ChulwalarStudy

Randy Lisbona, Christopher Farrar

July 27, 2016

Introduction

The Prime Minister of Chulwalar personally invited aspiring SMU Data Scientist Students Randy Lisbona and Christopher Farrar to analyze and forecast the islands export data for the year 2015. Randy and Chris were granted access to the islands economic data and chief statistical scientist, in order to answer the following questions.

- 1. What is the best model for the export data and how we define the best?
- 2. Which forecast model is the best fit and how we define it
- 3. All of the different models we could consider could be useful or good. How do we choose among equally good models

Analysis steps -Import the data

The source files provided by the Chulwalar department of statistical analysis and forecasting were imported into R 3.3.1 for time series analysis, These files were current as of July 18, 2016, reflecting Chulwalar exports data as of December 2015

- 1. ImportedAsIsDataChulwalar.csv
- 2. ImportedPlanDataChulwalar.csv
- 3. ImportedIndicatorsChulwalar.csv

Transform data into time series

In order to be able to work with the partial data sets later, these need to be split into individual vectors and converted into times series. 1. For details on time series conversion please refer to source file "./Analysis/TransformToTimeseries.R"

Basic data analysis

Correlation between As Is and Plan Data

Initial analysis involved checking correlation between As Is and Plan data in order to test how exact the planning is. 1. Correlation is a measure of linear relationship between two variables. 2. The Chulwalar department of statistical analysis and forecasting has done a commendable job in developing the Plan Data!

Table 1: Correlation between As and Plan data

type	corr
TotalAsIs-TotalPlan	0.92
EfakAsIs-EfakPlan	0.91
WugeAsIs-WugePlan	0.88

type	corr
TotalEtelAsIs-TotalEtelPlan	0.92
BlueEtelAsIs-BlueEtelPlan	0.80
RedEtelAsIs-RedEtelPlan	0.91
YearAsIs-YearPlan	0.96

The results show a very high planning accuracy.

```
## Call:
## lm(formula = TotalAsIs ~ TotalPlan, data = TotalAsIs)
## Residuals:
##
       Min
                1Q Median
                               3Q
                                      Max
## -770214 -196776
                    26017
                           182579
                                   672705
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 8.959e+04 1.521e+05
                                     0.589
                                              0.558
              9.627e-01 4.959e-02 19.413
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 332600 on 70 degrees of freedom
## Multiple R-squared: 0.8433, Adjusted R-squared: 0.8411
## F-statistic: 376.9 on 1 and 70 DF, p-value: < 2.2e-16
##
## Call:
## tslm(formula = TotalAsIs ~ TotalPlan, data = TotalAsIs)
##
## Residuals:
##
      Min
                1Q Median
                               3Q
                                      Max
## -770214 -196776
                    26017 182579
                                   672705
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 8.959e+04 1.521e+05
                                     0.589
                                              0.558
              9.627e-01 4.959e-02 19.413
## TotalPlan
                                              <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 332600 on 70 degrees of freedom
## Multiple R-squared: 0.8433, Adjusted R-squared: 0.8411
## F-statistic: 376.9 on 1 and 70 DF, p-value: < 2.2e-16
```

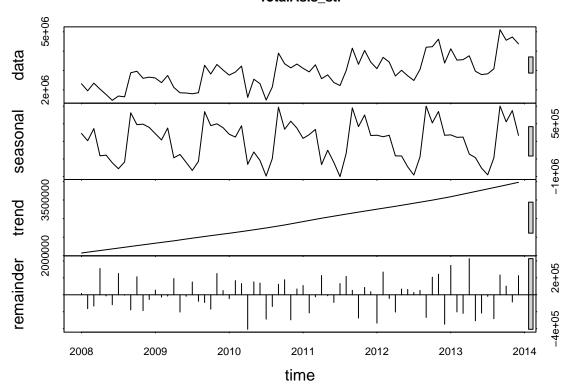
STL function (Seasonal Decomposition of Time Series by LOESS

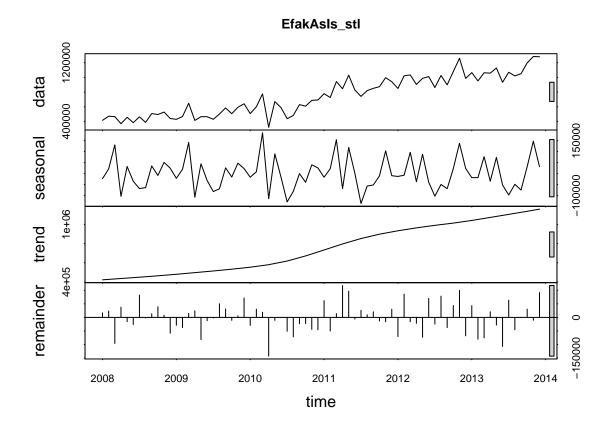
r stl() was used to seperate the trend, seasonality and remainder (remaining coincidential) components from one another.

- 1. The individual time series can be shown graphically and tabularly.
- 2. The trend of the total exports is almost linear.

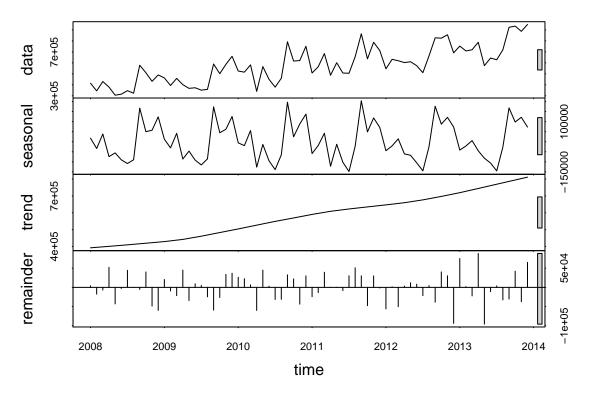
3. A relatively uniform seasonality can be seen.

