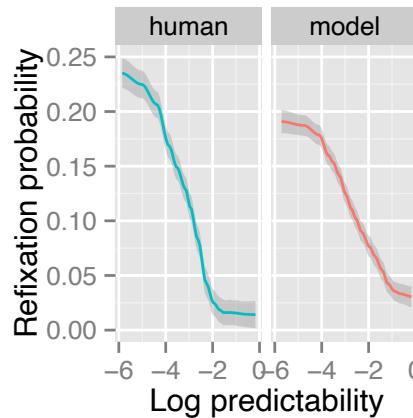
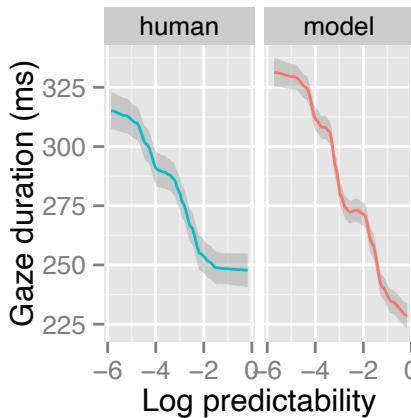
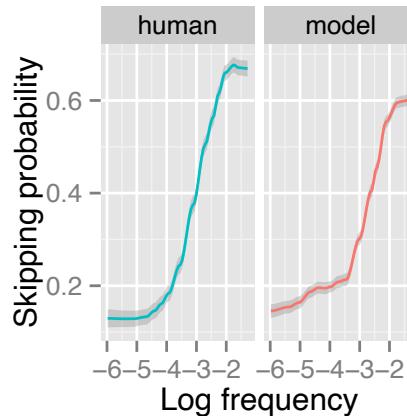
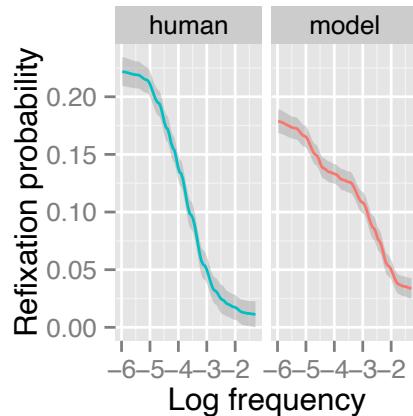
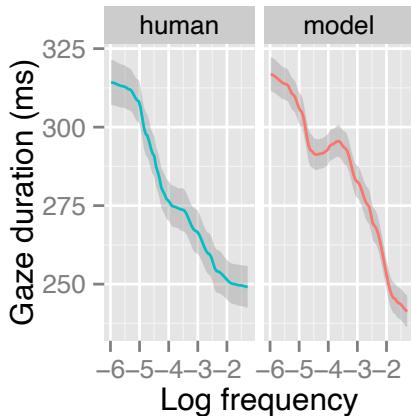
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- The method works, and gives intuitive results

Empirical match with human reading

- Benchmark measures in eye-movement modeling:

frequency



predicts size and
shape of all effects

predictability

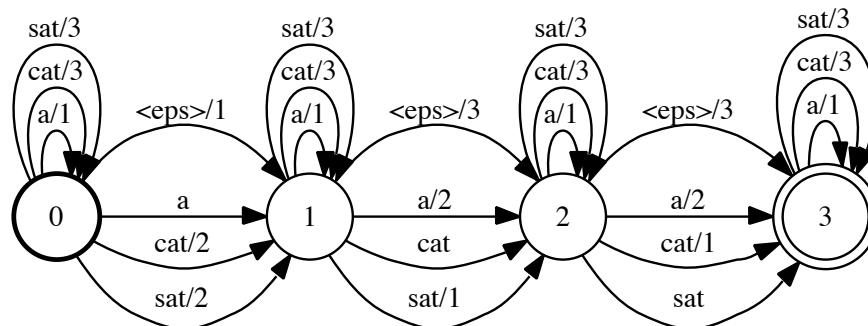
Bicknell & Levy (2012)

Success at empirical benchmarks

- Other models (E-Z Reader, SWIFT) get these too, but *stipulate* rel'nship between word properties & “processing rate”
- We *derive* these relationships from simple principles of noisy-channel perception and rational action

Noisy-channel processing: summary

- Noisy-channel models help us understand
 - Basic capabilities of human language comprehension
 - Outstanding puzzles in syntactic processing
- These models open up a rich typology of new sentence processing effects
- There is growing evidence for these effects
- These models pose new theoretical opportunities and architectural challenges for the study of human linguistic cognition



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