



Double Learning and TD Methods

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Re-thinking for the double learning concept



- Motivation
- Related work
- Simulation:
 - Implementing the Double Sarsa, Expected Sarsa, Double Expected Sarsa, and Two Step Sarsa.

Motivation



- Why we need double Q learning [1]
- Max operator will cause the positive bias
- In Q learning: Target policy is the greedy policy
- In SARSA: ϵ -greedy
- Maximization bias: maximum of the estimated values is larger than the maximum of the true values:
- Eg: for state s with many action a , true values for $q(s, a)$ are all zero, but the estimated values: some are negative and some are positive

Double Q Learning



- Problem source: We use the same samples to determine the maximization action and determine the value

$$Q_{t+1}(s_t, a_t) = Q_t(s_t, a_t) + \alpha_t(s_t, a_t) \left(r_t + \gamma \max_a Q_t(s_{t+1}, a) - Q_t(s_t, a_t) \right) .$$

- Potential solution: Divide the samples to two sets, and learn two estimates
- Core idea: Two estimators: A, and B

Double Q Learning



■ Discussion for Lemma 1:

Lemma 1. Let $X = \{X_1, \dots, X_M\}$ be a set of random variables and let $\mu^A = \{\mu_1^A, \dots, \mu_M^A\}$ and $\mu^B = \{\mu_1^B, \dots, \mu_M^B\}$ be two sets of unbiased estimators such that $E\{\mu_i^A\} = E\{\mu_i^B\} = E\{X_i\}$, for all i . Let $\mathcal{M} \stackrel{\text{def}}{=} \{j \mid E\{X_j\} = \max_i E\{X_i\}\}$ be the set of elements that maximize the expected values. Let a^* be an element that maximizes μ^A : $\mu_{a^*}^A = \max_i \mu_i^A$. Then $E\{\mu_{a^*}^B\} = E\{X_{a^*}\} \leq \max_i E\{X_i\}$. Furthermore, the inequality is strict if and only if $P(a^* \notin \mathcal{M}) > 0$.

Proof. Assume $a^* \in \mathcal{M}$. Then $E\{\mu_{a^*}^B\} = E\{X_{a^*}\} \stackrel{\text{def}}{=} \max_i E\{X_i\}$. Now assume $a^* \notin \mathcal{M}$ and choose $j \in \mathcal{M}$. Then $E\{\mu_{a^*}^B\} = E\{X_{a^*}\} < E\{X_j\} \stackrel{\text{def}}{=} \max_i E\{X_i\}$. These two possibilities are mutually exclusive, so the combined expectation can be expressed as

$$\begin{aligned} E\{\mu_{a^*}^B\} &= P(a^* \in \mathcal{M})E\{\mu_{a^*}^B \mid a^* \in \mathcal{M}\} + P(a^* \notin \mathcal{M})E\{\mu_{a^*}^B \mid a^* \notin \mathcal{M}\} \\ &= P(a^* \in \mathcal{M}) \max_i E\{X_i\} + P(a^* \notin \mathcal{M})E\{\mu_{a^*}^B \mid a^* \notin \mathcal{M}\} \\ &\leq P(a^* \in \mathcal{M}) \max_i E\{X_i\} + P(a^* \notin \mathcal{M}) \max_i E\{X_i\} = \max_i E\{X_i\} , \end{aligned}$$

Double Q Learning^[1]



■ Pseudo code:

Algorithm 1 Double Q-learning

```
1: Initialize  $Q^A, Q^B, s$ 
2: repeat
3:   Choose  $a$ , based on  $Q^A(s, \cdot)$  and  $Q^B(s, \cdot)$ , observe  $r, s'$ 
4:   Choose (e.g. random) either UPDATE(A) or UPDATE(B)
5:   if UPDATE(A) then
6:     Define  $a^* = \arg \max_a Q^A(s', a)$ 
7:      $Q^A(s, a) \leftarrow Q^A(s, a) + \alpha(s, a) (r + \gamma Q^B(s', a^*) - Q^A(s, a))$ 
8:   else if UPDATE(B) then
9:     Define  $b^* = \arg \max_a Q^B(s', a)$ 
10:     $Q^B(s, a) \leftarrow Q^B(s, a) + \alpha(s, a) (r + \gamma Q^A(s', b^*) - Q^B(s, a))$ 
11:   end if
12:    $s \leftarrow s'$ 
13: until end
```