TotalAsIs_stl

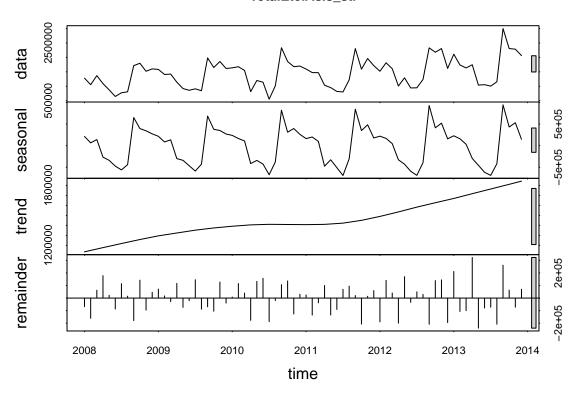




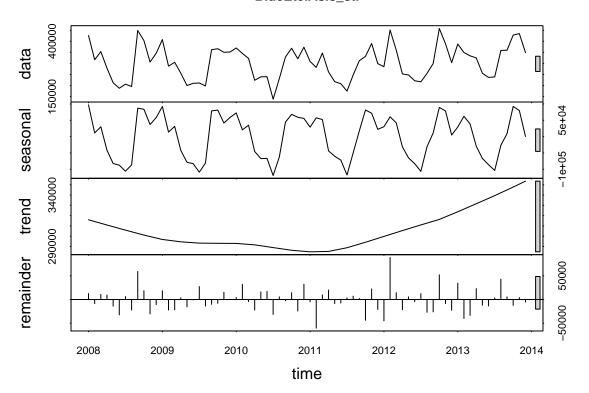
WugeAsIs_stI



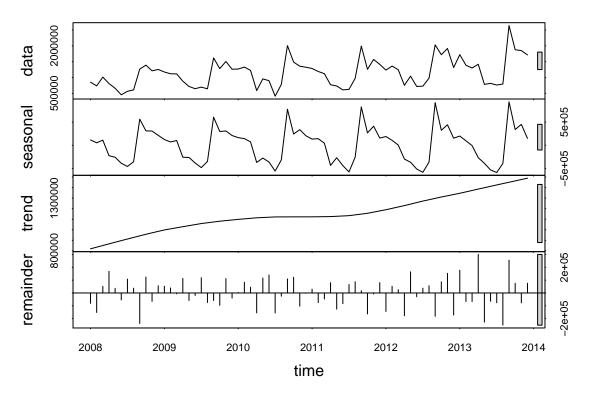
TotalEtelAsIs_stl



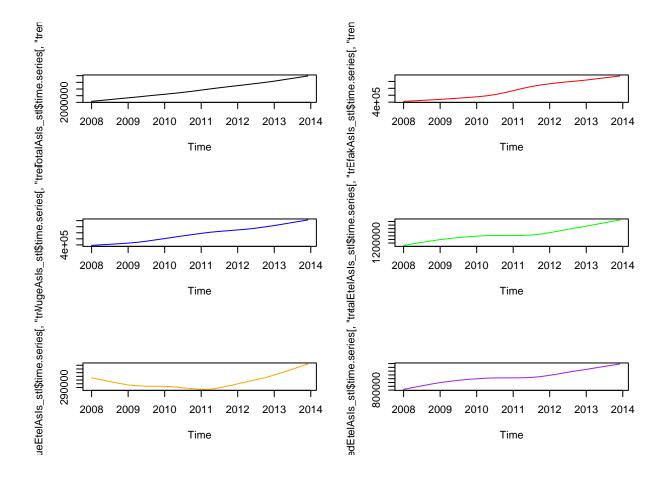
BlueEtelAsIs_stl



RedEtelAsIs_stl

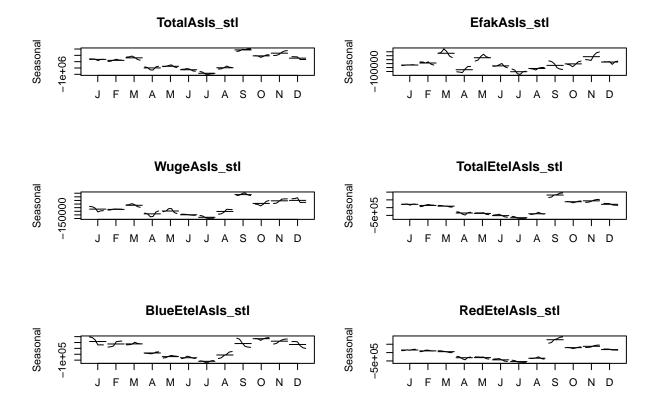


It is interesting to note that the almost linear trend is not seen in the individual segments. The individual trends run partially in opposite directions in the middle of the time scale, which causes the linear trend in the total As Is data.



Modify seasonal component to a monthly base

The modification of the seasonality component can also be changed into a monthly view. It only makes sense to do this if the seasonality componant as the trend looks almost identical and the remainder is then randomly spread.



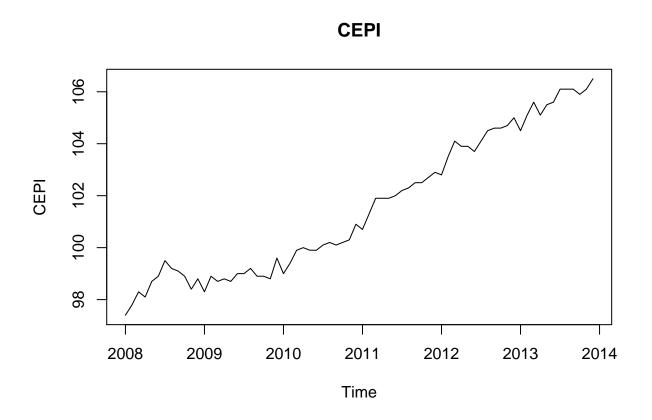
Correlation with external indicators

The indicators are as follows:

- Monthly Change in Export Price Index (CEPI)
- Monthly Satisfaction Index (SI) government based data
- Average monthly temperatures in Chulwalar
- Monthly births in Chulwalar
- Monthly Satisfaction Index (SI) external index
- Yearly Exports from Urbano
- Yearly number of Globalisation Party members in Chulwalar
- Monthly Average Export Price Index for Chulwalar
- Monthly Producer Price Index (PPI) for Etel in Chulwalar
- National Holidays
- Chulwalar Index (Total value of all companies in Chulwalar)
- Monthly Inflation rate in Chulwalar
- Proposed spending for National Holidays
- Influence of National Holiday

The indicators will be converted into individual vectors and subsequently converted into time series. The correlation of the indicators will then be tested against the As Is exports for Chulwalar.

Monthly Change in Export Price Index (CEPI)



```
## [1] 0.663925
```

Monthly Satisfaction Index (SI) government based data

SIGovVector <- c(ImportedIndicators[16:27,2],ImportedIndicators[16:27,3],ImportedIndicators[16:27,4],ImportedIndic

^{## [1] 0.9303543}

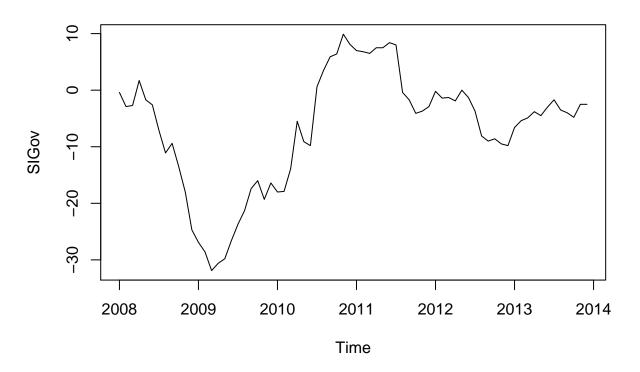
^{## [1] 0.7618551}

^{## [1] 0.339713}

^{## [1] 0.1448837}

^{## [1] 0.3587646}

SIGov



```
cor(TotalAsIs, SIGov)

## [1] 0.2007768

cor(EfakAsIs , SIGov)

## [1] 0.37934

cor(WugeAsIs, SIGov)

## [1] 0.3030266

cor(TotalEtelAsIs, SIGov)

## [1] 0.002556094

cor(BlueEtelAsIs , SIGov)

## [1] -0.04146932

cor(RedEtelAsIs , SIGov)
```

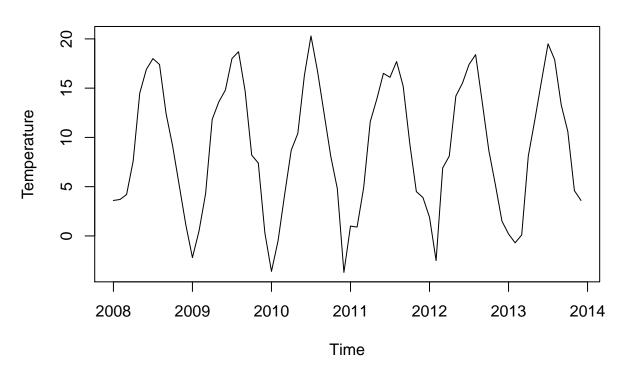
Average monthly temperatures in Chulwalar

[1] 0.009978415

TemperatureVector <- c(ImportedIndicators[30:41,2],ImportedIndicators[30:41,3],ImportedIndicators[30:41
Temperature <- ts(TemperatureVector, start=c(2008,1), end=c(2013,12), frequency=12)

[1] -0.4028941

Temperature

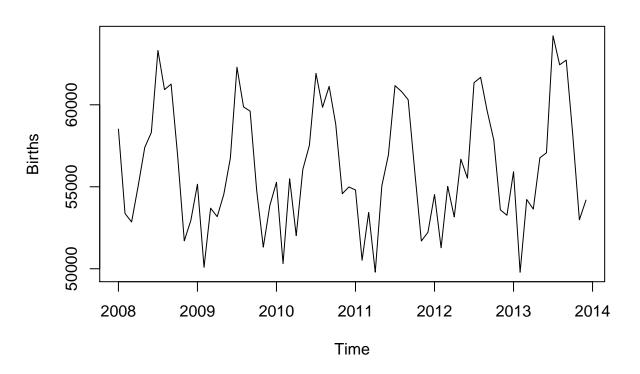


```
cor(TotalAsIs, Temperature)
## [1] -0.3429684
cor(EfakAsIs , Temperature)
## [1] -0.07951179
cor(WugeAsIs, Temperature)
## [1] -0.2045082
cor(TotalEtelAsIs, Temperature)
## [1] -0.453138
cor(BlueEtelAsIs , Temperature)
## [1] -0.6356067
cor(RedEtelAsIs , Temperature)
```

