Josef Fruehwald Laurel MacKenzie

University of Pennsylvania

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#### Outline

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#### The Statistics

Flat Models Hierarchical Models Markov Chain Monte Carlo

#### Case Studies

TD Retention **Auxiliary Contraction** 

#### Conclusions

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### Introduction

# Statistics and Sociolinguists

Introduction

- It has been recently argued that hierarchical statistical models are statistically appropriate for sociolinguistic data (Gorman, 2009; Johnson, 2009).
- Hierarchical models are also conceptually appropriate, since they model variation in the way sociolinguists view the world.

### Sociolinguistics in Statistics

Different variables exhibit different rates of "community cohesion" in ways which are potentially interesting.

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### Flat Models

# Historically...

- In the past, all models were "flat," pooling all speakers' data together.
- This was largely due to mathematical and computational limitations.

# Community Grammar

- Perhaps this is a feature, not a bug, as the object of sociolinguistic inquiry is larger than one speaker.
- But the statistics "see" the community grammar more like the Borg Collective.

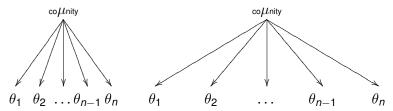
# Now...

 More work is emphasizing the statistical appropriateness of hierarchical models for sociolinguistic data.

### Community Grammar

 Hierarchical models also "see" variation as sociolinguists do: individuals coordinating themselves around a communal norm. (Labov, 2010)

- $\mu$  = Communal norm for some variable.
- $\theta_i$  = An individual speaker's rate for some variable.

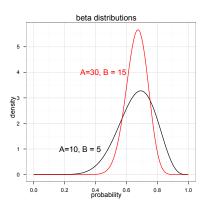


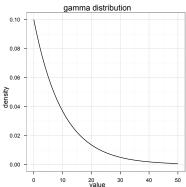
•  $\kappa$  will describe the degree of  $\kappa$ ohesion around the co $\mu$ nal norm, with higher  $\kappa$  values indicating greater cohesion.

#### A mathematical definition

- μ ∼ beta(A, B)
- $\theta_i \sim \text{beta}(\kappa \times \mu, \kappa \times (1 \mu))$
- {A, B,  $\kappa$ } ~ gamma(1,  $\frac{1}{10}$ )
- A beta distribution describes probabilities over probabilities.
  - A>B, skewed towards 1
  - A<B, skewed towards 0</li>
  - As A+B increases, so does the peakedness of the distribution.
- This gamma distribution is skewed towards small numbers, and is the common sort of distribution used to describe parameters like A, B and  $\kappa$ .







#### Markov Chain Monte Carlo Estimation

MCMC is a form of simulation which iteratively updates model parameters based on:

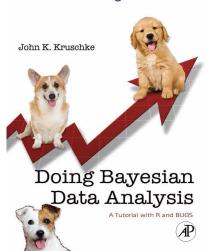
- The value this parameter had in the last iteration of the simulation.
- The likelihood of some value given the data, and the other parameter values.
- Some prior expectations about likely values for this parameter.

# Flexibility

It allows you to define models which do not submit to a regression formulation.

Markov Chain Monte Carlo Estimation

# **Further Reading**



# Implementation

- JAGS (just another Gibbs sampler).
- rjags package in R.

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#### All of our models will involve:

- One or more μ,
- speaker level  $\theta$  based on  $\mu$ ,
- a community cohesion coefficient  $\kappa$  for each  $\mu$ ,
- the inclusion of additional predictors relevant to the variable at hand.

# Regular Past vs. Semiweak

- Regular past > Semiweak (Labov et al., 1968)
  - packed > kept
- Guy (1991): Difference is caused by one process with probability p applying once to regular past, and twice to semiweak.
- Bermúdez-Otero (2010), Fruehwald (2011): There are two independent processes. Process one applies to both regular and semiweak, process two applies only to semiweak

# TD Retention Data

- Data is drawn from the Buckeye Corpus (Pitt et al., 2005).
  - 38 speakers from in or around Columbus, OH.
- 1,677 tokens of regular past.
- 329 tokens of semiweak past.

# TD Retention Model

#### **Parameters**

- One community-level  $\mu$  for each process:  $\mu_{one}$  and  $\mu_{two}$
- One cohesion coefficient related to each  $\mu$ :  $\kappa_{one}$  and  $\kappa_{two}$
- Two individual level parameters per speaker:  $\theta_{one}$  and  $\theta_{two}$

# Regression

- For each speaker, probability of retention =  $\hat{\theta}$ .
  - $\hat{\theta} = \theta_{one}$  for past tense.
  - $\hat{\theta} = \theta_{one} \times \theta_{two}$  for semiweak.
- $\hat{\theta}$  is scaled by additive logistic effects associated with preceding and following segments.

