Control With Gradient TD Methods + The Nonlinear Case COMP 767

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Overview

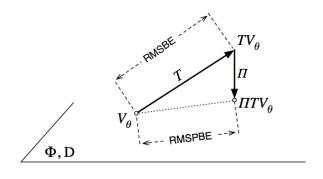
Gradient TD

Control With Gradient Methods

This slide is just to add slides.

The part we've covered:

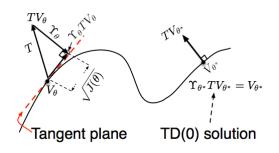
▶ This Picture:



$$MSPBE = ||(\Pi_{\theta} TV_{\theta} - V_{\theta})||_{D}^{2}$$
$$-1/2\nabla MSPBE = -\mathbb{E}[\delta \phi] - \gamma \mathbb{E}[\phi' \phi^{\top}]w$$
$$w = \mathbb{E}[\phi \phi^{\top}]^{-1} \mathbb{E}[\delta \phi]$$

The part we haven't:

This Picture:



MSPBE now projects onto the tangent space of the nonlinear function which we assume to be smooth enough to be locally linear.

$$egin{aligned} extit{MSPBE} &= ||\Pi_{ heta}(extit{T}V_{ heta} - V_{ heta})||_D^2 \ -1/2
abla extit{MSPBE} &= -\mathbb{E}[\delta\phi] - \gamma \mathbb{E}[\phi'\phi^{ op}]w + extit{h}(heta,w) \ w &= \mathbb{E}[\phi\phi^{ op}]^{-1}\mathbb{E}[\delta\phi] \end{aligned}$$

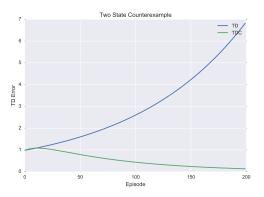
The part we haven't:

Update rules are much the same but now there are second order terms.

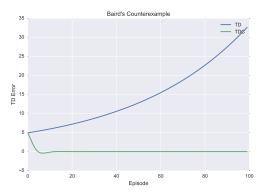
$$\theta_{k+1} = \Gamma \left[\theta_k + \alpha_k \{ \delta_k \phi_k - \gamma \phi_k' (\phi_k^\top w_k) - h_k \} \right]$$
$$h_k = \delta_k - (\phi_k^\top w_k) \delta^2 V_{\theta}(s_k) w_k$$

- note that now $\phi_k = \nabla V_{\theta}(s_k)$
- ▶ Also, Lee and Anderson, 2014 do this + control with small neural nets

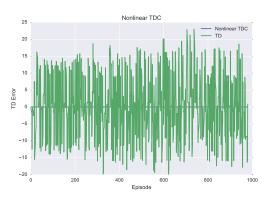
Quick Results



Quick Results

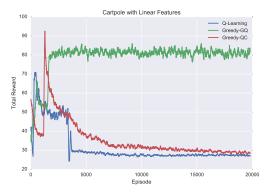


Quick Results



Simply Plug TDC or GTD2 into SARSA or Q-learning!

This is in the original feature space!



Simply Plug TDC or GTD2 into SARSA or Q-learning!

This is in the original feature space!