Monthly births in Chulwalar

BirthsVector <- c(ImportedIndicators [44:55,2], ImportedIndicators [44:55,3], ImportedIndicators [44:55,4], ImportedIndicators

Births



```
cor(TotalAsIs, Births)

## [1] -0.1190228

cor(EfakAsIs , Births)

## [1] -0.05802961

cor(WugeAsIs, Births)

## [1] -0.007371339

cor(TotalEtelAsIs, Births)

## [1] -0.1504242

cor(BlueEtelAsIs , Births)

## [1] -0.2812913

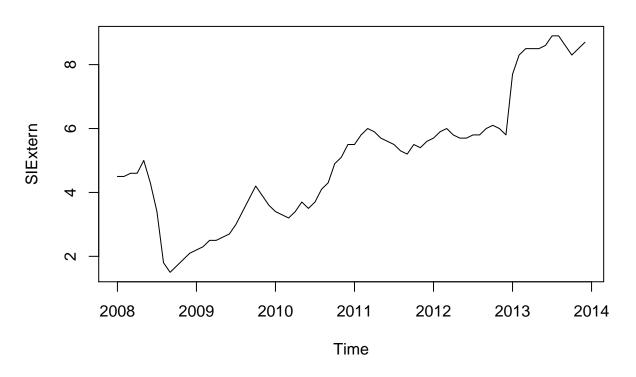
cor(RedEtelAsIs , Births)

## [1] -0.1217222
```

Monthly Satisfaction Index (SI) external index

SIExternVector <- c(ImportedIndicators[58:69,2],ImportedIndicators[58:69,3],ImportedIndicators[58:69,4] SIExtern <- ts(SIExternVector, start=c(2008,1), end=c(2013,12), frequency=12) plot(SIExtern, main="SIExtern")

SIExtern



```
cor(TotalAsIs, SIExtern)

## [1] 0.5883122

cor(EfakAsIs , SIExtern)

## [1] 0.8358147

cor(WugeAsIs, SIExtern)

## [1] 0.6786552

cor(TotalEtelAsIs, SIExtern)

## [1] 0.2865672

cor(BlueEtelAsIs , SIExtern)

## [1] 0.1604768

cor(RedEtelAsIs , SIExtern)

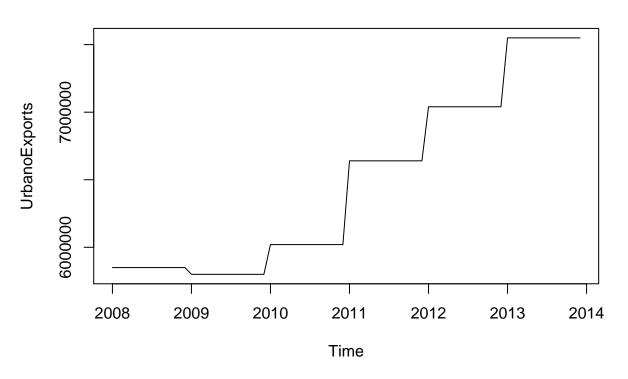
## [1] 0.2960946
```

Yearly exports from Urbano

[1] 0.3309962

UrbanoExportsVector <- c(ImportedIndicators[72:83,2],ImportedIndicators[72:83,3],ImportedIndicators[72:UrbanoExports <- ts(UrbanoExportsVector, start=c(2008,1), end=c(2013,12), frequency=12)
plot(UrbanoExports, main="UrbanoExports")</pre>

UrbanoExports

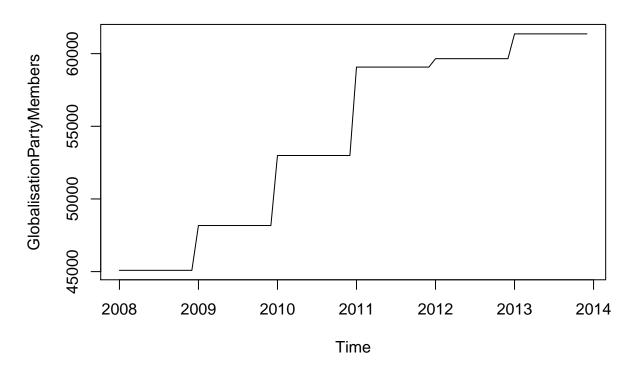


```
cor(TotalAsIs, UrbanoExports)
## [1] 0.638178
cor(EfakAsIs , UrbanoExports)
## [1] 0.9163565
cor(WugeAsIs, UrbanoExports)
## [1] 0.7118468
cor(TotalEtelAsIs, UrbanoExports)
## [1] 0.3182532
cor(BlueEtelAsIs , UrbanoExports)
## [1] 0.1655794
cor(RedEtelAsIs , UrbanoExports)
```

Yearly number of Globalisation Party members in Chulwalar

GlobalisationPartyMembersVector <- c(ImportedIndicators[86:97,2],ImportedIndicators[86:97,3],ImportedIndicators[86

GlobalisationPartyMembers

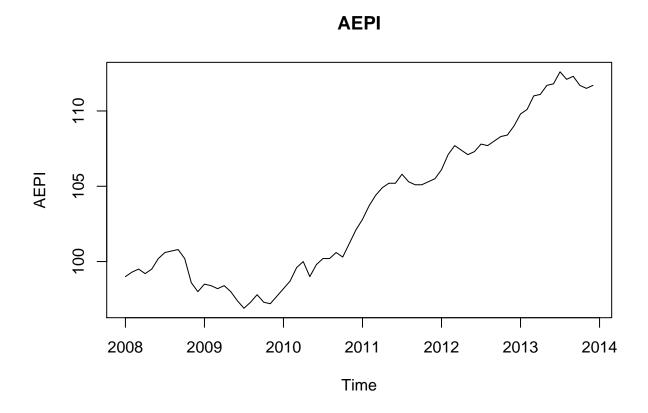


```
cor(TotalAsIs, GlobalisationPartyMembers)
## [1] 0.630084
cor(EfakAsIs , GlobalisationPartyMembers)
## [1] 0.8963942
cor(WugeAsIs, GlobalisationPartyMembers)
## [1] 0.7193864
cor(TotalEtelAsIs, GlobalisationPartyMembers)
## [1] 0.2994635
cor(BlueEtelAsIs , GlobalisationPartyMembers)
## [1] 0.08547266
cor(RedEtelAsIs , GlobalisationPartyMembers)
```

[1] 0.3234832

Monthly Average Export Price Index for Chulwalar

AEPIVector <- c(ImportedIndicators[100:111,2],ImportedIndicators[100:111,3],ImportedIndicators[100:111,4], AEPI <- ts(AEPIVector, start=c(2008,1), end=c(2013,12), frequency=12) plot(AEPI, main="AEPI")



```
cor(TotalAsIs, AEPI)

## [1] 0.625232

cor(EfakAsIs , AEPI)

## [1] 0.9056624

cor(WugeAsIs, AEPI)

## [1] 0.7159733

cor(TotalEtelAsIs, AEPI)

## [1] 0.3035506

cor(BlueEtelAsIs , AEPI)

## [1] 0.1577964

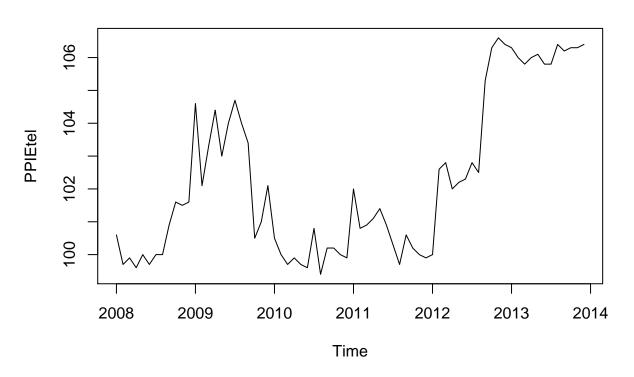
cor(RedEtelAsIs , AEPI)

## [1] 0.3157277
```

Monthly Producer Price Index (PPI) for Etel in Chulwalar

PPIEtelVector <- c(ImportedIndicators[114:125,2],ImportedIndicators[114:125,3],ImportedIndicators[114:1 PPIEtel <- ts(PPIEtelVector, start=c(2008,1), end=c(2013,12), frequency=12) plot(PPIEtel, main="PPIEtel")