Related work

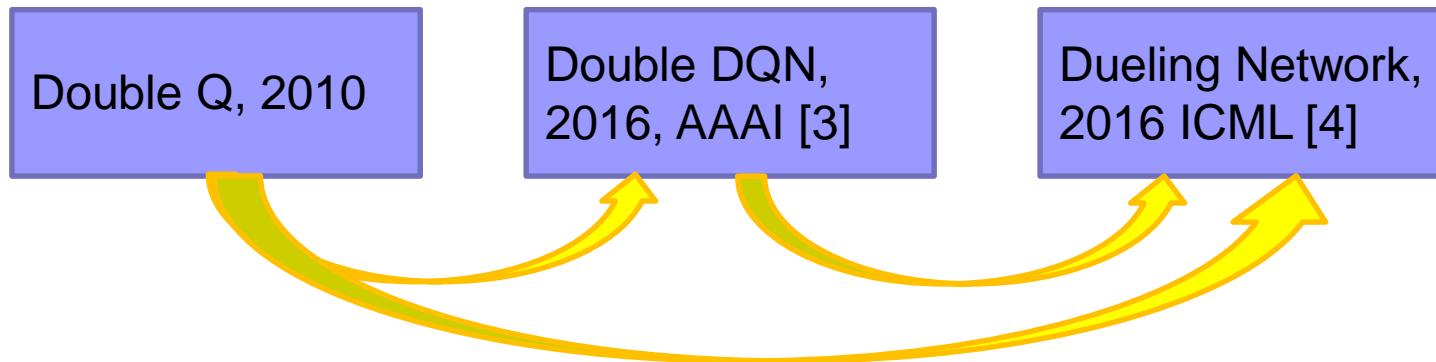


- Potential work mentioned in the paper:
 - Whether we can an unbiased off-policy RL algorithm without high variance
 - Implement double q learning idea for other Q learning extension algorithms: Delayed Q, Fitted Q Iteration
 - Extending the double learning concepts: Double Sarsa, and Double Expected Sarsa [2].

Related work



- Following work of double Q learning: (**Core idea: Two estimators, Asymmetric updating**)



Related work: Double DQN_[2]



- Extend from tabular to large scale:
 - The idea behind the Double Q-learning algorithm, can be generalized to work with **large-scale function approximation**.
 - Evaluate the greedy policy according to the online network, and using the target network to estimate its value.
 - Shows better performance in “Game Playing”

Related work: Dueling Network_[3]



- Following work of double Q learning:
 - Two separate estimators one for the state value function and one for the state-dependent action advantage function.
 - The two streams are **sharing a common convolutional feature learning module.**