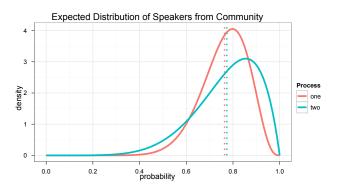
#### Results

	Process One	Process Two
$\mu$	0.76	0.77
A + B	22.08	20.89
$\kappa$	17.56	8.74

Preceding Segment	Effect
/r/	1.38
/1/	0.39
fricative	0.11
stop	-0.18
sibilant	-0.65
nasal	-1.06

Following Segment	Effect
vowel	1.19
pause	1.02
/ <b>y</b> /	0.27
/n/	-0.43
stop	-0.49
/l/	-0.53
sibilant	-0.82

#### Results



- regular past = process one
- semiweak = process one × process two



Conclusion

 Based on the different patterns in the speech community, it appears that there are two different processes involved in TD Retention.

# **Auxiliary Contraction**

• e.g. He <u>has</u>  $\sim$  he<u>'s</u> arrived

$$\left\{\begin{array}{c} \mathsf{NP} \\ \mathsf{pronoun} \end{array}\right\} \left\{\begin{array}{c} \mathit{had} \\ \mathit{has} \\ \mathit{have} \end{array}\right\}$$

- Is contraction...
  - ...a single, pan-auxiliary process?
  - ... multiple independent auxiliary-specific processes?

# **Auxiliary Contraction**

#### What underlies the surface alternation?

 Variable adjunction of an auxiliary to the element that precedes it (Kaisse 1983)

$$X^Aux \rightsquigarrow [[X]Aux]$$

 Each auxiliary has a full and a short allomorph; short form conditioned when adjunction has occurred

```
full /hæd/ /hæz/ /hæv/
short /d/ /z/ /v/
```

e.g. 3.sg.fem
$$^T_{[past]} \rightsquigarrow [[3.sg.fem]T_{[past]}] \rightarrow [[id]$$
  
3.sg.fem $^T_{[past]} \rightsquigarrow 3.sg.fem ^T_{[past]} \rightarrow [[i hæd]]$ 

# **Auxiliary Contraction** Data

- Data drawn from the Philadelphia Neighborhood Corpus (Labov & Rosenfelder 2011)
- 39 speakers from Philadelphia.

had	has	have
105	147	263

# Auxiliary Contraction Model

#### **Parameters**

- One  $\mu$  for each auxiliary ( $\mu_{had}$ ,  $\mu_{has}$ ,  $\mu_{have}$ )
- One κ for all three auxiliaries ( $\kappa_{same}$ )

- One  $\kappa$  for each auxiliary  $(\kappa_{diff})$
- A parameter which selects a  $\kappa_{diff}$  or  $\kappa_{same}$  preference
- For each speaker,  $\theta_{had}$ ,  $\theta_{has}$ ,  $\theta_{have}$

# Regression

- Additive logit effects for pronoun vs NP subjects (MacKenzie 2010)
- If the subject is an NP, slope for how many words in the NP (MacKenzie 2011) 4 D > 4 A > 4 B > 4 B >

# **Auxiliary Contraction**

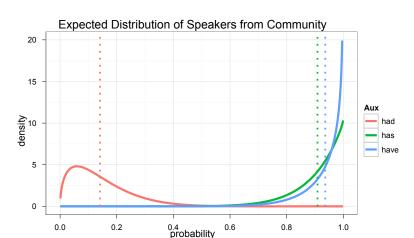
#### Results

	had	has	have
$\mu$	0.14	0.91	0.94
A + B	19.82	20.72	19.44
$\kappa_{ extit{diff}}$	10.89	8.48	11.61
$\kappa_{\it same}$		10.78	

 $\kappa_{same}$  preference = 0.53 (> .5 favors)

Effect
-1.29
-2.59

# Auxiliary Contraction Results



# Auxiliary Contraction Conclusion

 The similar patterns for each auxiliary in the speech community support the proposal that a single process underlies contraction of all auxiliaries.

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# Conclusions Case Studies

#### **TD** Retention

Based on the different patterns in the speech community, it appears that there are two, different processes involved in TD Retention.

#### **Auxiliary Contraction**

The different patterns in the speech community support the proposal that a single process underlies contraction of all auxiliaries.

# Conclusions Statistics

#### Hierarchical Models

- Hierarchical models are conceptually appropriate for sociolinguistic data.
- Hierarchical models can give us parameters that other models can't — namely, degree of community cohesion which can provide support for linguistic reasoning.

#### **MCMC**

 Markov Chain Monte Carlo methods allow us to fit and compare interesting models which cannot be fit as ordinary regression.

**Modeling Change** 

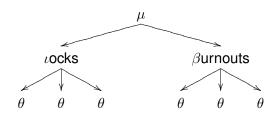
# **Changing Communal Norms**

•  $\mu \sim \text{time}$ 

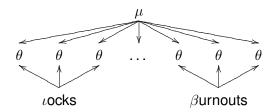
# **Changing Cohesion**

•  $\kappa \sim \text{time}$ 

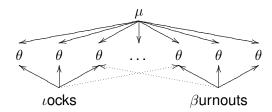
**Modeling Social Factors** 



Modeling Social Factors



Modeling Social Factors



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