PPIEtel



```
cor(TotalAsIs, PPIEtel)

## [1] 0.4836129

cor(EfakAsIs , PPIEtel)

## [1] 0.5865375

cor(WugeAsIs, PPIEtel)

## [1] 0.4920865

cor(TotalEtelAsIs, PPIEtel)

## [1] 0.3374707

cor(BlueEtelAsIs , PPIEtel)

## [1] 0.2445472

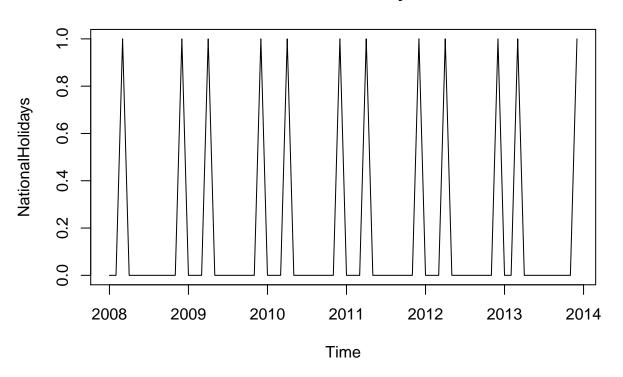
cor(RedEtelAsIs , PPIEtel)

## [1] 0.3391872
```

National Holidays

NationalHolidaysVector <- c(ImportedIndicators[170:181,2],ImportedIndicators[170:181,3],ImportedIndicat NationalHolidays <- ts(NationalHolidaysVector, start=c(2008,1), end=c(2013,12), frequency=12) plot(NationalHolidays, main="NationalHolidays")

NationalHolidays



```
cor(TotalAsIs, NationalHolidays)

## [1] -0.007883708

cor(EfakAsIs , NationalHolidays)

## [1] 0.001235706

cor(WugeAsIs, NationalHolidays)

## [1] 0.06505569

cor(TotalEtelAsIs, NationalHolidays)

## [1] -0.01081446

cor(BlueEtelAsIs , NationalHolidays)

## [1] 0.02903763

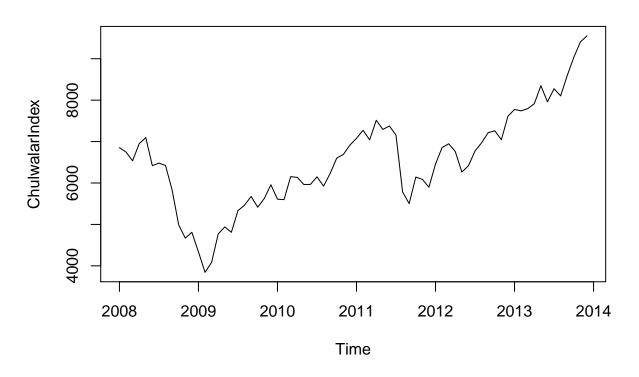
cor(RedEtelAsIs , NationalHolidays)
```

[1] -0.01717636

Chulwalar Index (Total value of all companies in Chulwalar)

ChulwalarIndexVector <- c(ImportedIndicators[128:139,2],ImportedIndicators[128:139,3],ImportedIndicator ChulwalarIndex <- ts(ChulwalarIndexVector, start=c(2008,1), end=c(2013,12), frequency=12) plot(ChulwalarIndex, main="ChulwalarIndex")

ChulwalarIndex

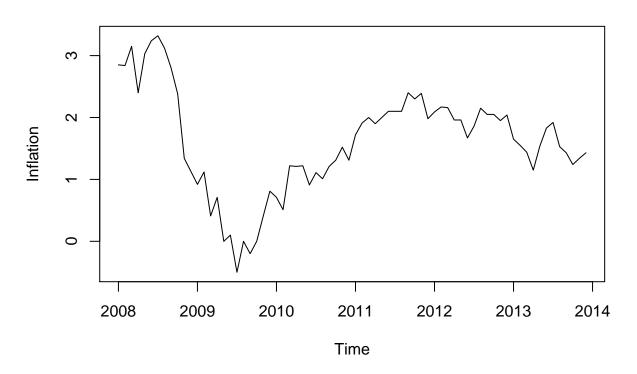


```
cor(TotalAsIs, ChulwalarIndex)
## [1] 0.4837017
cor(EfakAsIs , ChulwalarIndex)
## [1] 0.7129557
cor(WugeAsIs, ChulwalarIndex)
## [1] 0.5721568
cor(TotalEtelAsIs, ChulwalarIndex)
## [1] 0.2209171
cor(BlueEtelAsIs , ChulwalarIndex)
## [1] 0.1469233
cor(RedEtelAsIs , ChulwalarIndex)
## [1] 0.2242922
```

Monthly Inflation rate in Chulwalar

InflationVector <- c(ImportedIndicators[142:153,2],ImportedIndicators[142:153,3],ImportedIndicators[142
Inflation <- ts(InflationVector, start=c(2008,1), end=c(2013,12), frequency=12)
plot(Inflation, main="Inflation")</pre>

Inflation

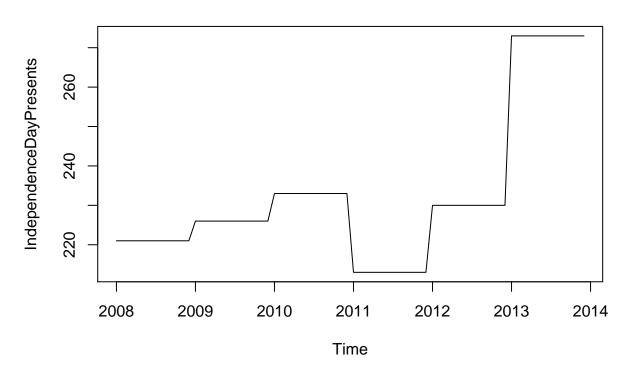


```
cor(TotalAsIs, Inflation)
## [1] 0.002438708
cor(EfakAsIs , Inflation)
## [1] 0.1454134
cor(WugeAsIs, Inflation)
## [1] 0.03191332
cor(TotalEtelAsIs, Inflation)
## [1] -0.08378282
cor(BlueEtelAsIs , Inflation)
## [1] 0.02117817
cor(RedEtelAsIs , Inflation)
## [1] -0.0982151
```

Proposed spending for Independence day presents

IndependenceDayPresentsVector <- c(ImportedIndicators[156:167,2],ImportedIndicators[156:167,3],Imported IndependenceDayPresents <- ts(IndependenceDayPresentsVector, start=c(2008,1), end=c(2013,12), frequency plot(IndependenceDayPresents, main="IndependenceDayPresents")

IndependenceDayPresents



```
cor(TotalAsIs, IndependenceDayPresents)

## [1] 0.4359522

cor(EfakAsIs , IndependenceDayPresents)

## [1] 0.5243145

cor(WugeAsIs, IndependenceDayPresents)

## [1] 0.4892437

cor(TotalEtelAsIs, IndependenceDayPresents)

## [1] 0.2872013

cor(BlueEtelAsIs , IndependenceDayPresents)

## [1] 0.2110373

cor(RedEtelAsIs , IndependenceDayPresents)

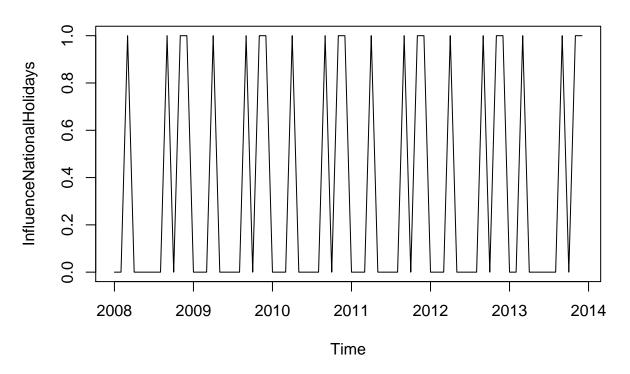
## [1] 0.2881631
```

Influence of National Holidays:

This indicator is an experiment where the influence of National Holidays is extended into the months leading up to the holiday. However later tests show that this indicator is no better for forecasting than the original National Holidays indicator.