Simulation Results

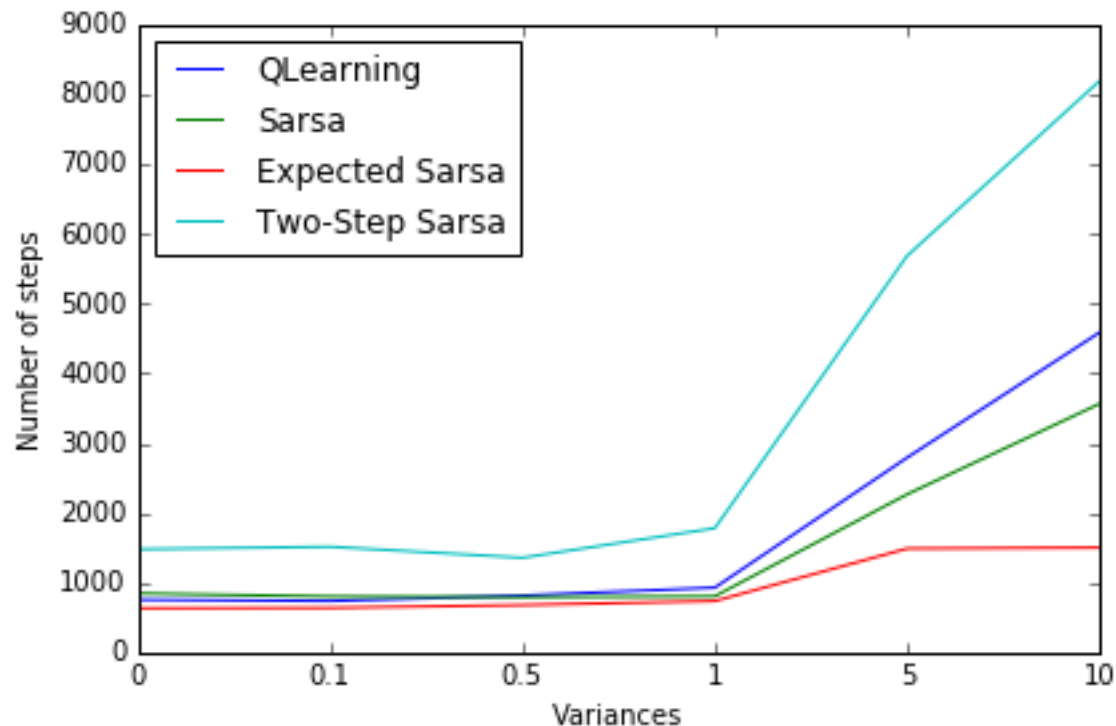


- I use the implementation of Weiwei Zhang's double q leaning, q learning, Sarsa as baselines. Use the same settings of simulation on CliffWalking.
- Provide implementations for: Double Sarsa, Expected Sarsa, Double Expected Sarsa, Two Step Sarsa.

Simulation Results



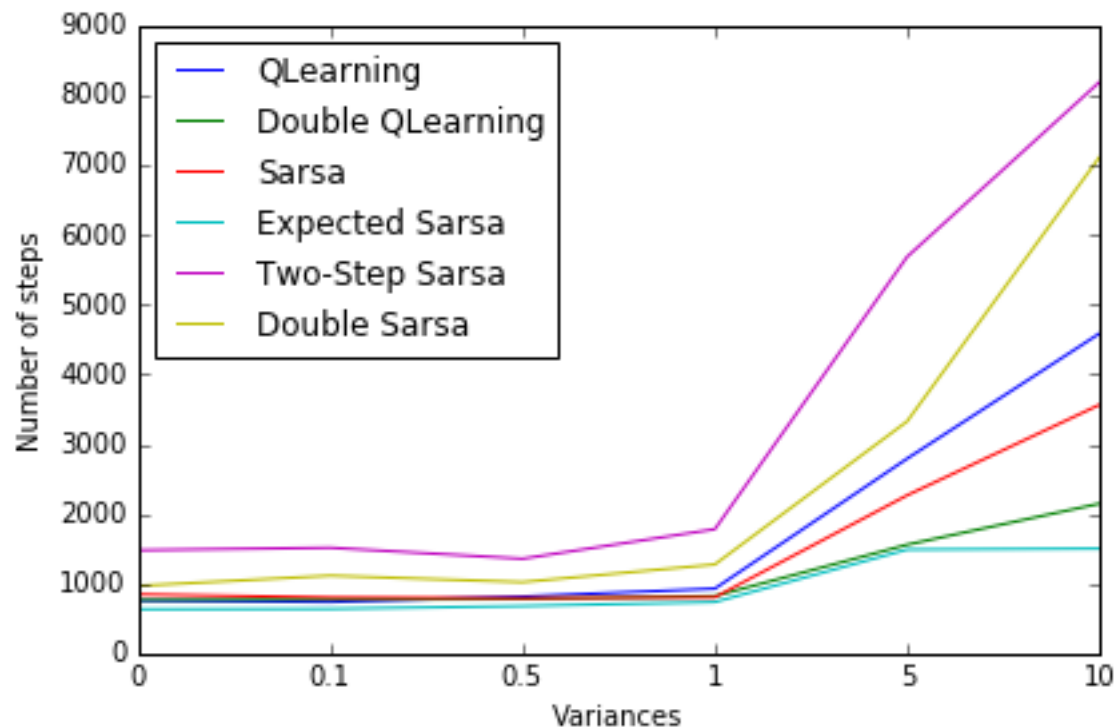
■ Comparison Q, Sarsa, Expected Sarsa, and Two-step Sarsa



Simulation Results



■ Comparison for all the algorithms



Reference



- [1] Hasselt H V. Double Q-learning[C], Advances in Neural Information Processing Systems. 2010: 2613-2621.
- [2] Ganger M, Duryea E, Hu W. Double Sarsa and Double Expected Sarsa with Shallow and Deep Learning[J]. Journal of Data Analysis and Information Processing, 2016, 4(04): 159.
- [3] Van Hasselt H, Guez A, Silver D. Deep Reinforcement Learning with Double Q-Learning[C], AAAI. 2016: 2094-2100.
- [4] Wang Z, Schaul T, Hessel M, et al. Dueling network architectures for deep reinforcement learning[J]. arXiv preprint arXiv:1511.06581, 2015.