InfluenceNationalHolidaysVector <- c(ImportedIndicators[184:195,2],ImportedIndicators[184:195,3],Import InfluenceNationalHolidays <- ts(InfluenceNationalHolidaysVector, start=c(2008,1), end=c(2013,12), frequenceNationalHolidays, main="InfluenceNationalHolidays")

InfluenceNationalHolidays



```
cor(TotalAsIs, InfluenceNationalHolidays)

## [1] 0.3717463

cor(EfakAsIs , InfluenceNationalHolidays)

## [1] 0.09926836

cor(WugeAsIs, InfluenceNationalHolidays)

## [1] 0.3712288

cor(TotalEtelAsIs, InfluenceNationalHolidays)

## [1] 0.4535836

cor(BlueEtelAsIs , InfluenceNationalHolidays)

## [1] 0.2792198
```

```
cor(RedEtelAsIs , InfluenceNationalHolidays)
## [1] 0.4643512
```

Check that the data import has worked

```
str(CEPIVector)
## num [1:72] 97.4 97.8 98.3 98.1 98.7 98.9 99.5 99.2 99.1 98.9 ...
str(SIGovVector)
## num [1:72] -0.4 -2.9 -2.7 1.7 -1.7 -2.6 -7.1 -11.1 -9.4 -13.5 ...
str(TemperatureVector)
## num [1:72] 3.6 3.7 4.2 7.6 14.5 16.9 18 17.4 12.4 9.1 ...
str(BirthsVector)
## num [1:72] 58519 53370 52852 55048 57398 ...
str(SIExternVector)
## num [1:72] 4.5 4.5 4.6 4.6 5 4.3 3.4 1.8 1.5 1.7 ...
str(UrbanoExportsVector)
## num [1:72] 5850000 5850000 5850000 5850000 5850000 5850000 5850000 5850000 5850000 ...
str(GlobalisationPartyMembersVector)
## num [1:72] 45089 45089 45089 45089 ...
str(AEPIVector)
## num [1:72] 99 99.3 99.5 99.2 99.5 ...
str(PPIEtelVector)
## num [1:72] 100.6 99.7 99.9 99.6 100 ...
str(NationalHolidaysVector)
## num [1:72] 0 0 1 0 0 0 0 0 0 0 ...
str(ChulwalarIndexVector)
## num [1:72] 6852 6748 6535 6949 7097 ...
str(InflationVector)
## num [1:72] 2.85 2.84 3.15 2.4 3.03 3.24 3.32 3.12 2.8 2.38 ...
str(IndependenceDayPresentsVector)
```

Forecasting models with smoothing and related approaches

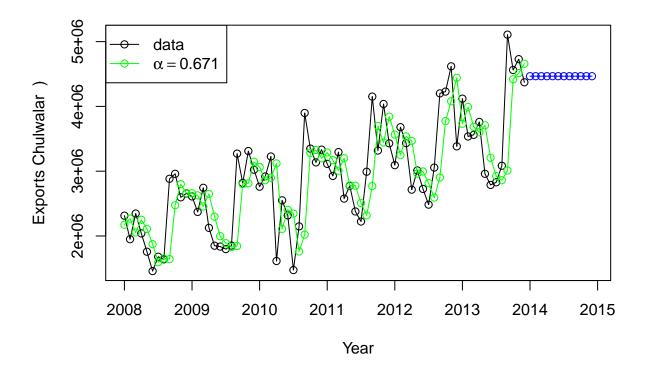
Exponential Smoothing uses past values to calculate a forecast. The strength with which each value influences the forecast is weakened with help of a smoothing parameter. Thus we are dealing with a weighted average, whose values fade out the longer ago they were in the past.

The Akaike's Information Criterion (AIC/AICc) or the Bayesian Information Criterion (BIC) should be at minimum.

Simple expontential smoothing

```
Model_ses <- ses(TotalAsIs, h=12)</pre>
summary(Model ses)
##
## Forecast method: Simple exponential smoothing
##
## Model Information:
## Simple exponential smoothing
##
## Call:
##
    ses(x = TotalAsIs, h = 12)
##
##
     Smoothing parameters:
##
       alpha = 0.671
##
##
     Initial states:
       1 = 2173226.7433
##
##
##
     sigma:
             609507
##
##
        AIC
                AICc
                           BIC
  2230.058 2230.232 2234.612
##
## Error measures:
##
                       ME
                            RMSE
                                      MAE
                                                 MPE
                                                         MAPE
                                                                   MASE
## Training set 47469.84 609507 429997.1 -1.511008 15.02336 1.172074
##
## Training set 0.02384493
##
## Forecasts:
##
            Point Forecast
                              Lo 80
                                      Hi 80
                                              Lo 95
## Jan 2014
                   4466448 3685333 5247562 3271836 5661059
## Feb 2014
                   4466448 3525801 5407094 3027853 5905042
## Mar 2014
                   4466448 3389650 5543245 2819628 6113267
## Apr 2014
                   4466448 3268880 5664015 2634926 6297969
## May 2014
                   4466448 3159220 5773675 2467215 6465680
## Jun 2014
                   4466448 3058072 5874823 2312524 6620371
## Jul 2014
                   4466448 2963718 5969177 2168221 6764674
                   4466448 2874947 6057948 2032458 6900437
## Aug 2014
## Sep 2014
                   4466448 2790873 6142022 1903878 7029017
## Oct 2014
                   4466448 2710821 6222074 1781448 7151447
## Nov 2014
                   4466448 2634263 6298632 1664363 7268532
```

```
OverallSummary <- GetForecastStats(Model_ses)
plot(Model_ses, plot.conf=FALSE, ylab="Exports Chulwalar")", xlab="Year", main="", fcol="white", type=
lines(fitted(Model_ses), col="green", type="o")
lines(Model_ses$mean, col="blue", type="o")
legend("topleft",lty=1, col=c(1,"green"), c("data", expression(alpha == 0.671)),pch=1)</pre>
```



Holt's linear trend method

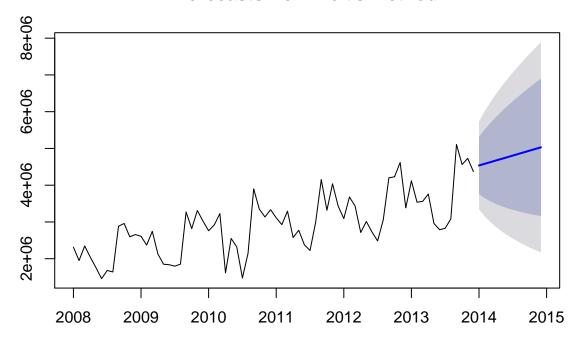
Holt added to the model in order to forecast using trends as well. For this it is necessary to add a beta, which determines the trend. If neither alpha nor beta is stated, both parameters will be optimised using ets(). The trend is exponential if the intercepts(level) and the gradient (slope) are multiplied with eachother. The values are worse. As the Beta was very low in the optimisation, the forecast is very similar to the ses() model.

```
Model_holt_1 <- holt(TotalAsIs,h=12)
summary(Model_holt_1)</pre>
```

```
##
## Forecast method: Holt's method
##
## Model Information:
## Holt's method
##
## Call:
## holt(x = TotalAsIs, h = 12)
```

```
##
##
     Smoothing parameters:
      alpha = 0.6571
##
##
       beta = 1e-04
##
##
     Initial states:
##
      1 = 2040390.7764
       b = 45050.7514
##
##
##
     sigma: 608119.1
##
##
        AIC
                AICc
## 2233.730 2234.327 2242.837
##
## Error measures:
##
                       ME
                              RMSE
                                    MAE
                                                  MPE
                                                           MAPE
                                                                     MASE
## Training set -16586.9 608119.1 441110.7 -3.88925 15.75307 1.202367
                       ACF1
## Training set 0.03462672
##
## Forecasts:
          Point Forecast Lo 80 Hi 80 Lo 95 Hi 95
             4536367 3757031 5315703 3344475 5728259
## Jan 2014
                  4581298 3648703 5513894 3155016 6007580
## Feb 2014
## Mar 2014
                  4626230 3562188 5690271 2998918 6253541
## Apr 2014
                  4671161 3490181 5852141 2865008 6477314
## May 2014
                   4716092 3428721 6003463 2747228 6684956
## Jun 2014
                   4761024 3375378 6146669 2641862 6880185
## Jul 2014
                   4805955 3328531 6283379 2546429 7065480
                4850886 3287035 6414738 2459182 7242591
4895818 3250047 6541588 2378829 7412807
4940749 3216925 6664573 2304387 7577111
## Aug 2014
## Sep 2014
## Oct 2014
## Nov 2014
                  4985680 3187164 6784196 2235088 7736273
                   5030612 3160363 6900860 2170314 7890909
## Dec 2014
plot(Model_holt_1)
```

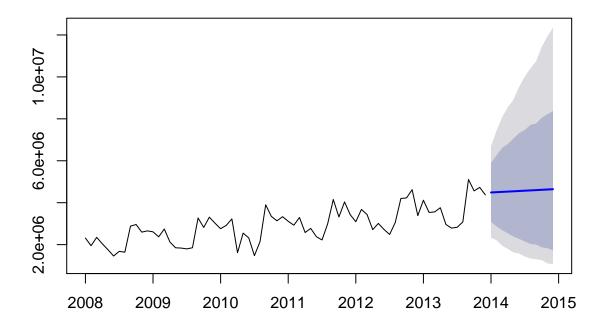
Forecasts from Holt's method



```
# expoential trend
Model_holt_2<- holt(TotalAsIs, exponential=TRUE,h=12)</pre>
summary(Model_holt_2)
##
## Forecast method: Holt's method with exponential trend
##
## Model Information:
## Holt's method with exponential trend
##
## Call:
    holt(x = TotalAsIs, h = 12, exponential = TRUE)
##
##
     Smoothing parameters:
##
       alpha = 0.6637
##
       beta = 1e-04
##
##
##
     Initial states:
       1 = 2041538.9468
##
##
       b = 1.0029
##
##
     sigma: 0.2438
##
##
        AIC
                AICc
                           BIC
## 2251.010 2251.607 2260.116
##
```

```
## Error measures:
##
                      ME
                             RMSE
                                        MAE
                                                  MPE
                                                          MAPE
                                                                   MASE
  Training set 37825.61 609787.5 433018.9 -1.838214 15.18487 1.180311
                      ACF1
## Training set 0.02918287
##
## Forecasts:
##
            Point Forecast
                             Lo 80
                                     Hi 80
                                              Lo 95
                                                       Hi 95
## Jan 2014
                   4488281 3088776 5895347 2332202
                                                     6686602
## Feb 2014
                   4502175 2865852 6263480 2205796
                                                     7452866
## Mar 2014
                   4516113 2691319 6619824 1941873
                                                     8087524
## Apr 2014
                   4530094 2540182 6802695 1795055
                                                     8561230
## May 2014
                   4544118 2381944 7067397 1625428
                                                     8924997
## Jun 2014
                   4558186 2276516 7316584 1579874
## Jul 2014
                   4572297 2149404 7470633 1430581 10018701
## Aug 2014
                   4586452 2037643 7711148 1337859 10406511
## Sep 2014
                   4600650 2006342 7776040 1302428 10741609
## Oct 2014
                   4614893 1872142 8051774 1261109 11434191
## Nov 2014
                   4629180 1834620 8218030 1106433 11928018
## Dec 2014
                   4643510 1729264 8373103 1071226 12348352
plot(Model_holt_2)
```

Forecasts from Holt's method with exponential trend



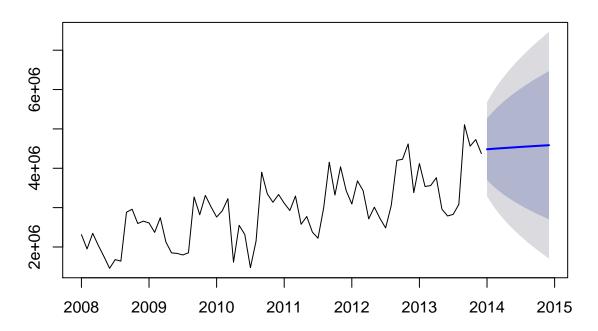
Dampened trends

As such simple trends tend to forecast the future to positively, we have added a dampener. This also works for exponential trends. We also plot the level and slope individually for each model.

```
Model_holt_3 <- holt(TotalAsIs, damped=TRUE,h=12)
summary(Model_holt_3)</pre>
```

```
##
## Forecast method: Damped Holt's method
## Model Information:
## Damped Holt's method
##
## Call:
   holt(x = TotalAsIs, h = 12, damped = TRUE)
##
##
##
     Smoothing parameters:
       alpha = 0.6613
##
       beta = 2e-04
##
       phi
##
             = 0.98
##
##
     Initial states:
##
       1 = 2040392.5761
##
       b = 45053.25
##
##
     sigma:
             608787.2
##
##
        AIC
                AICc
                           BIC
## 2235.888 2236.797 2247.272
##
## Error measures:
##
                              RMSE
                                        MAE
                                                  MPE
                                                           MAPE
                                                                    MASE
                      ME
## Training set 15578.94 608787.2 436909.7 -2.797612 15.46526 1.190916
##
                       ACF1
## Training set 0.03351419
##
## Forecasts:
##
            Point Forecast
                              Lo 80
                                      Hi 80
                                              Lo 95
## Jan 2014
                   4483618 3703426 5263811 3290417 5676819
## Feb 2014
                   4493914 3558436 5429391 3063224 5924603
## Mar 2014
                   4504003 3435520 5572486 2869899 6138107
## Apr 2014
                   4513891 3327168 5700614 2698955 6328827
## May 2014
                   4523581 3229332 5817829 2544198 6502963
## Jun 2014
                   4533077 3139534 5926619 2401837 6664316
## Jul 2014
                   4542383 3056128 6028638 2269352 6815413
## Aug 2014
                   4551503 2977955 6125051 2144969 6958036
## Sep 2014
                   4560440 2904162 6216719 2027381 7093499
## Oct 2014
                   4569199 2834101 6304298 1915595 7222803
## Nov 2014
                   4577783 2767264 6388301 1808834 7346732
## Dec 2014
                   4586195 2703249 6469141 1706477 7465913
```

Forecasts from Damped Holt's method

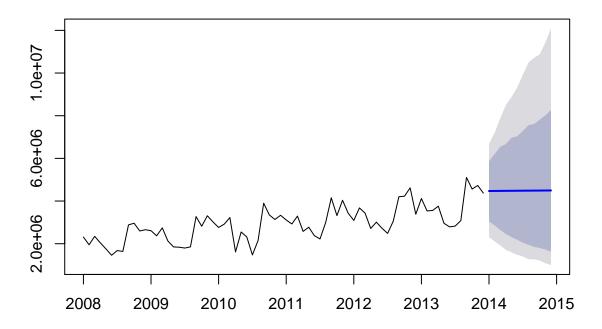


```
Model_holt_4 <- holt(TotalAsIs, exponential=TRUE, damped=TRUE, h=12)
summary(Model_holt_4)</pre>
```

```
##
## Forecast method: Damped Holt's method with exponential trend
## Model Information:
## Damped Holt's method with exponential trend
##
    holt(x = TotalAsIs, h = 12, damped = TRUE, exponential = TRUE)
##
##
##
     Smoothing parameters:
##
       alpha = 0.6679
       beta = 1e-04
##
             = 0.9799
##
       phi
##
##
     Initial states:
##
       1 = 2041541.9705
       b = 1.0019
##
##
##
     sigma: 0.2449
##
##
        AIC
                AICc
                          BIC
```

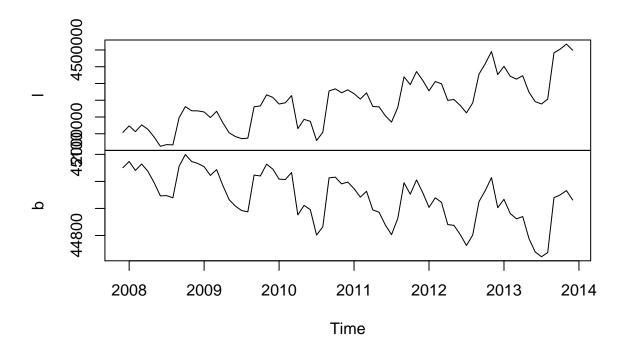
```
## 2253.216 2254.125 2264.600
##
## Error measures:
                                                                   MASE
##
                      ME
                             RMSE
                                        MAE
                                                  MPE
                                                          MAPE
## Training set 46119.56 609906.7 432069.1 -1.549114 15.11987 1.177722
##
                     ACF1
## Training set 0.0254941
##
## Forecasts:
##
            Point Forecast
                             Lo 80
                                     Hi 80
                                              Lo 95
                                                       Hi 95
## Jan 2014
                  4470648 3040929 5864323 2314513
                                                     6675597
## Feb 2014
                   4473164 2863707 6203336 2111849
                                                     7199488
## Mar 2014
                   4475630 2642712 6541923 1920488
                                                     7878829
## Apr 2014
                   4478047 2454945 6672650 1708073
                                                     8502659
## May 2014
                   4480418 2310553 6966096 1596736
                                                     8877890
## Jun 2014
                   4482742 2184766 7036856 1479052
                                                     9313377
## Jul 2014
                   4485020 2049701 7280710 1405349
                                                     9912633
## Aug 2014
                   4487253 1951122 7555157 1276735 10487697
## Sep 2014
                   4489443 1855882 7615298 1266672 10713430
## Oct 2014
                   4491589 1801385 7811538 1213268 10875295
## Nov 2014
                   4493694 1727609 8016311 1084686 11423677
## Dec 2014
                   4495757 1631264 8267988 1003413 12085156
plot(Model_holt_4)
```

Forecasts from Damped Holt's method with exponential trend



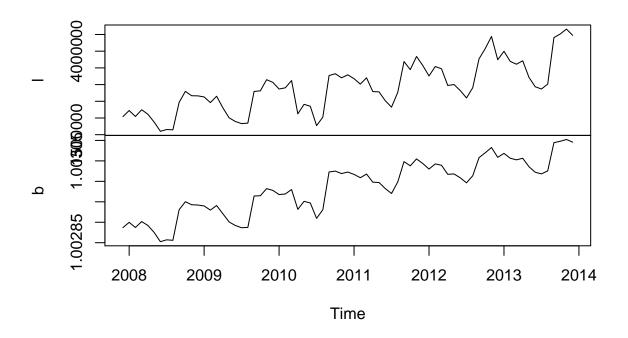
level and slope can be plotted individually for each model.
plot(Model_holt_1\$model\$state)

Model_holt_1\$model\$state



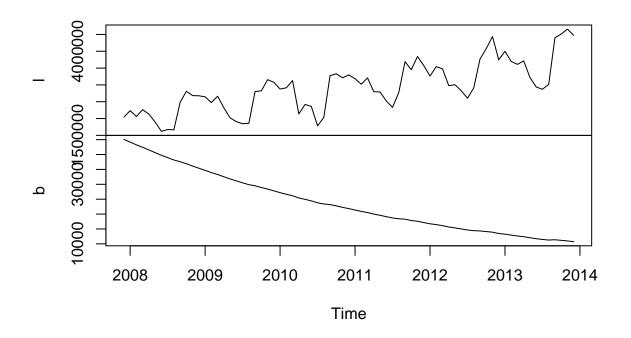
plot(Model_holt_2\$model\$state)

Model_holt_2\$model\$state



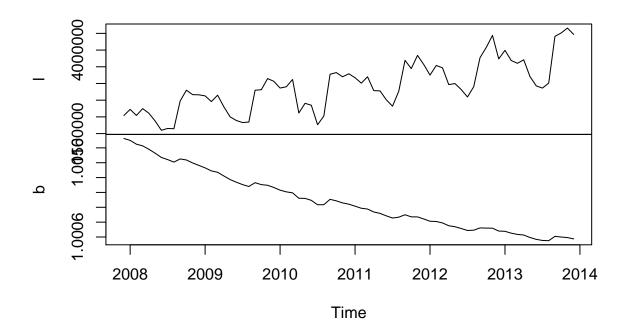
plot(Model_holt_3\$model\$state)

Model_holt_3\$model\$state

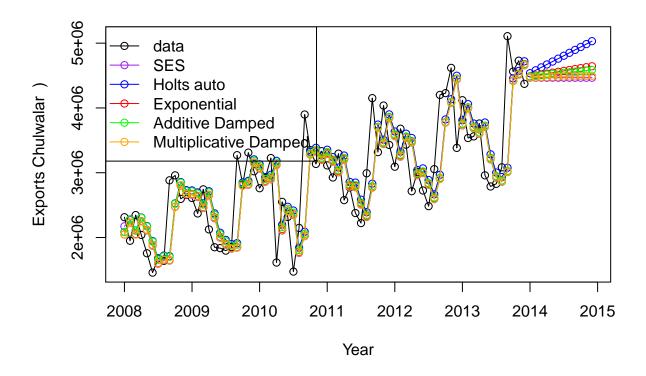


plot(Model_holt_4\$model\$state)

Model holt 4\$model\$state



```
plot(Model_holt_1, plot.conf=FALSE, ylab="Exports Chulwalar )", xlab="Year", main="", fcol="white", tylines(fitted(Model_ses), col="purple", type="o")
lines(fitted(Model_holt_1), col="blue", type="o")
lines(fitted(Model_holt_2), col="red", type="o")
lines(fitted(Model_holt_3), col="green", type="o")
lines(fitted(Model_holt_4), col="orange", type="o")
lines(Model_ses$mean, col="purple", type="o")
lines(Model_holt_1$mean, col="blue", type="o")
lines(Model_holt_2$mean, col="red", type="o")
lines(Model_holt_3$mean, col="green", type="o")
lines(Model_holt_4$mean, col="orange", type="o")
legend("topleft",lty=1, col=c(1,"purple","blue","red","green","orange"), c("data", "SES","Holts auto",
```



Holt-Winter's seasonal method

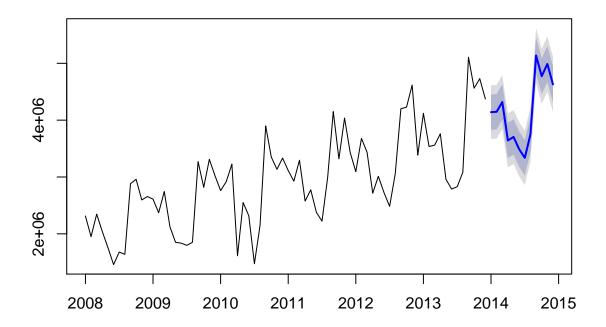
Holt and Winters have expanded Holt's model further to include the seasonality aspect. The parameter gamma, which is for smoothing the seasonality, was added to achieve this. The values are better than the models without seasonality. This is logical, since the data is strongly influenced by seasonality. In the following model, none of the parameters are given so that they will be optimised automatically. There are two models: one using an additive error model method and one using a multiplicative error model. The additive model gives slightly better results than the multiplicative model.

```
Model_hw_1 <- hw(TotalAsIs ,seasonal="additive",h=12)
summary(Model_hw_1)</pre>
```

```
##
## Forecast method: Holt-Winters' additive method
##
## Model Information:
##
   Holt-Winters' additive method
##
##
    hw(x = TotalAsIs, h = 12, seasonal = "additive")
##
##
##
     Smoothing parameters:
##
       alpha = 0.0087
       beta = 0.0087
##
##
       gamma = 1e-04
##
```

```
##
        Initial states:
##
          1 = 2047375.0884
           b = 22509.7631
##
           s=259168.3 654942.6 474529.8 876025.2 -475155 -852844
##
##
                      -664662.5 -412596.7 -438677.3 273215 138077.9 167976.7
##
      sigma: 241685
##
##
##
            AIC
                      AICc BIC
## 2124.856 2134.747 2161.283
## Error measures:
                                 ME RMSE MAE MPE MAPE
                                                                                                        MASE
## Training set 21615.43 241685 202218.5 -0.08252109 7.329458 0.5512016
                                  ACF1
## Training set -0.2819072
##
## Forecasts:
        Point Forecast Lo 80 Hi 80 Lo 95 Hi 95
## Jan 2014 4141204 3831472 4450936 3667510 4614898
## Feb 2014
                           4147309 3837472 4457147 3673453 4621165
## Mar 2014
                           4318537 4008512 4628563 3844394 4792680
## Mar 2014 4318537 4008512 4628563 3844394 4792680
## Apr 2014 3642744 3332425 3953063 3168153 4117335
## May 2014 3704865 3394124 4015605 3229628 4180102
## Jun 2014 3488859 3177546 3800173 3012746 3964973
## Jul 2014 3336738 3024677 3648799 2859482 3813994
## Aug 2014 3750478 3437474 4063482 3271780 4229176
## Sep 2014 5137771 4823607 5451935 4657298 5618244
## Oct 2014 4772337 4456775 5087900 4289726 5254949
## Nov 2014 4988809 4671591 5306028 4503665 5473953
## Dec 2014 4629097 4309943 4948252 4140992 5117202
plot(Model_hw_1)
```

Forecasts from Holt-Winters' additive method

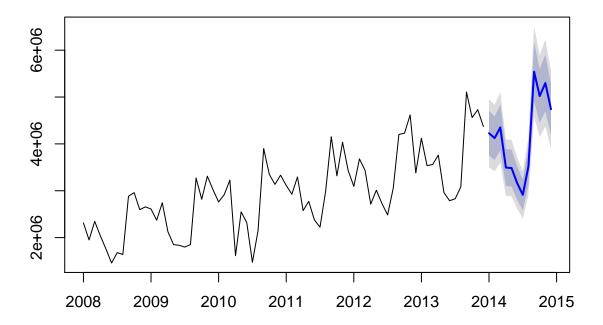


```
Model_hw_2 <- hw(TotalAsIs ,seasonal="multiplicative",h=12)
summary(Model_hw_2)</pre>
```

```
##
## Forecast method: Holt-Winters' multiplicative method
##
## Model Information:
## Holt-Winters' multiplicative method
##
## Call:
    hw(x = TotalAsIs, h = 12, seasonal = "multiplicative")
##
##
##
     Smoothing parameters:
##
       alpha = 0.025
       beta = 0.0062
##
##
       gamma = 1e-04
##
##
     Initial states:
##
       1 = 2026247.531
       b = 25395.1259
##
##
       s=1.0933 1.232 1.1763 1.3086 0.8384 0.699
              0.7653 0.8502 0.8596 1.0793 1.0316 1.0665
##
##
     sigma: 0.0877
##
##
                          BIC
##
        AIC
                AICc
```

```
## 2128.303 2138.194 2164.729
##
## Error measures:
##
                      ME
                             RMSE
                                        MAE
                                                   MPE
                                                           MAPE
                                                                     MASE
## Training set 17434.11 235296.6 191805.3 -0.3292809 7.213472 0.5228175
                      ACF1
##
## Training set -0.3514421
##
## Forecasts:
##
            Point Forecast
                             Lo 80
                                     Hi 80
                                              Lo 95
                   4226941 3751624 4702258 3500006 4953876
## Jan 2014
## Feb 2014
                   4123665 3659738 4587591 3414151 4833179
## Mar 2014
                   4350808 3860995 4840620 3601704 5099911
## Apr 2014
                   3494208 3100476 3887940 2892046 4096370
## May 2014
                   3484738 3091618 3877858 2883513 4085963
## Jun 2014
                   3162774 2805463 3520085 2616314 3709234
## Jul 2014
                   2912399 2582802 3241996 2408324 3416474
## Aug 2014
                   3521645 3122278 3921013 2910865 4132425
## Sep 2014
                   5540988 4911109 6170867 4577671 6504304
## Oct 2014
                   5020487 4448200 5592775 4145249 5895725
## Nov 2014
                   5299729 4693715 5905743 4372911 6226547
## Dec 2014
                   4740169 4196230 5284108 3908286 5572052
plot(Model_hw_2)
```

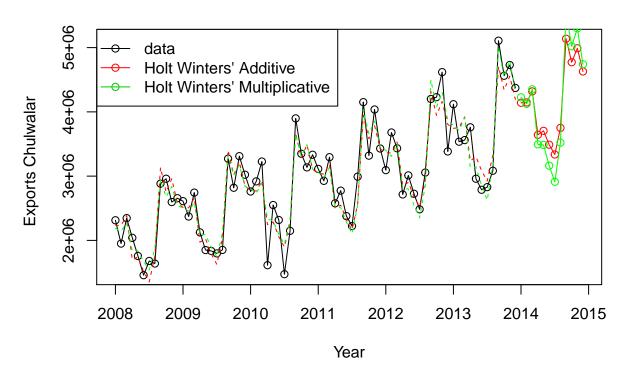
Forecasts from Holt-Winters' multiplicative method



plot(Model_hw_1, ylab="Exports Chulwalar ", plot.conf=FALSE, type="o", fcol="white", xlab="Year")
lines(fitted(Model_hw_1), col="red", lty=2)

```
lines(fitted(Model_hw_2), col="green", lty=2)
lines(Model_hw_1$mean, type="o", col="red")
lines(Model_hw_2$mean, type="o", col="green")
legend("topleft",lty=1, pch=1, col=1:3, c("data","Holt Winters' Additive","Holt Winters' Multiplicative
```

Forecasts from Holt-Winters' additive method



```
# In order to use the results later, they need to be converted into point forcasts.
Model_hw_1_df <-as.data.frame(Model_hw_1)</pre>
Model_hw_1_PointForecast <- ts(Model_hw_1_df$"Point Forecast", start=c(2014,1), end=c(2014,12), frequen
Model_hw_1_PointForecast
##
            Jan
                    Feb
                             Mar
                                             May
                                                      Jun
                                                              Jul
                                     Apr
                                                                      Aug
## 2014 4141204 4147309 4318537 3642744 3704865 3488859 3336738 3750478
##
                    Oct
                             Nov
                                     Dec
            Sep
## 2014 5137771 4772337 4988809 4629097
Model_hw_2_df <-as.data.frame(Model_hw_2)</pre>
Model_hw_2_PointForecast <- ts(Model_hw_2_df$"Point Forecast", start=c(2014,1), end=c(2014,12), frequen
Model_hw_2_PointForecast
##
            Jan
                    Feb
                             Mar
                                                      Jun
                                                              Jul
                                     Apr
                                             May
                                                                      Aug
## 2014 4226941 4123665 4350808 3494208 3484738 3162774 2912399 3521645
##
            Sep
                    Oct
                             Nov
                                     Dec
## 2014 5540988 5020487 5299729 4740169
# Output instruction for the data export of the results for further use in Excel.
#write.csv(Model hw 1 PointForecast, file='Model hw 1 PointForecast.csv')
#write.csv(Model_hw_2_PointForecast,file='Model_hw_2_PointForecast.csv')
```

Conclusion

- The ETS model was prefered over the ARIMA Model. In one sample ETS model, the Mean Absolute Squared Error of .55 was prefered 15 differnt ARIMA models with values greater than 1.0. ETS ME of 21,588 was prefered over wide ranging values of -18,789 to 178,628. Based on the review of the data, and the type of data being explored: Error, Trend, Seasonal algorithm "ETS AAA" is the preferred method over autoregressive integrated moving average "ARIMA". ARIMA is based on assumptions that residuals are uncorrelated and normally distributed. If this doesn't occur, then forecast intervals are incorrect. "ETS AAA" doesn't face the same limitations of looking at correlations in data, linearity and stationarity. Also ETS provides an automatic way of selecting the best method. ETS MASE of .55 provides a better value of greater than 0 but less than one.
- Reviewing the different model, to define the best fit is the model that proves the best prediction of error, robust to outliers, good indicator of central tendency and provides the best measure of goodness is the best fit.
- Holt's-Winters multiplicative method of MASE ".52", ME 17434.1, and RMSE 241,685 was prefered over other forecast models. When reviewing the different forecast models the root mean square error provided the best indicator for accurate forecasting. Taking into account seasonal fluctuations in the data was important during this case study. Lastly, when comparing "total-as-is" plan to the "total-plan" using linear regression model and time series models provided a better understanging of regression correlation and accuracy. The best fit for forecast is the model that provides the best time series review for your given data and the predication of bias and error in the data.
- All of the models are equally good when considering the specific data. Based on observation and analysis
 of the data, any model that provides trend analyses, seasonal interpretation (additive/multiplicative)
 and greater interpretation of potential error is the one chosen. The model that produces an accurate
 forecast is a model that contains a low U1 statistic. Important to consider Mean error values as well as
 taking into account a full range of values in a statistic output

Recommendation to Chulwalr Prime Minister:

When reviewing the different plots between efak, Wuge, and Etel. The primary export recommended would be Efak. It shows a strong linear progression from 2008 and is resistant to large swings in seasonal, export, and social holidays.